The Theory & Practice of Concurrent Programming

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1 SYNCHRONISATION PARADIGMS 2

1 Synchronisation Paradigms

1.1 Properties in Asynchronous computation

- 1. Safety
 - Nothing bad happens ever
 - If it is violated, it is done by a finite computation
- 2. Liveness
 - Something good happens eventually
 - Cannot be violated by a finite computation

1.2 Problems in Asynchronous computation

- 1. Mutual Exclusion (Safety)
 - cannot be solved by transient communication or interrupts
 - can be solved by shared variables that can be read or written
- 2. No Deadlock (Liveness): Some event A eventually happens.

1.3 Protocols in Asynchronous computation

- 1. Flag Protocol (from B's perspective):
 - Raise flag
 - While A's flag is up
 - Lower flag
 - Wait for A's flag to go down
 - Raise flag
 - Do something
 - Lower flag
- 2. Producer/Consumer:
 - For A(producer), while flag is up wait. So when flag becomes down, do something, then raise the flag.
 - For B(consumer), while flag is down, wait. So when flag becomes up, do something, then put down the flag.
- 3. Readers/Writers:

- Each thread i has size[i] counter. Only it increments or decrements.
- To get object's size, a thread reads a "snapshot" of all counters.
- This eliminates the bottleneck of "having exclusive access to the common counter".

1.4 Performance Measurement

Amdahl's law:

Speedup =
$$\frac{1\text{-thread execution time}}{n\text{-thread execution time}} = \frac{1}{1 - p + \frac{p}{n}}$$

where p is the fraction of the algorithm having parallel execution, and n is the number of threads.

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2 Concurrent Semantics

2.1 Notation

• x, y, z, \ldots shared memory locations

• a, b, c, \ldots private registers

• E, E_1, \ldots expressions over values (integers) and registers

• a := x read from location x into register a

• x := a write contents of register a to location x

• a := E assignment: compute E and write it to a

2.2 ConWhile concurrent programming language

 $\begin{array}{lll} B \in \operatorname{Bool} & ::= & \operatorname{true} \, | \, \operatorname{false} \, | \, \ldots \\ E \in \operatorname{Exp} & ::= & \ldots \, | \, E + E \, | \, \ldots \\ C \in \operatorname{Com} & ::= & a := E & \operatorname{assignment} \\ & | \, a := x & \operatorname{(memory) read} \\ & | \, x := a & \operatorname{(memory) write} \\ & | \, a := \operatorname{CAS}(x, E, E) \, | \, \operatorname{FAA}(x, E) & \operatorname{(memory) RMWs} \\ & | \, \operatorname{skip} \, | \, C; \, \, C \, | \, \operatorname{while} \, B \, \operatorname{do} \, C \\ & | \, \operatorname{if} \, B \, \operatorname{then} \, C \, \operatorname{else} \, C, \\ & | \, \operatorname{mfence} & \operatorname{memory fence} \, (\operatorname{TSO} \, \operatorname{only}) \end{array}$

where FAA (fetchAndAdd) is considered weak RMW because it enables synchronisation between two threads only, whereas CAS (compareAndSet) is considered strong RMW because it enables synchronisation among an arbitrary number of threads.

2.3 Sequential Consistency (SC)

Also called <u>Interleaving Semantics</u>. The instructions of each thread are executed in order. <u>Instructions of different threads interleave arbitrarily.</u>

• We model ConWhile concurrent program as a map from thread identifiers $(\tau \in \text{Tid})$ to sequential commands:

$$P \in \text{Prog} \triangleq \text{Tid} \to \text{Com}.$$

• We use || notation for concurrent programs and write

$$C_1 \parallel C_2 \parallel \ldots \parallel C_n$$

for the n-threaded program P with

$$dom(P) = \{\tau_1, \dots, \tau_n\}$$

and $P(\tau_i) = C_i \text{ for } i \in \{1, ..., n\}.$

• For instance, we write $dom(P_{sb}) = \{\tau_1, \tau_2\}$, with $P_{sb}(\tau_1) = x := 1; a := y;$ and $P_{sb}(\tau_2) = y := 1; b := x;$, therefore

$$P_{\rm sb} \triangleq x := 1; a := y; \parallel y := 1; b := x;$$

• We model the shared memory as a map from locations to values:

$$M \in \text{Mem} \triangleq \text{Loc} \rightarrow \text{Val}$$
,

where Val denotes the set of all values, including integer and Boolean values.

