

[영역] 5.기하



중 3 과정

5-2-2.평면도형에서의 활용(2)_특수한 직각삼각형의 변의 길이, 두 점 사이의 거리





◇「콘텐츠산업 진흥법 시행령」제33조에 의한 표시

1) 제작연월일 : 2016-10-25

2) 제작자 : 교육지대㈜

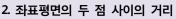
3) 이 콘텐츠는 「콘텐츠산업 진흥법」에 따라 최초 제작일부터 5년간 보호됩니다. ◇「콘텐츠산업 진흥법」외에도「저작권법」에 의하여 보호되는 콘텐츠의 경우, 그 콘텐츠의 전부 또는 일부를 무단으로 복제하거나 전송하는 것은 콘텐츠산업 진흥법 외에도 저작권법에 의한 법적 책임을 질 수 있습니다.

계산시 참고사항

1. 특수한 직각삼각형의 변의 길이

1) 세 내각의 크기가 45° , 45° , 90° 인 삼각형 $\angle A = \angle B = 45^\circ$ 이고, $\angle C = 90^\circ$ 인 직각삼각형의 세 변의 길이의 비는 $\overline{AB}: \overline{BC}: \overline{CA} = \sqrt{2}: 1: 1$

2) 세 내각의 크기가 30° , 60° , 90° 인 삼각형 $\angle A = 30^\circ$, $\angle B = 60^\circ$ 이고, $\angle C = 90^\circ$ 인 직각삼각형의 세 변의 길이의 비는 $\overline{AB} : \overline{BC} : \overline{CA} = 2 : 1 : \sqrt{3}$



1) 원점과 한 점 사이의 거리

: 원점 O와 한 점 $P(x_1, y_1)$ 사이의 거리 \Rightarrow $\overline{OP} = \sqrt{x_1^2 + y_1^2}$

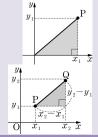
2) 두 점 사이의 거리

: 두 점 $P(x_1, y_1)$ 와 $Q(x_2, y_2)$ 사이의 거리

 $\Rightarrow \overline{PQ} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$







참고

 두 점 사이의 거리는 두 점을 빗변의 양 끝 점으로 하는 직각삼각형을 그린 후 피타고라스 정리를 이용하여 구한다.

주의 주의

● 다음과 같이 계산해도 된다.

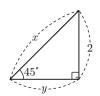
$$\overline{PQ} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$
$$= \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$



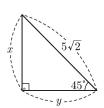
특수한 직각삼각형의 변의 길이

□ 다음 그림의 직각삼각형에서 x, y의 값을 각각 구하여라.

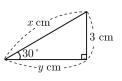
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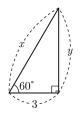
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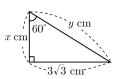


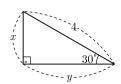
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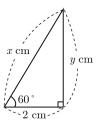
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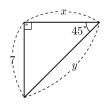




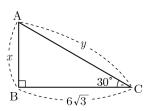
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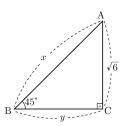
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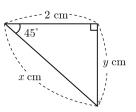
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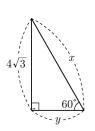
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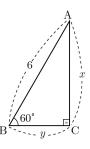
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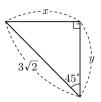
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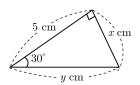


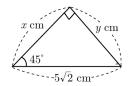
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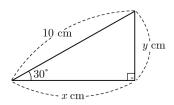
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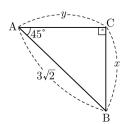




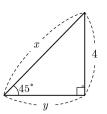
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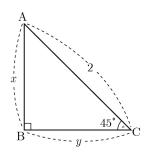
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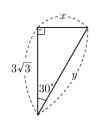
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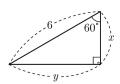
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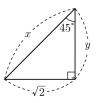
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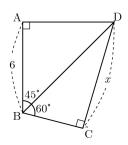


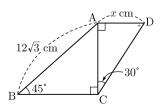
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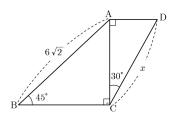


ightharpoonup 다음 그림에서 x의 값을 구하여라.

24.

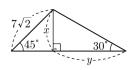




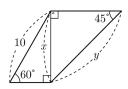


$lacksymbol{\square}$ 다음 그림에서 $x,\ y$ 의 값을 각각 구하여라.

