



◇「콘텐츠산업 진흥법 시행령」제33조에 의한 표시
 1) 제작연월일 : 2019-03-15
 2) 제작자 : 교육지대(주)
 3) 이 콘텐츠는 「콘텐츠산업 진흥법」에 따라 최초 제작일부터 5년간 보호됩니다.

◇「콘텐츠산업 진흥법」외에도「저작권법」에 의하여 보호되는 콘텐츠의 경우, 그 콘텐츠의 전부 또는 일부를 무단으로 복제하거나 전송하는 것은 콘텐츠산업 진흥법 외에도 저작권법에 의한 법적 책임을 질 수 있습니다.

01 구간에 따라 다르게 정의된 정적분의 계산

함수 $f(x) = \begin{cases} g(x) & (x \leq c) \\ h(x) & (x > c) \end{cases}$ 가 닫힌구간 $[a, b]$ 에서

연속이고 $a < c < b$ 일 때,

$$\int_a^b f(x)dx = \int_a^c g(x)dx + \int_c^b h(x)dx$$

■ 다음 정적분의 값을 구하여라.

1. $f(x) = \begin{cases} x^2 - 1 & (x \leq 1) \\ x - 1 & (x > 1) \end{cases}$ 일 때, $\int_0^2 f(x)dx$

2. $f(x) = \begin{cases} -x^2 + 1 & (x \leq 1) \\ x - 1 & (x > 1) \end{cases}$ 일 때, $\int_0^2 f(x)dx$

3. $f(x) = \begin{cases} x^2 & (x \leq 0) \\ 2x & (x > 0) \end{cases}$ 일 때, $\int_{-1}^1 f(x)dx$

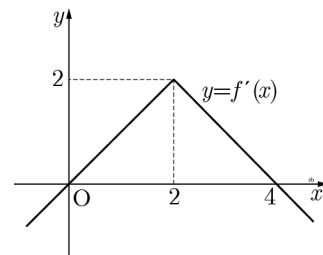
4. $f(x) = \begin{cases} x^2 & (x \leq 1) \\ 2 - x & (x > 1) \end{cases}$ 일 때, $\int_{-2}^2 f(x)dx$

5. $f(x) = \begin{cases} 2 & (x \leq 0) \\ -3x + 2 & (x > 0) \end{cases}$ 일 때, $\int_{-1}^1 xf(x)dx$

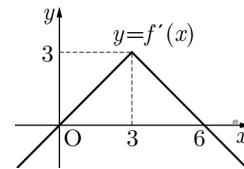
6. $f(x) = \begin{cases} x & (x < 1) \\ -x + 2 & (x \geq 1) \end{cases}$ 일 때, $\int_1^3 xf(x-1)dx$

■ 다음 정적분의 값을 구하여라.

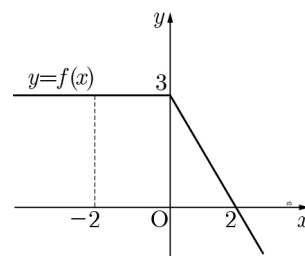
7. 연속함수 $f(x)$ 의 도함수 $y = f'(x)$ 의 그래프가 다음 그림과 같을 때, $f(4) - f(0)$ 의 값을 구하여라.



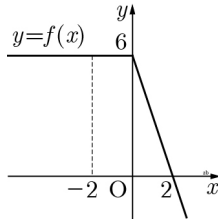
8. 연속함수 $f(x)$ 의 도함수 $y = f'(x)$ 의 그래프가 다음 그림과 같을 때, $f(6) - f(0)$ 의 값을 구하여라.



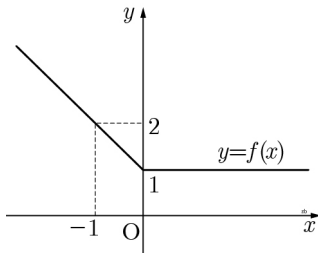
9. 함수 $y = f(x)$ 의 그래프가 다음 그림과 같을 때, 정적분 $\int_{-1}^1 xf(x)dx$ 의 값을 구하여라.



10. 함수 $y=f(x)$ 의 그래프가 다음 그림과 같을 때,
정적분 $\int_{-2}^2 xf(x)dx$ 의 값을 구하여라.



11. 함수 $y=f(x)$ 의 그래프가 다음 그림과 같을 때,
정적분 $\int_{-1}^1 xf(x)dx$ 의 값을 구하여라.



02 절댓값 기호를 포함한 함수의 정적분의 계산

절댓값 기호를 포함한 함수 $y=|f(x)|$ 의 정적분은 절댓값 기호 안의 식의 값이 0이 되는 x 의 값을 경계로 적분 구간을 나눈다.

■ 다음 정적분의 값을 구하여라.

