

[영역] 5.기하



중 2 과정

5-3-1.평행시변형의 정의와 성질





◇「콘텐츠산업 진흥법 시행령」제33조에 의한 표시

1) 제작연월일 : 2016-10-25

2) 제작자 : 교육지대㈜

3) 이 콘텐츠는 「콘텐츠산업 진흥법」에 따라 최초 제작일부터 5년간 보호됩니다.

◇「콘텐츠산업 진흥법」외에도「저작권법」에 의하여 보호되는 콘텐츠의 경우, 그 콘텐츠의 전부 또는 일부를 무단으로 복제하거나 전송하는 것은 콘텐츠산업 진흥법 외에도 저작권법에 의한 법적 책임을 질 수 있습니다.

계산시 참고사항

1. 평행사변형

1) 평행사변형: 두 쌍의 대변이 각각 평행한 사각형

⇒ □ABCD에서 AB//DC, AD//BC

2. 평행사변형의 성질

1) 두 쌍의 대변의 길이가 각각 같다.

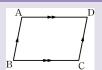
 $\Rightarrow \overline{AB} = \overline{DC}, \overline{AD} = \overline{BC}$

2) 두 쌍의 대각의 크기가 각각 같다.

 $\Rightarrow \angle A = \angle C, \angle B = \angle D$

3) 두 대각선은 서로를 이동분한다.

 $\Rightarrow \overline{AO} = \overline{CO}, \overline{BO} = \overline{DO}$









참고

● 평행사변형은 두 쌍의 대변이 각각 평행하므로 이웃하는 두 각의 크기의 합은 180°이다.

 $\stackrel{\text{\tiny 4}}{\neg}, \ \angle \ A + \angle \ B = \angle \ B + \angle \ C \\ = \angle \ C + \angle \ D \\ = \angle \ D + \angle \ A = 180 \ ^\circ$

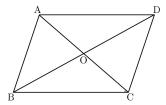
참고

사각형에서 서로 마주 보는 변을 대변, 서로 마주 보는 각을 대각이라 한다.



평행사변형

□ 다음 그림의 평행사변형 ABCD를 보고, 다음 ()안에 알 맞게 써넣어라.



1. $\overline{AB} = ($), $\overline{AD} = \overline{BC}$

2. $\overline{AO} = \overline{CO}$, $\overline{BO} = ($

 $\triangle ABO \equiv ($

4. () $\equiv \triangle AOD$

5. $\overline{\rm AD}//\overline{\rm BC}$, $\overline{\rm AB}//($

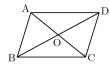
6. $\angle A = \angle C$, $\angle B = ($

7. ()= $\angle DOC$

8. $\angle DAO = ($

9. $\angle A + \angle B = \angle C + \angle D = ($

☐ 다음 평행사변형 ABCD에 대하여 다음 중 옳은 것에는 O 표, 옳지 않은 것에는 X표를 하여라.



10. $\overline{AB} = \overline{DC}$

()

11. $\angle ABC = \angle BCD$

- ()
- 12. $\angle ABC + \angle BCD = 180^{\circ}$
- ()

- 13. $\angle BAD + \angle BCD = 180^{\circ}$
- ()

14. $\overline{OA} = \overline{OB}$

()

15. $\triangle ABO \equiv \triangle ADO$

()

16. $\triangle AOD \equiv \triangle COB$

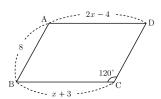
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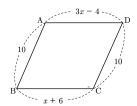
평행사변형의 성질

☑ 다음 그림과 같은 평행사변형 ABCD에서 x의 값을 구하여 라.

17.

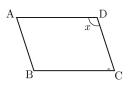


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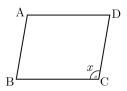


☑ 다음 평행사변형 ABCD에서 ∠x의 크기를 구하여라.

