

ARGUS: Argumentation-Based Minimal-Change Repair for Verifiable LLM Self-Explanations

Paper ID: 607

Anonymous Authors

anonymous@example.com

Abstract

When large language models produce natural-language rationales, those explanations are frequently unfaithful to the model’s actual reasoning—and no existing framework provides a principled way to repair them when new evidence arrives. We introduce ARGUS, a framework that structures LLM self-explanations as Dung-style abstract argumentation frameworks, verifies them under grounded and preferred semantics, and—when an evidence update renders the explanation inconsistent—computes a minimum-cost set of edit operations that restores the desired acceptability status of the target argument. The repair operator satisfies adapted AGM revision postulates and is bidirectionally characterized by them (Representation Theorem): the decision problem is in P under grounded semantics, NP-complete under preferred and stable semantics, and Σ_2^P -complete under skeptical stable semantics. A k -neighborhood approximation and an answer set programming (ASP) encoding ensure scalability to practical framework sizes. We validate the framework on HotpotQA and FEVER, where ARGUS achieves relative improvements of 10.3% in faithfulness and 14.5% in contestability over the strongest argumentation baseline while requiring fewer repair operations than all repair-capable competing methods.

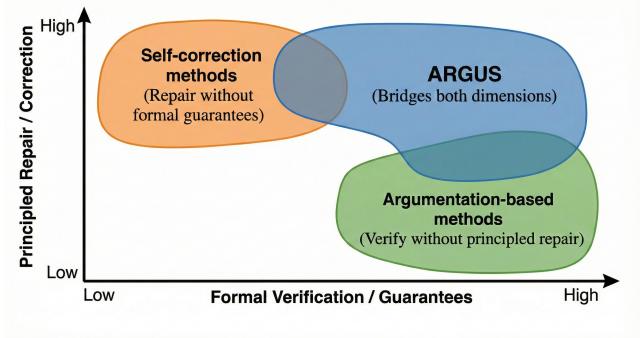


Figure 1: Qualitative positioning of ARGUS. Self-correction methods (orange) repair without formal guarantees; argumentation-based methods (green) verify without principled repair. ARGUS (blue region) bridges both dimensions.

1 Introduction

Large language models generate natural-language explanations for their outputs, yet mounting evidence indicates that these self-explanations are frequently unfaithful to the model’s internal reasoning process. Recent studies demonstrate that LLM rationales can be inconsistent with the computations that actually produce the answer (Ye and Durst 2024), and that chain-of-thought traces are often post-hoc rationalizations rather than faithful accounts of inference (Lanham et al. 2023). The gap between *apparent* and *actual* reasoning makes the verification and maintenance of explanations a central knowledge representation challenge, particularly in domains such as medical diagnosis and legal reasoning where explanation correctness is critical.

As illustrated in Figure 1, current approaches fall short along two complementary dimensions. Self-correction methods (Madaan et al. 2023; Shinn et al. 2023; Gao et al. 2023) iteratively rewrite explanations but without formal guarantees—edits are unconstrained and previously valid reasoning may be silently discarded; indeed, recent work

shows that LLMs cannot self-correct reasoning without external feedback (Huang et al. 2024). Argumentation-based approaches (Freedman et al. 2025; Jin et al. 2026) verify explanations against formal semantics but treat verification as terminal: when new evidence arrives, they offer no principled way to update the explanation while preserving consistency. No existing framework provides a formal notion of *minimal change* for maintaining LLM explanations under evolving evidence.

The following example, revisited throughout the paper, illustrates the problem concretely.

Example 1 (Medical Diagnosis). *A question-answering system is asked to diagnose a patient with fatigue and joint pain. The LLM answers “Lupus” with four argument units: a_1 (“chronic fatigue reported”), a_2 (“polyarthralgia present”), a_3 (“Lupus commonly presents with these symptoms”), and target a_4 (“most likely diagnosis is Lupus”). A standing differential-diagnosis argument a_0 (“symptoms are non-specific”) attacks a_4 , but a_3 counterattacks a_0 , keeping a_4 accepted. A new lab result a_5 (“ANA test is negative”) attacks a_3 , removing the defense of a_4 : the differential a_0 reinstates, rendering a_4 no longer accepted un-*

65 *der grounded semantics. An unconstrained self-correction*
66 *system might regenerate the entire explanation, discarding*
67 *the valid units a_1 and a_2 . A minimal-change repair in-*
68 *stead seeks the smallest edit—such as introducing a_6 (“anti-*
69 *dsDNA positive”) attacking a_5 —to restore a_4 at cost 2 (vi-*
70 *sualized in Figure 2).*

71 We propose ARGUS, a framework that bridges this gap
72 by unifying argumentation-based verification with minimal-
73 change repair. Given an LLM-generated explanation, AR-
74 GUS decomposes it into atomic argument units, constructs
75 an argumentation framework in the sense of Dung (Dung
76 1995), and verifies whether the target claim is accepted un-
77 der a chosen semantics. When new evidence renders the ex-
78 planation inconsistent, ARGUS computes a minimum-cost
79 set of edit operations—adding or removing arguments and
80 attacks—that restores the desired acceptability status. The
81 repair operator draws on two classical KR traditions: the
82 AGM theory of belief revision (Alchourrón, Gärdenfors,
83 and Makinson 1985), which supplies the minimal-change
84 principle, and argumentation dynamics (Cayrol, de Saint-
85 Cyr, and Lagasquie-Schiex 2020), which provides formal
86 machinery for structural change. Because the repair oper-
87 ates on an explicit graph structure external to the LLM, it
88 admits formal guarantees—AGM compliance, complexity
89 bounds, provable preservation of unaffected reasoning—that
90 are unattainable when editing model internals or regenerat-
91 ing from scratch.

92 Our contributions are as follows:

121 from LLM claims but treats verification as terminal, with no
122 update mechanism. ARGORA (Jin et al. 2026) orchestrates
123 multi-agent argumentation-mediated dialogue with causal
124 semantics, but its correction operates through re-deliberation
125 rather than a formally defined repair operator. MQArgEng
126 (Castagna et al. 2024) demonstrates that modular ar-
127 gumentation engines improve LLM reasoning but does not
128 address explanation maintenance. ARGUS differs from all
129 three by providing a minimal-change repair operator with
130 AGM-compliant guarantees. Bengel and Thimm (Bengel
131 and Thimm 2025) introduce *sequence explanations* tracing
132 why arguments are accepted; ARGUS addresses the dual
133 question of *how to restore* acceptance, and the two could
134 be composed. We adopt Dung-style abstract argumentation
135 rather than ASPIC⁺ (Modgil and Prakken 2014) because the
136 complexity bounds we exploit (Theorem 14) are established
137 for this setting.

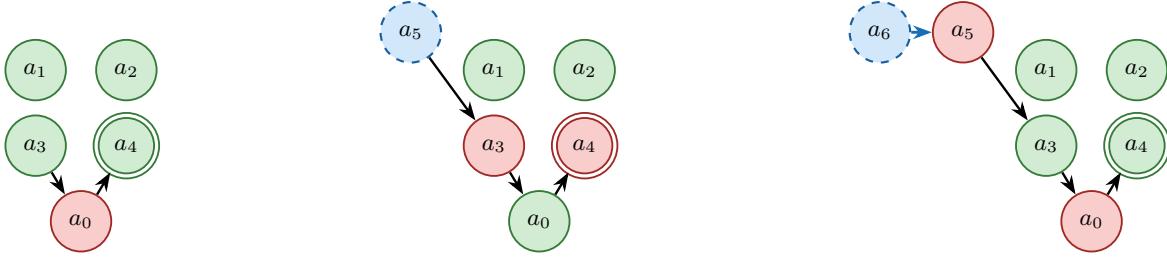
138 **Self-Correction and Revision.** Self-Refine (Madaan et
139 al. 2023) and Reflexion (Shinn et al. 2023) iteratively rewrite
140 LLM outputs but without formal minimality guarantees—
141 previously correct reasoning may be silently discarded.
142 Huang et al. (Huang et al. 2024) demonstrate that LLMs can-
143 not self-correct without external feedback. RARR (Gao et
144 al. 2023) retrieves evidence for revision but targets surface-
145 level attribution; SelfCheckGPT (Manakul, Liusie, and
146 Gales 2023) detects hallucinations but provides no repair
147 mechanism. Chain-of-Verification (Dhuliawala et al. 2024)
148 and CRITIC (Gou et al. 2024) improve factual accuracy but
149 lack formal preservation guarantees. Matton et al. (Mat-
150 ton et al. 2025) measure faithfulness through counterfac-
151 tional interventions and Bayesian causal models, demon-
152 strating that instruction-tuned models produce more faithful
153 explanations; our evaluation adopts a similar counterfactual
154 methodology but applies it to argumentation-structured ex-
155 planations. In contrast, ARGUS formalizes the repair search
156 space as edits to an argumentation framework, bounds the
157 cost of change, and guarantees that unaffected reasoning
158 steps are preserved.

