



◇ 「콘텐츠산업 진흥법 시행령」 제33조에 의한 표시

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3) 이 콘텐츠는 「콘텐츠산업 진흥법」에 따라 최초 제작일부터 5년간 보호됩니다.

◇ 「콘텐츠산업 진흥법」 외에도 「저작권법」에 의하여 보호되는 콘텐츠의 경우, 그 콘텐츠의 전부 또는 일부를 무단으로 복제하거나 전송하는 것은 콘텐츠산업 진흥법 외에도 저작권법에 의한 법적 책임을 질 수 있습니다.

## 계산시 참고사항

## 1. 곱셈공식

: 제곱근을 문자로 생각하고 다항식의 곱셈공식과 같은 방법으로 계산한다.

(1)  $(a+b)^2 = a^2 + 2ab + b^2$ ,  $(a-b)^2 = a^2 - 2ab + b^2$

(2)  $(a+b)(a-b) = a^2 - b^2$

(3)  $(x+a)(x+b) = x^2 + (a+b)x + ab$

(4)  $(ax+b)(cx+d) = acx^2 + (ad+bc)x + bd$

## 2. 곱셈공식을 이용한 분모의 유리화

: 분모가 두 개의 항으로 되어 있는 무리수일 때,  $(a+b)(a-b) = a^2 - b^2$ 을 이용하여 분모를 유리화한다.

$$\frac{c}{\sqrt{a} + \sqrt{b}} = \frac{c(\sqrt{a} - \sqrt{b})}{(\sqrt{a} + \sqrt{b})(\sqrt{a} - \sqrt{b})} = \frac{c(\sqrt{a} - \sqrt{b})}{a - b}$$

## 3. 식의 값 구하기

(1) 주어진 조건을 식에 직접 대입하여 식의 값을 구한다.

(2) 주어진 조건을 변형하여 식의 값을 구한다.



## 곱셈공식을 이용한 분모의 유리화

▣ 다음 분수를 유리화하여라.

1.  $\frac{1}{\sqrt{2}+1}$

2.  $\frac{3}{\sqrt{5}-\sqrt{2}}$

3.  $\frac{2-\sqrt{3}}{2+\sqrt{3}}$

4.  $\frac{\sqrt{5}+\sqrt{3}}{\sqrt{5}-\sqrt{3}}$

5.  $\frac{2}{\sqrt{5}+1}$

6.  $\frac{\sqrt{2}}{2-\sqrt{3}}$

7.  $\frac{1}{3-2\sqrt{2}}$

8.  $\frac{\sqrt{3}}{2\sqrt{3}-3}$

9.  $\frac{2\sqrt{2}}{\sqrt{6}-\sqrt{2}}$

10.  $\frac{4\sqrt{3}}{3-\sqrt{3}}$

11.  $\frac{\sqrt{5}+2}{\sqrt{5}-2}$

12.  $\frac{\sqrt{2}-1}{\sqrt{2}+1}$

13.  $\frac{3-\sqrt{5}}{3+\sqrt{5}}$

14.  $\frac{2(\sqrt{5}+\sqrt{3})}{\sqrt{5}-\sqrt{3}}$

15.  $\frac{2-\sqrt{2}}{3+2\sqrt{2}}$

16.  $\frac{\sqrt{27}-4}{\sqrt{3}-2}$

17.  $\frac{1}{1+\sqrt{2}}$

18.  $\frac{1}{2-\sqrt{3}}$

19.  $\frac{1}{\sqrt{5}+2}$

20.  $\frac{4}{1+\sqrt{5}}$

21.  $\frac{2}{\sqrt{3}-\sqrt{5}}$

22.  $\frac{2}{\sqrt{8}-\sqrt{6}}$

23.  $\frac{1}{3+2\sqrt{2}}$

24.  $\frac{1}{5-2\sqrt{6}}$

25.  $\frac{1}{2\sqrt{2}+\sqrt{7}}$

26.  $\frac{1}{3\sqrt{3}-2\sqrt{7}}$

27.  $\frac{3}{3-2\sqrt{3}}$

28.  $\frac{6}{2\sqrt{6}-3\sqrt{2}}$

29.  $\frac{2}{5\sqrt{2}+4\sqrt{3}}$

30.  $\frac{12}{2\sqrt{3}-3\sqrt{2}}$

31.  $\frac{2-\sqrt{5}}{2+\sqrt{5}}$

32.  $\frac{\sqrt{7}-\sqrt{3}}{\sqrt{7}+\sqrt{3}}$

33.  $\frac{4}{2\sqrt{5}+3}$

34.  $\frac{2}{3\sqrt{3}-2\sqrt{7}}$

35.  $\frac{\sqrt{10}+3}{\sqrt{10}-3}$

36.  $\frac{3}{3\sqrt{2}+2\sqrt{6}}$

37.  $\frac{\sqrt{7}}{3-\sqrt{7}}$

38.  $\frac{1}{\sqrt{6}+\sqrt{2}}-\frac{\sqrt{3}}{\sqrt{6}-\sqrt{2}}$

39.  $\frac{2}{\sqrt{3}+1}-\frac{4}{\sqrt{3}-1}$

43.  $(\sqrt{3}-\sqrt{6})^2$

44.  $(2\sqrt{7}-\sqrt{2})^2$

45.  $(\sqrt{7}+\sqrt{11})(\sqrt{7}-\sqrt{11})$

46.  $(3\sqrt{2}+4)(3\sqrt{2}-4)$

47.  $(-5+\sqrt{6})(-5-\sqrt{6})$

48.  $(\sqrt{5}-6)(\sqrt{5}+2)$

49.  $(\sqrt{3}+2)(\sqrt{3}+5)$

50.  $(\sqrt{2}+3\sqrt{5})(\sqrt{2}-\sqrt{5})$

51.  $(2\sqrt{7}+1)(\sqrt{7}-3)$

52.  $(3\sqrt{3}-\sqrt{2})(\sqrt{3}+\sqrt{2})$

53.  $(2+3\sqrt{5})(3-\sqrt{5})$

54.  $(\sqrt{6}+4)(2\sqrt{6}-3)$



### 곱셈공식을 이용한 식의 계산

■ 곱셈 공식을 이용하여 다음 식을 계산하여라.

