

01 / 내림차순과 오름차순

(1) **내림차순**: 다항식을 한 문자에 대하여 차수가 높은 항부터 낮은 항의 순서로 나타내는 것

(2) **오름차순**: 다항식을 한 문자에 대하여 차수가 낮은 항부터 높은 항의 순서로 나타내는 것

예) $x^2 + 4x^3 + 5x + 2$ 을

내림차순으로 정리하면 $4x^3 + x^2 + 5x + 2$

오름차순으로 정리하면 $2 + 5x + x^2 + 4x^3$

■ 다음 다항식을 x 에 대하여 내림차순으로 정리하여라.

1. $3x^3 - 5x + 2 + x^2$

2. $-x + 2x^2 + 1$

3. $x^2 - 1 - x$

4. $x - 2 - x^2 + x^3$

5. $4 + 4x^2 + 2x$

6. $x - 3x^2 - 12 + 5x^3$

7. $3xy - x^2 + 2y^2 + x - 5$

8. $2x^2 + 3xy - y^2 + x - 10y + 1$

■ 다음 식을 x 에 대하여 오름차순으로 정리하여라.

9. $x - 3x^2 + 2$

10. $10 + 2x^3 - x^2$


11. $x - 3x^2 - 12 + 5x^3$

12. $2x^2 - 5x + 4 + x^3$

13. $x^2 + x + 1$

14. $-x + 3 + x^2$

15. $-xy + x^3 + 3x^2 - 2y$

	연산문제		DATE	
			NAME	
	1-1-1. 다항식의 연산		GRADE	

01

내림차순과 오름차순

(1) 내림차순: 다항식을 한 문자에 대하여 차수가 높은 항부터 낮은 항의 순서로 나타내는 것

(2) 오름차순: 다항식을 한 문자에 대하여 차수가 낮은 항부터 높은 항의 순서로 나타내는 것

예 $x^2 + 4x^3 + 5x + 2$ 을

내림차순으로 정리하면 $4x^3 + x^2 + 5x + 2$

오름차순으로 정리하면 $2 + 5x + x^2 + 4x^3$

다음 다항식을 x 에 대하여 내림차순으로 정리하여라.

1. $3x^3 - 5x + 2 + x^2$

2. $-x + 2x^2 + 1$

3. $x^2 - 1 - x$

4. $x - 2 - x^2 + x^3$

5. $4 + 4x^2 + 2x$

6. $x - 3x^2 - 12 + 5x^3$

7. $3xy - x^2 + 2y^2 + x - 5$

8. $2x^2 + 3xy - y^2 + x - 10y + 1$

다음 식을 x 에 대하여 오름차순으로 정리하여라.

9. $x - 3x^2 + 2$

10. $10 + 2x^3 - x^2$

11. $x - 3x^2 - 12 + 5x^3$

12. $2x^2 - 5x + 4 + x^3$

13. $x^2 + x + 1$

14. $-x + 3 + x^2$

15. $-xy + x^3 + 3x^2 - 2y$

02 / 다항식의 덧셈과 뺄셈**(1) 다항식의 덧셈과 뺄셈**

① 괄호를 푼다

② 각 항을 동류항끼리 모아서 간단히 정리한다.

(2) 다항식의 덧셈에 대한 성질세 다항식 A, B, C 에 대하여① **교환법칙:** $A+B=B+A$ ② **결합법칙:** $(A+B)+C=A+(B+C)$ 예) $(2x^2+x)-(x^2-4)=2x^2+x-x^2+4=x^2+x+4$

■ 다음 식을 간단히 하여라.