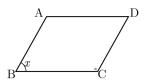
19. $\angle A : \angle B = 2 : 3$



20. $\angle A : \angle B = 5 : 4$

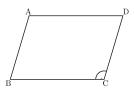


21. $\angle A : \angle D = 2 : 1$

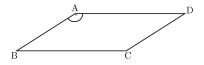


☑ 다음 그림을 보고 물음에 답하여라.

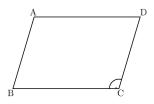
22. 평행사변형 ABCD에서 $\angle A: \angle B = 5:4$ 일 때, $\angle C$ 의 크 기를 구하여라.



23. **평행사변형** ABCD**에서** ∠A:∠B=3:1**일 때,** ∠A**의 크** 기를 구하여라.

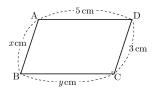


24. **평행사변형** ABCD**에서** ∠A와 ∠B**의 크기의 비가** 3:2일 때, ∠C의 크기를 구하여라.

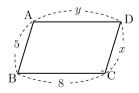


ightharpoonup 다음 그림과 같은 평행사변형 m ABCD에서 $m \it \it x$, $m \it \it y$ 의 값을 각각 구하여라.

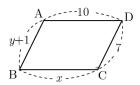
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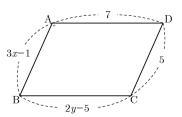
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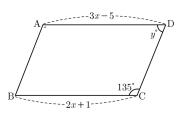
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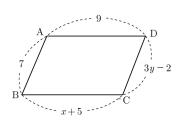
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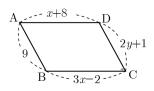
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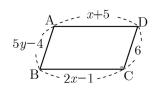
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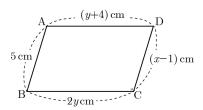
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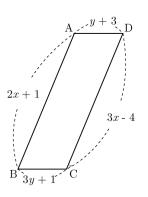


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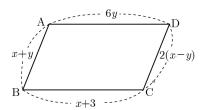


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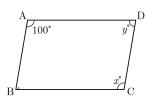




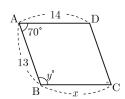
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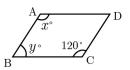
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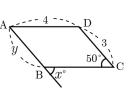
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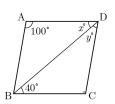
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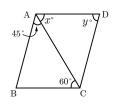
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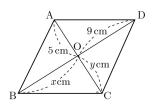
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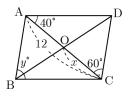
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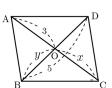
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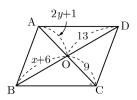
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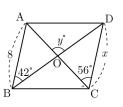


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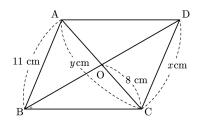


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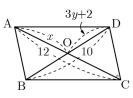




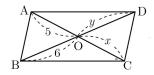
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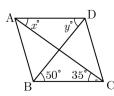
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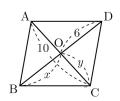
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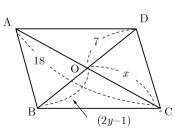
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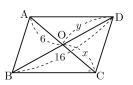
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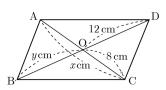
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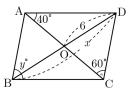
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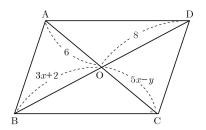
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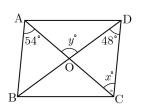


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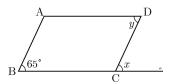
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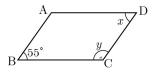


\square 다음 그림과 같은 평행사변형 ABCD에서 $\angle x$, $\angle y$ 의 크기를 각각 구하여라.

