

수학 계산력 강화

(1)인수분해의 뜻과 기본공식





◇「콘텐츠산업 진흥법 시행령」제33조에 의한 표시

- 1) 제작연월일 : 2018-03-05
- 2) 제작자 : 교육지대㈜
- 3) 이 콘텐츠는 「콘텐츠산업 진흥법」에 따라 최초 제작일부터 5년간 보호됩니다.

◇「콘텐츠산업 진흥법」외에도「저작권법」에 의하여 보호되는 콘텐츠의 경우, 그 콘텐츠의 전부 또는 일부를 무단으로 복제하거나 전송하는 것은 콘텐츠산업 진흥법외에도 저작권법에 의한 법적 책임을 질 수 있습니다.

01 / 인수분해

1. 인수분해

하나의 다항식을 두 개 이상의 다항식의 곱의 꼴로 나타내는 것

$$\frac{x^2+3x+2}{\overset{}{\text{한의}}} = \underbrace{(x+2)(x+1)}_{\overset{}{\text{한의}}} \underbrace{\overset{}{\text{전}}}_{\overset{}{\text{건}}} \underbrace{\overset{}{\text{건}}}_{\overset{}{\text{건}}}$$

2. 인수분해 기본공식

- (1) ma+mb=m(a+b), ma-mb=m(a-b)
- (2) $a^2 + 2ab + b^2 = (a+b)^2$, $a^2 2ab + b^2 = (a-b)^2$
- (3) $a^2 b^2 = (a+b)(a-b)$
- (4) $x^2 + (a+b)x + ab = (x+a)(x+b)$
- (5) $acx^2 + (ad+bc)x + bd = (ax+b)(cx+d)$

☑ 다음 식을 인수분해하여라.

- 1. -abc+a
- 2. ax + bx
- 3. x-xy
- 4. $2ab^2 + 6b$
- $5. \quad ax^2y + axy^2$
- 6. $a^3 16ab^2$
- 7. ay+by-cy