12. $\int_{-2}^1 |x+1| dx$

13. $\int_0^2 |x-1| dx$

14. $\int_{-1}^2 |x-1| dx$

15. $\int_0^3 |x-1| dx$

16. $\int_0^4 |x-1| dx$

17. $\int_0^3 |x-2| dx$

18. $\int_0^6 |x-4| dx$

19. $\int_0^2 |x^2-1| dx$

20. $\int_{-2}^2 |x^2-1| dx$

21. $\int_0^3 |x(x-2)| dx$

22. $\int_0^4 |x^2 - 2x| dx$

23. $\int_1^3 |x(x-2)| dx$

24. $\int_1^3 |3x^2 - 6x| dx$

25. $\int_0^2 |x^2 + x - 2| dx$

26. $\int_0^2 |x^2 - 4x + 3| dx$

27. $\int_{-1}^2 x|x-1| dx$

28. $\int_0^3 6x|x-1| dx$

03 / 우함수와 기함수의 정적분

함수 $f(x)$ 가 닫힌구간 $[a, b]$ 에서 연속일 때,

(1) $f(-x) = f(x)$ 이면, 즉 $f(x)$ 가 **우함수**이면

$$\int_{-a}^a f(x) dx = 2 \int_0^a f(x) dx$$

(2) $f(-x) = -f(x)$ 이면, 즉 $f(x)$ 가 **기함수**이면

$$\int_{-a}^a f(x) dx = 0$$

■ 다음 함수 중 $\int_a^b f(x) dx = \int_{-b}^{-a} f(x) dx$ 를 만족하는 것에는
'우', $\int_a^b f(x) dx = -\int_{-b}^{-a} f(x) dx$ 를 만족하는 것에는 '기'라고
괄호 안에 써 넣어라.

29. $f(x) = -x^3 - 2x$ ()

30. $f(x) = x^4 + x^2$ ()

31. $f(x) = x^5 + x$ ()

32. $f(x) = x^8 + 1$ ()

■ 다음 정적분의 값을 구하여라.

33. $\int_{-1}^1 (3x^2 + 4) dx$

34. $\int_{-1}^1 (x+1)(3x+2) dx$

$$35. \int_0^2 (2x^2 + 2x) dx - 2 \int_0^{-2} (x + x^2) dx$$

$$36. \int_{-1}^1 (x^2 + x + 1) dx - \int_{-1}^1 (x^2 - x + 1) dx$$

$$37. \int_{-2}^1 (6x^2 - 4x + 1) dx + \int_2^1 (-6x^2 + 4x - 1) dx$$

$$38. \int_{-1}^0 (3x^2 + 4x^3 + 5x^4) dx - \int_1^0 (3x^2 + 4x^3 + 5x^4) dx$$

$$39. \int_{-2}^2 (3x^2 + |x|) dx$$

$$40. \int_{-1}^1 (x^3 + 3x) dx$$

$$41. \int_{-1}^1 (x+1)(x^2 - x + 1) dx$$

$$42. \int_{-2}^2 (x^3 - 3x^2 - 2x + 4) dx$$

$$43. \int_{-1}^1 (5x^3 - 6x^2 - 7x + 8) dx$$

$$44. \int_{-2}^2 (100x^3 + 3x^2 - 90x + 1) dx$$

$$45. \int_{-3}^3 (-x^3 + 3x^2 + 4x - 2) dx$$

$$46. \int_{-1}^0 (x^3 - 3x^2 + 2) dx + \int_0^1 (x^3 - 3x^2 + 2) dx$$

$$47. \int_{-1}^0 (4x^3 - 2x + 1) dx + \int_0^1 (4x^3 - 2x + 1) dx$$

$$48. \int_{-2}^1 (x^3 + 6x^2 + 2x - 1) dx \\ + \int_1^2 (x^3 + 6x^2 + 2x - 1) dx$$

$$49. \int_{-1}^0 (1 + 2x + 3x^2 + 4x^3) dx \\ + \int_0^1 (1 + 2x + 3x^2 + 4x^3) dx$$

$$50. \int_{-1}^1 x(1-x)^2 dx$$

$$51. \int_{-2}^2 (5x^4 + 3x^3 - 7x - 1) dx$$

$$52. \int_{-1}^1 (5x^4 - 6x^3 + 3x^2 - 7x + 3) dx$$

$$53. \int_{-1}^1 (5x^4 + 4x^3 + 3x^2 + 2x + 1) dx$$

$$54. \int_{-1}^4 (5x^4 + 4x^3 + 3x^2) dx - \int_1^4 (5x^4 + 4x^3 + 3x^2) dx$$

$$55. \int_{-1}^1 (x^5 + 2x) dx$$

$$56. \int_{-2}^2 (x^5 - 2x^3 + 3x^2 - 1) dx$$

$$57. \int_{-5}^5 (6x^5 - 8x^3 + 3x^2 - 2) dx$$

$$58. \int_{-2}^2 (6x^5 - 4x^3 + 3x^2 + 2x + 1) dx$$

$$59. \int_{-2}^1 (x^5 + 3x^2 - 2x) dx - \int_2^1 (x^5 + 3x^2 - 2x) dx$$

$$60. \int_{-1}^1 x^3(1+x)^2 dx$$

$$61. \int_{-1}^1 (8x^9 - x^5 + 10x^4 - 3x^2 + 4) dx$$

$$62. \int_{-1}^1 (11x^{10} + 12x^{11} + 13x^{12} + 14x^{13}) dx$$

$$63. \int_{-1}^1 (x^{11} + 10x^9 - 25x^7 + 3x^2 - 9x + 2) dx$$



정답 및 해설

1) $-\frac{1}{6}$

$$\begin{aligned}
 \Rightarrow \int_0^2 f(x) dx &= \int_0^1 f(x) dx + \int_1^2 f(x) dx \\
 &= \int_0^1 (x^2 - 1) dx + \int_1^2 (x - 1) dx \\
 &= \left[\frac{1}{3}x^3 - x \right]_0^1 + \left[\frac{1}{2}x^2 - x \right]_1^2 \\
 &= -\frac{2}{3} + \frac{1}{2} = -\frac{1}{6}
 \end{aligned}$$

