

**Definitions**

**Isolated system:** No exchanges

**Closed system:** Only energy exchange

**Open system:** Energy & mass exchange

**Intensive state variables:**

Independent of mass

**Extensive state variables:**

Proportional to mass

**Reservoirs:** Infinite/very large system that remains unchanged when in contact with finite system.

**Mechanical equilibrium:**

No unbalanced forces

**Thermal equilibrium:**

No temperature differences

**Thermodynamic equilibrium:**

Intensive state variables of system are constant. Alternatively our system is in mechanical and thermal equilibrium.

**Reversible processes:**

Every intermediate is an equilibrium state.

**Quasi-static processes:**

Process sufficiently slow such that only infinitesimal temperature or pressure gradients exist.

Frictionless quasi-static processes are reversible.

**Cyclic processes:**

$$\Delta U = 0 \text{ and } W = Q$$

For conservative forces:

$$\oint dX = 0$$

where  $X$  is a state variable.

**Adiabatic processes:**  $\Delta Q = 0$

**Isothermal processes:**  $\Delta T = 0$

**Zeroth law**

If  $A$  is in thermal equilibrium with  $B$  and  $C$  separately then  $B$  and  $C$  are also in thermal equilibrium.

**Ideal gas state equation**

Given  $n$  moles of gas at temperature  $T$ :

$$PV = nRT$$

where  $R = 8.314 \text{ JK}^{-1} \text{ mol}^{-1}$ .

**First law**

Total energy  $E$  is conserved and:

$$dU = dQ - dW.$$

Note  $Q > 0$  represents energy transferred into system. When system does work on surroundings  $W > 0$ .

Work done by fluid in reversible adiabatic processes:

$$dW = PdV$$

and is in Joules (J).

**Isochoric heat capacity**

$$C_V(T) = \left( \frac{dQ}{dT} \right)_V = \left( \frac{\partial U}{\partial T} \right)_V$$

**Isoobaric heat capacity**

$$\begin{aligned} C_P &= \left( \frac{dQ}{dT} \right)_P \\ &= C_V + \left[ P + \left( \frac{\partial U}{\partial V} \right)_T \right] \left( \frac{\partial V}{\partial T} \right)_P \end{aligned}$$

Heat capacity has units  $\text{JK}^{-1}$ .

For ideal gases we have that:

$$C_P - C_V = nR.$$

Under reversible adiabatic processes:

$$TV^{\gamma-1} = \text{constant}$$

$$PV^\gamma = \text{constant}$$

$$T^{\frac{1}{\gamma-1}} V = \text{constant}$$

where  $\gamma$  is the adiabatic exponent:

$$U = \frac{f}{2} nRT$$

$$\gamma = \frac{C_P}{C_V} = \frac{f+2}{f}$$

regardless of degrees of freedom  $f$ .

**State function enthalpy**

$$H = U + PV$$

$$\begin{aligned} dH &= dU + VdP + PdV \\ &= dQ + VdP \end{aligned}$$

$$\therefore C_P = \left( \frac{\partial H}{\partial T} \right)_P$$

**Chemical reactions**

$$Q = \Delta U + P_0 \Delta V = \Delta H$$

Here  $P_0$  is constant.

- $Q < 0$ : exothermic (heat is released)
- $Q > 0$ : endothermic (heat is absorbed)

**Carnot's theorem**

Peak efficiency of a cyclic heat engine:

$$\eta = \frac{\dot{W}}{Q_H} = 1 - \frac{Q_C}{Q_H} = 1 - \frac{T_C}{T_H}$$

and is either in terms of rate or value, with units J or  $\text{Js}^{-1}$ .

**State function entropy**

$$S = \frac{Q}{T}$$

$$\therefore dU = TdS - PdV$$

**Entropy of mixing**

$$\Delta S = n_A R \ln \frac{V_A + V_B}{V_A} + n_B R \ln \frac{V_A + V_B}{V_B}$$

$$\Delta S_{mix} = -R(x_A \ln x_A + x_B \ln x_B)$$

$$x_A = \frac{n_A}{n_A + n_B} \text{ and } x_B = \frac{n_B}{n_A + n_B}$$

**Second law**

$$\Delta S_{total} = \Delta S_{system} + \Delta S_{reservoir} \geq 0$$

$$dS \geq \frac{dQ}{T}$$

**Helmholtz free energy**

$$F = U - TS$$

$$dF = -SdT - PdV$$

**Gibbs free energy**

$$G = H - TS$$

$$dG = -SdT + VdP$$

Chemical reactions are spontaneous if:

$$\Delta G = \Delta H - T\Delta S < 0.$$

**Maxwell relations**

$$\left( \frac{\partial T}{\partial V} \right)_S = - \left( \frac{\partial P}{\partial S} \right)_V$$

$$\left( \frac{\partial T}{\partial P} \right)_S = \left( \frac{\partial V}{\partial S} \right)_P$$

$$\left( \frac{\partial S}{\partial V} \right)_T = \left( \frac{\partial P}{\partial T} \right)_V$$

$$- \left( \frac{\partial S}{\partial P} \right)_T = \left( \frac{\partial V}{\partial T} \right)_P$$

The isobaric expansivity is defined as:

$$\beta = \frac{1}{V} \left( \frac{\partial V}{\partial T} \right)_P$$

and the isothermal compressibility:

$$\kappa_T = - \frac{1}{V} \left( \frac{\partial V}{\partial P} \right)_T.$$

**Clausius-Clapeyron equation**

The slope of any phase boundaries is:

$$\frac{dP}{dT} = \frac{\Delta S}{\Delta V}.$$

**Van der Waals state equation**

$$\left(P + \frac{an^2}{V^2}\right)(V - nb) = nRT$$

**Chemical potentials**

$$\mu = \frac{G}{N}$$

**Third law**

$S = 0$  at  $T = 0\text{K}$ .