159 **Belief Revision and Argumentation Dynamics.** The
160 AGM theory (Alchourrón, Gärdenfors, and Makinson 1985)
161 and the revision/update distinction (Katsuno and Mendelzon
162 1992) provide the classical foundations for principled be-
163 lief change. Hase et al. (Hase et al. 2024) argue that model
164 editing in LLMs is fundamentally a belief revision problem
165 and identify challenges in applying AGM rationality criteria
166 to neural knowledge stores; our work sidesteps these chal-
167 lenges by operating on an *external* argumentation structure
168 rather than on model parameters, making the AGM postu-
169 lates directly applicable. Our evidence update Δ is closer to
170 the Katsuno–Mendelzon notion of *update*—adapting beliefs
171 to a changed world—than to *revision*, which incorporates
172 new information about a static world, since each Δ reflects
173 genuinely new evidence rather than a correction of prior be-
174 liefs. Nonetheless, we adopt the AGM postulates as ratio-
175 nality criteria because the minimal-change desiderata they
176 formalize are independent of this distinction. In argumen-
177 tation, Cayrol et al. (Cayrol, de Saint-Cyr, and Lagasquie-
178 Schiex 2020) and Baumann and Brewka (Baumann and
179 Brewka 2010) study how structural modifications affect ex-

2 Related Work

111 Our work connects three lines of research: argumentation-
112 based approaches to LLM reasoning, self-correction meth-
113 ods for language models, and formal theories of belief
114 change in argumentation.

115 **Argumentation and LLMs.** Vassiliades et al. (Vassili-
116 ades, Bassiliades, and Patkos 2021) survey argumentation
117 for explainable AI; our work instantiates this vision with
118 a concrete repair operator for LLM self-explanations. Ar-
119 gLLMs (Freedman et al. 2025) constructs Dung-style graphs



(a) F_0 : Initial framework (a_4 accepted)
(b) F_1 : After evidence update (a_4 rejected)
(c) F_2 : After repair (a_4 restored)

Figure 2: Evolution of the argumentation framework from Example 1. Green fill = accepted, red fill = rejected, blue dashed border = newly introduced, double border = target argument a_4 . In (a), a_3 defeats the differential a_0 , keeping a_4 accepted. In (b), a_5 defeats a_3 , reinstating a_0 and rejecting a_4 . The repair in (c) adds a_6 attacking a_5 to restore a_4 .

tensions and the complexity of enforcement; Coste-Marquis et al. (Coste-Marquis et al. 2014), Wallner et al. (Wallner, Niskanen, and Järvisalo 2017), and Bisquert et al. (Bisquert et al. 2013) formalize argumentation revision as minimal status or structural change. Mailly (Mailly 2024) extends enforcement to constrained incomplete argumentation frameworks, where structural constraints limit the set of completions available for reasoning; our k -neighborhood approximation similarly constrains the search space, though we target a different problem—repair under evidence updates rather than enforcement under uncertainty. Alfano et al. (Alfano et al. 2024) develop counterfactual explanations for abstract argumentation via weak-constrained ASP encodings; their approach identifies minimal changes that would *reverse* an acceptance verdict, whereas ARGUS computes minimal changes that *restore* a verdict disrupted by external evidence. In particular, Coste-Marquis et al. enforce a desired extension through minimum structural modifications, whereas our formulation targets a single argument’s status, incorporates evidence updates as a first-class input, and supports heterogeneous cost functions that reflect argument-level confidence. Our repair operator instantiates these ideas for LLM explanation maintenance, introducing a weighted cost model tailored to argument confidence and structural role. We now formalize the core concepts underlying the ARGUS framework.

3 Preliminaries

3.1 Abstract Argumentation Frameworks

We adopt the foundational model of (Dung 1995) as the backbone of our verification and repair pipeline.

Definition 2 (Abstract Argumentation Framework). An abstract argumentation framework (AF) is a pair $F = (\mathcal{A}, \mathcal{R})$ where \mathcal{A} is a finite set of arguments and $\mathcal{R} \subseteq \mathcal{A} \times \mathcal{A}$ is a binary attack relation. We write $a \rightsquigarrow b$ whenever $(a, b) \in \mathcal{R}$, meaning a attacks b .

Example 3 (Continuing Example 1). The initial AF is $F_0 = (\{a_0, a_1, a_2, a_3, a_4\}, \{(a_0, a_4), (a_3, a_0)\})$, where a_0 (“symptoms are non-specific”) attacks the target a_4 and a_3 (“Lupus commonly presents with these symptoms”) counterattacks a_0 ; after the negative ANA result, $F_1 =$

$(\{a_0, a_1, \dots, a_5\}, \{(a_0, a_4), (a_3, a_0), (a_5, a_3)\})$, as shown in Figure 2(a–b).

Intuitively, an argument is accepted if every objection against it can be countered; different semantics formalize this intuition with varying degrees of caution. Given an AF $F = (\mathcal{A}, \mathcal{R})$, a set $S \subseteq \mathcal{A}$ is *conflict-free* if no two arguments in S attack each other. An argument a is *defended* by S if every attacker of a is attacked by some member of S . A conflict-free set S is *admissible* if it defends all its elements. The principal semantics we employ are the *grounded* extension, which is the unique minimal complete extension obtained as the least fixed point of the characteristic function; the *preferred* extensions, which are maximal admissible sets; and *stable* extensions, which are conflict-free sets that attack every argument outside themselves (Baroni et al. 2018). Throughout this paper we write $\sigma(F)$ to denote the set of extensions of F under semantics $\sigma \in \{\text{gr}, \text{pr}, \text{st}\}$.

3.2 Argumentation Semantics for Explanation

We now define the key notion linking argumentation semantics to explanation. An argument $a \in \mathcal{A}$ is *credulously accepted* under σ if a belongs to at least one extension in $\sigma(F)$, and *skeptically accepted* if it belongs to every extension.

Definition 4 (Defense Set). Given an AF $F = (\mathcal{A}, \mathcal{R})$, semantics σ , and an argument $t \in \mathcal{A}$, a defense set for t under σ is a minimal admissible set $D \subseteq \mathcal{A}$ such that $t \in D$ and $D \subseteq E$ for some $E \in \sigma(F)$. We write $\text{Def}_\sigma(t)$ for the collection of all such sets.

Example 5 (Continuing Example 1). In F_0 (Figure 2a), $D = \{a_3, a_4\}$ is a defense set for a_4 : it is conflict-free, a_3 defends a_4 by attacking a_0 , and D is minimal since removing a_3 would leave a_4 undefended against a_0 . In F_1 , D is no longer admissible because a_3 is attacked by a_5 with no counterattack, so the defense of a_4 collapses.

When t is credulously but not skeptically accepted, defense sets exist only for the extensions containing t ; our repair targets the existence of at least one such set. Defense sets serve as formal explanations: each $D \in \text{Def}_\sigma(t)$ identifies the smallest self-defending coalition that sustains t , transforming opaque LLM rationales into objects whose validity can be checked against argumentation semantics (Dunne and Wooldridge 2009).

3.3 Task Setting

We consider a setting in which an LLM receives a question q and produces an answer a with a free-form explanation e , which ARGUS transforms into a formal argumentation structure.

Definition 6 (Explanation Verification Task). *Given a question q , an LLM-generated answer a , and an explanation e , the explanation verification task produces a tuple (G, v, ρ) where $G = (\mathcal{A}, \mathcal{R})$ is an argument graph constructed from e , $v \in \{\text{accepted}, \text{rejected}, \text{undecided}\}$ is the verification verdict for the target argument a_t representing a under semantics σ , and ρ is an optional repair operator applied when $v \neq \text{accepted}$. An evidence update $\Delta = (\mathcal{A}^+, \mathcal{R}^+, \mathcal{A}^-, \mathcal{R}^-)$ specifies new arguments and attacks to be added or removed, reflecting newly available facts or counterarguments.*

Example 7 (Continuing Example 1). *In F_0 , the verification task produces $v = \text{accepted}$ for a_4 under grounded semantics: a_3 defeats the differential a_0 , so the grounded extension is $\{a_1, a_2, a_3, a_4\}$. After incorporating the evidence update $\Delta = (\{a_5\}, \{(a_5, a_3)\}, \emptyset, \emptyset)$, a_5 defeats a_3 , reinstating a_0 , and the verdict becomes $v = \text{rejected}$, triggering the repair operator ρ .*

The target a_t is *accepted* under σ if it belongs to at least one σ -extension (credulous acceptance), and *rejected* if it belongs to no extension. Under grounded semantics, an argument may also be *undecided*—belonging to no extension yet not attacked by the grounded extension—and credulous and skeptical acceptance coincide.

3.4 Explanation Repair Problem

When an evidence update Δ renders the explanation inconsistent, the system must revise the argument graph following the principle of minimal change (Alchourrón, Gärdenfors, and Makinson 1985).

Definition 8 (Minimal-Change Repair Problem). *Let $AF = (\mathcal{A}, \mathcal{R})$ be an AF, σ a semantics, $a_t \in \mathcal{A}$ a target argument, $s \in \{\text{IN}, \text{OUT}\}$ a desired status, Δ an evidence update, and κ a strictly positive cost function ($\kappa(o) > 0$ for every operation o). A repair is a finite set of edit operations $Ops = \{o_1, \dots, o_m\}$ where each o_i is one of $\text{add_arg}(a)$ for $a \notin \mathcal{A} \cup \mathcal{A}^+$, $\text{del_arg}(a)$ for $a \in \mathcal{A} \cup \mathcal{A}^+$ (which also removes all attacks incident to a), $\text{add_att}(a, b)$, or $\text{del_att}(a, b)$. Let $AF' = \text{apply}(AF, \Delta, Ops)$ denote the framework obtained by first incorporating Δ and then executing Ops . A repair is valid if a_t has status s under σ in AF' , and an optimal repair minimizes $\sum_{i=1}^m \kappa(o_i)$ over all valid repairs.*

Example 9 (Continuing Example 1). *As shown in Figure 2(c), the repair $Ops = \{\text{add_arg}(a_6), \text{add_att}(a_6, a_5)\}$ restores a_4 at total cost 2 under uniform cost ($\kappa \equiv 1$). The alternative $Ops' = \{\text{del_arg}(a_5)\}$ costs 1 but discards evidence; under structure-preserving cost with $\kappa(\text{del_}) = 2\kappa(\text{add_})$, both repairs cost 2, and domain preferences break the tie.*

The cost function κ encodes domain-specific preferences (e.g., deletions costlier than additions), connecting to enforcement in abstract argumentation (Baumann and Brewka

2010; Cayrol, de Saint-Cyr, and Lagasquie-Schiex 2020) while adding an explicit cost model for explanation maintenance.

