

# Itinerant Electron-Driven Chiral Magnetic Ordering and Spontaneous Quantum Hall Effect in Triangular Lattice Models

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We study the Kondo Lattice and the Hubbard models on a triangular lattice. We find that at the mean-field level, these rotationally invariant models naturally support a noncoplanar chiral magnetic ordering. It appears as a weak-coupling instability at the band filling factor  $3/4$  due to the perfect nesting of the itinerant electron Fermi surface. This ordering is a triangular-lattice counterpart of the collinear Neel ordering that occurs on the half-filled square lattice. While the long-range magnetic ordering is destroyed by thermal fluctuations, the chirality can persist up to a finite temperature, causing a spontaneous quantum Hall effect in the absence of any externally applied magnetic field.

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Interactions commonly lead to magnetism. For instance, the ground state of the half-filled Hubbard model becomes antiferromagnetic (AFM) for a finite on-site Coulomb interaction  $U$ . The AFM phase is collinear on bipartite lattices and exists for any finite  $U/t$  ( $t$  being the nearest-neighbor hopping) in the cases of square and cubic lattices due to nesting properties of the Fermi surface (FS). The situation is less clear when competing interactions or lattice topology lead to frustration and more complex magnetic orderings. For instance, a  $120^\circ$  three-sublattice (noncollinear) structure is stabilized on the half-filled triangular lattice for large enough  $U/t$  and a spin liquid ground state has been proposed for the kagome lattice. The *noncoplanar* spin orderings have proven to be particularly elusive. Besides being the next level in magnetic ordering complexity, the noncoplanar states have unusual transport [1] and magnetoelectric [2] properties resulting from their chiral structure. Consequently, it is important to find simple and realistic models in which such states could emerge and remain stable over a range of Hamiltonian parameters.

A triangular plaquette is a basic building block for lattices with built-in geometrical frustration. Assume that on every site  $i$  there is an ordered magnetic moment  $\mathbf{S}_i$ . If the moments on the plaquette are noncoplanar, the resulting scalar spin chirality,  $\langle \mathbf{S}_i \cdot \mathbf{S}_j \times \mathbf{S}_k \rangle \neq 0$ , breaks both the time-reversal and the parity symmetries. Notably, the scalar spin chirality can exist even without having statically ordered magnetic moments ( $\langle \mathbf{S}_i \rangle = \mathbf{0}$ ) [3]. When conduction electrons propagate through such a spin texture, they may exhibit spontaneous Hall effect in the absence of any externally applied magnetic field [4]. Moreover, if the spin ordering opens a full gap in the charge excitation spectrum, a spontaneous *quantum* Hall insulator can form [1]. This exotic phenomenon has the following origin: Because of the exchange interaction, the underlying local moment texture aligns the spins of the conduction electrons inducing a Berry phase in the electron wavefunction, which is indistinguishable from a “real” magnetic flux. Ohgushi

*et al.* [1], considered a model of 2D kagome ferromagnet where spin orbit interaction tilts the local moments so as to produce nonzero chirality. The spin configuration corresponded to total zero fictitious flux through the unit cell, while still creating nonzero quantized Hall conductivity at filling  $1/3$ . The authors were primarily concerned with the double exchange model, which assumes two species of electrons—the localized ones and the itinerant ones, but also suggested that similar physics may occur in a single band Hubbard-like model in the presence of spin-orbit interaction. Appearance of quantum Hall effects in systems with spontaneous *bond* ordering has recently been discussed in Raghu *et al.* [5].

In the present work we consider the Kondo lattice and the Hubbard models on a triangular lattice. We demonstrate that a noncoplanar magnetic ordering with uniform scalar spin chirality is self-consistently generated at the mean-field level. The magnetic ordering has the four-site unit cell, with the local spin orientations corresponding to the normals to the faces of a regular tetrahedron, see Fig. 1. This structure has been earlier proposed to describe the magnetic ordering in Mn monolayers on Cu(111) surfaces [6] and the nuclear spin ground state of a two-dimensional  $^3\text{He}$  [7]. In the Kondo lattice and the Hubbard models, this structure appears as a weak-coupling instability at  $3/4$  filling due to the nesting properties of the electronic Fermi surface, in close analogy to the magnetic instability of the half-filled square-lattice Hubbard model. The resulting insulating state at  $3/4$  filling exhibits spontaneous quantum Hall effect.