40.  $(\sqrt{3}+\sqrt{5})^2$

41.  $(2\sqrt{3}+1)^2$

42.  $(\sqrt{5}-4)^2$

$$55. \frac{1}{\sqrt{27}} \times \sqrt{15} - \frac{(2+\sqrt{5})^2}{3}$$

$$56. (\sqrt{6}+2)^2 - (3+2\sqrt{2})(3-2\sqrt{2})$$

$$57. (\sqrt{2}+\sqrt{3})^2 - (\sqrt{3}+1)(\sqrt{3}-1)$$



## 식의 값 구하기

▣ 다음 식의 값을 구하여라.

$$58. x = \sqrt{2}+3 \text{ 일 때, } x^2-6x \text{의 값}$$

$$59. x = 3-2\sqrt{2} \text{ 일 때, } x^2-6x+11 \text{의 값}$$

$$60. x = \frac{1}{3-2\sqrt{2}} \text{ 일 때, } x^2-6x-2 \text{의 값}$$

$$61. x = \frac{1}{2-\sqrt{5}} \text{ 일 때, } x^2+4x-5 \text{의 값}$$

$$62. x = 2+\sqrt{3} \text{ 일 때, } x^2-4x \text{의 값}$$

$$63. x = 2\sqrt{5}-3 \text{ 일 때, } x^2+6x+1 \text{의 값}$$

$$64. x = \frac{1}{\sqrt{2}+1} \text{ 일 때, } x^2-x+1 \text{의 값}$$

$$65. x = \frac{1}{\sqrt{5}+2} \text{ 일 때, } x^2-2x+3 \text{의 값}$$

$$66. x = 2-\sqrt{3} \text{ 일 때, } x^2-4x+10 \text{의 값}$$

$$67. x = \sqrt{7}-4 \text{ 일 때, } x^2+8x-5 \text{의 값}$$

$$68. x = \sqrt{6}-2 \text{ 일 때, } x^2+4x-3 \text{의 값}$$

$$69. x = 2\sqrt{5}-3 \text{ 일 때, } x^2+6x+3 \text{의 값}$$

$$70. x = 5-2\sqrt{2} \text{ 일 때, } x^2-10x+10 \text{의 값}$$

$$71. x = 4+\sqrt{3} \text{ 일 때, } x^2-8x-7 \text{의 값}$$

$$72. x = \frac{1}{2-\sqrt{3}} \text{ 일 때, } x^2+2x-5 \text{의 값}$$

$$73. x+y=\sqrt{5}, xy=1 \text{ 일 때, } x^2+y^2 \text{의 값}$$

$$74. a-b=3\sqrt{2}, a^2+b^2=8 \text{ 일 때, } ab \text{의 값}$$

$$75. x-\frac{1}{x}=\sqrt{3} \text{ 일 때, } x^2+\frac{1}{x^2} \text{의 값}$$

$$76. x+\frac{1}{x}=\sqrt{6} \text{ 일 때, } \left(x-\frac{1}{x}\right)^2 \text{의 값}$$

■  $x = \frac{1}{3-2\sqrt{2}}$ ,  $y = \frac{1}{3+2\sqrt{2}}$  일 때, 다음 식의 값을 구하여라.

77.  $x+y$

78.  $xy$

79.  $x^2+y^2$

80.  $\frac{y}{x} + \frac{x}{y}$

■  $x = \frac{1}{\sqrt{2}-\sqrt{3}}$ ,  $y = \frac{1}{\sqrt{2}+\sqrt{3}}$  일 때, 다음 식의 값을 구하여라.

81.  $x+y$

82.  $xy$

83.  $x^2+y^2$

■  $x = 2 + \sqrt{5}$ ,  $y = 2 - \sqrt{5}$  일 때, 다음 식의 값을 구하여라.

84.  $x+y$

85.  $xy$

86.  $x^2+y^2$

87.  $\frac{1}{x} + \frac{1}{y}$

88.  $\frac{y}{x} + \frac{x}{y}$

89.  $x^2+xy+y^2$

90.  $x^2+y^2+5xy$

■  $x = \sqrt{5}$ ,  $y = \sqrt{7}$  일 때, 다음 식의 값을 구하여라.

91.  $(x+y)(x-y)$

92.  $x(y+1)-y(x+1)$

93.  $(2x+y)(2x-y)$

94.  $(x+y)^2-(x-y)^2$

95.  $(2x+y)(2x-y)-2y^2$

96.  $(x+y)^2-3xy$

97.  $(x+1)(y+1)(x-1)(y-1)$

98.  $x(x+y)-x(x-y)-xy$

99.  $(x+4y)^2-8xy-(3x+y)(3x-y)$

■  $x = \frac{\sqrt{3}-\sqrt{2}}{\sqrt{3}+\sqrt{2}}$ ,  $y = \frac{\sqrt{3}+\sqrt{2}}{\sqrt{3}-\sqrt{2}}$  일 때, 다음 식의 값을 구하여라.

100.  $x+y$

101.  $xy$

102.  $x^2-10x+10$

■ 다음 유리수가 되도록 유리수  $a$ 의 값을 정하여라.