2) $\frac{7}{6}$

$$\begin{aligned}
 \Rightarrow \int_0^2 f(x) dx &= \int_0^1 f(x) dx + \int_1^2 f(x) dx \\
 &= \int_0^1 (-x^2 + 1) dx + \int_1^2 (x - 1) dx \\
 &= \left[-\frac{1}{3}x^3 + x \right]_0^1 + \left[\frac{1}{2}x^2 - x \right]_1^2 \\
 &= \frac{2}{3} + \frac{1}{2} = \frac{7}{6}
 \end{aligned}$$

3) $\frac{4}{3}$

$$\begin{aligned}
 \Rightarrow \int_{-1}^1 f(x) dx &= \int_{-1}^0 f(x) dx + \int_0^1 f(x) dx \\
 &= \int_{-1}^0 x^2 dx + \int_0^1 2x dx \\
 &= \left[\frac{1}{3}x^3 \right]_{-1}^0 + [x^2]_0^1 = \frac{1}{3} + 1 = \frac{4}{3}
 \end{aligned}$$

4) $\frac{7}{2}$

$$\begin{aligned}
 \Rightarrow \int_{-2}^2 f(x) dx &= \int_{-2}^{-1} f(x) dx + \int_{-1}^2 f(x) dx \\
 &= \int_{-2}^{-1} x^2 dx + \int_{-1}^2 (2 - x) dx \\
 &= \left[\frac{1}{3}x^3 \right]_{-2}^{-1} + \left[2x - \frac{1}{2}x^2 \right]_{-1}^2 = 3 + \frac{1}{2} = \frac{7}{2}
 \end{aligned}$$

5) -1

$$\begin{aligned}
 \Rightarrow f(x) &= \begin{cases} 2 & (x \leq 0) \\ -3x + 2 & (x > 0) \end{cases} \text{이므로} \\
 xf(x) &= \begin{cases} 2x & (x \leq 0) \\ -3x^2 + 2x & (x > 0) \end{cases} \\
 \int_{-1}^1 xf(x) dx &= \int_{-1}^0 2x dx + \int_0^1 (-3x^2 + 2x) dx \\
 &= [x^2]_{-1}^0 + [-x^3 + x^2]_0^1 = -1 + 0 = -1
 \end{aligned}$$

6) 2

$$\begin{aligned}
 \Rightarrow f(x-1) &= \begin{cases} x-1 & (x < 2) \\ -x+3 & (x \geq 2) \end{cases} \text{이므로} \\
 xf(x-1) &= \begin{cases} x^2-x & (x < 2) \\ -x^2+3x & (x \geq 2) \end{cases} \\
 \int_1^3 xf(x-1) dx &= \int_1^2 (x^2-x) dx + \int_2^3 (-x^2+3x) dx \\
 &= \left[\frac{1}{3}x^3 - \frac{1}{2}x^2 \right]_1^2 + \left[-\frac{1}{3}x^3 + \frac{3}{2}x^2 \right]_2^3 \\
 &= \frac{5}{6} + \frac{7}{6} = 2
 \end{aligned}$$

7) 4

$$\begin{aligned}
 \Rightarrow f'(x) &= \begin{cases} x & (x \leq 2) \\ 4-x & (x > 2) \end{cases} \text{이므로} \\
 \int_0^4 f'(x) dx &= \int_0^2 x dx + \int_2^4 (4-x) dx \\
 &= \left[\frac{x^2}{2} \right]_0^2 + \left[4x - \frac{x^2}{2} \right]_2^4 = 2 + 2 = 4 \\
 \int_0^4 f'(x) dx &= [f(x)]_0^4 = f(4) - f(0) \text{이므로} \\
 f(4) - f(0) &= 4
 \end{aligned}$$

8) 9

$$\begin{aligned}
 \Rightarrow \int_0^6 f'(x) dx &= [f(x)]_0^6 = f(6) - f(0) \text{이고} \\
 f'(x) &= \begin{cases} x & (x \leq 3) \\ 6-x & (x > 3) \end{cases} \text{이므로} \\
 \int_0^6 f'(x) dx &= \int_0^3 x dx + \int_3^6 (6-x) dx \\
 &= \left[\frac{1}{2}x^2 \right]_0^3 + \left[6x - \frac{1}{2}x^2 \right]_3^6 \\
 &= \frac{9}{2} + \frac{9}{2} = 9 \\
 \therefore f(6) - f(0) &= 9
 \end{aligned}$$

