Augustin's Concessions: A Problem for Indeterminate Credal States

Stefan Lukits

The claim is that rational agents are subject to a norm requiring sharp credences. I defend this claim in spite of the initially promising features of indeterminate credal states (from now on instates) to address problems which sharp credences have as they reflect the evidence at the foundation of a doxastic state. Traditionally, Bayesians have maintained that a rational agent, when holding a credence, holds a sharp credence. It has recently become popular to drop the requirement for credence functions to be sharp. There are now Bayesians who permit a rational agent to hold instates based on incomplete or ambiguous evidence. I will refer to Bayesians who continue to adhere to the classical theory of sharp credences for rational agents as 'Laplaceans' (e.g. Adam Elga and Roger White). I will refer to Bayesians who do not believe that a rational agent's credences are sharp as 'Booleans' (e.g. Peter Walley and James Joyce).

I will exclusively refer to indeterminate credal states (abbreviated 'instates', sometimes terminology such as 'imprecise' or 'mushy' credences is used as well) and mean by them a set of sharp credence functions (which some Booleans require to be convex) which it may be rational for an agent to hold within an otherwise orthodox Bayesian framework.

When we first hear of the advantages of instates, two of them sound particularly persuasive.

- RANGE Instates represent the possibility range for objective chances.
- INCOMPLETE Instates represent incompleteness or ambiguity of the evidence.

Here are some examples. Let a $coin_x$ be a Bernoulli generator that produces successes and failures with probability p_x for success, labeled H_x , and $1 - p_x$

for failure, labeled T_x . Physical coins may serve as Bernoulli generators, if we are willing to set aside that most of them are approximately fair.

Example 1: Range. Bob has two Bernoulli Generators in his lab, $coin_i$ and $coin_{ii}$. Bob has a database of $coin_i$ results and concludes on excellent evidence that $coin_i$ is fair. Bob has no evidence about the bias of $coin_{ii}$. As a Boolean, Bob assumes a sharp credence of $\{0.5\}$ for H_i and an indeterminate credal state of [0,1] for H_{ii} . He feels bad for Larry, his Laplacean colleague, who cannot distinguish between the two cases and who must assign a sharp credence of $\{0.5\}$ for both H_i and H_{ii} .

Example 2: Incomplete. Bob has another Bernoulli Generator, $coin_{iii}$, in his lab. His graduate student has submitted $coin_{iii}$ to countless experiments and emails Bob the resulting bias, but fails to include whether the bias of 2/3 is in favour of H_{iii} or in favour of T_{iii} . As a Boolean, Bob assumes an indeterminate credal state of [1/3, 2/3] (or $\{1/3, 2/3\}$, depending on whether convexity is required) for H_{iii} . He feels bad for Larry who must assign a sharp credence of $\{0.5\}$ for H_{iii} when Larry concurrently knows that his credence gets the bias wrong.

Against the force of RANGE and INCOMPLETE, I maintain that the Laplacean approach of assigning subjective probabilities to partitions of the event space (e.g. objective chances) and then aggregating them by David Lewis' summation formula into a single precise credence function is conceptually tidy and shares many of the formal virtues of Boolean theories. To put it provocatively, this paper defends a 0.5 sharp credence in heads in all three cases: for a coin of whose bias we are completely ignorant; for a coin whose fairness is supported by a lot of evidence; and even for a coin about whose bias we know that it is either 1/3 or 2/3 for heads.