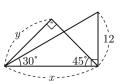
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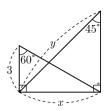
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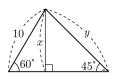
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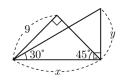
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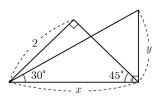
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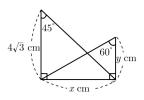
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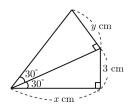
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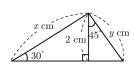
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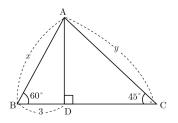


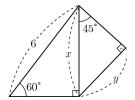
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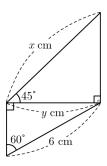
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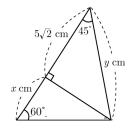




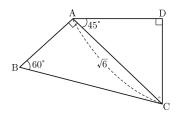
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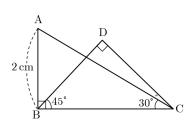
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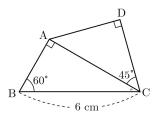
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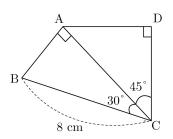


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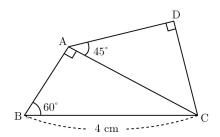


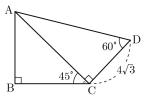
☑ □ABCD의 둘레의 길이를 구하여라.

44.



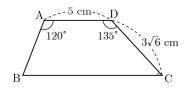
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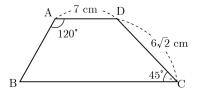


\square 다음 그림과 같이 $\overline{\rm AD}//\overline{\rm BC}$ 인 사다리꼴 $\overline{\rm ABCD}$ 의 둘레의 길이를 구하여라.

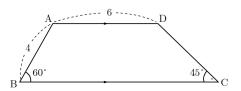
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48.



49.

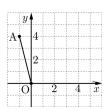


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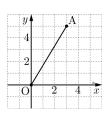
두 점 사이의 거리

☑ 다음 좌표평면에서 두 점 사이의 거리를 구하여라.

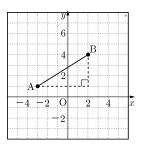
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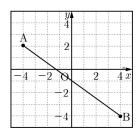
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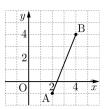
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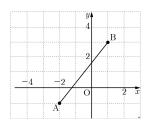
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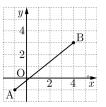


54.



55.





☑ 다음 점과 원점 ○ 사이의 거리를 구하여라.

- 57. (4, 3)
- 58. (2, 5)
- 59. (-1, 1)
- 60. (0, 2)
- (-1, 0)61.
- 62. (1, 2)
- 63. (-3, 4)
- 64. (5, -1)
- 65. (5, 3)
- 66. (-2, -3)
- 67. (-3, -2)
- 68. (-4, 6)
- 69. (-2, 4)

☑ 다음 두 점 사이의 거리를 구하여라.

- 70. (5, 4), (-4, -1)
- 71. (1, 1), (3, 5)
- 72. (-4, 7), (3, 4)
- 73. (-4, -1), (1, 2)
- 74. (-3, -8), (-2, -6)
- 75. (2, 3), (5, 6)
- 76. (4, 6), (-3, -1)

☑ 다음 두 점 사이의 거리를 구하여라.

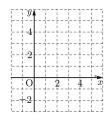
- 77. A(10, 4), B(4, -1)
- A(0, 1), B(2, 0)
- 79. A(2, -3), B(5, 3)
- 80. A(-2, -4), B(5, -1)
- 81. A(1, 1), B(3, 1)
- 82. A(-1, 2), B(-3, 1)

- 83. A(-3, 5), B(2, 3)
- 84. A(-2, -3), B(3, 3)
- 85. A(1, 3), B(-1, -3)
- 86. A(-2, -1), B(4, 3)
- 87. A(-1, 2), B(3, -2)
- 88. A(-2, 3), B(3, 2)
- 89. A(0, -2), B(5, -3)
- 90. A(-5, -2), B(-1, 8)
- 91. A(1, 3), B(-4, -1)
- 92. A(-1, 2), B(-3, -6)

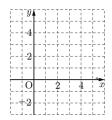
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좌표평면에서 삼각형의 종류와 넓이

- 세 점 A(1, -1), B(4, -1), C(4, 3)을 꼭짓점으로 하는 삼각형 ABC에 대하여 다음 물음에 답하여라.
- 93. 삼각형 ABC를 다음 좌표평면 위에 나타내어라.



- 94. AB 의 길이를 구하여라.
- 95. BC 의 길이를 구하여라.
- 97. 삼각형 ABC가 어떤 삼각형인지 말하여라.
- ☑ 세 점 A(2, -2), B(5, -1), C(5, 4을 꼭짓점으로 하는 삼각형 ABC에 대하여 다음 물음에 답하여라.
- 98. 삼각형 ABC를 다음 좌표평면 위에 나타내어라.



- 99. 점B의 길이를 구하여라.
- 100 BC 의 길이를 구하여라.
- 101 조점의 길이를 구하여라.
- 102 삼각형 ABC가 어떤 삼각형인지 말하여라.