103.  $-3+(a+2)\sqrt{3}$

104.  $2\sqrt{3}+6-a\sqrt{3}+3a$

105.  $6\sqrt{5}-4a-2+2a\sqrt{5}$

106.  $\frac{a+\sqrt{2}}{3\sqrt{2}+1}$

107.  $\frac{4-a\sqrt{2}}{5-2\sqrt{2}}$

108.  $(4+a\sqrt{5})(2-\sqrt{5})$

109.  $(a\sqrt{5}+3)(2\sqrt{5}-1)$

110.  $\sqrt{3}(\sqrt{3}+a)-\sqrt{12}(2+\sqrt{3})$

111.  $(4-3\sqrt{5})(a+2\sqrt{5})$

112.  $(3a+2\sqrt{11})(9-3\sqrt{11})$

113.  $(\sqrt{3}+a)(2\sqrt{3}-6)$

114.  $(6+2\sqrt{3})(a-\sqrt{3})$

115.  $(\sqrt{2}-4)^2-a(7-4\sqrt{2})$

## 정답 및 해설



- 1)  $\sqrt{2}-1$
- 2)  $\sqrt{5}+\sqrt{2}$   
 $\Rightarrow \frac{3}{\sqrt{5}-\sqrt{2}} = \frac{3(\sqrt{5}+\sqrt{2})}{(\sqrt{5}-\sqrt{2})(\sqrt{5}+\sqrt{2})} = \sqrt{5}+\sqrt{2}$
- 3)  $7-4\sqrt{3}$   
 $\Rightarrow \frac{2-\sqrt{3}}{2+\sqrt{3}} = \frac{(2-\sqrt{3})^2}{(2+\sqrt{3})(2-\sqrt{3})} = 7-4\sqrt{3}$
- 4)  $4+\sqrt{15}$   
 $\Rightarrow \frac{\sqrt{5}+\sqrt{3}}{\sqrt{5}-\sqrt{3}} = \frac{(\sqrt{5}+\sqrt{3})^2}{(\sqrt{5}-\sqrt{3})(\sqrt{5}+\sqrt{3})} = \frac{8+2\sqrt{15}}{2} = 4+\sqrt{15}$
- 5)  $\frac{\sqrt{5}-1}{2}$   
 $\Rightarrow \frac{2}{\sqrt{5}+1} = \frac{2(\sqrt{5}-1)}{(\sqrt{5}+1)(\sqrt{5}-1)} = \frac{2(\sqrt{5}-1)}{4} = \frac{\sqrt{5}-1}{2}$
- 6)  $2\sqrt{2}+\sqrt{6}$   
 $\Rightarrow \frac{\sqrt{2}}{2-\sqrt{3}} = \frac{\sqrt{2}(2+\sqrt{3})}{(2-\sqrt{3})(2+\sqrt{3})} = 2\sqrt{2}+\sqrt{6}$
- 7)  $3+2\sqrt{2}$   
 $\Rightarrow \frac{1}{3-2\sqrt{2}} = \frac{3+2\sqrt{2}}{(3-2\sqrt{2})(3+2\sqrt{2})} = 3+2\sqrt{2}$
- 8)  $2+\sqrt{3}$   
 $\Rightarrow \frac{\sqrt{3}}{2\sqrt{3}-3} = \frac{\sqrt{3}(2\sqrt{3}+3)}{(2\sqrt{3}-3)(2\sqrt{3}+3)} = \frac{6+3\sqrt{3}}{3} = 2+\sqrt{3}$
- 9)  $\sqrt{3}+1$   
 $\Rightarrow \frac{2\sqrt{2}}{\sqrt{6}-\sqrt{2}} = \frac{2\sqrt{2}(\sqrt{6}+\sqrt{2})}{(\sqrt{6}-\sqrt{2})(\sqrt{6}+\sqrt{2})} = \frac{4\sqrt{3}+4}{4} = \sqrt{3}+1$
- 10)  $2\sqrt{3}+2$   
 $\Rightarrow \frac{4\sqrt{3}}{3-\sqrt{3}} = \frac{4\sqrt{3}(3+\sqrt{3})}{(3-\sqrt{3})(3+\sqrt{3})} = \frac{12\sqrt{3}+12}{6} = 2\sqrt{3}+2$
- 11)  $9+4\sqrt{5}$   
 $\Rightarrow \frac{\sqrt{5}+2}{\sqrt{5}-2} = \frac{(\sqrt{5}+2)^2}{(\sqrt{5}-2)(\sqrt{5}+2)} = 5+4\sqrt{5}+4 = 9+4\sqrt{5}$
- 12)  $3-2\sqrt{2}$

$$\Rightarrow \frac{\sqrt{2}-1}{\sqrt{2}+1} = \frac{(\sqrt{2}-1)^2}{(\sqrt{2}+1)(\sqrt{2}-1)} = \frac{2-2\sqrt{2}+1}{2-1} = 3-2\sqrt{2}$$

$$13) \frac{7-3\sqrt{5}}{2}$$

$$\Rightarrow \frac{3-\sqrt{5}}{3+\sqrt{5}} = \frac{(3-\sqrt{5})^2}{(3+\sqrt{5})(3-\sqrt{5})} = \frac{9-6\sqrt{5}+5}{4} = \frac{14-6\sqrt{5}}{4} = \frac{7-3\sqrt{5}}{2}$$

$$14) 8+2\sqrt{15}$$

$$\Rightarrow \frac{2(\sqrt{5}+\sqrt{3})}{\sqrt{5}-\sqrt{3}} = \frac{2(\sqrt{5}+\sqrt{3})^2}{(\sqrt{5}-\sqrt{3})(\sqrt{5}+\sqrt{3})} = \frac{2(5+2\sqrt{15}+3)}{2} = 8+2\sqrt{15}$$

