



◇「콘텐츠산업 진흥법 시행령」제33조에 의한 표시

1) 제작연월일 : 2018-03-05

2) 제작자 : 교육지대(주)

3) 이 콘텐츠는 「콘텐츠산업 진흥법」에 따라 최초 제작일부터 5년간 보호됩니다.

◇「콘텐츠산업 진흥법」외에도 「저작권법」에 의하여 보호되는 콘텐츠의 경우, 그 콘텐츠의 전부 또는 일부를 무단으로 복제하거나 전송하는 것은 콘텐츠산업 진흥법 외에도 저작권법에 의한 법적 책임을 질 수 있습니다.

01 곱셈 공식(02) - ①

(1) $(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$,

$(a-b)^3 = a^3 - 3a^2b + 3ab^2 - b^3$

(2) $(a+b)(a^2-ab+b^2) = a^3 + b^3$,

$(a-b)(a^2+ab+b^2) = a^3 - b^3$

■ 곱셈 공식을 이용하여 다음 식을 전개하여라.

1. $(x+1)^3$

2. $(x-1)^3$

3. $(x-3)^3$

4. $(x-2)^3$

5. $(x-5)^3$

6. $(x+2)^3$

7. $(x+3)^3$

8. $(x+4)^3$

9. $(x-4)^3$

10. $(3x+1)^3$

11. $(3x-1)^3$

12. $(2x-3)^3$

13. $(3x-2)^3$

14. $(2x+1)^3$

15. $(3x+2)^3$

16. $(x+y)^3$

17. $(x-2y)^3$

18. $(3x-y)^3$

19. $(x-y)^3$

20. $(x-3y)^3$

21. $(4x - y)^3$

22. $(3x - 4y)^3$

23. $(x + 2y)^3$

24. $(3x + y)^3$

25. $(2x + 3y)^3$

26. $\left(3x + \frac{1}{3}y\right)^3$

▣ 다음 식을 전개하여라.

27. $(3x + 1)(9x^2 - 3x + 1)$

28. $(x + 1)(x^2 - x + 1)$

29. $(2a + 3b)(4a^2 - 6ab + 9b^2)$

30. $(x - 2)(x^2 + 2x + 4)$

31. $(2a - b)(4a^2 + 2ab + b^2)$

32. $(2x - 1)(4x^2 + 2x + 1)$

33. $(x + 2)(x^2 - 2x + 4)$

34. $(x + 1)(x^2 - x + 1)$

35. $(x + y)(x^2 - xy + y^2)$

36. $(x - 2)(x^2 + 2x + 4)$

37. $(x - 3)(x^2 + 3x + 9)$

38. $(3x - 1)(9x^2 + 3x + 1)$

39. $(x - y)(x^2 + xy + y^2)$

40. $(x + 2y)(x^2 - 2xy + 4y^2)$

41. $(a + 2b)(a^2 - 2ab + 4b^2)$

42. $(3a - 4b)(9a^2 + 12ab + 16b^2)$

43. $(3a - 1)(9a^2 + 3a + 1)$

02 곱셈공식(02) - ②

(1) $(a+b+c)^2 = a^2 + b^2 + c^2 + 2(ab+bc+ca)$

(2) $(a^2+ab+b^2)(a^2-ab+b^2) = a^4 + a^2b^2 + b^4$

(3) $(a+b+c)(a^2+b^2+c^2-ab-bc-ca)$
 $= a^3 + b^3 + c^3 - 3abc$

(4) $(x+a)(x+b)(x+c)$
 $= x^3 + (a+b+c)x^2 + (ab+bc+ca)x + abc$

(5) $(x-a)(x-b)(x-c)$
 $= x^3 - (a+b+c)x^2 + (ab+bc+ca)x - abc$

■ 곱셈 공식을 이용하여 다음 식을 전개하여라.

