

# Minimum XOR

There is a set of n nonnegative integers  $x_1, \ldots, x_n$  that you have to determine.

For determining it, you can make the following type of query: you give a nonnegative integer y and it is returned to you the value  $\min_{i=1,\dots,n} (x_i \oplus y)$ , where  $\oplus$  is the bitwise exclusive-or operation (XOR). You must find the values of the n numbers using at most 20000 queries.

$$\begin{array}{r}
11010 \\
\oplus 01110 \\
\hline
10100
\end{array}$$

# Input and output

This is an interactive problem. You must flush the output (cout << endl or cout << flush in C++, System.out.flush() in Java, stdout.flush() in Python).

The first line of the input contains an integer n, the number of elements of the set. You must read this value before making any query.

For making a query you must write a line in the format ? y, where y is an integer that must satisfy  $0 \le y < 2^{30}$ . Después making a query, you must read from the input an integer, the result. If you make an invalid query or exceed the query limit you will read -1, if your program reads -1 it must terminate immediately.

Once you have determined the *n* numbers, you must write a line with the format!  $x_1 \times x_2 \dots \times x_n$ , where  $x_1 < x_2 < \dots < x_n$  are the *n* integers of the set **in ascending order**. After writing this, your program must terminate.



# Sample

Input:

3			
1			
1			
0			
1			

#### Output:

```
? 1
? 2
? 3
? 4
! 0 3 5
```

Explaination: The hidden values are 0,3,5. The first line is n, the number of values. Then a query with y=1 is made: the interactor computes  $0\oplus 1=1,3\oplus 1=2,5\oplus 1=4$  and returns the smallest value, which is 1. Then for  $y=2,\ 0\oplus 2=2,3\oplus 2=1,5\oplus 2=7$  and 1 is returned. With  $y=3,\ 1\oplus 3=2,3\oplus 3=0,5\oplus 3=6$  and 0 is returned. With  $y=4,\ 1\oplus 4=5,3\oplus 4=7,5\oplus 4=1$  and 1 is returned. Finally, the elements of the set are given.

### Constraints

 $1 \le n \le 10000$ .

 $0 \le x_i < 2^{30}$ . The *n* values of  $x_i$  are distinct numbers.

You can make at most 20000 queries (giving the answer does not count as a query).

#### Subtasks

- 1. (7 points)  $x_i < 20000$ .
- 2. (13 points)  $x_i < 2^{15}$ .
- 3. (8 points) n = 2.
- 4. (20 points)  $n \le 300$ .
- 5. (12 points)  $n \le 600$ .
- 6. (20 points)  $n \le 5000$ .
- 7. (20 points) No additional constraints.