



◇ 「콘텐츠산업 진흥법 시행령」 제33조에 의한 표시

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3) 이 콘텐츠는 「콘텐츠산업 진흥법」에 따라 최초 제작일부터 5년간 보호됩니다.

◇ 「콘텐츠산업 진흥법」 외에도 「저작권법」에 의하여 보호되는 콘텐츠의 경우, 그 콘텐츠의 전부 또는 일부를 무단으로 복제하거나 전송하는 것은 콘텐츠산업 진흥법 외에도 저작권법에 의한 법적 책임을 질 수 있습니다.

01 여러 가지 각에 대한 삼각함수의 성질(1) $2n\pi + x$ 의 삼각함수 (단, n 은 정수)

① $\sin(2n\pi + x) = \sin x$

② $\cos(2n\pi + x) = \cos x$

③ $\tan(2n\pi + x) = \tan x$

(2) $-x$ 의 삼각함수

① $\sin(-x) = -\sin x$

② $\cos(-x) = \cos x$

③ $\tan(-x) = -\tan x$

(3) $\frac{\pi}{2} \pm x$ 의 삼각함수

① $\sin\left(\frac{\pi}{2} + x\right) = \cos x, \sin\left(\frac{\pi}{2} - x\right) = \cos x$

② $\cos\left(\frac{\pi}{2} + x\right) = -\sin x, \cos\left(\frac{\pi}{2} - x\right) = \sin x$

③ $\tan\left(\frac{\pi}{2} + x\right) = -\frac{1}{\tan x}, \tan\left(\frac{\pi}{2} - x\right) = \frac{1}{\tan x}$

(4) $\pi \pm x$ 의 삼각함수

① $\sin(\pi + x) = -\sin x, \sin(\pi - x) = \sin x$

② $\cos(\pi + x) = -\cos x, \cos(\pi - x) = -\cos x$

③ $\tan(\pi + x) = \tan x, \tan(\pi - x) = -\tan x$

■ 다음 θ 에 대하여 $\sin \theta, \cos \theta, \tan \theta$ 의 값을 구하여라.

1. $\theta = \frac{5}{4}\pi$

2. $\theta = \frac{7}{6}\pi$

3. $\theta = \frac{2}{3}\pi$

4. $\theta = -\frac{\pi}{3}$

5. $\theta = -\frac{\pi}{4}$

■ 다음 삼각함수의 값을 구하여라.

6. $\tan\left(\frac{\pi}{2} + \frac{\pi}{6}\right)$

7. $\tan\left(\frac{\pi}{2} - \frac{\pi}{6}\right)$

8. $\sin\left(\frac{\pi}{2} + \frac{\pi}{3}\right)$

9. $\sin \frac{5}{4}\pi$

10. $\tan \frac{4}{3}\pi$

11. $\cos \frac{7}{6}\pi$

12. $\tan \frac{19}{3}\pi$

13. $\tan\left(-\frac{9}{4}\pi\right)$

14. $\cos \frac{9}{4}\pi$

15. $\cos \frac{5}{4}\pi$

16. $\sin \frac{5}{6}\pi$

17. $\tan \frac{7}{3}\pi$

18. $\cos \frac{25}{6}\pi$

19. $\tan \frac{5}{6}\pi$

20. $\cos \frac{3}{4}\pi$

21. $\sin \frac{2}{3}\pi$

22. $\sin \frac{13}{6}\pi$

23. $\sin \left(-\frac{13}{6}\pi\right)$

24. $\sin \left(-\frac{\pi}{4}\right)$

25. $\cos \left(-\frac{\pi}{4}\right)$

26. $\sin \left(-\frac{\pi}{6}\right)$

27. $\tan \frac{11}{6}\pi$

28. $\sin 120^\circ$

29. $\tan 150^\circ$

30. $\cos 135^\circ$

31. $\sin 210^\circ$

32. $\tan 390^\circ$

33. $\tan 210^\circ$

34. $\cos 330^\circ$

35. $\sin 780^\circ$

36. $\cos 750^\circ$

37. $\sin 450^\circ$

38. $\cos 240^\circ$

■ 다음 삼각함수의 값을 이용하여
 $\sin(\pi+\theta)$, $\cos(\pi+\theta)$, $\tan(\pi+\theta)$ 의 값을 구하여라.
 (단, $0 < \theta < \frac{\pi}{2}$)

39. $\tan \theta = \frac{2}{3}$

40. $\cos \theta = \frac{4}{5}$

41. $\sin \theta = \frac{\sqrt{3}}{4}$

■ 다음 삼각함수의 값을 이용하여
 $\sin(\pi-\theta)$, $\cos(\pi-\theta)$, $\tan(\pi-\theta)$ 의 값을 구하여라.
 (단, $0 < \theta < \frac{\pi}{2}$)

42. $\tan \theta = \frac{\sqrt{6}}{3}$

43. $\cos \theta = \frac{4}{5}$

44. $\sin \theta = \frac{\sqrt{5}}{5}$

■ 다음 삼각함수의 값을 이용하여
 $\sin\left(\frac{\pi}{2}-\theta\right)$, $\cos\left(\frac{\pi}{2}-\theta\right)$, $\tan\left(\frac{\pi}{2}-\theta\right)$ 의 값을 구하여라.
 (단, $0 < \theta < \frac{\pi}{2}$)

45. $\tan \theta = \frac{\sqrt{2}}{2}$

46. $\cos \theta = \frac{12}{13}$

47. $\sin \theta = \frac{8}{17}$

■ 다음 삼각함수의 값을 이용하여
 $\sin\left(\frac{\pi}{2}+\theta\right)$, $\cos\left(\frac{\pi}{2}+\theta\right)$, $\tan\left(\frac{\pi}{2}+\theta\right)$ 의 값을 구하여라.
 (단, $0 < \theta < \frac{\pi}{2}$)

48. $\tan \theta = \frac{\sqrt{15}}{7}$

49. $\cos \theta = \frac{4}{5}$

50. $\cos \theta = \frac{5}{6}$

51. $\sin \theta = \frac{\sqrt{14}}{6}$

■ 다음 식의 값을 구하여라.

52. $\sin \frac{5}{6}\pi + \cos \frac{4}{3}\pi$

53. $\cos \frac{7\pi}{6} - \tan \frac{2\pi}{3}$

54. $\sin\left(\frac{3}{2}\pi - \frac{\pi}{3}\right) + \tan \frac{7}{4}\pi$

55. $\sin \frac{7}{6}\pi + \cos\left(-\frac{8}{3}\pi\right) - \tan\left(-\frac{7}{4}\pi\right)$

56. $\sin \frac{2}{3}\pi + \cos\left(-\frac{13}{6}\pi\right) + \tan \frac{8}{3}\pi$

57. $\frac{1}{\sin \frac{\pi}{3}} - \cos \frac{3}{4}\pi + 2\tan\left(-\frac{7}{6}\pi\right)$

58. $\sin\left(-\frac{13}{6}\pi\right)\cos\left(-\frac{2}{3}\pi\right) + \frac{1}{\sin 300^\circ} \cdot \tan 210^\circ$

■ 다음 식을 간단히 하여라.

