T. 用梯形设好初值问题。 y'=-2y+2x²+xx , y(0)=1 . 取步长片=0.1 . 计单约×=0.5 并列出数值计和均析件 y=exx+x²n误差

後世段ゼn送公式 [ȳn+1 = ȳn + h f (x̄n, ȳn) ȳn+1 = ȳn + ½[f(x̄n, ȳn) + f(x̄n+1, ȳn+1)]

直接整理处建改造法公式. yn+=yn+之[->yn+>xn2+>xn2+>xn->yn++xnn->yn++xnn-)

 $(1+h) y_{n+1} = y_n - hy_n + h x_n^2 + h x_n + h x_{n+1}^2 + h x_{n+1}$ $y_{n+1} = \frac{1-h}{1+h} y_n + \frac{h}{1+h} x_n (x_n+1) + \frac{h}{1+h} x_{n+1} (x_{n+1}+1)$

中方程计平 yn: Xo=0 yo=1 X1=0.1 y,=0.82 818. X2=0.2 .y=0.70942

X3 = 0.3 y3 = 0.63771 X4=0.4 y4 = 0.60813 X5 = 0.5 y5 = 0.61665

神野好好值: y(0)=1 y(0.1)=0.82873 y(0.2)=6.71032 y(0.3)=6.63881 y(0.4)-0.60933 y(0.3)=0.61788

·教育的好好误差为· 0,=0 01= \$5x/67 01= PX/0-4 03= 1.1x/0-3

du = 1.2×10-3 ds = 1.23×10-3

Tz 证明. yntz + (b-1) ynt1 - byn = 4h[(b+3) yntz +13b+1) y'n]

当龄十时是2附的.当分1时是2990

 $y_{n+2} = y(x_n) + 2hy'(x_n) + 2hy''(x_n) + \frac{4}{3}h^3y'''(x_n) + \frac{2}{3}h^4y''(x_n) + \cdots$

yn = y / xn)

 $y_{h+1} = y(x_h) + h y'(x_h) + \frac{h^2}{2} y''(x_h) + \frac{h^3}{6} y'''(x_h) + \frac{h^4}{24} y'(x_h) + \cdots$

y'n = y'(xn)

y'n+= y'(xn) + 2 hy"(xn) + 2h'y"(xn) + \frac{4}{3}h'y (xn) + \frac{4}{3}h'y (xn) + \frac{4}{3}h'y (xn)

 $2\lambda \sqrt{\lambda} - \frac{1}{\lambda} = y(\lambda_n) \cdot (1+b-1-b) + hy'(\lambda_n)(2+b-1) + \frac{h^2}{2}y''(\lambda_n)(4+b-1) + \frac{h^2}{6}y'^{(2)}(\lambda_n)(8+b-1) + \frac{h^2}{2}y''(\lambda_n)(16+b-1) + \frac{h^2}{2}y''(\lambda_n)(16+b$

... 当时·阿·库戈是沪山、当日·叶·麻提沪河

T3.
$$(\sqrt{\frac{16}{16}} + \frac{1}{2} + \frac{1}$$

血事中加减来降远县不产生误差,每次逐分计事的污采的用精确到小数三后来这一小数 进行保存. 试给出具体,真诚 (有报)过程)

[考虑xelon]上y·取值范围,无部件再出多长h·具体值]

设城[0,1]上选战准备当长为h · y'>o ·· y <4 ·· y' < y'(1)=17 ... | of (x,y) | EM= f, |y(2) (x) | EL = 13f. |y(1)(x) | ET = 1684 X=1 次=4 由步长 可知些代次教 n=-

力处进改拉弦《方弦谈差: △n+1 ≤ (1+ hM+ 上水)△n+(型+上)从

$$= \Delta_{h+1} + \frac{1}{h^{M} + \frac{h^{2} M^{2}}{2}} \left(\frac{mL}{4} + \frac{1}{12} \right) h^{2} \leq \left(H h^{M} + \frac{h^{2}}{2} m^{2} \right) \left[\Delta_{h} + \frac{1}{h^{M}} + \frac{h^{2} M^{2}}{2} \left(\frac{mL}{4} + \frac{T}{12} \right) h^{2} \right]$$

· · · (| + hm + \frac{h^2m^2}{2})^{h+1} [\Delta_0 + \frac{1}{hm + \frac{h^2m^2}{4}} (\frac{ml}{4} + \frac{T}{12})h^3]

后送教) 如从进改建改工名入误差: Sint ≤ (+hM+ 1/2 m²) Sin+ (+ 1/2)·1·10 (m放送代升到精确到小小数点 .. Shat + Int 1 (+ hm) - 1.10-m = (+hm+ 1)[Sn + 1 hm+ 1 hm (+ hm) . 1.10-m]

< (1+hm+ + 12m2) h+1 [So+ 1/2 (H + 1/2) . 1/2 1/2]					
		中西越早是求有.			

不知性可含 6n < 4×10-8 cn < 4×10-8

 $= \frac{1}{\sqrt{16}} \left[\left(\frac{1}{16} + \frac{1}{12} \right)^{h} - 1 \right] \left[\frac{1}{16} + \frac{1}{12} \right]^{3} \right] \sim \left(\frac{e^{M} - 1}{16} \right) \frac{h^{2}}{\sqrt{16}} \left(\frac{h^{2} + \frac{1}{12}}{16} \right) \leq \frac{1}{4} \times 10^{-8}$ $= \frac{1}{\sqrt{16}} \left[\left(\frac{1}{16} + \frac{h^{2}}{2} \right)^{h} - 1 \right] \left[\frac{1}{16} + \frac{h^{2}}{2} \right]^{2} \left(\frac{h^{2} + \frac{1}{12}}{16} \right)^{3} = \left(\frac{e^{M} - 1}{16} \right) \frac{1}{2h^{2}} \cdot \frac{1}{2} \cdot 10^{-10} \leq \frac{1}{4} \times 10^{-8}$

其中.M=8. L=138. T=1684. N=1

其中11-8. 上一, 本加.