

TOWARDS BETTER PERCEPTION OF URBAN INFORMATION: A VISUALIZATION PERSPECTIVE.

by

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31 October 2019

TABLE OF CONTENTS

Title Page	i
Authorization Page	ii
Signature Page	iii
Table of Contents	iv
List of Figures	vii
List of Tables	ix
Abstract	x
Chapter 1 Introduction	1
Chapter 2 Visual Exploration of Human-Scale Urban Forms Based on Street Views	2
2.1 Introduction	2
2.2 Related Work	4
2.2.1 Street View Analysis	4
2.2.2 Urban Data Visualization	5
2.2.3 Multivariate Geographical Data Visualization	6
2.2.4 Comparative Visualization	7
2.3 Background and Analytical Tasks	7
2.3.1 Background	7
2.3.2 Analytical Tasks	9
2.4 System Framework	10
2.5 Data Modeling	11
2.5.1 Data Collection	12
2.5.2 Feature Extraction	12
2.5.3 Data Querying and Filtering	13
2.6 Visualization Design	14

2.6.1	Design Rationales	14
2.6.2	Ranking Explorer	16
2.6.3	AOI Explorer	16
2.6.4	Street Explorer	20
2.6.5	User Interactions	23
2.7	Case Studies	25
2.7.1	City-scale Comparison	25
2.7.2	Region-scale Exploration	26
2.7.3	Street-scale Comparison	28
2.8	Expert Review	30
2.9	Discussion	32
2.10	Conclusion and Future Work	33
Chapter 3	Route-Aware Edge Bundling for Visualizing Origin-Destination Trails in Urban Traffic	35
3.1	Introduction	35
3.2	Related Work	37
3.3	Problem Statement and System Overview	39
3.3.1	KDEEB Algorithm	40
3.3.2	Problem Identification	41
3.3.3	RAEB Overview	42
3.4	Preprocessing	43
3.4.1	Basic Traffic Concepts	43
3.4.2	Map Matching	44
3.4.3	Hierarchical Route Structure Construction	45
3.4.4	Trail Abstraction	46
3.5	Bundling Method	47
3.5.1	Optimal Kernel Size	47
3.5.2	Density Map Generation	48
3.6	Evaluation	49
3.6.1	Normalized Mutual Information	49
3.6.2	Bundle Deviation	51
3.7	Applications	52

3.7.1	Artificial OD Trails	52
3.7.2	New York Taxi Trips	54
3.7.3	Shenzhen Taxi Trips	55
3.8	Discussion	56
3.8.1	Parameters	56
3.8.2	Performance	58
3.8.3	Applicability and Limitations	59
3.9	Conclusion and future work	60
References		62

LIST OF FIGURES

2.1	Overview of StreetVizor workflow. Our system consists of two phases: data modeling and interactive visual exploration.	10
2.2	Illustration of data preprocessing: sampling locations in New York City are generated from OpenStreetMap (left), a street view image is collected from Google Street View (center), and the image pixels are classified into six features using SegNet (right).	11
2.3	Data model: street views with six-dimensional features of <i>greenery</i> , <i>sky</i> , <i>building</i> , <i>road</i> , <i>vehicle</i> and <i>others</i> , are organized in an octree structure and a street lookup table.	14
2.4	StreetVizor system. (a) Control panel enables multi-scale navigation, ranking exploration, and feature filtering. (b) Side-by-side map views compare the spatial distribution of human-scale urban forms in two areas-of-interest (AOIs). (c) AOI statistic view presents the quantitative measurements, including correlation, histogram, and diversity in the AOIs shown in (b). (d) Street map views present detailed street views along two streets. (e) Street statistic view extends parallel coordinates with street layouts.	15
2.5	The AOI Statistic View combines (a) a scatterplot matrix to show pairwise correlations between two features, (b) small multiples of histogram bar charts to overview feature distributions, and (c) small multiples of deviation plots to present feature diversity.	17
2.6	Street Map View provides an overview of all street views along a street as colored points, and highlights images on two sides of the street. (a) A tree map showing the feature composition of an image will pop up when the mouse pointer is hovered over the image.	20
2.7	Overview of the construction process for Street Statistic View: (a) Construct minimum bounding box of the street network. (b) Rotate the street network such that its bounding box fits in the rendering space. (c) Plot the meriver style visualization within the rendering space. (d) Enhance parallel coordinates with street layouts on both sides.	22
2.8	AOI Map View compares spatial distributions of human-scale urban forms in Singapore (left) and Greater London (right). Orange points (buildings) are concentrated around the highlighted center area of Greater London, i.e., City of London.	23
2.9	AOI Statistic View in coordination with Fig. 2.8 presents quantitative measurements differences of human-scale urban forms in Singapore (red) and Greater London (blue).	24
2.10	Top three districts with highest building ratios, while bottom three with highest greenery ratios in Hong Kong.	25

2.11 Region-scale comparison of Tanglin in Singapore with Central Park in New York City.	27
2.12 Street Explorer compares the differences in human-scale urban forms of two streets in Brooklyn, New York City (left) and Kowloon, Hong Kong (right). The left street views contain more balanced features, whereas the right street views are dominated by building and road.	29
3.1 Methods for visualizing OD trails in urban traffic: (a) map matching, (b) vector map, (c) & (d) KDEEB bundles rendered in density and direction, respectively.	38
3.2 KDEEB applied to taxi trips in Manhattan with different kernel sizes p_r : (a) 120, (b) 80, (c) 40, and (d) 20. More detailed bundles are generated with smaller p_r .	40
3.3 Overview of RAEB pipeline. Our method mainly consists of three phases: <i>Preprocessing</i> for creating a proper initial layout, <i>Bundling</i> for bundling input OD trails, and <i>Evaluation</i> for generating a stable bundle structure.	41
3.4 Illustration of hierarchical route structure and OD trail abstraction: (a) Three route levels are constructed colored in blue, purple and green, respectively; a raw OD trail is abstracted in accordance to route (b) level-3, (c) level-2, and (d) level-1.	46
3.5 (left) Bundling stability p_{bs} measured at each bundling iteration for different decay ratios λ , (right) visually indistinguishable images are generated at iteration 10 and 11 for $\lambda = 0.9$.	50
3.6 Leftmost: raw 100K artificial OD trails on a grid road network in three hierarchies. (a) - (d): RAEB bundling results with route awareness parameter p_{ra} set to 0 - 3, respectively.	50
3.7 Left: raw 100K artificial OD trails on a hierarchical road network. Right: RAEB bundling result with p_{ra} set to 2.	51
3.8 Density maps of NYC taxi trips: (a) shortest paths mapped onto the road network, (b) KDEEB bundles with kernel size $p_r = 60$, (c) KDEEB bundles with $p_r = 21$, and (d) our RAEB bundles with $p_r = 21$.	52
3.9 Fine scale density maps of NYC taxi trips in Queens zone generated by (a) KDEEB, and (b) RAEB.	52
3.10 Density maps of Shenzhen taxi trips: (a) raw GPS records are mapped onto road network, (b) KDEEB bundles trips on close aerial roads together, while (c) RAEB preserves these roads. All lines are colored according to the OD directions.	53

LIST OF TABLES

3.1	Route hierarchy, OSM indicator and hierarchy score	45
3.2	Main parameter adaptions in RAEB, in comparison with these in KDEEB.	56
3.3	Statistics comparison of KDEEB and RAEB for datasets used in the experiments.	58

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ABSTRACT

TBD

CHAPTER 1

INTRODUCTION

TBD

CHAPTER 2

VISUAL EXPLORATION OF HUMAN-SCALE URBAN FORMS BASED ON STREET VIEWS

Urban forms at human-scale, i.e., urban environments that individuals can sense (e.g., sight, smell, and touch) in their daily lives, can provide unprecedented insights on a variety of applications, such as urban planning and environment auditing. The analysis of urban forms can help planners develop high-quality urban spaces through evidence-based design. However, such analysis is complex because of the involvement of spatial, multi-scale (i.e., city, region, and street), and multivariate (e.g., greenery and sky ratios) natures of urban forms. In addition, current methods either lack quantitative measurements or are limited to a small area. The primary contribution of this work is the design of StreetVizor, an interactive visual analytics system that helps planners leverage their domain knowledge in exploring human-scale urban forms based on street view images. Our system presents two-stage visual exploration: 1) an AOI Explorer for the visual comparison of spatial distributions and quantitative measurements in two areas-of-interest (AOIs) at city- and region-scales; 2) and a Street Explorer with a novel parallel coordinate plot for the exploration of the fine-grained details of the urban forms at the street-scale. We integrate visualization techniques with machine learning models to facilitate the detection of street view patterns. We illustrate the applicability of our approach with case studies on the real-world datasets of four cities, i.e., Hong Kong, Singapore, Greater London and New York City. Interviews with domain experts demonstrate the effectiveness of our system in facilitating various analytical tasks.

2.1 Introduction

Human-scale urban form describes fine-scale characteristics of urban environments that can be directly seen, touched, and experienced by a city's residents in their daily lives [54]. It is typically measured in high-resolution by sight and hearing, i.e., from several to tens

of meters. Compared with a city's scale, which is usually measured in kilometers, this scale is human-oriented. As humans pay more attention to interactive surroundings [26], understanding human-scale urban forms is essential for urban planners in designing high-quality urban spaces. However, traditional urbanism theories, such as small-scale surveys and mapping, are hard to provide in-depth guidance for effective urban planning and design at this fine scale.

Given the advancement of various sensing technologies, e.g., cameras and GPS devices, we can now quantitatively measure human-scale urban forms by analyzing big urban data. In particular, services, such as Google Street View (GSV) [4], provide detailed panoramic views of urban space from different geographic positions. These panoramic views can be utilized to measure various features, including greenery coverage and sky visibility, of human-scale urban forms visible to human eyes. Some pioneering studies have shown that neighborhood environment [64], street-level greenery [49], and even street safety [58] can be precisely assessed from these views.

However, GSV image exploration mainly focuses on either a particular feature (e.g., greenery coverage [49]) or a small area (e.g., neighborhood [64] and street [49, 58]). This deficiency limits its applicability in urban planning, where planners need to 1) quantitatively measure multivariate features of urban forms, including not only greenery coverage, but also sky visibility, and vehicle density [53]; 2) systematically explore urban forms in areas-of-interest (AOIs) at multiple scales, i.e., from small (e.g., streets) to mid (e.g., districts) to large scales (e.g., cities) [52]. In addition, direct means for the comparison of urban forms in two AOIs is desirable to allow planners to utilize information for the quick identification and improvement of factors that affect the quality of urban space.

A visual analytics tool is necessary to fulfill these requirements because it can integrate powerful computing capabilities to quantitatively measure multivariate features, with interactive visual interfaces to systematically explore and compare features in AOIs on demand [70]. Developing such a tool requires considerable effort because of the following reasons: first, as cities comprise vast amounts of street views, an efficient feature extraction algorithm is required to automatically uncover human-scale urban forms. Second, the development of a tool for the visual comparison of multivariate features in two AOIs requires an effective visual design that tackles the challenges of spatial, multivariate, and

comparative data visualizations.

In this paper, we introduce StreetVizor, a visual analytics system for the exploration of human-scale urban forms based on GSV images. We develop the system in an iterative design process: specific analysis requirements are described by a collaborating urban planner, and the designs are evaluated and refined against requirements. To present information in concisely, StreetVizor combines a set of well-established visualization techniques, including coordinated multiple views (CMVs) and scatterplot matrix, with a new design of parallel coordinates that integrate street layout information. Our system utilizes advanced clustering models to enable the efficient exploration of street view patterns. We apply StreetVizor in real-world datasets containing ~1.7 million of GSV images of four cities: Singapore, Hong Kong, Greater London, and New York City, and demonstrate its effectiveness through interviews with domain experts.

The main contributions of this work include:

- A fully automatic approach measuring human-scale urban forms by applying deep learning techniques on GSV images;
- A visual comparison framework for exploring human-scale urban forms on city-, region-, and street-scales;
- A novel visual design of parallel coordinates that integrate street layout information;
- Interesting insights revealed from case studies and expert interviews, such as the negative correlation between greenery and building features, and the differences in street views of two cities.

2.2 Related Work

This section discusses previous studies closely related to our work.

2.2.1 Street View Analysis

GSV system provides high quality and accurate panoramic images of hundreds of cities [4]. In recent years, researchers studying human-scale urban forms have utilized GSV im-

ages as a new and convenient data source. For example, researches have shown that the analysis of GSV images can be used to audit neighborhood environments [64], quantify street greenery [49], and predict street safety [58]. Nonetheless, the majority of these studies face scalability issues given their focus on either a particular feature [49] or a small area [49, 58, 64]. These issues can be addressed by incorporating deep learning techniques, which can be used to summarize city landscapes [18] and estimate the demographic makeup of a country [25].

In this work, we collect ~1.7 million GSV images of four representative mega-cities, and apply a deep learning technique [7] to automatically extract desired urban forms from the collected images. More importantly, we develop an effective visual analytics tool for urban planners to explore human-scale urban forms.

2.2.2 Urban Data Visualization

Vast amounts of urban data, including traffic [23, 81], social media [12, 84], environment [21], and simulated urban spaces [75], have been collected in an urban context. Big urban data brings in unprecedented opportunities for evidence-based urban design, and visualization systems can assist domain experts in finding evidence from the data. A systematic overview of visualization systems can be found in [89].

Qu et al. [63] presented a comprehensive visualization system for the analysis of a city's air pollution that affects the daily lives of residents. Their system integrates parallel coordinates and scatterplots to show relationships between high-dimensional air pollutants. In addition to air pollution, landmark visibility is related to the daily experience of a city's residents. Ortner et al. [60] visually compared the effects of candidate buildings on landmark visibility from various viewpoints. In this system, users can select a series of ranking schemes, and candidate buildings are then automatically sorted. Similar to our present work, Arietta et al. [5] associated visual elements with city attributes, including violent crime rates and housing prices. They developed various prototype visualizations, such as the visual boundary of urban neighborhoods.

Although different data are explored, these visualizations similarly employ CMVs, because urban data typically exhibits both spatial information and multi-dimensional at-

tributes. Our system also adopts this empirical approach. In addition, to address specific domain problems, we develop effective visualization techniques, including a novel parallel coordinates enhanced with street layouts.

2.2.3 Multivariate Geographical Data Visualization

Visualizing multivariate data is a hot topic in the visualization field. Numerous conventional approaches to this topic have been developed, and can be classified into two groups: 1) employing visualization techniques, such as parallel coordinates plot (PCP), scatterplot matrix, and star coordinates; and 2) projecting data points onto a two- or three-dimensional visual space that can be directly plotted on a screen, such as multi-dimensional scaling and principal component analysis. All these approaches have pros and cons. For example, although PCP presents all dimensional attributes without information loss, it can easily generate visual clutter with big data and pairwise correlations can only be shown on two nearby coordinates [34]. Many improvements have been developed to address these issues. These improvements include edge bundling to reduce visual clutter [37, 92], and hierarchical data clustering and the navigation of resulting structures [24, 88].

When multivariate data is dependent upon locations, the analytical tasks become more complex because geographical information needs to be revealed. Turkay et al. developed *Attribute Signature* [73], which employs a geographical map and small multiples of multivariate attributes to show geographic variability in attribute statistics. Goodwin et al. [28] further explored multivariate geographical data across scales by adopting new designs to show correlation, scale, and geographical information. The frameworks proposed by both studies can be generalized to explore multivariate geographical data.

In this work, human-scale urban forms to be explored are also multivariate geographical data: the features are in six dimensions and they are dependent on locations. We leverage the advantages of scatterplot matrix and PCP for different analytical tasks. Specifically, we employ scatterplot matrix for exploring features at city- and region scales given that it can effectively reveal correlations between all pair-wise features. We also arrange the views in a way similar to *Attribute Signature* [73], i.e., geographical information is presented on maps and multivariate attributes in small multiples. In addition, we develop a

novel PCP enhanced with a themeriver plot, which fits better with the analytical task of showing feature variations along street layout at street-scale.

2.2.4 Comparative Visualization

Gleicher et al. [27] classified techniques for visual comparison into three categories: 1) Juxtaposition, i.e., presenting objects next to each other. For example, NodeTrix [85] arranges two human brain networks side-by-side. 2) Superposition, i.e., presenting multiple objects on top of one another. Typical examples are time-series line graphs that plot the changes in several variables over time in the same coordinate system. 3) Explicit encoding, i.e., presenting differences or correlations between objects visually. For instance, the bivariate density map is employed in [87] to show the relationship between departure and arrival movements over space. In practice, these techniques are combined to address complex analytical tasks.

Our work adopts juxtaposition that arranges maps of two AOIs/streets side-by-side (Fig. 2.4(b) & (d)), and superposition to compare multivariate features of two AOIs/streets in the same coordinate system (Fig. 2.4(c) & (e)).

2.3 Background and Analytical Tasks

In this section, we introduce our research background and summarize the desired analytical tasks.

2.3.1 Background

Although the concept of human-scale urban form has only been recently defined [54], its discussions in the context of urban planning has a long history that can be traced back to the 1960s. A series of pioneering studies [26,40] claimed the positive effects of understanding human-scale urban forms in designing high-quality urban space. Visible human-scale urban forms are particularly important as human beings tend to pay most attentions to surroundings that can be directly seen [26].

