

# 수학 계산력 강화

#### (5)다항식의 나눗셈





◇「콘텐츠산업 진흥법 시행령」제33조에 의한 표시

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3) 이 콘텐츠는 「콘텐츠산업 진흥법」에 따라 최초 제작일부터 5년간 보호됩니다.

◇「콘텐츠산업 진흥법」외에도「저작권법」에 의하여 보호 되는 콘텐츠의 경우, 그 콘텐츠의 전부 또는 일부를 무 단으로 복제하거나 전송하는 것은 콘텐츠산업 진흥법 외에도 저작권법에 의한 법적 책임을 질 수 있습니다.

# 01 / 다항식의 나눗셈

1. (다항식)÷(단항식)의 꼴

$$(A+B) \div M = (A+B) \times \frac{1}{M} = \frac{A}{M} + \frac{B}{M}$$

2. (다항식)÷(다항식)의 꼴

두 다항식을 내림차순으로 정리한 다음 자연수의 나눗셈과 같은 방법으로 직접 나누어 몫과 나머지를 구한다. 이때 나머지의 차수가 나누는 식의 차수보다 작을 때까지 나눈다.

#### ☑ 다음 식을 계산하여라.

**1.** 
$$(a^4b^3 - 3a^2b^4) \div \left(-\frac{1}{2}ab^2\right)^2$$

**2.** 
$$\left(-\frac{1}{4}a^2b + ab^2 + 3ab\right) \div \frac{1}{4}ab$$

**3.** 
$$(4xy + xy^2 - 2x^2y) \div \left(-\frac{1}{3}xy\right)$$

**4.** 
$$(2ab^2-4a^2b+6a) \div (-2a)$$

**5.** 
$$(8ab^2+4ab) \div 2a$$

**6.** 
$$\left(\frac{1}{2}x^4y^3 - \frac{1}{3}xy^2\right) \div \left(-\frac{1}{6}xy^2\right)$$

7. 
$$\{6ab^2 + (2a^2b)^2\} \div \frac{2}{3}ab^2$$

**8.** 
$$(24x^2 - 18x^3) \div \frac{6x^2}{5}$$

**9.** 
$$(x^5y^2 - 2x^2y^5) \div \left(-\frac{1}{2}xy\right)^2$$

**10.** 
$$(8x^2 - 4xy) \div \frac{1}{2}x$$

**11.** 
$$(5xyz+10x^2y^2z) \div 5x$$

**12.** 
$$(2x^2z - 8x^2yz) \div 2xz$$

**13.** 
$$(6x^2yz - 15xz) \div 3xz$$

**14.** 
$$(12a^2bc^2 - 9ab^2c + 24abc^3) \div 3abc$$

**15.** 
$$(-12a^3b^2c^3 + 4ab^2c + 8ab^2c^2) \div (-4b^2c)$$

**16.** 
$$(x^2z^3+xy^3z^2) \div \frac{x}{y^2z^4}$$

**17.** 
$$(4xyz-6x^2yz) \div 2xy$$

**18.** 
$$(9a^3b^2c - abc - 3ab^2c) \div 3abc$$

**19.** 
$$(-4xyz+12x^2y^2z) \div (-4xy)$$

**20.** 
$$\left(\frac{2}{3}x^2y - \frac{xy}{3}\right) \div \frac{2}{3}x$$

**21.** 
$$(-xy+y^2) \div \left(-\frac{1}{5}y\right) - (12x^2 + 15xy) \div 3x$$

**22.** 
$$2x(4x-7y)-(8x^2y^2-4x^3y)\div \frac{2}{3}xy$$

**23.** 
$$(9a^2 - 48ab) \div (-3a) - (36b^2 - 16ab) \div 4b$$

**24.** 
$$-3a^2(2ab^2+b)-(12a^4b^2-8a^2b)\div 4a^2b$$