$$15) 10-7\sqrt{2}$$

$$\Rightarrow \frac{2-\sqrt{2}}{3+2\sqrt{2}} = \frac{(2-\sqrt{2})(3-2\sqrt{2})}{(3+2\sqrt{2})(3-2\sqrt{2})} = \frac{6-4\sqrt{2}-3\sqrt{2}+4}{9-8} = 10-7\sqrt{2}$$

$$16) -1-2\sqrt{3}$$

$$\Rightarrow \frac{\sqrt{27}-4}{\sqrt{3}-2} = \frac{(3\sqrt{3}-4)(\sqrt{3}+2)}{(\sqrt{3}-2)(\sqrt{3}+2)} = \frac{9+6\sqrt{3}-4\sqrt{3}-8}{-1} = -1-2\sqrt{3}$$

$$17) -1+\sqrt{2}$$

$$\Rightarrow \frac{1}{1+\sqrt{2}} = \frac{1-\sqrt{2}}{(1+\sqrt{2})(1-\sqrt{2})} = -1+\sqrt{2}$$

$$18) 2+\sqrt{3}$$

$$\Rightarrow \frac{1}{2-\sqrt{3}} = \frac{2+\sqrt{3}}{(2-\sqrt{3})(2+\sqrt{3})} = 2+\sqrt{3}$$

$$19) \sqrt{5}-2$$

$$\Rightarrow \frac{1}{\sqrt{5}+2} = \frac{-\sqrt{5}+2}{(\sqrt{5}+2)(-\sqrt{5}+2)} = \sqrt{5}-2$$

$$20) -1+\sqrt{5}$$

$$\Rightarrow \frac{4}{1+\sqrt{5}} = \frac{4(1-\sqrt{5})}{(1+\sqrt{5})(1-\sqrt{5})} = -1+\sqrt{5}$$

$$21) -\sqrt{3}-\sqrt{5}$$

$$\Rightarrow \frac{2}{\sqrt{3}-\sqrt{5}} = \frac{2(\sqrt{3}+\sqrt{5})}{(\sqrt{3}-\sqrt{5})(\sqrt{3}+\sqrt{5})} = -\sqrt{3}-\sqrt{5}$$

$$22) 2\sqrt{2}+\sqrt{6}$$

$$\Rightarrow \frac{2}{\sqrt{8}-\sqrt{6}} = \frac{2(\sqrt{8}+\sqrt{6})}{(\sqrt{8}-\sqrt{6})(\sqrt{8}+\sqrt{6})} = \sqrt{8}+\sqrt{6} = 2\sqrt{2}+\sqrt{6}$$

23)  $3-2\sqrt{2}$

$$\Rightarrow \frac{1}{3+2\sqrt{2}} = \frac{3-2\sqrt{2}}{(3+2\sqrt{2})(3-2\sqrt{2})} = 3-2\sqrt{2}$$

24)  $5+2\sqrt{6}$

$$\Rightarrow \frac{1}{5-2\sqrt{6}} = \frac{5+2\sqrt{6}}{(5-2\sqrt{6})(5+2\sqrt{6})} = 5+2\sqrt{6}$$

25)  $2\sqrt{2}-\sqrt{7}$

$$\Rightarrow \frac{1}{2\sqrt{2}+\sqrt{7}} = \frac{2\sqrt{2}-\sqrt{7}}{(2\sqrt{2}+\sqrt{7})(2\sqrt{2}-\sqrt{7})} \\ = 2\sqrt{2}-\sqrt{7}$$

26)  $-3\sqrt{3}-2\sqrt{7}$

$$\Rightarrow \frac{1}{3\sqrt{3}-2\sqrt{7}} = \frac{3\sqrt{3}+2\sqrt{7}}{(3\sqrt{3}-2\sqrt{7})(3\sqrt{3}+2\sqrt{7})} \\ = -3\sqrt{3}-2\sqrt{7}$$

27)  $-3-2\sqrt{3}$

$$\Rightarrow \frac{3}{3-2\sqrt{3}} = \frac{3(3+2\sqrt{3})}{(3-2\sqrt{3})(3+2\sqrt{3})} \\ = \frac{3(3+2\sqrt{3})}{-3} = -3-2\sqrt{3}$$

28)  $2\sqrt{6}+3\sqrt{2}$

$$\Rightarrow \frac{6}{2\sqrt{6}-3\sqrt{2}} = \frac{6(2\sqrt{6}+3\sqrt{2})}{(2\sqrt{6}-3\sqrt{2})(2\sqrt{6}+3\sqrt{2})} \\ = \frac{6(2\sqrt{6}+3\sqrt{2})}{24-18} = 2\sqrt{6}+3\sqrt{2}$$

29)  $5\sqrt{2}-4\sqrt{3}$

$$\Rightarrow \frac{2}{5\sqrt{2}+4\sqrt{3}} = \frac{2(5\sqrt{2}-4\sqrt{3})}{(5\sqrt{2}+4\sqrt{3})(5\sqrt{2}-4\sqrt{3})} \\ = 5\sqrt{2}-4\sqrt{3}$$

30)  $-4\sqrt{3}-6\sqrt{2}$

$$\Rightarrow \frac{12}{2\sqrt{3}-3\sqrt{2}} = \frac{12(2\sqrt{3}+3\sqrt{2})}{(2\sqrt{3}-3\sqrt{2})(2\sqrt{3}+3\sqrt{2})} \\ = -2(2\sqrt{3}+3\sqrt{2}) = -4\sqrt{3}-6\sqrt{2}$$

