A spatial stochastic discount factor estimator for private equity funds

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Declaration of interest

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Abstract

This paper proposes an improved stochastic discount factor estimation methodology suited for fund-level cash flows of private equity funds. The asymptotic inference framework for this semiparametric least-mean-distance estimator draws on a spatial notion, i.e., the idea that the economic distance between distinct private equity funds can be measured. We empirically test our new approach by estimating several simple stochastic discount factor models for a variety of private equity fund types. Given the high estimator variance revealed by empirical and Monte Carlo simulation results, we conjecture that naive semiparametric M-estimators like ours shall be exclusively used for single-factor models until considerably more vintage year information for private equity funds is available.

1 Introduction

Do investments in Private Equity (PE) funds offer abnormal returns to fund investors when risk-adjusted to/for public market factors? Currently, a popular approach to answer this question is to evaluate private equity fund cash flows by Stochastic Discount Factor (SDF) models that draw on public market return covariates. The basic idea for SDF model estimation is that the sum of all discounted fund net cash flows is expected to be zero when the true SDF is applied. Unfortunately, there is no conclusion about the best methodology to estimate these SDF models, as a variety of proposals coexists in the academic private equity fund literature (Driessen et al., 2012; Buchner, 2014; Korteweg and Nagel, 2016; Ang et al., 2018; Gredil et al., 2019).

This paper focuses on semiparametric approaches. Especially our conclusions from the insightful Driessen et al. (2012) and Korteweg and Nagel (2016) articles lead us to suggest an improved least-mean-distance estimator for SDF models. It can be applied to fund-level cash flow data of private equity funds. On the one hand, we provide asymptotic inference formulations that rely on the concept of spatial (near-epoch) dependency between funds following the pioneering idea in Korteweg and Nagel (2016). In this context, it is paramount to quantify the economic distance between funds by a measure like absolute vintage year difference or cash flow overlap¹. On the other hand, our least-mean-distance estimator arguably generalizes the Driessen et al. (2012) methodology, where we provide the asymptotic inference framework that was missing in the original paper. Additionally, we propose a simple solution to the 'exploding alpha' issue briefly mentioned in their paper. Our Monte Carlo results suggest that the same modification dramatically reduces the inherent bias associated with the original Driessen et al. (2012) estimator.

In the empirical application of our new estimator, we test simple linear and exponentially affine SDF models that can draw on the five return factors associated with the q^5 investment factor model recently proposed by Hou et al. (2020). Based on a Spatial Heteroskedasticity

¹However, this economic inter-fund distance refers NOT to the term least-mean-distance estimator.

and Autocorrelation Consistent (SHAC) covariance matrix estimator, we calculate asymptotic standard errors for the model coefficients. Moreover, we assess the small-sample variance of coefficient estimates and the out-of-sample performance of the different SDF models by hv-block cross-validation, which accounts for the inter-vintage-year dependence of private equity funds (Racine, 2000). We test one- and two-factor models for the following private equity fund types: Private Equity, Venture Capital, Private Debt, Real Estate, Natural Resources, and Infrastructure. All two-factor model results are devastating; not more than the single-market-factor model results may be reasonable given the high estimator variance.

The paper is structured as follows. Section 2 introduces our semiparametric least-mean-distance estimator and its corresponding asymptotic inference framework. Section 3 applies the method to estimate q^5 -investment-factor SDFs for various private equity fund types using simulated and real-world cash flows. Section 4 concludes.

2 Methodology

2.1 Least-mean-distance estimator

Let fund i = 1, 2, ..., n be characterized by its (net) cash flows $CF_{t,i}$ and its net asset values $NAV_{t,i}$ with discrete time index t = 1, 2, ..., T. The data generating processes for CF and NAV are left unspecified. The stochastic discount factor $\Psi_{\tau,t}$ can be used to calculate the time- τ price $P_{\tau,t,i}$ of a time-t cash flow of any given PE fund i

$$P_{\tau,t,i} = \Psi_{\tau,t} \cdot CF_{t,i} \tag{1}$$

As SDFs are commonly parameterized by a vector $\theta \in \mathbb{R}^p$, i.e., $\Psi_{t,\tau} \equiv \Psi_{t,\tau}(\theta)$, our goal is to find an estimation method for the optimal θ . For each fund i and all points τ within a common fund lifetime, the pricing error $\epsilon_{\tau,i}$ of all fund cash flows is calculated as

$$\epsilon_{\tau,i} = \sum_{t=1}^{T} P_{\tau,t,i} \qquad \forall \quad \tau, i \tag{2}$$

To decrease the bias and variance of the Driessen et al. (2012) estimator, we define the w-weighted τ -average fund pricing error as

$$\bar{\epsilon}_i = w_i \cdot \frac{1}{\operatorname{card}(\mathcal{T}_i)} \sum_{\tau \in \mathcal{T}_i} \epsilon_{\tau,i} \quad \forall \quad i$$
 (3)

where \mathcal{T}_i gives the set of relevant present value times τ for fund i. The cardinality $\operatorname{card}(\mathcal{T}_i)$ simply gives the number of present value dates used for the ith fund. The smallest possible set \mathcal{T}_i contains just a fund's starting date and the largest set contains all time periods bigger than the fund's starting date until now. The optimal set size of \mathcal{T} is studied by Monte Carlo simulations in subsection 3.3. Each fund i is characterized by its vintage year which can be expressed by $v_i = \min(\mathcal{T}_i) \in \{1, 2, \dots, V\}$, where V denotes the maximum vintage year used in a given data set. Finally, the scalar weighting factor w_i can be (i) one divided by the fund's invested capital for equal weighting of funds, (ii) one divided by the vintage year sum

of invested capital for vintage year weighting, (iii) the scalar one for fund-size weighting, or (iv) some macroeconomic deflator.