☑ 다음 세 점을 꼭짓점으로 하는 삼각형은 어떤 삼각형인지 말하여라.

103.
$$A(0, -1), B(4, 0), C(5, -4)$$

104.
$$O(0, 0), A(3, -2), B(5, 1)$$

105.
$$O(0, 0), A(3, 4), B(-2, 4)$$

107.
$$A(1, 0), B(5, 3), C(5, -2)$$

108.
$$A(-1, -1)$$
, $B(2, 5)$, $C(-9, 3)$

109 A(
$$-3$$
, 3), B(-2 , 2), C(-5 , 1)

110. A(-3, 0), B(3, 0), C(0,
$$3\sqrt{3}$$
)

111.
$$A(-2, 2), B(0, -3), C(3, 4)$$



정답 및 해설

- 1) $x = 2\sqrt{2}$, y = 2
- $\Rightarrow 2: x = 1: \sqrt{2} \qquad \therefore \quad x = 2\sqrt{2}$ $2: y = 1: 1 \qquad \therefore \quad y = 2$
- 2) x = 6, $y = 3\sqrt{3}$
- $\Rightarrow 3: x = 1:2 \qquad \therefore x = 6$ $3: y = 1: \sqrt{3} \qquad \therefore y = 3\sqrt{3}$
- 3) x = 5, y = 5
- $\Rightarrow x:5\sqrt{2}=1:\sqrt{2} \qquad \therefore x=5$ $y:5\sqrt{2}=1:\sqrt{2} \qquad \therefore y=5$
- 4) x = 6, $y = 3\sqrt{3}$
- $\Rightarrow x:3=2:1 \text{ ord} \quad x=6$ $y:3=\sqrt{3}:1 \text{ ord} \quad y=3\sqrt{3}$
- 5) x = 3, y = 6
- $\Rightarrow x:3\sqrt{3}=1:\sqrt{3} \text{ 에서 } x=3$ $3\sqrt{3}:y=\sqrt{3}:2\text{에서 } y=6$
- 6) $x=2, y=2\sqrt{3}$
- $\Rightarrow x:4=1:2 \qquad \therefore x=2$ $y:4=\sqrt{3}:2 \qquad \therefore y=2\sqrt{3}$
- 7) x = 7, $y = 7\sqrt{2}$
- $\Rightarrow 7: x = 1:1 \qquad \therefore x = 7$ $7: y = 1: \sqrt{2} \qquad \therefore y = 7\sqrt{2}$
- 8) $x = 2\sqrt{3}, y = \sqrt{6}$
- $\Rightarrow x: \sqrt{6} = \sqrt{2}: 1 \qquad \therefore x = 2\sqrt{3}$ $y: \sqrt{6} = 1: 1 \qquad \therefore y = \sqrt{6}$
- 9) x = 8, y = 4
- $\Rightarrow 4\sqrt{3} : x = \sqrt{3} : 2 \qquad \therefore x = 8$ $4\sqrt{3} : y = \sqrt{3} : 1 \qquad \therefore y = 4$
- 10) x = 3, y = 3
- $\Rightarrow 3\sqrt{2} : x = \sqrt{2} : 1 \qquad \therefore x = 3$ $3\sqrt{2} : y = \sqrt{2} : 1 \qquad \therefore y = 3$
- 11) x = 4, $y = 2\sqrt{3}$
- $\Rightarrow x:2=2:1$ 에서 x=4 $2:y=1:\sqrt{3}$ 에서 $y=2\sqrt{3}$
- 12) x = 6, y = 12
- $\Rightarrow x:6\sqrt{3}=1:\sqrt{3} \qquad \therefore x=6$ $y:6\sqrt{3}=2:\sqrt{3} \qquad \therefore y=12$