16. $2x^2-x+1+4x^2+5x-6$

17. $(10x^2+x-10)-(5x^2+4x+4)$

18. $(x^2+x+1)+(2x^2+x+3)$

19. $x+4y+1-(y+3x-2)$

20. $(-x^2+x-10)+(5x^2+4x+4)$

21. $(2x^2-3x-1)+(x^2+x+5)$

22. $(x^2+5)+(x^2+x+6)$

23. $x-y+1-(y+x-9)$

24. $(x+2y-1)+(2x-3y+2)$

25. $(x^2+2xy-3y^2)-(2x^2-5xy-y^2)$

26. $(2x-y+3)-3(x-2y+1)$

27. $(x^2+x+1)-(x^2+x+2)$

28. $x^2+4x+5-(x^2+2x+3)$

29. $2x^2+3x+5-(-x^2+x+2)$

30. $(2x^2+3x-2)+(x^2-2x+3)$

31. $(x^3+2x^2+4x)+(3x^2-x+2)$

32. $2x^2+xy+y^2-2(x^2-xy+y^2)$

33. $2(x^2-2x+3)-3(2x^2+5x-1)$

34. $x+7y+2-2y-3x-7-5y$

35. $(-x^3+4x^2-5)-(5x^3+2x^2+x+2)$

36. $(-x^3+4x^2-5)+(5x^3+2x^2+x+2)$

37. $(4x^2 + y^2) - (2xy - 5y^2) + (x^2 - 3xy)$

38. $(2x^3 + x^2 - 1) + (-x^3 + x - 3)$

39. $4x + 5 - \{x - 3(x - 2) - 4\}$

40. $3y - 3 + \{2 + 3x + (10 - x - y) - 1\}$

41. $a - b - \{2a - (b + 3a)\}$

42. $(a + b - 2c) - \{(a + b + c) - 3b\}$

43. $a - \{10 - b - c + (a + 2b + 2c) + 1\}$

44. $3 - a + 2\left[a - 4 - \frac{1}{2}\{a - 4 + 3(a - 2)\}\right]$

▣ 다음 두 다항식 A , B 에 대하여 $A + B$, $A - B$ 를 구하여라.

45. $A = -x^3 - 2x^2 - x + 4$, $B = x^3 - x^2 - 3x - 2$

46. $A = 5x^3 - 3x + 1$, $B = x^2 - x + 3$

47. $A = x^2 + 2x + 6$, $B = 3x^2 + 4x + 2$

▣ 두 다항식 $A = x^2 + 4x - 3$, $B = 3x^2 - 2x + 1$ 에 대하여 다음을 구하여라.

48. $A - 3B$

49. $3A + 2(B - A)$

50. $A - 2(A + B)$

51. $(A + 2B) - (3A + 2B)$

▣ 세 다항식 $A = x^2 + 3x - 5$, $B = -5x^2 - 3x + 2$, $C = -x^2 + 3x - 6$ 에 대하여 다음을 구하여라.

52. $A + B - C$

53. $B - 2(A - C)$

54. $A - 2B - 3C$

■ 두 다항식 $A = -2x^2 - 3xy + y^2$, $B = 4x^2 + 5xy - 2y^2$ 에 대하여 다음을 구하여라.

55. $B - (3A + 4B)$

56. $2(A - 2B) - 3(2A - B)$

57. $-(3B + A) + 2(A + 2B)$

■ 세 다항식 $A = x^3 - 2x^2 + 3x - 1$, $B = 3x^3 + x^2 - 4$, $C = -x^2 - 3x + 5$ 에 대하여 다음을 계산하여라.

58. $A + B - C$

59. $(A + 3B) - (A - 2C)$

60. $3A - (2B - C)$

■ 세 다항식 $A = -x^3 + 2x^2 + 1$, $B = x^2 + 4x$, $C = x^3 - 2x^2 + x + 7$ 에 대하여 다음을 계산하여라.

61. $A + B + C$

62. $2A + B - 3C$

63. $A - B - C$

64. $A + 2B - C$

65. $2A + B - 2(A - C)$

66. $4A - \{B + 3(A - C)\}$

■ 세 다항식 $A = 4x^3 - x^2 + 1$, $B = 2x^3 - 5x^2 + x + 3$, $C = x^3 - 7x^2 + 2$ 에 대하여 다음을 구하여라.

67. $2A - B$

68. $A - 2B + C$

69. $2A - 3(A - B) - C$

70. $(A + C) - (B - 2C)$

■ 다음 주어진 다항식에 대하여 <보기>의 식을 만족시키는 다항식 X 를 구하여라.