To find θ , our least-mean-distance estimator minimizes the average loss of $\bar{\epsilon}$

$$\hat{\theta} = \arg\min_{\theta \in \Theta} S_n(\theta) \quad \text{with} \quad S_n(\theta) = \frac{1}{n} \sum_{i=1}^n L(\bar{\epsilon}_i)$$
 (4)

where L denotes a loss function, e.g., $L(x) = (x - 0)^2$. Throughout the paper, the weighted average fund pricing error $\bar{\epsilon} \equiv \bar{\epsilon}(\theta)$ is regarded as nonlinear random function of the SDF parameter θ .

2.2 Cross-sectional unit: Individual fund vs. portfolio of funds

According to the classical value-additivity assumption in Hansen and Richard (1987) SDF models invariably shall hold for all pooled or unpooled assets. So in theory, it is not important if the test assets for our SDF are portfolio or individual fund cash flows. Practically it makes a difference and there are arguments both for and against portfolio formation.

In the risk premium literature, portfolio formation mainly helps to attenuate the errors-in-variable bias connected to two-pass asset pricing methods (Jegadeesh et al., 2019; Pukthuanthong et al., 2019). As this is no issue in our case, we could use individual funds. Cochrane (2011) argues that portfolio sorting (seen as an auxiliary nonparametric regression that imposes linearity on the relationship between returns and characteristics) shall be replaced by multivariate panel models due to the curse of dimensionality. Following the same nonparametric regression viewpoint, Cattaneo et al. (2019) derive a nonparametric framework where the optimal number of portfolios sorts acts as data-dependent tuning parameter that grows with sample size. Generally, the larger the portfolios, the easier any given SDF can price their cash flows since fewer test assets remain.

In the case of private equity funds, the pooling of fund cash flows helps to counter GP financial engineering², which might both change and mask the true risk profile of observed LP cash flows. Especially for private equity funds, portfolio formation based on vintage year is compelling due to its time-series-like indexing as done by Driessen et al. (2012). This procedure also offers large computational benefits as it drastically decreases the number of cross-sectional units. Further, as stated in Ang et al. (2020), portfolio formation allows more precise factor loading estimates due to decreasing idiosyncratic risk, but at the expense of sacrificing cross-sectional information. Finally, small (or fixed) T and large N set-ups may face finite sample problems (Raponi et al., 2020).

Assumption 1. For each vintage year, we pool fund cash flows to form n_v portfolios that serve as cross-sectional units. The two boundary cases are (i) single fund portfolios and (ii) just one portfolio per vintage year.

Without loss of generality, we refer to our cross-sectional units as funds although this is just a special case of a size- n_v -portfolio. In the simulation study in subsection 3.3 we compare both boundary cases (i) individual funds and (ii) vintage year portfolios.

²GPs may use bridge credit facilities below the hurdle rate to boost the fund's internal rate of return. This increases the probability of observing funds with only positive or only negative cash flows.

2.3 Asymptotic framework

To allow for multiple funds from the same vintage year in assumption 1, we employ an auxiliary 'spatial' notion as originally proposed by Korteweg and Nagel (2016). The spatial viewpoint is just a technical means to switch from time-series-like to a more panel-data-like indexing. Unlike typical panel data we do not follow multiple subjects over time, but for each point in time we exclusively observe multiple cross-sectional units (funds from that vintage year). This unusual two-dimensional indexing causes problems in the PE literature as it neatly fits neither in the (i) time-series, (ii) cross-sectional, nor (iii) panel data literature.

However, in this section, we basically follow the time-series asymptotic framework of Pötscher and Prucha (1997) since our 'spatial' distance measure is time and adaption to our case is thus straightforward. If we observe just one fund per vintage year (or, equivalently, form vintage year portfolios), it is easily seen that the framework of Pötscher and Prucha (1997) with time-series indexing can be directly applied (without any major modification).

2.3.1 Vintage year asymptotics

We assume that the ('spatial', i.e., economic) distance between cross-sectional units, i.e., private equity funds/portfolios, can be measured in a quantitative way. Here asymptotic results are derived for the case when the number of funds goes to infinity $n \to \infty$. However, to expose our SDF to enough distinct covariate realizations (economic conditions), identification of model parameters requires a sufficient number of funds from different vintage years in the fund-level data set used for model estimation as emphasized by Driessen et al. (2012) and Korteweg and Nagel (2016).

Assumption 2. (i) The number of vintage years $V \to \infty$ as $n \to \infty$. (ii) The number of funds per vintage year is bounded by some positive constant. (iii) The maximal fund lifetime is also bounded by a positive constant. (iv) The economic distance between fund i and j is measured by the vintage year difference $d_{i,j} = v_i - v_j$.

In terms of the spatial estimation literature, this assumption postulates increasing domain asymptotics and rules out so-called infill asymptotics. Infill asymptotics corresponds to the assumption of Driessen et al. (2012) that the number of funds per vintage tends to infinity.