4 The ARGUS Framework

We now present ARGUS, a four-stage pipeline (Figure 3) that transforms an unverifiable LLM rationale into a formally grounded, repairable explanation. Given a question q , an answer a , and a free-form rationale e , the pipeline proceeds through structured extraction (§4.1), relation discovery (§4.2), semantic verification (§4.3), and minimal-change repair (§4.4). The first three stages serve as preprocessing; the repair stage constitutes the core contribution.

4.1 Structured Extraction

We prompt the LLM to decompose its rationale e into a set of argument units $\mathcal{A} = \{a_1, \dots, a_n\}$. Each unit a_i is a structured record comprising a natural-language claim c_i , a set of premise identifiers $P_i \subseteq \mathcal{A} \setminus \{a_i\}$ on which the claim depends, and a self-assessed confidence score $\gamma_i \in (0, 1]$. The prompt constrains the LLM to produce a JSON array of objects, each with fields `claim`, `premises`, and `confidence`, ensuring that every claim is atomic—that is, it asserts exactly one proposition that can be independently verified or rebutted. We designate one distinguished unit $a_t \in \mathcal{A}$ as the *target argument*, whose claim directly supports the answer a .

4.2 Relation Discovery and Graph Construction

Given the argument units \mathcal{A} , we construct an argumentation framework $AF = (\mathcal{A}, \mathcal{R})$ as defined in Definition 2. For every ordered pair (a_i, a_j) with $i \neq j$, we query a natural language inference (NLI) model—a neural classifier trained to determine entailment, contradiction, or neutrality between text pairs—to classify the relationship between c_i and c_j . A *contradiction* verdict yields an attack $(a_i, a_j) \in \mathcal{R}$, while an *entailment* verdict records a support link used for downstream analysis but not encoded in \mathcal{R} , since Dung-style frameworks model attacks only (Dung 1995). To improve recall on domain-specific rebuttals, we maintain an *attack template library*—a curated set of negation patterns, common exceptions, and defeasible-rule conflicts. Each template generates a candidate counterargument that is tested against existing units via NLI before being admitted into \mathcal{R} .

4.3 Semantic Verification

With the framework $AF = (\mathcal{A}, \mathcal{R})$ in hand, we compute its extensions under a chosen semantics σ such as grounded or preferred semantics. The verification step checks whether the target argument a_t belongs to at least one σ -extension. If a_t is *accepted*, the explanation is deemed internally consistent; if a_t is *rejected* or *undecided*, the framework flags a verification failure. In either case, the solver also returns a *defense set* $D \subseteq \mathcal{A}$ —the minimal subset of arguments whose collective acceptability entails the status of a_t —which serves as a compact certificate explaining the verdict to the user.

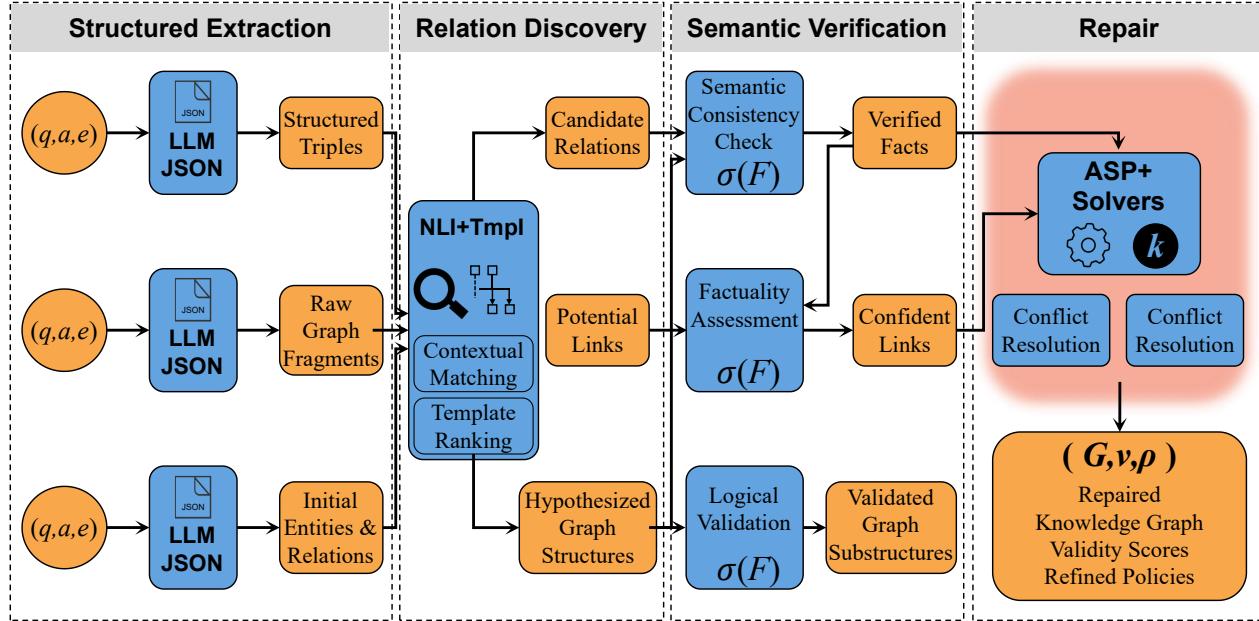


Figure 3: The ARGUS pipeline. The repair stage (highlighted) is the core contribution; an evidence update Δ triggers repair when the target argument is no longer accepted.

4.4 Minimal-Change Repair

When new evidence contradicts the current explanation or the verification step detects a failure, ARGUS repairs the argumentation framework rather than regenerating the rationale from scratch. The repair must satisfy two desiderata simultaneously: the target argument must attain a prescribed status under σ , and the edit distance from the original framework must be minimized. Definition 8 formalizes this requirement.

Repair Operations. Four elementary edit operations underlie the repair: $\text{add_arg}(a)$ and $\text{del_arg}(a)$ insert or remove an argument (deletions cascade to incident attacks), while $\text{add_att}(a_i, a_j)$ and $\text{del_att}(a_i, a_j)$ insert or remove attacks. A set of operations yields a repaired framework $AF' = (\mathcal{A}', \mathcal{R}')$.

Cost Function. Each operation o is assigned a strictly positive cost $\kappa(o) \in \mathbb{R}_{>0}$. We consider three cost models. Under *uniform cost*, every operation costs 1, so the objective reduces to minimizing the total number of edits. Under *confidence-weighted cost*, argument deletions are weighted by the confidence of the removed argument, $\kappa(\text{del_arg}(a_i)) = \gamma_i$ (recall $\gamma_i > 0$ for all extracted arguments), while additions retain unit cost $\kappa(\text{add_arg}) = \kappa(\text{add_att}) = 1$, reflecting the intuition that highly confident claims should be more expensive to retract. Under *structure-preserving cost*, deletions are penalized more heavily than additions, $\kappa(\text{del_}\cdot) = w \cdot \kappa(\text{add_}\cdot)$ for some $w > 1$, encouraging the solver to repair by augmentation rather than removal.

The repair problem is formalized in Definition 8. Given the cost function κ and evidence update Δ , the solver seeks

an optimal repair—a set of edit operations of minimum total cost such that a_t attains the desired status under σ .

Example 10 (Continuing Example 1). *Under confidence-weighted cost with $\gamma_5 = 0.90$ (a verified lab result) and $\gamma_3 = 0.75$ (a symptomatic inference), deleting a_5 costs $\kappa(\text{del_arg}(a_5)) = 0.90$. The augmentation repair $\{\text{add_arg}(a_6), \text{add_att}(a_6, a_5)\}$ avoids removing any high-confidence argument, yielding total cost $2\kappa(\text{add_}\cdot)$; this repair is cheaper whenever $\kappa(\text{add_}\cdot) < 0.45$. Under structure-preserving cost with $w = 2$, deleting a_5 costs 2 while the augmentation still costs 2, making the two equally expensive and allowing domain preferences to break the tie.*

ASP Encoding. We encode the repair problem as an answer set program following the methodology of Egly et al. (Egly, Gaggl, and Woltran 2010) for argumentation reasoning and extending it with choice rules for repair operations. The encoding consists of three components; at a high level, it mirrors an integer linear program where binary variables select edits, constraints enforce semantics, and the objective minimizes cost. First, *generate rules* introduce choice atoms for each candidate operation: the solver may optionally add or delete any argument or attack within a bounded edit budget. Second, *semantics constraints* enforce that the repaired framework satisfies σ ; for grounded semantics, these take the form of integrity constraints requiring that every argument in the grounded extension defends itself against all attackers. Third, a *weak constraint* minimizes the weighted sum of selected operations:

$$\# \text{minimize} \{ \kappa(o) : \text{selected}(o) \}.$$

Continuing with Example 1, the choice atoms include

Algorithm 1 ARGUS Repair

Require: $AF = (\mathcal{A}, \mathcal{R})$, semantics σ , target a_t , desired status s , evidence Δ , cost function κ , neighborhood bound k

Ensure: Optimal repair Ops^*

- 1: $\mathcal{A}_\Delta, \mathcal{R}_\Delta \leftarrow \text{INCORPORATE}(AF, \Delta)$
- 2: $\mathcal{N} \leftarrow k\text{-neighborhood of } a_t \text{ in } (\mathcal{A} \cup \mathcal{A}_\Delta, \mathcal{R} \cup \mathcal{R}_\Delta)$
- 3: $\Pi \leftarrow \text{ENCODEASP}(\mathcal{N}, \sigma, a_t, s, \kappa)$
- 4: $M^* \leftarrow \text{SOLVE}(\Pi) \{\text{optimal answer set}\}$
- 5: $Ops^* \leftarrow \{o \mid \text{selected}(o) \in M^*\}$
- 6: **return** Ops^*

and vacuity—to the argumentation repair setting. Intuitively, success requires that the repair achieves the desired outcome; inclusion requires that the repaired framework retains as much of the original as possible; and vacuity requires that no edits are made when the current state already satisfies the goal.