Over the past 10 months, we closely worked with a senior researcher (SR) in the field of evidence-based urban design – an emerging research topic in urban planning and design. SR pointed out that though urban planners have begun to realize the importance and usefulness of street views in analyzing visible urban forms (e.g., [49, 58, 64]), systematic and efficient methods that can facilitate exploration remain lacking. Hence, SR proposed the development of an efficient visual analytics tool for exploring human-scale urban forms based on GSV images.

To better understand the problem domain, we conducted several rounds of structured interviews with SR. The main analysis criteria are summarized below:

- **Multivariate Features.** As images contain rich information on the urban environment, the first step is to identify the urban forms for analysis. Here, we identify five key features that can reflect the quality and livability of street spaces [26, 40], i.e., greenery, sky, building, road, and vehicle features. Greenery reflects the pleasing greenery view of a street; sky and building are correlated with the sense of street closure negatively and positively, respectively; and increments in road and vehicle ratios decrease the willingness of people to walk and street attractiveness.
- **Street View Crawling.** To reveal the surrounding scenes of a street space, street views have to be crawled appropriately: successive images should reflect the continuous change in surrounding scenes. Hence, the distance between two successive views should not exceed a limit that produces discontinuous scenes; meanwhile, it should not be too small, which will cause computing overload. After experimenting with several options, we find 50 meters is a suitable value for the distance between two successive views.
- **Street View Directions.** Although GSV [29] provides 360-degree panorama imagery, only the front and back images in the directions of street headings at sampling locations are required. Side views are not utilized because of the following considerations: First, side views mainly present building facades and street sides and thus cannot correctly reflect other key features of street space, e.g., road. Second, side views are partially contained by the front and back images at nearby sampling locations.

To evaluate the effectiveness of our approach, we first experiment with a few representative cities. SR suggested Hong Kong, Singapore, Greater London, and New York City: Hong Kong and Singapore are dense cities with high-rise buildings in Asia. Greater London and New York City are well-planned cities in Europe and the US.

2.3.2 Analytical Tasks

After identifying the analysis criteria, SR further raised a list of questions for our system to address, including: *How are the identified features distributed in an AOI? What are the feature differences between two AOIs? What are the exact views that people can see on a street? Are there any representative views?*

Based on these questions, we compile a list of analytical tasks:

- T.1: **Efficient Multi-scale Exploration:** Human-scale urban forms are associated with street views at different locations that can be organized on city-, region- and street-scales. Planners first need an intuitive overview of the identified feature distributions within a city or a region (T.1.1). Next, planners need to explore the details of the urban forms, such as the exact street views, at street level (T.1.2). Effective interactions are required to assist users in navigating across different scales.
- T.2: **Quantitative Measurements:** SR emphasized the importance of quantitative measurements to evidence-based urban design. Here, given that an AOI/street can contain vast amounts of street views, planners should analyze the statistics of identified features, including correlations between features, distributions, and standard deviations (T.2.1). Filtering street views against the values of a specific feature is also important (T.2.2).
- T.3: **Effective Ranking and Comparison:** To help planners quickly narrow down the exploration scope, features among multiple AOIs/streets should be effectively ranked (T.3.1). Areas/streets with certain features of high values can be easily discovered for further exploration. After planners select two AOIs/streets, they need to compare the differences in spatial distributions (T.3.2) and the quantitative measurements (T.3.3) of the urban forms.

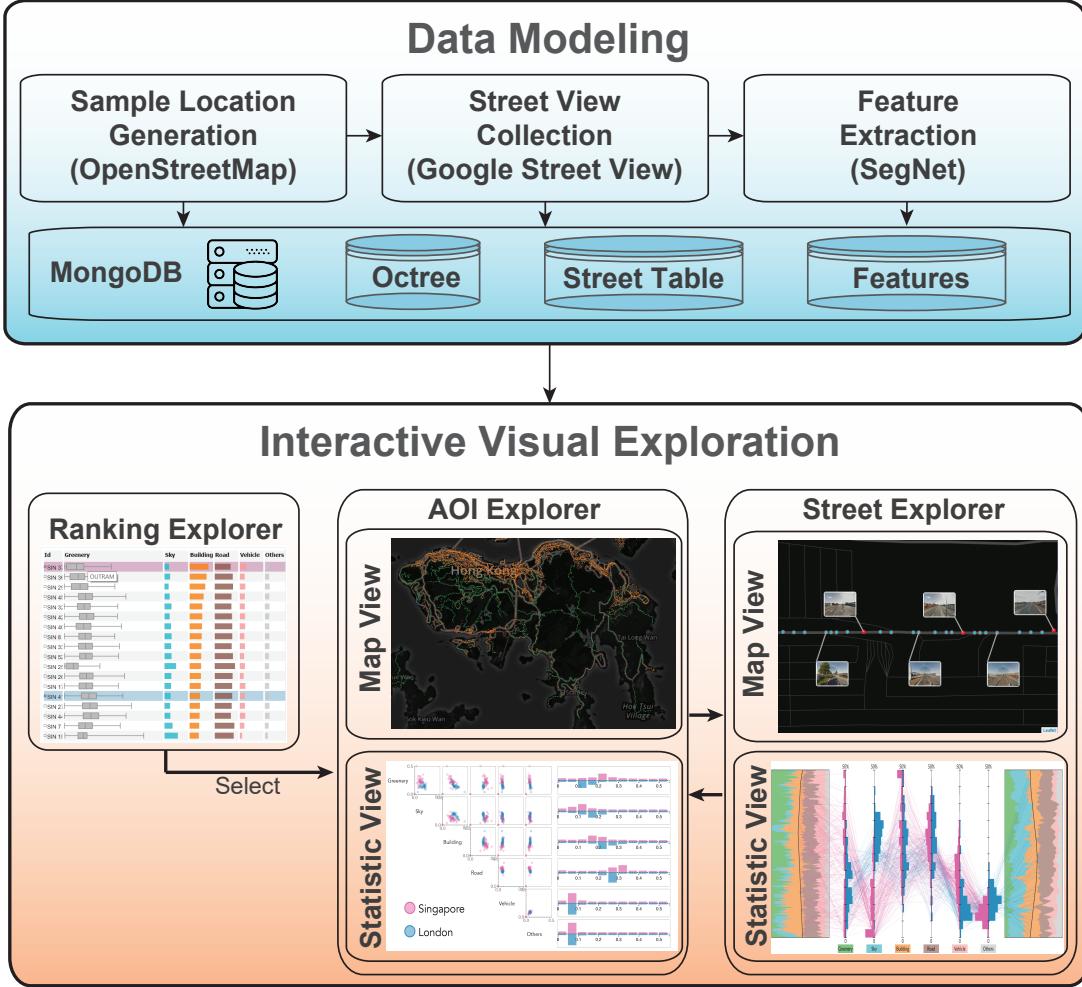


Figure 2.1. Overview of StreetVizor workflow. Our system consists of two phases: data modeling and interactive visual exploration.

2.4 System Framework

StreetVizor is a web-based application comprising two major phases, as illustrated in Fig. 2.1. In the data modeling phase, our system automatically collects hundreds of thousands of GSV images at sampling positions in each city generated from OpenStreetMap (OSM) (Section 2.5.1). Then, we classify the pixels of the collected images into 12 classes using SegNet, and extract the desired feature metric from the classification results (Section 2.5.2). Data collection and preprocessing are conducted offline on a high-performance workstation with 12 core 3.40 GHz Intel Core i7-6800K CPU and a GeForce GTX 1080 graphics card. Though enabled with GPU acceleration, the computation still takes several to 20 hours to preprocess images from each city. Then, we construct data structures, including an octree and a lookup table, to facilitate visual exploration, such as spatial query

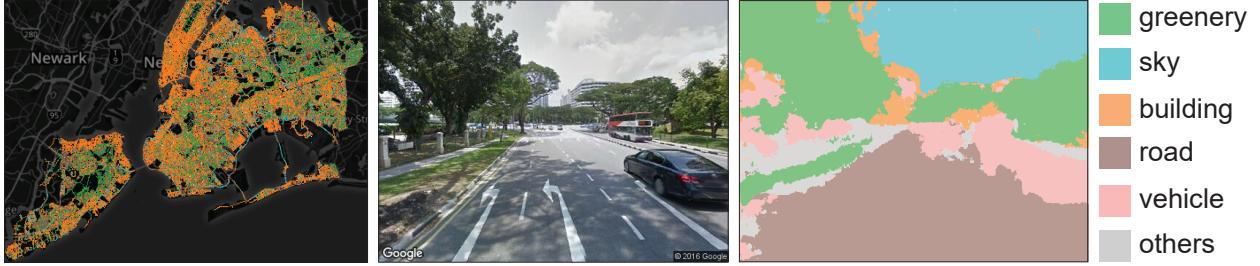


Figure 2.2. Illustration of data preprocessing: sampling locations in New York City are generated from OpenStreetMap (left), a street view image is collected from Google Street View (center), and the image pixels are classified into six features using SegNet (right).

and filtering (Section 2.5.3). The datasets are stored in a back-end MongoDB server with 2.4 GHz Intel Xeon E5-2620 CPU and 64 GB memory.

The interactive visual exploration phase consists of two stages: 1) Our system provides users with a Ranking Explorer that ranks and compares multiple AOIs/streets based on human-scale urban forms. Users can narrow down exploration by selecting two AOIs/streets for detailed comparison. 2) If two AOIs are selected, the system will present an AOI Explorer that compares the differences in human-scale urban forms in two AOIs at city- and region-scales. The AOI Explorer is composed of CMVs, including two juxtaposition map views for spatial exploration and a superposition statistic view for comparing various quantitative measurements, such as feature correlations and diversities. Users can further navigate down to select two streets, and our system will provide Street Explorer, which presents the fine details of human-scale urban forms at street-level. In Street Explorer, we present map views that show the geographical information and representative images of two streets. We also develop a novel PCP enhanced with themeriver along street layouts, allowing users to compare multivariate features and reveal feature distributions along the two streets. The visualization modules are implemented in D3.js and Three.js for different rendering requirements, and they are integrated using Vue.js.

2.5 Data Modeling

In this section, we first describe the collection of GSV images and the extraction of human-scale urban forms from the collected images. Furthermore, we present the methods for data querying and filtering.

2.5.1 Data Collection

Based on the configurations defined in Section 2.3.1, we develop an automatic approach to collect GSV images. We first download the area of a city from OSM [59] and extract the road network from the OSM data. Next, we apply a flood-fill algorithm that recursively goes through the entire road network every 50 meters, starting from a randomly selected location. After this operation is completed, a list of sampling locations ($\{\text{pos}\}$) with geographic information (lat & long) is generated. We then pass each (lat & long) into GSV API, and extract the corresponding street information (SI), including street name (s_name) and heading (h). Finally, we download front and back images at each sampling position by passing lat, long & h with the default field of view and pitch values into GSV API. Together with the downloaded image (Img), we model urban forms at human-scale (UF_{hs}) at each sampling location as:

$$\text{UF}_{hs} := \langle \text{pos}, \text{SI}, \text{Img} \rangle \quad (2.1)$$

We have collected ~ 147 k, ~ 183 k, ~ 685 k and ~ 637 k images of Hong Kong, Singapore, Greater London and New York City, respectively. Fig. 2.2 (left) presents all sampling locations (colored dots) in New York City generated from OSM, and (center) shows a sample street view image downloaded from GSV.

2.5.2 Feature Extraction

After collecting street views, we first classify the image pixels into 12 classes (e.g., sky and building) using SegNet [7], which is a robust pixel-wise semantic labeling tool with a global accuracy of 82.8%. Among the 12 classes, we count the number of pixels for the identified five features, i.e., greenery, sky, building, road, and vehicle, and summarize the remaining pixels as others. We then normalize the feature data because pixel counts (PC) as raw output values are not intuitive. The normalization is straightforward for each feature value (FV): $\text{FV}_i = \text{PC}_i / \text{PC}_{\text{Img}}$, where $i \in \{g, s, b, r, v, o\}$ represent the five features and others. Hence, all feature values are in the range of [0, 1]. Then, we can replace the

image (Img) with a feature metric (FM) as:

$$\text{Img} \rightarrow \text{FM} := \langle \text{FV}_g, \text{FV}_s, \text{FV}_b, \text{FV}_r, \text{FV}_v, \text{FV}_o \rangle \quad (2.2)$$

Fig. 2.2 (right) shows the classification result of the street view image in the center produced by SegNet.

2.5.3 Data Querying and Filtering

Based on Equations 2.1 and 2.2, we model human-scale urban forms (UF_{hs}) with the following attributes: position (pos), street information (SI), and feature metric (FM). By nature, the data exhibits the following properties: 1) spatial, i.e., positions; 2) multi-scale, because the positions can be hierarchically grouped in accordance with city and regional units, or street information; and 3) multivariate, i.e., the feature metric is in six-dimensional data space.

These complex data natures bring in challenges for our analytical tasks. To address these challenges, we further identify the following querying and filtering models that our system should support:

- **Spatial Query:** To overview the feature distributions within an AOI (T.1.1), our system should first support an efficient query of a list of $\{\text{UF}_{hs}\}$ with their pos laying in a given AOI. The AOI can be either an administrative zone (e.g., a city or a district) or a user-specified region defined using a lasso tool. We achieve the efficient spatial query operation by organizing all $\{\text{UF}_{hs}\}$ in a city in a four-level octree structure, in which the topmost level is the boundary of each city.
- **Street Query:** To support the exploration of human-scale urban forms at street-scale (T.1.2), our system should allow users to interactively query a street by its name. Here, we create a lookup table with street names as keys, and store corresponding UF_{hs} ids in each street slot.
- **Feature Filtering:** To accelerate filtering against a particular feature (T.2.2), our system first sorts all $\{\text{UF}_{hs}\}$ to be explored in increasing order for every feature. Then, we adopt a binary search approach in run time.

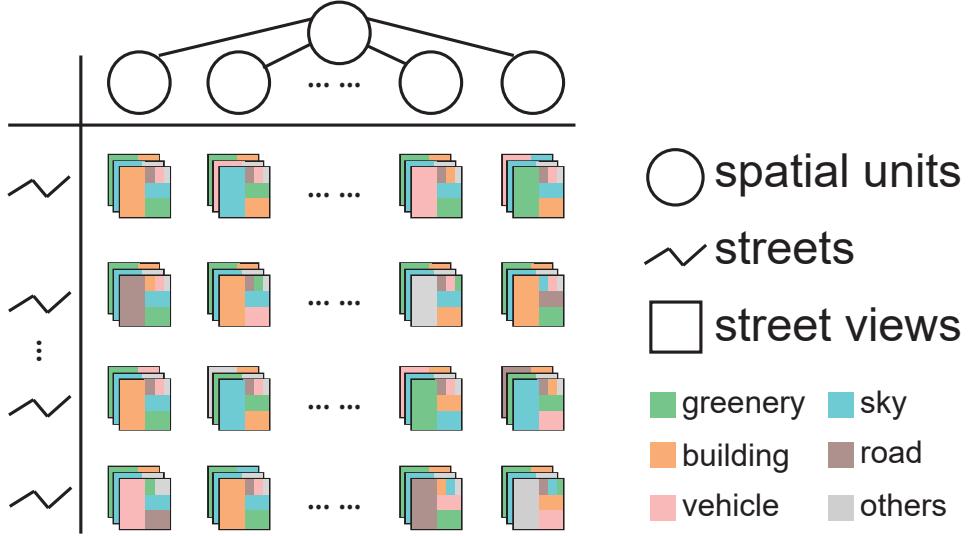


Figure 2.3. Data model: street views with six-dimensional features of *greenery*, *sky*, *building*, *road*, *vehicle* and *others*, are organized in an octree structure and a street lookup table.

Fig. 2.3 illustrates the data model that organizes the street views in an octree structure and a street lookup table. Each street view contains the six-dimensional features of *greenery*, *sky*, *building*, *road*, *vehicle*, and *others*. We store these querying and filtering models are stored in a back-end MongoDB database, as shown in Fig. 2.1.

2.6 Visualization Design

In this section, we first discuss the rationales behind our visualization design. Then, we provide a detailed description of the visualization techniques implemented in our system.