2.3.2 Law of large numbers

The global moment condition underlying our estimation approach is that the expected value of $\bar{\epsilon}$ shall be zero, if we use the optimal SDF parameter θ_0 . This technically means, instead of applying a time-series law of large numbers, we rely on a spatial (cross-sectional) law of large numbers, but acknowledge the statistical dependence of pricing errors with respect to vintage year differences between funds.

Assumption 3. The (i) time-trend and (ii) dependence structure of $\bar{\epsilon}$ shall allow

$$n^{-1} \sum_{i=1}^{n} \overline{\epsilon}_i \stackrel{a.s.}{\to} E[\overline{\epsilon}] \quad as \quad V, n \to \infty$$

Specifically, we assume the process $\bar{\epsilon}$ to be is spatial near-epoch dependent with respect to fund vintage years (Jenish and Prucha, 2012), i.e., two funds with distance $d_{i,j} > D$ are assumed to be independent.

To satisfy the time trend part (i) of this law of large number assumption, the weighting factor w, introduced in equation 3, can be used to make $\bar{\epsilon}$ stationary. Spatial near-epoch dependence with respect to fund vintage years formalizes the simple idea that two fund pricing errors $\bar{\epsilon}$ with a small absolute vintage year difference are supposed to be dependent sine they are exposed to the same macroeconomic conditions; whereas two funds with a very large absolute vintage year difference can be assumed independent.

2.3.3 Consistency

The estimator $\hat{\theta}$ shall converge in probability to the true parameter value θ_0 as the number of distinct vintage years in our data set goes to infinity. Multiple funds for a specific vintage year are not necessarily required but, of course, provide additional information that should be exploited if available.

Assumption 4. Consistency of $\hat{\theta}$ requires $\hat{\theta} \stackrel{p}{\rightarrow} \theta_0$ as $V, n \rightarrow \infty$. Thus $E[\bar{\epsilon}] = 0$ if and only if $\theta = \theta_0$. The parameter space is compact $\theta \in \Theta$.

Compactness of Θ can be assured by lower and upper bounds for all parameters that can be justified by economic reasoning. In our case, e.g., a market beta factor of ten seems implausible for PE funds because of the implied risk and return expectations.

2.3.4 Central limit theorem

To assess the significance of our parameter estimates, we want to describe the asymptotic distribution of the parameter vector as a normal distribution.

Assumption 5. (i) $\sqrt{n}(\hat{\theta} - \theta_0) \stackrel{d}{\to} \mathcal{N}(0, \Sigma)$ as $V, n \to \infty$ with covariance matrix Σ . (ii) The covariance matrix Σ can be characterized by Pötscher and Prucha (1997, Theorem 11.2.b, Theorem H.1).

The formal proof of assumption 5 may be derived in analogy to the GMM case in (Jenish and Prucha, 2012, Theorem 4) that shows that the general structure of the Pötscher and Prucha (1997) framework also applies to the spatial near-epoch dependent case.

2.4 Large sample inference

In the time-series near-epoch-dependent least-mean-distance literature, Σ can be characterized according to Pötscher and Prucha (1997, Theorem 11.2.b, Theorem H.1):

$$\mathbf{\Sigma} = C^{-1} \Lambda (C^{-1})^{\top}$$

with expected Hessian matrix converging to C as $V, n \to \infty$

$$E\left(\nabla_{\theta\theta}S_n\right)\to C$$

and the expected covariance matrix of gradients converging to Λ as $V, n \to \infty$

$$nE\left[\nabla_{\theta}S_n(\nabla_{\theta}S_n)^{\top}\right] \to \Lambda$$

Here, the gradient vector $\nabla_{\theta} S_n$ is denoted as column vector. We define the corresponding finite sample estimators analogously to Pötscher and Prucha (1997, Chapters 12, 13.1), and numerically approximate the first and second partial derivatives by finite differences ($\delta \to 0$):

$$f_x(x,y) \approx \frac{f(x+\delta,y) - f(x-\delta,y)}{2\delta}$$

$$f_{xx}(x,y) \approx \frac{f(x+\delta,y) + f(x-\delta,y) - 2f(x,y)}{\delta^2}$$

$$f_{xy}(x,y) \approx \frac{f(x+\delta,y+\delta) + f(x-\delta,y-\delta) - f(x+\delta,y-\delta) - f(x-\delta,y+\delta)}{4\delta^2}$$

 \hat{C} is relatively straightforward

$$\hat{C} = \frac{1}{n} \sum_{i=1}^{n} \nabla_{\theta\theta} L(\epsilon_i)$$

Due to the spatial near-epoch dependence, the involved and computationally expensive part is to consistently estimate $\hat{\Lambda}$ by a Spatial Heteroskedasticity and Autocorrelation Consistent (SHAC) covariance matrix estimator (Kim and Sun, 2011, equation 2)

$$\hat{\Lambda} = \frac{1}{n} \sum_{i=1}^{n} \sum_{j=1}^{n} k_{i,j} \left[\nabla_{\theta} L\left(\epsilon_{i}\right) \left(\nabla_{\theta} L\left(\epsilon_{j}\right)\right)^{\top} \right]$$
(5)

We define the kernel weight k as

$$k_{i,j} \equiv K\left(\frac{d_{i,j}}{b_n}\right)$$

with kernel function $K: \mathbb{R} \to [0,1]$ satisfies K(0) = 1, K(x) = K(-x), $\int_{-\infty}^{\infty} K^2(x) dx < \infty$, and $K(\cdot)$ continuous at zero and at all but a finite number of other points. A common choice is the Bartlett kernel $K_{BT}(x) = \max(0, 1 - |x|)$; see equation 2.7 in Andrews (1991) for other popular kernel choices. This means, absolute vintage year differences larger than the bandwidth (or truncation) parameter $b_n = D$ are considered independent and are thus excluded from the $\hat{\Lambda}$ estimation formula.