44. $(a+b-c)^2$

45. $(a+b+c)^2$

46. $(a+2b+3c)^2$

47. $(x+y-2z)^2$

48. $(x-3y-2z)^2$

49. $(3x-2y+z)^2$

50. $(x-2y+1)^2$

51. $(x+y+z)^2$

52. $(x+y-z)^2$

53. $(2x+2y-3z)^2$

54. $(x-2y-3z)^2$

55. $(x-y+z)^2$

56. $(a+2b-c)^2$

57. $(x^2+x+1)(x^2-x+1)$

58. $(x^2+xy+y^2)(x^2-xy+y^2)$

59. $(4x^2+6xy+9y^2)(4x^2-6xy+9y^2)$

60. $(x^2+2x+4)(x^2-2x+4)$

61. $(2a+b-c)(4a^2+b^2+c^2-2ab+bc+2ca)$

62. $(x+y+2z)(x^2+y^2+4z^2-xy-2yz-2zx)$

63. $(a+b+c)(a^2+b^2+c^2-ab-bc-ca)$

$$64. (a+b-c)(a^2+b^2+c^2-ab+bc+ca)$$

$$65. (a+b+2c)(a^2+b^2+4c^2-ab-2bc-2ca)$$

$$66. (x+y-1)(x^2+y^2-xy+x+y+1)$$

$$67. (x+y+2)(x^2+y^2-xy-2x-2y+4)$$

03 공통부분이 있는 식의 전개

공통부분을 찾아 치환한 후 여러 가지 곱셈공식을 이용하여 식을 전개한다.

▣ 다음 식을 전개하여라.

$$68. (x+y+5)(x+y-3)$$

$$69. (x^2+x+2)(x^2+x+1)$$

$$70. (x^2-2x-3)(x^2-2x-2)$$

$$71. (x^2+2x+4)(x^2-2x+4)$$

$$72. (4x^2+2xy+y^2)(4x^2-2xy+y^2)$$

$$73. (-x-y+3)(x+y+3)$$

$$74. (x+1)(x+2)(x+3)(x+4)$$

$$75. (x+1)(x-2)(x+3)(x-4)$$

$$76. x(x-1)(x+3)(x-4)$$

$$77. (x-1)(x+2)(x-3)(x+4)$$

$$78. (x-2)(x-1)(x+2)(x+3)$$



정답 및 해설

1) $x^3 + 3x^2 + 3x + 1$

$$\Rightarrow (x+1)^3 = x^3 + 3 \cdot x^2 \cdot 1 + 3 \cdot x \cdot 1^2 + 1^3 \\ = x^3 + 3x^2 + 3x + 1$$

2) $x^3 - 3x^2 + 3x - 1$

$$\Rightarrow (x-1)^3 = x^3 - 3 \cdot x^2 \cdot 1 + 3 \cdot x \cdot 1^2 - 1^3 \\ = x^3 - 3x^2 + 3x - 1$$

3) $x^3 - 9x^2 + 27x - 27$

$$\Rightarrow (x-3)^3 = x^3 + 3 \cdot x^2 \cdot (-3) + 3 \cdot x \cdot (-3)^2 + (-3)^3 \\ = x^3 - 9x^2 + 27x - 27$$

4) $x^3 - 6x^2 + 12x - 8$

$$\Rightarrow (x-2)^3 = x^3 + 3 \cdot x^2 \cdot (-2) + 3 \cdot x \cdot (-2)^2 + (-2)^3 \\ = x^3 - 6x^2 + 12x - 8$$

5) $x^3 - 15x^2 + 75x - 125$

$$\Rightarrow (x-5)^3 = x^3 + 3 \cdot x^2 \cdot (-5) + 3 \cdot x \cdot (-5)^2 + (-5)^3 \\ = x^3 - 15x^2 + 75x - 125$$

6) $x^3 + 6x^2 + 12x + 8$

$$\Rightarrow (x+2)^3 = x^3 + 3 \cdot x^2 \cdot 2 + 3 \cdot x \cdot 2^2 + 2^3 \\ = x^3 + 6x^2 + 12x + 8$$