31)  $-9+4\sqrt{5}$

$$\Rightarrow \frac{2-\sqrt{5}}{2+\sqrt{5}} = \frac{(2-\sqrt{5})^2}{(2+\sqrt{5})(2-\sqrt{5})} = -(9-4\sqrt{5}) \\ = -9+4\sqrt{5}$$

32)  $\frac{5-\sqrt{21}}{2}$

$$\Rightarrow \frac{\sqrt{7}-\sqrt{3}}{\sqrt{7}+\sqrt{3}} = \frac{(\sqrt{7}-\sqrt{3})^2}{(\sqrt{7}+\sqrt{3})(\sqrt{7}-\sqrt{3})} = \frac{10-2\sqrt{21}}{4} \\ = \frac{5-\sqrt{21}}{2}$$

33)  $\frac{8\sqrt{5}-12}{11}$

$$\Rightarrow \frac{4}{2\sqrt{5}+3} = \frac{4(2\sqrt{5}-3)}{(2\sqrt{5}+3)(2\sqrt{5}-3)} = \frac{8\sqrt{5}-12}{11}$$

34)  $-6\sqrt{3}-4\sqrt{7}$

$$\Rightarrow \frac{2}{3\sqrt{3}-2\sqrt{7}} = \frac{2(3\sqrt{3}+2\sqrt{7})}{(3\sqrt{3}-2\sqrt{7})(3\sqrt{3}+2\sqrt{7})} \\ = -6\sqrt{3}-4\sqrt{7}$$

35)  $19+6\sqrt{10}$

36)  $\frac{-3\sqrt{2}+2\sqrt{6}}{2}$

$$\Rightarrow \frac{3}{3\sqrt{2}+2\sqrt{6}} = \frac{3(3\sqrt{2}-2\sqrt{6})}{(3\sqrt{2}+2\sqrt{6})(3\sqrt{2}-2\sqrt{6})} \\ = \frac{-3\sqrt{2}+2\sqrt{6}}{2}$$

37)  $\frac{3\sqrt{7}+7}{2}$

38)  $-\sqrt{2}$

39)  $-3-\sqrt{3}$

40)  $8+2\sqrt{15}$

$$\Rightarrow (\sqrt{3}+\sqrt{5})^2 = 3+2\sqrt{15}+5 = 8+2\sqrt{15}$$

41)  $13+4\sqrt{3}$

$$\Rightarrow (2\sqrt{3}+1)^2 = 12+4\sqrt{3}+1 = 13+4\sqrt{3}$$

42)  $21-8\sqrt{5}$

$$\Rightarrow (\sqrt{5}-4)^2 = 5-8\sqrt{5}+16 = 21-8\sqrt{5}$$

43)  $9-6\sqrt{2}$

$$\Rightarrow (\sqrt{3}-\sqrt{6})^2 = 3-6\sqrt{2}+6 = 9-6\sqrt{2}$$

44)  $30-4\sqrt{14}$

$$\Rightarrow (2\sqrt{7}-\sqrt{2})^2 = 28-4\sqrt{14}+2 = 30-4\sqrt{14}$$

45)  $-4$

$$\Rightarrow (\sqrt{7}+\sqrt{11})(\sqrt{7}-\sqrt{11}) = 7-11 = -4$$

46)  $2$

$$\Rightarrow (3\sqrt{2}+4)(3\sqrt{2}-4) = 18-16 = 2$$

47)  $19$

$$\Rightarrow (-5+\sqrt{6})(-5-\sqrt{6}) = 25-6 = 19$$

48)  $-7-4\sqrt{5}$

$$\Rightarrow (\sqrt{5}-6)(\sqrt{5}+2) = 5+2\sqrt{5}-6\sqrt{5}-12 = -7-4\sqrt{5}$$



49)  $13+7\sqrt{3}$

$$\Rightarrow (\sqrt{3}+2)(\sqrt{3}+5) = 3+5\sqrt{3}+2\sqrt{3}+10 = 13+7\sqrt{3}$$

50)  $-13+2\sqrt{10}$

$$\Rightarrow (\sqrt{2}+3\sqrt{5})(\sqrt{2}-\sqrt{5}) \\ = 2-\sqrt{10}+3\sqrt{10}-15 = -13+2\sqrt{10}$$

51)  $11-5\sqrt{7}$

$$\Rightarrow (2\sqrt{7}+1)(\sqrt{7}-3) = 14-6\sqrt{7}+\sqrt{7}-3 = 11-5\sqrt{7}$$

52)  $7+2\sqrt{6}$

53)  $-9+7\sqrt{5}$

$$\Rightarrow (2+3\sqrt{5})(3-\sqrt{5}) = 6-2\sqrt{5}+9\sqrt{5}-15 = -9+7\sqrt{5}$$

54)  $5\sqrt{6}$

$$\Rightarrow (\sqrt{6}+4)(2\sqrt{6}-3) = 12-3\sqrt{6}+8\sqrt{6}-12 = 5\sqrt{6}$$

55)  $-3-\sqrt{5}$

$$\Rightarrow (\text{주어진 식})$$

$$= \frac{1}{3\sqrt{3}} \times \sqrt{15} - \frac{9+4\sqrt{5}}{3} = \frac{\sqrt{5}}{3} - \frac{9+4\sqrt{5}}{3} \\ = \frac{-9-3\sqrt{5}}{3} = -3-\sqrt{5}$$

56)  $9+4\sqrt{6}$

$$\Rightarrow (\text{주어진 식})$$

$$= 6+4\sqrt{6}+4-(9-8) = 10+4\sqrt{6}-1 = 9+4\sqrt{6}$$

57)  $3+2\sqrt{6}$

58)  $-7$

$$\Rightarrow x = \sqrt{2}+3 \text{에서 } x-3 = \sqrt{2} \text{이므로 양변을 각각 제곱하면} \\ (x-3)^2 = (\sqrt{2})^2, \quad x^2-6x+9=2 \\ \therefore x^2-6x = -7$$