- 13) $x = 2\sqrt{2}, y = 2$
- $\Rightarrow 2: x = 1: \sqrt{2} \text{ old } x = 2\sqrt{2}$ 2: y = 1: 1 old y = 2
- 14) $x = 3\sqrt{3}, y = 3$
- $\Rightarrow 6: x = 2: \sqrt{3} \qquad \therefore x = 3\sqrt{3}$ $6: y = 2:1 \qquad \therefore y = 3$
- 15) $x = \frac{5\sqrt{3}}{3}$, $y = \frac{10\sqrt{3}}{3}$
- $x:5=1:\sqrt{3} \text{ 에서 } x=\frac{5\sqrt{3}}{3}$ $5:y=\sqrt{3}:2$ 에서 $y=\frac{10\sqrt{3}}{3}$
- 16) x = 5, y = 5
- $\Rightarrow x:5\sqrt{2}=1:\sqrt{2} \text{ MM } x=5$ $y:5\sqrt{2}=1:\sqrt{2} \text{ MM } y=5$
- 17) $x = 5\sqrt{3}, y = 5$
- $\Rightarrow 1:2=y:10, 2y=10 \therefore y=5$ $x=\sqrt{10^2-5^2}=\sqrt{100-25}=\sqrt{75}=5\sqrt{3}$
- 18) x = y = 3
- 다 \triangle ABC에서 x:y=1:1이므로 x=y이다. $1:\sqrt{2}=x:3\sqrt{2},\ \sqrt{2}\,x=3\sqrt{2}$ $\therefore \ x=y=3$
- 19) $x = 4\sqrt{2}$, y = 4
- \Rightarrow 주어진 직각삼각형에서 $x:4=\sqrt{2}:1$ 이므로 $x=4\sqrt{2}$ y:4=1:1이므로 y=4
- 20) $x = \sqrt{2}, y = \sqrt{2}$
- $\Rightarrow 2: x = \sqrt{2}: 1 \qquad \therefore x = \sqrt{2}$ $2: y = \sqrt{2}: 1 \qquad \therefore y = \sqrt{2}$
- 21) x = 3, y = 6
- $\Rightarrow 3\sqrt{3} : x = \sqrt{3} : 1 \qquad \therefore x = 3$ $3\sqrt{3} : y = \sqrt{3} : 2 \qquad \therefore y = 6$
- 22) x = 3, $y = 3\sqrt{3}$
- $\Rightarrow 6: x = 2:1 \qquad \therefore x = 3$ $6: y = 2: \sqrt{3} \qquad \therefore 3\sqrt{3}$
- 23) x = 2, $y = \sqrt{2}$
- $\Rightarrow \sqrt{2} : x = 1 : \sqrt{2} \qquad \therefore x = 2$ $\sqrt{2} : y = 1 : 1 \qquad \therefore y = \sqrt{2}$
- 24) $3\sqrt{6}$
- ⇒ 직각삼각형 ABD에서

 $\overline{AB}:\overline{BD}=1:\sqrt{2}$ 이므로 $\overline{BD}=6\sqrt{2}$

직각삼각형 BCD에서

 $\overline{\text{BD}}:\overline{\text{CD}}=2:\sqrt{3}$ 이므로 $x=\overline{\text{CD}}=3\sqrt{6}$

25) $6\sqrt{2}$

$$\Rightarrow$$
 \triangle ABC에서 $1:\sqrt{2}=\overline{AC}:12\sqrt{3}, \sqrt{2}\overline{AC}=12\sqrt{3}$

$$\therefore \overline{AC} = \frac{12\sqrt{3}}{\sqrt{2}} = \frac{12\sqrt{6}}{2} = 6\sqrt{6}$$

$$\triangle$$
ACD에서 $1: \sqrt{3} = x: 6\sqrt{6}, \sqrt{3}x = 6\sqrt{6}$

$$\therefore x = \frac{6\sqrt{6}}{\sqrt{3}} = 6\sqrt{2}$$

26) $4\sqrt{3}$

$$\Rightarrow$$
 $\triangle ABC \cap M : \sqrt{2} = \overline{AC} : 6\sqrt{2}, \sqrt{2} \overline{AC} = 6\sqrt{2}$

$$\therefore \overline{AC} = \frac{6\sqrt{2}}{\sqrt{2}} = 6$$

$$\triangle$$
ACD에서 $\sqrt{3}: 2=6:x, \sqrt{3}x=12$

$$\therefore x = \frac{12}{\sqrt{3}} = \frac{12\sqrt{3}}{3} = 4\sqrt{3}$$

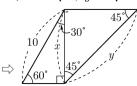
27) x = 7, $y = 7\sqrt{3}$

$$\Rightarrow 7\sqrt{2}: x = \sqrt{2}: 1$$
 $\therefore x = 7$

$$7: y = 1: \sqrt{3} \qquad \therefore \quad y = 7\sqrt{3}$$

$$\therefore y = 7\sqrt{3}$$

28) $x = 5\sqrt{3}$, $y = 5\sqrt{6}$



$$10: x = 2: \sqrt{3}$$

$$\therefore x = 5\sqrt{3}$$

$$5\sqrt{3}: y = 1: \sqrt{2}$$
 : $y = 5\sqrt{6}$

$$\therefore y = 5\sqrt{6}$$

29)
$$x = 12\sqrt{3}$$
, $y = 6\sqrt{6}$

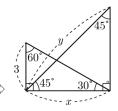
$$\Rightarrow 12: x = 1: \sqrt{3} \qquad \therefore x = 12\sqrt{3}$$