In large samples, the vector of parameter standard errors can thus be estimated by

$$\operatorname{SE}(\hat{\theta}) = \sqrt{\operatorname{diag}\left[n^{-\frac{1}{2}}\hat{C}^{-1}\hat{\Lambda}(\hat{C}^{-1})^{\top}(n^{-\frac{1}{2}})^{\top}\right]} = \sqrt{\operatorname{diag}\left[\hat{C}^{-1}\hat{\Lambda}(\hat{C}^{-1})^{\top}\right] \cdot \frac{1}{n}}$$

However, in view of the limited amount of available private equity data (typically the oldest vintages start in the 1980s), asymptotic characterizations of Σ and $SE(\hat{\theta})$ are of limited importance. In empirical applications, the small sample behavior of an estimation method for private equity data is more relevant than its asymptotic theory. Moreover, the standard asymptotic distribution associated with an estimator is generally not valid for post-model-selection inference, i.e., if a model selection procedure is applied to find the best model from a collection of competitors (Leeb and Pötscher, 2005).

2.5 Comparison to similar estimators

Our least-mean-distance estimator developed in section 2.1 belongs to the class of semiparametric nonlinear M-estimators as defined in Pötscher and Prucha (1997). The estimator exhibits a cross-sectional nature since $S_n(\theta)$ in equation 4 takes the sample average with respect to funds rather than with respect to a vintage-year-based time-series. We intentionally opt against the most prominent semiparametric nonlinear M-estimator framework, i.e., classical time-series Generalized Method of Moments (GMM) (Hansen, 1982, 2012). A classical GMM approach requires the construction of stationary, ergodic time-series of moment conditions that are used to empirically estimate the expected value of pricing errors in equation 2. The stationarity requirement of classical time-series GMM restricts us with respect to (i) more elaborate weighting-schemes for w, like fund-size weighting, and (ii) the usage of fund cash flows from non-realized vintages.

The Driessen et al. (2012) approach is most closely related to our methodology. However, they regard vintage year portfolios as their cross-sectional units; we can also use individual funds. The Driessen et al. (2012) asymptotic theory assumes the number of funds (or deals) per vintage year portfolio to go to infinity. Our asymptotic theory lets both (i) the number of vintage years and (ii) the number of funds go to infinity, but bounds the number of funds per vintage year. Further, Driessen et al. (2012) discount all fund cash flows just to the first cash flow date (like in a classical net present value calculation). In contrast, we additionally average over all dates within \mathcal{T}_i to alleviate the exploding alpha issue briefly mentioned in their paper (and more thoroughly so in an earlier working paper version). Although Driessen et al. (2012) describe their estimator as a one-step GMM approach, we consider it as special case of our least-mean-distance estimator. Specifically, if someone accepts the assumptions from subsection 2.3, our large sample inference framework from subsection 2.4 applies to their case without any significant modification.

Korteweg and Nagel (2016) first of all realized the usefulness of employing an auxiliary spatial framework to handle a fund-level panel dataset of private equity funds. They measure the economic distance between two private equity funds (by the degree of cash flow overlap) to account for the cross-sectional dependence between funds. Concretely, their asymptotic inference framework draws on the spatial HAC estimator of Conley (1999). However, they ultimately utilize a classical GMM estimator, thus a time-series law of large numbers. Timeseries GMM estimators inherently bear the risk of under-identification, if the corresponding time-series is constructed by pooling all fund cash flows from a given fund type. To counter under-identification, additional characteristic based fund portfolios could be used to increase the number of moment conditions per fund type; also random portfolios in combination with bootstrapping make sense. Yet, Korteweg and Nagel (2016) take another approach and introduce the concept of Generalized Public Market Equivalent (GPME) which elegantly avoids the under-identification issue. Firstly, a public market SDF model is estimated by pricing public trading strategies that shall replicate PE funds instead of directly pricing the observed PE fund cash flows. Only in a second step, these public market SDF models are applied to evaluate private equity fund cash flows.

3 Empirical application

3.1 Data

We use the Preqin cash flow data set as of 26th February 2020. We pool all regions and analyze the following fund types (using the Preqin asset class classification): PE ("Private Equity"; 2248 distinct funds in data set), VC ("Venture Capital"; 871), RE ("Real Estate"; 742), PD ("Private Debt"; 441), INF ("Infrastructure", 144), NR ("Natural Resources", 138). For these fund types we extract all (i) equal-weighted and (ii) fund-size-weighted cash flow series. For non-liquidated funds we treat the latest net asset value as final cash flow. We explicitly refrain from excluding the most recent vintage years.

The public market factors that enter our SDF draw on the US data set of the recently popularized q^5 investment factor model sourced from http://global-q.org/factors.html (Hou et al., 2015, 2020). Their five factor model includes: MKT the market excess return, ME the size factor, IA the investment factor, ROE the return on equity factor, and EG the expected growth factor.