71. $A = -x^2 + 2xy + 6y^2$, $B = 4x^2 - 5xy + 3y^2$

<보기>
 $A - 3X = -B$

72. $A = x^2 + xy - 3y^2$, $B = 3x^2 - xy + y^2$

<보기>
 $A - 2X = B$

73. $A = 2x^2 + x + 2$, $B = 3x^2 - 2x + 3$

<보기>
 $2A - X = B$

74. $A = 2x^2 + 5xy - 4y^2$, $B = -x^2 + 3xy + 6y^2$

<보기>
 $X = A - B$

75. $A = x^2 + 2xy - y^2$, $B = x^2 - xy - 5y^2$

<보기>
 $3A + X = B$

76. $A = x^3 - 3x^2 + x - 4$, $B = 3x^2 - 9x + 6$

<보기>
 $3(X + 2A) = B$

77. $A = x^2 - xy - 2y^2$, $B = x^2 - xy - y^2$

<보기>
 $A - 2(X + B) = -3A$

78. $A = 3x^2 + 2xy - 4y^2$, $B = x^2 - xy + y^2$

<보기>
 $X + 3(A - B) = 2A$

79. $A = 3x^2 + 5x - 2$, $B = x^2 - 2x + 1$

<보기>
 $3B - 2(X - A) = 5B$

80. $A = 2x^3 - 4x^2 + 6$, $B = 5x^3 - 2x + 1$,
 $C = 3x^3 - 4x^2 - 3x$

<보기>
 $A + 4(X + C) = 2B$



정답 및 해설

1) $3x^3 + x^2 - 5x + 2$

2) $2x^2 - x + 1$

3) $x^2 - x - 1$

4) $x^3 - x^2 + x - 2$

5) $4x^2 + 2x + 4$

6) $5x^3 - 3x^2 + x - 12$

7) $-x^2 + (3y+1)x + 2y^2 - 5$

8) $2x^2 + (3y+1)x - y^2 - 10y + 1$

9) $2 + x - 3x^2$

10) $10 - x^2 + 2x^3$

11) $-12 + x - 3x^2 + 5x^3$

12) $4 - 5x + 2x^2 + x^3$

13) $1 + x + x^2$

14) $3 - x + x^2$

15) $-2y - yx + 3x^2 + x^3$

16) $6x^2 + 4x - 5$

17) $5x^2 - 3x - 14$

$$\begin{aligned} \Rightarrow (10x^2 + x - 10) - (5x^2 + 4x + 4) \\ = 10x^2 + x - 10 - 5x^2 - 4x - 4 \\ = (10x^2 - 5x^2) + (x - 4x) + (-10 - 4) \\ = 5x^2 - 3x - 14 \end{aligned}$$

18) $3x^2 + 2x + 4$

$$\begin{aligned} \Rightarrow (x^2 + x + 1) + (2x^2 + x + 3) \\ = (x^2 + 2x^2) + (x + x) + (1 + 3) \\ = 3x^2 + 2x + 4 \end{aligned}$$

19) $-2x + 3y + 3$

$$\begin{aligned} \Rightarrow x + 4y + 1 - (y + 3x - 2) = x + 4y + 1 - y - 3x + 2 \\ = -2x + 3y + 3 \end{aligned}$$

20) $4x^2 + 5x - 6$

$$\begin{aligned} \Rightarrow (-x^2 + x - 10) + (5x^2 + 4x + 4) \\ = (-x^2 + 5x^2) + (x + 4x) + (-10 + 4) \\ = 4x^2 + 5x - 6 \end{aligned}$$

21) $3x^2 - 2x + 4$

$$\begin{aligned} \Rightarrow (2x^2 - 3x - 1) + (x^2 + x + 5) \\ = (2x^2 + x^2) + (-3x + x) + (-1 + 5) \\ = 3x^2 - 2x + 4 \end{aligned}$$

22) $2x^2 + x + 11$

$$\begin{aligned} \Rightarrow (x^2 + 5) + (x^2 + x + 6) \\ = (x^2 + x^2) + x + (5 + 6) \\ = 2x^2 + x + 11 \end{aligned}$$