• We define store as a map from registers to values:

$$s \in \text{Store} \triangleq \text{Reg} \rightarrow \text{Val}.$$

• We define store map associating each thread with its private store:

$$S \in \mathrm{SMap} \triangleq \mathrm{Tid} \to \mathrm{Store}.$$

- An \underline{SC} configuration is a triple, (P, S, M), comprising a program P to be executed, the store map S, and the shared memory M.
- The program transitions describe the steps in program executions.
- The <u>storage transitions</u> describe how instructions interact with the storage (memory) system.
- An SC transition label, $l \in Lab$, may be:
 - the *empty* label ϵ to denote a silent transition
 - a read label (R, x, v) to denote reading value v from memory location x
 - a write label (W, x, v) to denote writing value v to memory location x
 - a successful RMW label (RMW, x, v_0, v_n) to denote updating the value of location x to v_n when the old value of x is v_0

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- a failed RMW label (RMW, x, v_0, \perp) to denote a failed CAS instruction where the old value of x does not match v_0 .
- Assume that store s has the mapping for all Boolean expressions B and program expressions E.
- SC Sequential Transitions (Familiar Cases):

$$\frac{C_1, s \xrightarrow{l}_c C_1', s'}{C_1; C_2, s \xrightarrow{l}_c C_1'; C_2, s'} \qquad \overline{\mathtt{skip}; C, s \xrightarrow{\epsilon}_c C, s}$$

$$\underline{s(B) = \mathtt{true}} \qquad \underline{s(B) = \mathtt{false}}$$

$$\underline{if \, B \, \mathtt{then} \, C_1 \, \mathtt{else} \, C_2, s \xrightarrow{\epsilon}_c C_1, s} \qquad \overline{if \, B \, \mathtt{then} \, C_1 \, \mathtt{else} \, C_2, s \xrightarrow{\epsilon}_c C_2, s}$$

while
$$B$$
 do $C, s \xrightarrow{\epsilon}_c$ if B then $(C;$ while B do $C)$ else skip, s
$$\frac{s(E) = v \qquad s' = s[a \mapsto v]}{a := E, s \xrightarrow{\epsilon}_c \text{ skip}, s'}$$

• SC Sequential Transitions (New Cases):

$$x := a \qquad \frac{s(a) = v}{x := a, s \xrightarrow{(\mathbf{W}, x, v)}_{c} \operatorname{skip}, s}$$

$$a := x \qquad \frac{s' = s[a \mapsto v]}{a := x, s \xrightarrow{(\mathbf{R}, x, v)}_{c} \operatorname{skip}, s'}$$

$$FAA(x, E) \qquad \frac{s(E) = v \quad v_n = v_0 + v}{FAA(x, E), s \xrightarrow{(\mathbf{RMW}, x, v_0, v_n)}_{c} \operatorname{skip}, s}$$

$$CAS(x, E_0, E_n) \text{ (success)} \qquad \frac{s(E_0) = v_0 \quad s(E_n) = v_n \quad s' = s[a \mapsto 1]}{a := \operatorname{CAS}(x, E_0, E_n), s \xrightarrow{(\mathbf{RMW}, x, v_0, v_n)}_{c} \operatorname{skip}, s'}$$

$$\frac{s(E_0) = v_0 \quad v \neq v_0 \quad s' = s[a \mapsto 0]}{a := \operatorname{CAS}(x, E_0, E_n), s \xrightarrow{(\mathbf{RMW}, x, v_1, \bot)}_{c} \operatorname{skip}, s'}$$

$$c \operatorname{Skip}, s'$$

• SC (Concurrent) Program Transitions:

$$\frac{P(\tau) = C \quad S(\tau) = s \quad C, s \xrightarrow{l}_{c} C', s' \quad P' = P[\tau \mapsto C'] \quad S' = S[\tau \mapsto s']}{P, S \xrightarrow{\tau:l}_{p} P', S'}$$

• SC Storage Transitions (of the form $M \xrightarrow{\tau:l}_m M'$):

$$\begin{array}{ll} \operatorname{Read} & \frac{M(x) = v}{M \xrightarrow{\tau: (\mathbf{R}, x, v)}_m M} \\ \operatorname{Write} & \frac{M' = M[x \mapsto v]}{M \xrightarrow{\tau: (\mathbf{W}, x, v)}_m M'} \\ \operatorname{RMW}, x, v_0, v_n & \frac{M(x) = v_0 \quad M' = M[x \mapsto v_n]}{M \xrightarrow{\tau: (\operatorname{RMW}, x, v_0, v_n)}_m M'} \\ \operatorname{RMW}, x, v, \bot & \frac{M(x) = v}{M \xrightarrow{\tau: (\operatorname{RMW}, x, v, \bot)}_m M'} \end{array}$$

• SC Operational Semantics:

silent transition
$$\frac{P, S \xrightarrow{\tau \cdot \epsilon}_{p} P', S'}{P, S, M \to P', S', M}$$
both program and storage systems take the same transition
$$\frac{P, S \xrightarrow{\tau \cdot \epsilon}_{p} P', S'}{P, S, M \to P', S', M'}$$

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- We write \rightarrow^* for the reflexive, transitive closure of \rightarrow .
- SC Traces
 - The initial memory, $M_0 \triangleq \lambda x.0$.
 - The initial store, $s_0 \triangleq \lambda a.0$.
 - The initial store map, $S_0 \triangleq \lambda \tau . s_0$.
 - The terminated program, $P_{\text{skip}} \triangleq \lambda \tau.\text{skip}$.
 - Given a program P, an ${\bf SC\text{-}trace}$ of P is an evaluation path s.t.

$$P, S_0, M_0 \rightarrow^* P_{\mathtt{skip}}, S, M$$

where the pair (S, M) denotes an **SC-outcome**.

