

Homework 1 Minh Cao

2025-01-15

Question 1

- a. There is a positive association between height of athlete and length of jump
- b. There is a linear upward trend between two variable => we can use linear regression
- c. Choice: 1. Reason: Positive and Upward
- d. The response is quantitative, explanatory variable is also quantitative
- e. Predited length of the jump is:

```
X = 72
yhat = 6.4285 + 1.0534*X
yhat
```

```
## [1] 82.2733
```

- f. The slope of the linear equation
- g. No
- h. The coach cannot conclude that because this is an observational study, there might be a counfounding variable for the length of the jump (ie, diet, spleep, etc)
- i. It will stay the same because we will still calculate the distance length in inches then convert it to feet
- j. It will not stay the same because the scale of explanatory variable will change. This would lead change to the intercept
- k. The correlation will stay the same. When we scale the y value (ie, convert it from inch to feet), the correlation result stay the same

Question 2

- a. Yes, researcher could randomly assign participants to be in different group of amounts of time spent outside.
- b. We cannot come to this conclusion because it is from an observational study. There can be confounding factors contribute to the decrease in blood pressure (ie, diet, stress level, etc)
- c. Number of miles someone jogs each day could make someone go outside and expose to the nature, jogging also help reduces blood pressure => Confounding variable

Question 3

Quantitative variable: BCPM, GPA, VR, PS, WS, BS, MCAT, Apps Categorical variable: Sex

Question 4

- a.

- Response: reasoning scores
- explanatory variable: Sex

b.

- Response: AcceptStatus
- explanatory variable: Sex

c.

- Response: MCAT
- explanatory variable: GPA

d.

- Response: AcceptStatus
- explanatory variable: BCPM

Question 5

```
data = read.csv("C:/Users/caoqu/OneDrive/PC/UCI/STUDY/WINTER_25/DATA_210P_Statistical_Methods_I/data/Mc
head(data)
```

```
##      Accept Acceptance Sex BCPM  GPA VR PS WS BS MCAT Apps
## 1      D           0   F 3.59 3.62 11  9  9  9  38    5
## 2      A           1   M 3.75 3.84 12 13  8 12  45    3
## 3      A           1   F 3.24 3.23  9 10  5  9  33   19
## 4      A           1   F 3.74 3.69 12 11  7 10  40    5
## 5      A           1   F 3.53 3.38  9 11  4 11  35   11
## 6      A           1   M 3.59 3.72 10  9  7 10  36    5
```

a.

```
accept_df = data[data$Accept == "A",]
reject_df = data[data$Accept == "D",]

print("Five number summary for GPA for admitted students")
```

```
## [1] "Five number summary for GPA for admitted students"
```

```
summary(accept_df$GPA)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      3.140   3.545   3.715   3.693   3.888   3.970
```

```
print("Five number summary for GPA for rejected students")
```

```
## [1] "Five number summary for GPA for rejected students"
```

```
summary(reject_df$GPA)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      2.720   3.290   3.380   3.385   3.610   3.770
```

b.

- Mean GPA of accepted group is about 3.693, while mean GPA of rejected group is 3.385.
- Min accepted GPA of admitted student is 3.140 while max GPA of rejected student is 3.770 => GPA is not the only factor

Question 6

a.

```
model = lm(MCAT~GPA, data = data)
```

```
summary(model)
```

```
##
## Call:
## lm(formula = MCAT ~ GPA, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11.4148  -2.5168  -0.1519   2.6653   8.6616
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    3.923      6.922   0.567   0.573
## GPA            9.104      1.942   4.688 1.97e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.088 on 53 degrees of freedom
## Multiple R-squared:  0.2931, Adjusted R-squared:  0.2798
## F-statistic: 21.98 on 1 and 53 DF,  p-value: 1.969e-05
```

- Estimated Regression equation: $\widehat{MCAT} = 3.923 + 9.104 * GPA$

b.

$$SSE = \sum (y_i - \hat{y}_i)^2 = \sum (Y_i - (3.923 + 9.104 * X_i))^2$$

c.

- Slope: 9.104

Interpretation: For one unit increase in GPA, the MCAT score increase by 9.104 points

d.

- The slope is 3.923

Interpretation: When GPA = 0, the MCAT score is 3.923

This interpretation is not meaningful

e.

```
MCAT_30 = 3.923 + 9.104 * 3.0
```

```
MCAT_40 = 3.923 + 9.104 * 4.0
```

```
sprintf("Mcat score for 3.0 GPA: %f", MCAT_30)
```

```
## [1] "Mcat score for 3.0 GPA: 31.235000"
```

```
sprintf("Mcat score for 3.0 GPA: %f", MCAT_40)
```

```
## [1] "Mcat score for 3.0 GPA: 40.339000"
```

f. The difference is:

```
9.104*2
```

```
## [1] 18.208
```

g. No, since is an observational study, there are many other factors that could contribute in increase MCAT score other than GPA

Question 7

- Randomized experiments help negate the effect of confounder.