7) $x^3 + 9x^2 + 27x + 27$

$$\Rightarrow (x+3)^3 = x^3 + 3 \cdot x^2 \cdot 3 + 3 \cdot x \cdot 3^2 + 3^3 \\ = x^3 + 9x^2 + 27x + 27$$

8) $x^3 + 12x^2 + 48x + 64$

$$\Rightarrow (x+4)^3 = x^3 + 3 \cdot x^2 \cdot 4 + 3 \cdot x \cdot 4^2 + 4^3 \\ = x^3 + 12x^2 + 48x + 64$$

9) $x^3 - 12x^2 + 48x - 64$

$$\Rightarrow (x-4)^3 = x^3 + 3 \cdot x^2 \cdot (-4) + 3 \cdot x \cdot (-4)^2 + (-4)^3 \\ = x^3 - 12x^2 + 48x - 64$$

10) $27x^3 + 27x^2 + 9x + 1$

$$\Rightarrow (3x+1)^3 = (3x)^3 + 3 \cdot (3x)^2 \cdot 1 + 3 \cdot 3x \cdot 1^2 + 1^3 \\ = 27x^3 + 27x^2 + 9x + 1$$

11) $27x^3 - 27x^2 + 9x - 1$

$$\Rightarrow (3x-1)^3 \\ = (3x)^3 + 3 \cdot (3x)^2 \cdot (-1) + 3 \cdot 3x \cdot (-1)^2 + (-1)^3 \\ = 27x^3 - 27x^2 + 9x - 1$$

12) $8x^3 - 36x^2 + 54x - 27$

$$\Rightarrow (2x-3)^3 \\ = (2x)^3 + 3 \cdot (2x)^2 \cdot (-3) + 3 \cdot 2x \cdot (-3)^2 + (-3)^3 \\ = 8x^3 - 36x^2 + 54x - 27$$

13) $27x^3 - 54x^2 + 36x - 8$

$$\Rightarrow (3x-2)^3 \\ = (3x)^3 + 3 \cdot (3x)^2 \cdot (-2) + 3 \cdot 3x \cdot (-2)^2 + (-2)^3 \\ = 27x^3 - 54x^2 + 36x - 8$$

14) $8x^3 + 12x^2 + 6x + 1$

$$\Rightarrow (2x+1)^3 = (2x)^3 + 3 \cdot (2x)^2 \cdot 1 + 3 \cdot 2x \cdot 1^2 + 1^3 \\ = 8x^3 + 12x^2 + 6x + 1$$

15) $27x^3 + 54x^2 + 36x + 8$

$$\Rightarrow (3x+2)^3 = (3x)^3 + 3 \cdot (3x)^2 \cdot 2 + 3 \cdot 3x \cdot 2^2 + 2^3 \\ = 27x^3 + 54x^2 + 36x + 8$$

16) $x^3 + 3x^2y + 3xy^2 + y^3$

$$\Rightarrow (x+y)^3 = x^3 + 3 \cdot x^2 \cdot y + 3 \cdot x \cdot y^2 + y^3 \\ = x^3 + 3x^2y + 3xy^2 + y^3$$

17) $x^3 - 6x^2y + 12xy^2 - 8y^3$

$$\Rightarrow (x-2y)^3 = x^3 + 3 \cdot x^2 \cdot (-2y) + 3 \cdot x \cdot (-2y)^2 + (-2y)^3 \\ = x^3 - 6x^2y + 12xy^2 - 8y^3$$

18) $27x^3 - 27x^2y + 9xy^2 - y^3$

$$\Rightarrow (3x-y)^3 \\ = (3x)^3 + 3 \cdot (3x)^2 \cdot (-y) + 3 \cdot 3x \cdot (-y)^2 + (-y)^3 \\ = 27x^3 - 27x^2y + 9xy^2 - y^3$$

19) $x^3 - 3x^2y + 3xy^2 - y^3$

$$\Rightarrow (x-y)^3 = x^3 + 3 \cdot x^2 \cdot (-y) + 3 \cdot x \cdot (-y)^2 + (-y)^3 \\ = x^3 - 3x^2y + 3xy^2 - y^3$$