9) $-\frac{1}{2}$

$$\begin{aligned}
 \Rightarrow f(x) &= \begin{cases} 3 & (x \leq 0) \\ -\frac{3}{2}x + 3 & (x > 0) \end{cases} \text{이므로} \\
 \int_{-1}^1 xf(x) dx &= \int_{-1}^0 3x dx + \int_0^1 \left(-\frac{3}{2}x^2 + 3x \right) dx \\
 &= \left[\frac{3}{2}x^2 \right]_{-1}^0 + \left[-\frac{1}{2}x^3 + \frac{3}{2}x^2 \right]_0^1 \\
 &= -\frac{3}{2} + 1 = -\frac{1}{2}
 \end{aligned}$$

10) -8

$$\Rightarrow f(x) = \begin{cases} 6 & (x \leq 0) \\ -3x + 6 & (x > 0) \end{cases} \text{이므로}$$

$$\begin{aligned}\int_{-2}^2 xf(x)dx &= \int_{-2}^0 6xdx + \int_0^2 (-3x^2 + 6x)dx \\ &= [3x^2]_{-2}^0 + [-x^3 + 3x^2]_0^2 \\ &= -12 + 4 = -8\end{aligned}$$

11) $-\frac{1}{3}$

$$\Rightarrow f(x) = \begin{cases} -x+1 & (x \leq 0) \\ 1 & (x > 0) \end{cases} \text{이므로}$$

$$\begin{aligned}\int_{-1}^1 xf(x)dx &= \int_{-1}^0 (-x^2 + x)dx + \int_0^1 xdx \\ &= \left[-\frac{1}{3}x^3 + \frac{1}{2}x^2\right]_{-1}^0 + \left[\frac{1}{2}x^2\right]_0^1 = -\frac{5}{6} + \frac{1}{2} = -\frac{1}{3}\end{aligned}$$

12) $\frac{5}{2}$

$$\Rightarrow |x+1| = \begin{cases} -x-1 & (x \leq -1) \\ x+1 & (x > -1) \end{cases} \text{이므로}$$

$$\begin{aligned}\int_{-2}^1 |x+1|dx &= \int_{-2}^{-1} (-x-1)dx + \int_{-1}^1 (x+1)dx \\ &= \left[-\frac{1}{2}x^2 - x\right]_{-2}^{-1} + \left[\frac{1}{2}x^2 + x\right]_{-1}^1 \\ &= \frac{1}{2} + 2 = \frac{5}{2}\end{aligned}$$

13) 1

$$\Rightarrow |x-1| = \begin{cases} x-1 & (x \geq 1) \\ -x+1 & (x \leq 1) \end{cases} \text{이므로}$$

$$\begin{aligned}\int_0^2 |x-1|dx &= \int_0^1 (-x+1)dx + \int_1^2 (x-1)dx \\ &= \left[-\frac{1}{2}x^2 + x\right]_0^1 + \left[\frac{1}{2}x^2 - x\right]_1^2 \\ &= \frac{1}{2} + \frac{1}{2} = 1\end{aligned}$$

14) $\frac{5}{2}$

$$\Rightarrow |x-1| = \begin{cases} x-1 & (x \geq 1) \\ -x+1 & (x \leq 1) \end{cases} \text{이므로}$$

$$\begin{aligned}\int_{-1}^2 |x-1|dx &= \int_{-1}^1 (-x+1)dx + \int_1^2 (x-1)dx \\ &= \left[-\frac{1}{2}x^2 + x\right]_{-1}^1 + \left[\frac{1}{2}x^2 - x\right]_1^2 \\ &= 2 + \frac{1}{2} = \frac{5}{2}\end{aligned}$$

15) $\frac{5}{2}$

$$\Rightarrow |x-1| = \begin{cases} 1-x & (x \leq 1) \\ x-1 & (x > 1) \end{cases} \text{이므로}$$

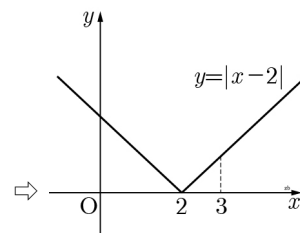
$$\int_0^3 |x-1|dx = \int_0^1 (1-x)dx + \int_1^3 (x-1)dx$$

$$\begin{aligned}&= \left[x - \frac{1}{2}x^2\right]_0^1 + \left[\frac{1}{2}x^2 - x\right]_1^3 \\ &= \frac{1}{2} + 2 = \frac{5}{2}\end{aligned}$$

16) 5

$$\begin{aligned}\Rightarrow \int_0^4 |x-1|dx &= \int_0^1 (-x+1)dx + \int_1^4 (x-1)dx \\ &= \left[-\frac{1}{2}x^2 + x\right]_0^1 + \left[\frac{1}{2}x^2 - x\right]_1^4 = \frac{1}{2} + \frac{9}{2} = 5\end{aligned}$$

17) $\frac{5}{2}$



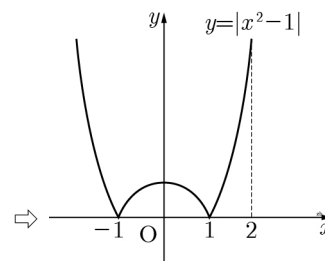
$$|x-2| = \begin{cases} -(x-2) & (0 \leq x \leq 2) \\ x-2 & (2 < x \leq 3) \end{cases} \text{이므로}$$

$$\begin{aligned}\int_0^3 |x-2|dx &= \int_0^2 (-x+2)dx + \int_2^3 (x-2)dx \\ &= \left[-\frac{1}{2}x^2 + 2x\right]_0^2 + \left[\frac{1}{2}x^2 - 2x\right]_2^3 = 2 + \frac{1}{2} = \frac{5}{2}\end{aligned}$$

