

Topics for Test 1, ISyE 6644 Online Masters in Analytics, Summer 2018

1. I've tried my best to make this list as complete as possible, but I may have missed a topic or two. That being said, you are responsible for everything that we did in class or homework.
2. As Georgia Tech students, you are expected to formulate problems and solution strategies which are more than mere rote regurgitation of material you learned in class. Thus, you shouldn't be surprised if some questions cover natural extensions of material from class.
3. I will supply all necessary tables, but you can feel free to use your own. You may need the standard normal tables, and there is a small, nonzero chance that you'll need t or χ^2 tables.

OK, so off we go! Here's the list of all of the stuff we've done so far...

1. Intro Material

- a. Definition of simulation
- b. Advantages and disadvantages of simulation
- c. History of simulation
- d. Typical questions and applications

2. Calculus, Probability, and Statistics Review

- a. **Calculus** ←- I will *not* ask any test questions on the Calculus material (which was optional material for the course)
 - i. Basic definitions
 - ii. Derivatives
 - iii. Solving for zeros
 - iv. Integration
 - v. Numerical integration
- b. **Probability Preliminaries**
 - i. Conditional probability
 - ii. Independent events
 - iii. Definition of random variable
 - iv. Discrete RV's and probability mass function
 - v. Continuous RV's and probability density function
 - vi. Cumulative distribution function
- c. **Simulating RV's (first pass)**
 - i. Discrete uniform distribution
 - ii. General discrete distribution
 - iii. Inverse Transform Theorem for continuous RV's

- iv. Exponential (and other) continuous distributions via IVT.
 - v. Generating $U(0,1)$'s via desert island algorithm, including walk-through of pseudo-code.
- d. Expected Values
 - i. Definition
 - ii. Discrete and continuous examples of expected value
 - iii. Law of the Unconscious Statistician
 - iv. Moments, central moments, variance, standard deviation
 - v. Discrete and continuous examples of LOTUS
 - vi. Moment generating function
 - vii. Examples and properties of mgf's
- e. Functions of a RV
 - i. Discrete examples
 - ii. Continuous examples
 - iii. IVT methods (again) with examples
 - iv. Relationship with LOTUS
- f. Jointly distributed RV's
 - i. Definition of joint cdf
 - ii. Marginal cdf's
 - iii. Joint and marginal pmf's
 - iv. Joint and marginal pdf's
 - v. Examples for discrete and continuous cases
 - vi. Independent RV's
 - vii. Conditional pmf's and pdf's
 - viii. Conditional expectation \leftarrow no test questions on this (optional) material!
 - ix. Double expectation $E(E(Y|X)) = EY$, including examples \leftarrow no test questions on this (optional) material!
- g. Covariance and correlation
 - i. Definitions
 - ii. Relationship between independence and correlation
 - iii. Examples
 - iv. Miscellaneous properties (e.g., $\text{Var}(X+Y)$, bounds on correlation, etc.)
- h. Probability distributions
 - i. Discrete distributions
 - 1. Bernoulli
 - 2. Binomial
 - 3. Geometric
 - 4. Poisson (including discussion on Poisson processes)
 - ii. Continuous distributions
 - 1. Uniform
 - 2. Exponential (including memoryless property)

- 3. Erlang, Gamma distributions
- 4. Triangular
- 5. Normal (including Standard Normal)
- 6. Other sampling distributions (including chi-square, t, F, and various relationships with each other)
- i. Limit theorems
 - i. Linear combinations of independent normal (including distribution of sample mean)
 - ii. Convergence in distribution
 - iii. Law of Large Numbers
 - iv. Central Limit Theorem for independent and identically distributed data.
 - v. Examples
- j. Statistics Tidbits
 - i. Properties of sample mean and sample variance
 - ii. Confidence intervals for the mean and variance

3. Hand Simulations

- a. Monte Carlo integration
- b. Determining π via simulation (dart tossing on a circle and sphere)
- c. Single-server queue (including FIFO and LIFO service disciplines)
- d. (s,S) inventory system
- e. Simulating RV's (repeats some material from the Prob/Stats review)
- f. Spreadsheet simulation (e.g., stock portfolio in Excel)

4. General Simulation Principles

- a. Steps in a simulation study
- b. List of various simulation definitions (e.g., event, system state, simulation clock, etc.)
- c. Event-Scheduling vs. Process Interaction modeling approaches
- d. How are events processed?
- e. Future events list + extended example

5. Baby Arena Stuff

You'll only be responsible for the first few lessons, since you may not have even started the first Arena HW yet! In fact, the purpose of including any of this on the list is just my way of making you look at a little of the Arena material.

- a. Layout of Arena screen (panels, modules, etc.)
- b. Basic Process modules (CREATE, PROCESS, DISPOSE, DECIDE, ASSIGN, etc.)
- c. SEIZE-DELAY-RELEASE inside of the PROCESS module.
- d. Really simple examples, e.g. (partial list),

- i. Single-server queue
- ii. Parallel servers
- iii. Easy DECIDE module manipulations (by chance, and by condition)