20) $x^3 - 9x^2y + 27xy^2 - 27y^3$

$$\Rightarrow (x-3y)^3 = x^3 + 3 \cdot x^2 \cdot (-3y) + 3 \cdot x \cdot (-3y)^2 + (-3y)^3 \\ = x^3 - 9x^2y + 27xy^2 - 27y^3$$

21) $64x^3 - 48x^2y + 12xy^2 - y^3$

$$\Rightarrow (4x-y)^3 \\ = (4x)^3 + 3 \cdot (4x)^2 \cdot (-y) + 3 \cdot 4x \cdot (-y)^2 + (-y)^3 \\ = 64x^3 - 48x^2y + 12xy^2 - y^3$$

22) $27x^3 - 108x^2y + 144xy^2 - 64y^3$

23) $x^3 + 6x^2y + 12xy^2 + 8y^3$

$$\Rightarrow (x+2y)^3 = x^3 + 3 \cdot x^2 \cdot 2y + 3 \cdot x \cdot (2y)^2 + (2y)^3 \\ = x^3 + 6x^2y + 12xy^2 + 8y^3$$

24) $27x^3 + 27x^2y + 9xy^2 + y^3$

$$\Rightarrow (3x+y)^3 = (3x)^3 + 3 \cdot (3x)^2 \cdot y + 3 \cdot 3x \cdot y^2 + y^3 \\ = 27x^3 + 27x^2y + 9xy^2 + y^3$$

25) $8x^3 + 36x^2y + 54xy^2 + 27y^3$

$$\Rightarrow (2x+3y)^3 = (2x)^3 + 3 \cdot (2x)^2 \cdot 3y + 3 \cdot 2x \cdot (3y)^2 + (3y)^3 \\ = 8x^3 + 36x^2y + 54xy^2 + 27y^3$$

26) $27x^3 + 9x^2y + xy^2 + \frac{1}{27}y^3$

$$\begin{aligned} \Rightarrow \left(3x + \frac{1}{3}y\right)^3 \\ = (3x)^3 + 3 \cdot (3x)^2 \cdot \frac{1}{3}y + 3 \cdot 3x \cdot \left(\frac{1}{3}y\right)^2 + \left(\frac{1}{3}y\right)^3 \\ = 27x^3 + 9x^2y + xy^2 + \frac{1}{27}y^3 \end{aligned}$$

$$27) 27x^3 + 1$$

$$\begin{aligned} \Rightarrow (3x+1)(9x^2-3x+1) &= (3x+1)\{(3x)^2-3x \cdot 1+1^2\} \\ &= (3x)^3+1^3 \\ &= 27x^3+1 \end{aligned}$$

$$28) x^3+1$$

$$\Rightarrow (x+1)(x^2-x+1) = (x+1)(x^2-x \cdot 1+1^2) = x^3+1$$

$$29) 8a^3+27b^3$$

$$\begin{aligned} \Rightarrow (2a+3b)(4a^2-6ab+9b^2) \\ = (2a+3b)\{(2a)^2-2a \cdot 3b+(3b)^2\} \\ = (2a)^3+(3b)^3 = 8a^3+27b^3 \end{aligned}$$

$$30) x^3-8$$

$$\Rightarrow (x-2)(x^2+2x+4) = (x-2)(x^2+x \cdot 2+2^2) = x^3-8$$

$$31) 8a^3-b^3$$

$$\Rightarrow (2a-b)(4a^2+2ab+b^2) = (2a)^3-b^3 = 8a^3-b^3$$

$$32) 8x^3-1$$

$$\Rightarrow (2x-1)(4x^2+2x+1) = (2x)^3-1^3 = 8x^3-1$$

$$33) x^3+8$$

$$\begin{aligned} \Rightarrow (x+2)(x^2-2x+4) &= (x+2)(x^2-x \cdot 2+2^2) \\ &= x^3+2^3 = x^3+8 \end{aligned}$$

