

Answer

Step 1

Write a program to enter a natural number n and find all sphenic numbers from 1 to n using Recursion (combined with iteration if necessary).

Note: A sphenic number is a product of $p*q*r$ where p , q , and r are three distinct prime numbers.

Example: $30 = 2 * 3 * 5$; $42 = 2 * 3 * 7$; $66 = 2 * 3 * 11$.

30, 42, 66, 70, 78, 102, 105, 110, 114, 130, 138, 154, 165, ... are sphenic numbers.

Step 2

```
#include <iostream>
```

```
#include <cstring>
```

```
using namespace std;
```

```
bool primes[1001]; // array will store all the prime numbers from 0 to 1000. Primes  
will be marked as true
```

```
// seive of eratosthenes to find all primes les sthan 1000
```

```
void primeSieve()
```

```
{
```

```
    // initialize all entries of 'primes' as true
```

```
    memset(primes, true, sizeof(primes));
```

```
    // traverse all numbers and mark their multiples as false
```

```
    // do not traverse false numbers
```

```
    for (int p = 2; p * p < 1001; p++)
```

```
    {
```

```
        if (primes[p])
```

```
        {
```

```
            for (int i = p * 2; i < 1001; i = i + p)
```

```

        primes[i] = false;

    }

}

}

// function to return true if number is sphenic

bool isSphenic(int number)

{

    int arr1[8] = {0}; // array to store 8 divisors

    int count = 0;    // track the number of divisors

    int j = 0;

    for (int i = 1; i <= number; i++)

    {

        if (number % i == 0 && count < 9)

        {

            count++;

            arr1[j++] = i;

        }

    }

    // if there are 8 divisors and the divisors are primes, the number is sphenic

    if (count == 8 && (primes[arr1[1]] && primes[arr1[2]] && primes[arr1[3]]))

        return true;

    return false;

}

// main function

```

```
int main()
{
    int n;

    cout << "Enter n : ";

    cin >> n;

    // generate all prime numbers

    primeSieve();

    cout << "The sphenic numbers between 1 and " << n << " are:\n";

    for (int i = 1; i <= n; i++)
    {
        if(isSphenic(i))
            cout << i << "\n";
    }
}
```