$$x = 12\sqrt{3}$$

$$12\sqrt{3}: y = \sqrt{2}: 1$$
 : $y = 6\sqrt{6}$

$$\therefore y = 6\sqrt{6}$$

30)
$$x = 3\sqrt{3}$$
, $y = 3\sqrt{6}$



$$3: x = 1: \sqrt{3} \qquad \therefore x = 3\sqrt{3}$$

$$\therefore x = 3\sqrt{3}$$

$$3\sqrt{3}: y = 1: \sqrt{2}$$

$$\therefore y = 3\sqrt{6}$$

31)
$$x = 5\sqrt{3}$$
, $y = 5\sqrt{6}$

$$\Rightarrow 10: x = 2: \sqrt{3} \qquad \therefore x = 5\sqrt{3}$$

$$r = 5\sqrt{3}$$

$$5\sqrt{3}: y=1:\sqrt{2}$$

$$\therefore y = 5\sqrt{6}$$

32)
$$x = 9\sqrt{2}$$
, $y = 3\sqrt{6}$

$$\Rightarrow 9: x = 1: \sqrt{2} \qquad \therefore x = 9\sqrt{2}$$

$$\therefore x = 9\sqrt{2}$$

$$9\sqrt{2}: y = \sqrt{3}: 1$$
 : $y = 3\sqrt{6}$

:
$$y = 3\sqrt{6}$$

33)
$$x = 2\sqrt{2}$$
, $y = \frac{2\sqrt{6}}{3}$

$$\Rightarrow 1 \cdot \sqrt{2} = 2 \cdot x$$

$$\Rightarrow 1: \sqrt{2} = 2: x \qquad \therefore x = 2\sqrt{2}$$

$$1: \sqrt{3} = y: 2\sqrt{2}, \ \sqrt{3}y = 2\sqrt{2}$$

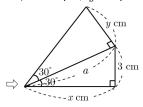
$$\therefore y = \frac{2\sqrt{2}}{\sqrt{3}} = \frac{2\sqrt{6}}{3}$$

34)
$$x = 4\sqrt{3}$$
, $y = 4$

$$\Rightarrow$$
 $4\sqrt{3}$: $x = 1$: 1에서 $x = 4\sqrt{3}$

$$4\sqrt{3}: y = \sqrt{3}: 1$$
에서 $y = 4$

35)
$$x = 3\sqrt{3}$$
, $y = 2\sqrt{3}$



 $x:3=\sqrt{3}:1$ 에서 $x=3\sqrt{3}$

$$a:3=2:1$$
에서 $a=6$

$$6: y = \sqrt{3}: 1$$
에서 $y = 2\sqrt{3}$

36)
$$x = 4$$
, $y = 2\sqrt{2}$

$$\Rightarrow x:2=2:101$$
 $\Rightarrow x=4$

$$2: y = 1: \sqrt{2}$$
에서 $y = 2\sqrt{2}$

37)
$$x = 6$$
, $y = 3\sqrt{6}$

$$3: x = 1:2$$
 $\therefore x = 6$

$$3: \overline{AD} = 1: \sqrt{3}$$
 $\therefore \overline{AD} = 3\sqrt{3}$

$$\triangle$$
ACD는 $\overline{AD} = \overline{CD}$ 인 직각이등변삼각형이므로

$$3\sqrt{3}: y=1:\sqrt{2}$$
 $\therefore y=3\sqrt{6}$

38)
$$x = 3\sqrt{3}$$
, $y = \frac{3\sqrt{6}}{2}$

$$\Leftrightarrow 6: x = 2: \sqrt{3}$$
이므로 $2x = 6\sqrt{3}$
$$\therefore x = 3\sqrt{3}$$

$$3\sqrt{3}: y = \sqrt{2}: 1$$
이므로 $\sqrt{2}y = 3\sqrt{3}$ $\therefore y = \frac{3\sqrt{6}}{2}$

$$\therefore y = \frac{3\sqrt{6}}{2}$$

39)
$$x = 3\sqrt{6}$$
, $y = 3\sqrt{3}$

$$\Rightarrow 2: \sqrt{3} = 6: y \qquad \therefore y = 3\sqrt{3} (cm) \\ 1: \sqrt{2} = 3\sqrt{3}: x \qquad \therefore x = 3\sqrt{6} (cm)$$

$$1: \sqrt{2} = 3\sqrt{3}: x \quad \therefore x = 3\sqrt{6} (cm)$$

40)
$$x = \frac{5\sqrt{6}}{3}$$
, $y = 10$

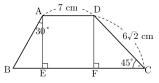
$$\Rightarrow 5\sqrt{2}: y=1:\sqrt{2}$$
 에서 $y=10$