59. $\frac{\sin\left(\frac{3}{2}\pi - \theta\right)}{\cos\left(\frac{\pi}{2} + \theta\right)\cos^2\theta} - \frac{\sin(\pi + \theta)\tan(\pi - \theta)}{\cos\left(\frac{3}{2}\pi + \theta\right)}$

60. $\frac{\cos(\pi + \theta)}{\sin\left(\frac{3}{2}\pi + \theta\right)} + \frac{\tan \frac{19}{4}\pi}{\sin \frac{5}{2}\pi - \cos^2\left(\frac{5}{2}\pi - \theta\right)}$

■ 다음 식의 값을 구하여라.

61. $\frac{\cos(\pi - \theta)\tan(\pi - \theta)}{\cos\left(\frac{\pi}{2} - \theta\right)}$

62. $\sin\left(\frac{5\pi}{2} - \theta\right) + \cos(-\pi + \theta) + \sin\left(\frac{3}{2}\pi + \theta\right) + \cos(-\theta)$

63. $\sin\left(\frac{\pi}{2} - \theta\right) - \sin(\pi - \theta) + \cos(\pi + \theta) + \cos\left(\frac{3\pi}{2} + \theta\right)$

64. $\sin^2\left(\frac{\pi}{2} + \theta\right) + \sin^2(\pi + \theta)$

$$65. \frac{\sin(\pi+\theta)\tan^2(\pi-\theta)}{\cos\left(\frac{3}{2}\pi+\theta\right)} - \frac{\sin\left(\frac{3}{2}\pi-\theta\right)}{\sin\left(\frac{\pi}{2}+\theta\right)\cos^2\theta}$$

$$66. \frac{\sin\theta\sin\left(\frac{\pi}{2}+\theta\right)}{\tan\left(\frac{\pi}{2}+\theta\right)} + \cos\theta\tan\left(\frac{\pi}{2}-\theta\right)\cos\left(\frac{\pi}{2}+\theta\right)$$

$$67. \sin\left(\frac{\pi}{2}-\frac{\pi}{3}\right) + \sin\left(\pi+\frac{\pi}{6}\right) - \cos\left(\frac{\pi}{2}+\frac{\pi}{3}\right)$$

▣ 다음 식의 값을 구하여라.

$$68. \tan 1^\circ \tan 3^\circ \tan 5^\circ \cdots \tan 87^\circ \tan 89^\circ$$

$$69. \sin^2 5^\circ + \sin^2 10^\circ + \sin^2 15^\circ + \cdots + \sin^2 90^\circ$$

$$70. \tan 2^\circ \times \tan 4^\circ \times \cdots \times \tan 86^\circ \times \tan 88^\circ$$

$$71. \cos^2 0^\circ + \cos^2 10^\circ + \cos^2 20^\circ + \cdots + \cos^2 90^\circ$$

$$72. \cos^2 0^\circ + \cos^2 1^\circ + \cos^2 2^\circ + \cdots + \cos^2 360^\circ$$

$$73. \tan 1^\circ \tan 2^\circ \cdots \tan 8^\circ \tan 89^\circ$$

$$74. \cos^2 10^\circ + \cos^2 20^\circ + \cdots + \cos^2 70^\circ + \cos^2 80^\circ$$

$$75. \sin^2 1^\circ + \sin^2 2^\circ + \cdots + \sin^2 89^\circ + \sin^2 90^\circ$$

$$76. \sin^2 10^\circ + \sin^2 20^\circ + \sin^2 30^\circ + \cdots + \sin^2 80^\circ$$

$$77. \cos^2 1^\circ + \cos^2 2^\circ + \cdots + \cos^2 88^\circ + \cos^2 89^\circ$$

$$78. \sin^2 10^\circ + \sin^2 20^\circ + \cdots + \sin^2 80^\circ + \sin^2 90^\circ$$



정답 및 해설

$$1) \sin \frac{5}{4}\pi = -\frac{\sqrt{2}}{2}, \cos \frac{5}{4}\pi = -\frac{\sqrt{2}}{2}, \tan \frac{5}{4}\pi = 1$$

$$\Rightarrow \sin \frac{5}{4}\pi = \sin \left(\pi + \frac{\pi}{4} \right) = -\sin \frac{\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$\cos \frac{5}{4}\pi = \cos \left(\pi + \frac{\pi}{4} \right) = -\cos \frac{\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$\tan \frac{5}{4}\pi = \tan \left(\pi + \frac{\pi}{4} \right) = \tan \frac{\pi}{4} = 1$$

$$2) \sin \frac{7}{6}\pi = -\frac{1}{2}, \cos \frac{7}{6}\pi = -\frac{\sqrt{3}}{2}, \tan \frac{7}{6}\pi = \frac{\sqrt{3}}{3}$$

$$\Rightarrow \sin \frac{7}{6}\pi = \sin \left(\pi + \frac{\pi}{6} \right) = -\sin \frac{\pi}{6} = -\frac{1}{2}$$

$$\cos \frac{7}{6}\pi = \cos \left(\pi + \frac{\pi}{6} \right) = -\cos \frac{\pi}{6} = -\frac{\sqrt{3}}{2}$$

$$\tan \frac{7}{6}\pi = \tan \left(\pi + \frac{\pi}{6} \right) = \tan \frac{\pi}{6} = \frac{\sqrt{3}}{3}$$

$$3) \sin \frac{2}{3}\pi = \frac{\sqrt{3}}{2}, \cos \frac{2}{3}\pi = -\frac{1}{2}, \tan \frac{2}{3}\pi = -\sqrt{3}$$

$$\Rightarrow \sin \frac{2}{3}\pi = \sin \left(\pi - \frac{\pi}{3} \right) = \sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}$$

$$\cos \frac{2}{3}\pi = \cos \left(\pi - \frac{\pi}{3} \right) = -\cos \frac{\pi}{3} = -\frac{1}{2}$$

$$\tan \frac{2}{3}\pi = \tan \left(\pi - \frac{\pi}{3} \right) = -\tan \frac{\pi}{3} = -\sqrt{3}$$

$$4) \sin \left(-\frac{\pi}{3} \right) = -\frac{\sqrt{3}}{2}, \cos \left(-\frac{\pi}{3} \right) = \frac{1}{2},$$

$$\tan \left(-\frac{\pi}{3} \right) = -\sqrt{3}$$

$$\Rightarrow \sin \left(-\frac{\pi}{3} \right) = -\sin \frac{\pi}{3} = -\frac{\sqrt{3}}{2}$$

$$\cos \left(-\frac{\pi}{3} \right) = \cos \frac{\pi}{3} = \frac{1}{2}$$

$$\tan \left(-\frac{\pi}{3} \right) = -\tan \frac{\pi}{3} = -\sqrt{3}$$

$$5) \sin \left(-\frac{\pi}{4} \right) = -\frac{\sqrt{2}}{2}, \cos \left(-\frac{\pi}{4} \right) = \frac{\sqrt{2}}{2},$$