**25.** 
$$(9x^2+6xy) \div (-3x) - (12xy-16y^2) \div 2y$$

## ☑ 다음을 계산하여 몫과 나머지를 각각 구하여라.

**26.** 
$$(3x^3-11x^2+5) \div (3x-2)$$

**27.** 
$$(3x^3+5x^2+x-7) \div (3x-1)$$

**28.** 
$$(x^3-2x^2+5) \div (x-3)$$

**29.** 
$$(2x^3+x^2-7x+4) \div (2x-1)$$

**30.** 
$$(2x^3+x^2-3x-5) \div (x+1)$$

**31.** 
$$(15x^3 - 23x^2 + 6) \div (3x - 1)$$

**32.** 
$$(2x^3-5x^2+4) \div (x^2-2x-3)$$

**33.** 
$$(2x^3+x^2-3x+1) \div (x^2-2x+3)$$

**34.** 
$$(3x^3-5x^2+4x-7) \div (x^2+2)$$

**35.** 
$$(-2x^3+x^2-x+1) \div (x^2+1)$$

**36.** 
$$(2x^3+2x^2-x+4) \div (x^2-2x+2)$$

**37.** 
$$(4x^3+5x^2-3x-1) \div (x^2+2x-3)$$

**38.** 
$$(2x^3-7x-2) \div (x^2+3x+1)$$

**39.** 
$$(2x^3-3x^2+4x+1) \div (x^2-x-2)$$

### ☑ 다음 나눗셈을 하여 몫과 나머지를 구하여라.

**40.** 
$$x+1$$
) $x^3-3x^2+4x+1$ 

**41.** 
$$x+1\overline{\smash)x^2+3x+1}$$

**42.** 
$$x+1$$
) $x^3+2x^2-5x+2$ 

**43.** 
$$-x-1\overline{\smash{\big)}\,2x^2-4x+5}$$

**44.** 
$$3x+2$$
)  $6x^2+5x-1$ 

**45.** 
$$x+1)$$
  $-5x^2-3x-1$ 

**46.** 
$$x+2)\overline{4x^3-x^2+5x+6}$$

**47.** 
$$x-2)\overline{)2x^3+3x^2+4x+5}$$

**48.** 
$$x-1)-2x^3-4x^2+3x+2$$

**49.** 
$$x^2 + x + 1 \overline{)x^3 + 2x^2 + 3x + 3}$$

**50.** 
$$x^2-x+2)\overline{)2x^3-x^2+3x-8}$$

**51.** 
$$x^2 + 2x - 1$$
  $x^3 + 5x^2 - 3x + 2$ 

**52.** 
$$2x^2+2x-1$$
  $\overline{\smash{\big)}\,4x^3+2x^2-3x+6}$ 

**53.** 
$$x^2 - 2x - 1) \overline{4x^3 - x^2 - 2x + 6}$$

# 02 / 다항식의 나눗셈의 성질

다항식 A를 다항식  $B(B \neq 0)$ 로 나누었을 때의 몫을 Q, 나머지를 R라고 하면

A = BQ + R (단, R의 차수는 B의 차수보다 낮다.) 가 성립한다.

특히 R=0일 때, A는 B로 나누어떨어진다고 한다.

- $\blacksquare$  다음 두 다항식 A,B에 대하여 A를 B로 나누었을 때의 몫 Q와 나머지 R를 구하여 A = BQ + R 꼴로 나타내어라.
- **54.**  $A = 2x^2 5x + 3, B = x + 1$
- **55.**  $A = x^3 + 3x^2 x + 2, B = x 1$
- **56.**  $A = 2x^3 3x^2 + x 3, B = x 2$
- **57.**  $A = -x^2 + 2x + 5, B = x + 2$
- **58.**  $A = 2x^3 + x^2 7x + 7$ , B = 2x 1
- **59.**  $A = 2x^3 + x^2 x + 1, B = x^2 + 1$