23) $-2y + 10$

$$\begin{aligned} \Rightarrow x - y + 1 - (y + x - 9) = x - y + 1 - y - x + 9 \\ = -2y + 10 \end{aligned}$$

24) $3x - y + 1$

25) $-x^2 + 7xy - 2y^2$

$$\begin{aligned} \Rightarrow (x^2 + 2xy - 3y^2) - (2x^2 - 5xy - y^2) \\ = x^2 + 2xy - 3y^2 - 2x^2 + 5xy + y^2 \\ = -x^2 + 7xy - 2y^2 \end{aligned}$$

26) $-x + 5y$

$$\begin{aligned} \Rightarrow (2x - y + 3) - 3(x - 2y + 1) = 2x - y + 3 - 3x + 6y - 3 \\ = -x + 5y \end{aligned}$$

27) -1

$$\begin{aligned} \Rightarrow (x^2 + x + 1) - (x^2 + x + 2) \\ = x^2 + x + 1 - x^2 - x - 2 \\ = (x^2 - x^2) + (x - x) + (1 - 2) \\ = -1 \end{aligned}$$

28) $2x + 2$

29) $3x^2 + 2x + 3$

30) $3x^2 + x + 1$

31) $x^3 + 5x^2 + 3x + 2$

32) $3xy - y^2$

33) $-4x^2 - 19x + 9$

34) $-2x - 5$

35) $-6x^3 + 2x^2 - x - 7$

$$\begin{aligned} \Rightarrow (-x^3 + 4x^2 - 5) - (5x^3 + 2x^2 + x + 2) \\ = -x^3 + 4x^2 - 5 - 5x^3 - 2x^2 - x - 2 \\ = (-x^3 - 5x^3) + (4x^2 - 2x^2) - x + (-5 - 2) \\ = -6x^3 + 2x^2 - x - 7 \end{aligned}$$

36) $4x^3 + 6x^2 + x - 3$

$$\begin{aligned} \Rightarrow (-x^3 + 4x^2 - 5) + (5x^3 + 2x^2 + x + 2) \\ = (-x^3 + 5x^3) + (4x^2 + 2x^2) + x + (-5 + 2) \\ = 4x^3 + 6x^2 + x - 3 \end{aligned}$$

37) $5x^2 - 5xy + 6y^2$

$$\begin{aligned} \Rightarrow (4x^2+y^2)-(2xy-5y^2)+(x^2-3xy) \\ = 4x^2+y^2-2xy+5y^2+x^2-3xy \\ = 5x^2-5xy+6y^2 \end{aligned}$$

$$38) x^3+x^2+x-4$$

$$39) 6x+3$$

$$\begin{aligned} \Rightarrow 4x+5-\{x-3(x-2)-4\} \\ = 4x+5-(x-3x+6-4) \\ = 4x+5-(-2x+2) \\ = 4x+5+2x-2 \\ = 6x+3 \end{aligned}$$

$$40) 2x+2y+8$$

$$\begin{aligned} \Rightarrow 3y-3+\{2+3x+(10-x-y)-1\} \\ = 3y-3+(2+3x+10-x-y-1) \\ = 3y-3+(2x-y+11) \\ = 2x+2y+8 \end{aligned}$$

$$41) 2a$$

$$\begin{aligned} \Rightarrow a-b-\{2a-(b+3a)\} &= a-b-(2a-b-3a) \\ &= a-b-(-a-b) \\ &= a-b+a+b=2a \end{aligned}$$

$$42) 3b-3c$$

$$\begin{aligned} \Rightarrow (a+b-2c)-\{(a+b+c)-3b\} \\ = a+b-2c-(a-2b+c) \\ = a+b-2c-a+2b-c \\ = 3b-3c \end{aligned}$$

$$43) -b-c-11$$

$$\begin{aligned} \Rightarrow a-\{10-b-c+(a+2b+2c)+1\} \\ = a-(10-b-c+a+2b+2c+1) \\ = a-(a+b+c+11) \\ = -b-c-11 \end{aligned}$$