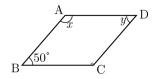
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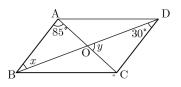
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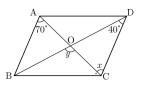
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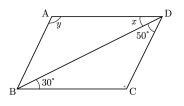
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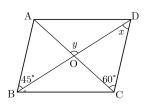
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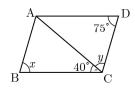
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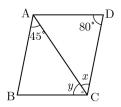
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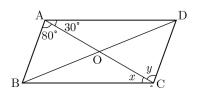
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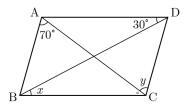


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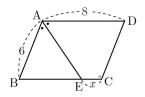




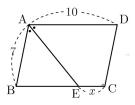
평행사변형의 성질의 응용

\square 다음 평행사변형 ABCD에서 x의 값을 구하여라.

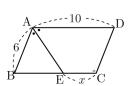
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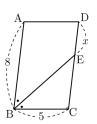
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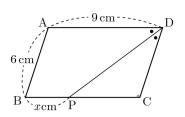
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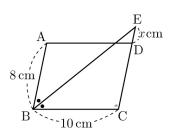
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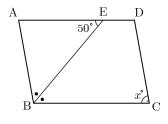
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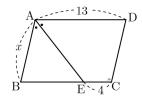
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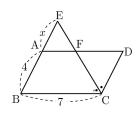
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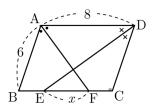


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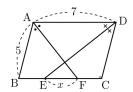


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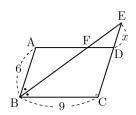




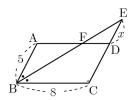
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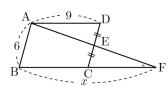
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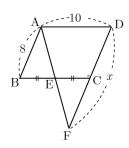
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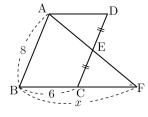
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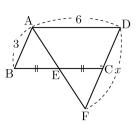
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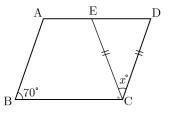
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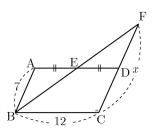


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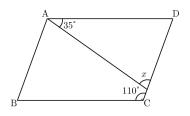
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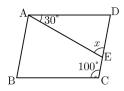


ightharpoonup 다음 평행사변형 ABCD에서 $\angle x$ 의 크기를 구하여라.

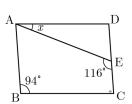
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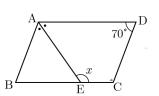
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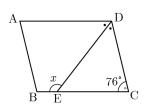
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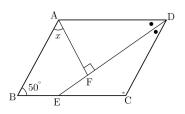
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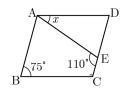
92.



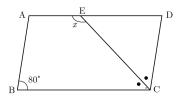
93.



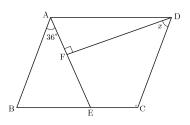
94.

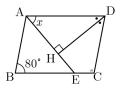


95.



96.







- 1) CD
- 2) DO
- 3) △CDO
- 4) △COB
- 5) DC
- 6) ∠D
- 7) ∠BOA
- 8) ∠BCO
- 9) 180°
- 10) O
- 11) X
- 12) O
- 13) X
- 14) X
- 15) X
- 16) O
- 17) 7
- 18) 5
- \Rightarrow $\angle x = \angle B = 180^{\circ} \times \frac{3}{5} = 108^{\circ}$
- 20) 100°
- $\Rightarrow \angle x = \angle A = 180^{\circ} \times \frac{5}{9} = 100^{\circ}$
- 21) 60°
- $\Rightarrow \angle x = \angle D = 180^{\circ} \times \frac{1}{3} = 60^{\circ}$
- 22) 100°
- $\Rightarrow \angle C = \angle A = 180^{\circ} \times \frac{5}{9} = 100^{\circ}$
- 23) 135°

