



Kuantum Kaynak Teorilerine Giriş

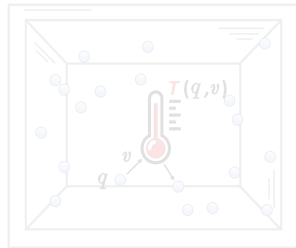
KUANTUM TERMODİNAMİK

$\langle \text{QSB} \mid \text{KU} \rangle$

Dr. Onur Pusuluk

Koç Üniversitesi

11 Nisan 2021



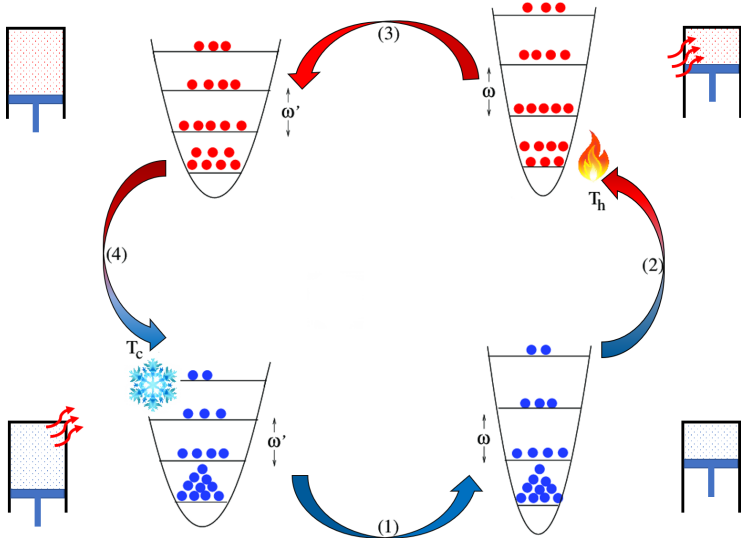
Prolog: Tekil Sistemlerin Termodinamiği
Kuantum “Isı” Makineleri
Kuantum Isı Transfer Mekanizmaları

Monologlar: Termodinamik Vs Kuantum
IID Limitin Ötesi?

Diyaloglar: Kuantum Termodinamik
Açık Sistem Yaklaşımı
Kaynak Teorisi Yaklaşımı

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Otto Çevrimi



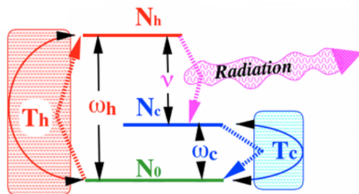
VOLUME 2, NUMBER 6

PHYSICAL REVIEW LETTERS

MARCH 15, 1959

THREE-LEVEL MASERS AS HEAT ENGINES

H. E. D. Scovil and E. O. Schulz-DuBois



REPORT

A single-atom heat engine

Johannes Roßnagel^{1,*}, Samuel T. Dawkins¹, Karl N. Tolazzi², Obinna Abah³, Eric Lutz³, Ferdinand Sc...

* See all authors and affiliations

Science 15 Apr 2016:
Vol. 352, Issue 6283, pp. 325-329
DOI: 10.1126/science.aad6320

A single-atom heat engine

Eric Lutz

Physics Today 73, 5, 66 (2020)

<https://doi.org/10.1063/PT.3.4482>

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Editors' Suggestion

Experimental Demonstration of Quantum Effects in the Operation of Microscopic Heat Engines

James Klatzow, Jonas N. Becker, Patrick M. Ledingham, Christian Weinzettl, Krzysztof T. Kaczmarek, Dylan J. Saunders, Joshua Nunn, Ian A. Walmsley, Raam Uzdin, and Eilon Poem
Phys. Rev. Lett. 122, 110601 – Published 20 March 2019

PhysiCS See Viewpoint: Powering an Engine with Quantum Coherence

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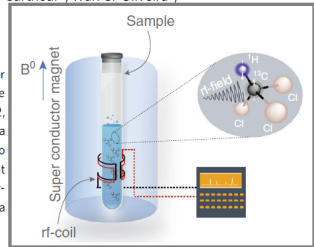
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Ortak Yaklaşım?