• SC is **neither** deterministic **nor** confluent.

2.4 Total Store Ordering (TSO)

TSO = SC + write-read reordering. This allows the weak Store Buffering (SB) behaviour. We can stop the reordering by using memory fences or RMWs, which can impede performance.

• In addition to the concurrent program, shared memory, store, and store map defined in the SC, we have an addition buffer associating each thread, modelled as a FIFO sequence of (delayed) write label:

$$b \in \mathrm{Buff} \triangleq \mathrm{Seq} \, \langle \mathrm{WLab} \rangle \qquad \mathrm{WLab} \triangleq \big\{ (\mathrm{W}, x, v) \, | \, x \in \mathrm{Loc} \, \land \, v \in \mathrm{Val} \big\} \, .$$

That is, a buffer entry (W, x, v) denotes a delayed write on x with value v.

• We define buffer map associating each thread with its private buffer:

$$B \in \mathrm{BMap} \triangleq \mathrm{Tid} \to \mathrm{Buff}.$$

- An TSO configuration is a quadruple, (P, S, M, B), comprising the program P to be executed, the store map S, the shared memory M and the buffer map B.
- A TSO transition label, $l \in Lab$, may be:
 - an SC label, namely ϵ , (R, x, v), (W, x, v), (RMW, x, v_0, v_n) , (RMW, x, v_0, \perp)
 - a memory fence label MF for executing an mfence.
- TSO Sequential Transition (New case):

$$\begin{array}{ccc} \texttt{mfence} & & & & \\ & & & \\ & & \texttt{mfence}, s & \xrightarrow{\texttt{MF}}_c \texttt{skip}, s \end{array}$$

- TSO Program Transitions: the same as SC Program Transition.
- TSO Storage Transitions (of the form $M, B \xrightarrow{\tau:l}_m M', B'$):

$$\frac{B(\tau) = b \quad \text{get}(\mathbf{M}, b, x) = v}{M, B \xrightarrow{\tau:(\mathbf{R}, x, v)}_{m} M, B}, \text{ where }$$

Read

$$\gcd(M, b, x) \triangleq \begin{cases}
v & \text{if } \exists b_1, b_2 \text{ s.t. } b = b_1.(W, x, v).b_2 \\
& \land \neg \exists v' \text{ s.t. } (W, x, v') \in b_2 \\
M(x) & \text{otherwise}
\end{cases}$$
where the pair (S, M) denotes a **TSO-outco**

• TSO is also **neither** deterministic **nor** confluent.

Write
$$\frac{B(\tau) = b \qquad b' = b.(\mathbf{W}, x, v) \qquad B' = B[\tau \mapsto b']}{M, B \xrightarrow{\tau:(\mathbf{W}, x, v)}_{m} M, B'}$$

$$\text{Memory Fence} \qquad \frac{B(\tau) = \emptyset}{M, B \xrightarrow{\tau: \texttt{MF}}_{c} M, B}$$

$$\begin{array}{ll} \text{RMW}, x, v_0, v_n & \frac{B(\tau) = \emptyset \quad M(x) = v_0 \quad M' = M[x \mapsto v_n]}{M, B \xrightarrow{\tau: (\text{RMW}, x, v_0, v_n)}_{m} M', B} \\ \\ \text{RMW}, x, v, \bot & \frac{B(\tau) = \emptyset \quad M(x) = v}{M, B \xrightarrow{\tau: (\text{RMW}, x, v, \bot)}_{m} M, B} \\ \\ \text{unbuffer} & \frac{B(\tau) = (\text{W}, x, v).b \quad M' = M[x \mapsto v] \quad B' = B[\tau \mapsto b]}{M, B \xrightarrow{\tau: \epsilon}_{m} M', B'} \end{array}$$

• TSO Operational Semantics:

silent transition in program
$$\frac{P,S \xrightarrow{\tau \cdot \epsilon}_{p} P', S'}{P,S,M,B \to P',S',M,B}$$
silent transition in storage system
$$\frac{M,B \xrightarrow{\tau \cdot \epsilon}_{m} M',B'}{P,S,M,B \to P,S,M',B'}$$
both program and storage system take the same transition
$$\frac{P,S \xrightarrow{\tau \cdot \epsilon}_{p} P',S' M,B \xrightarrow{\tau \cdot \epsilon}_{m} M',B'}{P,S,M,B \to P',S',M',B'}$$

- We write \rightarrow^* for the reflexive, transitive closure of \rightarrow , the same as the SC's.
- TSO Traces
 - In addition to the initial memory, initial store, initial store map, and the terminated program defined in SC, we have the initial buffer map, $B_0 \triangleq \lambda \tau.\emptyset.$
 - Given a program P, the initial TSO-configuration of P is (P, S_0, M_0, B_0) .
 - Given a program P, a **TSO-trace** of P is an evaluation path s.t.

$$P, S_0, M_0, B_0 \rightarrow^* P_{\mathtt{skip}}, S, M, B_0$$

where the pair (S, M) denotes a **TSO-outcome**.