59)  $10$

$$\Rightarrow x = 3-2\sqrt{2} \text{에서 } x-3 = -2\sqrt{2} \text{이므로 양변을 각각 제곱하면} \\ (x-3)^2 = (-2\sqrt{2})^2, \quad x^2-6x+9=8 \\ \therefore x^2-6x = -1 \quad \therefore x^2-6x+11 = 10$$

60)  $-3$

$$\Rightarrow x = \frac{1}{3-2\sqrt{2}} = \frac{3+2\sqrt{2}}{(3-2\sqrt{2})(3+2\sqrt{2})} = 3+2\sqrt{2} \text{에서} \\ x-3 = 2\sqrt{2} \text{이므로 양변을 각각 제곱하면} \\ (x-3)^2 = (2\sqrt{2})^2, \quad x^2-6x+9=8 \\ \therefore x^2-6x = -1 \quad \therefore x^2-6x-2 = -3$$

61)  $-4$

$$\Rightarrow x = \frac{1}{2-\sqrt{5}} = \frac{2+\sqrt{5}}{(2-\sqrt{5})(2+\sqrt{5})} = -2-\sqrt{5} \text{에서}$$

$$x+2 = -\sqrt{5} \text{이므로 양변을 각각 제곱하면}$$

$$(x+2)^2 = (-\sqrt{5})^2$$

$$x^2+4x+4=5, \quad x^2+4x=1$$

$$\therefore x^2+4x-5 = -4$$

62)  $-1$

$$\Rightarrow x = 2+\sqrt{3} \text{에서 } x-2 = \sqrt{3} \text{이므로 양변을 각각 제곱하} \\ \text{면 } (x-2)^2 = (\sqrt{3})^2, \quad x^2-4x+4=3 \\ \therefore x^2-4x = -1$$

63)  $12$

$$\Rightarrow x = 2\sqrt{5}-3 \text{에서 } x+3 = 2\sqrt{5} \text{이므로 양변을 각각 제곱하} \\ \text{면 } (x+3)^2 = (2\sqrt{5})^2, \quad x^2+6x+9=20 \\ \therefore x^2+6x = 11 \quad \therefore x^2+6x+1 = 12$$

64)  $5-3\sqrt{2}$

$$\Rightarrow x = \frac{1}{\sqrt{2}+1} = \frac{\sqrt{2}-1}{(\sqrt{2}+1)(\sqrt{2}-1)} = \sqrt{2}-1 \\ \therefore x^2-x+1 = (\sqrt{2}-1)^2 - (\sqrt{2}-1) + 1 \\ = 3-2\sqrt{2} - \sqrt{2} + 1 + 1 = 5-3\sqrt{2}$$

65)  $16-6\sqrt{5}$

$$\Rightarrow x = \frac{1}{\sqrt{5}+2} = \frac{\sqrt{5}-2}{(\sqrt{5}+2)(\sqrt{5}-2)} = \sqrt{5}-2 \\ \therefore x^2-2x+3 = (\sqrt{5}-2)^2 - 2(\sqrt{5}-2) + 3 \\ = 9-4\sqrt{5} - 2\sqrt{5} + 4 + 3 = 16-6\sqrt{5}$$

66)  $9$

$$\Rightarrow x = 2-\sqrt{3} \text{에서 } x-2 = -\sqrt{3} \text{이므로} \\ (x-2)^2 = (-\sqrt{3})^2, \quad x^2-4x+4=3, \\ x^2-4x = -1 \\ \therefore x^2-4x+10 = -1+10 = 9$$

67)  $-14$

$$\Rightarrow x = \sqrt{7}-4 \text{에서 } x+4 = \sqrt{7} \text{이므로} \\ (x+4)^2 = (\sqrt{7})^2, \quad x^2+8x+16=7, \\ x^2+8x = -9 \\ \therefore x^2+8x-5 = -9-5 = -14$$

68)  $-1$

$$\Rightarrow x = \sqrt{6}-2 \text{에서 } x+2 = \sqrt{6} \text{이므로} \\ (x+2)^2 = (\sqrt{6})^2, \quad x^2+4x+4=6, \quad x^2+4x=2 \\ \therefore x^2+4x-3 = 2-3 = -1$$

69)  $14$

$$\Rightarrow x = 2\sqrt{5}-3 \text{에서 } x+3 = 2\sqrt{5} \text{이므로} \\ (x+3)^2 = (2\sqrt{5})^2, \quad x^2+6x+9=20, \\ x^2+6x = 11 \\ \therefore x^2+6x+3 = 11+3 = 14$$

70)  $-7$ 

$$\begin{aligned} \Rightarrow x &= 5 - 2\sqrt{2} \text{에서 } x-5 = -2\sqrt{2} \text{이므로} \\ (x-5)^2 &= (-2\sqrt{2})^2, \quad x^2 - 10x + 25 = 8, \\ x^2 - 10x &= -17 \\ \therefore x^2 - 10x + 10 &= -17 + 10 = -7 \end{aligned}$$

71)  $-20$ 

$$\begin{aligned} \Rightarrow x &= 4 + \sqrt{3} \text{에서 } x-4 = \sqrt{3} \text{이므로} \\ (x-4)^2 &= (\sqrt{3})^2, \quad x^2 - 8x + 16 = 3 \\ x^2 - 8x &= -13 \\ \therefore x^2 - 8x - 7 &= -13 - 7 = -20 \end{aligned}$$