Let us first consider the Kondo-Lattice Hamiltonian,

$$H = -t \sum_{\langle ij \rangle} c_{i\alpha}^\dagger c_{j\alpha} - J \sum_i \mathbf{S}_i \cdot c_{i\alpha}^\dagger \boldsymbol{\sigma}_{\alpha\beta} c_{i\beta}, \quad (1)$$

which describes electrons hopping between the nearest-neighbor sites of triangular lattice interacting via on-site exchange coupling  $J$  with the localized moments  $\mathbf{S}_i$ . The operator  $c_{i\alpha}^\dagger$  ( $c_{i\alpha}$ ) creates (destroys) an electron with spin  $\alpha$  on site  $i$  and  $\boldsymbol{\sigma}_{\alpha\beta} = (\sigma_{\alpha\beta}^x, \sigma_{\alpha\beta}^y, \sigma_{\alpha\beta}^z)$  is a vector of the

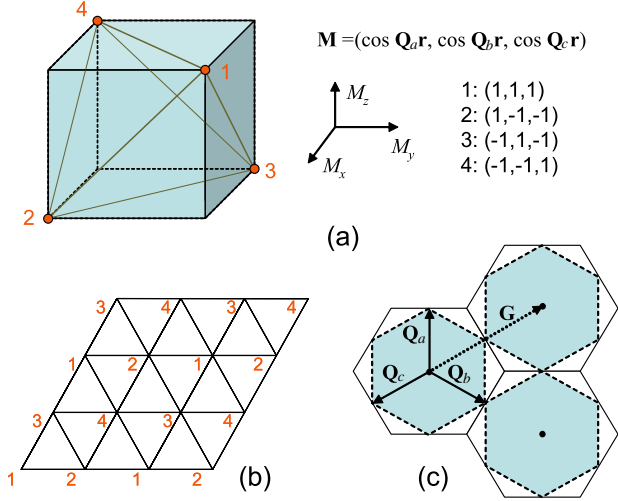


FIG. 1 (color online). Chiral spin ordering on a triangular lattice. (a) Four possible orientations of the local magnetic moments. They correspond to the normals to the faces of a regular tetrahedron. (b) Arrangement of the local moments on the real space lattice.  $\mathbf{a}_1$  and  $\mathbf{a}_2$  are the unit lattice vectors. (c) Momentum space. Unshaded hexagons define the Brillouin zones.  $\mathbf{G}$  is one of the reciprocal lattice vectors. Vectors  $\mathbf{Q}_\eta$  are the ordering vectors for the tetrahedral chiral order ( $|\mathbf{Q}_\eta| = G/2$ ). Note that  $\mathbf{Q}_\eta$  perfectly nest the 3/4-filled FS (shaded hexagons).

Pauli matrices. This model may describe various  $d$ - and  $f$ -electron compounds, with  $J$  being the ferromagnetic Hund's coupling in the first case and the antiferromagnetic Kondo exchange in the latter. We consider the classical limit  $S \gg 1$  for the localized spins. Then, the magnitude of  $|\mathbf{S}_i| = S$  is fixed and the only remaining degree of freedom is the spin orientation. The sign of  $J$  is irrelevant (the spectrum does not depend on this sign and the eigenstates are connected by a global time-reversal transformation of the localized spins). In the following, we take  $J > 0$ .