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3 Linearization

3.1 Notation

- A q.enq(x) Invocation: \langle thread \rangle \langle object \rangle \langle method \rangle (\langle arguments \rangle)
- A q:void Response: \langle thread \rangle \langle object \rangle: \langle result \rangle
- H Sequence of invocations and responses, which looks like:

```
A q.enq(3)
A q:void
A q.enq(5)

H = B p.enq(4)
B p:void
B q.deq()
B q:3
```

3.2 Definitions

- Invocation and response match if thread and object names agree
- Object Projections:

• Thread Projections:

- An invocation is <u>pending</u> if it has no matching response. It may or may not have taken effect.
- A complete subhistory is a history where pending invocations are discarded.
- A <u>sequential history</u> is one whose invocations are always *immediately* followed by their respective responses.
- A <u>well-formed</u> history is one whose per-thread projections are sequential.
- Equivalent histories are those which have the same threads and their perthread projections are the same.
- A sequential specification is some way of telling whether a single-thread, single-object history, is legal.
- A sequential history H is <u>legal</u> if for every object x, H|x is in the sequential specification for x.
- A method call <u>precedes</u> another if its response event precedes the other's invocation event.
 - Given history H, method executions m_0, m_1 in H, we say

$$m_0 \rightarrow_H m_1$$

if m_0 precedes m_1 .

- The above relation is a partial order. It is <u>total</u> order if H is sequential.

• History H is <u>linearizable</u> if

- it can be extended to a *complete* history G
- G is equivalent to a legal sequential history S, where $\rightarrow_{\mathbf{G}} \subseteq \rightarrow_{\mathbf{S}}$.
- Remarks on linearizability:
 - For pending invocations which took effect, keep them, and discard the rest.
 - \rightarrow_H stands for the set of all precedence relations in history H.
 - Focus on <u>total</u>(defined in every state) method.
 - Partial methods are equivalent to thread blocking, and blocking is unrelated to synchronisation.
 - We can identify "linearization points" to help check if executions are linearizable. The point

- * is between invocation and response events
- * correspond to the effect of the call
- * "justify" the whole execution

• Composability Theorem:

History H is linearizable $\iff \forall$ object x, H|x is linearizable.

- History H is sequentially consistent (SC) if
 - it can be extended to a *complete* history G
 - G is equivalent to a legal sequential history S, where $\rightarrow_{\mathbf{G}} \subseteq \rightarrow_{\mathbf{S}}$.
- Remarks on SC:
 - Cannot re-order operations done by the same thread
 - Can re-order non-overlapping operations done by different threads
 - SC is too strong for hardware architecture, yet too weak for software specification.
 - SC is useful for abstracting software *implementation*.
- (non-examinable) Progress conditions (from least ideal to most ideal):
 - Deadlock-free: some thread trying to acquire the lock eventually succeeds.
 - Starvation-free: *every* thread trying to acquire the lock eventually succeeds.
 - Lock-free: $some\ {\it thread}\ {\it calling}\ a\ {\it method}\ eventually\ returns.$
 - Wait-free: every thread calling a method eventually returns.

4 Concurrency in C++

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4.1 Threads and Locks

```
4.1.1 std::thread
#include <thread>
#include <functional> // Provides std::ref
// approach 1
void Foo(int by_value, std::string& by_reference) { ... }
std::string world = "World";
std::thread t1(Foo, 1, std::ref(world));
// approach 2
int y, x = 3;
std::thread t2([x, &y]() -> void {
   y = x * 42;
});
t1.join();
t2.join();
4.1.2 std::mutex
#include <mutex>
std::mutex mutex_;
mutex_.lock();
mutex_.unlock();
4.1.3 std::scoped_lock<std::mutex>
class ScopedLock {
public:
   explicit ScopedLock(std::mutex &mutex) : mutex_(mutex) {
       mutex_.lock();
   ~ScopedLock() {
       mutex_.unlock();
private:
```

```
std::mutex &mutex_;
};
4.1.4 std::unique_lock<std::mutex>
  • constructed with one mutex
  • locks mutex on construction (default), or deferred locking:
    std::unique_lock<std::mutex> lock(mutex_, std::defer_lock);
  • allows unlocking and relocking
  • unlocks mutex on destruction if still held
  • supports transfer of ownership to a distinct unique owner via std::move.
4.1.5 std::condition_variable
#include <condition_variable>
std::condition_variable condition_;
condition_.notify_one();
condition_.notify_all();
std::unique_lock<std::mutex> lock(mutex_);
/* Assuming that the thread has locked the mutex:
 * 1. return if predicate holds (continue executing code after wait())
 * 2. release lock
 * 3. block until another thread signals (via notify_one or norify_all)
 * 4. acquire lock, then return to step 1
condition_.wait(lock, [...]() -> bool {
   return ...;
}):
      Atomics
4.2
       Operations on std::atomic<T>
```

- store(x): store value x of type T
- load(): yields value of type T
- exchange(x): store x and return old value
- compare_exchange_strong(expected, desired):

- Success: old value is expected, store desired, return true
- <u>Failure</u>: old value not expected, store old value to expected, return false

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• compare_exchange_weak(expected, desired): the same as the previous operation, except that it allows to fail spuriously, i.e. fail even if old value is expected.

