

Homework 5 of Introduction to Analysis(II)

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1. (a) If $x \in A$, $d(x, A) = \|x - x\| = 0$ and $d(x, B) = k > 0$, $\phi(x) = \frac{0}{0+k} = 0$. If $x \in B$, $d(x, A) = l > 0$ and $d(x, B) = 0$, $\phi(x) = \frac{l}{l+0} = 1$. If $x \notin A \wedge x \notin B$, $d(x, A) = l$ and $d(x, B) = k$, $\phi(x) = \frac{l}{l+k} < 1$ and is positive. Thus, $0 \leq \phi(x) \leq 1$ for all $x \in \mathbb{R}^n$.

(b)