$$\tan \left(-\frac{\pi}{4} \right) = -1$$

$$\Rightarrow \sin \left(-\frac{\pi}{4} \right) = -\sin \frac{\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$\cos \left(-\frac{\pi}{4} \right) = \cos \frac{\pi}{4} = \frac{\sqrt{2}}{2}$$

$$\tan \left(-\frac{\pi}{4} \right) = -\tan \frac{\pi}{4} = -1$$

$$6) -\sqrt{3}$$

$$\Rightarrow \tan \left(\frac{\pi}{2} + \frac{\pi}{6} \right) = -\frac{1}{\tan \frac{\pi}{6}} = -\sqrt{3}$$

$$7) \sqrt{3}$$

$$\Rightarrow \tan \left(\frac{\pi}{2} - \frac{\pi}{6} \right) = \frac{1}{\tan \frac{\pi}{6}} = \sqrt{3}$$

$$8) \frac{1}{2}$$

$$\Rightarrow \sin \left(\frac{\pi}{2} + \frac{\pi}{3} \right) = \cos \frac{\pi}{3} = \frac{1}{2}$$

$$9) -\frac{\sqrt{2}}{2}$$

$$\Rightarrow \sin \frac{5}{4}\pi = \sin \left(\pi + \frac{\pi}{4} \right) = -\sin \frac{\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$10) \sqrt{3}$$

$$\Rightarrow \tan \frac{4}{3}\pi = \tan \left(\pi + \frac{\pi}{3} \right) = \tan \frac{\pi}{3} = \sqrt{3}$$

$$11) -\frac{\sqrt{3}}{2}$$

$$\Rightarrow \cos \frac{7}{6}\pi = \cos \left(\pi + \frac{\pi}{6} \right) = -\cos \frac{\pi}{6} = -\frac{\sqrt{3}}{2}$$

$$12) \sqrt{3}$$

$$\Rightarrow \tan \frac{19}{3}\pi = \tan \left(6\pi + \frac{\pi}{3} \right) = \tan \frac{\pi}{3} = \sqrt{3}$$

$$13) -1$$

$$\Rightarrow \tan \left(-\frac{9}{4}\pi \right) = -\tan \frac{9}{4}\pi = -\tan \left(2\pi + \frac{\pi}{4} \right) \\ = -\tan \frac{\pi}{4} = -1$$

$$14) \frac{\sqrt{2}}{2}$$

$$\Rightarrow \cos \frac{9}{4}\pi = \cos \left(2\pi + \frac{\pi}{4} \right) = \cos \frac{\pi}{4} = \frac{\sqrt{2}}{2}$$

$$15) -\frac{\sqrt{2}}{2}$$

$$\Rightarrow \cos \frac{5}{4}\pi = \cos \left(\pi + \frac{\pi}{4} \right) = -\cos \frac{\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$16) \frac{1}{2}$$

$$\Rightarrow \sin \frac{5}{6}\pi = \sin \left(\pi - \frac{\pi}{6} \right) = \sin \frac{\pi}{6} = \frac{1}{2}$$

$$17) \sqrt{3}$$

$$\Rightarrow \tan \frac{7}{3}\pi = \tan \left(2\pi + \frac{\pi}{3} \right) = \tan \frac{\pi}{3} = \sqrt{3}$$

$$18) \frac{\sqrt{3}}{2}$$

$$\Rightarrow \cos \frac{25}{6}\pi = \cos \left(4\pi + \frac{\pi}{6}\right) = \cos \frac{\pi}{6} = \frac{\sqrt{3}}{2}$$

$$19) -\frac{\sqrt{3}}{3}$$

$$\Rightarrow \tan \frac{5}{6}\pi = \tan \left(\pi - \frac{\pi}{6}\right) = -\tan \frac{\pi}{6} = -\frac{\sqrt{3}}{3}$$

$$20) -\frac{\sqrt{2}}{2}$$

$$\Rightarrow \cos \frac{3}{4}\pi = \cos \left(\pi - \frac{\pi}{4}\right) = -\cos \frac{\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$21) \frac{\sqrt{3}}{2}$$

$$\Rightarrow \sin \frac{2}{3}\pi = \sin \left(\pi - \frac{\pi}{3}\right) = \sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}$$

$$22) \frac{1}{2}$$

$$\Rightarrow \sin \frac{13}{6}\pi = \sin \left(2\pi + \frac{\pi}{6}\right) = \sin \frac{\pi}{6} = \frac{1}{2}$$

$$23) -\frac{1}{2}$$

$$\begin{aligned} \Rightarrow \sin \left(-\frac{13}{6}\pi\right) &= -\sin \frac{13}{6}\pi = -\sin \left(2\pi + \frac{\pi}{6}\right) \\ &= -\sin \frac{\pi}{6} = -\frac{1}{2} \end{aligned}$$

$$24) -\frac{\sqrt{2}}{2}$$

$$\Rightarrow \sin \left(-\frac{\pi}{4}\right) = -\sin \frac{\pi}{4} = -\frac{\sqrt{2}}{2}$$

$$25) \frac{\sqrt{2}}{2}$$

$$\Rightarrow \cos \left(-\frac{\pi}{4}\right) = \cos \frac{\pi}{4} = \frac{\sqrt{2}}{2}$$

$$26) -\frac{1}{2}$$

$$\Rightarrow \sin \left(-\frac{\pi}{6}\right) = -\sin \frac{\pi}{6} = -\frac{1}{2}$$

$$27) -\frac{\sqrt{3}}{3}$$

$$\begin{aligned} \Rightarrow \tan \frac{11}{6}\pi &= \tan \left(2\pi - \frac{\pi}{6}\right) = \tan \left(-\frac{\pi}{6}\right) \\ &= -\tan \frac{\pi}{6} = -\frac{\sqrt{3}}{3} \end{aligned}$$

$$28) \frac{\sqrt{3}}{2}$$

$$\Rightarrow \sin 120^\circ = \sin (90^\circ + 30^\circ) = \cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$29) -\frac{\sqrt{3}}{3}$$

$$\Rightarrow \tan 150^\circ = \tan (90^\circ + 60^\circ) = -\frac{1}{\tan 60^\circ} = -\frac{\sqrt{3}}{3}$$

$$30) -\frac{\sqrt{2}}{2}$$

$$\Rightarrow \cos 135^\circ = \cos (90^\circ + 45^\circ) = -\sin 45^\circ = -\frac{\sqrt{2}}{2}$$

$$31) -\frac{1}{2}$$

$$\Rightarrow \sin 210^\circ = \sin (180^\circ + 30^\circ) = -\sin 30^\circ = -\frac{1}{2}$$

$$32) \frac{\sqrt{3}}{3}$$

$$\Rightarrow \tan 390^\circ = \tan (360^\circ + 30^\circ) = \tan 30^\circ = \frac{\sqrt{3}}{3}$$

$$33) \frac{\sqrt{3}}{3}$$

$$\Rightarrow \tan 210^\circ = \tan (180^\circ + 30^\circ) = \tan 30^\circ = \frac{\sqrt{3}}{3}$$

$$34) \frac{\sqrt{3}}{2}$$

$$\begin{aligned} \Rightarrow \cos 330^\circ &= \cos (360^\circ - 30^\circ) = \cos (-30^\circ) \\ &= \cos 30^\circ = \frac{\sqrt{3}}{2} \end{aligned}$$

$$35) \frac{\sqrt{3}}{2}$$

$$\Rightarrow \sin 780^\circ = \sin (360^\circ \times 2 + 60^\circ) = \sin 60^\circ = \frac{\sqrt{3}}{2}$$

$$36) \frac{\sqrt{3}}{2}$$

$$\Rightarrow \cos 750^\circ = \cos (2 \times 360^\circ + 30^\circ) = \cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$37) 1$$