4.2.2 (RMW) Operations on std::atomic<integral_type>

- fetch_add(x): replace the value with (value + x), return old value.
- fetch_sub(x): similar
- fetch_and(x): similar
- fetch_or(x): similar
- fetch_xor(x): similar

4.2.3 Memory ordering

- Atomics are sequentially consistent by default.
- Relaxed memory order only guarantee sequential consistency per location.
- Acquire semantics prevents memory reordering of the read-acquire with any read or write operation that <u>follows</u> it in program order, i.e. all memory operations after read-acquire happen after read-acquire.
- Release semantics prevents memory reordering of the write-release with any read or write operation that <u>precedes</u> it in program order. i.e. all memory operations before write-release happen before write-release.
- In fact, acquiring a lock implies acquire semantics, releasing a lock implies release semantics!
- Please refer to this for detailed explanation and discussion on acquire-release semantics.
- various atomics semantics:

- std::memory_order_seq_cst

- std::memory_order_relaxed

- std::memory_order_release

```
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```

```
- std::memory_order_acquire
                                                                                             _mm_pause();
      - std::memory_order_acq_rel
                                                                                     } while (lock_bit_.load());
                                                                                     // observed the lock being free -- try to grab it
  example code snippet: x.fetch_add(1, std::memory_order_acq_rel);
                                                                                  }
                                                                              }
4.3 SpinLock
4.3.1 Local spinning
                                                                              4.3.4 Exponential backoff
void Lock() {
                                                                              void Lock() {
   // lock_bit_ is a boolean, represents if lock is acquired
                                                                                  const size_t kMinBackoffIterations = 4u;
   while (lock_bit_.exchange(true)) {
                                                                                  const size_t kMaxBackoffIterations = 1u << 10u;</pre>
       // Did not get the lock -- spin until it's free
                                                                                  size_t backoff_iterations = kMinBackoffIterations;
       while (lock_bit_.load()) {
                                                                                  while (lock_bit_.exchange(true)) {
           // someone still holds the lock
                                                                                     // Did not get the lock -- spin until it's free
       // observed the lock being free -- try to grab it
                                                                                         for (size_t i = 0; i < backoff_iterations; i++) {</pre>
   }
                                                                                             // Tell hardware that we are spinning
}
                                                                                             _mm_pause();
                                                                                         backoff_iterations =
4.3.2 Active backoff
                                                                                             std::min(backoff_iterations << 1, kMaxBackoffIterations);</pre>
                                                                                     } while (lock_bit_.load());
void Lock() {
                                                                                     // observed the lock being free -- try to grab it
   while (lock_bit_.exchange(true)) {
                                                                                  }
       // Did not get the lock -- spin until it's free
                                                                              }
       do {
           for (volatile size_t i = 0; i < 100; i++) {</pre>
              // Do nothing
                                                                              4.3.5 Ticket lock (Fairness)
                                                                              class SpinLockTicket {
       } while (lock_bit_.load());
                                                                              public:
       // observed the lock being free -- try to grab it
                                                                                  SpinLockTicket() : next_ticket_(0), now_serving_(0) {}
   }
}
                                                                                  void Lock() {
                                                                                     const auto ticket = next_ticket_.fetch_add(1);
4.3.3 Passive backoff
                                                                                     while (now_serving_.load() != ticket) {
                                                                                         _mm_pause();
#include <emmintrin.h>
                                                                                  }
void Lock() {
    while (lock_bit_.exchange(true)) {
       // Did not get the lock -- spin until it's free
                                                                                  void Unlock() {
       do {
                                                                                     now_serving_.store(now_serving_.load() + 1);
           for (size_t i = 0; i < 4; i++) {
                                                                                  }
              // Tell hardware that we are spinning
```

