

## Definitions

**Isolated system:** No exchanges

**Closed system:** Only energy exchange

**Open system:** Energy & mass exchange

**Intensive state variables:**

Independent of mass

**Extensive state variables:**

Proportional to mass

**Reservoirs:** Infinite/very large system that remains unchanged when in contact with finite system.

**Mechanical equilibrium:**

No unbalanced forces

**Thermal equilibrium:**

No temperature differences

**Thermodynamic equilibrium:**

Intensive state variables of system are constant. Alternatively our system is in mechanical and thermal equilibrium.

**Reversible processes:**

Every intermediate is an equilibrium state.

**Quasi-static processes:**

Process sufficiently slow such that only infinitesimal temperature or pressure gradients exist.

Frictionless quasi-static processes are reversible.

**Cyclic processes:**

$$\oint dX = 0$$

where  $X$  is a state variable.

## Zeroth law

If  $A$  is in thermal equilibrium with  $B$  and  $C$  separately then  $B$  and  $C$  are also in thermal equilibrium.

## Ideal gas state equation

Given  $n$  moles of gas at temperature  $T$ :

$$PV = nRT$$

where  $R = 8.314 \text{ JK}^{-1} \text{ mol}^{-1}$ .

## First law

$$dU = dQ - dW$$

Note  $Q > 0$  represents energy transferred into system. When system does work on surroundings  $W > 0$ .

Work done by fluid in reversible process:

$$dW = PdV.$$

## Isochoric heat capacity

$$C_V(T) = \left( \frac{dQ}{dT} \right)_V = \left( \frac{\partial U}{\partial T} \right)_V$$

## Isobaric heat capacity

$$\begin{aligned} C_P &= \left( \frac{dQ}{dT} \right)_P \\ &= C_V + \left[ P + \left( \frac{\partial U}{\partial V} \right)_T \right] \left( \frac{\partial V}{\partial T} \right)_P \end{aligned}$$

Heat capacity has units  $\text{JK}^{-1}$ .

For ideal gases:

$$C_P - C_V = nR$$

$$TV^{\gamma-1} = \text{constant}$$

$$\gamma = \frac{C_P}{C_V}.$$

## State function enthalpy

$$H = U + PV$$

$$\begin{aligned} dH &= dU + VdP + PdV \\ &= dQ + VdP \end{aligned}$$

$$\therefore C_P = \left( \frac{\partial H}{\partial T} \right)_P$$

## Chemical reactions

$$Q = \Delta U + P_0 \Delta V = \Delta H$$

Here  $P_0$  is constant.

- $Q < 0$ : exothermic (heat is released)
- $Q > 0$ : endothermic (heat is absorbed)

## Carnot's theorem

Peak efficiency of a cyclic heat engine:

$$\eta = 1 - \frac{Q_C}{Q_H}.$$

## State function entropy

$$S = \frac{Q}{T}$$

For reversible cyclic heat engine:

$$dS = \frac{dQ}{T}.$$

$$\therefore dU = TdS - PdV$$