NATURE COMMUNICATIONS | <https://doi.org/10.1038/s41467-019-10333-7>

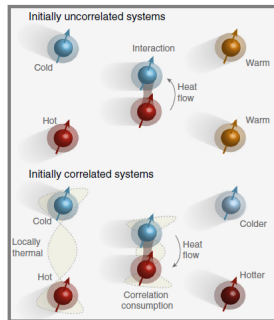
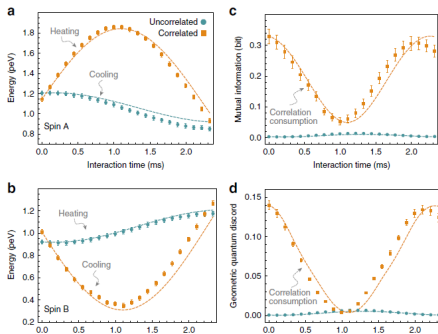
Reversing the direction of heat flow using quantum correlations

Kaonan Micadei^{1,2,8}, John P.S. Peterson^{3,8}, Alexandre M. Souza³, Roberto S. Sarthour³, Ivan S. Oliveira³, Gabriel T. Landi⁴, Tiago B. Batalhão^{5,6}, Roberto M. Serra^{1,7} & Eric Lutz²

Heat spontaneously flows from hot to cold in standard thermodynamics. However, the latter theory presupposes the absence of initial correlations between interacting systems. We here experimentally demonstrate the reversal of heat flow for two quantum correlated spins-1/2, initially prepared in local thermal states at different effective temperatures, employing a Nuclear Magnetic Resonance setup. We observe a spontaneous energy flow from the cold to the hot system. This process is enabled by a trade off between correlations and entropy that we quantify with information-theoretical quantities. These results highlight the subtle interplay of quantum mechanics, thermodynamics and information theory. They further provide a mechanism to control heat on the microscale.



NATURE COMMUNICATIONS | <https://doi.org/10.1038/s41467-019-10333-7>



Quantum Rayleigh Problem and Thermocoherent Onsager Relations

Onur Pusuluk¹ and Özgür E. Müstecaplıoğlu¹

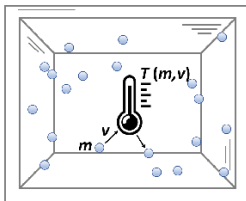
¹Department of Physics, Koç University, Sarıyer, İstanbul, 34450 Turkey

arXiv:2006.03186

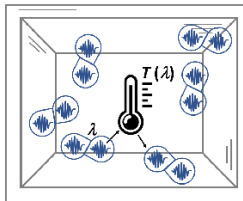
$$\mathcal{J}_h = L_{hh} \Delta(1/T) + L_{hc} \Delta(C/T) \quad (1)$$

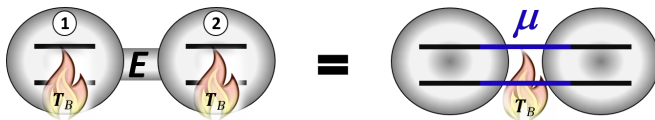
$$\mathcal{J}_c = L_{ch} \Delta(1/T) + L_{cc} \Delta(C/T) \quad (2)$$

(a)

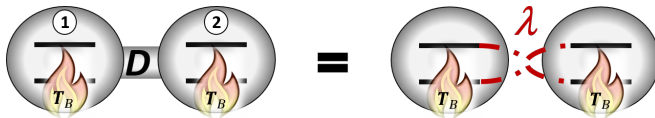


(b)

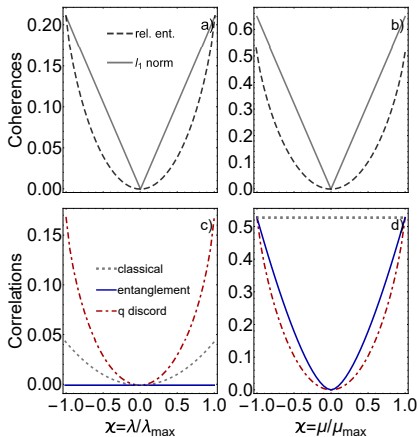




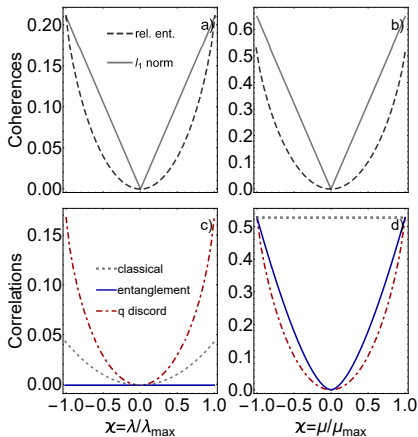
$$\rho_E = p_g |gg\rangle\langle gg| + p_e |ee\rangle\langle ee| + (\mu |gg\rangle\langle ee| + \text{h.c.}) = \begin{pmatrix} p_g & 0 & 0 & \mu \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ \mu & 0 & 0 & p_e \end{pmatrix}$$