- $\Rightarrow \angle A = 180^{\circ} \times \frac{3}{4} = 135^{\circ}$
- 24) 108°
- \Rightarrow $\angle C = \angle A = 180^{\circ} \times \frac{3}{5} = 108^{\circ}$
- 25) x = 3, y = 5
- 26) x = 5, y = 8
- 27) x = 10, y = 6
- 28) x=2, y=6
- 29) x = 6, y = 45
- ⇨ 평행사변형은 두 쌍의 대변의 길이가 같으므로 2x+1=3x-5 : x=6평행사변형은 두 쌍의 대각의 크기가 같으므로 $y^{\circ} + 135^{\circ} = 180^{\circ}$: y = 45
- 30) x = 4, y = 3
- 31) x = 5, y = 4
- $\Rightarrow x+8=3x-201 \text{M} \quad x=5$ 9 = 2y + 1에서 y = 4
- 32) x = 6, y = 2
- $\Rightarrow x+5=2x-1$ 에서 x=65y-4=6에서 y=2
- 33) x = 6, y = 4
- 34) x = 5, y = 1
- $\Rightarrow 2x+1=3x-4, x=5$ y+3=3y+1, y=1
- 35) x = 3, y = 1
- $\Rightarrow x+y=2(x-y), x+y=2x-2y$ $\therefore x=3y$ x+3=6y, 3y+3=6y, 3y=3 $\therefore y=1, x=3$
- 36) x = 100, y = 80
- 37) x = 14, y = 110
- 38) x = 120, y = 60
- 39) x = 50, y = 3
- 40) x = 40, y = 40
- 41) x = 60, y = 75
- 42) x = 9, y = 5
- 43) x = 6, y = 80

$$\Rightarrow x = \frac{1}{2} \times 12 = 6$$

$$\angle ABC = \angle D = 180^{\circ} - (40^{\circ} + 60^{\circ}) = 80^{\circ}$$

$$\therefore y = 80$$

44)
$$x=3$$
, $y=\frac{5}{2}$

45)
$$x = 7$$
, $y = 4$

$$\Rightarrow x+6=13 \text{ odd } x=7$$
$$2y+1=9 \text{ odd } y=4$$

46)
$$x = 8$$
, $y = 98$

$$\Rightarrow x = \overline{AB} = 8$$

 $\angle ODC = \angle OBA = 42^{\circ} (엊각) 이므로$
 $\angle AOD = 42^{\circ} + 56^{\circ} = 98^{\circ} \therefore y = 98$

47)
$$x = 11$$
, $y = 16$

48)
$$x = 5$$
, $y = 6$

49)
$$x = 6, y = 5$$

50)
$$x = 6$$
, $y = 8$

51)
$$x = 12, y = 80$$

52)
$$x = 54$$
, $y = 102$

$$ightharpoonup$$
 $ightharpoonup$ ig

53)
$$x = 6$$
, $y = 1$

$$\Rightarrow x = \frac{1}{2} \times 12 = 6, 3y + 2 = 5 \text{ old } y = 1$$

54)
$$x = 35, y = 50$$

55)
$$x = 9$$
, $y = 4$

56)
$$x = 16$$
, $y = 12$

57)
$$x=2$$
, $y=4$

평행사변형의 두 대각선은 서로를 이등분하므로
$$3x+2=8,\ 5x-y=6$$
이다.
 $\therefore \ x=2,\ y=4$

58)
$$\angle x = 65^{\circ}$$
, $\angle y = 65^{\circ}$

59)
$$\angle x = 55^{\circ}, \angle y = 125^{\circ}$$

60)
$$\angle x = 130^{\circ}, \angle y = 50^{\circ}$$

61)
$$\angle x = 30^{\circ}$$
, $\angle y = 65^{\circ}$

$$\Rightarrow$$
 $\overline{AB}//\overline{DC}$ 이므로 $\angle x = \angle BDC = 30^{\circ}$ (엇각)

$$\triangle$$
OAB에서 \angle AOB = 180 $^{\circ}$ $-$ (85 $^{\circ}$ $+$ 30 $^{\circ}$) = 65 $^{\circ}$ 이므로 \angle y = \angle AOB = 65 $^{\circ}$ (맞꼭지각)