3.2 Model and estimator specifications

We test a simple linear SDF model as in Driessen et al. (2012)

$$\Psi_{\tau,t}^{SL}(\theta) = \prod_{h=0}^{t} \left(1 + \alpha + r_h + \sum_{j} \beta_j F_{j,h} \right)^{-1} \prod_{h=0}^{\tau} \left(1 + \alpha + r_h + \sum_{j} \beta_j F_{j,h} \right)$$
 (6)

and an exponential affine SDF model adapted from Korteweg and Nagel (2016)

$$\Psi_{\tau,t}^{\text{EA}}(\theta) = \exp\left[-\sum_{h=\tau}^{t} \left(\alpha + \log(1+r_h) + \sum_{j\in J} \beta_j \cdot \log(1+F_{j,h})\right)\right]$$
(7)

with (arithmetic) risk-free return r, (arithmetic) zero-net-investment portfolio returns F_j , and parameter vector $\theta = (\alpha, \beta)$. To avoid overfitting, we just test six simple SDF models that contain {MKT} alone or {MKT} plus {ME or IA or ROE or EG or Alpha}. In equation 4, we use the quadratic loss function $L(x) = x^2$.

To assess the parameter significance, we compute the asymptotic standard errors as outlined in subsection 2.4. The Bartlett kernel's bandwidth $b_n = D$ is selected as 12 years, i.e., funds with absolute vintage year differences larger than 12 years are assumed to be independent.

Additionally, we want to test the finite - or more honestly small - sample parameter significance and the out-of-sample performance of our SDF models. Here we draw on hv-block cross validation to account for the dependency between funds from adjacent vintage years caused by overlapping fund cash flows (Racine, 2000). Therefore, we form three partitions for several vintage year groups. As larger validation sets are preferred for model selection, the validation set (v-block) always contains funds of three neighboring vintage years (e.g. 2000, 2001, 2002). To reduce the dependency between training and validation set, we remove all funds from three-year-adjacent vintage years, i.e., the h-block (e.g. 1997, 1998, 1999, 2003,

2004, 2005). Funds from the remaining vintage years enter the training set and are thus used for model estimation (e.g. 1985-1996, 2006-2019). We apply ten-fold cross validation using the ten validation sets described in table 1. This means, we replace the bootstrap standard error calculation of Driessen et al. (2012) by hv-block cross validation since the new method focuses directly on the out-of-sample performance of the SDF models and, in addition to it, is computationally cheaper.

training.before	h.block.before	v.block	h.block.after	training.after
estimation	remove	validation	remove	estimation
start-1984	1985,1986,1987	1988,1989,1990	1991,1992,1993	1994-end
start-1987	1988,1989,1990	1991,1992,1993	1994,1995,1996	1997-end
start-1990	1991,1992,1993	1994,1995,1996	1997,1998,1999	2000-end
start-1993	1994,1995,1996	1997,1998,1999	2000,2001,2002	2003-end
start-1996	1997,1998,1999	2000,2001,2002	2003,2004,2005	2006-end
start-1999	2000,2001,2002	2003,2004,2005	2006,2007,2008	2009-end
start-2002	2003,2004,2005	2006,2007,2008	2009,2010,2011	2012-end
start-2005	2006,2007,2008	2009,2010,2011	2012,2013,2014	2015-end
start-2008	2009,2010,2011	2012,2013,2014	2015,2016,2017	2018-end
start-2011	2012,2013,2014	2015,2016,2017	2018,2019,2020	2021-end

Table 1: Partitions used for hv-block cross validation.

3.3 Simulation study

Our Monte Carlo experiments examine the following questions related to the bias and variance of our estimation methodology in finite samples. Is it beneficial to use vintage year portfolios instead of individual funds? Which SDF model performs better when we also use the corresponding data generating process (i.e., assume correct model specification)? How is estimator precision affected by varying numbers of vintage years or cross-sectional units? Which is the optimal set of present value times \mathcal{T} ?

We use historical q-investment factors from period 1986 to 2005 and simulate 20 funds for each of these 20 vintage years. Each fund contains 15 deals with equal investment amounts and exactly one divestment cash flow. Deals are entered within the first five years of fund lifetime following a discrete uniform distribution and afterwards held between one to ten years again uniformly distributed. The deal returns are generated by the simple linear or exponential affine SDF models described in equations 6 and 7. In the base case, we just use the MKT factor with $\beta_{\text{MKT}} = 1$ and in each month add a normal i.i.d. error term with standard deviation $\sigma = 0.2$ and zero mean. Additionally, we test an intercept term α of -0.25% per month and a high β_{MKT} of 2.5. In the exponential affine case, we adjust the log-normally distributed error mean to zero by subtracting $0.5\sigma^2$. If a negative return exceeds -100%, the company defaults with a zero exit cash flow. In contrast, the error term in the simulations of Driessen et al. (2012) is more well-behaved as it follows a shifted lognormal distribution that, even with arbitrarily high error term variance, just allows for returns below say -99%, if the market return is close to its lower bound (see equation 9

in their online appendix). In our base case, the set of present value dates \mathcal{T} contains all months from the first cash flow to maximum month 180. To assess the bias and variance of our estimator, we simulate 1,000 test scenarios for vintage year portfolios and just 200 test cases when using individual funds due to memory restrictions.