8.
$$(a-b)c+b(b-a)$$

9.
$$a(x-y)-b(y-x)$$

10.
$$1-m-n+mn$$

11.
$$ac-bd-ad+bc$$

12.
$$ab+a+b+1$$

13.
$$(x+1)y^2 + (x+1)y$$

14.
$$a(b-1)-b+1$$

15.
$$(a+b)^2+2(a+b)$$

16.
$$ax + by - ay - bx$$

17.
$$3ab - 6a^2b + 15a^2b^2$$

18.
$$(x-y)^2 - 3y(y-x)$$

19.
$$x^2y + y^2z - y^3 - x^2z$$

20.
$$x^2 - y^2 + xz - yz$$

21.
$$x^3y - xy^3$$

22.
$$xy+y^2-xz-yz$$

23.
$$(x-1)a+(x-1)$$

24.
$$x^3y - x^3$$

25.
$$1-m-n+mn$$

26.
$$16a^2 - 24ab + 9b^2$$

27.
$$9x^2 + 6x + 1$$

28.
$$x^2 - 16y^2$$

29.
$$16x^2 - y^2$$

30.
$$25x^2 - y^2$$

31.
$$27a^2 - 12b^2$$

32.
$$(x+2)^2-(x-1)^2$$

33.
$$64x^2 - 9y^2$$

34.
$$x^2-4$$

35.
$$a^2-4b^2$$

36.
$$x^2-9$$

37.
$$9a^2 - 16b^2$$

38.
$$a^4 - b^4$$

39.
$$a^2-(b-c)^2$$

40.
$$a^2 + 2ab + b^2 - c^2$$

41.
$$a^2 - 9b^2$$

42.
$$-25x^2+1$$

43.
$$\frac{1}{4}x^2 - y^2$$

44.
$$6a^2 - 13a - 5$$

45.
$$x^2 + 10x + 21$$

46.
$$x^2 + 3x + 2$$

47.
$$2x^2 - x - 3$$

48.
$$x^2 - 8x + 7$$

49.
$$3a^2 + 4a - 7$$

50.
$$x^2 - 10x + 21$$

51.
$$x^2 - 2xy - 8y^2$$

52.
$$13a^2 - 8ab - 5b^2$$

53.
$$x^2 + 12x + 36$$

54.
$$9x^2 - 6x + 1$$

55.
$$3a^2 + 4ab - 7b^2$$

56.
$$2x^2 + xy - 3y^2$$

57.
$$9x^2 - 24xy + 16y^2$$

58.
$$a^2 + 10ab + 25b^2$$

59.
$$x^2-2+\frac{1}{x^2}$$

60.
$$x^2 - 10x + 25$$

61.
$$x^2 + x + \frac{1}{4}$$

62.
$$4x^2+4x+1$$

63.
$$x^2 - \frac{2}{5}x + \frac{1}{25}$$

64.
$$5x^2 + x - 18$$

65.
$$a^2+2a+1$$

66.
$$x^2 + 4x + 3$$

67.
$$a^2 - ab - 20b^2$$

68.
$$5a^2 - 8ab - 4b^2$$

69.
$$x^2 - 6xy + 8y^2$$

70.
$$a^2 + 10ab + 21b^2$$

71.
$$4x^2 + 3x - 1$$

72.
$$3x^2 + 11xy - 4y^2$$

73.
$$x^2 - 6x + 8$$

74.
$$x^2 + \frac{2}{3}x + \frac{1}{9}$$

75.
$$4a^2 + 28ab + 49b^2$$

76.
$$25x^2 - 30xy + 9y^2$$

77.
$$x^2 + 6x + 9$$

78.
$$25a^2 - 10a + 1$$

79.
$$x^2 - 8x + 16$$

80.
$$4x^2 + 12xy + 9y^2$$

81.
$$x^2 - 5xy + \frac{25}{4}y^2$$

82.
$$4abx^2 - 4ab^2xy + ab^3y^2$$

정답 및 해설

1)
$$a(1-bc)$$

2)
$$x(a+b)$$

3)
$$x(1-y)$$

4)
$$2b(ab+3)$$

5)
$$axy(x+y)$$

6)
$$a(a+4b)(a-4b)$$

$$\Rightarrow a^3 - 16ab^2 = a(a^2 - 16b^2) = a(a + 4b)(a - 4b)$$

7)
$$y(a+b-c)$$

8)
$$-(a-b)(b-c)$$

$$\Rightarrow (a-b)c+b(b-a) = (a-b)(c-b)$$
$$= -(a-b)(b-c)$$

9)
$$(a+b)(x-y)$$

$$\begin{array}{l} \Rightarrow \ a(x-y)-b(y-x)=a(x-y)+b(x-y) \\ = (a+b)(x-y) \end{array}$$

10)
$$(1-m)(1-n)$$

$$\Rightarrow 1 - m - n + mn = 1 - m - n(1 - m) \\ = (1 - m)(1 - n)$$

11)
$$(c-d)(a+b)$$

$$\Rightarrow ac-bd-ad+bc = a(c-d)+b(c-d) = (c-d)(a+b)$$

12)
$$(a+1)(b+1)$$

13)
$$y(x+1)(y+1)$$

14)
$$(a-1)(b-1)$$

15)
$$(a+b)(a+b+2)$$

16)
$$(a-b)(x-y)$$

17)
$$3ab(1-2a+5ab)$$

18)
$$(x-y)(x+2y)$$

$$\Rightarrow (x-y)^2 - 3y(y-x) = (x-y)\{(x-y) + 3y\} = (x-y)(x+2y)$$

19)
$$(x+y)(x-y)(y-z)$$

$$\Rightarrow x^{2}y + y^{2}z - y^{3} - x^{2}z = x^{2}(y-z) - y^{2}(y-z) = (y-z)(x^{2} - y^{2}) = (x+y)(x-y)(y-z)$$

20)
$$(x-y)(x+y+z)$$

$$\Rightarrow x^2 - y^2 + xz - yz = (x+y)(x-y) + z(x-y)$$
$$= (x-y)(x+y+z)$$

21)
$$xy(x+y)(x-y)$$

22)
$$(x+y)(y-z)$$

$$\Rightarrow \begin{array}{l} xy+y^2-xz-yz \\ =y(x+y)-z(x+y)=(x+y)(y-z) \end{array}$$