The simplest limit of  $H$  is the strong coupling,  $JS/t \gg 1$ . Two disconnected sectors appear in this regime: the low (high) energy subspace of states in which conduction electrons hop between neighboring sites remaining parallel (antiparallel) to the local moment  $\mathbf{S}_i$ . Within each sector, the conduction electron spin orientation is enslaved to its position, and the effective hopping amplitude acquires a quantum mechanical phase [8]. This Berry phase is indistinguishable from the Aharonov-Bohm phase in an externally applied magnetic field [9]. The effective Berry flux through a closed path is half of the solid angle subtended by the electron spin while moving along the path [10]. The fluxes experienced by electrons with spins aligned and antialigned with the local moments are equal in magnitude but opposite in sign. For the specific case of “tetrahedral” ordering, Fig. 1, the solid angle subtended by local moments in corners of each elementary triangular plaquette is clearly  $\Omega = 4\pi/4$ . Thus, in the limit of strong coupling, the problem is equivalent to one of electrons on a triangular

lattice in a uniform spin-dependent magnetic field corresponding to flux  $\phi_\sigma = \sigma\pi/2$  per triangular plaquette. The overall energy splitting between the spin-up and spin-down sectors is  $2JS$ . The energy spectrum can be easily found,

$$E_{\mathbf{k}} = \pm JS \pm \frac{2t}{\sqrt{3}} (\cos^2 \mathbf{k} \cdot \mathbf{a}_1 + \cos^2 \mathbf{k} \cdot \mathbf{a}_2 + \cos^2 \mathbf{k} \cdot \mathbf{a}_3)^{1/2}, \quad (2)$$

where  $\mathbf{a}_1$  and  $\mathbf{a}_2$  real space lattice vectors and  $\mathbf{a}_3 = \mathbf{a}_1 - \mathbf{a}_2$ . Since the real space (magnetic) unit cell has doubled, this dispersion is defined on *half* of the original reciprocal unit cell. The amplitude of the hopping is reduced by a factor  $\sqrt{3}$  due to the angle  $\theta$  between the neighboring spins,  $t \rightarrow t \cos(\theta/2) = t/\sqrt{3}$ . There are total four energy-split bands—(2 spins)  $\times$  (2 sites in magnetic unit cell). Thus for fillings that are integer multiples of  $1/4$ , the system is an insulator. Filling  $1/2$  corresponds to full filling of the spin-up sector, and therefore it is equivalent to a band insulator, with  $\sigma_{xy} = 0$ . The “interesting” fillings are  $1/4$  and  $3/4$ . From the explicit treatment of spinless electrons on triangular lattice [11], one finds that  $|\sigma_{xy}| = e^2/h$  in both cases, but with opposite signs, since spin-up and spin-down electrons experience opposite effective magnetic fluxes.

Now we turn to the case of an arbitrary  $JS/t$ . From Fig. 1, the unit cell in the ordered state is *quadrupled*—it is now spanned by vectors  $2\mathbf{a}_1$  and  $2\mathbf{a}_2$ . It is convenient to treat to problem in the momentum space. For that we notice that the tetrahedral magnetic ordering is equivalent to the so-called  $3q$  noncoplanar state, with the order parameter

$$\mathbf{S}(\mathbf{r}) = (S_a \cos \mathbf{Q}_a \cdot \mathbf{r}, S_b \cos \mathbf{Q}_b \cdot \mathbf{r}, S_c \cos \mathbf{Q}_c \cdot \mathbf{r}). \quad (3)$$

The amplitudes  $S_\alpha$  are equal in magnitude but can have different signs (arbitrary global rotation of the triad in the spin space yields an equivalent state). The ordering vectors  $\mathbf{Q}_\alpha$  are equal to half of the reciprocal lattice vectors; see Fig. 1(c). Therefore, momenta  $+\mathbf{Q}_\eta$  and  $-\mathbf{Q}_\eta$  are equivalent ( $\mathbf{Q}_\eta \equiv -\mathbf{Q}_\eta$ ), and  $\pm \mathbf{Q}_a \pm \mathbf{Q}_b \pm \mathbf{Q}_c \equiv 0$ . The scalar chirality, defined as a counterclockwise triple product  $\mathbf{S}_1 \cdot (\mathbf{S}_2 \times \mathbf{S}_3) \propto S_a S_b S_c$  around a plaquette [e.g., 123 in Fig. 1(b)] can be either positive or negative, depending on the choice of  $S_\alpha$ . To be specific, let us chose all  $S_\alpha > 0$ , Fig. 1(a). In momentum space the Hamiltonian Eq. (1) becomes