18) 10

$$\begin{aligned}\Rightarrow \int_0^6 |x-4|dx &= \int_0^4 (-x+4)dx + \int_4^6 (x-4)dx \\ &= \left[-\frac{1}{2}x^2 + 4x\right]_0^4 + \left[\frac{1}{2}x^2 - 4x\right]_4^6 = 8 + 2 = 10\end{aligned}$$

19) 2



$$\begin{aligned}\int_0^2 |x^2-1|dx &= \int_0^1 (-x^2+1)dx + \int_1^2 (x^2-1)dx \\ &= \left[-\frac{x^3}{3} + x\right]_0^1 + \left[\frac{x^3}{3} - x\right]_1^2 = \frac{2}{3} + \frac{4}{3} = 2\end{aligned}$$

20) 4

$$\begin{aligned}
 &\Rightarrow \int_{-2}^2 |x^2 - 1| dx \\
 &= \int_{-2}^{-1} (x^2 - 1) dx + \int_{-1}^1 (-x^2 + 1) dx + \int_1^2 (x^2 - 1) dx \\
 &= \left[\frac{1}{3}x^3 - x \right]_{-2}^{-1} + \left[-\frac{1}{3}x^3 + x \right]_{-1}^1 + \left[\frac{1}{3}x^3 - x \right]_1^2 \\
 &= \frac{4}{3} + \frac{4}{3} + \frac{4}{3} = 4
 \end{aligned}$$

21) $\frac{8}{3}$

$$\begin{aligned}
 &\Rightarrow |x(x-2)| = \begin{cases} 2x-x^2 & (0 \leq x \leq 2) \\ x^2-2x & (x < 0 \text{ 또는 } x > 2) \end{cases} \text{이므로} \\
 &\int_0^3 |x(x-2)| dx \\
 &= \int_0^2 (2x-x^2) dx + \int_2^3 (x^2-2x) dx \\
 &= \left[x^2 - \frac{1}{3}x^3 \right]_0^2 + \left[\frac{1}{3}x^3 - x^2 \right]_2^3 \\
 &= \frac{4}{3} + \frac{4}{3} = \frac{8}{3}
 \end{aligned}$$

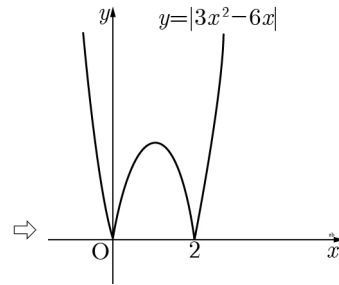
22) 8

$$\begin{aligned}
 &\Rightarrow |x(x-2)| = \begin{cases} x^2-2x & (x \leq 0 \text{ 또는 } x \geq 2) \\ -x^2+2x & (0 \leq x \leq 2) \end{cases} \text{이므로} \\
 &\int_0^4 |x^2-2x| dx \\
 &= \int_0^2 (-x^2+2x) dx + \int_2^4 (x^2-2x) dx \\
 &= \left[-\frac{1}{3}x^3 + x^2 \right]_0^2 + \left[\frac{1}{3}x^3 - x^2 \right]_2^4 \\
 &= \frac{4}{3} + \frac{20}{3} = 8
 \end{aligned}$$

23) 2

$$\begin{aligned}
 &\Rightarrow |x(x-2)| = \begin{cases} x^2-2x & (x \leq 0 \text{ 또는 } x \geq 2) \\ -x^2+2x & (0 \leq x \leq 2) \end{cases} \text{이므로} \\
 &\int_1^3 |x(x-2)| dx \\
 &= \int_1^2 (-x^2+2x) dx + \int_2^3 (x^2-2x) dx \\
 &= \left[-\frac{1}{3}x^3 + x^2 \right]_1^2 + \left[\frac{1}{3}x^3 - x^2 \right]_2^3 \\
 &= \frac{2}{3} + \frac{4}{3} = 2
 \end{aligned}$$

24) 6



$$\begin{aligned}
 &\Rightarrow \int_1^3 |3x^2 - 6x| dx \\
 &= \int_1^2 (-3x^2 + 6x) dx + \int_2^3 (3x^2 - 6x) dx \\
 &= \left[-x^3 + 3x^2 \right]_1^2 + \left[x^3 - 3x^2 \right]_2^3 \\
 &= 2 + 4 = 6
 \end{aligned}$$

25) 3

$$\begin{aligned}
 &\Rightarrow |x^2+x-2| = \begin{cases} -x^2-x+2 & (-2 \leq x \leq 1) \\ x^2+x-2 & (x < -2 \text{ 또는 } x > 1) \end{cases} \text{이므로} \\
 &\int_0^2 |x^2+x-2| dx \\
 &= \int_0^1 (-x^2-x+2) dx + \int_1^2 (x^2+x-2) dx \\
 &= \left[-\frac{1}{3}x^3 - \frac{1}{2}x^2 + 2x \right]_0^1 + \left[\frac{1}{3}x^3 + \frac{1}{2}x^2 - 2x \right]_1^2 \\
 &= \frac{7}{6} + \frac{11}{6} = 3
 \end{aligned}$$