**60.** 
$$A = 4x^3 + 3x + 2$$
,  $B = x^2 - 2x + 3$ 

**61.** 
$$A = 4x^3 - x + 2, B = 2x^2 + x + 2$$

**62.** 
$$A = 3x^3 + x^2 - 3x + 3$$
,  $B = x^2 - x + 1$ 

**63.** 
$$A = x^3 - 3x^2 + x - 3, B = x^2 - 2x - 1$$

**64.** 
$$A = x^3 + 2x^2 + x + 1, B = x^2 + x + 2$$

**65.** 
$$A = x^3 + 2x - 1, B = x^2 + 2x - 1$$

**66.** 
$$A = 3x^3 + 3x^2 - 2x + 2, B = x^2 - x + 2$$

**67.** 
$$A = 3x^3 - x^2 + 4x + 3$$
,  $B = x^2 + 2$ 

**68.** 
$$A = 2x^3 + 2x^2 - x + 1$$
,  $B = x^2 - x + 1$ 

## 정답 및 해설

1) 
$$\frac{4a^2}{b}$$
 - 12

$$\begin{split} \Leftrightarrow & (a^4b^3 - 3a^2b^4) \div \left( -\frac{1}{2}ab^2 \right)^2 = (a^4b^3 - 3a^2b^4) \div \left( \frac{1}{4}a^2b^4 \right) \\ & = (a^4b^3 - 3a^2b^4) \times \frac{4}{a^2b^4} \\ & = \frac{4a^2}{b} - 12 \end{split}$$

2) 
$$-a+4b+12$$

$$\begin{split} & \Leftrightarrow \left( -\frac{1}{4}a^2b + ab^2 + 3ab \right) \div \frac{1}{4}ab \\ & = \left( -\frac{1}{4}a^2b + ab^2 + 3ab \right) \times \frac{4}{ab} = -a + 4b + 12 \end{split}$$

3) 
$$6x - 3y - 12$$

$$\Rightarrow (4xy + xy^2 - 2x^2y) \div \left(-\frac{1}{3}xy\right)$$
$$= (4xy + xy^2 - 2x^2y) \times \left(-\frac{3}{xy}\right) = 6x - 3y - 12$$

4) 
$$-b^2 + 2ab - 3$$

5) 
$$4b^2 + 2b$$

6) 
$$-3x^3y+2$$

$$\Rightarrow \left(\frac{1}{2}x^4y^3 - \frac{1}{3}xy^2\right) \div \left(-\frac{1}{6}xy^2\right)$$

$$= \left(\frac{1}{2}x^4y^3 - \frac{1}{3}xy^2\right) \times \left(-\frac{6}{xy^2}\right)$$

$$= \frac{1}{2}x^4y^3 \times \left(-\frac{6}{xy^2}\right) - \frac{1}{3}xy^2 \times \left(-\frac{6}{xy^2}\right)$$

$$= -3x^3y + 2$$

7) 
$$9+6a^3$$

$$\Leftrightarrow \{6ab^2 + (2a^2b)^2\} \div \frac{2}{3}ab^2$$
$$= (6ab^2 + 4a^4b^2) \times \frac{3}{2ab^2} = 9 + 6a^3$$

8) 
$$20-15x$$

$$\Rightarrow (24x^2 - 18x^3) \div \frac{6x^2}{5}$$
$$= (24x^2 - 18x^3) \times \frac{5}{6x^2} = 20 - 15x$$

9) 
$$4x^3 - 8u^3$$

$$\Rightarrow (x^5y^2 - 2x^2y^5) \div \left(-\frac{1}{2}xy\right)^2$$

$$= (x^5y^2 - 2x^2y^5) \div \frac{1}{4}x^2y^2$$

$$= (x^5y^2 - 2x^2y^5) \times \frac{4}{x^2y^2} = 4x^3 - 8y^3$$

10) 
$$16x - 8y$$

$$\Rightarrow (8x^2 - 4xy) \div \frac{1}{2}x = (8x^2 - 4xy) \times \frac{2}{x} = 16x - 8y$$