23)
$$(x-1)(a+1)$$

24)
$$x^3(y-1)$$

25)
$$(1-m)(1-n)$$

$$\Rightarrow 1 - m - n + mn = (1 - m) - n(1 - m) = (1 - m)(1 - n)$$

26)
$$(4a-3b)^2$$

$$\Rightarrow 16a^2 - 24ab + 9b^2 = (4a)^2 - 2 \cdot 4a \cdot 3b + (3b)^2$$
$$= (4a - 3b)^2$$

27)
$$(3x+1)^2$$

$$\Rightarrow 9x^2 + 6x + 1 = (3x)^2 + 2 \cdot 3x \cdot 1 + 1^2$$

= $(3x+1)^2$

28)
$$(x+4y)(x-4y)$$

29)
$$(4x+y)(4x-y)$$

30)
$$(5x+y)(5x-y)$$

$$\Rightarrow 25x^2 - y^2 = (5x)^2 - y^2 = (5x + y)(5x - y)$$

31)
$$3(3a+2b)(3a-2b)$$

$$\Rightarrow 27a^2 - 12b^2 = 3(9a^2 - 4b^2) = 3\{(3a)^2 - (2b)^2\}$$

= 3(3a+2b)(3a-2b)

32)
$$3(2x+1)$$

$$\Rightarrow (x+2)^2 - (x-1)^2 = (x+2+x-1)(x+2-x+1)$$

= 3(2x+1)

33)
$$(8x+3y)(8x-3y)$$

34)
$$(x+2)(x-2)$$

35)
$$(a+2b)(a-2b)$$

36)
$$(x+3)(x-3)$$

37)
$$(3a+4b)(3a-4b)$$

38)
$$(a-b)(a+b)(a^2+b^2)$$

$$\Rightarrow a^4 - b^4 = (a^2 - b^2)(a^2 + b^2)$$

= $(a - b)(a + b)(a^2 + b^2)$

39)
$$(a+b-c)(a-b+c)$$

40)
$$(a+b+c)(a+b-c)$$

41)
$$(a+3b)(a-3b)$$

42)
$$-(5x+1)(5x-1)$$

43)
$$\left(\frac{1}{2}x+y\right)\left(\frac{1}{2}x-y\right)$$

44)
$$(3a+1)(2a-5)$$

45)
$$(x+3)(x+7)$$

46)
$$(x+1)(x+2)$$

47)
$$(2x-3)(x+1)$$

48)
$$(x-1)(x-7)$$

49)
$$(3a+7)(a-1)$$

50)
$$(x-3)(x-7)$$

51)
$$(x-4y)(x+2y)$$

52)
$$(13a+5b)(a-b)$$

53)
$$(x+6)^2$$

54)
$$(3x-1)^2$$

55)
$$(3a+7b)(a-b)$$

56)
$$(2x+3y)(x-y)$$

57)
$$(3x-4y)^2$$

58)
$$(a+5b)^2$$

59)
$$\left(x - \frac{1}{x}\right)^2$$

60)
$$(x-5)^2$$

61)
$$\left(x + \frac{1}{2}\right)^2$$

62)
$$(2x+1)^2$$

63)
$$\left(x - \frac{1}{5}\right)^2$$

64)
$$(x+2)(5x-9)$$

65)
$$(a+1)^2$$

66)
$$(x+1)(x+3)$$

67)
$$(a+4b)(a-5b)$$

68)
$$(5a+2b)(a-2b)$$

69)
$$(x-2y)(x-4y)$$

70)
$$(a+3b)(a+7b)$$

71)
$$(4x-1)(x+1)$$

72)
$$(3x-y)(x+4y)$$

73)
$$(x-2)(x-4)$$

74)
$$\left(x + \frac{1}{3}\right)^2$$

75)
$$(2a+7b)^2$$

76)
$$(5x-3y)^2$$

77)
$$(x+3)^2$$

78)
$$(5a-1)^2$$

79)
$$(x-4)^2$$

80)
$$(2x+3y)^2$$

81)
$$\left(x - \frac{5}{2}y\right)^2$$

82)
$$ab(2x-by)^2$$

$$\begin{array}{l} \Longrightarrow \ 4abx^2-4ab^2xy+ab^3y^2=ab\left(4x^2-4bxy+b^2y^2\right)\\ =ab\left(2x-by\right)^2 \end{array}$$