26) 2

$$\begin{aligned}
 &\Rightarrow |x^2-4x+3| = \begin{cases} x^2-4x+3 & (x < 1 \text{ 또는 } x > 3) \\ -x^2+4x-3 & (1 \leq x \leq 3) \end{cases} \text{이므로} \\
 &\int_0^2 |x^2-4x+3| dx \\
 &= \int_0^1 (x^2-4x+3) dx + \int_1^2 (-x^2+4x-3) dx \\
 &= \left[\frac{1}{3}x^3 - 2x^2 + 3x \right]_0^1 + \left[-\frac{1}{3}x^3 + 2x^2 - 3x \right]_1^2 \\
 &= \frac{4}{3} + \frac{2}{3} = 2
 \end{aligned}$$

27) $\frac{1}{6}$

$$\begin{aligned}
 &\Rightarrow |x|x-1| = \begin{cases} x(1-x) & (x \leq 1) \\ x(x-1) & (x > 1) \end{cases} \text{이므로} \\
 &\int_{-1}^2 |x|x-1| dx \\
 &= \int_{-1}^1 x(1-x) dx + \int_1^2 x(x-1) dx \\
 &= \int_{-1}^1 (x-x^2) dx + \int_1^2 (x^2-x) dx
 \end{aligned}$$

$$= \left[\frac{1}{2}x^2 - \frac{1}{3}x^3 \right]_{-1}^1 + \left[\frac{1}{3}x^3 - \frac{1}{2}x^2 \right]_1^2$$

$$= -\frac{2}{3} + \frac{5}{6} = \frac{1}{6}$$

28) 29

$$\Rightarrow 6x|x-1| = \begin{cases} 6x(1-x) & (x \leq 1) \\ 6x(x-1) & (x > 1) \end{cases} \text{이므로}$$