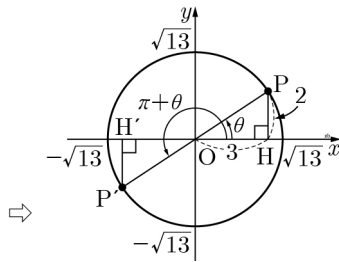
$$\Rightarrow \sin 450^\circ = \sin (360^\circ + 90^\circ) = \sin 90^\circ = 1$$

$$38) -\frac{1}{2}$$

$$\Rightarrow \cos 240^\circ = \cos (180^\circ + 60^\circ) = -\cos 60^\circ = -\frac{1}{2}$$

$$39) \sin (\pi + \theta) = -\frac{2\sqrt{13}}{13}, \cos (\pi + \theta) = -\frac{3\sqrt{13}}{13}$$

$$\tan (\pi + \theta) = \frac{2}{3}$$



$$\Rightarrow \overline{OP} = \sqrt{3^2 + 2^2} = \sqrt{13} \text{ 이므로 } \sin(\pi + \theta) = -\frac{2\sqrt{13}}{\sqrt{13}}$$

$$\cos(\pi + \theta) = -\frac{3\sqrt{13}}{13}, \tan(\pi + \theta) = \frac{2}{3}$$

$$40) \sin(\pi + \theta) = -\frac{3}{5}, \cos(\pi + \theta) = -\frac{4}{5},$$

$$\tan(\pi + \theta) = \frac{3}{4}$$

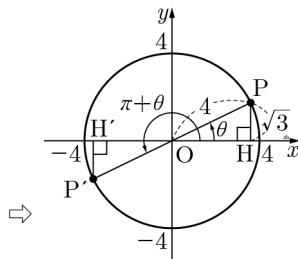
$$\Rightarrow \cos\theta = \frac{4}{5} \text{ 일 때 } \sin\theta = \frac{3}{5}, \tan\theta = \frac{3}{4} \text{ 이므로}$$

$$\sin(\pi + \theta) = -\frac{3}{5}, \cos(\pi + \theta) = -\frac{4}{5}$$

$$\tan(\pi + \theta) = \frac{3}{4}$$

$$41) \sin(\pi + \theta) = -\frac{\sqrt{3}}{4}, \cos(\pi + \theta) = -\frac{\sqrt{13}}{4}$$

$$\tan(\pi + \theta) = \frac{\sqrt{3}}{\sqrt{13}} = \frac{\sqrt{39}}{13}$$



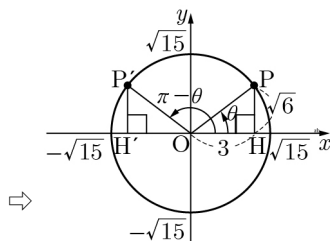
$$\Rightarrow \overline{OH} = \sqrt{4^2 - \sqrt{3}^2} = \sqrt{13} \text{ 이므로}$$

$$\sin(\pi + \theta) = -\frac{\sqrt{3}}{4}, \cos(\pi + \theta) = -\frac{\sqrt{13}}{4}$$

$$\tan(\pi + \theta) = \frac{\sqrt{3}}{\sqrt{13}} = \frac{\sqrt{39}}{13}$$

$$42) \sin(\pi - \theta) = \frac{\sqrt{10}}{5}, \cos(\pi - \theta) = -\frac{\sqrt{15}}{5},$$

$$\tan(\pi - \theta) = -\frac{\sqrt{6}}{3}$$



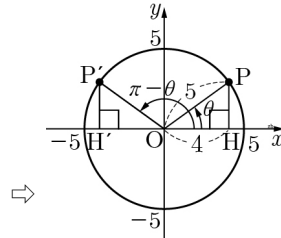
$$\Rightarrow \overline{OP} = \sqrt{3^2 + \sqrt{6}^2} = \sqrt{15} \text{ 이므로}$$

$$\sin(\pi - \theta) = \frac{\sqrt{10}}{5}, \cos(\pi - \theta) = -\frac{\sqrt{15}}{5}$$

$$\tan(\pi - \theta) = -\frac{\sqrt{6}}{3}$$

$$43) \sin(\pi - \theta) = \frac{3}{5}, \cos(\pi - \theta) = -\frac{4}{5},$$

$$\tan(\pi - \theta) = -\frac{3}{4}$$



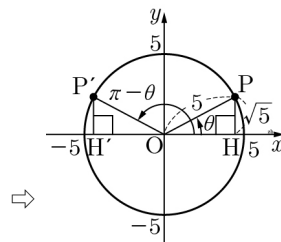
$$\Rightarrow \overline{HP} = \sqrt{5^2 - 4^2} = 3 \text{ 이므로}$$

$$\sin(\pi - \theta) = \frac{3}{5}, \cos(\pi - \theta) = -\frac{4}{5}$$

$$\tan(\pi - \theta) = -\frac{3}{4}$$

$$44) \sin(\pi - \theta) = \frac{\sqrt{5}}{5}, \cos(\pi - \theta) = -\frac{2\sqrt{5}}{5},$$

$$\tan(\pi - \theta) = -\frac{1}{2}$$



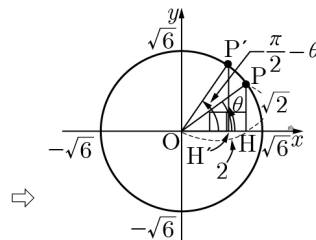
$$\Rightarrow \overline{OH} = \sqrt{5^2 - \sqrt{5}^2} = 2\sqrt{5} \text{ 이므로}$$

$$\sin(\pi - \theta) = \frac{\sqrt{5}}{5}, \cos(\pi - \theta) = -\frac{2\sqrt{5}}{5}$$

$$\tan(\pi - \theta) = -\frac{1}{2}$$

$$45) \sin\left(\frac{\pi}{2} - \theta\right) = \frac{\sqrt{6}}{3}, \cos\left(\frac{\pi}{2} - \theta\right) = \frac{\sqrt{3}}{3}$$

