

**Exercise 1**

Consider a LIBOR market model for the evolution of the LIBOR rates

$$L_i := L(T_i, T_{i+1}), \quad i = 1, \dots, n-1,$$

for a given tenure structure  $T_0 = 0 < T_1 < \dots < T_n$ . An exchange option involving two LIBOR rates  $L(T_i, T_{i+1})$  and  $L(T_k, T_{k+1})$ , with  $0 < i < k < n$ , is the product paying

$$(L(T_i, T_{i+1}; T_i) - L(T_k, T_{k+1}; T_k))^+, \quad (1)$$

at time  $T_{k+1}$ . Write a class `MyExchangeOption` extending

```
net.finmath.montecarlo.interestrategy.products.AbstractLIBORMonteCarloProduct
```

whose method

```
getValue(double evaluationTime, TermStructureMonteCarloSimulationModel model)
```

returns the (discounted) payoff (1) as a `RandomVariable`. You can take the structure of the class from `MyDigitalCaplet` of last exercise handout.

**Exercise 2**

Write a `static` method, that can be added to the class

```
com.andreamazzon.LIBORMarketModelConstruction,
```

taking as inputs a double `correlationDecayParameter` and an object `oldLIBORSimulation` of type

```
net.finmath.montecarlo.interestrategy.LIBORModelMonteCarloSimulationModel,
```

and returning a `LIBORModelMonteCarloSimulationModel`. In particular, scope of this method is to return a clone of `oldLIBORSimulation`, changing its `LIBORCorrelationModel` (if it has any, if not you can just return an `Exception`) with a `LIBORCorrelationModelExponentialDecay` object whose correlation decay parameter is `correlationDecayParameter`.

**Hint:** for this exercise you have to find and use the appropriate methods of the Finmath library. Here are some steps for a *possible* solution, but you are of course free to proceed as you want.

- (a) Get the `TermStructureModel oldModel` object contained in `oldLIBORSimulation`;
- (b) get the `LIBORCovarianceModel oldCovarianceModel` object contained in `oldModel`;
- (c) construct a `LIBORCorrelationModel newCorrelationModel` with the constructor of the suitable class, by giving it `correlationDecayParameter` and other objects you can get from `oldCovarianceModel`;
- (d) use `newCorrelationModel` in order to construct an appropriate `HashMap`, that you can pass to the `getCloneWithModifiedData` method called by `oldCovarianceModel`;
- (e) pass the object obtained in this way to the `getCloneWithModifiedCovarianceModel` method, called by `oldModel`;
- (f) use the object got in the last step, together with the Brownian Motion that you can get from `oldLIBORSimulation`, to construct the new `LIBORMonteCarloSimulationFromLIBORModel` object as we saw in the last exercise session.

Note that some of these step you might have to downcast.

### Exercise 3

Consider again the product with payoff (1), when the underlying processes are taken from a LIBOR Market Model  $L_i := L(T_i, T_{i+1})$ ,  $1 \leq i \leq n-1$ , with

$$dL_i(t) = L_i(t)\sigma_i(t)dW_i(t), \quad 0 \leq t \leq T_i, \quad i = 0, \dots, n-1, \quad (2)$$

where  $d\langle W_i, W_j \rangle(t) = \rho_{i,j}(t)dt$ .

Write a test class whose main goal is to print the value of the option for two processes from (2), for different values of the decay correlation parameter  $\alpha > 0$  such that

$$\rho_{i,j}(t) = e^{-\alpha|T_i - T_j|}, \quad 0 < i, j < n.$$

In order to accomplish this you can:

- (a) construct an object `LIBORModelMonteCarloSimulationModel` with the `createLIBORMarketModel` method we have seen last time, for a given value of  $\alpha$  and some parameters of your choice, and pass it to the `getValue` method of the `MyExchangeOption`, together with the periods identifying the LIBORs you want;
- (b) then change the value of  $\alpha$  inside a `for` loop, and call again `getValue`. In this `for` loop, you don't have to create the `LIBORModelMonteCarloSimulationModel` object from scratch, but you can use the method of Exercise 2. This would save time.

Before looking at the results, try to guess what you expect: the price will increase or decrease with  $\alpha$ ?