$$x:5\sqrt{2}=1:\sqrt{3}$$
 에서 $x=\frac{5\sqrt{6}}{3}$

- 41) $\sqrt{3}$
- 42) $\sqrt{6}$ cm
- 다 직각삼각형 ABC에서 $\overline{AB}:\overline{BC}=1:\sqrt{3}$ 이므로 $2:\overline{BC}=1:\sqrt{3}$ $\therefore \overline{BC}=2\sqrt{3}$ 직각삼각형 BCD에서 $\overline{CD}:\overline{BC}=1:\sqrt{2}$ 이므로 $\overline{CD}:2\sqrt{3}=1:\sqrt{2}$ $\therefore \overline{CD}=\sqrt{6}$
- 43) $\frac{3\sqrt{6}}{2}$ cm
- ightharpoonup 직각삼각형 ABC에서 $ightharpoonup \overline{AC}:\overline{BC}=\sqrt{3}:2$ 이므로 $ightharpoonup \overline{AC}=3\sqrt{3}$ (cm) 직각삼각형 ACD에서 $ightharpoonup \overline{CD}:\overline{AC}=1:\sqrt{2}$ 이므로 $ightharpoonup \overline{CD}=rac{3\sqrt{6}}{2}$ (cm)
- 44) $4(3+\sqrt{6})$ cm
- 다 $\overline{AB} = 4 \text{cm}$, $\overline{AC} = 4\sqrt{3} \text{ cm}$ $1: \sqrt{2} = \overline{AD}: 4\sqrt{3}$ $\therefore \overline{AD} = 2\sqrt{6}$ 따라서 $\square ABCD$ 의 둘레는 $4+8+2\sqrt{6}+2\sqrt{6}=12+4\sqrt{6}=4(3+\sqrt{6})(\text{cm})$
- 45) $(2\sqrt{6}+6)$ cm
- $\Rightarrow \sqrt{3}: 2 = \overline{AC}: 4, \ 2\overline{AC} = 4\sqrt{3}, \ \overline{AC} = 2\sqrt{3}$
- $1: \sqrt{2} = \overline{AD}: 2\sqrt{3}, \sqrt{2}\overline{AD} = 2\sqrt{3}, \overline{AD} = \sqrt{6}$
- \square ABCD의 둘레의 길이는 $\overline{AB}+\overline{BC}+\overline{CD}+\overline{DA}$ = $2+4+\sqrt{6}+\sqrt{6}=6+2\sqrt{6}$ 이 된다.
- 46) $12(\sqrt{2}+\sqrt{3})$
- \Rightarrow $\triangle ACD에서 <math>1: \sqrt{3} = 4\sqrt{3}: \overline{AC}$ $\therefore \overline{AC} = 12$ $2: 1 = \overline{AD}: 4\sqrt{3}$ $\therefore \overline{AD} = 8\sqrt{3}$ $\triangle ABC에서 <math>1: \sqrt{2} = \overline{AB}: 12, \sqrt{2} \overline{AB} = 12$ $\therefore \overline{AB} = \frac{12}{\sqrt{2}} = \frac{12\sqrt{2}}{2} = 6\sqrt{2}$

 \triangle ABC는 직각이등변삼각형이므로 $\overline{\mathrm{BC}} = 6\sqrt{2}$ 이다.

- \therefore (\square ABCD의 둘레)= $12\sqrt{2}+12\sqrt{3}=12(\sqrt{2}+\sqrt{3})$
- 47) $19+3\sqrt{6}+3\sqrt{3}$ (cm)
- 48) $20+6\sqrt{2}+6\sqrt{3}$
- ightharpoonup 점 A와 점 D에서 $ightharpoonup \overline{BC}$ 에 내린 수선의 발을 ightharpoonup E, F라고 하자.



 \triangle CDF에서 $1: \sqrt{2} = \overline{CF}: 6\sqrt{2}$,

$$\sqrt{2} \, \overline{\text{CF}} = 6 \sqrt{2}$$
 $\therefore \overline{\text{CF}} = 6 \text{ (cm)}$

$$\triangle ABE에서 1: \sqrt{3} = \overline{BE}:6, \sqrt{3}\overline{BE}=6,$$

$$\therefore \overline{BE} = \frac{6}{\sqrt{3}} = \frac{6\sqrt{3}}{3} = 2\sqrt{3} \text{ (cm)}$$