$$44) -3a+5$$

$$\begin{aligned} \Rightarrow 3-a+2\left[a-4-\frac{1}{2}\{a-4+3(a-2)\}\right] \\ = 3-a+2\left\{a-4-\frac{1}{2}(a-4+3a-6)\right\} \\ = 3-a+2\left\{a-4-\frac{1}{2}(4a-10)\right\} \\ = 3-a+2(a-4-2a+5) \\ = 3-a+2(-a+1) \\ = 3-a-2a+2=-3a+5 \end{aligned}$$

$$45) A+B=-3x^2-4x+2, \quad A-B=-2x^3-x^2+2x+6$$

$$\begin{aligned} \Rightarrow A+B &= (-x^3-2x^2-x+4)+(x^3-x^2-3x-2) \\ &= -3x^2-4x+2 \end{aligned}$$

$$\begin{aligned} A-B &= (-x^3-2x^2-x+4)-(x^3-x^2-3x-2) \\ &= -2x^3-x^2+2x+6 \end{aligned}$$

$$46) A+B=5x^3+x^2-4x+4,$$

$$A-B=5x^3-x^2-2x-2$$

$$\begin{aligned} \Rightarrow A+B &= (5x^3-3x+1)+(x^2-x+3) \\ &= 5x^3+x^2-4x+4 \end{aligned}$$

$$\begin{aligned} A-B &= (5x^3-3x+1)-(x^2-x+3) \\ &= 5x^3-x^2-2x-2 \end{aligned}$$

$$47) A+B=4x^2+6x+8, \quad A-B=-2x^2-2x+4$$

$$48) -8x^2+10x-6$$

$$\begin{aligned} \Rightarrow A-3B &= (x^2+4x-3)-3(3x^2-2x+1) \\ &= x^2+4x-3-9x^2+6x-3 \\ &= -8x^2+10x-6 \end{aligned}$$

$$49) 7x^2-1$$

$$\begin{aligned} \Rightarrow 3A+2(B-A) &= A+2B \\ &= (x^2+4x-3)+2(3x^2-2x+1) \\ &= x^2+4x-3+6x^2-4x+2=7x^2-1 \end{aligned}$$

$$50) 5x^2-8x+5$$

$$\begin{aligned} \Rightarrow A-2(A+B) &= A-2A-2B=-A-2B \\ &= -(x^2+4x-3)-2(3x^2-2x+1) \\ &= -x^2-4x+3-6x^2+4x-2 \\ &= -7x^2+1 \end{aligned}$$

$$51) -2x^2-8x+6$$

$$\begin{aligned} \Rightarrow (A+2B)-(3A+2B) &= A+2B-3A-2B=-2A \\ &= -2(x^2+4x-3)=-2x^2-8x+6 \end{aligned}$$

$$52) -3x^2-3x+3$$

$$\begin{aligned} \Rightarrow A+B-C &= (x^2+3x-5)+(-5x^2-3x+2)-(-x^2+3x-6) \\ &= x^2+3x-5-5x^2-3x+2+x^2-3x+6 \\ &= -3x^2-3x+3 \end{aligned}$$

$$53) -9x^2-3x$$

$$\begin{aligned} \Rightarrow B-2(A-C) &= B-2A+2C \\ &= (-5x^2-3x+2)-2(x^2+3x-5) \\ &\quad +2(-x^2+3x-6) \\ &= -5x^2-3x+2-2x^2-6x+10-2x^2+6x-12 \\ &= -9x^2-3x \end{aligned}$$

$$54) 14x^2+9$$

$$\begin{aligned} \Rightarrow A-2B-3C &= (x^2+3x-5)-2(-5x^2-3x+2) \\ &\quad -3(-x^2+3x-6) \\ &= x^2+3x-5+10x^2+6x-4+3x^2-9x+18 \\ &= 14x^2+9 \end{aligned}$$

$$55) -6x^2-6xy+3y^2$$

$$\begin{aligned} \Rightarrow B-(3A+4B) &= B-3A-4B=-3A-3B \\ &= -3(-2x^2-3xy+y^2)-3(4x^2+5xy-2y^2) \\ &= 6x^2+9xy-3y^2-12x^2-15xy+6y^2 \\ &= -6x^2-6xy+3y^2 \end{aligned}$$