$$H = \sum_{\mathbf{k}\sigma} \epsilon_{\mathbf{k}} c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}\sigma} - J \sum_{\mathbf{k}\alpha\beta\eta} S_\eta c_{\mathbf{k}\alpha}^\dagger \sigma_{\alpha\beta}^\eta c_{\mathbf{k}+\mathbf{Q}_\eta\beta}, \quad (4)$$

where  $\epsilon_{\mathbf{k}} = -2t \sum_{i=1}^3 \cos \mathbf{k} \cdot \mathbf{a}_i$  and  $\eta = a, b, c$ . The momentum summation is over the quarter of the original reciprocal unit cell. The Hamiltonian splits into two disjoint parts

$$H = \mathbf{c}_I^\dagger \hat{H} \mathbf{c}_I + \mathbf{c}_{II}^\dagger \hat{H} \mathbf{c}_{II}, \quad (5)$$

$$\hat{H} = \begin{pmatrix} \epsilon_{\mathbf{k}} & JS_a & iJS_b & JS_c \\ S_a & \epsilon_{\mathbf{k}+\mathbf{Q}_a} & -JS_c & -iJS_b \\ -iJS_b & -JS_c & \epsilon_{\mathbf{k}+\mathbf{Q}_b} & JS_a \\ JS_c & iJS_b & JS_a & \epsilon_{\mathbf{k}+\mathbf{Q}_c} \end{pmatrix}, \quad (6)$$

where  $\mathbf{c}_I^\dagger = (c_{\mathbf{k}\uparrow}^\dagger, c_{\mathbf{k}+\mathbf{Q}_a\uparrow}^\dagger, c_{\mathbf{k}+\mathbf{Q}_b\uparrow}^\dagger, c_{\mathbf{k}+\mathbf{Q}_c\uparrow}^\dagger)$  and  $\mathbf{c}_{II}^\dagger = (c_{\mathbf{k}\downarrow}^\dagger, c_{\mathbf{k}+\mathbf{Q}_a\downarrow}^\dagger, -c_{\mathbf{k}+\mathbf{Q}_b\downarrow}^\dagger, -c_{\mathbf{k}+\mathbf{Q}_c\downarrow}^\dagger)$ . Therefore, the spectrum is (at least) doubly degenerate. The physical reason for the degeneracy is the same as for the degeneracy between the spin-up and spin-down band in a mean-field treatment of an antiferromagnet on a square lattice—the spin-up and spin-down wave functions are related by a lattice translation combined with a spin rotation. Indeed, from Fig. 1(b), the local moment arrangement changes as  $(1 \leftrightarrow 2, 3 \leftrightarrow 4)$  under translation by  $\mathbf{a}_1$ . From Fig. 1(a), a spin rotation by angle  $\pi$  around  $x$  axis restores the initial state. Therefore, the composition of both transformations leaves  $\hat{H}$  unchanged, while  $c_{II} \leftrightarrow c_I$ .

Figure 2 shows the band structure corresponding to  $H$  in the reduced (quarter) reciprocal unit cell with the axes chosen along  $\mathbf{Q}_a$  and  $\mathbf{Q}_b$ . For an arbitrary value of  $JS/t$ , there are four pairs of degenerate bands. For large enough  $JS/t$ , there is a gap between all pairs, and the dispersion is well described by Eq. (2). The Hall conductivity can be calculated directly using the Kubo formula,

$$\sigma_{xy} = \frac{e^2}{h} \frac{1}{2\pi i} \sum_{nm\mathbf{k}} \frac{j_x^{nm} j_y^{mn}}{(\epsilon_{n\mathbf{k}} - \epsilon_{m\mathbf{k}})^2} [n_F(\epsilon_{n\mathbf{k}}) - n_F(\epsilon_{m\mathbf{k}})], \quad (7)$$

with summation performed over all 8 bands  $n, m$  and  $(j_x, j_y)$  being the  $x$  and  $y$  components of the current operator. At zero temperature, when the Fermi distribution functions  $n_F$  are 1 for occupied bands and 0 for the empty ones, we recover the results for  $\sigma_{xy}$  obtained earlier for  $JS/t \gg 1$ . Each pair of degenerate bands contributes Chern number