$$34) x^3+1$$

$$\begin{aligned} \Rightarrow (x+1)(x^2-x+1) &= (x+1)(x^2-x \cdot 1+1^2) \\ &= x^3+1^3 = x^3+1 \end{aligned}$$

$$35) x^3+y^3$$

$$\Rightarrow (x+y)(x^2-xy+y^2) = x^3+y^3$$

$$36) x^3-8$$

$$\Rightarrow (x-2)(x^2+2x+4) = x^3-2^3 = x^3-8$$

$$37) x^3-27$$

$$38) 27x^3-1$$

$$\Rightarrow (3x-1)(9x^2+3x+1) = (3x)^3-1^3 = 27x^3-1$$

$$39) x^3-y^3$$

$$\Rightarrow (x-y)(x^2+xy+y^2) = x^3-y^3$$

$$40) x^3+8y^3$$

$$\begin{aligned} \Rightarrow (x+2y)(x^2-2xy+4y^2) &= x^3+(2y)^3 \\ &= x^3+8y^3 \end{aligned}$$

$$41) a^3+8b^3$$

$$\Rightarrow (a+2b)(a^2-2ab+4b^2) = a^3+(2b)^3 = a^3+8b^3$$

$$42) 27a^3-64b^3$$

$$\begin{aligned} \Rightarrow (3a-4b)(9a^2+12ab+16b^2) &= (3a)^3-(4b)^3 \\ &= 27a^3-64b^3 \end{aligned}$$

$$43) 27a^3-1$$

$$\begin{aligned} \Rightarrow (3a-1)(9a^2+3a+1) &= (3a)^3-1^3 \\ &= 27a^3-1 \end{aligned}$$

$$44) a^2+b^2+c^2+2ab-2bc-2ca$$

$$\begin{aligned} \Rightarrow (a+b-c)^2 &= \{a+b+(-c)\}^2 \\ &= a^2+b^2+c^2+2ab-2bc-2ca \end{aligned}$$

$$45) a^2+b^2+c^2+2ab+2bc+2ca$$

$$\begin{aligned} \Rightarrow (a+b+c)^2 &= a^2+b^2+c^2+2(ab+bc+ca) \\ &= a^2+b^2+c^2+2ab+2bc+2ca \end{aligned}$$

$$46) a^2+4b^2+9c^2+4ab+12bc+6ca$$

$$\begin{aligned} \Rightarrow (a+2b+3c)^2 &= a^2+(2b)^2+(3c)^2+2 \cdot a \cdot 2b+2 \cdot 2b \cdot 3c+2 \cdot 3c \cdot a \\ &= a^2+4b^2+9c^2+4ab+12bc+6ca \end{aligned}$$

$$47) x^2+y^2+4z^2+2xy-4yz-4zx$$

$$\begin{aligned} \Rightarrow (x+y-2z)^2 &= \{x+y+(-2z)\}^2 \\ &= x^2+y^2+4z^2+2xy-4yz-4zx \end{aligned}$$

$$48) x^2+9y^2+4z^2-6xy+12yz-4zx$$

$$\begin{aligned} \Rightarrow (x-3y-2z)^2 &= \{x+(-3y)+(-2z)\}^2 \\ &= x^2+9y^2+4z^2-6xy+12yz-4zx \end{aligned}$$

$$49) 9x^2+4y^2+z^2-12xy-4yz+6zx$$

$$\begin{aligned} \Rightarrow (3x-2y+z)^2 &= \{3x+(-2y)+z\}^2 \\ &= 9x^2+4y^2+z^2-12xy-4yz+6zx \end{aligned}$$

$$50) x^2+4y^2-4xy+2x-4y+1$$

$$\begin{aligned} \Rightarrow (x-2y+1)^2 &= \{x+(-2y)+1\}^2 \\ &= x^2+4y^2+1^2-4xy-4y+2x \\ &= x^2+4y^2-4xy+2x-4y+1 \end{aligned}$$