62)
$$\angle x = 70^{\circ}$$
, $\angle y = 110^{\circ}$

$$ightleftrightarrow$$
 $ightleftarrow$ $ightleftarrow$

63)
$$\angle x = 30^{\circ}$$
, $\angle y = 100^{\circ}$

64)
$$\angle x = 45^{\circ}$$
, $\angle y = 105^{\circ}$

$$ightharpoons$$
 $ightharpoons$ $ightharpoo$

65)
$$\angle x = 75^{\circ}, \angle y = 65^{\circ}$$

$$Arr$$
 Arr Arr

66)
$$\angle x = 45^{\circ}, \angle y = 55^{\circ}$$

$$Arr$$
 $Arr x =
Arr BAC = 75 \degree (엇각)$
 $Arr B =
Arr D = 80 \degree 0 | 므로$
 $Arr y = 180 \degree - (45 \degree + 80 \degree) = 55 \degree$

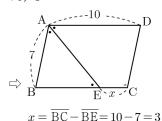
67)
$$\angle x = 30^{\circ}$$
, $\angle y = 80^{\circ}$

68)
$$\angle x = 30^{\circ}$$
, $\angle y = 70^{\circ}$

69) 2

⇒
$$\angle$$
 DAE = \angle AEB (엇각)이므로 \angle BAE = \angle BEA \triangle ABE는 이등변삼각형이므로 $\overline{AB} = \overline{BE}$ $\therefore x = \overline{BC} - \overline{BE} = 8 - 6 = 2$

70) 3



71) 4

$$Arr$$
 Arr Arr

72) 3

$$\angle$$
 ABE = \angle CEB(엇각)이므로 $\overline{BC} = \overline{CE}$
 $x = \overline{CD} - \overline{CE} = 8 - 5 = 3$

73) 3

□ AD//BC 이므로 ∠DPC = ∠ADP(엇각)
이때 ∠ADP = ∠CDP이므로 ∠CDP = ∠DPC
따라서 △PCD는 이등변삼각형이므로

 $\overline{PC} = \overline{DC} = 6 \text{ (cm)}$. $\overline{BP} = \overline{BC} - \overline{PC}$ 이므로 x = 9 - 6 = 3

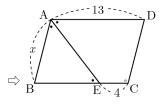
74) 2

 $ightarrow \overline{AB}//\overline{CE}$ 이므로 $\angle ABE = \angle CEB()$ 어때 $\angle ABE = \angle CBE$ 이므로 $\angle CBE = \angle CEB$ 따라서 $\triangle BCE$ 는 이등변삼각형이므로 $\overline{CE} = \overline{BC} = 10(cm)$, $\overline{DE} = \overline{CE} - \overline{CD}$ 이므로 x = 10 - 8 = 2

75) 80

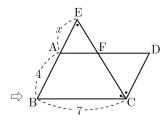
□ AD//BC이므로 ∠EBC = ∠AEB = 50°(엇작)
 ∴ ∠B = 2∠EBC = 2×50° = 100°
 따라서 ∠B + ∠C = 180°이므로
 ∠C = 180° - 100° = 80°
 ∴ x = 80

76) 9



 $x = \overline{BE} = \overline{BC} - \overline{EC} = 13 - 4 = 9$

77) 3



 $x = \overline{BB} - \overline{AB} = 7 - 4 = 3$

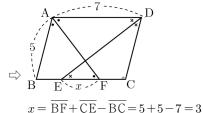
78) 4

□ ∠DAF = ∠AFB (엇각), ∠ADE = ∠DEC (엇각)이므로
 □ △ABF와 △DEC는 각각 이등변삼각형이다.