- $1:2=2\sqrt{3}:\overline{AB}$ $\therefore \overline{AB}=4\sqrt{3}$ (cm)
- (□ABCD의 둘레의 길이)
- $=\overline{AD}+\overline{DC}+\overline{CF}+\overline{FE}+\overline{EB}+\overline{BA}$
- $=7+6\sqrt{2}+6+7+2\sqrt{3}+4\sqrt{3}$
- $=20+6\sqrt{2}+6\sqrt{3}$ (cm)
- 49) $18+2\sqrt{3}+2\sqrt{6}$
- 50) $\sqrt{17}$
- \Rightarrow A(-1, 4), O(0, 0) 사이의 거리는 $\overline{AO} = \sqrt{(-1)^2 + 4^2} = \sqrt{17}$
- 51) $\sqrt{34}$
- \Rightarrow A(3, 5), O(0, 0) 사이의 거리는 $\overline{AO} = \sqrt{3^2 + 5^2} = \sqrt{34}$
- 52) $\overline{AB} = \sqrt{34}$
- $\Rightarrow \overline{AB} = \sqrt{(-3-2)^2 + (1-4)^2} = \sqrt{34}$
- 53) 10
- 54) $\sqrt{29}$
- 다 A(2, -1), B(4, 4)사이의 거리는 $\overline{AB} = \sqrt{(4-2)^2 + (4+1)^2} = \sqrt{29}$
- 55) 5
- 56) $\sqrt{41}$
- A(-1, -1), B(4, 3) 사이의 거리는 $\overline{AB} = \sqrt{(4+1)^2 + (3+1)^2} = \sqrt{41}$
- 57) 5
- $\Rightarrow \sqrt{4^2+3^2} = \sqrt{25} = 5$
- 58) $\sqrt{29}$
- $\Rightarrow \sqrt{2^2 + 5^2} = \sqrt{29}$
- 59) $\sqrt{2}$
- $\Rightarrow \sqrt{(-1)^2+1^2}=\sqrt{2}$
- 60) 2

- 61) 1
- 62) $\sqrt{5}$
- 63) 5
- 64) $\sqrt{26}$
- 65) $\sqrt{34}$
- 66) $\sqrt{13}$
- 67) $\sqrt{13}$
- $\Rightarrow \sqrt{(-3)^2 + (-2)^2} = \sqrt{13}$
- 68) $2\sqrt{13}$
- $\Rightarrow \sqrt{(-4)^2+6^2} = 2\sqrt{13}$
- 69) $2\sqrt{5}$
- $\Rightarrow \overline{OA} = \sqrt{(-2)^2 + 4^2} = 2\sqrt{5}$
- 70) $\sqrt{106}$
- $\Rightarrow \sqrt{(-4-5)^2+(-1-4)^2} = \sqrt{106}$
- 71) $\sqrt{20}$
- $\Rightarrow \sqrt{(3-1)^2+(5-1)^2} = \sqrt{20}$
- 72) $\sqrt{58}$
- $\Rightarrow \sqrt{(3+4)^2+(4-7)^2} = \sqrt{58}$
- 73) $\sqrt{34}$
- $\Rightarrow \sqrt{\{1-(-4)\}^2+\{2-(-1)\}^2} = \sqrt{34}$
- 74) $\sqrt{5}$
- 75) $3\sqrt{2}$
- $\Rightarrow \sqrt{(5-2)^2+(6-3)^2} = \sqrt{18} = 3\sqrt{2}$
- 76) $7\sqrt{2}$
- $\Rightarrow \sqrt{(-3-4)^2+(-1-6)^2} = \sqrt{98} = 7\sqrt{2}$
- 77) $\sqrt{61}$
- $\Rightarrow \overline{AB} = \sqrt{(4-10)^2 + (-1-4)^2} = \sqrt{61}$
- 78) $\sqrt{5}$
- $\Rightarrow \overline{AB} = \sqrt{(2-0)^2 + (0-1)^2} = \sqrt{5}$
- 79) $3\sqrt{5}$
- $\Rightarrow \overline{AB} = \sqrt{(2-5)^2 + (-3-3)^2} = 3\sqrt{5}$
- 80) ②
- $\Rightarrow \overline{AB} = \sqrt{(-2-5)^2 + (-4+1)^2} = \sqrt{58}$

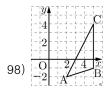
- 81) 2
- $\Rightarrow \overline{AB} = \sqrt{(3-1)^2 + (1-1)^2} = \sqrt{4} = 2$
- 82) $\sqrt{5}$
- $\Rightarrow \overline{AB} = \sqrt{\{-3 (-1)\}^2 + (1 2)^2} = \sqrt{5}$
- 83) $\sqrt{29}$
- $\Rightarrow \overline{AB} = \sqrt{\{2-(-3)\}^2 + (3-5)^2} = \sqrt{29}$
- 84) $\sqrt{61}$
- $\Rightarrow \overline{AB} = \sqrt{(3-(-2))^2 + (3-(-3))^2} = \sqrt{61}$
- 85) $2\sqrt{10}$
- $\Rightarrow \overline{AB} = \sqrt{(-1-1)^2 + (-3-3)^2} = \sqrt{40} = 2\sqrt{10}$
- 86) $2\sqrt{13}$
- $\Rightarrow \overline{AB} = \sqrt{(-2-4)^2 + (-1-3)^2} = 2\sqrt{13}$
- 87) $4\sqrt{2}$
- $\Rightarrow \overline{AB} = \sqrt{(3+1)^2 + (-2-2)^2} = \sqrt{16+16} = \sqrt{32} = 4\sqrt{2}$
- 88) $\sqrt{26}$
- $\Rightarrow \overline{AB} = \sqrt{(3+2)^2 + (2-3)^2} = \sqrt{26}$
- 89) $\sqrt{26}$
- $\Rightarrow \overline{AB} = \sqrt{(5-0)^2 + (-3+2)^2} = \sqrt{26}$
- 90) $2\sqrt{29}$
- $\Rightarrow \overline{AB} = \sqrt{(-1+5)^2 + (8+2)^2} = 2\sqrt{29}$
- 91) $\sqrt{41}$
- $\Rightarrow \overline{AB} = \sqrt{(-4-1)^2 + (-1-3)^2} = \sqrt{41}$
- 92) $2\sqrt{17}$
- $\Rightarrow \overline{AB} = \sqrt{(-3 (-1))^2 + (-6 2)^2} = 2\sqrt{17}$