$$51) x^2+y^2+z^2+2xy+2yz+2zx$$

$$\Rightarrow (x+y+z)^2 = x^2+y^2+z^2+2xy+2yz+2zx$$

$$52) x^2+y^2+z^2+2xy-2yz-2zx$$

$$\begin{aligned} \Rightarrow (x+y-z)^2 &= \{z+y+(-z)\}^2 \\ &= x^2+y^2+z^2+2xy-2yz-2zx \end{aligned}$$

$$53) 4x^2+4y^2+9z^2+8xy-12yz-12zx$$

$$\begin{aligned} \Rightarrow (2x+2y-3z)^2 &= \{2x+2y+(-3z)\}^2 \\ &= 4x^2+4y^2+9z^2+8xy-12yz-12zx \end{aligned}$$

$$54) x^2+4y^2+9z^2-4xy+12yz-6zx$$

$$\begin{aligned} \Rightarrow (x-2y-3z)^2 &= \{x+(-2y)+(-3z)\}^2 \\ &= x^2+4y^2+9z^2-4xy+12yz-6zx \end{aligned}$$

$$55) x^2 + y^2 + z^2 - 2xy - 2yz + 2zx$$

$$\Rightarrow (x-y+z)^2 = \{x+(-y)+z\}^2 \\ = x^2 + y^2 + z^2 - 2xy - 2yz + 2zx$$

$$56) a^2 + 4b^2 + c^2 + 4ab - 4bc - 2ca$$

$$\Rightarrow (a+2b-c)^2 \\ = a^2 + (2b)^2 + (-c)^2 + 2 \cdot a \cdot 2b + 2 \cdot 2b \cdot (-c) + 2 \cdot (-c) \cdot a \\ = a^2 + 4b^2 + c^2 + 4ab - 4bc - 2ca$$

$$57) x^4 + x^2 + 1$$

$$\Rightarrow (x^2+x+1)(x^2-x+1) = x^4 + x^2 \cdot 1^2 + 1^4 = x^4 + x^2 + 1$$

$$58) x^4 + x^2y^2 + y^4$$

$$\Rightarrow (x^2+xy+y^2)(x^2-xy+y^2) = x^4 + x^2y^2 + y^4$$

$$59) 16x^4 + 36x^2y^2 + 81y^4$$

$$\Rightarrow (4x^2+6xy+9y^2)(4x^2-6xy+9y^2) \\ = (2x)^4 + (2x)^2 \cdot (3y)^2 + (3y)^4 \\ = 16x^4 + 36x^2y^2 + 81y^4$$

$$60) x^4 + 4x^2 + 16$$

$$\Rightarrow (x^2+2x+4)(x^2-2x+4) = x^4 + x^2 \cdot 2^2 + 2^4 \\ = x^4 + 4x^2 + 16$$

$$61) 8a^3 + b^3 - c^3 + 6abc$$

$$\Rightarrow (2a+b-c)(4a^2+b^2+c^2-2ab+bc+2ca) \\ = (2a)^3 + b^3 + (-c)^3 - 3 \cdot 2a \cdot b \cdot (-c) \\ = 8a^3 + b^3 - c^3 + 6abc$$

$$62) x^3 + y^3 + 8z^3 - 6xyz$$

$$\Rightarrow (x+y+2z)(x^2+y^2+4z^2-xy-2yz-2zx) \\ = x^3 + y^3 + (2z)^3 - 3 \cdot x \cdot y \cdot 2z \\ = x^3 + y^3 + 8z^3 - 6xyz$$

$$63) a^3 + b^3 + c^3 - 3abc$$

$$\Rightarrow (a+b+c)(a^2+b^2+c^2-ab-bc-ca) \\ = a(a^2+b^2+c^2-ab-bc-ca) \\ + b(a^2+b^2+c^2-ab-bc-ca) \\ + c(a^2+b^2+c^2-ab-bc-ca) \\ = a^3+ab^2+ac^2-a^2b-abc-ca^2 \\ + ba^2+b^3+bc^2-ab^2-b^2c-abc \\ + ca^2+cb^2+c^3-abc-bc^2-c^2a \\ = a^3+b^3+c^3-3abc$$