2.6.1 Design Rationales

To address the complex analytical tasks (Section ??), a proper visual design should follow the design rationales below:

R.1: **Overview+Details:** To facilitate multi-scale exploration, our system should follow the information-seeking mantra: “Overview first, zoom and filter, then details on demand” [69]. First, the system should provide an overview of human-scale urban forms at city- and region-scales, and then allow users to explore more details

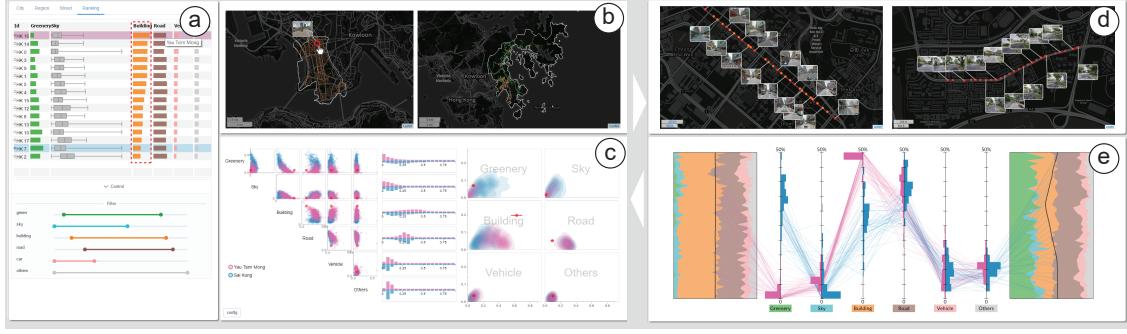


Figure 2.4. StreetVizor system. (a) Control panel enables multi-scale navigation, ranking exploration, and feature filtering. (b) Side-by-side map views compare the spatial distribution of human-scale urban forms in two areas-of-interest (AOIs). (c) AOI statistic view presents the quantitative measurements, including correlation, histogram, and diversity in the AOIs shown in (b). (d) Street map views present detailed street views along two streets. (e) Street statistic view extends parallel coordinates with street layouts.

at street-scale. Efficient query and filtering should be provided to enable smooth transitions between these scales.

R.2: Coordinated Multiple Views: Our system should effectively reveal multiple perspectives information of human-scale urban forms, including geographical locations and multivariate features. CMVs that present linked information and allow users to explore data from multiple joint-perspectives fulfill this requirement.

R.3: Effective Comparison: To enable effective data comparison, different comparative visualization techniques should be employed for multiple-perspective information. Specifically, given that spatial information for two AOIs/streets is unsuitable for direct overlay, we adopt side-by-side map views. On the other hand, the feature metric can be mapped on the same scope. Therefor, we select a superposition visualization to reveal the differences.

R.4: Visual Consistency: Since multi-scale and multiple-perspective visualizations are to be designed, the system should maintain visual consistency across different visualization modules. We realize visual consistency by 1) applying the same layout, i.e., presenting spatial information on the top and quantitative measurements on the bottom, in AOI Explorer and Street Explorer; 2) employing consistent color mappings. Specifically, we set green, light blue, orange, brown, light pink, and gray to represent the features of greenery, sky, building, road, vehicle, and others, respectively. AOIs/streets on the left and right side are colored as red and blue, respectively.

2.6.2 Ranking Explorer

Ranking Explorer is developed to overview feature attributes across multiple AOI/street candidates to help users quickly identify AOIs/streets for comparison (T.3.1). The explorer presents each candidate as a row and arranges its multivariate information in seven columns. The first column provides general information, such as city and region/street id. The remaining columns present the six features' mean values as bars, where mean values are normalized and encoded by bar lengths. Clicking the body of a feature column of interest will expand the column as a boxplot to show statistical distributions. The explorer also allows users to sort candidates against a particular feature and the ranking will update correspondingly. Such designs have been well established and evaluated in a previous work [51].

Fig. 2.4(a) ranks all districts in Hong Kong in accordance with building feature (red dashed box). As an example, we observe the detailed statistics of the sky feature. We select the column for this feature and expand it to boxplot. By comparing the orderings of greenery, sky, and building features, we find greenery and sky features are correlated, while they are negatively correlated with the building feature. This information helps users narrow down the comparison choices to 1) district HK 16 (Yau Tsim Mong) with the highest building ratio and 2) district HK 7 (Sai Kung) with low building and high greenery ratios, as shown in Figs. 2.4(b) & (c).

2.6.3 AOI Explorer

AOI Explorer is developed to provide efficient comparison of human-scale urban forms at city- and region-scales (T.1.1). The explorer integrates coordinated multiple views, including:

AOI Map View

We develop side-by-side map views (Figure. 2.4(b)) to compare the spatial distributions of human-scale urban forms in two AOIs (T.3.2). Each map view consists of: 1) a background map layer implemented with Leaflet.js to allow users to change map style (e.g. satellite,

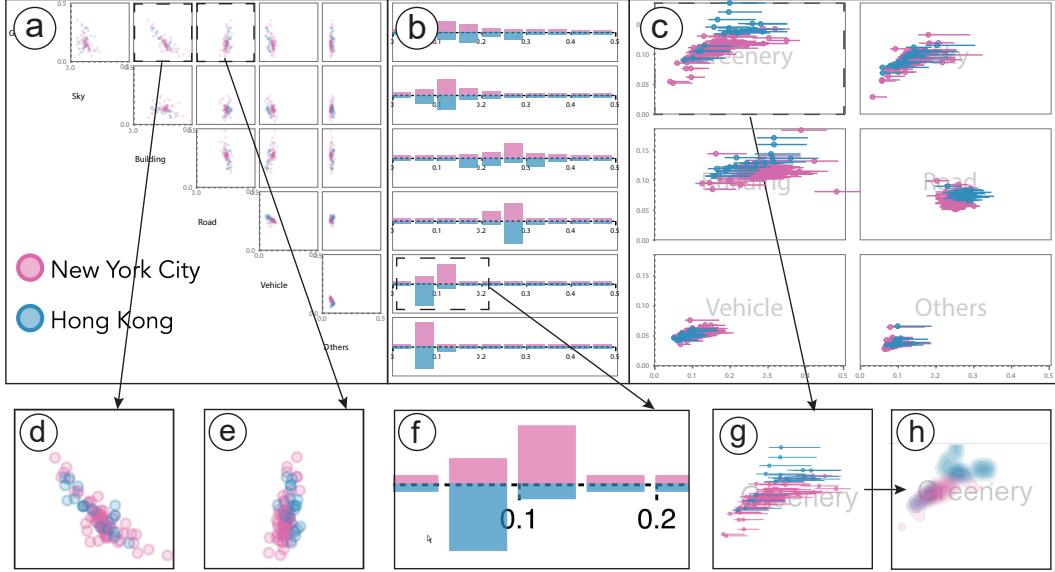


Figure 2.5. The AOI Statistic View combines (a) a scatterplot matrix to show pair-wise correlations between two features, (b) small multiples of histogram bar charts to overview feature distributions, and (c) small multiples of deviation plots to present feature diversity.

street, and sport) for different purposes; and 2) a point density map overlaid on top of the background map layer, with points representing street views. The density points are evenly sampled on each street with an upper limit of 10,000 points. Point color corresponds to the maximum feature value in the street view image. A corresponding street view image will pop up when the mouse pointer hovers over a point. Users can select two cities or regions from the navigation panel, or directly manipulate AOIs on the map views with a lasso tool.

Heat map is an alternative design for the point density map. However, in this work, we focus on the simultaneous analysis of multiple features of human-scale urban forms. Compositing these features into one heat map [65] will require redundant user interactions. In addition, sampling positions are generated along the street network. Thus, no street views is collected from many places across a city. In this case, the heat map will generate ambiguity between the two scenarios of 1) no record or 2) low feature values in a region.

AOI Statistic View

Besides the map view, which enables the comparison of spatial distributions of human-scale urban forms, we develop AOI Statistic View to allow users to compare various quantitative measurements (T.3.3). Nonetheless, each AOI may contain too many street views (up to several hundred thousand) that will overload the rendering process. Moreover, the street views will occlude each other if we simply plot all of them. To address this problem, we cluster street views into groups based on either their administrative units (districts, divisions, and streets) or a mean-shift clustering algorithm [14] that works as follows.

Mean Shift Clustering. We cluster urban forms based on their feature metric and geographical positions. Our algorithm works in the following way: given an input list of N human-scale urban forms $\{UF_{hs}\}$, we first normalize the lat & long attributes of each UF_{hs} against the boundary of all $\{UF_{hs}\}$. Then, we combine the normalized lat_{nor} & $long_{nor}$ with the feature metric to construct a new dataset $X := \{x_1, x_2, \dots, x_N\}$, where each data point x_i is in an eight-dimensional space, $R^8 := < lat_{nor}, long_{nor}, FV_g, FV_s, FV_b, FV_r, FV_v, FV_o >$. The distance between two data points is measured as their Euclidean distance. We then estimate a bandwidth h from X , and apply mean-shift clustering algorithm on X using a flat kernel. Here, the bandwidth estimation and mean shift clustering are performed with a machine learning library *scikit-learn* [61]. Finally, we generate a list of m urban form clusters $C := \{c_1, c_2, \dots, c_m\}$, where each cluster c_i contains n data point $c_i := \{x_1, x_2, \dots, x_n\}$.

The clustering process groups geographically close street views with similar feature attributes together. Given that locations are integrated as two-dimensional spaces, the algorithm forms more local clusters than an algorithm without considering spatial information, which usually generates several big clusters with too many street views. The algorithm may be further improved by adopting a network-based distance measurement approach other than Euclidean distance. We expect to form more representative clusters of street views with street network information. Nonetheless, the current approach fulfills our requirement of reducing visual clutter.

After generating the clusters C , we further compute and visualize the following quantitative measurements:

- **Feature Correlation:** We first compute the mean values of the identified features, i.e., *greenery*, *sky*, *building*, *road*, *vehicle*, and *others* in each cluster c_i . We then plot the pair-wise correlations using a scatterplot matrix (Fig. 2.5(a)). Notice that the clusters in the left and right AOIs are colored red and blue, respectively.
- **Feature Histogram:** Though feature values fall in the range of [0% - 100%], we seldom find feature values that exceed 50%. Thus, we only consider the range [0% - 50%]. For each feature, we divide the range into 10 even parts, i.e., [0% - 5%), [5% - 10%)..., and aggregate the corresponding value in each street view to each part. Then, histograms for each feature are plotted as bar charts in an up and down manner for AOIs on the left and right, respectively. The six histogram bar charts are arranged in small multiples next to the scatterplot matrix (Fig. 2.5(b)).
- **Feature Diversity:** We use standard deviation to indicate the measured feature diversity measured for each cluster, and design diversity views that are arranged as six side-by-side small multiples for each feature as shown in Figure 2.5(c). In every feature diversity view, each cluster is represented as a dot with its x-value indicating the averaged feature value and y-value indicating standard deviation. In addition, we use line segments to indicate the largest and smallest feature values in each cluster. In case an AOI may have hundreds of clusters that lead to serious visual clutter problem, we implement a contour map view [11] (Fig. 2.5(h)) to show overall distribution patterns. Users can interactively choose one of the views in accordance with different requirements.

The AOI Statistic View comparison of New York City (red) and Hong Kong (blue) is shown in Fig. 2.5. From the view, we can easily identify some obvious patterns. For example, in both cities, *greenery* and *building* features are negatively correlated (Fig. 2.5(d)). The correlations between other pairwise features, e.g., *greenery* and *road* (Fig. 2.5(e)), are not obvious. From Fig. 2.5(f), we find that the vehicle ratio is higher in New York City than in Hong Kong. In addition, we find that although the *greenery* values are similar for both cities, diversity is higher in Hong Kong (Fig. 2.5(g)). This results reflects that greenery is better integrated into street space in New York City than in Hong Kong.



Figure 2.6. Street Map View provides an overview of all street views along a street as colored points, and highlights images on two sides of the street. (a) A tree map showing the feature composition of an image will pop up when the mouse pointer is hovered over the image.

2.6.4 Street Explorer

Street Explorer is developed to enable the efficient comparison of human-scale urban forms at street-scale (T.1.2). The explorer adapts the same layout as that in the AOI Explorer, i.e., juxtaposition map views are placed on the top of the explorer, whereas detailed statistics view are on the bottom.

Street Map View

Similar to AOI Map View, Street Map View is also developed on top of a background map layer that is implemented using Leaflet.js. Street views on the street are over-viewed as points with colors that correspond to primary features, i.e., green for greenery, light blue for sky and orange for building. In contrast to AOI Map View, Street Map View presents more details of human-scale urban forms by displaying the corresponding street view images along the two sides of a street. The images are evenly selected in the direction of the street heading. In particular, the feature compositions of an image are displayed as a tree map [68] when users hover their mouse pointer over the image. An example is provided in Fig. 2.6(a).

Street Statistic View

The design goal for this view is to allow users to quantitatively compare human-scale urban forms from two streets. Although we can utilize the same views shown in the AOI Statistic View, our collaborating domain expert SR is not satisfied. SR strongly recommended encoding street layout information in the view, so that users can better leverage their knowledge about streets to perform in-depth analysis. SR felt the spatial information was not well integrated with the Street Map View.

Based on this goal, we experimented with a few alternative designs and informally evaluated design prototypes with SR. For our first prototype, we designed some glyphs, such as a radial chart or tree map, and directly overlaid the glyphs on the map view. The design was aborted because isolating statistics on the two maps weakened the effects of comparison. In addition, such a design easily generated visual clutter, which requires redundant user interactions or clustering to address. For the second prototype, we encoded street layout information in a similar design as the AOI Statistic View. However, this method was extremely difficult because the rendering space was fully utilized.

PCP with Street Layout. Inspired by [63], we ultimately develop a design of a parallel coordinates enhanced with street layouts (Fig. 2.7(d)). We elaborate the construction of this design as follows:

Bounding Box Construction (Fig. 2.7(a)). The first step is to construct a minimum bounding box (MBB) of the street layout. We find the starting (A) and ending (B) points, and generate a primary axis pointing from A to B. MBB is generated as the minimum rectangle that contains all nodes of the street network parallel with the primary axis.

Street Layout Rotation (Fig. 2.7(b)). Next, we rotate the street layout such that MBB fits in the rendering space, i.e., A and B lay on the top and bottom (or vice versa) sides of the rendering space, and the rotated MBB lays in the center. In the case that MBB is wider than the rendering space, the street layout outside the rendering space is clipped. The rotation direction (clockwise or anticlockwise) is determined based on the direction that produces the minimum rotation angle.

ThemeRiver Plotting (Fig. 2.7(c)). To fully utilize rendering space, we plot a themeriver-

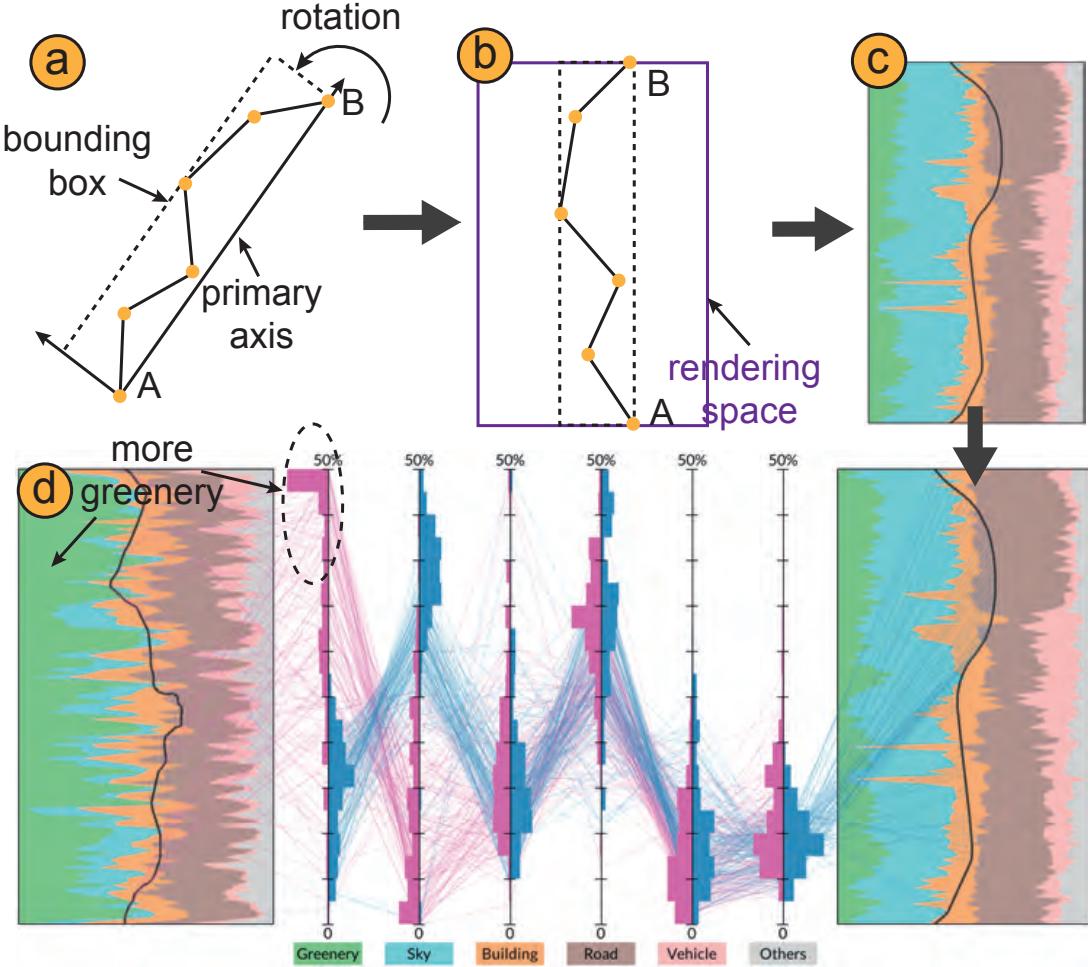


Figure 2.7. Overview of the construction process for Street Statistic View: (a) Construct minimum bounding box of the street network. (b) Rotate the street network such that its bounding box fits in the rendering space. (c) Plot themeriver style visualization within the rendering space. (d) Enhance parallel coordinates with street layouts on both sides.

style [33] visualization to show changes in feature values along a street layout. Here, the themeriver is plotted in the vertical instead of the traditionally horizontal direction because the street layout is aligned along the y-axis after rotation. Next, given that street views are sampled evenly along the street layout, we map the street views equally onto the y-axis, i.e., y-values of the themeriver plot reflects the relative positions of street views along the street layout.