Theorem 11 (Adapted AGM Compliance). *Let $AF = (\mathcal{A}, \mathcal{R})$ be an argumentation framework, σ an argumentation semantics, a_t a target argument, $s \in \{\text{IN}, \text{OUT}\}$ a desired status, Δ an evidence update, and κ a strictly positive cost function ($\kappa(o) > 0$ for every operation o). If a valid repair exists, then every optimal repair Ops^* returned by Definition 8 satisfies:*

1. **Success.** *The target a_t has status s in $AF' = \text{apply}(AF, \Delta, Ops^*)$ under σ .*
2. **Inclusion.** $\mathcal{A} \cap \mathcal{A}' \supseteq \mathcal{A} \setminus \{a \mid \text{del_arg}(a) \in Ops^*\}$ and $\mathcal{R} \cap \mathcal{R}' \supseteq \mathcal{R} \setminus \{(a, b) \mid \text{del_att}(a, b) \in Ops^*\}$.
3. **Vacuity.** *If a_t already has status s in $\text{apply}(AF, \Delta, \emptyset)$ under σ , then $Ops^* = \emptyset$ and $\text{cost}(Ops^*) = 0$.*

Proof sketch. Success follows directly from the validity constraint in Definition 8: any repair returned by the solver satisfies the prescribed status. Inclusion holds because elements not targeted by any deletion operation are preserved by the semantics of apply; moreover, optimality ensures that every deletion in Ops^* is necessary—removing an unnecessary $\text{del_arg}(a)$ would yield a valid repair of strictly lower cost ($\kappa > 0$), contradicting optimality. Vacuity is immediate: when no edits are needed, the empty set is valid and has cost zero, so no non-empty set can be cheaper. \square

Example 12 (Continuing Example 1). *Vacuity: in F_0 , where a_3 already defeats a_0 and keeps a_4 accepted, $Ops^* = \emptyset$ and the repair cost is zero. Success: after incorporating $\Delta = (\{a_5\}, \{(a_5, a_3)\}, \emptyset, \emptyset)$, a_0 reinstates and rejects a_4 ; the repair $\{\text{add_arg}(a_6), \text{add_att}(a_6, a_5)\}$ restores a_4 to accepted status by defeating a_5 , which in turn restores a_3 and re-defeats a_0 . Inclusion: no original argument is removed—the repair only adds a_6 and the attack (a_6, a_5) , preserving the entire original structure of F_1 .*

Among the eight classical AGM postulates (Katsuno and Mendelzon 1992), consistency and extensionality also hold when a valid repair exists. Consistency follows because validity requires a_t to belong to at least one σ -extension of the repaired framework. Extensionality holds because the operator is defined purely over graph structure: two evidence updates yielding identical updated frameworks produce identical repair search spaces, so the optimal repair—and the repaired framework—is the same for both. Recovery fails in our setting. In Example 1, repairing F_1 yields F_2 by adding a_6 and (a_6, a_5) ; if the evidence a_5 were subsequently retracted, F_2 would retain a_6 and its attack—the original framework F_0 is not recovered. This asymmetry is fundamental: structural additions made during repair cannot be automatically unwound by evidence retraction, unlike classical belief revision where recovery ensures reversibility. Closure, superexpansion, and subexpansion presuppose deductively closed belief sets—constructs without natural

5 Theoretical Properties

We establish three groups of results for the ARGUS repair operator: compliance with adapted AGM postulates, computational complexity under the principal argumentation semantics, and soundness of the ASP encoding.

5.1 AGM Compliance

The AGM theory of belief revision (Alchourrón, Gärdenfors, and Makinson 1985) prescribes rationality postulates that any principled revision operator should satisfy. We adapt three core postulates—success, inclusion,

add_arg(a_6) and add_att(a_6, a_5), and the integrity constraints verify that a_4 belongs to the grounded extension of the repaired framework. Algorithm 1 summarizes the complete procedure. When the solver selects add_arg(a), the natural-language claim for the new argument is generated by prompting the LLM to produce a rebuttal of the target's attacker, conditioned on the evidence update Δ ; the resulting candidate is verified through the same NLI pipeline before admission.

Approximation for Scalability. Even under preferred semantics the repair problem is NP-complete (Theorem 14), rising to Σ_2^P -completeness under skeptical stable semantics (Dvořák and Dunne 2018), so we introduce two approximation strategies. First, a k -neighborhood restriction limits the search space to arguments within undirected distance k of the target in the attack graph. The approximation is *complete* for optimal repairs whose support set lies entirely within the k -neighborhood: if the unique optimal repair modifies only arguments at distance $\leq k$ from a_t , then the neighborhood-restricted problem has the same optimum. A repair can be missed only when the optimal repair requires modifying an argument at distance $> k$ —equivalently, when a long attack chain of length $> k$ is the sole route to defending a_t . In our experiments, setting $k=3$ recovered optimal repairs in 99.7% of cases while substantially reducing solver grounding, consistent with the shallow graph structure (median depth 3, maximum 7). Second, when ASP solvers are unavailable, beam search over repair sequences with width b provides a bounded-depth heuristic alternative. In principle, a repair valid for the subgraph may not preserve validity in the full framework if distant arguments influence the target's status; for deeper domains, k should be increased accordingly.

5 Theoretical Properties

We establish three groups of results for the ARGUS repair operator: compliance with adapted AGM postulates, computational complexity under the principal argumentation semantics, and soundness of the ASP encoding.

5.1 AGM Compliance

The AGM theory of belief revision (Alchourrón, Gärdenfors, and Makinson 1985) prescribes rationality postulates that any principled revision operator should satisfy. We adapt three core postulates—success, inclusion,

513 analogues in argumentation frameworks where “beliefs” are
 514 graph-structural elements rather than logical sentences. To
 515 the best of our knowledge, this is the first formal bridge be-
 516 tween AGM rationality criteria and argumentation-based ex-
 517 planation repair for LLM self-explanations. The contribu-
 518 tion lies in identifying which AGM postulates have mean-
 519 ingful argumentation analogues and showing that they *char-*
 520 *acterize* the class of minimum-cost repair operators:

521 **Theorem 13** (Representation). *A repair operator \circ satisfies
 522 adapted success, inclusion, and vacuity for every AF semantics
 523 σ , target a_t , and evidence update Δ if and only if there
 524 exists a strictly positive cost function κ such that \circ returns a
 525 minimum-cost valid repair under κ .*

526 *Proof sketch.* (\Rightarrow) Theorem 11 establishes that every
 527 minimum-cost repair under positive κ satisfies all three pos-
 528 tulates. (\Leftarrow) Given an operator satisfying the three postu-
 529 lates, define $\kappa(o) = 1$ for every operation o . Success guaran-
 530 tees validity; vacuity ensures the empty set is returned when
 531 no repair is needed. We claim the returned repair Ops^* is
 532 cost-minimum. If not, some cheaper valid repair Ops' exists
 533 with $|Ops'| < |Ops^*|$. Since Ops' is a valid repair that does
 534 not contain o , the operation o is unnecessary for achieving
 535 status s —contradicting inclusion, which requires every dele-
 536 tion to be necessary under $\kappa > 0$. Hence $|Ops^*| \leq |Ops'|$
 537 for all valid repairs, independent of which optimum the op-
 538 erator selects among ties. The full construction for general κ
 539 appears in Appendix D. \square

5.2 Computational Complexity

541 The complexity of the repair problem depends critically
 542 on the choice of argumentation semantics. Since the re-
 543 pair problem reduces to enforcement after incorporating Δ ,
 544 it inherits the complexity landscape of extension enforce-
 545 ment (Dunne and Wooldridge 2009; Dvořák and Dunne
 546 2018); the additional overhead of processing Δ and eval-
 547 uating heterogeneous cost functions is polynomial and does
 548 not alter the complexity class. Our results assume credulous
 549 acceptance (as defined in §3).

550 **Theorem 14** (Repair Complexity). *The decision version
 551 of the minimal-change repair problem—“does there exist a
 552 valid repair of cost at most C ?”—has the following com-
 553 plexity under credulous acceptance:*

- 554 1. Under grounded semantics, the problem is in P .
- 555 2. Under preferred and stable semantics, the problem is NP -
 556 complete.