```
private:
    std::atomic<size_t> next_ticket_;
    std::atomic<size_t> now_serving_;
};
```

4.3.6 Comments

- lock_bit_.exchange(true): performs Test-And-Set(TAS) operation.
 - It enters the memory to set lock_bit_ to true, and return its old value
 - It also thrashes the cached values (cache thrashing) for other cores,
 i.e. the cached value of lock_bit_ is invalidated for other cores. This leads to memory access when other cores load the value of lock_bit_ and cache the value thereafter.
- lock_bit_.load(): loads the value of lock_bit_.
 - If cached value of lock_bit_ is valid, load the value from cache.
 - Otherwise load the value from memory.
- volatile: a hint to the implementation to avoid aggressive optimisation involving the object.
- _mm_pause(): calls x86's underlying processor instructions for hinting that program is spinning.
 - Allows the processor to "do nothing" more efficiently, thereby reducing energy consumption.
 - Does *not* include OS context switch.

4.4 Futex and Hybrid Lock

4.4.1 FUTEX_WAIT

- Arguments: int *p, int v.
- Returns immediately if *p != v.
- Otherwise, adds thread to wait queue associated with p.

4.4.2 FUTEX_WAKE

- Arguments: int *p, int wake_count.
- Wake up wake_count threads that are on the wait queue for p.
- 1 and INT_MAX: the only sensible values for wake_count.

4.4.3 Simple mutex with futex

```
class MutexSimple {
public:
    MutexSimple() : state_(kFree) {}
    /* Atomically exchange state_ with 1
     * Result is not kLocked: got the mutex! No need to call futex
     * Otherwise call FUTEX WAIT
     * If NOW state_ == kLocked: someone else unlocked the mutex!
     * return immediately to the while loop condition to perform TAS
     * otherwise go to sleep.
     */
    void Lock() {
       while (state_.exchange(kLocked) == kLocked) {
           syscall(SYS_futex, reinterpret_cast<int*>(&state_), FUTEX_WAIT,
               kLocked, nullptr, nullptr, 0);
       }
    }
    /* Store 0 to state
     * Call FUTEX_WAKE in case other threads are waiting
     * Ask FUTEX_WAKE to wake up one waiter
     */
    void Unlock() {
       state_.store(kFree);
       syscall(SYS_futex, reinterpret_cast<int*>(&state_), FUTEX_WAKE, 1,
           nullptr, nullptr, 0);
   }
private:
    const int kFree = 0;
    const int kLocked = 1;
    std::atomic<int> state_;
};
4.4.4 Smart futex-based mutex
class MutexFutex {
public:
    MutexFutex() : state_(kFree) {}
    /* It is NOT possible to have a thread sleeping forever.
```

```
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```

```
* Neutral (N): The thread isn't interested in the lock.
 * Critical (C): The thread holds the lock.
 * Trying (T): In the do-while loop to try to acquire lock again.
 * Sleeping (S): Sleeping due to having called FUTEX_WAIT.
 * To have a thread sleeping forever, we must have either
 * C, N, N, ..., N, S and state_ == 1
 * OR
 * N, N, N, ..., N, S and state_ == 0.
 * In order to enter the state S, we must have been through:
 * C, N, N, ..., N, T or N, N, N, ..., N, T
 * and T could only be changed from N if there is alr a thread in C.
 * The 1st situation implies state_ == 2 after T changes to S.
 * The 2nd situation doesn't make sense at all.
 */
void Lock() {
   int old_value = cmpxchg(kFree, kLockedNoWaiters);
   if (old_value == kFree) {
       // We got the lock without contention - good
       return;
   }
       // Call FUTEX_WAIT if someone else got the lock.
       // Think exhaustively in this approach:
       // when old_value == x,
       // what happen when state_ is one of \{0, 1, 2\}\setminus\{x\}?
       if (old_value == kLockedWaiters ||
               cmpxchg(kLockedNoWaiters, kLockedWaiters) != kFree) {
           syscall(SYS_futex, reinterpret_cast<int*>(&state_),
               FUTEX_WAIT, kLockedWaiters, nullptr, nullptr, 0);
       old_value = cmpxchg(kFree, kLockedWaiters);
       // whoever manages to have old_value == kFree got the lock!
   } while (old_value != kFree);
}
/* If state_ == 2, we think there were waiters when we locked,
 * therefore should call FUTEX_WAKE.
 * If state_ == 1, we think there were no waiters when we locked,
 * therefore unnecessary to call FUTEX_WAKE.
 * But either way, ensure that state_ is 0 when Unlock() returns.
 */
void Unlock() {
   if (state_.fetch_sub(1) == kLockedWaiters) {
```

5 CONCURRENCY IN HASKELL

5 Concurrency in Haskell

5.1 Thread

```
import Control.Concurrent
-- forkIO :: IO () -> IO ThreadId
import Control.Monad
import System.IO

putChars :: Char -> Int -> IO ()
putChars _ O = return ()
putChars c n = do
    putChar c
    putChars c (n - 1)

main = do
    hSetBuffering stdout NoBuffering
    forkIO (putChars 'B' 10000)
    putChars 'A' 10000
```

5.2 Join Thread

```
-- newMVar :: a -> IO (MVar a)
-- counter <- newMVar 0
-- counter :: MVar Integer
-- newEmptyMVar :: IO (MVar a)
-- handle <- newEmptyMVar
-- handle <- Any
-- takeMVar :: MVar a -> IO a
-- putMVar :: MVar a -> a -> IO ()
-- readMVar :: MVar a -> IO a
-- () is a Unit type, which has exactly one value - () itself.
import Control.Concurrent
import Control.Monad
import System.IO
thread1 :: MVar () -> IO ()
thread1 handle = do
   print "I am thread 1"
   putMVar handle ()
```

```
thread2 :: MVar () -> IO ()
thread2 handle = do
    print "I am thread 2"
    putMVar handle ()

main = do
    hSetBuffering stdout NoBuffering
    handle1 <- newEmptyMVar
    handle2 <- newEmptyMVar
    forkIO (thread1 handle1)
    forkIO (thread2 handle2)
    takeMVar handle1
    takeMVar handle2</pre>
```