72)  $6 + 6\sqrt{3}$ 

$$\begin{aligned} \Rightarrow x &= \frac{1}{2-\sqrt{3}} = \frac{2+\sqrt{3}}{(2-\sqrt{3})(2+\sqrt{3})} = 2+\sqrt{3} \\ \therefore x^2 + 2x - 5 &= (2+\sqrt{3})^2 + 2(2+\sqrt{3}) - 5 \\ &= 7 + 4\sqrt{3} + 4 + 2\sqrt{3} - 5 = 6 + 6\sqrt{3} \end{aligned}$$

73)  $3$ 

$$\Rightarrow x^2 + y^2 = (x+y)^2 - 2xy = (\sqrt{5})^2 - 2 \times 1 = 3$$

74)  $-5$ 

$$\begin{aligned} \Rightarrow (a-b)^2 &= a^2 - 2ab + b^2 \text{에서} \\ (3\sqrt{2})^2 &= 8 - 2ab \\ 18 &= 8 - 2ab \quad \therefore ab = -5 \end{aligned}$$

75)  $5$ 

$$\Rightarrow x^2 + \frac{1}{x^2} = \left(x - \frac{1}{x}\right)^2 + 2 = (\sqrt{3})^2 + 2 = 5$$

76)  $2$ 

$$\Rightarrow \left(x - \frac{1}{x}\right)^2 = \left(x + \frac{1}{x}\right)^2 - 4 = (\sqrt{6})^2 - 4 = 2$$

77)  $6$ 

$$\begin{aligned} \Rightarrow x &= \frac{1}{3-2\sqrt{2}} = \frac{3+2\sqrt{2}}{(3-2\sqrt{2})(3+2\sqrt{2})} = 3+2\sqrt{2} \\ y &= \frac{1}{3+2\sqrt{2}} = \frac{3-2\sqrt{2}}{(3+2\sqrt{2})(3-2\sqrt{2})} = 3-2\sqrt{2} \\ \therefore x+y &= (3+2\sqrt{2}) + (3-2\sqrt{2}) = 6 \end{aligned}$$

78)  $1$ 

$$\Rightarrow xy = (3+2\sqrt{2})(3-2\sqrt{2}) = 9-8 = 1$$

79)  $34$ 

$$\Rightarrow x^2 + y^2 = (x+y)^2 - 2xy = 6^2 - 2 \times 1 = 34$$

80)  $34$ 

$$\Rightarrow \frac{y}{x} + \frac{x}{y} = \frac{x^2 + y^2}{xy} = 34$$

81)  $-2\sqrt{2}$ 

$$\begin{aligned} \Rightarrow x &= \frac{1}{\sqrt{2}-\sqrt{3}} = \frac{\sqrt{2}+\sqrt{3}}{(\sqrt{2}-\sqrt{3})(\sqrt{2}+\sqrt{3})} \\ &= -\sqrt{2}-\sqrt{3} \\ y &= \frac{1}{\sqrt{2}+\sqrt{3}} = \frac{\sqrt{2}-\sqrt{3}}{(\sqrt{2}+\sqrt{3})(\sqrt{2}-\sqrt{3})} = -\sqrt{2}+\sqrt{3} \\ \therefore x+y &= (-\sqrt{2}-\sqrt{3}) + (-\sqrt{2}+\sqrt{3}) = -2\sqrt{2} \end{aligned}$$

82)  $-1$ 

$$\begin{aligned} \Rightarrow x &= -\sqrt{2}-\sqrt{3}, \quad y = -\sqrt{2}+\sqrt{3} \text{이므로} \\ \therefore xy &= (-\sqrt{2}-\sqrt{3})(-\sqrt{2}+\sqrt{3}) = 2-3 = -1 \end{aligned}$$

83)  $10$ 

$$\begin{aligned} \Rightarrow x &= -\sqrt{2}-\sqrt{3}, \quad y = -\sqrt{2}+\sqrt{3} \text{이므로} \\ \therefore x^2 + y^2 &= (x+y)^2 - 2xy = (-2\sqrt{2})^2 - 2 \times (-1) \\ &= 8+2 = 10 \end{aligned}$$

84)  $4$ 

$$\Rightarrow x+y = (2+\sqrt{5}) + (2-\sqrt{5}) = 4$$

85)  $-1$ 

$$\Rightarrow xy = (2+\sqrt{5})(2-\sqrt{5}) = -1$$

86)  $18$ 

$$\Rightarrow x^2 + y^2 = (x+y)^2 - 2xy = 4^2 - 2 \times (-1) = 18$$

87)  $-4$ 

$$\Rightarrow \frac{1}{x} + \frac{1}{y} = \frac{x+y}{xy} = \frac{4}{-1} = -4$$

88)  $-18$ 

$$\Rightarrow \frac{y}{x} + \frac{x}{y} = \frac{x^2 + y^2}{xy} = \frac{18}{-1} = -18$$

89)  $17$ 

$$\Rightarrow x^2 + xy + y^2 = x^2 + y^2 + xy = 18 - 1 = 17$$

90)  $13$ 

$$\Rightarrow x^2 + y^2 + 5xy = (x+y)^2 + 3xy = 4^2 + 3 \times (-1) = 13$$

91)  $-2$ 

$$\begin{aligned} \Rightarrow (x+y)(x-y) &= x^2 - y^2 = (\sqrt{5})^2 - (\sqrt{7})^2 \\ &= 5-7 = -2 \end{aligned}$$