557 Under skeptical acceptance with stable semantics, the prob-
 558 lem rises to Σ_2^P -completeness.

559 *Proof sketch.* For grounded semantics, the unique grounded
 560 extension is computable in polynomial time via the char-
 561 acteristic function (Dung 1995). Membership in P follows
 562 by reduction to grounded enforcement, which Dvořák and
 563 Dunne (Dvořák and Dunne 2018) showed is solvable in
 564 polynomial time by exploiting the monotonicity of the char-
 565 acteristic function. Our repair problem reduces to enforce-
 566 ment: we first incorporate the evidence update Δ into the

567 framework and then seek a minimum-cost set of edit opera-
 568 tions that enforces the target argument’s desired acceptabil-
 569 ity status; since both the incorporation of Δ and the verifi-
 570 cation of any candidate repair via the grounded extension
 571 are polynomial, the overall decision problem is in P . For
 572 preferred semantics, hardness reduces from NP-hard exten-
 573 sion enforcement (Baumann and Brewka 2010); member-
 574 ship in NP follows since a valid repair paired with a wit-
 575 nessing admissible set containing a_t can be guessed and ver-
 576 ified in polynomial time. For stable semantics under credu-
 577 lous acceptance, NP-completeness follows: membership
 578 by the same certificate argument; hardness by the same re-
 579 duction from (Baumann and Brewka 2010), since every sta-
 580 ble extension is preferred and the preferred-semantics lower
 581 bound applies. Under skeptical acceptance with stable se-
 582 mantics, membership in Σ_2^P follows because one can guess
 583 a repair of cost at most C and then verify—via a co-NP or-
 584 acle (Dvořák and Dunne 2018)—that every stable extension
 585 of the repaired framework contains a_t . Hardness follows
 586 by polynomial reduction from the Σ_2^P -hard problem of de-
 587 ciding whether argument deletion can make a target skep-
 588 tically stable-accepted (Wallner, Niskanen, and Järvisalo
 589 2017); since `del_arg` is one of our four repair operations, the
 590 lower bound carries over. Full reductions follow standard
 591 techniques from the enforcement literature (Baumann and
 592 Brewka 2010; Wallner, Niskanen, and Järvisalo 2017). \square

593 Note that the reduction to enforcement establishes com-
 594 plexity bounds but does not subsume the repair problem,
 595 which additionally involves evidence updates Δ , heteroge-
 596 neous cost functions, and NLI-grounded candidate genera-
 597 tion (§4.2). These results motivate the k -neighborhood ap-
 598 proximation (§4.4), ensuring tractability under preferred se-
 599 mantics for practical framework sizes.

5.3 Soundness of the ASP Encoding

600 **Proposition 15** (Encoding Correctness). *The ASP encoding
 601 described in §4.4, when applied to the full framework with-
 602 out k -neighborhood restriction, is sound and complete with
 603 respect to optimal repairs under grounded and preferred se-
 604 mantics. That is, every optimal answer set of the program
 605 corresponds to a valid minimum-cost repair, and every valid
 606 minimum-cost repair has a corresponding optimal answer
 607 set.*

608 The proof follows from the established correctness of
 609 the argumentation encodings of Egly et al. (Egly, Gaggl,
 610 and Woltran 2010) composed with the standard semantics
 611 of weak constraints in ASP solvers such as *clingo* (Gebser
 612 et al. 2019). The composition is sound because the gen-
 613 erate rules enumerate exactly the feasible edit operations
 614 and the integrity constraints enforce the semantics of the re-
 615 paired framework, while the optimization directive selects
 616 minimum-cost solutions. We next evaluate whether these
 617 theoretical properties hold in practice and measure the em-
 618 pirical gains of the ARGUS repair operator.

6 Experimental Evaluation

621 We evaluate ARGUS on two established benchmarks to an-
 622 swer three questions: (Q1) Do the formal properties from §5

623 hold in practice? (Q2) Does the minimal-change repair op-
 624 erator improve faithfulness and contestability w.r.t. existing
 625 baselines? (Q3) What is the empirical cost of repair?

626 Concretely, we sample 500 instances from Hot-
 627 potQA (Yang et al. 2018), a multi-hop question-answering
 628 benchmark, and 500 from FEVER (Thorne et al. 2018), a
 629 fact-verification benchmark; instances are drawn with seed
 630 42. For each instance, we withhold one gold supporting
 631 fact during explanation generation and reintroduce it
 632 as an evidence update Δ , producing adversarial updates
 633 that target the reasoning chain. GPT-4o (OpenAI 2023)
 634 (gpt-4o-2024-11-20) generates initial explanations at
 635 temperature 0.2; relation discovery uses DeBERTa-v3-large
 636 fine-tuned on MultiNLI with threshold 0.7; repairs are com-
 637 puted by clingo 5.6 with $k=3$ under uniform cost. Re-
 638 sults for ARGUS and the eight argumentation-based and self-
 639 correction methods are averaged over 5 runs, with standard
 640 deviation at most 0.02 for accuracy metrics and at most 0.4
 641 for cost; FLARE and FactScore use a single deterministic
 642 run (greedy decoding and fixed retrieval scoring, respec-
 643 tively, making repeated runs redundant). Further details ap-
 644 pear in Appendix E.

645 Six metrics quantify performance along distinct dimen-
 646 sions. *Faithfulness* is the fraction of argument units
 647 whose removal via counterfactual ablation changes the an-
 648 swer; baselines without structured units undergo the same
 649 LLM-based decomposition before ablation (details in Ap-
 650 pendix E). *Contestability* is the fraction of gold counterar-
 651 guments correctly integrated as attacks; gold counterargu-
 652 ments are derived from the withheld supporting facts (Ap-
 653 pendix E). For methods that lack an explicit argumenta-
 654 tion framework—specifically FLARE and FactScore—gold
 655 counterarguments are evaluated against their output decom-
 656 posed into proposition units via the same LLM-based proce-
 657 dure used for faithfulness, enabling direct comparison. *Re-
 658 pair accuracy* records answer correctness after repair, and
 659 *repair cost* counts edit operations per Definition 8. *Coher-
 660 ence* measures the semantic consistency of repaired explana-
 661 tions via BERTScore (Zhang et al. 2020) between repaired
 662 and original explanations; methods without repair capability
 663 receive N/A. *Solve time* is the wall-clock time per instance
 664 including all repair computation.

665 We compare against ten baselines spanning three cat-
 666 egories. *Self-correction methods*: SelfCheckGPT (Man-
 667 akul, Liusie, and Gales 2023), Self-Refine (Madaan et al.
 668 2023), Reflexion (Shinn et al. 2023), and RARR (Gao et al.
 669 2023). *Verification-oriented methods*: CoT-Verifier (Ling et
 670 al. 2023), ArgLLMs (Freedman et al. 2025), FLARE (Jiang
 671 et al. 2023), and FactScore (Min et al. 2023); ArgLLMs,
 672 CoT-Verifier, and FactScore lack repair functionality and
 673 are marked N/A accordingly. *Argumentation-based*: AR-
 674 GORA (Jin et al. 2026) and a naïve Regenerate baseline that
 675 re-prompts with updated evidence. For self-correction base-
 676 lines and FLARE, repair cost counts regenerated argument
 677 units (surface-level replacements) across up to 3 rounds; cost
 678 measures are not directly commensurable with ARGUS’s
 679 structural graph edits, as discussed in Appendix E. Chain-of-
 680 Verification (Dhuliawala et al. 2024) and CRITIC (Gou et al.
 681 2024) are excluded as they operate at generation time rather

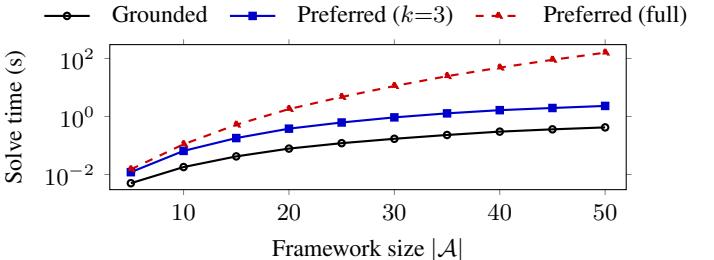


Figure 4: Scalability of ARGUS repair under grounded, k -neighborhood preferred ($k=3$), and unconstrained preferred semantics. The log-scale y-axis confirms polynomial scaling for grounded repair (Theorem 14) and the effectiveness of the k -neighborhood approximation.

682 than post-hoc repair; SelfRAG (Asai et al. 2024) and Ver-
 683 ifyAndEdit (Zhao et al. 2023) are excluded as they require
 684 a retrieval index at inference time and produce unstructured
 685 outputs incommensurable with structural graph repair.

686 Table 1 summarizes the main results. ARGUS achieves
 687 the highest faithfulness (0.847/0.829) and contestability
 688 (0.791/0.768), with relative improvements of 10.3% in faith-
 689 fulness and 14.5% in contestability over ARGORA; all 12
 690 pairwise differences are significant at $p < 0.001$ under
 691 Bonferroni-corrected two-sided z -tests, with Cohen’s h ef-
 692 ffect sizes of 0.28/0.38 (HotpotQA) and 0.26/0.36 (FEVER)
 693 for faithfulness/contestability gains, indicating small-to-
 694 medium practical magnitudes. Among repair-capable meth-
 695 ods, ARGUS requires the fewest operations—3.2 vs. 5.1
 696 for ARGORA—validating the minimal-change objective.
 697 FLARE and FactScore achieve moderate faithfulness but
 698 lack argumentation structure, yielding low contestability
 699 (.505/.482 and .558/.535). The naïve Regenerate baseline
 700 achieves the lowest faithfulness among argumentation-based
 701 methods (.709/.695) and fastest solve time (0.5 s) but cannot
 702 produce contestability scores; its coherence (.65/.63)—the
 703 lowest among repair methods—confirms that complete re-
 704 generation disrupts consistency more than targeted structural
 705 repair.