$$56) 4x^2+7xy-2y^2$$

$$\begin{aligned} \Rightarrow 2(A-2B)-3(2A-B) &= 2A-4B-6A+3B=-4A-B \end{aligned}$$

$$\begin{aligned}
&= -4(-2x^2 - 3xy + y^2) - (4x^2 + 5xy - 2y^2) \\
&= 8x^2 + 12xy - 4y^2 - 4x^2 - 5xy + 2y^2 \\
&= 4x^2 + 7xy - 2y^2
\end{aligned}$$

$$\begin{aligned}
57) \quad & 2x^2 + 2xy - y^2 \\
\Rightarrow & -(3B + A) + 2(A + 2B) \\
&= -3B - A + 2A + 4B = A + B \\
&= (-2x^2 - 3xy + y^2) + (4x^2 + 5xy - 2y^2) \\
&= 2x^2 + 2xy - y^2
\end{aligned}$$

$$\begin{aligned}
58) \quad & 4x^3 + 6x - 10 \\
\Rightarrow & A + B - C \\
&= (x^3 - 2x^2 + 3x - 1) + (3x^3 + x^2 - 4) - (-x^2 - 3x + 5) \\
&= (x^3 - 2x^2 + 3x - 1) + (3x^3 + x^2 - 4) + x^2 + 3x - 5 \\
&= 4x^3 + 6x - 10
\end{aligned}$$

$$\begin{aligned}
59) \quad & 9x^3 + x^2 - 6x - 2 \\
\Rightarrow & (A + 3B) - (A - 2C) = A + 3B - A + 2C = 3B + 2C \\
&= 3(3x^3 + x^2 - 4) + 2(-x^2 - 3x + 5) \\
&= 9x^3 + 3x^2 - 12 - 2x^2 - 6x + 10 \\
&= 9x^3 + x^2 - 6x - 2
\end{aligned}$$

$$\begin{aligned}
60) \quad & -3x^3 - 9x^2 + 6x + 10 \\
\Rightarrow & 3A - (2B - C) = 3A - 2B + C \\
&= 3(x^3 - 2x^2 + 3x - 1) - 2(3x^3 + x^2 - 4) + (-x^2 - 3x + 5) \\
&= -3x^3 - 9x^2 + 6x + 10
\end{aligned}$$

$$\begin{aligned}
61) \quad & x^2 + 5x + 8 \\
\Rightarrow & A + B + C \\
&= (-x^3 + 2x^2 + 1) + (x^2 + 4x) + (x^3 - 2x^2 + x + 7) \\
&= x^2 + 5x + 8
\end{aligned}$$

$$\begin{aligned}
62) \quad & -5x^3 + 11x^2 + x - 19 \\
\Rightarrow & 2A + B - 3C \\
&= 2(-x^3 + 2x^2 + 1) + (x^2 + 4x) - 3(x^3 - 2x^2 + x + 7) \\
&= -2x^3 + 4x^2 + 2 + x^2 + 4x - 3x^3 + 6x^2 - 3x - 21 \\
&= -5x^3 + 11x^2 + x - 19
\end{aligned}$$

$$\begin{aligned}
63) \quad & -2x^3 + 3x^2 - 5x - 6 \\
\Rightarrow & A - B - C \\
&= (-x^3 + 2x^2 + 1) - (x^2 + 4x) - (x^3 - 2x^2 + x + 7) \\
&= (-x^3 + 2x^2 + 1) - x^2 - 4x - x^3 + 2x^2 - x - 7 \\
&= -2x^3 + 3x^2 - 5x - 6
\end{aligned}$$

$$\begin{aligned}
64) \quad & -2x^3 + 6x^2 + 7x - 6 \\
\Rightarrow & A + 2B - C \\
&= (-x^3 + 2x^2 + 1) + 2(x^2 + 4x) - (x^3 - 2x^2 + x + 7) \\
&= -x^3 + 2x^2 + 1 + 2x^2 + 8x - x^3 + 2x^2 - x - 7 \\
&= -2x^3 + 6x^2 + 7x - 6
\end{aligned}$$

