

✓ Congratulations! You passed!

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1. In this assessment, you will be tested on all of the different topics you have covered in this module. Good luck!

1 / 1 point

A ship travels with velocity given by $\begin{bmatrix} 1 \\ 2 \end{bmatrix}$, with current flowing in the direction given by $\begin{bmatrix} 1 \\ 1 \end{bmatrix}$ with respect to some co-ordinate axes.

What is the velocity of the ship in the direction of the current?

- ☐ $\begin{bmatrix} 2/3 \\ 3/2 \end{bmatrix}$
- ☒ $\begin{bmatrix} 3/2 \\ 3/2 \end{bmatrix}$
- ☐ $\begin{bmatrix} 3/2 \\ 2/3 \end{bmatrix}$
- ☐ $\begin{bmatrix} 2/3 \\ 2/3 \end{bmatrix}$

✓ Correct

This is the vector projection of the velocity of the ship onto the velocity of the current.

2. A ball travels with velocity given by $\begin{bmatrix} 2 \\ 1 \end{bmatrix}$, with wind blowing in the direction given by $\begin{bmatrix} 3 \\ -4 \end{bmatrix}$ with respect to some co-ordinate axes.

1 / 1 point

What is the size of the velocity of the ball in the direction of the wind?

- ☐ $-\frac{5}{\sqrt{5}}$
- ☒ $\frac{5}{\sqrt{5}}$
- ☐ $\frac{5}{\sqrt{2}}$
- ☐ $-\frac{5}{5}$

✓ Correct

This is the scalar projection of the velocity of the ball onto the velocity of the wind.

3. Given vectors $\mathbf{v} = \begin{bmatrix} -4 \\ -3 \\ 8 \end{bmatrix}$, $\mathbf{b}_1 = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$, $\mathbf{b}_2 = \begin{bmatrix} -2 \\ 1 \\ 0 \end{bmatrix}$ and $\mathbf{b}_3 = \begin{bmatrix} -3 \\ -6 \\ 5 \end{bmatrix}$ all written in the standard basis,

1 / 1 point

what is \mathbf{v} in the basis defined by \mathbf{b}_1 , \mathbf{b}_2 and \mathbf{b}_3 ? You are given that \mathbf{b}_1 , \mathbf{b}_2 and \mathbf{b}_3 are all pairwise orthogonal to each other.

☒ $\begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$

☐ $\begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}$

☐ $\begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$

☐ $\begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}$

✓ **Correct**

This is a change of basis in 3 dimensions.

4. Are the following vectors linearly independent?

1 / 1 point

$\mathbf{a} = \begin{bmatrix} 1 \\ 2 \\ -1 \end{bmatrix}, \mathbf{b} = \begin{bmatrix} 3 \\ -4 \\ 5 \end{bmatrix}$ and $\mathbf{c} = \begin{bmatrix} 1 \\ -8 \\ 7 \end{bmatrix}$.

☐ Yes

☒ No

✓ **Correct**

One can be written as a linear combination of the other two.

5. At 12:00 pm, a spaceship is at position $\begin{bmatrix} 3 \\ 2 \\ 4 \end{bmatrix}$ km away from the origin with respect to some 3 dimensional coordinate system. The ship is travelling with velocity $\begin{bmatrix} -1 \\ 2 \\ -3 \end{bmatrix}$ km/h. What is the location of the spaceship after 2 hours have passed?

1 / 1 point

☐ $\begin{bmatrix} -1 \\ -6 \\ 2 \end{bmatrix}$

☒ $\begin{bmatrix} 1 \\ 6 \\ -2 \end{bmatrix}$

☐ $\begin{bmatrix} -2 \\ 4 \\ -1 \end{bmatrix}$

☐ $\begin{bmatrix} 2 \\ 4 \\ 1 \end{bmatrix}$

✓ **Correct**

This takes the idea of vectors in the context of a moving body.