11) 
$$yz + 2xy^2z$$

$$\Rightarrow (5xyz + 10x^2y^2z) \div 5x$$

$$= \frac{5xyz + 10x^2y^2z}{5x}$$

$$= \frac{5xyz}{5x} + \frac{10x^2y^2z}{5x} = yz + 2xy^2z$$

12) 
$$x - 4xy$$

$$\Rightarrow (2x^2z - 8x^2yz) \div 2xz$$

$$= \frac{2x^2z}{2xz} - \frac{8x^2yz}{2xz} = x - 4xy$$

13) 
$$2xy-5$$

14) 
$$4ac - 3b + 8c^2$$

15) 
$$3a^3c^2 - a - 2ac$$

$$\begin{array}{l} \Leftrightarrow \ (-12a^3b^2c^3 + 4ab^2c + 8ab^2c^2) \div (-4b^2c) \\ = \frac{-12a^3b^2c^3}{-4b^2c} + \frac{4ab^2c}{-4b^2c} + \frac{8ab^2c^2}{-4b^2c} = 3a^3c^2 - a - 2ac \end{array}$$

16) 
$$xy^2z^7 + y^5z^6$$

$$\Rightarrow (x^2z^3 + xy^3z^2) \div \frac{x}{y^2z^4}$$
$$= (x^2z^3 + xy^3z^2) \times \frac{y^2z^4}{x} = xy^2z^7 + y^5z^6$$

17) 
$$2z - 3xz$$

$$\Rightarrow (4xyz - 6x^2yz) \div 2xy$$

$$= \frac{4xyz - 6x^2yz}{2xy}$$

$$= \frac{4xyz}{2xy} - \frac{6x^2yz}{2xy} = 2z - 3xz$$

18) 
$$3a^2b - \frac{1}{3} - b$$

$$\begin{array}{l} \Longrightarrow \ (9a^3b^2c - abc - 3ab^2c) \div 3abc \\ = \frac{9a^3b^2c}{3abc} - \frac{abc}{3abc} - \frac{3ab^2c}{3abc} = 3a^2b - \frac{1}{3} - b \end{array}$$

19) 
$$z - 3xyz$$

$$\Rightarrow (-4xyz + 12x^2y^2z) \div (-4xy) = \frac{-4xyz}{-4xy} + \frac{12x^2y^2z}{-4xy} = z - 3xyz$$

20) 
$$xy - \frac{y}{2}$$

$$\Rightarrow \left(\frac{2}{3}x^2y - \frac{xy}{3}\right) \div \frac{2}{3}x = \left(\frac{2}{3}x^2y - \frac{xy}{3}\right) \times \frac{3}{2x} = xy - \frac{y}{2}$$

21) 
$$x - 10y$$

$$\Rightarrow (-xy+y^2) \div \left(-\frac{1}{5}y\right) - (12x^2 + 15xy) \div 3x$$
$$= (-xy+y^2) \times \left(-\frac{5}{y}\right) - (12x^2 + 15xy) \times \frac{1}{3x}$$

$$=5x-5y-4x-5y$$
$$=x-10y$$

22) 
$$14x^2 - 26xy$$

$$\Rightarrow 2x(4x-7y) - (8x^2y^2 - 4x^3y) \div \frac{2}{3}xy$$

$$= 8x^2 - 14xy - (8x^2y^2 - 4x^3y) \times \frac{3}{2xy}$$

$$= 8x^2 - 14xy - 12xy + 6x^2$$

$$= 14x^2 - 26xy$$

23) 
$$a + 7b$$

$$\Rightarrow (9a^2 - 48ab) \div (-3a) - (36b^2 - 16ab) \div 4b$$
  
= -3a + 16b - 9b + 4a = a + 7b

24) 
$$-6a^3b^2-6a^2b+2$$

$$\Rightarrow -3a^2(2ab^2+b) - (12a^4b^2 - 8a^2b) \div 4a^2b$$
  
=  $-6a^3b^2 - 3a^2b - 3a^2b + 2 = -6a^3b^2 - 6a^2b + 2$ 

25) 
$$-9x+6y$$

$$\Rightarrow (9x^2 + 6xy) \div (-3x) - (12xy - 16y^2) \div 2y$$
  
= -3x - 2y - 6x + 8y = -9x + 6y

26) 몫 : 
$$x^2-3x-2$$
, 나머지 : 1

$$\begin{array}{c}
x^2 - 3x - 2 \\
3x - 2)3x^3 - 11x^2 + 5 \\
\underline{3x^3 - 2x^2} \\
-9x^2 \\
\underline{-9x^2 + 6x} \\
-6x + 5 \\
\underline{-6x + 4} \\
1
\end{array}$$