$$\begin{aligned}
65) \quad & 2x^3 - 3x^2 + 6x + 14 \\
\Rightarrow & 2A + B - 2(A - C) = 2A + B - 2A + 2C = B + 2C
\end{aligned}$$

$$\begin{aligned}
&= (x^2 + 4x) + 2(x^3 - 2x^2 + x + 7) \\
&= x^2 + 4x + 2x^3 - 4x^2 + 2x + 14 \\
&= 2x^3 - 3x^2 + 6x + 14
\end{aligned}$$

$$\begin{aligned}
66) \quad & 2x^3 - 5x^2 - x + 22 \\
\Rightarrow & 4A - \{B + 3(A - C)\} \\
&= 4A - B - 3A + 3C = A - B + 3C \\
&= (-x^3 + 2x^2 + 1) - (x^2 + 4x) + 3(x^3 - 2x^2 + x + 7) \\
&= -x^3 + 2x^2 + 1 - x^2 - 4x + 3x^3 - 6x^2 + 3x + 21 \\
&= 2x^3 - 5x^2 - x + 22
\end{aligned}$$

$$\begin{aligned}
67) \quad & 6x^3 + 3x^2 - x - 1 \\
\Rightarrow & 2A - B = 2(4x^3 - x^2 + 1) - (2x^3 - 5x^2 + x + 3) \\
&= 8x^3 - 2x^2 + 2 - 2x^3 + 5x^2 - x - 3 \\
&= 6x^3 + 3x^2 - x - 1
\end{aligned}$$

$$\begin{aligned}
68) \quad & x^3 + 2x^2 - 2x - 3 \\
\Rightarrow & A - 2B + C \\
&= (4x^3 - x^2 + 1) - 2(2x^3 - 5x^2 + x + 3) \\
&\quad + (x^3 - 7x^2 + 2) \\
&= 4x^3 - x^2 + 1 - 4x^3 + 10x^2 - 2x - 6 + x^3 - 7x^2 + 2 \\
&= x^3 + 2x^2 - 2x - 3
\end{aligned}$$

$$\begin{aligned}
69) \quad & x^3 - 7x^2 + 3x + 6 \\
\Rightarrow & 2A - 3(A - B) - C \\
&= 2A - 3A + 3B - C = -A + 3B - C \\
&= -(4x^3 - x^2 + 1) + 3(2x^3 - 5x^2 + x + 3) \\
&\quad - (x^3 - 7x^2 + 2) \\
&= -4x^3 + x^2 - 1 + 6x^3 - 15x^2 + 3x + 9 - x^3 + 7x^2 - 2 \\
&= x^3 - 7x^2 + 3x + 6
\end{aligned}$$

$$\begin{aligned}
70) \quad & 5x^3 - 17x^2 - x + 4 \\
\Rightarrow & (A + C) - (B - 2C) = A + C - B + 2C = A - B + 3C \\
&= (4x^3 - x^2 + 1) - (2x^3 - 5x^2 + x + 3) \\
&\quad + 3(x^3 - 7x^2 + 2) \\
&= 4x^3 - x^2 + 1 - 2x^3 + 5x^2 - x - 3 + 3x^3 - 21x^2 + 6 \\
&= 5x^3 - 17x^2 - x + 4
\end{aligned}$$

$$\begin{aligned}
71) \quad & x^2 - xy + 3y^2 \\
\Rightarrow & A - 3X = -B \text{에} \text{서} \\
& 3X = A + B \\
&= (-x^2 + 2xy + 6y^2) + (4x^2 - 5xy + 3y^2) \\
&= 3x^2 - 3xy + 9y^2
\end{aligned}$$

$$\therefore X = \frac{1}{3}(3x^2 - 3xy + 9y^2) = x^2 - xy + 3y^2$$

$$\begin{aligned}
72) \quad & -x^2 + xy - 2y^2 \\
\Rightarrow & A - 2X = B \text{에} \text{서} \quad -2X = -A + B \text{이므로} \\
& 2X = A - B \\
&= (x^2 + xy - 3y^2) - (3x^2 - xy + y^2) \\
&= -2x^2 + 2xy - 4y^2
\end{aligned}$$