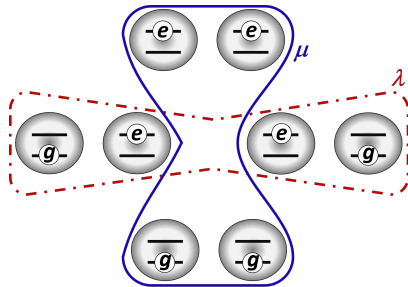
$$\rho_D = (p_g |g\rangle\langle g| + p_e |e\rangle\langle e|)^{\otimes 2} + (\lambda |ge\rangle\langle eg| + \text{h.c.}) = \begin{pmatrix} p_g^2 & 0 & 0 & 0 \\ 0 & p_g p_e & \lambda & 0 \\ 0 & \lambda & p_g p_e & 0 \\ 0 & 0 & 0 & p_e^2 \end{pmatrix}$$

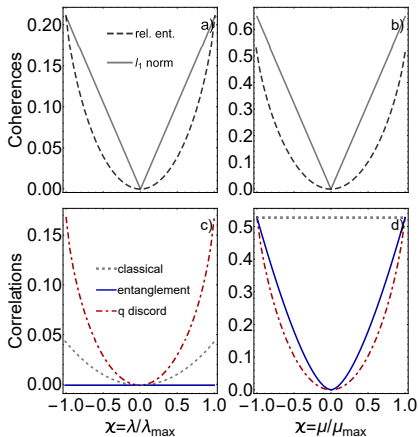


$$E_g = 1, E_e = 2, \beta_B = 2.$$

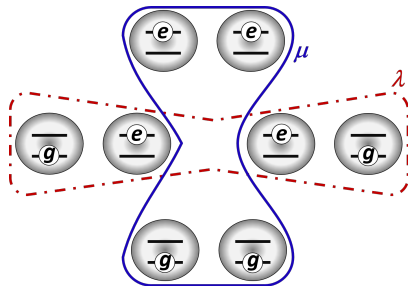


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Entropy 18, 244 (2016); PRE 99, 042145 (2019)

Sci. Rep. 9, 3191; PRR 1, 033097 (2019); PRA 102, 042220 (2020)

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Termodinamik Vs Kuantum





► 1. Yasa: $\Delta E = Q + W$



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$$\rho_{12} \neq \rho_1 \otimes \rho_2$$

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0: Sistem-Banyo Bölüşümü



► İndirgenmiş Tanımlama

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► Dengeye Yaklaşma

$$\rho_S(t) = \Lambda_t(\rho_S(0)) \rightarrow \rho_S^\infty = \exp(-\beta_B \hat{H}_S) / \mathcal{Z}$$

1: Enerji Değişimi



► Enerjinin Korunumu

$$[\hat{H}_S, \hat{H}_{SB}] = 0 \Rightarrow dE_S = -dE_B$$

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$$\mathcal{P} \equiv \text{tr}[\rho_S \frac{\partial}{\partial t} \hat{H}_S]$$

$$\mathcal{J} \equiv \text{tr}[\rho_S \mathcal{D}(\rho_S)]$$

2: Entropi Değişimi



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$$S[\Lambda_t(\rho_S)||\Lambda_t(\rho_S^\infty)] \leq S[\rho_S||\rho_S^\infty]$$

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- Kaynak değeri olan durumlar:

$$(\rho, \hat{H})$$

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$$[U(\rho \otimes \rho_\beta)U^\dagger]$$

$$[\hat{H}_{tot}, U] = 0$$

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- İzinli (Termal) Dönüşümler:

$$(\rho, \hat{H}) \rightarrow (\sigma, \hat{H}')$$

Article | Published: 26 June 2013

Fundamental limitations for quantum and nanoscale thermodynamics

Michał Horodecki & Jonathan Oppenheim 

Nature Communications **4**, Article number: 2059 (2013) | [Download Citation](#) 

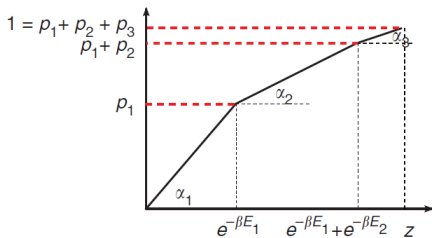
The second laws of quantum thermodynamics