$$64) a^3 + b^3 - c^3 + 3abc$$

$$\Rightarrow (a+b-c)(a^2+b^2+c^2-ab+bc+ca) \\ = a^3+b^3+(-c)^3-3 \cdot a \cdot b \cdot (-c) \\ = a^3+b^3-c^3+3abc$$

$$65) a^3 + b^3 + 8c^3 - 6abc$$

$$\Rightarrow (a+b+2c)(a^2+b^2+4c^2-ab-2bc-2ca) \\ = (a+b+2c)\{a^2+b^2+(2c)^2-ab-b \cdot 2c-2c \cdot a\} \\ = a^3+b^3+(2c)^3-3 \cdot a \cdot b \cdot 2c$$

$$= a^3+b^3+8c^3-6abc$$

$$66) x^3 + y^3 + 3xy - 1$$

$$\Rightarrow (x+y-1)(x^2+y^2-xy+x+y+1) \\ = x^3+y^3+(-1)^3-3 \cdot x \cdot y \cdot (-1) \\ = x^3+y^3+3xy-1$$

$$67) x^3 + y^3 - 6xy + 8$$

$$\Rightarrow (x+y+2)(x^2+y^2-xy-2x-2y+4) \\ = (x+y+2)(x^2+y^2+2^2-xy-2y-2x) \\ = x^3+y^3+2^3-3 \cdot x \cdot y \cdot 2 \\ = x^3+y^3-6xy+8$$

$$68) x^2 + 2xy + y^2 + 2x + 2y - 15$$

$$\Rightarrow (x+y+5)(x+y-3) \text{에서 } x+y=t \text{로 치환하면} \\ (t+5)(t-3) = t^2+2t-15 \text{이다.}$$

$x+y=t$ 를 위 식에 대입하고 전개하면

$$(x+y)^2+2(x+y)-15 = x^2+2xy+y^2+2x+2y-15 \\ \text{가 성립한다.}$$

$$69) x^4 + 2x^3 + 4x^2 + 3x + 2$$

$$\Rightarrow x^2+x=t \text{로 치환하면} \\ (x^2+x+2)(x^2+x+1) \\ = (t+2)(t+1) = t^2+3t+2 \\ t=x^2+x \text{를 대입하면} \\ = (x^2+x)^2+3(x^2+x)+2 \\ = x^4+2x^3+x^2+3x^2+3x+2 \\ = x^4+2x^3+4x^2+3x+2$$

$$70) x^4 - 4x^3 - x^2 + 10x + 6$$

$$\Rightarrow x^2-2x=A \text{로 치환하면} \\ (x^2-2x-3)(x^2-2x-2) \\ = (A-3)(A-2) \\ = A^2-5A+6 \\ = (x^2-2x)^2-5(x^2-2x)+6 \\ = x^4-4x^3-x^2+10x+6$$

$$71) x^4 + 4x^2 + 16$$

$$\Rightarrow (x^2+2x+4)(x^2-2x+4) \text{에서 } x^2+4=t \text{로 치환하면} \\ (x^2+2x+4)(x^2-2x+4) = (t+2x)(t-2x) \\ = t^2-4x^2 \\ = (x^2+4)^2-4x^2 \\ = (x^4+8x^2+16)-4x^2 \\ = x^4+4x^2+16$$

$$72) 16x^4 + 4x^2y^2 + y^4$$

$$\Rightarrow (4x^2+2xy+y^2)(4x^2-2xy+y^2) \\ = (2x)^4 + (2x)^2y^2 + y^4 \\ = 16x^4 + 4x^2y^2 + y^4$$

$$73) -x^2 - 2xy - y^2 + 9$$

$$\Rightarrow (-x-y+3)(x+y+3) = -(x+y-3)(x+y+3) \text{에서} \\ x+y=t \text{로 치환하면}$$