92)  $\sqrt{5}-\sqrt{7}$ 

$$\Rightarrow x(y+1) - y(x+1) = xy + x - xy - y = x - y = \sqrt{5} - \sqrt{7}$$

93)  $13$ 

$$\Rightarrow (2x+y)(2x-y) = 4x^2 - y^2 = 4(\sqrt{5})^2 - (\sqrt{7})^2 = 13$$

94)  $4\sqrt{35}$ 

$$\begin{aligned} \Rightarrow (x+y)^2 - (x-y)^2 &= x^2 + 2xy + y^2 - (x^2 - 2xy + y^2) \\ &= 4xy = 4\sqrt{5}\sqrt{7} = 4\sqrt{35} \end{aligned}$$

95) -1

$$\Rightarrow (2x+y)(2x-y)-2y^2=4x^2-y^2-2y^2=4x^2-3y^2$$

$$=4 \times (\sqrt{5})^2-3 \times (\sqrt{7})^2=20-21=-1$$

96)  $12-\sqrt{35}$ 

$$\Rightarrow (x+y)^2-3xy=x^2+y^2+2xy-3xy=x^2+y^2-xy$$

$$=(\sqrt{5})^2+(\sqrt{7})^2-\sqrt{5}\sqrt{7}=5+7-\sqrt{35}=12-\sqrt{35}$$

97) 24

$$\Rightarrow (x+1)(y+1)(x-1)(y-1)$$

$$=(x+1)(x-1)(y+1)(y-1)=(x^2-1)(y^2-1)$$

$$=\{(\sqrt{5})^2-1\}\{(\sqrt{7})^2-1\}=4 \times 6=24$$

98)  $\sqrt{35}$ 

$$\Rightarrow x(x+y)-x(x-y)-xy=x^2+xy-x^2+xy-xy$$

$$=xy=\sqrt{5}\sqrt{7}=\sqrt{35}$$

99) 79

$$\Rightarrow (x+4y)^2-8xy-(3x+y)(3x-y)$$

$$=x^2+8xy+16y^2-8xy-(9x^2-y^2)$$

$$=-8x^2+17y^2$$

$$=-8 \times (\sqrt{5})^2+17 \times (\sqrt{7})^2$$

$$=79$$

100) 10

$$\Rightarrow x=\frac{\sqrt{3}-\sqrt{2}}{\sqrt{3}+\sqrt{2}}=\frac{(\sqrt{3}-\sqrt{2})^2}{(\sqrt{3}+\sqrt{2})(\sqrt{3}-\sqrt{2})}$$

$$=(\sqrt{3}-\sqrt{2})^2=5-2\sqrt{6}$$

$$y=\frac{\sqrt{3}+\sqrt{2}}{\sqrt{3}-\sqrt{2}}=\frac{(\sqrt{3}+\sqrt{2})^2}{(\sqrt{3}-\sqrt{2})(\sqrt{3}+\sqrt{2})}$$

$$=(\sqrt{3}+\sqrt{2})^2=5+2\sqrt{6}$$

$$\therefore x+y=(5-2\sqrt{6})+(5+2\sqrt{6})=10$$

101) 1

$$\Rightarrow x=5-2\sqrt{6}, y=5+2\sqrt{6} \text{ 이므로}$$

$$\therefore xy=(5-2\sqrt{6})(5+2\sqrt{6})=25-24=1$$

102) 9

$$\Rightarrow x=5-2\sqrt{6}, y=5+2\sqrt{6} \text{ 이므로}$$

$$\therefore x^2-10x+10=(x-5)^2-15=(5-2\sqrt{6}-5)^2-15$$

$$=24-15=9$$

103) -2

$$\Rightarrow (a+2)\sqrt{3}=0 \text{ 이므로 } a+2=0 \quad \therefore a=-2$$

104) 2

$$\Rightarrow (\text{주어진 식})=(2-a)\sqrt{3}+6+3a \text{ 가 유리수가 되려면}$$

$$2-a=0 \quad \therefore a=2$$

105) -3

$$\Rightarrow (\text{주어진 식})=(6+2a)\sqrt{5}-4a-2 \text{ 가 유리수가 되려면}$$

$$6+2a=0 \quad \therefore a=-3$$

106)  $\frac{1}{3}$ 

$$\Rightarrow \frac{a+\sqrt{2}}{3\sqrt{2}+1}=\frac{(a+\sqrt{2})(3\sqrt{2}-1)}{(3\sqrt{2}+1)(3\sqrt{2}-1)}=\frac{6-a+(3a-1)\sqrt{2}}{17}$$

$$\text{유리수가 되려면 } 3a-1=0 \quad \therefore a=\frac{1}{3}$$

107)  $\frac{8}{5}$ 

$$\Rightarrow \frac{4-a\sqrt{2}}{5-2\sqrt{2}}=\frac{(4-a\sqrt{2})(5+2\sqrt{2})}{(5-2\sqrt{2})(5+2\sqrt{2})}=\frac{20-4a+(8-5a)\sqrt{2}}{17}$$

$$\text{유리수가 되려면 } 8-5a=0 \text{ 이므로 } a=\frac{8}{5}$$

108) 2

$$\Rightarrow (\text{주어진 식})=8-5a+(-4+2a)\sqrt{5} \text{ 가 유리수가 되려면}$$

$$-4+2a=0 \quad \therefore a=2$$

109) 6

$$\Rightarrow (a\sqrt{5}+3)(2\sqrt{5}-1)=10a-3+(6-a)\sqrt{5} \text{ 가}$$

$$\text{유리수가 되려면 } 6-a=0 \quad \therefore a=6$$

110) 4

$$\Rightarrow \sqrt{3}(\sqrt{3}+a)-\sqrt{12}(2+\sqrt{3})$$

$$=3+a\sqrt{3}-4\sqrt{3}-6=-3+(a-4)\sqrt{3}$$

$$\text{유리수가 되려면 } a-4=0 \quad \therefore a=4$$

111)  $\frac{8}{3}$ 

112) 2

113) 3

114) 3

115) 2