We start plotting the themeriver visualization using the left side of the rendering space as the baseline and calculate the upper bound x-values for the *greenery* feature. The upper bound x-values of the *greenery* layer are then used as baseline values for the next feature, i.e., *sky*. This process is repeated until all features are plotted. To support better feature comparison, our system allows users to reorder feature sequence by clicking on

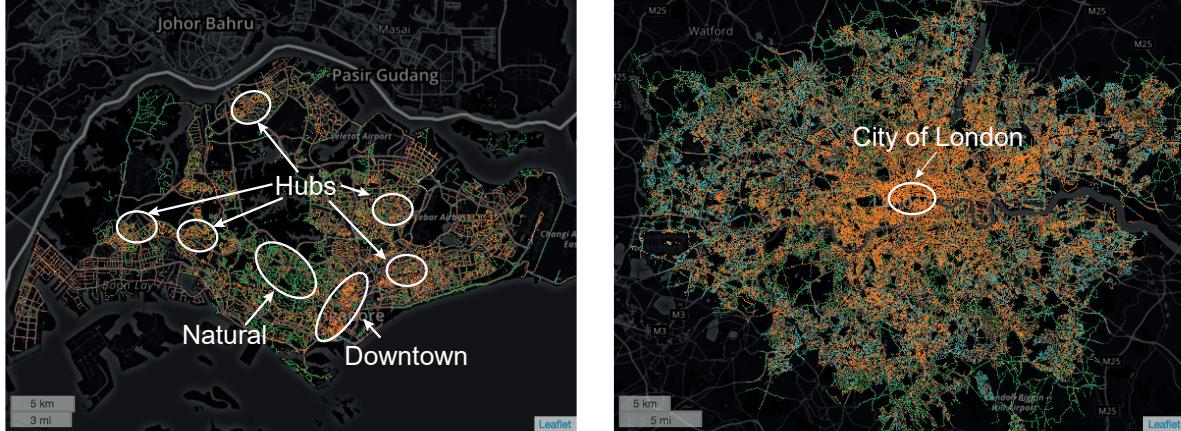


Figure 2.8. AOI Map View compares spatial distributions of human-scale urban forms in Singapore (left) and Greater London (right). Orange points (buildings) are concentrated around the highlighted center area of Greater London, i.e., City of London.

the feature layer of interest and shifting it to the left side [10].

PCP Integration (Fig. 2.7(d)). The themeriver plot can be used as a coordinate for the PCP. To enable comparison between two streets, we integrate their themeriver plots into a PCP on left and right sides, and the identified features are used as other coordinates. Each street view is conveniently presented as a polygonal line, which is colored as red and blue for left and right street views, respectively. In addition, we aggregate the feature values via binning techniques on left and right sides of each feature coordinate to facilitate the visual comparison of feature distributions.

Fig. 2.7(d) presents an example Street Statistic View. A first glimpse at the two themeriver plots, we can find that the left street contains more greenery, while on the right street people can see more sky. This can be found in the distribution comparison on the greenery & sky coordinates in the middle. Besides, we can also find that feature values vary dramatically on the left themeriver plot, showing street views are very different along the left street.

2.6.5 User Interactions

In addition to basic interactions in each view, StreetVizor also provides a control panel (Fig. 2.4(a)) that enables:

- *Multi-scale Navigation.* To help users navigate effectively across different scales, we

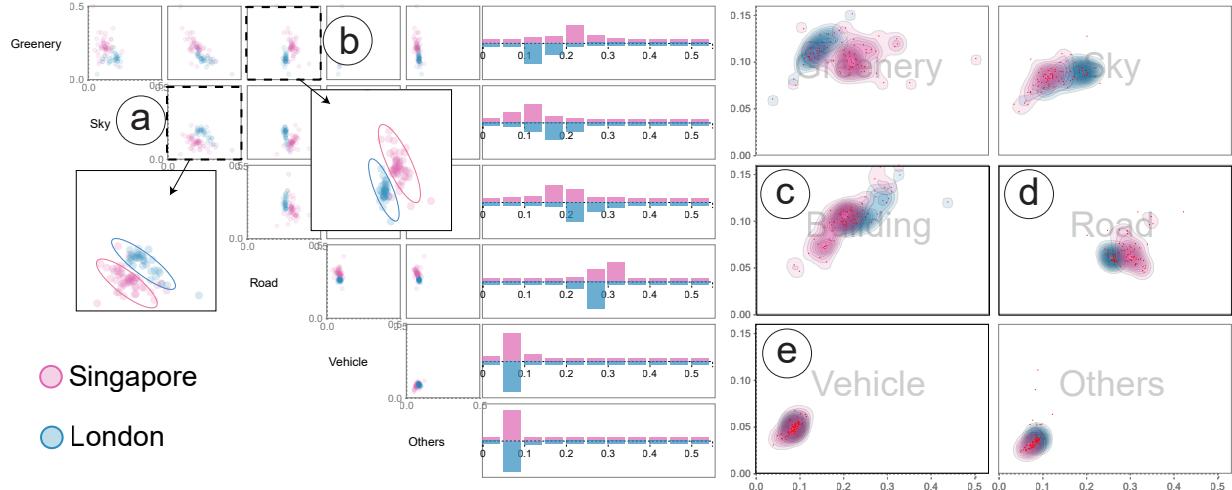


Figure 2.9. AOI Statistic View in coordination with Fig. 2.8 presents quantitative measurements differences of human-scale urban forms in Singapore (red) and Greater London (blue).

develop city-, region- and street-panels. The city-panel lists all four cities, i.e., Hong Kong, Singapore, Greater London, and New York City. Users start navigation by selecting a city. The region-panel will then list all administrative regions under the city. For instance, City of London and Kingston will be listed if Greater London is selected. Similarly, the street-panel lists all the streets inside a selected city or region.

- *Feature Filtering.* Our system also supports filtering human-scale urban forms against a specific feature by specifying the value range with feature sliders. By default, each feature slide within [0 - 1], and users can change the minimum and maximum values by dragging the slider buttons.

In addition, our system also supports the following user interactions to facilitate visual exploration.

- *Details on Demand.* To enable overview+details (R.1), we develop a set of interactions that allow users to explore the details of human-scale urban forms on demand. For example, if a street view point is selected in the AOI Map View, the corresponding image will show up. Thus, users can leverage their domain knowledge by visually examining street views.
- *Linking.* Our system supports automatic linking among the visualization modules in both AOI Explorer and Street Explorer for coordination across multiple views (R.2).

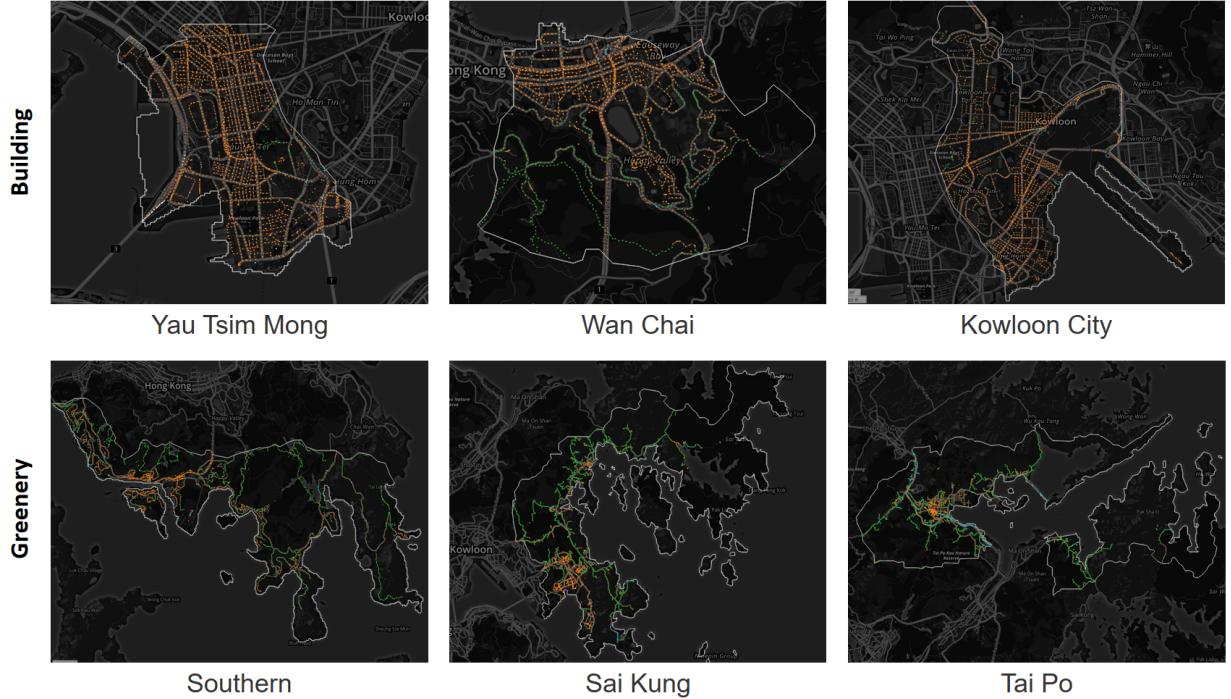


Figure 2.10. Top three districts with highest building ratios, while bottom three with highest greenery ratios in Hong Kong.

For example, if a specific street view on the AOI Map View is selected, the cluster that contains the street view in the scatterplot matrix and the diversity views will be highlighted accordingly.

2.7 Case Studies

This section presents three case studies on the application of StreetVizor in assisting urban planners to explore and compare human-scale urban forms on the city-, region-, and street-scales.

2.7.1 City-scale Comparison

Comparing Spatial Distribution. With the AOI Map View, our system allows users to compare spatial distributions of human-scale urban forms in two AOIs (T.1.1). Fig. 2.8 presents a comparison between Singapore (left) and Greater London (right). As shown in the figure, more orange points surround the highlighted white circle, whereas more green points can be found at marginal areas in Greater London. This indicates that more buildings are

constructed around the City of London, reflecting that this city is more urbanized compared with other areas. By contrast, Singapore's urban forms are evenly distributed. More orange points are found in the highlighted downtown and region hubs, and more green points can be found in natural areas. Our collaborator SR explained the reason for the different spatial distributions of urban forms in Greater London and Singapore: Greater London likely expanded its urbanization from the City of London to surrounding areas, whereas Singapore, as an island city, cannot expand.

Comparing Quantitative Measurements. We can further explore the differences in quantitative measurements with AOI Statistic View (T.2.1 & T.3.3). Fig. 2.9 shows the AOI Statistic View in coordination with Fig. 2.8. From the scatterplot matrix, we find that greenery and building features are negatively correlated. This result is the same as that shown in Fig. 2.5(d). Given that buildings are artifacts and greenery is natural, the negative correlation between building and greenery features in all four cities indicates that artifacts increase and natural environments decrease with increasing urbanization. To improve livability, many urban planners have proposed integrating more natural spaces in street space. In addition, Fig. 2.9(a) shows that sky and building ratios are higher in London than in Singapore. By contrast, greenery and road ratios are higher in Singapore than in London (Fig. 2.9(b)). These findings can also be found from the middle histogram bar charts. In addition, the diversity views further show some interesting patterns. For example, building and road diversities are more concentrated in London than those in Singapore, as shown in Fig. 2.9(c) & (d), and likely resulted from the different standards for building and road construction in the two cities. Vehicle usage rates are low in both cities, as shown in Fig. 2.9(e).

2.7.2 Region-scale Exploration

Given that human-scale urban forms are highly associated with the daily lives of residents, we posit that urban forms could reflect the functionalities of a region. Study 1 already reveals the negative correlations between greenery and building features, and we hypothesize that these two urban forms can reflect urbanization levels. To evaluate the hypothesis, we further explore these two features at region-scale (T.1.1). Using rank-

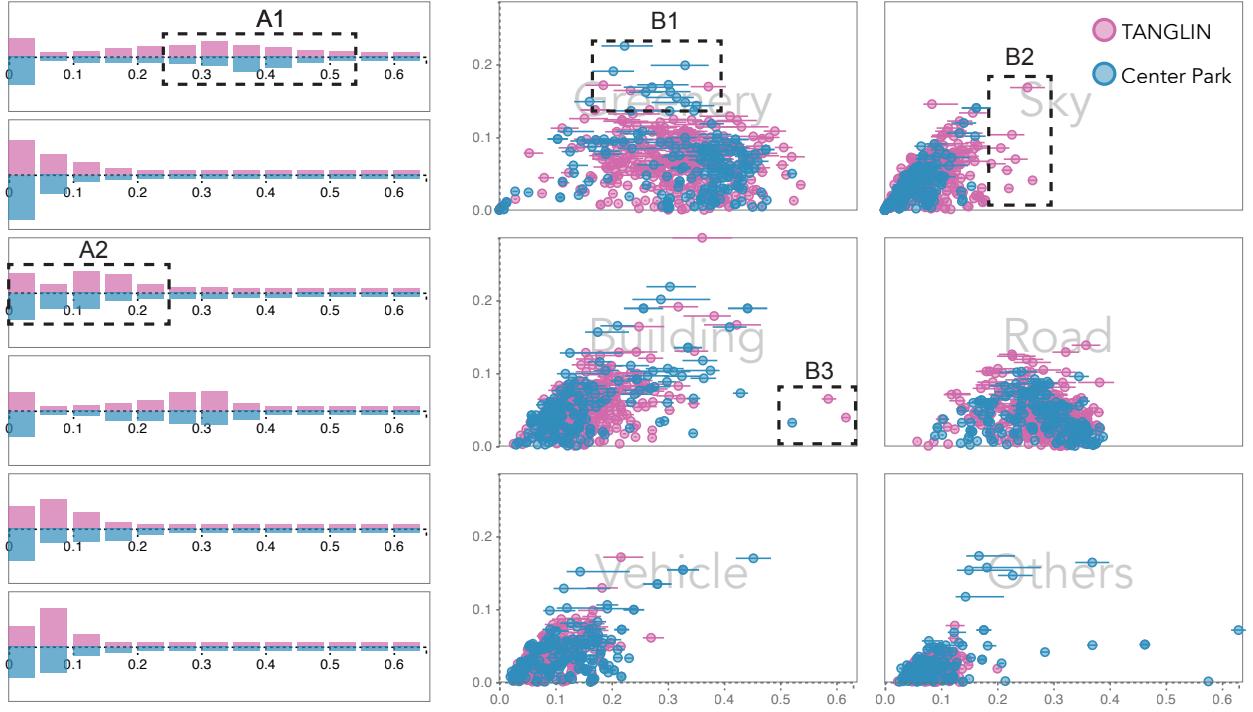


Figure 2.11. Region-scale comparison of Tanglin in Singapore with Central Park in New York City.

ing functions, we sort administrative districts in Hong Kong based on these two features. Fig. ?? presents an overview of three districts with highest values for each feature. The top three districts are Yau Tsim Mong, Wan Chai, and Kowloon City. They are all business centers in Hong Kong, and we find these districts are mostly covered by orange points (building). By contrast, the bottom three districts contain highest values for greenery. In particular, the greenest district is Southern Island, which is reserved as country parks. The other two districts are also well-known natural areas in Hong Kong.

In addition to exploring regions with different functionalities, urban planners are also interested in comparing regions with similar functionalities. Here, we leverage our knowledge of famous regions in two different cities, i.e., Tanglin in Singapore (see the region highlighted as natural in Fig. 2.8) and Central Park in New York City. Both of these regions are well-known parks. After selecting these regions, we find that nearly all streets in the two regions are dominated by green points, indicating that both regions contain considerable greenery as intended. However, we find some differences between these two regions by looking deeper into the Street Statistics View (Fig. 2.11). First, through the feature histogram bar charts, we find that Central Park has slightly higher greenery ratios

(A1), whereas Tanglin has slightly higher building ratios (A2). Though these differences are marginal, they reflect that more buildings are present in Tanglin, partially because Singapore tries to maximize land usage for building construction. In addition, by grouping street views based on street units, we glean more information from the diversity plots. Here, we first obtain the overview that greenery feature has relatively higher mean values and deviations than the other five features. We also find some anomalies. For example, some streets have relatively low mean values but high deviations for greenery in Central Park (B1), whereas certain streets have high sky visibility in Tanglin (B2), and some streets have very high building ratios in both regions (B3).

The results of this study show that human-scale urban forms are correlated with regional functionalities. Meanwhile, even though two regions may have the same functionalities, street spaces in regions can be different between two cities. This may reflect the differences in city planning and development strategies between cities.