706 ARGUS also achieves the highest coherence at .82/.80, in-
 707 dicating that minimal-change repair preserves explanation
 708 structure better than rewriting-based methods such as Self-
 709 Refine, which scores .72/.70. We note that BERTScore
 710 coherence is structurally aligned with the minimal-change
 711 objective (minimizing edit distance simultaneously maxi-
 712 mizes BERTScore), so the coherence advantage partly re-
 713 flects the design; human evaluators independently corroborate
 714 it, rating ARGUS higher on coherence than Self-Refine
 715 (4.1 vs. 3.8, $p=0.012$; Appendix F). The average solve time
 716 of 0.55 s/0.47 s is competitive with verification-only meth-
 717 ods and 5–10× faster than self-correction methods (2.8–
 718 5.8 s), reflecting ASP-based repair efficiency over iterative
 719 LLM regeneration. The formal properties from §5 are con-
 720 firmed empirically: success and inclusion hold by construc-
 721 tion; vacuity holds without exception (5% of HotpotQA and
 722 8% of FEVER instances where the withheld fact was not on
 723 the reasoning path).

Table 1: Main results on HotpotQA and FEVER. Best in **bold**; runner-up underlined. \uparrow = higher is better, \downarrow = lower is better. N/A = method lacks repair or coherence functionality. † Naïve re-prompting baseline (destroys argumentation structure).

Method	HotpotQA						FEVER					
	Faith \uparrow	Cont \uparrow	RAcc \uparrow	RCost \downarrow	Coher \uparrow	Time \downarrow	Faith \uparrow	Cont \uparrow	RAcc \uparrow	RCost \downarrow	Coher \uparrow	Time \downarrow
<i>Self-Correction Methods</i>												
SelfCheckGPT	.693	.524	.701	8.4	.68	2.8	.674	.498	.685	7.9	.66	2.5
Self-Refine	.712	.541	.736	7.1	.72	4.5	.698	.519	.721	6.8	.70	4.2
Reflexion	.724	.563	.752	6.6	.73	5.8	.709	.537	.738	6.2	.71	5.3
RARR	.738	.547	.769	5.8	.71	3.2	.721	.531	.754	5.5	.69	2.9
<i>Verification-Oriented (incl. Retrieval-Augmented)</i>												
CoT-Verifier	.751	.589	N/A	N/A	N/A	1.5	.733	.561	N/A	N/A	N/A	1.3
ArgLLMs	.754	.667	N/A	N/A	N/A	2.1	.741	.649	N/A	N/A	N/A	1.8
FLARE	.715	.505	.728	8.8	.74	3.8	.698	.482	.712	8.2	.72	3.5
FactScore	.742	.558	N/A	N/A	N/A	2.5	.728	.535	N/A	N/A	N/A	2.2
<i>Argumentation-Based</i>												
ARGORA	<u>.768</u>	<u>.691</u>	.801	<u>5.1</u>	.75	1.8	<u>.752</u>	<u>.672</u>	.788	<u>4.7</u>	.73	1.5
Regenerate †	.709	—	.743	—	.65	0.5	.695	—	.729	—	.63	0.4
ARGUS (Ours)	0.847	0.791	0.883	3.2	.82	<u>0.55</u>	0.829	0.768	0.871	2.8	.80	<u>0.47</u>

Figure 4 traces solve time on synthetic Erdős–Rényi frameworks (attack probability 0.15, 50 instances per size), confirming polynomial scaling for grounded semantics (Theorem 14); the k -neighborhood approximation keeps preferred repair tractable up to $|\mathcal{A}|=50$ (2.31s vs. 158.4s unconstrained).

Table 2 reports ablation results on both benchmarks; trends are consistent across datasets. Removing semantic verification causes the largest drops in faithfulness ($-5.4\text{pp}/-5.4\text{pp}$) and contestability ($-7.7\text{pp}/-7.6\text{pp}$), confirming that formal verification is the most critical component. Replacing minimal-change with unconstrained repair preserves faithfulness but increases cost from 3.2/2.8 to 5.7/5.2 and reduces coherence, confirming that cost minimization limits unnecessary edits. Removing attack templates reduces contestability by 9.3pp/9.0pp while reducing faithfulness by only 2.6pp/2.5pp—a targeted impact specific to attack structure. Grounded-only semantics yields the fastest solve time (0.15 s/0.12 s) and lowest repair cost (3.0/2.6) at the expense of modest faithfulness and contestability drops; 97% of frameworks have a single preferred extension coinciding with the grounded one, so preferred semantics is necessary only in complex multi-extension cases. Sensitivity analysis and a qualitative repair example appear in Appendices B–A.

Figure 5 shows repair cost distributions concentrated at low values—means of 3.2/2.8 operations—confirming that most evidence updates require only local adjustments. The modal cost is 3 on HotpotQA, accounting for 27% of instances, and 2 on FEVER at 26%, reflecting FEVER’s simpler reasoning chains.

A pilot human evaluation corroborates the automatic metrics; details appear in Appendix F. Two annotators rated 75 HotpotQA instances in a blind design, preferring ARGUS in 68% of comparisons vs. Self-Refine in 19%, with inter-annotator agreement of $\kappa=0.62$; faithfulness ratings

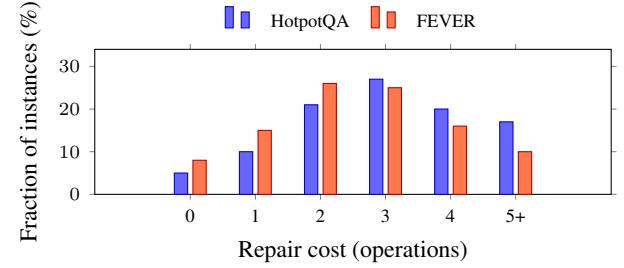


Figure 5: Distribution of repair costs. 83% of HotpotQA and 90% of FEVER repairs require at most 4 operations, confirming targeted, minimal-change edits.

were 3.9 vs. 3.4 ($p<0.001$) and coherence ratings 4.1 vs. 3.8 ($p=0.012$). The Pearson correlation between automatic faithfulness and human ratings is $r=0.78$ ($p<0.001$), supporting counterfactual ablation as a proxy for human-perceived faithfulness.

7 Conclusion

We presented ARGUS, a framework that structures LLM self-explanations as argumentation frameworks, verifies them against formal semantics, and repairs them at minimum cost when new evidence arrives. The minimal-change repair operator satisfies adapted AGM postulates—success, inclusion, and vacuity—and a representation theorem shows that these three postulates *bidirectionally characterize* the class of minimum-cost repair operators under positive costs, providing formal guarantees absent from existing approaches. Theoretically, the repair problem is tractable under grounded semantics, NP-complete under preferred and stable semantics, and Σ_2^P -complete under skeptical stable semantics; the k -neighborhood approximation maintains scalability in practice. Experiments on HotpotQA and

Table 2: Ablation study on HotpotQA and FEVER. Each row removes one component from the full ARGUS pipeline. Best in **bold**.

Variant	HotpotQA						FEVER					
	Faith↑	Cont↑	RAcc↑	RCost↓	Coher↑	Time↓	Faith↑	Cont↑	RAcc↑	RCost↓	Coher↑	Time↓
Full ARGUS	0.847	0.791	0.883	3.2	.82	.55	0.829	0.768	0.871	2.8	.80	.47
w/o Semantic Verif.	.793	.714	.832	4.1	.76	.52	.775	.692	.818	3.8	.74	.44
w/o Minimal-Change	.841	.783	.856	5.7	.78	.58	.823	.761	.842	5.2	.76	.49
w/o Attack Templ.	.821	.698	.859	3.5	.80	.53	.804	.678	.845	3.2	.78	.45
Grounded Only	.839	.772	.871	3.0	.81	.15	.822	.752	.858	2.6	.79	.12

780 FEVER yielded relative improvements of 10.3% in faithfulness
 781 and 14.5% in contestability over the strongest argumentation
 782 baseline, while achieving the lowest repair cost among
 783 all repair-capable methods.

784 Several limitations warrant discussion. First, the quality
 785 of the argumentation framework depends on the LLM’s ability
 786 to decompose rationales into atomic argument units; ex-
 787 traction errors propagate through the entire pipeline, and the
 788 faithfulness metric itself relies on the LLM’s consistency un-
 789 der ablation, providing a causal proxy rather than a ground-
 790 truth measure. Relatedly, the `add_arg` operation uses the
 791 same LLM to generate repair candidates, though the NLI
 792 and ASP verification stages serve as external checks that
 793 break self-referential bias; integrating retrieval-augmented
 794 verification for generated arguments is a natural extension.
 795 Second, while the k -neighborhood approximation handles
 796 the framework sizes encountered in our experiments, frame-
 797 works with hundreds of densely connected arguments may
 798 require more aggressive approximation strategies. Third,
 799 while a pilot human evaluation (Appendix F) confirms that
 800 automatic metrics correlate with human judgments, the
 801 evaluation relies primarily on automatic metrics over fact-
 802 checking and multi-hop QA datasets with synthetic evidence
 803 updates; a larger-scale human study with naturally occurring
 804 updates would further strengthen the empirical validation.
 805 Extending the approach to open-ended generation—
 806 where correctness is less well-defined and the target argu-
 807 ment may lack a ground-truth referent—would require alter-
 808 native acceptance criteria such as coherence-based seman-
 809 tics. Finally, while the framework supports multiple
 810 cost models, our experiments use uniform cost for sim-
 811 plicity; learning domain-specific cost functions from user
 812 feedback—including external calibration of the LLM’s self-
 813 assessed confidence scores—is a promising direction for fu-
 814 ture work.