∴ 몫 : 
$$x^2 - 3x - 2$$
 , 나머지 : 1

27) 몫: 
$$x^2 + 2x + 1$$
, 나머지:  $-6$ 

⇒ 
$$3x^3 + 5x^2 + x - 7$$
을  $3x - 1$ 로 나누면  $3x^3 + 5x^2 + x - 7 = (3x - 1)(x^2 + 2x + 1) - 6$ 이므로

몫은  $x^2 + 2x + 1$ 이다.

28) 몫:
$$x^2 + x + 3$$
, 나머지:14

$$x - 3) x^{3} - 2x^{2} + 5$$

$$x^{3} - 3x^{2}$$

$$x^{2}$$

$$x^{2}$$

$$x^{2}$$

$$x^{2} - 3x$$

$$3x + 5$$

$$3x - 9$$

$$\therefore$$
 몫: $x^2 + x + 3$ , 나머지:14

29) 몫: 
$$x^2+x-3$$
, 나머지: 1

$$\begin{array}{c} \Rightarrow & \underline{x^2 + x - 3} \\ 2x - 1)2x^3 + x^2 - 7x + 4 \\ \underline{2x^3 - x^2} \\ 2x^2 - 7x \\ \underline{2x^2 - 7x} \\ \underline{-6x + 4} \\ \underline{-6x + 3} \\ 1 \end{array}$$

따라서 몫은  $x^2+x-3$  이고, 나머지는 1 이다.

30) 몫: 
$$2x^2 - x - 2$$
, 나머지:  $-3$ 

31) 몫 : 
$$5x^2-6x-2$$
.나머지 : 4

32) 몫: 
$$2x-1$$
, 나머지:  $4x+1$ 

$$\therefore$$
 몫 :  $2x + 5$ , 나머지 :  $x - 14$ 

34) 몫: 
$$3x-5$$
, 나머지:  $-2x+3$ 

⇒  $3x^3-5x^2+4x-7$ 을  $x^2+2$ 로 나누면

 $3x^3-5x^2+4x-7=(x^2+2)(3x-5)-2x+3$ 이므로

몫은  $3x-5$ 이고 나머지는  $-2x+3$ 이다.

$$x^{2}+1 \frac{-2x+1}{-2x^{3}+x^{2}-x+1} \frac{-2x^{3}-2x}{x^{2}+x+1} \frac{x^{2}+x+1}{x^{2}+1}$$

$$\therefore$$
 몫 : $-2x+1$ , 나머지 :  $x$ 

36) 몫 : 
$$2x+6$$
, 나머지 :  $7x-8$ 

$$\Rightarrow 2x^3+2x^2-x+4 \equiv x^2-2x+2$$
로 나누면 
$$2x^3+2x^2-x+4=(2x+6)(x^2-2x+2)+7x-8$$
에서 몫은  $2x+6$ 이고 나머지는  $7x-8$ 이다.