$$\tan\left(\frac{\pi}{2} - \theta\right) = \sqrt{2}$$



$$\Rightarrow \overline{OP} = \sqrt{2^2 + \sqrt{2}^2} = \sqrt{6} \text{ 이므로}$$

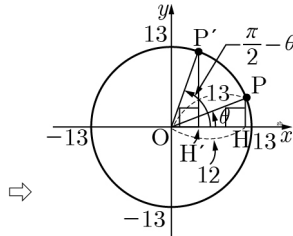
$$\sin\left(\frac{\pi}{2} - \theta\right) = \frac{\sqrt{6}}{3}$$

$$\cos\left(\frac{\pi}{2}-\theta\right)=\frac{\sqrt{3}}{3}$$

$$\tan\left(\frac{\pi}{2}-\theta\right)=\sqrt{2}$$

$$46) \sin\left(\frac{\pi}{2}-\theta\right)=\frac{12}{13}, \cos\left(\frac{\pi}{2}-\theta\right)=\frac{5}{13}$$

$$\tan\left(\frac{\pi}{2}-\theta\right)=\frac{12}{5}$$



⇒

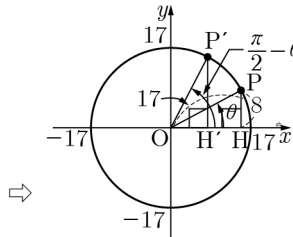
$$\overline{HP} = \sqrt{13^2 - 12^2} = 5 \text{ 이므로}$$

$$\sin\left(\frac{\pi}{2}-\theta\right)=\frac{12}{13}, \cos\left(\frac{\pi}{2}-\theta\right)=\frac{5}{13}$$

$$\tan\left(\frac{\pi}{2}-\theta\right)=\frac{12}{5}$$

$$47) \sin\left(\frac{\pi}{2}-\theta\right)=\frac{15}{17}, \cos\left(\frac{\pi}{2}-\theta\right)=\frac{8}{17}$$

$$\tan\left(\frac{\pi}{2}-\theta\right)=\frac{15}{8}$$



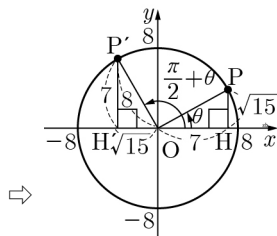
⇒

$$\overline{OH} = \sqrt{17^2 - 8^2} = 15 \text{ 이므로 } \sin\left(\frac{\pi}{2}-\theta\right)=\frac{15}{17}$$

$$\cos\left(\frac{\pi}{2}-\theta\right)=\frac{8}{17}, \tan\left(\frac{\pi}{2}-\theta\right)=\frac{15}{8}$$

$$48) \sin\left(\frac{\pi}{2}+\theta\right)=\frac{7}{8}, \cos\left(\frac{\pi}{2}+\theta\right)=-\frac{\sqrt{15}}{8}$$

$$\tan\left(\frac{\pi}{2}+\theta\right)=-\frac{7\sqrt{15}}{15}$$



⇒

$$\overline{OP} = \sqrt{7^2 + \sqrt{15}^2} = 8 \text{ 이므로}$$

$$\sin\left(\frac{\pi}{2}+\theta\right)=\frac{7}{8}, \cos\left(\frac{\pi}{2}+\theta\right)=-\frac{\sqrt{15}}{8}$$

$$\tan\left(\frac{\pi}{2}+\theta\right)=-\frac{7\sqrt{15}}{15}$$

$$49) \sin\left(\frac{\pi}{2}+\theta\right)=\frac{4}{5}, \cos\left(\frac{\pi}{2}+\theta\right)=-\frac{3}{5},$$

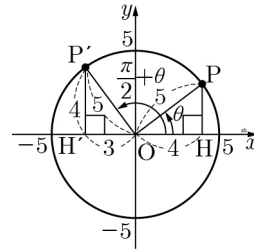
$$\tan\left(\frac{\pi}{2}+\theta\right)=-\frac{4}{3}$$

⇒ △POH와 △OP'H'이 합동이고,

$$\overline{HP} = \sqrt{5^2 - 4^2} = 3 \text{ 이므로}$$

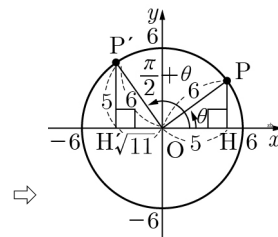
$$\sin\left(\frac{\pi}{2}+\theta\right)=\frac{4}{5}, \cos\left(\frac{\pi}{2}+\theta\right)=-\frac{3}{5}$$

$$\tan\left(\frac{\pi}{2}+\theta\right)=-\frac{4}{3}$$



$$50) \sin\left(\frac{\pi}{2}+\theta\right)=\frac{5}{6}, \cos\left(\frac{\pi}{2}+\theta\right)=-\frac{\sqrt{11}}{6}$$

$$\tan\left(\frac{\pi}{2}+\theta\right)=-\frac{5\sqrt{11}}{11}$$



⇒

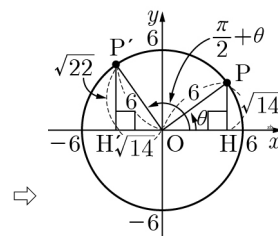
$$\overline{HP} = \sqrt{6^2 - 5^2} = \sqrt{11} \text{ 이므로}$$

$$\sin\left(\frac{\pi}{2}+\theta\right)=\frac{5}{6}, \cos\left(\frac{\pi}{2}+\theta\right)=-\frac{\sqrt{11}}{6}$$

$$\tan\left(\frac{\pi}{2}+\theta\right)=-\frac{5\sqrt{11}}{11}$$

$$51) \sin\left(\frac{\pi}{2}+\theta\right)=\frac{\sqrt{22}}{6}, \cos\left(\frac{\pi}{2}+\theta\right)=-\frac{\sqrt{14}}{6}$$

$$\tan\left(\frac{\pi}{2}+\theta\right)=-\frac{\sqrt{77}}{7}$$



⇒

$$\overline{OH} = \sqrt{6^2 - \sqrt{14}^2} = \sqrt{22} \text{ 이므로}$$

$$\sin\left(\frac{\pi}{2}+\theta\right)=\frac{\sqrt{22}}{6}, \cos\left(\frac{\pi}{2}+\theta\right)=-\frac{\sqrt{14}}{6}$$

$$\tan\left(\frac{\pi}{2}+\theta\right)=-\frac{\sqrt{77}}{7}$$

52) 0

$$\Rightarrow \sin \frac{5}{6}\pi = \frac{1}{2}, \cos \frac{4}{3}\pi = -\frac{1}{2} \text{ 이므로 } \frac{1}{2} - \frac{1}{2} = 0 \text{ 이다.}$$

