COMPSCI 402 Artificial Intelligence

Assignment 3 – MDP Total points: 8-point

- **Q1.** Pacman is using MDPs to maximize his expected utility. In each environment:
 - Pacman has the standard actions {North, East, South, West} unless blocked by an outer wall
 - There is a reward of 1 point when eating the dot (for example, in the grid below, R(C; South; F) = 1)
 - The game ends when the dot is eaten
- (a) Consider the following grid where there is a single food pellet in the bottom right corner (F). The discount factor is 0.5. There is no living reward. The states are simply the grid locations.

А	В	С
D	Е	F

(i) What is the optimal policy for each state? (1-point)

State	$\pi(state)$
Α	
В	
С	
D	
E	

(ii) What is the optimal value for the state of being in the upper left corner (A)? Reminder: the discount factor is 0.5. (1-point)

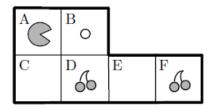
 $V^{*}(A) =$

k	V(A)	V(B)	V(C)	V(D)	V(E)	V(F)
0						
1						
2						
3						
4						

(iii) Using value iteration with the value of all states equal to zero at k=0, for which iteration k will $V_k(A) = V^*(A)$? (1-point)

k =

(b) Consider a new Pacman level that begins with cherries in locations D and F. Landing on a grid position with cherries is worth 5 points and then the cherries at that position **disappear**. There is still one dot, worth 1 point. The game still only ends when the dot is eaten.

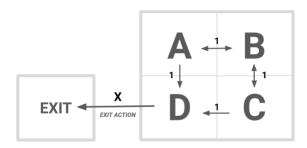


(i) With no discount ($\gamma = 1$) and a living reward of -1, what is the optimal policy for the states in this level's state space? (1-point)

State (hint: three-element tuple)	$\pi(state)$
Α,	
Α,	
Α,	
Α,	
С,	
С,	
С,	
С,	
D,	
D,	
Ε,	
Ε,	
Ε,	
Ε,	
F,	
F,	

(ii) With no discount ($\gamma=1$), what is the range of living reward values such that Pacman eats exactly one cherry when starting at position A? (1-point)

Q2. In this MDP, the available actions at **state A, B, C** are *LEFT, RIGHT, UP*, and *DOWN* unless there is a wall in that direction. The only action at **state D** is the *EXIT ACTION* and gives the agent a **reward of x**. The **reward for non-exit actions is always 1**.



(a) Let all actions be deterministic. Assume $\gamma = \frac{1}{2}$. Express the following in terms of x. (1-point)

$$V^*(D) =$$

$$V^*(C) =$$

$$V^*(A) =$$

$$V^{*}(B) =$$

(b) Let any non-exit action be successful with **probability**= $\frac{1}{2}$. Otherwise, the agent stays in the same state with **reward = 0**. The EXIT ACTION from the state D is still deterministic and will always succeed. Assume that $\gamma = \frac{1}{2}$. For which value of x does $Q^*(A;DOWN) = Q^*(A;RIGHT)$? Box your answer and justify/show your work. (1-point)

(c) We now add one more layer of complexity. Turns out that the reward function is not guaranteed to give a particular reward when the agent takes an action. Every time an agent transitions from one state to another, once the agent reaches the new state s', a fair 6-sided dice is rolled. If the dices lands with value s', the agent receives the reward s', and an array a