37) 몫:
$$4x-3$$
, 나머지: $15x-10$ 

$$x^2 + 2x - 3$$
)  $4x^3 + 5x^2 - 3x - 1$   $\frac{4x^3 + 8x^2 - 12x}{-3x^2 + 9x - 1}$   $\rightarrow$   $\frac{-3x^2 - 6x + 9}{15x - 10}$  : 몫: $4x - 3$ , 나머

[5] : 15x - 10

38) 몫:2x-6, 나머지:9x+4

$$\begin{array}{r}
2x - 6 \\
x^2 + 3x + 1 ) 2x^3 - 7x - 2 \\
2x^3 + 6x^2 + 2x \\
- 6x^2 - 9x - 2 \\
- 6x^2 - 18x - 6 \\
9x + 4
\end{array}$$

 $\therefore$ 몫:2x-6, 나머지:9x+4

39) 몫: 
$$2x-1$$
 나머지:  $7x-1$ 

$$\Rightarrow 2x^3 - 3x^2 + 4x + 1$$
을  $x^2 - x - 2$ 로 나누면 
$$2x^3 - 3x^2 + 4x + 1 = (2x - 1)(x^2 - x - 2) + 7x - 1$$

40) 몫:
$$x^2 - 4x + 8$$
, 나머지: $-7$ 

$$\begin{array}{r} x^2 - 4x + 8 \\ x + 1)x^3 - 3x^2 + 4x + 1 \\ \underline{x^3 + x^2} \\ -4x^2 + 4x \\ \underline{-4x^2 - 4x} \\ 8x + 1 \\ \underline{8x + 8} \\ -7 \end{array}$$

41) 몫: x+2, 나머지:-1

$$\begin{array}{c} \Rightarrow \quad \underline{x+2} \\ x+1)x^2+3x+1 \\ \underline{x^2+x} \\ \underline{2x+1} \\ \underline{2x+2} \\ -1 \end{array}$$

42) 몫:
$$x^2+x-6$$
, 나머지:8

$$\begin{array}{c} \Rightarrow & \frac{x^2 + x - 6}{x + 1)x^3 + 2x^2 - 5x + 2} \\ & \frac{x^3 + x^2}{x^2 - 5x} \\ & \frac{x^2 - 5x}{x^2 + x} \\ & \frac{-6x + 2}{-6x - 6} \\ & 8 \end{array}$$

43) 몫:-2x+6, 나머지:11

44) 몫:
$$2x + \frac{1}{3}$$
, 나머지: $-\frac{5}{3}$ 

$$\Rightarrow \frac{2x + \frac{1}{3}}{3x + 2)} \xrightarrow{6x^2 + 5x - 1} \xrightarrow{6x^2 + 4x} \xrightarrow{x - 1} \xrightarrow{x + \frac{2}{3}} -\frac{5}{3}$$

45) 몫:-5x+2, 나머지:-3

$$\Rightarrow \frac{-5x+2}{x+1)-5x^2-3x-1} \\ -5x^2-5x \\ 2x-1 \\ 2x+2 \\ -3$$

46) 몫:4x²-9x+23, 나머지:-40

$$\begin{array}{c} \Leftrightarrow & \frac{4x^2 - 9x + 23}{x + 2)4x^3 - x^2 + 5x + 6} \\ & \underline{4x^3 + 8x^2} \\ \hline & -9x^2 + 5x \\ \underline{-9x^2 - 18x} \\ & \underline{23x + 6} \\ \underline{-23x + 46} \\ & -40 \end{array}$$

47) 몫:  $2x^2 + 7x + 18$ , 나머지: 41

48) 몫:
$$-2x^2-6x-3$$
, 나머지: $-1$ 

49) 몫: x+1 나머지: x+2

$$x+1 \leftarrow \frac{x}{3}$$

$$x^2+x+1)x^3+2x^2+3x+3$$

$$x^3+x^2+x$$

$$x^2+2x+3$$

$$x^2+x+1$$

$$x+2 \leftarrow$$

50) 몫: 2x+1, 나머지: -10

$$\Rightarrow 2x^3 - x^2 + 3x - 8 = x^2 - x + 2$$
로 나누면  
$$2x^3 - x^2 + 3x - 8 = (x^2 - x + 2)(2x + 1) - 10$$