양변을 2로 나누면

$$\therefore X = -x^2 + xy - 2y^2$$

$$73) x^2 + 4x + 1$$

$$\Rightarrow 2A - X = B \text{에} \text{서} \quad X = 2A - B$$

$$\begin{aligned} \therefore X &= 2A - B = 2(2x^2 + x + 2) - (3x^2 - 2x + 3) \\ &= 4x^2 + 2x + 4 - 3x^2 + 2x - 3 \\ &= x^2 + 4x + 1 \end{aligned}$$

$$74) 3x^2 + 2xy - 10y^2$$

$$\begin{aligned} \Rightarrow X &= A - B \\ &= (2x^2 + 5xy - 4y^2) - (-x^2 + 3xy + 6y^2) \\ &= 3x^2 + 2xy - 10y^2 \end{aligned}$$

$$75) -2x^2 - 7xy - 2y^2$$

$$\begin{aligned} \Rightarrow 3A + X &= B \text{에} \text{서} \\ X &= -3A + B \\ &= -3(x^2 + 2xy - y^2) + (x^2 - xy - 5y^2) \\ &= -3x^2 - 6xy + 3y^2 + x^2 - xy - 5y^2 \\ &= -2x^2 - 7xy - 2y^2 \end{aligned}$$

$$76) -2x^3 + 7x^2 - 5x + 10$$

$$\Rightarrow 3(X + 2A) = B \text{에} \text{서} \quad 3X + 6A = B \text{이므로}$$

$$\begin{aligned} 3X &= -6A + B \\ &= -6(x^3 - 3x^2 + x - 4) + (3x^2 - 9x + 6) \\ &= -6x^3 + 18x^2 - 6x + 24 + 3x^2 - 9x + 6 \\ &= -6x^3 + 21x^2 - 15x + 30 \end{aligned}$$

$$\therefore X = -2x^3 + 7x^2 - 5x + 10$$

$$77) x^2 - xy - 3y^2$$

$$\begin{aligned} \Rightarrow A - 2(X + B) &= -3A \text{에} \text{서} \\ A - 2X - 2B &= -3A, \quad 2X = 4A - 2B \end{aligned}$$

$$\begin{aligned} \therefore X &= 2A - B \\ &= 2(x^2 - xy - 2y^2) - (x^2 - xy - y^2) \\ &= 2x^2 - 2xy - 4y^2 - x^2 + xy + y^2 \\ &= x^2 - xy - 3y^2 \end{aligned}$$

$$78) -5xy + 7y^2$$

$$\begin{aligned} \Rightarrow X + 3(A - B) &= 2A \text{에} \text{서} \\ X &= 2A - 3(A - B) \\ &= -A + 3B \\ &= -(3x^2 + 2xy - 4y^2) + 3(x^2 - xy + y^2) \\ &= -3x^2 - 2xy + 4y^2 + 3x^2 - 3xy + 3y^2 \\ &= -5xy + 7y^2 \end{aligned}$$

$$79) 2x^2 + 7x - 3$$

$$\begin{aligned} \Rightarrow 3B - 2(X - A) &= 5B \text{에} \text{서} \\ 3B - 2X + 2A &= 5B, \quad 2X = 2A - 2B \\ \therefore X &= A - B = (3x^2 + 5x - 2) - (x^2 - 2x + 1) \\ &= 2x^2 + 7x - 3 \end{aligned}$$

$$80) -x^3 + 5x^2 + 2x - 1$$

$$\begin{aligned} \Rightarrow A + 4(X + C) &= 2B \text{에} \text{서} \quad A + 4X + 4C = 2B \text{이므로} \\ 4X &= -A + 2B - 4C \\ &= -(2x^3 - 4x^2 + 6) + 2(5x^3 - 2x + 1) - 4(3x^3 - 4x^2 - 3x) \\ &= -2x^3 + 4x^2 - 6 + 10x^3 - 4x + 2 - 12x^3 + 16x^2 + 12x \\ &= -4x^3 + 20x^2 + 8x - 4 \end{aligned}$$

$$\therefore X = -x^3 + 5x^2 + 2x - 1$$