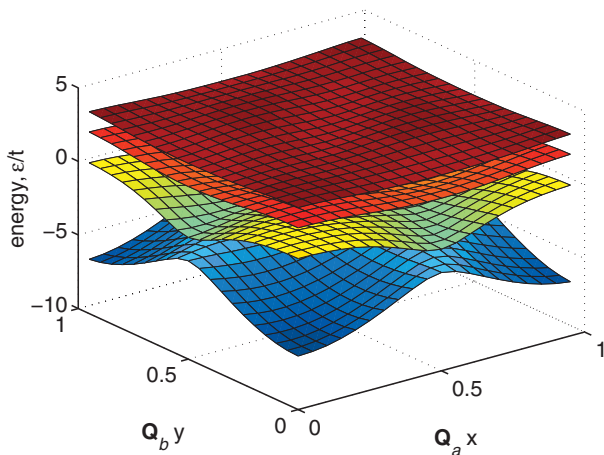


FIG. 2 (color). Band structure corresponding to Eq. (5). The coupling strength is  $JS/t = 1$ . The axes are chosen along  $\mathbf{Q}_a$  and  $\mathbf{Q}_b$  and point (0,0) corresponds to the center of the first Brillouin zone.

$\pm 1$ , instead of 0 or  $\pm 2$ , due to the additional local (in  $\mathbf{k}$ -space)  $SU(2)$  symmetry implied by the degeneracy [12].

For small  $JS/t$ , the lower three pairs of bands overlap. However, the gap between the two upper bands persists for arbitrarily small  $JS/t$ . This signifies a weak-coupling instability towards  $3q$  ordering at  $3/4$  filling (1.5 electrons per site). Indeed, at this filling the FS of noninteracting electrons is a regular hexagon inscribed into the first Brillouin zone [see Fig. 1(c)]. The vectors  $\mathbf{Q}_\eta$  perfectly nest all sides of the FS, and hence a local interaction will cause the  $3q$  instability. In general, an ordering  $\mathbf{S}_\eta \cos(\mathbf{Q}_\eta r)$  with arbitrarily directed  $\mathbf{S}_\eta$  is expected. However, the constraint of same magnetization magnitude on every lattice site  $|\mathbf{S}_i| = S$  requires that  $\mathbf{S}_\eta$  be mutually orthogonal, leading to Eq. (3). The quantum Hall conductivity at  $3/4$  filling for arbitrarily small  $JS/t$  is  $\sigma_{xy} = e^2/h$  at zero temperature.

We now consider the possibility that the local moments do not originate from localized electrons on different orbitals, but are generated self-consistently in a single-band Hubbard model  $H_{\text{Hubb}}$  on a triangular lattice. The connection between this case and the one studied above is evident from the mean-field expression of  $H_{\text{Hubb}}$  [10]:

$$H_{\text{Hubb}} = -t \sum_{\langle ij \rangle} c_{i\alpha}^\dagger c_{j\alpha} - \frac{2U}{3} \sum_i 2\langle \mathbf{S}_i \rangle \mathbf{S}_i - \langle \mathbf{S}_i \rangle^2. \quad (8)$$

Now all the spin degrees of freedom are provided by the same (itinerant) electrons and  $\langle \mathbf{S}_i \rangle = \frac{1}{2} \langle c_{i\alpha}^\dagger \boldsymbol{\sigma}_{\alpha\beta} c_{i\beta} \rangle$ . The result of the self-consistent calculation for the noncoplanar  $3q$  order parameter as a function of temperature is presented in Figure 3. The finite-temperature calculation of the transverse conductivity based on Eq. (7) reveals that  $\sigma_{xy}$  is a good proxy of the order parameter.