51) 몫: x+3 나머지: -8x+5

52) 몫:
$$2x-1$$
 나머지: $x+5$ 

53) 몫:
$$4x+7$$
 나머지: $16x+13$ 

$$\begin{array}{c} \Leftrightarrow & \underbrace{4x + 7 \Leftarrow \frac{\Box}{\Box}} \\ x^2 - 2x - 1)4x^3 - x^2 - 2x + 6 \\ \underline{4x^3 - 8x^2 - 4x} \\ \hline & 7x^2 + 2x + 6 \\ \underline{-7x^2 - 14x - 7} \\ \hline & 16x + 13 \Leftarrow \downarrow 먼지$$

54) 
$$2x^2 - 5x + 3 = (x+1)(2x-7) + 10$$

다 
$$\frac{2x-7}{x+1)2x^2-5x+3}$$
  $\stackrel{\mathbb{R}}{\rightleftharpoons}$   $\frac{2x^2+2x}{-7x+3}$   $\stackrel{}{\rightleftharpoons}$   $2x\times(x+1)$   $\frac{2x^2+2x}{-7x-7}$   $\stackrel{}{\Leftarrow}$   $-7\times(x+1)$   $\stackrel{}{\rightleftharpoons}$  나머지

$$\therefore 2x^2 - 5x + 3 = (x+1)(2x-7) + 10$$

55) 
$$x^3 + 3x^2 - x + 2 = (x - 1)(x^2 + 4x + 3) + 5$$

$$\Rightarrow \frac{x^{2}+4x+3}{x-1)x^{3}+3x^{2}-x+2}$$

$$\frac{x^{3}-x^{2}}{4x^{2}-x+2}$$

$$\frac{4x^{2}-x+2}{3x+2}$$

$$\frac{3x+2}{5}$$

$$\therefore x^3 + 3x^2 - x + 2 = (x - 1)(x^2 + 4x + 3) + 5$$

56) 
$$2x^3 - 3x^2 + x - 3 = (x - 2)(2x^2 + x + 3) + 3$$

$$\begin{array}{c}
\Rightarrow & 2x^2 + x + 3 \\
x - 2) \overline{\smash{\big)}\ 2x^3 - 3x^2 + x - 3} \\
\underline{2x^3 - 4x^2} \\
x^2 + x - 3 \\
\underline{x^2 - 2x} \\
3x - 3 \\
3x - 6 \\
3
\end{array}$$

$$\therefore 2x^3 - 3x^2 + x - 3 = (x - 2)(2x^2 + x + 3) + 3$$

57) 
$$-x^2+2x+5=(x+2)(-x+4)-3$$

$$\Rightarrow \frac{-x+4}{x+2)-x^2+2x+5}$$

$$\frac{-x^2-2x}{4x+5}$$

$$\frac{4x+8}{-3}$$

$$\therefore -x^2 + 2x + 5 = (x+2)(-x+4) - 3$$

58) 
$$2x^3 + x^2 - 7x + 7 = (2x - 1)(x^2 + x - 3) + 4$$

$$\begin{array}{r}
x^2 + x - 3 \\
2x - 1 \overline{\smash{\big)}\ 2x^3 + x^2 - 7x + 7} \\
\underline{2x^3 - x^2} \\
2x^2 - 7x \\
\underline{2x^2 - 7x} \\
\underline{-6x + 7} \\
\underline{-6x + 3} \\
4
\end{array}$$

$$\therefore 2x^3 + x^2 - 7x + 7 = (2x - 1)(x^2 + x - 3) + 4$$

59) 
$$2x^3 + x^2 - x + 1 = (x^2 + 1)(2x + 1) - 3x$$

$$\Rightarrow \frac{2x+1}{x^2+1} = \frac{2x^3+x^2-x+1}{2x^3+2x} = \frac{x^2-3x+1}{x^2-3x} = \frac{x^2-3x+1}{-3x}$$

$$\therefore 2x^3 + x^2 - x + 1 = (x^2 + 1)(2x + 1) - 3x$$

60) 
$$(x^2-2x+3)(4x+8)+7x-22$$

$$4x^3 + 3x + 2 = (x^2 - 2x + 3)(4x + 8) + 7x - 22$$
이므로  
 $Q = 4x + 8$   $R = 7x - 22$ 이다.