2.7.3 Street-scale Comparison

Our collaborating domain expert SR is interested in comparing the fine-grained details of two streets (T.1.2). StreetVizor meets this requirement with Street Explorer. Here, we select one street from Brooklyn, New York City, and one from Kowloon, Hong Kong. Both streets are representative streets of each district.

Fig. 2.12 presents the visual comparison of these two streets. The map views provide an overview that nearly half of the street views are mostly green (greenery), and the other half are mostly orange (building) on the street from Brooklyn. By contrast, the street views in Kowloon are mostly orange (building). We can observe more details by looking at the street view images. As shown on the top images, more greenery and sky with low buildings are seen in the left two images, whereas the right two images are filled with building and road. The tree map of the leftmost image shows the street view is well balanced with greenery, road, building, and vehicle features. Notice that the street view is also highlighted in the bottom Street Statistic View. More details on the quantitative measurements of street views can be observed in the bottom Street Statistic View. The themeriver plots clearly show differences in feature distributions: street views in Brooklyn are more mixed with balanced greenery, sky, building, road, and vehicle

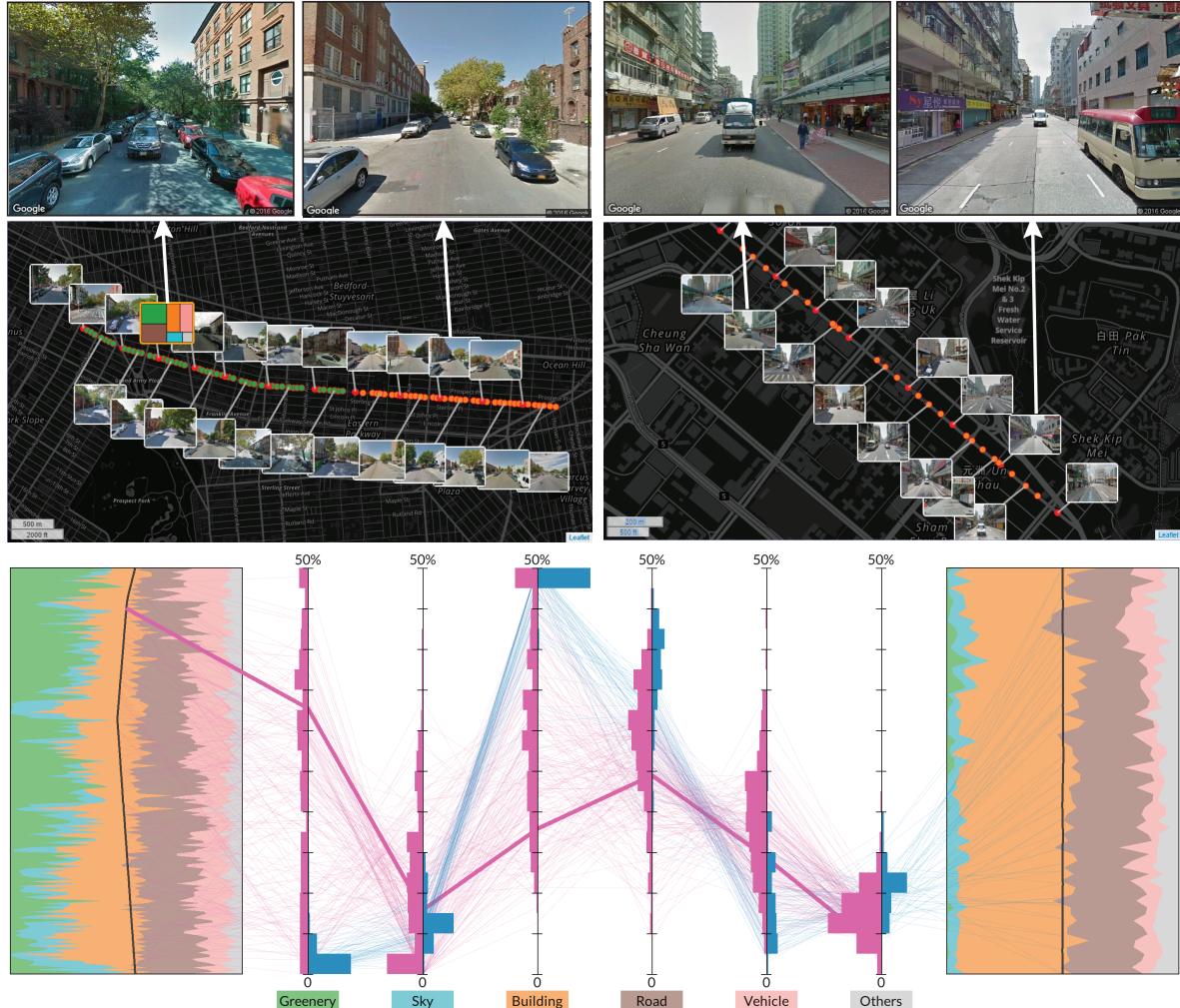


Figure 2.12. Street Explorer compares the differences in human-scale urban forms of two streets in Brooklyn, New York City (left) and Kowloon, Hong Kong (right). The left street views contain more balanced features, whereas the right street views are dominated by building and road.

features, whereas street views in Kowloon are mostly filled with building and road features. The histogram bars in PCP further confirm this observation: most street views in Kowloon have less than 10% greenery and sky.

Though it is well known in the field of urban planning that New York City is well integrated with natural features and that Hong Kong has more high-rise buildings, SR is excited to see our system can present these differences so intuitively. “Street Explorer can definitely improve our work efficiency,” SR commented.

2.8 Expert Review

To evaluate the effectiveness of StreetVizor, we conducted expert interviews with two independent domain experts other than our collaborating senior researcher SR. One of them focuses on designing livable public space (denoted as EA), and the other is an urban ecologist aiming at improving greenery in cities (denoted as EB). Hence, the experts are from different backgrounds: SR and EA in urban planning, while EB in ecology. In the interviews, we started with explaining the visual encodings and interface design, and demonstrated to them how our system works. Then, we showed them the case studies, and allowed them to explore the system by themselves for about twenty minutes in the end. In general, both experts agree that the way we study human-scale urban forms with street view images is a promising direction. Their detailed feedbacks are summarized below.

Methodology and Approach. EA agreed with SR that evidence-based urban design is becoming a trend in urban planning. He commented, "StreetVizor is far more than simply a visualization platform. Rather, it is an excellent combination of machine learning and visualization techniques, together with classical urban design theories in place-making". EB also expressed that "street view images as an emerging data source can reflect urban environments well", and a visual analytics system can greatly facilitate the exploration of street views.

Interactive Visual Design. Both experts confirmed that StreetVizor is nicely designed according to the problem domain. They appreciated the visual consistency across different views. EA highlighted "it is very important to use the same colors in different views". SR agreed the workflow of ranking multiple AOIs/streets with Ranking Explorer, and comparing two AOIs/streets for details through AOI and Street Explorer is helpful. "It is easier for me to identify interested regions, such as those in Hong Kong (Fig. ??)", commented by SR. The AOI Explorer is nicely designed with intuitive map and statistic views. In particular, "the statistic view seamlessly integrates three easily understandable plots", commented by EB. By referring to the scatterplot matrix in Fig. 2.5 & Fig. 2.9, EA was excited to see the negative correlation between greenery and building – "there are much space to improve". EA also liked the visual comparison of human-scale urban form dis-

tributions over space (Fig. 2.8), as it reflects the differences of urbanization process and master plans in different cities.

The experts thought presenting street view images in the Street Explorer is intuitive, and mouse hover over to show tree map is helpful. In contrary, it was difficult in the beginning for both experts to understand the PCP enhanced with street layout information, especially the themeriver plot. But after exploration, they agreed it is an excellent idea, as it clearly reveals the feature distributions along street. “Though not common, I believe there are many applications and potentials for the enhanced PCP”, commented by EB.

Applicability. Both domain experts would like to apply our system to deal with practical problems in their domains. Expertized in urban planning and design, EA emphasized “the lack of efficient tools for human-scale management and design obstacles creating high-quality urban streets.” StreetVizor has a great potential to be employed by planners and designers to “build more pedestrian-oriented and livable streets.” EA also commented “StreetVizor is highly applicable for evaluating case studies in urban planning”. For example, planners can select several key areas, e.g., CBDs, among different cities and then compare their spatial features to develop appropriate strategies in urban renewal. EB would like to apply our system in environment monitoring, since “the large amount of GSV images can provide rich information of urban environment”. He suggested to extend our system in exploring a time-series street view dataset, so that it would allow him to monitor environment changes.

Limitations and Improvements. The experts pointed out some limitations in our system. In this work, we explore only six features of human-scale urban forms. Both experts suggested to extract more urban forms, such as aesthetic amenities and mental well-being, from street view images. This will advance our system’s analytical capabilities and extend its applicabilities. For instance, a recent study [41] shows that certain relationship may exist between street greenery & sky ratio and the risk of health challenges. Besides, they proposed to improve our visual designs. EB noticed the feature histogram bars in AOI and Street Statistic View are designed differently: one in horizontal, and the other one in vertical style. He felt the vertical histogram bars are confusing, as they “do not fit our work habits”. EA suggested the Street Statistic View can be further improved, by

“encoding neighboring street layouts in the plot”, to reflect spatial information better.

2.9 Discussion

In this work, we combine automatic machine learning and interactive visual analytics techniques to explore human-scale urban forms. The combination of methods tackles the challenges of integrating information from multiple perspectives and at different scales for analysis. This approach is attractive for urban planners [52, 53] because it shows the possibility of transferring traditional subjective and intuitive-oriented urban design to evidence-based and big-data informed methods.

The analysis of human-scale urban form in this work relies heavily on a deep learning technique for image classification. Therefore, classification accuracy poses serious challenges in our approach. We select SegNet, which achieves a global accuracy of 82.8%, out of the different classification techniques that we tried. The case studies show that the classification technique could provide reasonable analytical results on city- and region-scale human-scale urban form patterns. Nonetheless, the results remain unsatisfactory in many cases, especially when users would like to examine fine detailed urban forms at street-scale. We envision applying a more advanced classification algorithm in the near future, given the rapid evolution of image classification techniques. In addition, the classification is preprocessed offline. Our system does not support the analysis of street views queried on runtime. Thus, its applicability is limited and domain knowledge of planners are underutilized in exploring street views in other cities. This deficiency can also be resolved with advancement in image classification algorithms and machine computing capabilities.

Moreover, we expect that our system will face scalability issues when the number of street view images increase (e.g. when analyzing street views in more cities). To tackle this problem, we can integrate more advanced data structures, such as nanocubes [50] or Gaussian cubes [80] for spatial data querying. More levels of detail and abstraction can also be introduced to handle this problem. The increase in image number will also burden street view clustering in the interactive exploration process. We anticipate that certain pre-configurations will facilitate this process.

Presenting multivariate data with spatial information is challenging. We tackle this challenge by integrating popular PCP with a themeriver plot along an adjusted street layout. The case studies and feedbacks from experts demonstrate the effectiveness of this design. Nonetheless, there are some issues with our design. First, it represents street layout as a simple spline, which is not sufficiently intuitive when the street is straight. We plan to encode more semantic labels, such as neighboring streets, in the design, as suggested by EA. Second, although the majority of the streets (over 95%) that we have explored can be rotated and fitted in the rendering space, adjustment does not work in some cases. Typical examples are streets in a spiral layout. A more general approach should be developed that can reveal the street layout intuitively and seamlessly fit the street layout in the rendering space.

2.10 Conclusion and Future Work

In this paper, we introduce StreetVizor, a visual analytics system for the exploration of human-scale urban forms based on GSV images. Through discussions with a collaborating researcher who specializes in evidence-based urban planning, we identify various analysis criteria and formulate a set of analytical tasks. We integrate some well-estimated visualization techniques, such as juxtaposition map views, scatterplot matrix, and small multiples, into our system. Specifically, we design an enhanced parallel coordinates with street layout to present coordinated feature values and reveal feature distributions along a street layout. StreetVizor is used to analyze ~1.7 million street views from Hong Kong, Singapore, Greater London, and New York City. Using our system, domain experts detect some interesting patterns, such as the negative correlation between greenery and building features. The experts also agree that our system has a wide range of applications, in areas like public space design and street environment monitoring.

There are several promising directions for future work. First, we would like to extract more high-level information, such as signboards, from GSV images. The signboards can then be compared with points-of-interest information extracted from other data sources, e.g., Foursquare or Google Places. We anticipate revealing some interesting patterns by fusing multiple types of big urban data. In addition, to address the scalability issues, we

plan to develop more advanced data structures (e.g., [50,80]) to improve the querying and filtering processes in our method. Besides, we would like to explore new visual interfaces to compare detailed statistics of human-scale urban forms across multiple AOIs/streets at the same time.

CHAPTER 3

ROUTE-AWARE EDGE BUNDLING FOR VISUALIZING ORIGIN-DESTINATION TRAILS IN URBAN TRAFFIC

Origin-destination(OD) trails describe movements across geographical locations, which can be visualized as direct lines connecting ODs. The visualization method, however, causes clutter issues for large amounts of OD trails. Edge bundling methods can mitigate the problem, yet bundling OD trails in urban traffic data remains under-explored. This work presents a new approach, namely route aware edge bundling (RAEB), specifically designed to fill the gap. We identify inconsiderate settings of conventional kernel density estimation edge bundling (KDEEB) when applied to urban traffic data, including non-optimal kernel size and road neglect. The limitations are addressed in RAEB by introduction of a comprehensive pipeline comprising preprocessing, bundling and evaluation processes. A series of new parameters, together with adaptions of existing ones, are employed in the pipeline. Experiments with artificial and real-world traffic data demonstrate advancements of RAEB in various applications, including preservation of road network topology and support of multi-scale exploration.

3.1 Introduction

Movement can be defined as change of an object's positions or geometric attributes over time [17]. Within a specific time period, the movement of an object can be modeled with an origin (O), a destination (D), and consecutive positions (trail) in-between. Due to fast development of location sensing technologies, massive amounts of OD trails, such as vessel movements and taxi trips, have been collected. Studies of OD trails have revealed many movement patterns and contributed to many applications, e.g. diseases spread control [8] and transportation planning [79].

Visualizing OD trails is a hot yet challenging topic. Conventional method that connects origins to destinations with lines [72] can easily cause visual clutter. To tackle the problem, methods of aggregating trails into flows are usually employed. A number of automatic techniques have emerged, such as intelligent routing layout [62, 76] and spatial mapping [2, 32]. These methods are preferable for revealing overall traffic patterns for answering general questions, e.g., what are popular roads in a city? where do people head to? However, the methods mostly ignores information of individual OD trail. In certain scenarios such as to find abnormal people movements, additional analytics are required to complement the visualization.

Wrapping up OD trails into bundles can reveal overall traffic patterns, meanwhile keep individual OD trail. Many bundling methods including spring-based (e.g., [36, 66]), image-based (e.g., [39, 48]), and geometry-based (e.g., [16, 35]), have been proposed. These techniques have been successfully employed for many different datasets such as Internet connections and migrations. In these data, it is flexible to manipulate edges as long as node connections are kept. This, however, does not hold for OD trails in urban traffic data. In a city, humans and vehicles are moving along roads, and many activities including traffic jams and accidents, are happening on roads. Hence, OD trails are constrained by road networks. Trail information is equally, if not more, important as ODs for urban traffic data.

Among various edge bundling methods, kernel density estimation (KDEEB) [39] is in state-of-the-art with advantages in speed and generality. However, we identify several inconsiderate settings of KDEEB when applied to OD trails in urban traffic data, including non-optimal kernel size and road neglect. These settings wreck applicability of KDEEB for movement visualization, which requires to preserve road network topology and to support multi-scale exploration. This work presents a new method, namely route-aware edge bundling (RAEB), specifically designed to address the limitations. RAEB employs a comprehensive pipeline consisting of preprocessing, bundling and evaluation processes. A series of new parameters such as route awareness and bundling stability, which leverage advanced techniques from geography and image processing fields, are introduced. Experiments on artificial and real-world urban traffic data show that RAEB can generate more realistic results, meanwhile achieve fast computation speed comparable to KDEEB.

The primary contributions of this work include:

- We develop a new edge bundling method of RAEB, which includes a comprehensive pipeline consisting of preprocessing, bundling, and evaluation processes.
- We adapt existing parameters in KDEEB, and introduce a series of new parameters, to better fit OD trails in urban traffic.
- We conduct several experiments using artificial and real-world urban traffic data to demonstrate effectiveness of RAEB.

3.2 Related Work

Urban Traffic Visual Analytics. In order to facilitate exploration of human/vehicle/goods movement in cities, many visual analytics for urban traffic data have been developed. These visual analytics can facilitate understanding of urban dynamics and human activities, and also enhance traffic management and assessment. Systematic reviews of these works are presented in [1, 13]. In particular, some visual analytics have been specifically developed for studying OD trails in urban traffic. Among them, advanced indexing methods (e.g., [22, 86]) and new interaction models (e.g., [43, 86]), have been developed to facilitate movement query. After filtering OD trails, these visual analytics are typically complemented with statistical analysis, and the analysis results are then presented with statistical graphics.