$$\int_0^3 6x|x-1| dx$$

$$= \int_0^1 6x(1-x) dx + \int_1^3 6x(x-1) dx$$

$$= \int_0^1 (6x - 6x^2) dx + \int_1^3 (6x^2 - 6x) dx$$

$$= [3x^2 - 2x^3]_0^1 + [2x^3 - 3x^2]_1^3 = 1 + 28 = 29$$

29) 기

$$\Rightarrow \int_a^b f(x) dx = - \int_{-b}^{-a} f(x) dx \text{를 만족하면 함수}$$

$$y=f(x) \text{의 그래프는 원점에 대하여 대칭이다.}$$

$$f(x) = -x^3 - 2x \text{는 원점에 대하여 대칭이므로 '기'이다.}$$

30) 우

$$\Rightarrow \int_a^b f(x) dx = \int_{-b}^{-a} f(x) dx \text{를 만족하면 함수}$$

$$y=f(x) \text{의 그래프는 } y \text{축에 대하여 대칭이다.}$$

$$f(x) = x^4 + x^2 \text{은 } y \text{축에 대하여 대칭이므로 '우'이다.}$$

31) 기

$$\Rightarrow \int_a^b f(x) dx = - \int_{-b}^{-a} f(x) dx \text{를 만족하면 함수}$$

$$y=f(x) \text{의 그래프는 원점에 대하여 대칭이다.}$$

$$f(x) = x^5 + x \text{는 원점에 대하여 대칭이므로 '기'이다.}$$

32) 우

$$\Rightarrow \int_a^b f(x) dx = \int_{-b}^{-a} f(x) dx \text{를 만족하면 함수}$$

$$y=f(x) \text{의 그래프는 } y \text{축에 대하여 대칭이다.}$$

$$f(x) = x^8 + 1 \text{는 } y \text{축에 대하여 대칭이므로 '우'이다.}$$

33) 10

$$\Rightarrow \int_{-1}^1 (3x^2 + 4) dx = 2 \int_0^1 (3x^2 + 4) dx$$

$$= 2[x^3 + 4x]_0^1 = 10$$

34) 6

$$\Rightarrow \int_{-1}^1 (x+1)(3x+2) dx = \int_{-1}^1 (3x^2 + 5x + 2) dx$$

$$= \int_{-1}^1 (3x^2 + 2) dx + \int_{-1}^1 5x dx$$

$$= 2 \int_0^1 (3x^2 + 2) dx$$

$$= 2[x^3 + 2x]_0^1$$

$$= 2 \cdot 3 = 6$$

35) $\frac{32}{3}$

$$\Rightarrow \int_0^2 (2x^2 + 2x) dx - 2 \int_0^{-2} (x + x^2) dx$$

$$= \int_0^2 (2x^2 + 2x) dx + \int_{-2}^0 (2x + 2x^2) dx$$

$$= \int_{-2}^2 (2x^2 + 2x) dx$$

$$= 2 \int_0^2 2x^2 dx = 2 \left[\frac{2}{3}x^3 \right]_0^2 = \frac{32}{3}$$

36) 0

$$\Rightarrow \int_{-1}^1 (x^2 + x + 1) dx - \int_{-1}^1 (x^2 - x + 1) dx$$

$$= \int_{-1}^1 2x dx = 0$$

37) 36

$$\Rightarrow \int_{-2}^1 (6x^2 - 4x + 1) dx + \int_2^1 (-6x^2 + 4x - 1) dx$$

$$= \int_{-2}^1 (6x^2 - 4x + 1) dx + \int_1^2 (6x^2 - 4x + 1) dx$$

$$= \int_{-2}^2 (6x^2 - 4x + 1) dx$$

$$= 2 \int_0^2 (6x^2 + 1) dx$$

$$= 2[2x^3 + x]_0^2$$

$$= 2(16 + 2) = 36$$

38) 4

$$\Rightarrow \int_{-1}^0 (3x^2 + 4x^3 + 5x^4) dx - \int_1^0 (3x^2 + 4x^3 + 5x^4) dx$$

$$= \int_{-1}^0 (3x^2 + 4x^3 + 5x^4) dx + \int_0^1 (3x^2 + 4x^3 + 5x^4) dx$$

$$= \int_{-1}^1 (3x^2 + 4x^3 + 5x^4) dx = 2 \int_0^1 (3x^2 + 5x^4) dx$$

$$= 2[x^3 + x^5]_0^1 = 4$$

39) 20

$$\Rightarrow y = |x| \text{는 } y \text{축에 대하여 대칭인 함수이므로}$$

$$\int_{-2}^2 (3x^2 + |x|) dx = 2 \int_0^2 (3x^2 + x) dx$$

$$= 2 \left[x^3 + \frac{1}{2}x^2 \right]_0^2$$

$$= 2 \times 10 = 20$$

40) 0

$$\Rightarrow \int_{-1}^1 (x^3 + 3x) dx = 0$$

41) 2

$$\begin{aligned} &\Rightarrow \int_{-1}^1 (x+1)(x^2-x+1)dx \\ &= \int_{-1}^1 (x^3+1)dx = 2 \int_0^1 1dx \\ &= 2[x]_0^1 = 2 \end{aligned}$$

42) 0

$$\begin{aligned} &\Rightarrow \int_{-2}^2 (x^3-3x^2-2x+4)dx = 2 \int_0^2 (-3x^2+4)dx \\ &= 2[-x^3+4x]_0^2 = 0 \end{aligned}$$

43) 12

$$\begin{aligned} &\Rightarrow \int_{-1}^1 (5x^3-6x^2-7x+8)dx \\ &= 2 \int_0^1 (-6x^2+8)dx \\ &= 2[-2x^3+8x]_0^1 \\ &= 2(-2+8) = 12 \end{aligned}$$

44) 20

$$\begin{aligned} &\Rightarrow \int_{-2}^2 (100x^3+3x^2-90x+1)dx \\ &= 2 \int_0^2 (3x^2+1)dx \\ &= 2[x^3+x]_0^2 \\ &= 2(8+2) = 20 \end{aligned}$$

45) 42

$$\begin{aligned} &\Rightarrow \int_{-3}^3 (-x^3+3x^2+4x-2)dx \\ &= \int_{-3}^3 (3x^2-2)dx + \int_{-3}^3 (-x^3+4x)dx \\ &= 2 \int_0^3 (3x^2-2)dx = 2[x^3-2x]_0^3 \\ &= 2 \cdot 21 = 42 \end{aligned}$$

46) 2

$$\begin{aligned} &\Rightarrow \int_{-1}^0 (x^3-3x^2+2)dx + \int_0^1 (x^3-3x^2+2)dx \\ &= \int_{-1}^1 (x^3-3x^2+2)dx = 2 \int_0^1 (-3x^2+2)dx \\ &= 2[-x^3+2x]_0^1 = 2 \times 1 = 2 \end{aligned}$$

47) 2

$$\begin{aligned} &\Rightarrow \int_{-1}^0 (4x^3-2x+1)dx + \int_0^1 (4x^3-2x+1)dx \\ &= \int_{-1}^1 (4x^3-2x+1)dx = 2 \int_0^1 1dx \\ &= 2[x]_0^1 = 2 \end{aligned}$$

48) 28

$$\begin{aligned} &\Rightarrow \int_{-2}^1 (x^3+6x^2+2x-1)dx \\ &\quad + \int_1^2 (x^3+6x^2+2x-1)dx \\ &= \int_{-2}^2 (x^3+6x^2+2x-1)dx \\ &= 2 \int_0^2 (6x^2-1)dx \\ &= 2[2x^3-x]_0^2 \\ &= 2(16-2) = 28 \end{aligned}$$

49) 4

$$\begin{aligned} &\Rightarrow \int_{-1}^0 (1+2x+3x^2+4x^3)dx \\ &\quad + \int_0^1 (1+2x+3x^2+4x^3)dx \\ &= \int_{-1}^1 (1+2x+3x^2+4x^3)dx \\ &= 2 \int_0^1 (1+3x^2)dx \\ &= 2[x+x^3]_0^1 = 2 \times 2 = 4 \end{aligned}$$

50) $-\frac{4}{3}$

$$\begin{aligned} &\Rightarrow \int_{-1}^1 x(1-x)^2dx = \int_{-1}^1 (x^3-2x^2+x)dx \\ &= 2 \int_0^1 (-2x^2)dx \\ &= 2\left[-\frac{2}{3}x^3\right]_0^1 = -\frac{4}{3} \end{aligned}$$