$$\begin{aligned}
 -(x+y-3)(x+y+3) &= -(t-3)(t+3) \\
 &= -t^2 + 9 \\
 &= -(x+y)^2 + 9 \\
 &= -(x^2 + 2xy + y^2) + 9 \\
 &= -x^2 - 2xy - y^2 + 9
 \end{aligned}$$

$$74) x^4 + 10x^3 + 35x^2 + 50x + 24$$

$$\begin{aligned}
 \Rightarrow (x+1)(x+2)(x+3)(x+4) \\
 &= (x+1)(x+4)(x+2)(x+3) \\
 &= (x^2 + 5x + 4)(x^2 + 5x + 6) \\
 &= (t+4)(t+6) \leftarrow x^2 + 5x = t \text{로 치환} \\
 &= t^2 + 10t + 24 \\
 &= (x^2 + 5x)^2 + 10(x^2 + 5x) + 24 \leftarrow t = x^2 + 5x \text{를 대입} \\
 &= x^4 + 10x^3 + 25x^2 + 10x^2 + 50x + 24 \\
 &= x^4 + 10x^3 + 35x^2 + 50x + 24
 \end{aligned}$$

$$75) x^4 - 2x^3 - 13x^2 + 14x + 24$$

$$\begin{aligned}
 \Rightarrow (x+1)(x-2)(x+3)(x-4) \\
 &= \{(x+1)(x-2)\}\{(x+3)(x-4)\} \\
 &= (x^2 - x - 2)(x^2 - x - 12) \\
 &\text{위 식에서 } x^2 - x = A \text{로 치환하면} \\
 &(A-2)(A-12) = A^2 - 14A + 24 \\
 &= (x^2 - x)^2 - 14(x^2 - x) + 24 \\
 &= x^4 - 2x^3 + x^2 - 14x^2 + 14x + 24 \\
 &= x^4 - 2x^3 - 13x^2 + 14x + 24
 \end{aligned}$$

$$76) x^4 - 2x^3 - 11x^2 + 12x$$

$$\begin{aligned}
 \Rightarrow x(x-1)(x+3)(x-4) \\
 &= (x^2 - x)(x^2 - x - 12) \\
 &= t(t-12) \leftarrow x^2 - x = t \text{로 치환} \\
 &= t^2 - 12t \\
 &= (x^2 - x)^2 - 12(x^2 - x) \leftarrow t = x^2 - x \text{를 대입} \\
 &= x^4 - 2x^3 + x^2 - 12x^2 + 12x \\
 &= x^4 - 2x^3 - 11x^2 + 12x
 \end{aligned}$$

$$77) x^4 + 2x^3 - 13x^2 - 14x + 24$$

$$\begin{aligned}
 \Rightarrow (x-1)(x+2)(x-3)(x+4) \\
 &= (x^2 + x - 2)(x^2 + x - 12) \\
 &= (t-2)(t-12) \leftarrow x^2 + x = t \text{로 치환} \\
 &= t^2 - 14t + 24 \\
 &= (x^2 + x)^2 - 14(x^2 + x) + 24 \leftarrow t = x^2 + x \text{를 대입} \\
 &= x^4 + 2x^3 + x^2 - 14x^2 - 14x + 24 \\
 &= x^4 + 2x^3 - 13x^2 - 14x + 24
 \end{aligned}$$

$$78) x^4 + 2x^3 - 7x^2 - 8x + 12$$

$$\begin{aligned}
 \Rightarrow (x-2)(x-1)(x+2)(x+3) \\
 &= \{(x-2)(x+3)\}\{(x-1)(x+2)\} \\
 &= (x^2 + x - 6)(x^2 + x - 2) \\
 &x^2 + x - 2 = A \text{로 치환하면} \\
 &= A(A-4) = A^2 - 4A \\
 &= (x^2 + x - 2)^2 - 4(x^2 + x - 2) \\
 &= x^4 + 2x^3 - 7x^2 - 8x + 12
 \end{aligned}$$