- 94) 3
- $\Rightarrow \overline{AB} = \sqrt{(4-1)^2 + \{-1 (-1)\}^2} = \sqrt{9} = 3$
- 95) 4
- $\Rightarrow \overline{BC} = \sqrt{(4-4)^2 + (3-(-1))^2} = \sqrt{16} = 4$
- 96) 5
- $\Rightarrow \overline{CA} = \sqrt{(4-1)^2 + (3-(-1))^2} = \sqrt{25} = 5$

97) 직각삼각형

 \Rightarrow $\overline{CA^2} = \overline{AB^2} + \overline{BC^2}$ 이므로 직각삼각형이다.



99)
$$\sqrt{10}$$

$$\Rightarrow \overline{AB} = \sqrt{(5-2)^2 + (-1-(-2))^2} = \sqrt{10}$$

100) 5

$$\Rightarrow \overline{BC} = \sqrt{(5-5)^2 + (4-(-1))^2} = \sqrt{25} = 5$$

101) $3\sqrt{5}$

$$\Rightarrow \overline{CA} = \sqrt{(5-2)^2 + (4-(-2))^2} = \sqrt{45} = 3\sqrt{5}$$

102) 둔각삼각형

 \Rightarrow $\overline{CA^2} > \overline{AB^2} + \overline{BC^2}$ 이므로 둔각삼각형이다.

104) ∠A=90°인 직각이등변삼각형

105) 이등변삼각형

106) 이등변삼각형

107) 이등변삼각형

$$\Rightarrow \overline{AB} = \sqrt{(5-1)^2 + (3-0)^2} = \sqrt{25} = 5$$

$$\overline{BC} = \sqrt{(5-5)^2 + (-2-3)^2} = \sqrt{25} = 5$$
 $\overline{CA} = \sqrt{(1-5)^2 + \{0-(-2)\}^2} = \sqrt{20} = 2\sqrt{5}$
따라서 $\overline{AB} = \overline{BC}$ 이므로 $\triangle ABC = 0$ 등변삼각형이다.

108) ∠A=90°인 직각삼각형

$$\overline{AB} = \sqrt{\{2 - (-1)\}^2 + \{5 - (-1)\}^2} = \sqrt{45} = 3\sqrt{5}$$

$$\overline{BC} = \sqrt{(-9 - 2)^2 + (3 - 5)^2} = \sqrt{125} = 5\sqrt{5}$$

$$\overline{CA} = \sqrt{\{-1 - (-9)\}^2 + (-1 - 3)^2} = \sqrt{80} = 4\sqrt{5}$$
 따라서 $\overline{BC}^2 = \overline{AB}^2 + \overline{CA}^2$ 이므로
$$\Delta ABC \succeq \angle A = 90^\circ \ \text{인 직각삼각형이다}.$$

109) ∠A=90°인 직각삼각형

$$\overline{AB} = \sqrt{\{-2 - (-3)\}^2 + (2 - 3)^2} = \sqrt{2}$$
 $\overline{BC} = \sqrt{\{-5 - (-2)\}^2 + (1 - 2)^2} = \sqrt{10}$ $\overline{CA} = \sqrt{\{-3 - (-5)\}^2 + (3 - 1)^2} = \sqrt{8} = 2\sqrt{2}$ 따라서 $\overline{BC}^2 = \overline{AB}^2 + \overline{CA}^2$ 이므로 $\triangle ABC \succeq \angle A = 90$ ° 인 작각삼각형이다.

110) 정삼각형

$$Arr AB = \sqrt{\{3 - (-3)\}^2 + (0 - 0)^2} = \sqrt{36} = 6$$

$$Arr BC = \sqrt{(0 - 3)^2 + (3\sqrt{3} - 0)^2} = \sqrt{36} = 6$$

$$Arr CA = \sqrt{(-3 - 0)^2 + (0 - 3\sqrt{3})^2} = \sqrt{36} = 6$$
따라서 $Arr AB =
Arr BC =
Arr ABC =$

111) ∠A=90°인 직각이등변삼각형