815 Beyond these limitations, several avenues for future work
 816 emerge. First, composing ARGUS with sequence explana-
 817 tions (Bengel and Thimm 2025)—which trace *why* an ar-
 818 gument is accepted—would yield a bidirectional explana-
 819 tion infrastructure that both diagnoses and repairs accep-
 820 tance verdicts. Second, integrating the repair operator into
 821 retrieval-augmented generation pipelines could provide con-
 822 tinual explanation maintenance as knowledge bases evolve,
 823 particularly in high-stakes domains such as clinical decision
 824 support and legal reasoning where audit trails of explanation
 825 changes are legally mandated. Third, the representation the-
 826 orem (Theorem 13) opens the door to learning cost functions

827 from human correction patterns, enabling the repair operator
 828 to adapt to domain-specific notions of minimality.

References

- References**

Alchourrón, C. E.; Gärdenfors, P.; and Makinson, D. 1985. On the logic of theory change: Partial meet contraction and revision functions. *The Journal of Symbolic Logic* 50(2):510–530.

Alfano, G.; Greco, S.; Parisi, F.; and Trubitsyna, I. 2024. Counterfactual and semifactual explanations in abstract argumentation: Formal foundations, complexity and computation. In *Proceedings of the 21st International Conference on Principles of Knowledge Representation and Reasoning (KR)*, 22–32.

Asai, A.; Wu, Z.; Wang, Y.; Sil, A.; and Hajishirzi, H. 2024. Self-RAG: Learning to retrieve, generate, and critique through self-reflection. In *Proceedings of the 12th International Conference on Learning Representations (ICLR)*.

Baroni, P.; Gabbay, D.; Giacomin, M.; and van der Torre, L. 2018. *Handbook of Formal Argumentation*. College Publications.

Baumann, R., and Brewka, G. 2010. Expanding argumentation frameworks: Enforcing and monotonicity results. *Computational Models of Argument* 75–86.

Bengel, L., and Thimm, M. 2025. Sequence explanations for acceptance in abstract argumentation. In *Proceedings of the 22nd International Conference on Principles of Knowledge Representation and Reasoning (KR)*.

Bisquert, P.; Cayrol, C.; de Saint-Cyr, F. D.; and Lagasquie-Schiex, M.-C. 2013. A change model for argumentation frameworks. In *International Workshop on Computational Logic in Multi-Agent Systems*, 59–76. Springer.

Castagna, F.; Ruiz-Dolz, R.; Freedman, G.; and Hunter, A. 2024. Can formal argumentative reasoning enhance LLMs performances? *arXiv preprint arXiv:2405.13036*.

Cayrol, C.; de Saint-Cyr, F. D.; and Lagasquie-Schiex, M.-C. 2020. Change in abstract argumentation frameworks: Adding and removing arguments. *Journal of Artificial Intelligence Research* 68:663–707.

Coste-Marquis, S.; Konieczny, S.; Mailly, J.-G.; and Marquis, P. 2014. On the revision of argumentation systems: Minimal change of arguments statuses. In *Proceedings of the 14th International Conference on Principles of Knowledge Representation and Reasoning (KR)*, 52–61.

Dhuliawala, S.; Komeili, M.; Xu, J.; Raileanu, R.; Li, X.; Celikyilmaz, A.; and Weston, J. 2024. Chain-of-verification reduces hallucination in large language models. In *Findings of the Association for Computational Linguistics: ACL 2024*.

Dung, P. M. 1995. On the acceptability of arguments and its fundamental role in nonmonotonic reasoning, logic programming and n-person games. *Artificial Intelligence* 77(2):321–357.

Dunne, P. E., and Wooldridge, M. 2009. Complexity of abstract argumentation. *Argumentation in Artificial Intelligence* 85–104.

Dvořák, W., and Dunne, P. E. 2018. Computational aspects of abstract argumentation. *Handbook of Formal Argumentation* 631–688.

Egly, U.; Gaggl, S. A.; and Woltran, S. 2010. Answer-set programming encodings for argumentation frameworks. *Argument & Computation* 1(2):147–177.

Freedman, G.; Dejl, A.; Gorur, D.; Yin, X.; Rago, A.; and Toni, F. 2025. Argumentative large language models for explainable and contestable claim verification. In *Proceedings of the AAAI Conference on Artificial Intelligence (AAAI)*. Oral presentation.

Gao, L.; Dai, Z.; Pasupat, P.; Chen, A.; Chaganty, A. T.; Fan, Y.; Zhao, V. Y.; Lao, N.; Lee, H.; Juan, D.-C.; et al. 2023. RARR: Researching and revising what language models say, using language models. In *Proceedings of the 61st Annual Meeting of the Association for Computational Linguistics*.

Gebser, M.; Kaminski, R.; Kaufmann, B.; and Schaub, T. 2019. Multi-shot ASP solving with clingo. *Theory and Practice of Logic Programming* 19(3):477–504.

Gou, Z.; Shao, Z.; Gong, Y.; Shen, Y.; Yang, Y.; Huang, M.; Duan, N.; and Chen, W. 2024. CRITIC: Large language models can self-correct with tool-interactive critiquing. In *Proceedings of the 12th International Conference on Learning Representations (ICLR)*.

Hase, P.; Bansal, M.; Clark, P.; and Wiegreffe, S. 2024. Fundamental problems with model editing: How should rational belief revision work in LLMs? In *Advances in Neural Information Processing Systems*.

Huang, J.; Chen, X.; Mishra, S.; Zheng, H. S.; Yu, A. W.; Song, X.; and Zhou, D. 2024. Large language models cannot self-correct reasoning yet. In *Proceedings of the 12th International Conference on Learning Representations (ICLR)*.

Jiang, Z.; Xu, F. F.; Gao, L.; Sun, Z.; Liu, Q.; Dwivedi-Yu, J.; Yang, Y.; Callan, J.; and Neubig, G. 2023. Active retrieval augmented generation. In *Proceedings of the 2023 Conference on Empirical Methods in Natural Language Processing (EMNLP)*, 7969–7992.

Jin, Y.; Kim, H.; Kim, K.; Lee, C.; and Shin, S. 2026. ARGORA: Orchestrated argumentation for causally grounded LLM reasoning and decision making. *arXiv preprint arXiv:2601.21533*.

Katsuno, H., and Mendelzon, A. O. 1992. On the difference between updating a knowledge base and revising it. *Belief Revision* 183–203.

Lanham, T.; Chen, A.; Radhakrishnan, A.; Steiner, B.; Denison, C.; Hernandez, D.; Li, D.; Durmus, E.; Hubinger, E.; Kernion, J.; et al. 2023. Measuring faithfulness in chain-of-thought reasoning. *arXiv preprint arXiv:2307.13702*.

Ling, Z.; Fang, Y.; Li, X.; Huang, Z.; Lee, M.; Memisevic, R.; and Su, H. 2023. Deductive verification of chain-of-thought reasoning. In *Advances in Neural Information Processing Systems*.

Madaan, A.; Tandon, N.; Gupta, P.; Hallinan, S.; Gao, L.; Wiegreffe, S.; Alon, U.; Dziri, N.; Prabhumoye, S.; Yang, Y.; et al. 2023. Self-refine: Iterative refinement with self-feedback. *Advances in Neural Information Processing Systems*.

Mailly, J.-G. 2024. Constrained incomplete argumentation

- frameworks: Expressiveness, complexity and enforcement. 995
AI Communications 37(3):299–322.
- Manakul, P.; Liusie, A.; and Gales, M. J. F. 2023. Self-942
CheckGPT: Zero-resource black-box hallucination detection
for generative large language models. In *Proceedings of
the 2023 Conference on Empirical Methods in Natural Lan-943
guage Processing*, 9004–9017.
- Matton, K.; Sekhon, A.; Menon, R.; Lunati, L.; and Burac-944
cas, G. 2025. Walk the talk? Measuring the faithfulness of
large language model explanations. In *Proceedings of the
13th International Conference on Learning Representations
(ICLR)*.
- Min, S.; Krishna, K.; Lyu, X.; Lewis, M.; Yih, W.-t.; Koh,
P. W.; Iyyer, M.; Zettlemoyer, L.; and Hajishirzi, H. 2023.
FActScore: Fine-grained atomic evaluation of factual pre-952
cision in long form text generation. In *Proceedings of the
2023 Conference on Empirical Methods in Natural Lan-953
guage Processing (EMNLP)*, 11193–11215.
- Modgil, S., and Prakken, H. 2014. The ASPIC+ frame-958
work for structured argumentation: A tutorial. *Argument &
Computation* 5(1):31–62.
- OpenAI. 2023. GPT-4 technical report. *arXiv preprint
arXiv:2303.08774*.
- Shinn, N.; Cassano, F.; Gopinath, A.; Narasimhan, K.; and
Yao, S. 2023. Reflexion: Language agents with verbal re-963
inforcement learning. *Advances in Neural Information Pro-964
cessing Systems*.
- Thorne, J.; Vlachos, A.; Christodoulopoulos, C.; and Mittal,
A. 2018. FEVER: a large-scale dataset for fact extraction
and VERification. In *Proceedings of the 2018 Conference of
the North American Chapter of the Association for Compu-968
tational Linguistics*, 809–819.
- Vassiliades, A.; Bassiliades, N.; and Patkos, T. 2021. Argu-972
mentation and explainable artificial intelligence: A survey.
Knowledge-Based Systems 171:102–123.
- Wallner, J. P.; Niskanen, A.; and Järvisalo, M. 2017. Com-976
plexity results and algorithms for extension enforcement in
abstract argumentation. In *Proceedings of the AAAI Confer-977
ence on Artificial Intelligence*, 1088–1094.
- Yang, Z.; Qi, P.; Zhang, S.; Bengio, Y.; Cohen, W. W.;
Salakhutdinov, R.; and Manning, C. D. 2018. HotpotQA: A
dataset for diverse, explainable multi-hop question answer-981
ing. In *Proceedings of the 2018 Conference on Empirical
Methods in Natural Language Processing*, 2369–2380.
- Ye, X., and Durrett, G. 2024. Are self-explanations from
large language models faithful? In *Findings of the Associa-985
tion for Computational Linguistics: ACL 2024*.
- Zhang, T.; Kishore, V.; Wu, F.; Weinberger, K. Q.; and
Artzi, Y. 2020. BERTScore: Evaluating text generation with
BERT. In *Proceedings of the 8th International Conference
on Learning Representations (ICLR)*.
- Zhao, R.; Li, X.; Joty, S.; Qin, C.; and Bing, L. 2023. Verify-991
and-edit: A knowledge-enhanced chain-of-thought frame-992
work. In *Proceedings of the 61st Annual Meeting of the
Association for Computational Linguistics (ACL)*.