Cross-sectional unit i: As presumed in subsection 2.2, vintage year portfolio results appear to have lower bias and variance when compared to individual funds. For the simple linear SDF and maximum month 180, the mean and standard deviation of the coefficient estimate $\hat{\beta}_{\text{MKT}}$ is 1.016 (0.2) for the vintage year portfolio and 1.096 (0.376) for individual funds. However, for individual funds we just simulate 200 iterations due to the high computational cost.

SDF model Ψ : In our base case with vintage year portfolios, the exponential affine SDF shows a mean and standard deviation of 1.011 (0.175) compared to the 1.016 (0.2) achieved by the simple linear SDF. Generally, the exponential affine SDF model and the simple linear SDF model exhibit similar bias and variance when comparing panels A and B in table 4. This indicates that the results are not overly sensitive to the choice of SDF model.

Moreover, the perceived superiority of exponential affine SDFs is probably rather theoretical than practical as other proponents also emphasize their universality mainly from a mathematical perspective without providing supportive empirical or simulation results (Gourieroux and Monfort, 2007; Bertholon et al., 2008).

Varying vintages V and portfolio sizes n/V: To test the effect of varying data sizes available for MKT factor estimation, we in/decrease the (i) number of vintage years and (ii) the number of funds per vintage year (cf. table 2). Here we use vintage year portfolios and the simple linear SDF. Increasing the number of deals/funds per vintage year portfolio appears to decrease the estimator's variance more effectively than adding more vintage years. However, the bias is almost the same for all tested specifications. Generally, we seem to need many new data points to assure a reasonable variance of our estimator.

	Base	Big n/V	$\mathrm{Big}\ V$	$\mathrm{Big}\ V$	Small V	Small V
Start vintage	1986	1986	1967	1967	1986	1996
End vintage	2005	2005	2005	2005	1995	2005
#Funds per vintage	20	40	10	20	20	20
Mean β_{MKT}	1.011	1.020	0.993	1.015	1.027	0.934
Stdv β_{MKT}	0.187	0.133	0.263	0.227	0.232	0.418

Table 2: Simulation study for varying number of vintages and number of funds per vintage with true $\beta_{\text{MKT}} = 1$, maximum month 180, and 500 simulation iterations.

Size of set \mathcal{T} : The results in table 4 indicate that we can control the bias by an appropriate choice of the set \mathcal{T} . The bias almost vanishes when we average over all present value dates in the maximal fund lifetime of 180 months. For smaller or larger sets for \mathcal{T} we find increasing

bias. As outlined in the online appendix, this also holds when we reduce the maximal fund lifetime to 10 years; in this case, the smallest bias is obtained for maximum month 120.

In table 4 for both true and false model specifications, the α standard deviation is very high compared to its mean value. This may indicate it is rather delicate to empirically determine private equity's historical outperformance by our semiparametric estimator.

To conclude, our simulations study rationalizes two key practices from the Driessen et al. (2012) paper: (i) vintage year portfolio formation helps to improve estimator precision and (ii) increasing the number of funds per vintage seems to be more effective in controlling estimator variance that increasing the number of vintages³. However, our examples with correct specification cannot support the assumption of Korteweg and Nagel (2016) that (iii) the exponential affine SDF is (clearly) superior to the simple liner SDF in a multi-period framework; actually their bias and variances are quite equal. Moreover, our simulation study suggests that (iv) averaging pricing errors over multiple dates strikingly reduces the bias inherent to the original procedure of Driessen et al. (2012) that just discounts all cash flows to the fund inception date. Actually, choosing the set \mathcal{T} according to the fund lifetime seems to decrease the bias (and to a lesser extend also the variance) more effectively than all other measures combined.

3.4 Empirical results

Following the conclusions from the previous subsection, we use vintage year portfolios to estimate simple linear SDF models with maximum month 180. Asymptotic inference results for the full dataset are exhibited in table 5 for fund-size weighting and in table 7 for equal weighting. The results for hv-block cross-validation are displayed in table 6 for fund-size weighting and in table 8 for equal weighting. We generally analyze the results in a two step procedure: For a given model specification, we use the cross-validation error (i.e., the average out-of-sample error) to select the best model for each fund type, but analyze the corresponding coefficient estimates from the asymptotic inference tables (estimated on the total data set). Therefore, for each fund type the SDF models in the asymptotic inference tables 5 and 7 are sorted by the corresponding cross-validation error. Throughout this subsection, we define the statistical significance of coefficient estimates in terms of a t-ratio $\hat{\theta}[SE(\hat{\theta})]^{-1}$ greater than 1.96.

Table 3 helps to get a rough overview over tables 5 to 8 as it summarizes their absolute column means. We see that the standard errors (SEs) implied by hv-block cross-validation are considerably smaller than the asymptotic results. Just looking at asymptotic standard errors, fund-size weighting exhibits substantially larger SEs than fund equal-weighting. Assuming independence between funds from different vintages decreases asymptotic SEs by approximately 30-40% when compared to a realistic kernel bandwidth of D = 12. But even these independent SEs rarely imply statistical significance coefficient estimates with t-ratios bigger than 1.96. In table 5 with fund-size weighting, just one out of 36 models exhibit significant MKT and second factor estimates. In the case of equal-weighting, table 7 also

³Finding (ii) may explain the choice of Driessen et al. (2012) to employ an asymptotic law that lets the number of deals/funds per vintage tend to infinity.