53) $\frac{\sqrt{3}}{2}$

$$\Rightarrow \cos \frac{7}{6}\pi = -\frac{\sqrt{3}}{2}, \tan \frac{2}{3}\pi = -\sqrt{3}$$

$$\cos \frac{7\pi}{6} - \tan \frac{2\pi}{3} = -\frac{\sqrt{3}}{2} + \sqrt{3} = \frac{\sqrt{3}}{2}$$

54) $-\frac{3}{2}$

$$\Rightarrow \sin\left(\frac{3}{2}\pi - \frac{\pi}{3}\right) = \sin\left\{2\pi - \left(\frac{\pi}{2} + \frac{\pi}{3}\right)\right\}$$

$$= -\sin\left(\frac{\pi}{2} + \frac{\pi}{3}\right) = -\cos\left(-\frac{\pi}{3}\right) = -\frac{1}{2}$$

$$\tan \frac{7}{4}\pi = \tan \frac{3}{4}\pi = -1$$

$$\therefore \sin\left(\frac{3}{2}\pi - \frac{\pi}{3}\right) + \tan \frac{7}{4}\pi = -\frac{1}{2} - 1 = -\frac{3}{2}$$

55) -2

56) 0

$$\Rightarrow \sin \frac{2}{3}\pi = \sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}$$

$$\cos\left(-\frac{13}{6}\pi\right) = \cos\left(-\frac{\pi}{6}\right) = \cos \frac{\pi}{6} = \frac{\sqrt{3}}{2}$$

$$\tan \frac{8}{3}\pi = \tan\left(-\frac{\pi}{3}\right) = -\tan \frac{\pi}{3} = -\sqrt{3}$$

$$\frac{\sqrt{3}}{2} + \frac{\sqrt{3}}{2} - \sqrt{3} = 0$$

57) $\frac{\sqrt{2}}{2}$

$$\Rightarrow \frac{1}{\sin \frac{\pi}{3}} = \frac{1}{\frac{\sqrt{3}}{2}} = \frac{2}{\sqrt{3}} = \frac{2\sqrt{3}}{3}$$

$$\cos \frac{3}{4}\pi = -\frac{\sqrt{2}}{2}$$

$$\tan\left(-\frac{7}{6}\pi\right) = \tan\left(-\frac{\pi}{6}\right) = -\tan \frac{\pi}{6} = -\left(\frac{1}{\sqrt{3}}\right) = -\frac{\sqrt{3}}{3}$$

$$(\text{주어진 값}) = \frac{2\sqrt{3}}{3} + \frac{\sqrt{2}}{2} - \frac{2\sqrt{3}}{3} = \frac{\sqrt{2}}{2}$$

58) $-\frac{5}{12}$ 59) $\frac{1}{\tan \theta}$

$$\Rightarrow \sin\left(\frac{3}{2}\pi - \theta\right) = -\cos \theta, \cos\left(\frac{\pi}{2} + \theta\right) = -\sin \theta$$

$$\sin(\pi + \theta) = -\sin \theta, \tan(\pi - \theta) = -\tan \theta$$

$$\cos\left(\frac{3}{2}\pi + \theta\right) = \sin \theta$$

따라서 주어진 값은

$$\frac{-\cos \theta}{-\sin \theta \cos^2 \theta} - \frac{-\sin \theta (-\tan \theta)}{\sin \theta} = \frac{\cos \theta}{\sin \theta \cos^2 \theta} - \frac{\sin \theta \tan \theta}{\sin \theta}$$

$$= \frac{1}{\sin \theta \cos \theta} - \tan \theta = \frac{1}{\sin \theta \cos \theta} - \frac{\sin \theta}{\cos \theta} = \frac{1 - \sin^2 \theta}{\sin \theta \cos \theta}$$

$$= \frac{\cos^2 \theta}{\sin \theta \cos \theta} = \frac{\cos \theta}{\sin \theta} = \frac{1}{\tan \theta}$$

60) $-\tan^2 \theta$

$$\Rightarrow \cos(\pi + \theta) = -\cos \theta, \sin\left(\frac{3}{2}\pi + \theta\right) = -\cos \theta$$

$$\tan \frac{19}{4}\pi = \tan\left(4\pi + \frac{3}{4}\pi\right) = \tan \frac{3}{4}\pi = -1$$

$$\sin \frac{5}{2}\pi = \sin\left(2\pi + \frac{\pi}{2}\right) = \sin \frac{\pi}{2} = 1$$

$$\cos\left(\frac{5}{2}\pi - \theta\right) = \cos\left(\frac{\pi}{2} - \theta\right) = \sin \theta$$

$$(\text{주어진 식}) = \frac{-\cos \theta}{-\cos \theta} + \frac{(-1)}{1 - \sin^2 \theta} = 1 - \frac{1}{\cos^2 \theta}$$

$$= \frac{\cos^2 \theta - 1}{\cos^2 \theta} = -\frac{\sin^2 \theta}{\cos^2 \theta} = -\tan^2 \theta$$

61) 1

$$\Rightarrow \frac{\cos(\pi - \theta) \tan(\pi - \theta)}{\cos\left(\frac{\pi}{2} - \theta\right)} = \frac{-\cos \theta \times (-\tan \theta)}{\sin \theta}$$

$$= \cos \theta \times \frac{\sin \theta}{\cos \theta} \times \frac{1}{\sin \theta} = 1$$

62) 0

$$\Rightarrow \sin\left(\frac{5\pi}{2} - \theta\right) + \cos(-\pi + \theta) + \sin\left(\frac{3}{2}\pi + \theta\right) + \cos(-\theta)$$

$$= \cos \theta - \cos \theta - \cos \theta + \cos \theta = 0$$

63) 0

$$\Rightarrow \sin\left(\frac{\pi}{2} - \theta\right) - \sin(\pi - \theta) + \cos(\pi + \theta) + \cos\left(\frac{3}{2}\pi + \theta\right)$$

$$= \cos \theta - \sin \theta - \cos \theta + \sin \theta = 0$$

64) 1

$$\Rightarrow \sin\left(\frac{\pi}{2} + \theta\right) = \cos \theta$$

$$\sin(\pi + \theta) = -\sin \theta$$

$$\therefore \sin^2\left(\frac{\pi}{2} + \theta\right) + \sin^2(\pi + \theta) = \cos^2 \theta + \sin^2 \theta = 1$$

65) 1

$$\Rightarrow \frac{\sin(\pi + \theta) \tan^2(\pi - \theta)}{\cos\left(\frac{3}{2}\pi + \theta\right)} - \frac{\sin\left(\frac{3}{2}\pi - \theta\right)}{\sin\left(\frac{\pi}{2} + \theta\right) \cos^2 \theta}$$

$$= \frac{-\sin \theta \tan^2 \theta}{\sin \theta} - \frac{-\cos \theta}{\cos^3 \theta} = -\tan^2 \theta + \frac{1}{\cos^2 \theta} = 1$$