Figure 3.1(a) presents a density map of Manhattan green taxi trips mapped on road network. The visualization method is employed in many visual analytics for urban traffic. Though commonly available, the visualization requires additional analytics to reveal overall traffic patterns. This work aims to develop a new visualization technique which can present traffic patterns in one view. Such a visualization can be complementary with existing analytics techniques.

OD Movement Visualization. Urban traffic such as taxi trips and mobile phone traces can be categorized as movement data. The data are commonly modeled as OD trails containing information of origin, destination, and in-between trails. Many OD visualization

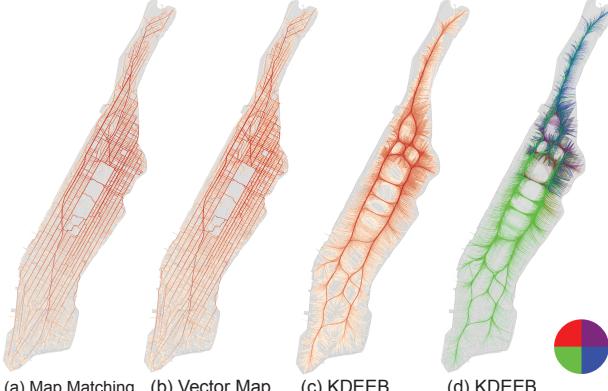


Figure 3.1. Methods for visualizing OD trails in urban traffic: (a) map matching, (b) vector map, (c) & (d) KDEEB bundles rendered in density and direction, respectively.

techniques have been devised, which in general can be categorized into matrix- and flow-based. Matrix-based techniques represent ODs as a matrix, with cell colors representing flow magnitudes of OD pairs. Sorting of rows and columns are usually used to make cluster patterns apparent [82]. The techniques can clearly show OD flow magnitudes, yet it fails to present geographical information. OD map [83] was devised to address the shortage. The approach divides a traditional OD matrix into two layers, where the first and second layer represents origins and destinations, respectively. Flow-based techniques provide a more intuitive way to show geographical information. However, the methods face scalability issues for huge amounts of OD movements, as the display will be cluttered with excessive edge crossings. To mitigate clutters, spatial aggregation methods are usually employed. OD aggregation methods such as graph partitioning [31] and density-based clustering [77], have been proposed to cluster ODs. Spatial aggregation can also be accomplished by grouping trails into continuous flows in flow map layout [62] or composite layout [15].

Both matrix- and flow-based methods perform well in reducing clutter, yet information of individual OD trail is not preserved. This may cause unexpected information loss when exploring urban traffic data. For example, an abnormal suspect movement to a remote place can be grouped together with normal trips.

Edge Bundling. To show individual OD trail, we treat ODs as nodes, and trails as links in a node-link graph, and employ edge bundling methods to reduce clutters. Systematic overviews of state-of-the-art edge bundling techniques can be found in [47, 90]. Here, we just give an overview.

Methods for general graphs can be categorized in three categories [90]. *Spring-based* methods model edges as springs, and generate bundled graph layout by assigning forces to the edges that can attract or repel each other (e.g., [36]). These methods usually suffer from high computational complexity and the processes are time-consuming. *Geometry-based* methods cluster edges based on potential control meshes in the input graph, which can be constructed through hierarchical graph drawing [35], triangulation [46, 91], complex polygons [16], and functional decomposition [38]. Control meshes make geometry-based methods flexible and easy to control, yet the construction process can be time-consuming when the graph is large. *Image-based* methods utilize image-processing to accelerate the bundling process. Skeleton-based (SBEB [20]) and kernel density estimation (KDEEB [39]) methods are developed in this category. Compared with the other two groups of methods, image-based methods leverage GPU’s powerful computing capacity, making them computationally efficient and scalable to handle millions of edges [48, 74].

Besides, many edge bundling methods are developed targeting at improving certain features such as to minimize ambiguity [6, 56] and to reveal directional edge patterns [67]. Some other methods are developed for specific applications such as to visualize geographical data in 3D [45, 71] and neural connections in brain [9, 85]. Closely related to our work, vector map [71] employs road network as a reference graph for edge bundling and represent the bundles as B-splines. The approach is preferable for avoiding intersecting with obstacles in 3D, while marginal improvements are accomplished for urban traffic data on dense road networks. Figure 3.1(b) presents a vector map for Manhattan taxi trips in finest scale, which is very close to the original map as in Figure 3.1(a). In comparison, Figure 3.1(c) & (d) present KDEEB bundles with bundle lines colored in flow density and OD direction, respectively. Main traffic roads and flow directions can be identified easily. Nevertheless, there are many limitations of KDEEB when applied to urban traffic data. We address these limitations with a new bundling method of RAEB.

3.3 Problem Statement and System Overview

This section briefly describes KDEEB algorithm, followed by a discussion of inconsiderate settings when applied to OD trails in urban traffic. An overview of RAEB is presented at

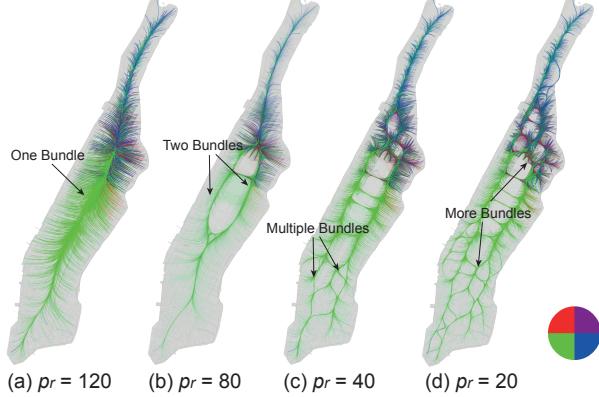


Figure 3.2. KDEEB applied to taxi trips in Manhattan with different kernel sizes p_r : (a) 120, (b) 80, (c) 40, and (d) 20. More detailed bundles are generated with smaller p_r .
the end.

3.3.1 KDEEB Algorithm

KDEEB is a fast edge bundling method for visualizing dense graphs. It employs a general pipeline with edge sampling, splatting, gradient estimation, edge advection, and bundle smoothing. In edge sampling step, an edge e_i is divided into uniformly-sampled polylines, i.e., $e_i = \{x_j\}$, with user-given sampling step σ . After that, KDEEB computes a density map $\rho : \mathbb{R}^2 \rightarrow \mathbb{R}^+$ as

$$\rho(x \in \mathbb{R}^2) = \sum_{y \in D} K\left(\frac{\|x - y\|}{p_r}\right) \quad (3.1)$$

where K is a parabolic radial kernel and p_r is kernel radius. Next, each edge sampling site x_j is advected to a new position x'_j as:

$$x'_j = x_j + p_r \frac{\nabla \rho}{\|\nabla \rho\|} \quad (3.2)$$

Finally, a smoothing function is applied on x_j to remove jitters created by the advection step. These steps are repeated p_n times until stable bundles are generated.

Parameter Setting. KDEEB requires several parameters to be preset by users. Following settings are recommended [74]:

- Kernel radius p_r : Initial value set to 5% of graph drawing size. A constant decay ratio λ in $[0.5, 0.9]$ is applied to p_r at each bundling iteration n .

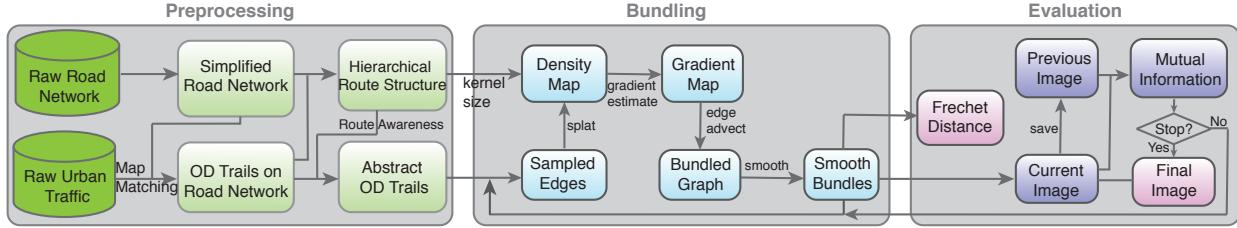


Figure 3.3. Overview of RAEB pipeline. Our method mainly consists of three phases: *Preprocessing* for creating a proper initial layout, *Bundling* for bundling input OD trails, and *Evaluation* for generating a stable bundle structure.

- Bundling iteration p_n : An integer in between 10 to 15.

3.3.2 Problem Identification

The parameter settings are recommended for general graphs that consist of fixed nodes and connections between them. For such a graph, it is free to manipulate node connections into smooth polylines. However, when applied to OD trails in urban traffic data, KDEEB encounters the following issues.

- *P1: Non-optimal Kernel Radius.* Kernel radius p_r in KDEEB is solely based on graph drawing size, while ignores geometric properties of road network. Figure 3.2 presents KDEEB results generated with different kernel sizes for taxi trips in Manhattan: 120, 80, 40, and 20 in (a) - (d), respectively. Sizes for graph drawing are all 720×1440 , thus KDEEB would recommend $p_r = 80$ as 5% of graph graphing size. However, smaller p_r generate more detailed and visual appealing bundles, comparing Figure 3.2(b) to (c) & (d). This happens because most space in graph drawing are not utilized, due to the long and thin shape of Manhattan island. In addition, urban traffic can unevenly spread in a city, such as Shenzhen taxi data (Section 3.7.3), making small p_r preferable.
- *P2: Road Neglect.* Urban traffic are moving along roads in a city, thus OD trails should be constrained to roads in a city. However, KDEEB represents each OD connection with a direct line, while ignores information about the road network. Thus, resulting bundles can be displaced far away from the roads. This can cause impression of

traffic moving in wrong positions, such as those bundles in between Manhattan and Brooklyn (Section 3.7.1). The displacements can also add difficulty to mentally map original OD trails with resulting bundle lines.

Besides, KDEEB lacks a quantitative method to automatically terminate bundling iterations.

- *P3: Preset Bundling Iterations.* KDEEB is an image-based edge bundling method. Most of these bundling methods generate bundling results in an iterative way. The number of bundling iterations p_n is preset based on practical experience: 10 in KDEEB [39], while 15 in CUBu [74]. The numbers are chosen because tight and stable bundles are generated. However, these conditions are rather subjective, which can vary among individuals and may be affected by other parameters like image size and sampling step.

3.3.3 RAEB Overview

We develop route-aware edge bundling (RAEB), a comprehensive edge bundling method specifically designed for visualizing OD trails in urban traffic. As illustrated in Figure 3.3, RAEB pipeline mainly consists of three parts: *Preprocessing*, *Bundling*, and *Evaluation*.

In *Preprocessing*, RAEB first generates a simplified road network from the input one such as open street map (OSM). Raw OD trails are mapped onto simplified road network using map matching algorithms. Together with urban traffic information, simplified road network can be organized in a hierarchical route structure. OD trails can be abstracted accordingly depending on a new parameter of route awareness defined by users. A value for kernel size is also measured based on geometric property of the route structure.

The abstract OD trails are passed into *Bundling* stage as input graph. Bundling process is an image-based approach similar to KDEEB workflow. Specifically, we discard the preset parameter of bundling iteration p_n in KDEEB. Instead, we introduce a new parameter of bundling stability, which is measured as normalized mutual information between images generated by two consecutive iterations. The measurement is done in the *Evaluation* stage. If bundling stability reaches a threshold, we terminate the bundling iteration and

export a final image. Besides, we measure Fréchet distance between generated bundles to OD trails mapped on the road network. The measurement complements final image with a quantitative metric that reveals quality of a bundling method.

3.4 Preprocessing

This work leverages both OD trails and road network to improve edge bundling quality. This section introduces major steps in *Preprocessing* stage, including: map matching, hierarchical road structure construction, and trail abstraction.

3.4.1 Basic Traffic Concepts

Road Network: A road network can be modeled as a directed graph $\bar{G} = (\bar{V}, \bar{E})$, where \bar{V} is the set of nodes in \bar{G} and \bar{E} is the set of edges connecting nodes in \bar{V} . Degree of a vertex \bar{v} , denoted as $\deg(\bar{v})$, indicating the number of edges connected to \bar{v} . By this, a vertex $\bar{v} \in \bar{V}$ can be classified as an endpoint with $\deg(\bar{v}) = 1$, a midpoint with $\deg(\bar{v}) = 2$, or an intersection with $\deg(\bar{v}) > 2$. To facilitate computation, we can simplify \bar{G} into a simplified graph $G = (V, R)$, where V is the union of endpoints and intersections, and R is a set of links connecting nodes in V . Each link r represents a sequence of n consecutive nodes in \bar{V} :

$$r := \bar{v}_1 \rightarrow \bar{v}_2 \rightarrow \dots \rightarrow \bar{v}_n, \quad \forall \bar{v}_i \in \bar{V} \quad (3.3)$$

where \bar{v}_1 and \bar{v}_n are endpoints or intersections, while the other nodes are midpoints. For the sake of clarity, we use the term *route* to describe such a link. Computation tasks, including shortest path query and map matching, are performed on the simplified graph G .

Urban Traffic: Thanks to open data campaign, many urban traffic data are available nowadays. Typically, raw urban traffic data can come in either of the following forms:

- *UT-1:* origin and destination locations only, such as New York taxi trips [22] and Singapore public transportation rides [86]. Such a raw trip t_{raw} can be represented

as $t_{\text{raw}} := l_o \rightarrow l_d$, where l_o and l_d represent origin and destination locations, respectively.

- *UT-2*: a sequence of GPS positions, such as Stuttgart scooter fleet [43] and Hangzhou taxi trips [78]. Such a raw trip t_{raw} can be represented as $t_{\text{raw}} := l_1 \rightarrow l_2 \rightarrow \dots \rightarrow l_n$, where $l_i \subset \mathbb{R}^2$. l_1 and l_n are origin and destination, i.e., l_o and l_d .

Both forms of urban traffic data can be generalized as a traffic graph $G_t = (L, T)$, where L is the set of locations and T is the set of trips represented as sequential connections of locations.

3.4.2 Map Matching

Constraining movements over an underlying road network, i.e., mapping traffic graph $G_t := (L, T)$ to road network $G := (V, R)$, is usually a preliminary step for urban traffic analysis. This is necessary. First, recorded locations get errors due to imprecise GPS localization, while road network is precise and constant. Second, G_t can be much more complex than G : Taking New York traffic for an example, there are over millions of taxi trips per day, resulting in millions of locations L , yet its simplified road network contains less than 100K routes. Therefore, map matching can enrich effective analysis and visualization.

There are many map matching methods available, including shortest path, minimum turns, and ST-matching [55] for GPS traces. These methods are preferable for different dataset. We employ the following methods for corresponding urban traffic.

- For *UT-1*, i.e., $t_{\text{raw}} = l_o \rightarrow l_d$, we first find corresponding closest nodes $v_o \in V$, $v_d \in V$ for l_o and l_d respectively. After that, we search for the shortest path between v_o and v_d in G .
- For *UT-2*, i.e., $t_{\text{raw}} = l_1 \rightarrow l_2 \rightarrow \dots \rightarrow l_n$, we use ST-matching algorithm, which considers not only spatial features of road network, but also temporal constraints. The method was later visually investigated and optimized with an interactive interface [42].

Category	Exemplary OSM Indicator	Score (r_{hier})
Expressway	motorway, trunk	1
Trunk Road	primary, motorway_link	0.75
Secondary Road	secondary, tertiary	0.5
Branch Road	unclassified, residential	0.25

Table 3.1. Route hierarchy, OSM indicator and hierarchy score

Both methods return a sequence of routes $r_1 \rightarrow r_2 \rightarrow \dots \rightarrow r_n$ in G for each OD trail t_{raw} . We then combine the routes with origin (l_o) and destination (l_d) locations of t_{raw} . Thus, both types of t_{raw} are converted to the same map matching form.

$$t_{map} := l_o \rightarrow r_1 \rightarrow r_2 \rightarrow \dots \rightarrow r_n \rightarrow l_d. \quad (3.4)$$

Here the OD trail's origin l_o and destination l_d are kept.

3.4.3 Hierarchical Route Structure Construction

A road network is usually designed in hierarchical levels to avoid dense direct connections among regions. This inspires us to construct a hierarchical route structure to benefit edge bundling. Although urban roads are organized hierarchically, it does not consider OD trails. This work makes use of the following attributes of a route r in $G := (V, R)$ to construct a hierarchical route structure.

Route length ($\text{len}(r)$). Visual appearance of each OD trail is determined by its routes on road network. Longer a route, more it will affect the visual appearance. Thus an important component affecting route hierarchy is route length. Here, $\text{len}(r)$ is measured in Euclidean space and normalized over the whole road network.

Road hierarchy ($\text{hier}(r)$). Urban roads are classified into hierarchies: freeways, arterials, collectors, and local roads. Similar descriptions can also be found elsewhere [78]. A higher level usually indicates faster traffic speed and less access to property. OSM provides more detailed indicators of road hierarchy, e.g., trunk, primary, tertiary, etc. To keep consistent, we classify these indicators into four hierarchies. A route r in each hierarchy is assigned an score according to Table 3.1.