	MKT F	actor		2nd Fac	etor		
	Estim.	SE	SE.indep	Estim.	SE	SE.indep	Weighting
AI	0.75	27.06	19.73	0.80	28.95	20.94	FW_VYP_SL
CV	0.85	0.38		0.59	0.51		FW_VYP_SL
AI	0.76	26.75	16.16	0.76	11.25	6.69	EW_VYP_SL
CV	0.84	0.34		0.62	0.50		EW_VYP_SL

Table 3: Top-level overview over tables 5 to 8: Averages of absolute coefficient estimates and standard errors.

shows just one significant models out of 36.

In summary, the results reveal very weak two-factor models with MKT plus a second q-investment factor. As also the simulation results from the previous subsection indicate rather high variance associated with our semiparametric estimator (given the amount of data typically available), we recommend to focus on single MKT factor models even when their asymptotic t-ratios are below 1.96. At least the hv-block cross validation results imply significant one-factor MKT models for fund types PE, VC, PD, INF. In contrast, RE is just significant for equal-weighting and NR is insignificant for both weighting schemes.

Focus on PE and VC Here, we briefly summarize the one-factor MKT and the two-factor Alpha model estimates for fund types PE (i.e., mainly Buyout and Growth) and VC. For PE, all one-factor MKT model β_{MKT} estimates fall in the range from 1.13 to 1.28. If we add an α term, all β_{MKT} estimates decrease to the range 0.61 to 0.77 with annualized α coefficients of approximately positive 4-5% per year. For VC, the one-factor MKT model β_{MKT} estimates are in the range from 0.80 to 1.14. If we add an α term, all β_{MKT} estimates strongly increase to the range 1.81 to 2.06 with annualized α coefficients of approximately negative 6-7% per year. These results at least weakly indicate - given the insignificant asymptotic standard errors - that PE funds outperform public markets with a market beta coefficient of less than one which suggest low market risk. On the other hand, VC underperforms public markets with market beta coefficients of roughly two which implies high market risk.

4 Conclusion

Theoretically, our least-mean-distance estimator can be easily generalized to estimate SDF models for all kinds of non-traded cash flows. If in data-rich environments asymptotic inference is deemed prudent, the economic distance measure essential for SHAC estimation can include multiple dimensions, e.g., temporal, geographic, and industry sector proximity.

Practically, in the data-sparse private equity domain, we strongly advise to always challenge asymptotic inference results by resampling or cross-validation techniques that are adapted to the dependency structure of overlapping fund cash flows. However, even their conclusions should be double-checked, to avoid unreasonable instances, e.g., where hv-block cross-validation chooses dubious models with negative MKT factor estimates.

Semiparametric estimators commonly exhibit problematic small sample behavior. In accordance, our simulation results prompt us to conclude that the closely related Driessen

et al. (2012) estimator may exhibit more bias and variance than assumed in the original paper. Fortunately, at least the bias can be easily reduced by averaging pricing errors over all dates within the fund lifetime. Given the amount of currently available data, the fund-level data generating process still seems to be too complex for naive semiparametric estimators like the one analyzed in this paper. Since (basically) all two-factor models' asymptotic standard errors appear statistically insignificant in our empirically analyses, we conjecture that our SDF method shall be exclusively used for a single-MKT-factor SDF until considerably more vintage year information for private equity funds is available.

If someone wants to estimate more complex SDF models that incorporate additional factors, more structure is needed. This can be parametric assumptions for the data generating process (Ang et al., 2018) or to extract additional information from intermediate net asset values (Gredil et al., 2019; Brown et al., 2020). A first 'modern' approach to the same problem is the application of machine learning techniques that regularize/shrink all coefficients other than the MKT factor. Secondly, given the high estimator variance revealed in the simulation study, machine learning methods that create a strong learner by combining multiple weak learners seem also worth considering (boosting, bagging, model averaging).

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1 - stdv 0.269 2792 9.968 0.342 866 13.347 60 - mean 1.129 0.138 0.933 2.103 -0.086 2.285 60 - stdv 0.242 0.245 0.363 0.302 0.253 0.406 120 - mean 1.058 0.112 0.906 2.063 -0.085 2.239
60 - mean 1.129 0.138 0.933 2.103 -0.086 2.285 60 - stdv 0.242 0.245 0.363 0.302 0.253 0.406 120 - mean 1.058 0.112 0.906 2.063 -0.085 2.239
60 - stdv 0.242 0.245 0.363 0.302 0.253 0.406 120 - mean 1.058 0.112 0.906 2.063 -0.085 2.239
120 - mean 1.058 0.112 0.906 2.063 -0.085 2.239
120 - stdv 0.200 0.214 0.313 0.253 0.239 0.385
180 - mean 1.016 0.041 0.965 2.052 -0.161 2.370
180 - stdv 0.200 0.172 0.334 0.277 0.173 0.403
240 - mean 0.987 -0.053 1.077 2.072 -0.277 2.589
240 - stdv 0.223 0.162 0.361 0.326 0.118 0.375
300 - mean 0.946 -0.149 1.175 2.080 -0.357 2.714
300 - stdv 0.235 0.174 0.377 0.398 0.114 0.366
360 - mean 0.895 -0.245 1.269 2.048 -0.461 2.859
360 - stdv 0.268 0.201 0.399 0.551 0.140 0.386
Panel B: exponential affine SDF
MaxMonth $\beta = 1$ $\alpha = 0$ $\beta = 1$ $\beta = 2.5$ $\alpha = -0.25$ $\beta = 2.5$
1 - mean 1.207 203 1.276 2.256 692 1.704
1 - stdv 0.344 314 0.710 0.290 13 1.666
60 - mean 1.146 0.126 0.941 2.264 -0.018 2.277
60 - stdv 0.275 0.264 0.386 0.256 0.370 0.473
120 - mean 1.062 0.107 0.908 2.221 0.009 2.205
120 - stdv 0.200 0.237 0.333 0.187 0.357 0.448
180 - mean 1.011 0.027 0.971 2.182 -0.136 2.358
180 - stdv 0.175 0.211 0.366 0.168 0.344 0.505
240 - mean 0.972 -0.088 1.095 2.144 -0.441 2.723
240 - stdv 0.174 0.224 0.406 0.178 0.317 0.503
300 - mean 0.928 -0.202 1.203 2.083 -0.717 2.985
300 - stdv 0.181 0.253 0.426 0.254 0.340 0.513
360 - mean 0.874 -0.319 1.304 1.685 -1.095 3.272
360 - stdv 0.208 0.291 0.447 0.772 0.374 0.586