66) -1

$$\begin{aligned} \Rightarrow & \frac{\sin \theta \sin \left(\frac{\pi}{2} + \theta\right)}{\tan \left(\frac{\pi}{2} + \theta\right)} + \cos \theta \tan \left(\frac{\pi}{2} - \theta\right) \cos \left(\frac{\pi}{2} + \theta\right) \\ &= \sin \theta \times \cos \theta \times (-\tan \theta) + \cos \theta \times \frac{1}{\tan \theta} \times (-\sin \theta) \\ &= \sin \theta \times \cos \theta \times \left(-\frac{\sin \theta}{\cos \theta}\right) + \cos \theta \times \frac{\cos \theta}{\sin \theta} \times (-\sin \theta) \\ &= -\sin^2 \theta - \cos^2 \theta = -(\sin^2 \theta + \cos^2 \theta) = -1 \end{aligned}$$

67) $\frac{\sqrt{3}}{2}$

$$\begin{aligned} \Rightarrow & \sin \left(\frac{\pi}{2} - \frac{\pi}{3}\right) + \sin \left(\pi + \frac{\pi}{6}\right) - \cos \left(\frac{\pi}{2} + \frac{\pi}{3}\right) \\ &= \cos \frac{\pi}{3} - \sin \frac{\pi}{6} + \sin \frac{\pi}{3} \\ &= \frac{1}{2} - \frac{1}{2} + \frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{2} \end{aligned}$$

68) 1

$$\begin{aligned} \Rightarrow & 1^\circ + 89^\circ = 3^\circ + 87^\circ = \dots = 43^\circ + 47^\circ = 90^\circ \text{에서} \\ & \tan 1^\circ = \tan (90^\circ - 89^\circ) = \frac{1}{\tan 89^\circ}, \\ & \tan 3^\circ = \tan (90^\circ - 87^\circ) = \frac{1}{\tan 87^\circ}, \\ & \vdots \\ & \tan 43^\circ = \tan (90^\circ - 47^\circ) = \frac{1}{\tan 47^\circ} \text{이므로} \\ & \tan 1^\circ \tan 89^\circ = \frac{1}{\tan 89^\circ} \cdot \tan 89^\circ = 1, \\ & \tan 3^\circ \tan 87^\circ = \frac{1}{\tan 87^\circ} \cdot \tan 87^\circ = 1, \\ & \vdots \\ & \tan 43^\circ \tan 47^\circ = \frac{1}{\tan 47^\circ} \cdot \tan 47^\circ = 1 \\ & \therefore \tan 1^\circ \tan 3^\circ \dots \tan 87^\circ \tan 89^\circ \\ &= 1 \cdot 1 \cdot \dots \cdot 1 \cdot \tan 45^\circ = 1 \end{aligned}$$

69) $\frac{19}{2}$

$$\begin{aligned} \Rightarrow & \sin (90^\circ - \theta) = \cos \theta \text{이므로} \\ & \sin^2 5^\circ + \sin^2 10^\circ + \sin^2 15^\circ + \dots + \sin^2 90^\circ \\ &= (\sin^2 5^\circ + \sin^2 85^\circ) + (\sin^2 10^\circ + \sin^2 80^\circ) + \\ & \dots + (\sin^2 40^\circ + \sin^2 50^\circ) + \sin^2 45^\circ + \sin^2 90^\circ \\ &= (\sin^2 5^\circ + \cos^2 5^\circ) + (\sin^2 10^\circ + \cos^2 10^\circ) + \\ & \dots + (\sin^2 40^\circ + \cos^2 40^\circ) + \sin^2 45^\circ + \sin^2 90^\circ \\ &= 1 \times 8 + \left(\frac{\sqrt{2}}{2}\right)^2 + 1 = \frac{19}{2} \end{aligned}$$

70) 1

$$\begin{aligned} \Rightarrow & \tan (90^\circ - \theta) = \frac{1}{\tan \theta} \text{이므로} \\ & \tan \theta \times \tan (90^\circ - \theta) = 1 \\ & \therefore \tan 2^\circ \times \tan 4^\circ \times \dots \times \tan 86^\circ \times \tan 88^\circ \end{aligned}$$

$$\begin{aligned} &= (\tan 2^\circ \times \tan 88^\circ) \times (\tan 4^\circ \times \tan 86^\circ) \times \\ & \dots \times (\tan 44^\circ \times \tan 46^\circ) \\ &= \left(\tan 2^\circ \times \frac{1}{\tan 2^\circ}\right) \times \left(\tan 4^\circ \times \frac{1}{\tan 4^\circ}\right) \times \\ & \dots \times \left(\tan 44^\circ \times \frac{1}{\tan 44^\circ}\right) \\ &= 1 \end{aligned}$$

71) 5

$$\begin{aligned} \Rightarrow & \cos (90^\circ - \theta) = \sin \theta \text{이므로} \\ & \cos^2 \theta + \cos^2 (90^\circ - \theta) = \cos^2 \theta + \sin^2 \theta = 1 \\ & \therefore \cos^2 0^\circ + \cos^2 10^\circ + \cos^2 20^\circ + \dots + \cos^2 90^\circ \\ &= (\cos^2 0^\circ + \cos^2 90^\circ) + (\cos^2 10^\circ + \cos^2 80^\circ) + \\ & \dots + (\cos^2 40^\circ + \cos^2 50^\circ) \\ &= (\cos^2 0^\circ + \sin^2 0^\circ) + (\cos^2 10^\circ + \sin^2 10^\circ) + \\ & \dots + (\cos^2 40^\circ + \sin^2 40^\circ) \\ &= 1 + 1 + 1 + 1 + 1 = 5 \end{aligned}$$

72) 181

$$\begin{aligned} \Rightarrow & \cos^2 (2\pi - \theta) = \cos^2 \theta, \cos^2 (\pi - \theta) = \cos^2 \theta \\ & , \cos^2 \left(\frac{\pi}{2} - \theta\right) = \sin^2 \theta \\ & \text{를 이용하여 주어진 식을 정리하면} \\ & 2(\cos^2 1^\circ + \dots + \cos^2 179^\circ) + 2\cos^2 0^\circ + \cos^2 180^\circ \\ &= 4(\cos^2 1^\circ + \cos^2 2^\circ + \dots + \cos^2 88^\circ + \cos^2 89^\circ) + 3 \\ &= 4 \times 44 + 4\cos^2 45^\circ + 3 = 181 \\ & (\because \cos^2 \alpha + \sin^2 \alpha = 1) \end{aligned}$$