Flow magnitude ($\text{flow}(r)$). Flow magnitude measures how many OD trails pass through

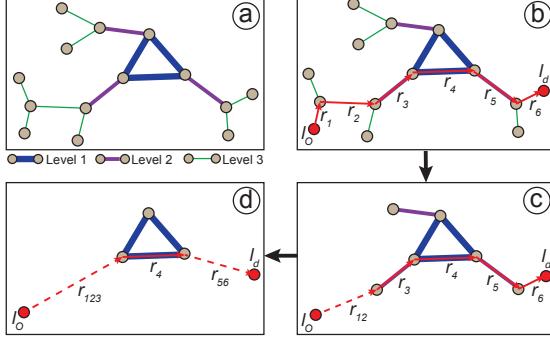


Figure 3.4. Illustration of hierarchical route structure and OD trail abstraction: (a) Three route levels are constructed colored in blue, purple and green, respectively; a raw OD trail is abstracted in accordance to route (b) level-3, (c) level-2, and (d) level-1.

a route r . The previous two factors purely rely on road network, while $\text{flow}(r)$ reflects the importance of a route in consideration of OD trails. Here, $\text{flow}(r)$ is measured by counting how many mapped OD trails passing through r , and then normalized.

By this, each route can be represented by a vector $V(r) := \langle \text{len}(r), \text{hier}(r), \text{flow}(r) \rangle$. Score of a route $\text{score}(r)$ can be measured as $\text{score}(r) = \sum w_i \times V(r)_i$, where the weights $w_i (i = 1, 2, 3)$ controls how much each attribute affects route weight. We choose 0.3, 0.1, and 0.6 in this work, which highlights the importance of flow magnitude. In the end, all routes are sorted in descending order according to their weights. The routes R are further subdivided into multiple hierarchical levels R^1, R^2, \dots, R^n . Each level of routes accounts for top- k routes.

3.4.4 Trail Abstraction

P2 states that road network is omitted in original KDEEB, which can lead to wrong depiction in geographical space and poor support of multi-scale exploration. We introduce a new parameter of route awareness p_{ra} , which defines the level of trail abstraction, to tackle this issue. Higher p_{ra} indicates that more details of OD trails should be preserved. Given a hierarchical route structure in n levels, p_{ra} can range from 0 to n . If p_{ra} is set to zero, OD trails will be abstracted to straight lines connecting ODs directly. If p_{ra} is set to n , no abstraction will be applied. If p_{ra} is set to a value m in $[1, n - 1]$, routes in level-1 to level- m will be preserved.

Figure 3.4(a) presents an exemplary road network with a hierarchical route structure.

The routes are categorized into three levels: blue thick lines for level 1, purple medium lines for level 2, and green thin lines for level 3. Figure 3.4(b-d) illustrates an example of how a raw OD trail of $l_o \rightarrow r_1 \rightarrow \dots \rightarrow r_6 \rightarrow l_d$ can be abstracted in accordance to the hierarchical route structure shown in Figure 3.4(a). In Figure 3.4(b), p_{ra} is set 3, and all routes are preserved. In Figure 3.4(c), p_{ra} is set 2, so route r_1 and r_2 will be merged together as they are both level-3 routes. In Figure 3.4(d), p_{ra} is set 1, thus only route r_4 will be kept.

3.5 Bundling Method

Algorithm 1 KernelSizeMeasurement

Input: Top N sorted routes as polyline list $\mathbf{P} = \{P_1, \dots, P_N\}$

Output: Initial kernel size p_r

```

1: Let  $d[ ][ ]$  denote distance between polyline pairs
2: for  $i = 1$  to  $N$  do
3:   for  $j = i + 1$  to  $N$  do
4:      $d[i][j] = d[j][i] = \text{DiscreteFrechetDistance}(P_i, P_j)$ 
5: Let  $\mathbf{C}$  denote a list of polyline clusters;
6:  $\mathbf{C} = \text{DBSCAN}(\mathbf{P}, \text{eps}, \text{minNum})$ ;
7:  $C_{\max} = \arg\max_{|C_i|} (C_i | C_i \in \mathbf{C})$ ;
8: Initialize  $d_{geo} = 0$ ;
9: Let  $\text{count} = |C_{\max}| \times (|C_{\max}| - 1)$ ;
10: for each  $P_i \in C_{\max}$  do
11:   for each  $P_j \in C_{\max}$  &&  $P_i \neq P_j$  do
12:      $d_{geo} = d_{geo} + d[i][j] / \text{count}$ ;
13:  $p_r = \text{ToDrawingSpace}(d_{geo} / 2)$ ;
14: return  $p_r$ 

```

RAEB adapts KDEEB bundling algorithm [39] to better reveal topology of urban traffic. This sections presents amendments employed by RAEB, including kernel size measurement and density map generation.

3.5.1 Optimal Kernel Size

KDEEB only considers the size of graph drawing when determining kernel size. This strategy may not be optimal for bundling OD trails in urban traffic (*P1*). Ideally, the chosen

kernel size should be able to bundle closely-related OD trails (e.g., movements on bi-directional roads), while separate loosely-correlated OD trails (e.g., movements on two different highways).

To address *P1*, both graph drawing size and geometric property of road network should be considered. We develop an automatic process for measuring initial kernel size, as outlined in Algorithm 1. Here, top N routes are extracted from *Preprocessing* stage. The routes are treated as a polyline list \mathbf{P} , and inputted into the algorithm. Pair-wise distance between each pair of ploylines are computed. Then a DBSCAN algorithm is applied to group the polylines into polyline clusters \mathbf{C} . The cluster with maximum number of polylines is extracted, and denoted as C_{\max} . Average geographical distance d_{geo} is computed for polylines in C_{\max} . Finally, half of d_{geo} is converted to p_r in graph drawing space, and p_r is returned as the initial kernel size.

Basically, the algorithm first computes average geographical route distance in the top N routes, and then converts the distance to graph drawing space. N should not be too small that the routes are not representative for the whole road network; meanwhile, it should not be too big to overlap route awareness. From our experiments, we find 1% of whole route size is appropriate for N . Besides, another important factor is the distance metric between two polylines. Here, we choose discrete Frechet distance, which measures similarity of two polylines considering both locations and ordering of the points along the polylines. The metric is one of the most popular methods for movement analysis [30], and can be computed efficiently [19].

3.5.2 Density Map Generation

KDEEB omits trail information (*P3*), as it connects ODs with directed lines. We aim to keep bundles close to OD trails on road network. More specifically, in *Preprocessing* stage, each OD trail is abstracted into a sequence of artificial directed lines and real routes in road network. The artificial directed lines are free to manipulated, while we would like to keep the bundle layout spatially close to the real routes. In addition, it is preferable to keep the bundling paradigm of advecting sampling sites towards high density directions.

To achieve this goal, we modify the density map generation used by KDEEB. Let de-

note a list of routes $R_{\text{aware}} \subset \mathbb{R}^2$ are kept for route awareness. Since sampling sites are advected towards their gradient directions, gradients of points along R_{aware} should be either (1) zero, or (2) pointing to route direction. To minimize effects on densities surrounding R_{aware} , we choose the second option. Instead of Eqn. 3.1, we now use

$$\rho_{\text{od}} = \rho + D(x|x \in R_{\text{aware}}) \quad (3.5)$$

where $D(x) \in \mathbb{R}^+$ is a constant assigned to a point $x \in R_{\text{aware}}$. High D value will make it more likely that gradient at x points to the same direction with the route.

3.6 Evaluation

Besides introduction of *Preprocessing* and adaptions in *Bundling*, post hoc bundling evaluation methods are also developed in RAEB. This section introduces these methods, including mutual information and bundle deviation measurements.

3.6.1 Normalized Mutual Information

After each bundling iteration, a bundling method needs to decide whether the bundling iteration should continue or not. KDEEB presets a bundling iteration parameter p_n , similar to many other bundling methods including SBEB, FTTEB, and CUBu. $p_n = 10$ is chosen such that the bundles converge to a stable structure. Structure stability is basically the perception of visual similarity between images generated in two consecutive bundling iterations. However, the perception can be easily biased by many factors, including people's color perception difference, lighting conditions, etc. It lacks a quantitative method for measuring structure stability.

We employ mutual information (MI) - a basic concept from information theory, as a quantitative indicator for measuring bundling stability. Maes et al. [57] introduced MI to measure statistic dependence between intensities of corresponding voxels in two medical images. This work measures MI between images generated in consecutive bundling iterations, which are geometrically aligned. Hence, the measurement is simplified without geometry matching. Let denote two input images X and Y . MI is computed as:

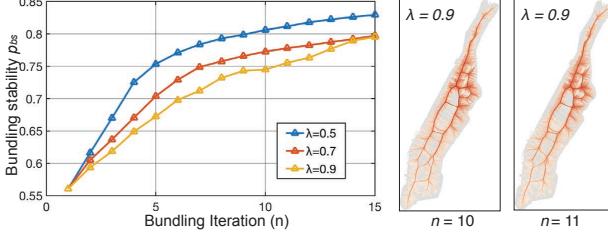


Figure 3.5. (left) Bundling stability p_{bs} measured at each bundling iteration for different decay ratios λ , (right) visually indistinguishable images are generated at iteration 10 and 11 for $\lambda = 0.9$.

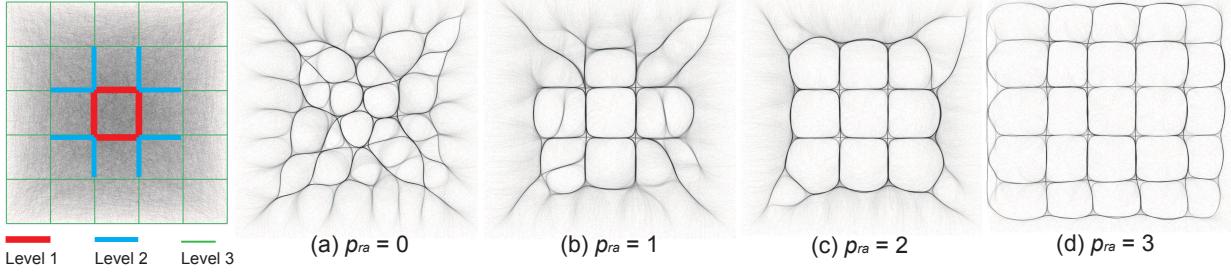


Figure 3.6. Leftmost: raw 100K artificial OD trails on a grid road network in three hierarchies. (a) - (d): RAEB bundling results with route awareness parameter p_{ra} set to 0 - 3, respectively.

$$I(X, Y) = \sum_x \sum_y p(x, y) \log\left(\frac{p(x, y)}{p(x)p(y)}\right) \quad (3.6)$$

where $p(x)$ and $p(y)$ indicate the intensity at $x \in X$ and $y \in Y$, and $p(x, y)$ measures the joint value between $p(x)$ and $p(y)$. MI is affected by image size, while we prefer a constant measurement for different graph drawings. Hence, we adopt normalized MI (NMI):

$$NMI(X, Y) = \frac{2I(X, Y)}{H(X) + H(Y)} \quad (3.7)$$

where $H(X) = -\sum p(x)\log(p(x))$ that measures entropy for X .

We introduce a new parameter of bundling stability p_{bs} . p_{bs} is computed in every iteration as $NMI(I_n, I_{n-1})$, where I_n and I_{n-1} denote images generated at iteration n and $n - 1$, respectively. Figure 3.5(left) presents NMIs at each bundling iteration for three different kernel size decay ratios λ . It is observed that NMI increases when bundling iteration increases, and smaller λ leads to faster NMI increment. All NMIs pass over 0.75 around iteration 10, and reach close to 0.8 at iteration 15. Figure 3.5(right) shows two

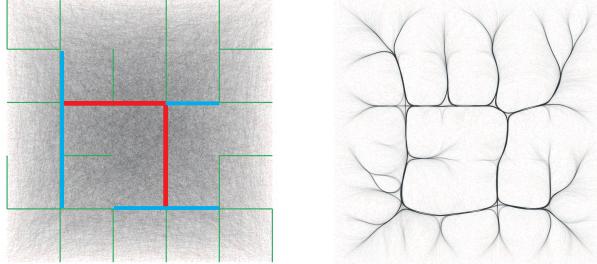


Figure 3.7. Left: raw 100K artificial OD trails on a hierarchical road network. Right: RAEB bundling result with p_{ra} set to 2.

images at iteration 10 and 11 for $\lambda = 0.9$. The images are hardly distinguishable from each other. Thus, we can claim the bundling produces stable results, and the process can terminate. In this way, we determine a threshold for p_{bs} to control bundle termination. If a bigger threshold is chosen, more stable results will be generated.

3.6.2 Bundle Deviation

p_{bs} is introduced for measuring visual stability of bundle layouts generated by one bundling method. However, p_{bs} is not suitable for comparing bundling quality of multiple bundling methods. Many evaluation metrics can be used for comparing graph layouts, such as edge crossing, ambiguity, and edge direction. These metrics are suitable for general graphs without a ground truth. However, OD trails studied in this work are constrained in roads in a city. We would like to keep the generated bundles close to their OD trails on the road network. Though map matching algorithm can introduce errors, this work treats mapped OD trails as ground truth, instead of raw OD trails. This is because of: for *UT-1* urban traffic, only origin and destination information are recorded; for *UT-2* urban traffic, accuracy of GPS positions are not perfect.

We introduce a new parameter of bundle deviation, denoted as p_d , to measure distance between final bundles and OD trails mapped on the road network. Both bundles and OD trails can be modeled as polylines made up of sequential positions in geographical space. Thus, the distance between them can be measured using discrete Frechet Distance. We calculate mean distances for all bundles, and map the mean in graph drawing space.

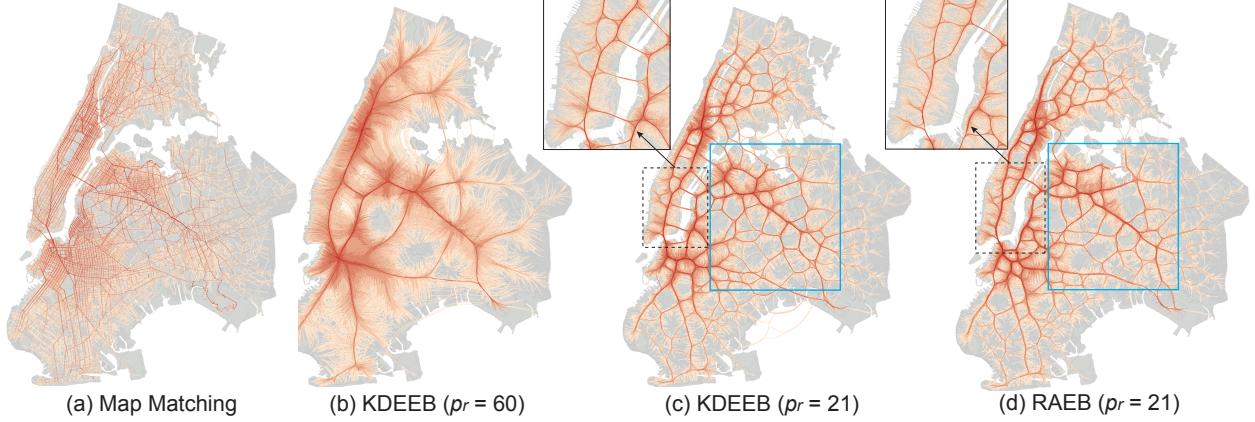


Figure 3.8. Density maps of NYC taxi trips: (a) shortest paths mapped onto the road network, (b) KDEEB bundles with kernel size $p_r = 60$, (c) KDEEB bundles with $p_r = 21$, and (d) our RAEB bundles with $p_r = 21$.

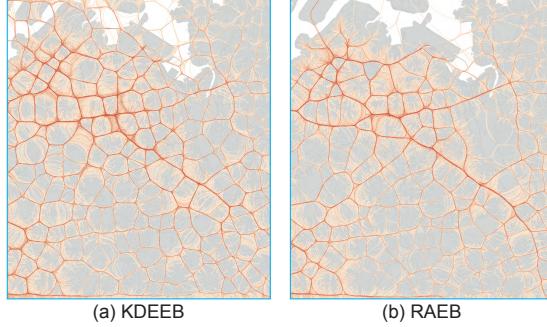


Figure 3.9. Fine scale density maps of NYC taxi trips in Queens zone generated by (a) KDEEB, and (b) RAEB.

3.7 Applications

This section presents applications of RAEB on artificial OD trails, and real-world taxi data in New York and Shenzhen. We show advancements of RAEB over KDEEB.