 $\therefore \overline{BF} = \overline{AB}, \overline{CE} = \overline{CD}$

 $\therefore x = \overline{BF} + \overline{CE} - \overline{BC} = 6 + 6 - 8 = 4$

79) 3



8U) 3

□ ∠ABE = ∠BEC(엇각)이므로 ∠EBC = ∠BEC

 $\therefore \overline{EC} = \overline{BC} = 8$

 $\therefore x = \overline{EC} - \overline{DC} = 8 - 5 = 3$

81) 16

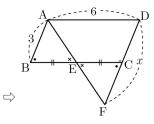
ightarrow ightarrow ightarrow ABE = ightarrow FCE (엇각), ightarrow ightarrow ightarrow ightarrow AEB = ightarrow FEC (맞꼭지각)이므로 ightarrow ABE = ightarrow AFCE (ASA 합동)

 $\therefore \overline{CF} = \overline{BA}$

평행사변형에서 대변의 길이는 같으므로 $\overline{\mathrm{AB}} = \overline{\mathrm{DC}}$

 $\therefore x = \overline{DC} + \overline{CF} = 8 + 8 = 16$

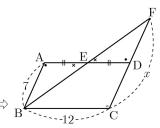
82) 6



 $\triangle ABE \equiv \triangle FCE(ASA$ 합동)

 $\therefore x = \overline{DC} + \overline{CF} = 3 + 3 = 6$

83) 14



 $\triangle ABE \equiv \triangle DFE(ASA 합동)$

 $\therefore x = \overline{CD} + \overline{DF} = 7 + 7 = 14$

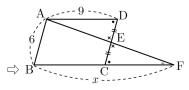
84) 3

Arr Arr ABE =
Arr BEC(엇각)이므로 <math>
Arr ABCE는 이등변 삼각형 이다.

 $\therefore \overline{EC} = \overline{BC}$

 $\therefore x = \overline{EC} - \overline{DC} = 9 - 6 = 3$

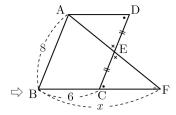
85) 18



 $\triangle AED \equiv \triangle FEC(ASA 합동)$

 $\therefore x = \overline{BC} + \overline{CF} = 9 + 9 = 18$

86) 12



$$\triangle$$
AED = \triangle FEC(ASA 합동)
 $\therefore x = \overline{BC} + \overline{CF} = 6 + 6 = 12$

- 87) 40
- Arr $Arr D =
 Arr B = 70^\circ$ Arr B =
 Arr D =
 Arr
- 88) 75°

$$\Rightarrow$$
 $\angle x = 180^{\circ} - 35^{\circ} - 70^{\circ} = 75^{\circ}$

89) 70°

$$\angle D = 180^{\circ} - 100^{\circ} = 80^{\circ}$$
이므로
 $\angle x = 180^{\circ} - (30^{\circ} + 80^{\circ}) = 70^{\circ}$

90) 22°

$$ightharpoonup$$
 $ightrarpoonup$ $ightharpoonup$ ig

91) 125°

$$ightharpoonup egin{aligned} igsplus BAD &= 180\,^\circ - 70\,^\circ = 110\,^\circ \mbox{ 이므로} \ & \ igsplus BAE &= rac{1}{2} \times 110\,^\circ = 55\,^\circ \ \mbox{ 따라서 } \ igsplus B &= 70\,^\circ \mbox{ 이므로 } \ igsplus x = 55\,^\circ + 70\,^\circ = 125\,^\circ \end{aligned}$$

92) 128°

$$Arr$$
 Arr Arr ADC = $180\,^{\circ}$ - $76\,^{\circ}$ = $104\,^{\circ}$ 이므로 Arr EDC = $104\,^{\circ}$ $axtriangle$ $axtriangle$ Arr $axtriangle$ $axtriangle$

- 94) 35°
- $ightharpoonup \angle D = \angle B = 75\,^{\circ}$ 이므로 $\triangle AED에서 \ \angle x = 110\,^{\circ} 75\,^{\circ} = 35\,^{\circ}$
- 95) 130 °
- 96) 54°
- 97) 50°

$$Arr$$
 Arr Arr ADC = Arr ABC = $80\degree$ 이므로
$$Arr$$
 ADH = $\frac{1}{2} \times 80\degree = 40\degree$
$$Arr$$
 Arr Arr