5.3 Mutual Exclusion

```
import Control.Concurrent
import Control.Monad
import System.IO
printProtected :: MVar () -> String -> IO ()
printProtected mutex message = do
   putMVar mutex ()
   print message
   takeMVar mutex
thread1 :: MVar () -> MVar () -> IO ()
thread1 mutex handle = do
   printProtected mutex "I'm"
   printProtected mutex "thread1"
   putMVar handle ()
thread2 :: MVar () -> MVar () -> IO ()
thread2 mutex handle = do
   printProtected mutex "!I'm"
   printProtected mutex "!thread2"
   putMVar handle ()
main = do
   hSetBuffering stdout NoBuffering
   handle1 <- newEmptyMVar
   handle2 <- newEmptyMVar
   mutex <- newEmptyMVar</pre>
   forkIO (thread1 mutex handle1)
```

5 CONCURRENCY IN HASKELL

```
forkIO (thread2 mutex handle2)
takeMVar handle1
takeMVar handle2
```

5.4 Messasge Passing – Producer-Consumer

```
import Control.Concurrent
import Control.Monad
import System. IO
-- producer put elem one-by-one to let consumer consume
sendToConsumers :: MVar Int -> Int -> IO ()
sendToConsumers 0 = return ()
sendToConsumers p2c n = do
   putMVar p2c 1
   sendToConsumers p2c (n - 1)
-- get all processed elems from c2p and return the number
getFromConsumers :: MVar Int -> Int -> I0 Int
getFromConsumers _ 0 = return 0
getFromConsumers c2p n = do
   val <- takeMVar c2p</pre>
    theRest <- getFromConsumers c2p (n - 1)
    return (val + theRest)
-- send elems to consumers via p2c,
-- collect the processed ones back via c2p,
-- and eventually put the total number of consumption into the result
producer :: MVar Int -> MVar Int -> Int -> Int -> MVar Int -> IO ()
producer p2c c2p numElems numConsumers result = do
   sendToConsumers p2c numElems
    combinedConsumerValues <- getFromConsumers c2p numConsumers</pre>
   putMVar result combinedConsumerValues
-- consume n data from p2c and return them
consumeData :: MVar Int -> Int -> IO Int
consumeData 0 = return 0
consumeData p2c n = do
   val <- takeMVar p2c
   rest <- consumeData p2c (n - 1)
   return (val + rest)
-- put the result of consumption into c2p
consumer :: MVar Int -> MVar Int -> Int -> MVar () -> IO ()
```

```
consumer p2c c2p numElems handle = do
    myResult <- consumeData p2c numElems
    putMVar c2p myResult
    putMVar handle ()
main = do
    args <- getArgs</pre>
    let numConsumers = read (args!!0) :: Int
    let elemsPerConsumer = read (args!!1) :: Int
    p2c <- newEmptyMVar
    c2p <- newEmptyMVar
    -- mapM :: Monad m \Rightarrow (a \rightarrow m b) \rightarrow [a] \rightarrow m [b]
    -- mapM_{-} :: Monad m => (a -> m b) -> [a] -> m ()
    -- Create an MVar per consumer to serve as a handle
    consumerHandles <- mapM (\_ -> newEmptyMVar) [1..numConsumers]
    -- Fork a producer
    producerResult <- newEmptyMVar</pre>
    forkIO (producer p2c c2p (numConsumers * elemsPerConsumer)
        numConsumers producerResult)
    -- Fork numConsumers consumers
    mapM_ (\handle -> forkIO (consumer p2c c2p elemsPerConsumer handle))
        consumerHandles
    -- Join the consumers (not strictly needed)
    mapM_ takeMVar consumerHandles
    -- Join the producer
    result <- takeMVar producerResult
    -- Print the final result
    print result
     Linked List
```

```
import Control.Concurrent
import Control.Monad
import System.IO
import System.Environment

type Stream a = MVar (Item a)
```

```
data Item a =
   Item a
               -- the value
        (Stream a) -- the rest
data Channel a =
    Channel (Mvar (Stream a))
           (Mvar (Stream a))
newChannel :: IO (Channel a)
newChannel = do
    hole <- newEmptyMVar
   readEnd <- newMVar hole
    writeEnd <- newMVar hole
    return (Channel readEnd writeEnd)
readChannel :: Channel a -> IO a
readChannel (Channel readEndPtr _) = do
    readEnd <- takeMVar readEndPtr</pre>
    Item value theRest <- takeMVar readEnd</pre>
    putMVar readEndPtr theRest
    return value
writeChannel :: Channel a -> a -> IO ()
writeChannel (Channel _ writeEndptr) value = do
    writeEnd <- takeMVar writeEndptr</pre>
    newHole <- newEmptyMVar</pre>
    putMVar writeEnd (Item value newHole)
    putMVar writeEndptr newHole
```