61) 
$$4x^3 - x + 2 = (2x^2 + x + 2)(2x - 1) + (-4x + 4)$$

$$\Rightarrow \frac{2x-1}{2x^2+x+2)4x^3 - x + 2} \\ \frac{4x^3+2x^2+4x}{-2x^2-5x+2} \\ \frac{-2x^2-x-2}{-4x+4}$$

$$\therefore 4x^3 - x + 2 = (2x^2 + x + 2)(2x - 1) + (-4x + 4)$$

62) 
$$(x^2-x+1)(3x+4)-2x-1$$

$$3x^3 + x^2 - 3x + 3 = (x^2 - x + 1)(3x + 4) - 2x - 1$$

63) 
$$x^3 - 3x^2 + x - 3 = (x^2 - 2x - 1)(x - 1) - 4$$

$$\begin{array}{c}
x - 1 \\
x^2 - 2x - 1 \overline{\smash)x^3 - 3x^2 + x - 3} \\
\underline{x^3 - 2x^2 - x} \\
-x^2 + 2x - 3 \\
\underline{-x^2 + 2x + 1} \\
-4
\end{array}$$

$$\therefore x^3 - 3x^2 + x - 3 = (x^2 - 2x - 1)(x - 1) - 4$$

64) 
$$(x^2+x+2)(x+1)+(-2x-1)$$

$$\Rightarrow \frac{x+1}{x^2+x+2} \stackrel{\longleftarrow}{=} Q$$

$$x^2+x+2)x^3+2x^2+x+1$$

$$x^3+x^2+2x$$

$$x^2-x+1$$

$$x^2+x+2$$

$$-2x-1 \stackrel{\longleftarrow}{=} R$$

$$\therefore x^3+2x^2+x+1 = (x^2+x+2)(x+1)+(-2x-1)$$

65) 
$$(x^2+2x-1)(x-2)+7x-3$$

$$\Rightarrow \frac{x-2 \iff Q}{x^2+2x-1} \frac{x^3+2x^2-x}{-2x^2+3x-1} \frac{x^3+2x^2-x}{-2x^2+4x+2} \frac{-2x^2-4x+2}{7x-3 \iff R}$$

$$\therefore x^3 + 2x - 1 = (x^2 + 2x - 1)(x - 2) + 7x - 3$$

66) 
$$(x^2-x+2)(3x+6)-2x-10$$

$$\Rightarrow 3x+6 \iff Q$$

$$x^2-x+2)3x^3+3x^2-2x+2$$

$$3x^3-3x^2+6x$$

$$6x^2-8x+2$$

$$6x^2-6x+12$$

$$-2x-10 \iff R$$

$$\therefore 3x^3+3x^2-2x+2=(x^2-x+2)(3x+6)-2x-10$$

67) 
$$3x^3 - x^2 + 4x + 3 = (x^2 + 2)(3x - 1) - 2x + 5$$

$$x^{2}+2)\overline{\smash{\big)}\,3x^{3}-x^{2}+4x+3}^{3}$$

$$2x^{3}+6x$$

$$-x^{2}-2x+3$$

$$-x^{2}-2$$

$$-2x+5$$

$$\therefore 3x^3 - x^2 + 4x + 3 = (x^2 + 2)(3x - 1) - 2x + 5$$

68) 
$$(x^2-x+1)(2x+4)+x-3$$

$$\begin{array}{c} \Rightarrow & \underbrace{\frac{2x+4}{x^2-x+1}}_{2x^3+2x^2-x+1} \\ \underbrace{\frac{2x^3-2x^2+2x}{4x^2-3x+1}}_{4x^2-4x+4} \\ \underbrace{\frac{-4x^2-4x+4}{x-3}}_{x-3} = R \end{array}$$

$$\therefore 2x^3 + 2x^2 - x + 1 = (x^2 - x + 1)(2x + 4) + x - 3$$