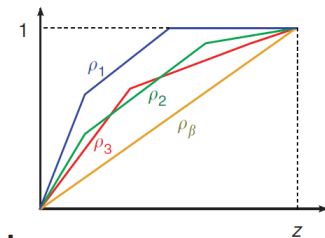
Fernando Brandão, Michał Horodecki, Nelly Ng, Jonathan Oppenheim, and Stephanie Wehner

PNAS March 17, 2015 112 (11) 3275-3279; first published February 9, 2015 <https://doi.org/10.1073/pnas.1411728112>

Edited by Peter W. Shor, Massachusetts Institute of Technology, Cambridge, MA, and approved January 12, 2015
(received for review June 26, 2014)



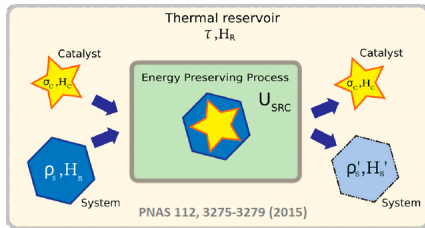
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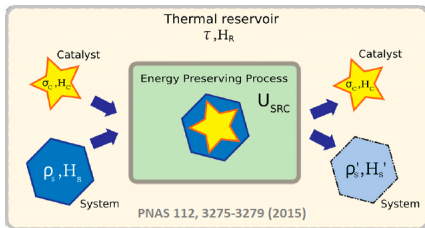
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Nat Commun 4, 2059 (2013)

2. Yasa Ailesi ve Katalitik Dönüşümler



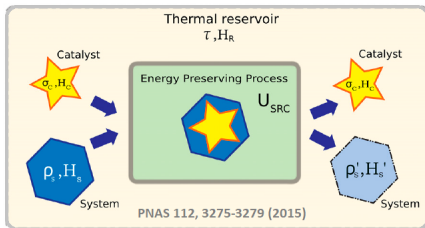
2. Yasa Ailesi ve Katalitik Dönüşümler



$$F_\alpha(\rho, \rho_\beta) := kTD_\alpha(\rho \parallel \rho_\beta) - kT \log Z$$

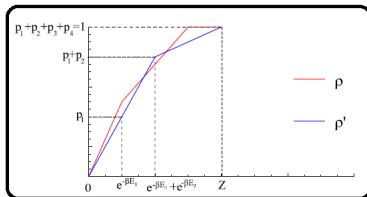
$$D_\alpha(\rho \parallel \rho_\beta) = \frac{\text{sgn}(\alpha)}{\alpha - 1} \log \sum_i p_i^\alpha q_i^{1-\alpha}$$

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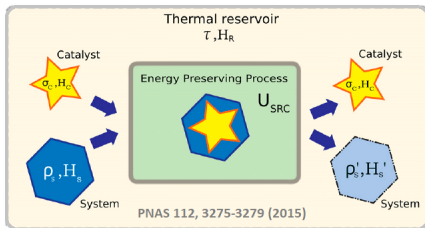


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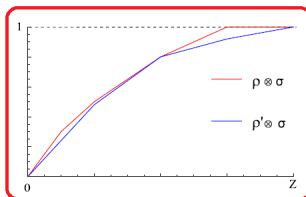
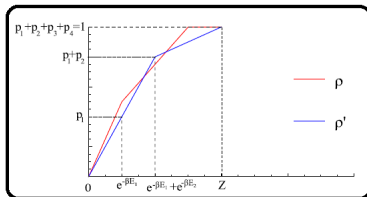


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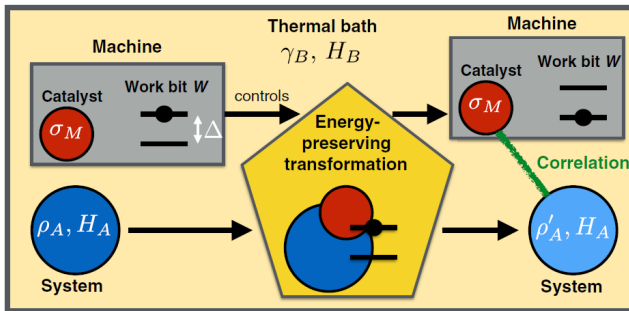


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PHYSICAL REVIEW X 8, 041051 (2018)

Correlating Thermal Machines and the Second Law at the Nanoscale

Markus P. Müller



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Fin