3.7.1 Artificial OD Trails

Our first example uses a random graph with 100K OD trails, and 5×5 grid and hierarchical reference graphs to simulate conventional road networks. Raw OD trials and corresponding road networks are shown in the leftmost figures of Figure 3.6 and Figure 3.7. The OD trails are first mapped to underlying road networks using shortest path algorithm, and then both road networks are divided into three hierarchies that are colored in red, blue and green, respectively. In the last, we apply RAEB on the OD trails, with all graph

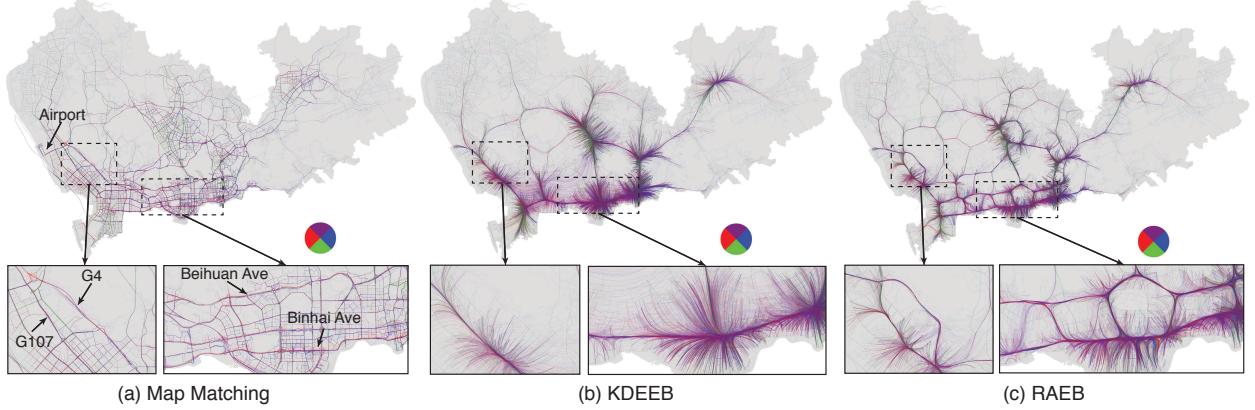


Figure 3.10. Density maps of Shenzhen taxi trips: (a) raw GPS records are mapped onto road network, (b) KDEEB bundles trips on close aerial roads together, while (c) RAEB preserves these roads. All lines are colored according to the OD directions.

drawing sizes set to 1280×1280 and initial kernel sizes p_r set to 60.

In advance of KDEEB, RAEB allows to preserve route awareness by controlling parameter p_{ra} . To evaluate the effects of p_{ra} , we set p_{ra} to 0 - 3, and apply RAEB to OD trails on the grid road network as shown in the leftmost figure of Figure 3.6. The results are shown in Figure 3.6 (a) - (d). In (a), p_{ra} is set to 0, i.e., no route awareness will be preserved. In this case, RAEB should be equivalent to KDEEB with other parameters the same. The proof is demonstrated in (a), which shows smooth bundles similar to those in the original KDEEB [39]. To preserve level 1 routes, we set p_{ra} to 1, and the result is shown in (b). As expected, OD trails around the red lines are bundled together with bundles following red lines, while other OD trails are bundled with bundles spreading arbitrarily in the graph drawing. More route awareness can be preserved as we increase p_{ra} to 2 and 3, as shown in Figure 3.6 (c) & (d).

More importantly, route awareness p_{ra} can be used to preserve topology of underlying road network. Figure 3.7 (right) shows bundling result of RAEB applied to OD trails on a hierarchical road network that is shown in Figure 3.7(left). Here, p_{ra} is set to 2, such that to preserve both the red and blue lines. It is clear that the resulting bundles follow the lines, making it easy to trace OD trails. In contrast, KDEEB will generate the same result with that in Figure 3.6(a), as the underlying road network information is not used.

3.7.2 New York Taxi Trips

In reality, a road network is usually much more complex, and OD trails are more dynamic than the artificial ones. In this experiment, we further compare RAEB with KDEEB using results generated from New York taxi trips.

The road network employed in this study is extracted from OpenStreetMap (OSM) within the boundary of Manhattan, Brooklyn, Queens, and Bronx zones, where most origins and destinations are located. The raw network consists of 133,154 nodes, 166,122 edges, and it is simplified to 97,336 routes. The OD trails studied in this experiment are 100K taxi trips extracted from one-month trip records. The original records consist of various attributes for each trip, including vendor id, pickup & dropoff times and positions, and fare amount, etc. We use the pickup & dropoff positions, and map it onto the road network using shortest path algorithm. Figure 3.8(a) presents a density map of the mapped taxi trips.

Figure 3.8(b - d) show bundling results generated by KDEEB and RAEB, with graph drawing sizes set to 1080×1440 . The experiment is started with KDEEB recommended settings of kernel size $p_r = 60$ (about 5% of graph drawing size) and $p_n = 10$. Figure 3.8(b) shows the bundling result, which clearly presents several main bundles. The bundles reveal primary traffic movements over the whole city. Yet in other ways, the results are heavily bundled, missing details of road network topology. To show more details, we measure initial kernel size considering both graph drawing and geometric property of road network as described in Section 3.5.1. p_r is reduced to 21. Figure 3.8(c) shows the corresponding KDEEB bundling results. More bundles are formed, in line with arterial roads in New York. However, there are many bundles lying by non-existing roads, as those shown in the highlighted region in-between Manhattan and Brooklyn. This illustration can cause wrong impression of bridges connecting the zones. Figure 3.8(d) shows results generated by RAEB, with $p_r = 21$ and route awareness $p_{ra} = 1$. The undesirable bundles are removed by our method.

Visualization of urban traffic should support multi-scale exploration – an important characteristic for movement data visualization. In the context of this work, a good edge bundling algorithm should provide smooth transitions of bundling results at different

scales. We further evaluate multi-scale exploration by zooming into the blue region in Queens zone as in Figure 3.8(c) & (d), and applying KDEEB and RAEB on the OD trails. The fine scale bundling results are presented in Figure 3.9(a) & (b), respectively. More bundles are generated by both methods, as the same effect when zooming into maps. However, it is difficult to visually match bundles in Figure 3.8(c) with those in Figure 3.9(a). In comparison, bundles in Figure 3.8(d) can be more easily identified in Figure 3.9(d).

3.7.3 Shenzhen Taxi Trips

We further evaluate the performance of RAEB using taxi trips in Shenzhen, with road network extracted from OSM. In total, there are 161K nodes and 177K edges, and the edges are simplified to 51K routes. The OD trails are one-week taxi trip records. Unlike New York taxi records with only origin and destination positions, Shenzhen’s data contain a sequence of GPS positions recorded in every 20 seconds. We clean and extract in total 50K taxi trips from the records. The trips are further mapped onto the road network using ST-matching algorithm [55].

Figure 3.10(a) presents a graph of the map matching results in the size of 2160×1280 . The lines of a trip are colored according to direction from the trip’s origin to destination. The graph shows that most taxi trips are recorded in the southern region of Shenzhen, which borders on Hong Kong and is more developed than other regions. The unevenly distributed taxi trips make it improper to use kernel size p_r recommended by KDEEB, which is over 100 as 5% of the graph drawing size. Instead, our method suggests $p_r = 26$, considering the road network topology as well.

Using this setting of p_r , both KDEEB and RAEB reaches stable states at iteration 8. Figure 3.10(b) & (c) show the corresponding results, respectively. Both methods create smooth bundles in line with arterial roads in Shenzhen, indicating p_r measured by our method is preferable. Besides, nearly the same bundles are generated in regions other than south part, except that RAEB’s result shows more details. More dissimilar results are shown in the highlighted areas. Expressways G4 and G107 lead traffic to Shenzhen airport in the left region, while Beihuan and Binhai avenues holds main traffic in the right one. KDEEB merges OD trails passing these roads, while our method splits the bundles. In short, RAEB generates results more similar to real-world scenarios.

Parameters	KDEEB	RAEB
Route awareness (p_{ra})	—	0 - Number of road hierarchies
Kernel size (p_r)	Graph drawing	Graph drawing and road network geometry
Bundling iterations (p_n)	10 - 15	—
Bundling stability (p_s)	—	NMI between images in consecutive iterations
Bundling deviation (p_d)	—	Average Frechet distance of bundles to OD trails

Table 3.2. Main parameter adaptions in RAEB, in comparison with these in KDEEB.

3.8 Discussion

The experiments demonstrate that RAEB outperforms KDEEB in visualizing OD trails in urban traffic data. The first experiment with artificial data shows that the introduction of route awareness p_{ra} in RAEB distinguishes grid and hierarchical network structures. The second experiment presents the comparisons between KDEEB and RAEB using New York taxi data, which records only origin and destination positions. The results with different kernel size p_r and in multi-scales indicate that, (1) p_r should be measured based on not only graph drawing size, but also underlying road network topology; and (2) RAEB supports better multi-scale exploration. The robustness of RAEB is further demonstrated through the third experiment with Shenzhen taxi data, which records a sequence of GPS positions in every 20 seconds.

The advancements are achieved by parameter settings adopted in RAEB. This section presents detailed discussion on the parameters, followed by performance comparison between RAEB and KDEEB. In the end, we discuss about generality and limitation issues.

3.8.1 Parameters

RAEB adapts and introduces new parameters to better visualize OD trails in urban traffic data. Table 3.2 presents an overview of these parameter settings in comparison with those in KDEEB.

- **Route awareness (p_{ra}):** An input graph for KDEEB is straight lines connecting end

nodes directly. As discussed in the first experiment with artificial OD trails, such an input graph cannot distinguish grid and hierarchical road networks. Instead, we introduce route awareness parameter p_{ra} to control layout of input graph. The first experiment also shows that p_{ra} can be manipulated to generate bundles representing levels of details of road network. If p_{ra} is set to zero, input graph will be straight lines and the results are the same with KDEEB; if p_{ra} is set to the highest number of road hierarchies, input graph will be OD trails in line with road network, and more roads can be preserved.

- **Kernel size (p_r):** In the second experiment with New York taxi data, we show that the parameter kernel size p_r can control bundling coarseness. KDEEB computes p_r as 5% of graph drawing size, which will generate coarse bundles that can only reveal main traffic connections (Figure 3.8(b)). Instead, RAEB suggests p_r should be measured based on both graph drawing size and road network geometry. In this way, a smaller p_r is generated, and fine bundles that reveal details of street networks are generated (Figure 3.8(c) & (d)). The advantage of our approach is further demonstrated using Shenzhen taxi data, which exhibits imbalanced distribution of taxi trips in the city.
- **Bundling iteration (p_n):** KDEEB presets bundling iteration p_n to a fixed number in between 10 - 15, such that to terminate the bundling process. The choice of a suitable p_n , however, needs much experience and varies among different people. Adjustments in other parameters may also require fitting of the parameter. RAEB discards this subjective parameter.
- **Bundling stability p_s :** Instead, RAEB introduces a new parameter – bundling stability p_s , to control bundling process termination. p_s is measured as normalized mutual information (NMI) between images generated in two consecutive bundling iterations. NMI is a common metric in image processing field, thus can be easily integrated. When p_s reaches a predefined threshold, which means that visually a stable structure is generated, the bundling process will be automatically terminated.
- **Bundling deviation p_d :** While p_s measures bundling stability of a bundling method, it still lacks a method to quantitatively compare multiple ones. The parameter bundling

Graph	Edge Samples	p_n	Time (sec.)		Deviation (pixel)	
			KDEEB	RAEB	KDEEB	RAEB
Random (grid)	4.6M	13	40.3	50.7	18.37	12.58
NewYork	3.1M	11	34.3	42.9	15.40	9.88
Shenzhen	1.3M	8	13.8	22.8	13.71	10.53

Table 3.3. Statistics comparison of KDEEB and RAEB for datasets used in the experiments.

deviation p_d is introduced to fill the gap. p_d is measured as average Frechet distance of bundles to corresponding OD trails. The measurement is widely employed in geographical science, and we compare KDEEB and RAEB regarding the parameter below.

Some of these parameters can be automatically computed, including p_r and p_d , while settings of p_{ra} and p_s can be consistent across different input data. From the experiments, we recommend 1 for p_{ra} (corresponding to top 5% ranked routes), and 75% for p_s .

3.8.2 Performance

Table 3.3 shows comparison of KDEEB and RAEB for the datasets used in the experiments. Both methods are implemented in Java running on a MacBook Pro with a 3.1 GHz Core i7 and Radeon Pro 560 graphics. We employ the same kernel size p_r and bundling iterations p_n measured by our approach for both methods.

KDEEB's bundling process include sampling, splatting, advecting and smoothing steps. Bundling time for each iteration is mainly determined by number of edge samples and kernel size. Since kernel size measured by our approach is generally smaller than that by KDEEB, bundling time is reduced. The total running times for KDEEB methods are comparable with those in the original work [39]. RAEB requires an additional step of bundling stability measurement, which is determined by the graph drawing size. This adds in a running time of less than 1 seconds in each iteration for all three experiments. The measurement is computed in every bundling iteration, thus we can shorten time by reducing the measurement frequency. All the steps can be further accelerated using GPU e.g. CUDA [74].

On the other side, bundles generated by our method are more close to OD trials, as revealed by comparison regarding bundling deviation. From the table, RAEB reduces about 1/3 deviations of those in KDEEB for artificial and New York taxi datasets. The improvement is smaller for Shenzhen taxi data, though graph drawing in Shenzhen experiment is bigger. This is probably because taxi trips are concentrated in a small area in the south of Shenzhen. Nevertheless, the result image by RAEB shows more improvements than that by KDEEB (Figure 3.10(c) vs (b)).

3.8.3 Applicability and Limitations

The experiments have shown the applicability of RAEB for bundling and visualizing OD trails in urban traffic using real-world taxi data. RAEB introduces new parameters of route awareness p_{ra} and bundling deviation p_d , and adapts existing measurement of kernel size p_r , to better fit road network topology. The approach can be extended to other types of urban traffic data, such as commuter trips using public transportation, or people traces derived from call detail records. These dataset consists of both OD trails and underlying road network. Through advanced map matching algorithms, urban traffic's real paths on a road network can be recovered. However, the parameters are not applicable to general graphs with information of only node connections, except for bundling stability p_{bs} .

Edge bundling methods face a common issue of unrealistic bundle lines. Specifically for OD trails in urban traffic, bundle lines should not be far away from real paths. RAEB mitigates the issue with route awareness p_{ra} for controlling edge layout of input graph, and bundling stability p_{bs} for generating stable results. The first experiment shows that p_{ra} can preserve certain routes on demand, while the second experiment reveals that RAEB supports better multi-scale exploration. Experimental results of bundling deviations p_d further proves the advantage of RAEB over KDEEB. Nevertheless, these parameters can only constrain bundle layout in certain extent, as resulting bundle lines are still displaced from OD trials. In scenarios requiring precise positions, such as query movements passing through a waypoint [43] or road segment [78], visual hints are required to remind the displacement.

Bundles generated by RAEB can show clear traffic patterns, meanwhile preserve road network topology better than KDEEB in a city. These main goals of this work have been

successfully achieved, as demonstrated by the experiments. On the other hand, RAEB is not able to reveal detailed traffic patterns such as directional movements. Direction is of recognized importance for studying OD trails in urban traffic [86]. This limitation can be addressed by including directional information in density estimation or edge advecting functions, as described in CUBu [74]. Besides, RAEB is an image-based edge bundling method, constraining its applicability for 2D rendering only. Applications such as to bundle movements [45, 71] and fiber tracts [38] in 3D, and graphs in virtual reality [44], need spring- or geometry-based bundling methods.

3.9 Conclusion and future work

OD visualization is challenging – no universally good technique is available for visualizing arbitrary ODs [3]. In particular, this work studies OD trails in urban traffic. We identify inconsiderate settings of existing kernel density estimation edge bundling (KDEEB) method when applied in the scenario. This is because KDEEB was developed for general graphs such as airlines and migrations, while ignores data nature of urban traffic data. These inconsiderate settings can cause domain-specific problems such as no preservation of road network topology and poor support of multi-scale exploration. We contribute to the field with a new technique, namely route-aware edge bundling (RAEB). The bundling process is complemented with preprocessing that generate more proper input edge layout, and evaluation that create more stable visual results. A series of parameter adaption and introduction are made to better cater to geometric properties of OD trails and road networks. We compare RAEB with KDEEB in regarding to bundling time and deviation using artificial and real-world taxi data. The experiment results show that RAEB outperforms KDEEB in reducing bundling deviation meanwhile achieving comparable computation speed.

Even though RAEB is specifically designed for bundling OD trails in urban traffic, some parameters such as bundling stability p_{bs} can be applicable to other iterative edge bundling methods, including SBEB [20] and FDEB [36]. We would like to try integrating these parameters in the bundling methods, such that to make them more controllable. We also realize many computation tasks in RAEB can be parallelized, thus bundling effi-

ciency can be improved by GPU acceleration. It would be worthy to reimplement RAEB in GPU, similar to CUBu [74]. Besides bundling control and efficiency issues, how to access bundling quality and faithfulness are the main challenges hindering the applicability of edge bundling methods [47]. Our experiences in developing RAEB suggest that in specific application scenarios, these challenges can be solved with domain knowledges. On the basis of treating OD trails mapped onto road network as ground truth, our proposed parameter of bundling deviation p_d is a quality and faithfulness metric in certain extent. The parameters is derived from Frechet distance that is a common metric in geographical science. In the future, we would like to apply RAEB in other fields such as to visualize neural connections in brain [9,85]. Adaptions are most likely required, and we envision close collaborations with domain experts can facilitate the development.

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