51) 60

$$\begin{aligned} &\Rightarrow \int_{-2}^2 (5x^4+3x^3-7x-1)dx \\ &= \int_{-2}^2 (5x^4-1)dx + \int_{-2}^2 (3x^3-7x)dx \\ &= 2 \int_0^2 (5x^4-1)dx = 2[x^5-x]_0^2 \\ &= 2 \cdot 30 = 60 \end{aligned}$$

52) 10

$$\begin{aligned} &\Rightarrow \int_{-1}^1 (5x^4-6x^3+3x^2-7x+3)dx \\ &= 2 \int_0^1 (5x^4+3x^2+3)dx = 2[x^5+x^3+3x]_0^1 \\ &= 2 \times 5 = 10 \end{aligned}$$

53) 6

$$\begin{aligned} &\Rightarrow \int_{-1}^1 (5x^4+4x^3+3x^2+2x+1)dx \\ &= 2 \int_0^1 (5x^4+3x^2+1)dx = 2[x^5+x^3+x]_0^1 = 6 \end{aligned}$$

54) 4

$$\begin{aligned}
&\Rightarrow \int_{-1}^4 (5x^4 + 4x^3 + 3x^2) dx - \int_1^4 (5x^4 + 4x^3 + 3x^2) dx \\
&= \int_{-1}^4 (5x^4 + 4x^3 + 3x^2) dx + \int_4^1 (5x^4 + 4x^3 + 3x^2) dx \\
&= \int_{-1}^1 (5x^4 + 4x^3 + 3x^2) dx \\
&= 2 \int_0^1 (5x^4 + 3x^2) dx \\
&= 2 \left[x^5 + x^3 \right]_0^1 \\
&= 2(1+1) = 4
\end{aligned}$$

55) 0

$$\Rightarrow \int_{-1}^1 (x^5 + 2x) dx = 0$$

56) 12

$$\begin{aligned}
&\Rightarrow \int_{-2}^2 (x^5 - 2x^3 + 3x^2 - 1) dx \\
&= 2 \int_0^2 (3x^2 - 1) dx \\
&= 2 \left[x^3 - x \right]_0^2 \\
&= 2(8-2) = 12
\end{aligned}$$

57) 230

$$\begin{aligned}
&\Rightarrow \int_{-5}^5 (6x^5 - 8x^3 + 3x^2 - 2) dx \\
&= 2 \int_0^5 (3x^2 - 2) dx \\
&= 2 \left[x^3 - 2x \right]_0^5 \\
&= 2(125 - 10) = 230
\end{aligned}$$

58) 20

$$\begin{aligned}
&\Rightarrow \int_{-2}^2 (6x^5 - 4x^3 + 3x^2 + 2x + 1) dx \\
&= 2 \int_0^2 (3x^2 + 1) dx \\
&= 2 \left[x^3 + x \right]_0^2 \\
&= 2(8+2) = 20
\end{aligned}$$

59) 16

$$\begin{aligned}
&\Rightarrow \int_{-2}^1 (x^5 + 3x^2 - 2x) dx - \int_2^1 (x^5 + 3x^2 - 2x) dx \\
&= \int_{-2}^1 (x^5 + 3x^2 - 2x) dx + \int_1^2 (x^5 + 3x^2 - 2x) dx \\
&= \int_{-2}^2 (x^5 + 3x^2 - 2x) dx \\
&= 2 \int_0^2 3x^2 dx \\
&= 2 \left[x^3 \right]_0^2 = 2 \times 8 = 16
\end{aligned}$$

60) $\frac{4}{5}$

$$\begin{aligned}
&\Rightarrow \int_{-1}^1 x^3 (1+x)^2 dx \\
&= \int_{-1}^1 x^3 (1+2x+x^2) dx \\
&= 2 \int_0^1 2x^4 dx = 2 \left[\frac{2}{5} x^5 \right]_0^1 = \frac{4}{5}
\end{aligned}$$

61) 10

$$\begin{aligned}
&\Rightarrow \int_{-1}^1 (8x^9 - x^5 + 10x^4 - 3x^2 + 4) dx \\
&= 2 \int_0^1 (10x^4 - 3x^2 + 4) dx \\
&= 2 \left[2x^5 - x^3 + 4x \right]_0^1 \\
&= 2(2-1+4) = 10
\end{aligned}$$

62) 4

$$\begin{aligned}
&\Rightarrow \int_{-1}^1 (11x^{10} + 12x^{11} + 13x^{12} + 14x^{13}) dx \\
&= 2 \int_0^1 (11x^{10} + 13x^{12}) dx = 2 \left[x^{11} + x^{13} \right]_0^1 = 4
\end{aligned}$$

63) 6

$$\begin{aligned}
&\Rightarrow \int_{-1}^1 (x^{11} + 10x^9 - 25x^7 + 3x^2 - 9x + 2) dx \\
&= 2 \int_0^1 (3x^2 + 2) dx \\
&= 2 \left[x^3 + 2x \right]_0^1 \\
&= 2(1+2) = 6
\end{aligned}$$