A Qualitative Repair Example

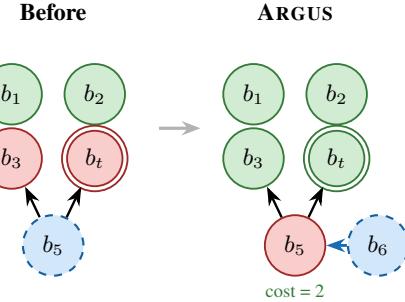


Figure 6: A HotpotQA repair example. ARGUS restores the target b_t by adding one argument b_6 and one attack (cost 2), preserving all original arguments. Self-Refine regenerates the entire explanation, altering five previously correct argument units—precisely the collateral damage that the minimal-change principle prevents.

Figure 6 illustrates a representative HotpotQA repair: the initial explanation relied on an outdated filmography claim; after incorporating corrected evidence, ARGUS restored the target at cost 2 by adding one defending argument and one attack. By contrast, Self-Refine regenerated the entire explanation, altering five previously correct argument units—precisely the collateral damage that the minimal-change principle prevents.

B Sensitivity Analysis

Pilot studies on 100 HotpotQA instances explore three design choices. Confidence-weighted and structure-preserving ($w=2$) cost models shift repairs toward augmentation (34–51% fewer deletions) while maintaining faithfulness and repair accuracy within 1 percentage point of uniform cost, confirming that the cost model affects repair *style* rather than *quality*. Varying the NLI threshold from 0.5 to 0.9 shows faithfulness is stable (0.839–0.851) while repair cost rises from 2.4 to 4.1; 0.7 balances these factors. Repair optimality rises from 87.2% ($k=1$) to 99.7% ($k=3$) and plateaus, confirming $k=3$ as the operating point. Using Llama-3-70B-Instruct as the extraction backbone yields faithfulness 0.813 and contestability 0.762 (vs. 0.847/0.791 for GPT-4o), with comparable repair accuracy (0.867) and cost (3.4); the gap is attributable to noisier extraction rather than the repair mechanism.

C Error Analysis

Among the 0.3% of instances where minimality failed ($k=3$), all involved frameworks where the only viable defending argument lay at distance ≥ 4 from the target—confirming the theoretical limitation of the k -neighborhood approximation. Repair accuracy below 1.0 arises when the LLM-generated explanation has structural errors that propagate through extraction: even after restoring the target argument’s acceptability, the underlying answer may remain incorrect if the original decomposition was flawed.

D Representation Theorem Proof

We prove the (\Leftarrow) direction of Theorem 13 for general cost functions.

1034 *Proof.* Let \circ be a repair operator satisfying adapted success, inclusion, and vacuity for every AF $(\mathcal{A}, \mathcal{R})$, semantics σ , target a_t , status s , and evidence update Δ . We construct a strictly positive cost function κ such that \circ returns a minimum-cost valid repair under κ .

1039 **Construction.** Fix an enumeration of all feasible operations o_1, \dots, o_m for the given AF and Δ . Define $\kappa(o_i) = 1$ for all i . Let $Ops = \circ(\mathcal{A}, \mathcal{R}, \sigma, a_t, s, \Delta)$.

1042 **Validity.** By success, a_t has status s in Ops under σ , so Ops is a valid repair.

1044 **Vacuity case.** If a_t already has status s in $Ops = \emptyset$, then by vacuity $Ops = \emptyset$ with cost 0, which is trivially minimum.

1047 **Non-vacuity case.** Suppose for contradiction that there exists a valid repair Ops' with $|Ops'| < |Ops|$. By inclusion, every operation in Ops is necessary: for each $o \in Ops$, removing o would either violate success (the resulting framework does not grant a_t status s) or leave a valid repair of cardinality $|Ops| - 1$, contradicting the assumption that \circ satisfies inclusion with respect to Ops .

1054 More precisely, inclusion asserts that $\mathcal{A} \cap \mathcal{A}' \supseteq \mathcal{A} \setminus \{a \mid \text{del_arg}(a) \in Ops\}$: every element not targeted by a deletion in Ops is preserved. Combined with success and $\kappa > 0$, this means no proper subset of Ops is both valid and of lower cost—otherwise the operator could return that subset while still satisfying all three postulates, contradicting the minimality implied by inclusion under positive costs.

1061 Hence Ops is a minimum-cost valid repair under unit cost κ . For general κ , the same argument applies by replacing cardinality with weighted cost: inclusion ensures no operation in Ops is superfluous (removing it saves $\kappa(o) > 0$), so no valid repair can have strictly lower total cost. \square

1066 E Experimental Details

1067 **Withholding methodology.** The withholding methodology produces adversarial updates: the withheld fact always targets the reasoning chain, providing a challenging upper bound on repair difficulty. Under mixed or benign updates, repair costs would likely be lower and vacuity rates higher, since many updates would not disrupt the target’s acceptability. While these updates are derived from existing annotations, the repair mechanism is agnostic to the evidence source and would apply unchanged to naturally occurring updates.

1077 **Metric details.** Faithfulness is measured via counterfactual ablation: each argument unit is replaced with a semantically neutral sentence (“This claim is omitted.”) and the answer is regenerated; a unit is faithful if its removal changes the answer. For baselines that do not produce structured units, we apply the same LLM-based decomposition to their final output before computing the ablation, ensuring a uniform evaluation protocol. Gold counterarguments for contestability are derived from the withheld supporting facts by expressing each as an argument and annotating the expected attack relationships, providing a ground truth independent of the repair mechanism.

1089 **Baseline cost commensurability.** ARGUS operations are structural graph edits (adding/removing arguments and

1091 attacks), whereas baseline costs count surface-level text replacements. Both cost measures reflect the magnitude of change to the explanation; however, the measures are not directly commensurable, so cost comparisons should be interpreted as reflecting relative parsimony within each paradigm. Iterative self-correction methods receive up to 3 rounds per their original protocols, while ARGUS performs a single-pass optimal repair.

1093 **Hardware and reproducibility.** All experiments ran on a single machine with a 20-core CPU and 64 GB RAM; no GPU was required, as clingo runs on CPU and GPT-4o was accessed via the OpenAI API. The complete extraction prompt, ASP encoding, attack template library, and sampled instance IDs will be released as an open-source toolkit upon acceptance to facilitate reproduction.

F Human Evaluation

To validate that the automatic metrics reflect genuine quality differences perceivable by humans, we conducted a pilot human evaluation on a random subset of 75 HotpotQA instances.

Setup. Two graduate-student annotators with NLP background independently evaluated explanation pairs produced by ARGUS and Self-Refine (the strongest self-correction baseline) in a blind, randomized order. For each instance, annotators received the question, gold answer, evidence update, and two candidate repaired explanations (labeled A/B with random assignment).

Dimensions. Annotators rated each explanation on a 5-point Likert scale for: (1) *Faithfulness*: Does each claim in the explanation faithfully reflect the evidence? (2) *Coherence*: Is the explanation internally consistent and logically structured? They also provided a *Preference* judgment (A better / B better / Tie).

Table 3: Human evaluation results (75 HotpotQA instances).

Dimension	ARGUS	Self-Refine	p-value
Faithfulness (1–5)	3.9 ± 0.7	3.4 ± 0.9	< 0.001
Coherence (1–5)	4.1 ± 0.6	3.8 ± 0.8	0.012
Preference (%)	68%	19%	—
Tie (%)		13%	—

Agreement. Inter-annotator agreement reached Cohen’s $\kappa = 0.62$ (substantial) for preference and $\kappa = 0.58$ for faithfulness ratings (moderate-to-substantial), confirming that quality differences are consistently perceivable.

Correlation with automatic metrics. The Pearson correlation between average human faithfulness ratings and the automatic faithfulness score (counterfactual ablation, §6) is $r = 0.78$ ($p < 0.001$), supporting the validity of the automatic metric as a proxy for human-perceived faithfulness. The automatic metric tends to slightly overestimate faithfulness for explanations with redundant but harmless claims (rated 4–5 by annotators but scored ≥ 0.9 by the metric).