$H_{\text{Hubb}}$  has the same form as Eq. (1) but  $\langle \mathbf{S}_i \rangle^2$  is no longer fixed due to quantum fluctuations ( $\mathbf{S}_i$  is now in the  $S = 1/2$  quantum limit). The relaxation of this constraint allows for

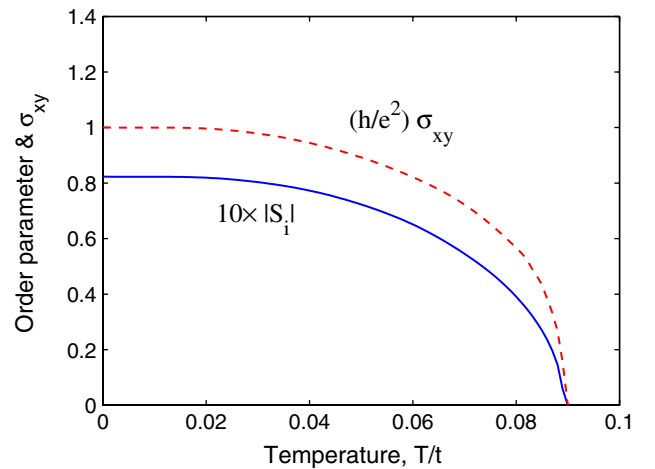


FIG. 3 (color online). Hubbard model,  $U = 4t$ . The magnitude of the order parameter for noncoplanar  $3q$  structure and Hall conductivity as a function of temperature.

more general  $3q$  structures such as collinear or coplanar. The energy difference between the  $3q$  collinear, coplanar, and noncoplanar structures is very small, since it is caused by the interaction between the order parameters  $\mathbf{S}_\eta$  at the corners of the FS. Numerically we find that the coplanar (but noncollinear) phase is not favored, while the noncoplanar and collinear [13]  $3q$  structures are very close in energy at the mean-field level. An analysis beyond mean field would be required to determine the relative stability of the two phases.

A spontaneous breaking of a continuous symmetry is impossible at finite temperature in 2D for short-range interactions [14]. Does this imply that finite-temperature spontaneous quantum Hall effect is impossible? To answer this question we need to analyze the symmetry of the problem in more detail. To that end we consider the Ginzburg-Landau theory for the  $3q$  magnetic structure. It can be constructed in close analogy to the theory for the Heisenberg antiferromagnet on a square lattice. However, instead of a single mean-field order parameter at momentum  $(\pi, \pi)$ , now there are three order parameters, with the ordering wavevectors  $\mathbf{Q}_\eta$ . To the lowest order, they do not interact and each is described by the standard AFM Lagrangian,  $\mathcal{L}_\eta = [-r + \omega^2 - (\mathbf{q} - \mathbf{Q}_\eta)^2]|\mathbf{S}_\eta^q|^2 - u|\mathbf{S}_\eta^q|^4/2$ , with appropriately scaled frequencies and momenta [15]. The transition is controlled by the parameter  $r$  which can be tuned by, e.g., temperature. Given the momentum space structure of the order parameters, the first symmetry-allowed term that selects the mutual orientation of the order parameters is  $\mathcal{L}_{\text{int}} = v[\mathbf{S}_a \cdot (\mathbf{S}_b \times \mathbf{S}_c)]^2$ . Negative value of  $v$  favors noncoplanar configuration with  $\mathbf{S}_\eta$  orthogonal to each other, while  $v > 0$  favors configuration with  $\mathbf{S}_\eta$  collinear [13]. This term reduces the symmetry of the Lagrangian down to  $SO(3) \times Z_2$ ; however, being higher order in  $S$ , it does not modify the mean-field transition temperature. Noncoplanar ordering corresponds to complete breaking of this symmetry. Thus, by the number of  $SO(3)$  generators, there are three gapless (linearly dispersing) Goldstone modes. In addition, there are three modes that have a small gap  $\sqrt{-vr^2/u^2}$  induced by the orientation-locking term.