6 Dynamic Data Race Detection (Vector Clockbased)

6.1 Definitions and Assumptions

- N: maximum number of threads tracked by algorithm.
- $\{0, 1, \ldots, N-1\}$: set of thread ids, denoting *Threads*.
- Synchronisation is via a set of locks, denoting *Locks*.
- *Locations* is a set of possibly-shared memory locations.
- Logical clock $\in \mathbb{N}$: increases each time the thread releases a mutex.
- Vector clock $V \triangleq (c_0, c_1, \dots, c_{N-1})$: a tuple of N logical clocks, where

$$V(t) = c_t$$
.

- VC is the set of all vector clocks.
- Bottom vector clock $\perp \triangleq (0, 0, \dots, 0)$.
- Partial order on V:

$$V_1 \sqsubseteq V_2 \iff \forall t. V_1(t) \le V_2(t).$$

• Join of vector clocks:

 $V_1 \sqcup V_2 = \text{pointwise maximum of } V_1 \text{ and } V_2.$

• Increment:

$$\operatorname{inc}_t(V) = V[t \mapsto V(t) + 1].$$

6.2 Vector Clock Algorithm State

- $C: Threads \mapsto VC$
 - $-C_t$: shorthand for C(t), represents what thread t knows about the VC.
 - $-C_t(t)$ is t's logical clock.
 - For $u \neq t$, $C_t(u) = z$ means "thread t knows that thread u's logical clock is at least z.
 - When t acquires a lock, t gets information about the logical clocks of threads who previously held the lock.

- $L: Locks \mapsto VC$
 - $-L_m$: shorthand for L(m), represents the logical clock each thread has last time it released m.
 - $-L_m(t) = 0$ means that t has never released m.
 - Otherwise $L_m(t)$ was t's logical clock last time t releases m.
- $R: Location \mapsto VC$
 - $-R_x$: shorthand for R(x), represents the logical clock each thread had last time it read from x.
 - $-R_x(t)=0$ means that t has never read from x.
 - Otherwise $R_x(t)$ was t's logical clock last time t read from x.
- $W: Location \mapsto VC$
 - $-W_x$: shorthand for W(x), represents the logical clock each thread had last time it wrote to x.
 - $-W_x(t)=0$ means that t has never written to x.
 - Otherwise $W_x(t)$ was t's logical clock last time t wrote to x.

6.3 Initial Analysis State

- $C = (\operatorname{inc}_0(\bot), \operatorname{inc}_1(\bot), \ldots, \operatorname{inc}_{N-1}(\bot))$
- $L = \lambda m. \perp$
- $R = \lambda x. \perp$
- $W = \lambda x. \perp$

6.4 Intercepted Operations

• rd(t, x): interception of a read by thread t from possibly-shared memory location x.

$$\frac{W_x \sqsubseteq C_t \qquad R' = R[x \mapsto R_x[t \mapsto C_t(t)]]}{(C, L, R, W) \xrightarrow{\mathtt{rd(t, x)}} (C, L, R', W)}$$

• wr(t, x): interception of a write by thread t to possibly-shared memory location x.

$$\frac{W_x \sqsubseteq C_t \qquad R_x \sqsubseteq C_t \qquad W' = W[x \mapsto W_x[t \mapsto C_t(t)]]}{(C, L, R, W) \xrightarrow{\text{wr(t,x)}} (C, L, R, W')}$$

• acq(t, m): interception of an acquire of m by t.

$$\frac{C' = C[t \mapsto (C_t \sqcup L_m)]}{(C, L, R, W) \xrightarrow{\operatorname{acq(t,m)}} (C', L, R, W)}$$

• rel(t, m): interception of a release of m by t.

$$\frac{L' = L[m \mapsto C_t] \qquad C' = C[t \mapsto \operatorname{inc}_t(C_t)]}{(C, L, R, W) \xrightarrow{\operatorname{rel(t,m)}} (C', L', R, W)}$$

6.5 Race Rules

• Write-Read race rule:

$$\frac{\exists u. W_x(u) > C_t(u)}{(C, L, R, W) \xrightarrow{\mathtt{rd(t,x)}} \mathtt{WriteReadRace}(u, t, x)}$$

• Write-Write race rule:

$$\frac{\exists u. W_x(u) > C_t(u)}{(C, L, R, W) \xrightarrow{\text{wr(t,x)}} \text{WriteWriteRace}(u, t, x)}$$

• Read-Write race rule:

$$\frac{\exists u . R_x(u) > C_t(u)}{(C, L, R, W) \xrightarrow{\operatorname{wr(t,x)}} \operatorname{ReadWriteRace}(u, t, x)}$$