73) 1

$$\begin{aligned} \Rightarrow & \tan 1^\circ \tan 2^\circ \dots \tan 88^\circ \tan 89^\circ \text{에서} \\ & 1^\circ + 89^\circ = 2^\circ + 88^\circ = \dots = 44^\circ + 46^\circ = 90^\circ \text{이므로} \\ & \tan 1^\circ = \tan (90^\circ - 89^\circ) = \frac{1}{\tan 89^\circ}, \\ & \tan 2^\circ = \tan (90^\circ - 88^\circ) = \frac{1}{\tan 88^\circ}, \\ & \vdots \\ & \tan 44^\circ = \tan (90^\circ - 46^\circ) = \frac{1}{\tan 46^\circ} \\ & \text{이때, } \tan 1^\circ \tan 89^\circ = \frac{1}{\tan 89^\circ} \tan 89^\circ = 1, \\ & \tan 2^\circ \tan 88^\circ = \frac{1}{\tan 88^\circ} \tan 88^\circ = 1, \\ & \vdots \\ & \tan 44^\circ \tan 46^\circ = \frac{1}{\tan 46^\circ} \tan 46^\circ = 1 \\ & \text{이므로 주어진 식의 값은} \\ & \tan 1^\circ \tan 2^\circ \dots \tan 88^\circ \tan 89^\circ \\ &= 1 \cdot 1 \cdot \dots \cdot 1 \cdot \tan 45^\circ = 1 \end{aligned}$$

74) 4

$$\begin{aligned} \Rightarrow & \cos^2 10^\circ + \cos^2 20^\circ + \dots + \cos^2 70^\circ + \cos^2 80^\circ \text{에서} \\ & 10^\circ + 80^\circ = 20^\circ + 70^\circ = \dots = 40^\circ + 50^\circ = 90^\circ \text{이} \end{aligned}$$

므로

$$\cos 10^\circ = \cos (90^\circ - 80^\circ) = \sin 80^\circ,$$

$$\cos 20^\circ = \cos (90^\circ - 70^\circ) = \sin 70^\circ,$$

$$\cos 30^\circ = \cos (90^\circ - 60^\circ) = \sin 60^\circ$$

$$\cos 40^\circ = \cos (90^\circ - 50^\circ) = \sin 50^\circ$$

이때,

$$\cos^2 10^\circ + \cos^2 80^\circ = \sin^2 80^\circ + \cos^2 80^\circ = 1,$$

$$\cos^2 20^\circ + \cos^2 70^\circ = \sin^2 70^\circ + \cos^2 70^\circ = 1,$$

$$\cos^2 30^\circ + \cos^2 60^\circ = \sin^2 60^\circ + \cos^2 60^\circ = 1,$$

$$\cos^2 40^\circ + \cos^2 50^\circ = \sin^2 50^\circ + \cos^2 50^\circ = 1$$

이므로 주어진 식의 값은

$$\cos^2 10^\circ + \cos^2 20^\circ + \cdots + \cos^2 70^\circ + \cos^2 80^\circ \\ = 1 + 1 + 1 + 1 = 4$$

75) $\frac{91}{2}$

$\Rightarrow \sin^2 1^\circ + \sin^2 2^\circ + \cdots + \sin^2 89^\circ + \sin^2 90^\circ$ 에서
 $1^\circ + 89^\circ = 2^\circ + 88^\circ = \cdots = 44^\circ + 46^\circ = 90^\circ$ 이므로

$$\sin 1^\circ = \sin (90^\circ - 89^\circ) = \cos 89^\circ$$

$$\sin 2^\circ = \sin (90^\circ - 88^\circ) = \cos 88^\circ,$$

\vdots

$$\sin 44^\circ = \sin (90^\circ - 46^\circ) = \cos 46^\circ$$

이때,

$$\sin^2 1^\circ + \sin^2 89^\circ = \cos^2 89^\circ + \sin^2 89^\circ = 1,$$

$$\sin^2 2^\circ + \sin^2 88^\circ = \cos^2 88^\circ + \sin^2 88^\circ = 1,$$

\vdots

$$\sin^2 44^\circ + \sin^2 46^\circ = \cos^2 46^\circ + \sin^2 46^\circ = 1$$

이므로 주어진 식의 값은

$$\sin^2 1^\circ + \sin^2 2^\circ + \cdots + \sin^2 89^\circ + \sin^2 90^\circ$$

$$= 44 + \sin^2 45^\circ + \sin^2 90^\circ$$

$$= 44 + \frac{1}{2} + 1 = \frac{91}{2}$$

76) 4

$$\Rightarrow \sin(90^\circ - x^\circ) = \cos(x^\circ)$$

주어진 값은

$$\sin^2 10^\circ + \sin^2 20^\circ + \cdots + \cos^2 10^\circ$$

$$(\sin^2 10^\circ + \cos^2 10^\circ) + \cdots + (\sin^2 40^\circ + \cos^2 40^\circ) = 4$$

77) $\frac{89}{2}$

$\Rightarrow 1^\circ + 89^\circ = 2^\circ + 88^\circ = \cdots = 44^\circ + 46^\circ = 90^\circ$ 에서

$$\cos 1^\circ = \cos (90^\circ - 89^\circ) = \sin 89^\circ,$$

$$\cos 2^\circ = \cos (90^\circ - 88^\circ) = \sin 88^\circ,$$

\vdots

$$\cos 44^\circ = \cos (90^\circ - 46^\circ) = \sin 46^\circ$$

$$\cos^2 1^\circ + \cos^2 89^\circ = \sin^2 89^\circ + \cos^2 89^\circ = 1,$$

$$\cos^2 2^\circ + \cos^2 88^\circ = \sin^2 88^\circ + \cos^2 88^\circ = 1,$$

\vdots

$$\cos^2 44^\circ + \cos^2 46^\circ = \sin^2 46^\circ + \cos^2 46^\circ = 1$$

$$\therefore \cos^2 1^\circ + \cos^2 2^\circ + \cdots + \cos^2 88^\circ + \cos^2 89^\circ$$

$$= 44 + \cos^2 45^\circ = 44 + \frac{1}{2} = \frac{89}{2}$$

78) 5

$\Rightarrow 10^\circ + 80^\circ = 20^\circ + 70^\circ = \cdots = 40^\circ + 50^\circ$ 에서

$$\sin 10^\circ = \sin (90^\circ - 80^\circ) = \cos 80^\circ,$$

$$\sin 20^\circ = \sin (90^\circ - 70^\circ) = \cos 70^\circ,$$

$$\sin 30^\circ = \sin (90^\circ - 60^\circ) = \cos 60^\circ$$

$$\sin 40^\circ = \sin (90^\circ - 50^\circ) = \cos 50^\circ$$

$$\sin^2 10^\circ + \sin^2 80^\circ = \cos^2 80^\circ + \sin^2 80^\circ = 1,$$

$$\sin^2 20^\circ + \sin^2 70^\circ = \cos^2 70^\circ + \sin^2 70^\circ = 1,$$

$$\sin^2 30^\circ + \sin^2 60^\circ = \cos^2 60^\circ + \sin^2 60^\circ = 1$$

$$\sin^2 40^\circ + \sin^2 50^\circ = \cos^2 50^\circ + \sin^2 50^\circ = 1$$

$$\therefore \sin^2 10^\circ + \sin^2 20^\circ + \cdots + \sin^2 80^\circ + \sin^2 90^\circ$$

$$= 1 + 1 + 1 + 1 + \sin^2 90^\circ = 4 + 1 = 5$$