The gapless modes are responsible for the destruction of the long-range magnetic ordering at finite temperature. However, smooth distortion of the magnetic texture does not necessarily destroy the chirality [16]. The chirality is a discrete (Ising) order parameter, which can be destroyed in two ways: Through point defects—vortices, and line defects—domain walls. Since the order parameter space (the “vacuum manifold”) of the model is given by  $SO(3)$ , there are only two topologically distinct kinds of  $(Z_2)$  vortices—the trivial and the nontrivial one [17], in contrast to the more familiar  $U(1)$  vortices, which can have an arbitrary integer winding number. At the vortex core, one or more of the order parameters  $\mathbf{S}_\eta$  is completely suppressed. The vortices effectively reduce the *magnitude* of average chirality, without changing its sign. On the other hand, a

domain wall corresponds to a line where the sign of chirality changes via mutual reorientation of the order parameters, without necessarily changing their magnitude (at the domain wall the state is coplanar). The finite-temperature transition can be governed by either proliferation of domain walls [18] or vortices [19], depending on the relative importance of the individual order parameter stiffness and the chiral locking term in the free energy. For the small- $U$  Hubbard model the chiral term is relatively weak. Thus the domain walls have low energy cost, and the phase transition is likely to be in the generalized Ising class [7].

In conclusion, we studied a model of itinerant electrons interacting with a chiral magnetic texture on a triangular lattice. We found that at  $3/4$  filling the system can become a spontaneous quantum Hall insulator, even without static magnetic ordering. One possible material realization is  $\text{Na}_{0.5}\text{CoO}_2$  [20].

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- [1] K. Ohgushi, S. Murakami, and N. Nagaosa, *Phys. Rev. B* **62**, R6065 (2000).
  - [2] L. N. Bulaevskii *et al.*, *Phys. Rev. B* **78**, 024402 (2008).
  - [3] J. C. Domenge *et al.*, *Phys. Rev. B* **72**, 024433 (2005).
  - [4] Y. Taguchi *et al.*, *Science* **291**, 2573 (2001).
  - [5] S. Raghu *et al.*, *Phys. Rev. Lett.* **100**, 156401 (2008).
  - [6] Ph. Kurz *et al.*, *Phys. Rev. Lett.* **86**, 1106 (2001).
  - [7] T. Momoi, K. Kubo, and K. Niki, *Phys. Rev. Lett.* **79**, 2081 (1997).
  - [8] P. W. Anderson and H. Hasegawa, *Phys. Rev.* **100**, 675 (1955).
  - [9] R. Peierls, *Z. Phys.* **80**, 763 (1933).
  - [10] E. Fradkin, *Field Theories of Condensed Matter Systems* (Perseus Books, New York, 1991).
  - [11] Y. Hatsugai and M. Kohmoto, *Phys. Rev. B* **42**, 8282 (1990).
  - [12] M. Kohmoto, *Ann. Phys. (N.Y.)* **160**, 343 (1985).
  - [13] L. Balents and A. Paramakanti, *Phys. Rev. B* **67**, 134427 (2003).
  - [14] N. D. Mermin and H. Wagner, *Phys. Rev. Lett.* **17**, 1133 (1966).
  - [15] Note that near  $T = 0$  free electron susceptibility is most strongly divergent at momenta  $\mathbf{Q}_i$  but is highly anisotropic.
  - [16] J. Villain, *J. Phys. (Paris)* **38**, 385 (1977).
  - [17] H. Kawamura and S. Miyashita, *J. Phys. Soc. Jpn.* **53**, 4138 (1984).
  - [18] L. Capriotti and S. Sachdev, *Phys. Rev. Lett.* **93**, 257206 (2004).
  - [19] J.-C. Domenge *et al.*, *Phys. Rev. B* **77**, 172413 (2008).
  - [20] F. L. Ning *et al.*, *Phys. Rev. Lett.* **100**, 086405 (2008).