

# Homework 6 of Introduction to Analysis(II)

AM15 黃琦翔 111652028

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1. Let  $\phi(x) = \arctan(x)$ , then  $\phi \circ f(x) = \phi(f(x))$  is bdd by  $(-\frac{\pi}{2}, \frac{\pi}{2})$ . Then, by Tietze's Extension Theorem, there exists  $g \in C(\mathbb{R}^n, \mathbb{R})$  s.t.  $g(x) = \phi(f(x))$  for all  $x \in D$  and  $\sup |g(x)| = \sup |\phi(f(x))| \leq \frac{\pi}{2}$ .

Thus, there exists  $h(x) = \tan(g(x))$  in  $C(\mathbb{R}^n, \mathbb{R})$  and  $h(x) = f(x)$  for all  $x \in D$  by  $\phi(x)$  is invertible.

- 2.