Table 4: Simulation study to compare the simple linear with the exponential affine SDF and to determine the optimal size of the set \mathcal{T} . Here we always use vintage year portfolios and 1000 simulation iterations. For better readability, $\beta_{\text{MKT}} = \beta$ and all monthly α values are multiplied by 100.

	MKT F	actor a		2nd Factor			
Type	Estim.	SE	SE.indep	Factor	Estim.	SE	SE.indep
PE	0.709	2.470	1.153	EG	0.807	4.693	1.960
PE	0.770	7.976	3.348	ROE	1.540	5.140	3.499
PE	1.126	1.003	0.868	MKT	1.126	1.003	0.868
PE	0.644	1.234	0.585	Alpha	0.003	0.036	0.013
PE	1.121	1.023	0.897	ME	0.074	2.021	0.915
PE	1.158	1.125	1.068	IA	-0.338	2.499	1.259
VC	1.053	4.150	2.733	IA	-1.959	2.100	1.767
VC	1.114	3.861	2.894	ME	-1.383	5.102	2.211
VC	1.806	11.391	4.279	Alpha	-0.006	0.124	0.046
VC	0.801	704.455	561.598	MKT	0.801	704.455	561.598
VC	1.429	8.073	3.219	ROE	-1.306	18.055	6.919
VC	1.507	17.322	6.966	EG	-0.904	15.344	5.737
PD	0.885	1.040	1.242	MKT	0.885	1.040	1.242
PD	0.660	0.095	0.039	Alpha	0.002	0.001	0.000
PD	0.826	1.707	1.443	EG	0.143	20.341	7.506
PD	0.849	2.921	2.146	ME	0.301	2.739	1.518
PD	0.887	1.378	1.244	ROE	-0.023	6.925	2.553
PD	0.863	2.942	2.224	IA	0.247	5.306	3.607
$\overline{\mathrm{RE}}$	0.578	1.827	1.196	MKT	0.578	1.827	1.196
RE	1.303	5.463	2.259	Alpha	-0.006	0.088	0.034
RE	0.200	2.598	1.356	ROE	3.118	2.579	6.629
RE	0.202	3.297	1.965	EG	0.844	2.478	1.828
RE	0.756	3.043	2.192	IA	-1.938	1.879	0.783
RE	0.887	1.167	0.858	ME	-2.059	1.300	0.563
NR	-0.215	2.367	1.976	EG	0.909	14.505	7.475
NR	0.191	3.136	4.242	MKT	0.191	3.136	4.242
NR	-0.674	58.003	24.234	Alpha	0.008	0.230	0.098
NR	-0.020	0.954	2.210	ROE	1.128	4.830	5.066
NR	0.143	3.236	4.116		-0.768	1.808	2.154
NR	0.212	4.209	5.450	ME	-0.575	1.603	1.252
INF	0.824	3.201	2.815	MKT	0.824	3.201	2.815
INF	0.190	7.133	3.288	Alpha	0.005	0.030	0.025
INF	0.317	23.904	10.658	EG	0.848	45.836	20.176
INF	0.470	9.316	4.237	ROE	1.245	5.531	6.134
INF	0.778	5.951	5.424	ME	-0.811	3.712	4.349
INF	0.661	61.329	33.819	IA	-1.108	150.713	85.733

Table 5: Asymptotic inference with FW-VYP-SL max month 180, and D=12.

	MKT I	Factor				
Type	Mean	SD	Factor	Mean	SD	CV-error
PE	0.867	0.276	EG	0.720	0.137	112808.000
PE	0.927	0.305	ROE	1.375	0.420	126801.000
PE	1.276	0.296	MKT	1.276	0.296	151964.000
PE	0.772	0.238	Alpha	0.004	0.002	154805.000
PE	1.317	0.396	ME	0.236	0.664	209319.000
PE	1.311	0.370	IA	0.014	0.703	210650.000
$\overline{\text{VC}}$	1.045	0.126	IA	-1.890	0.238	11858.000
VC	1.172	0.126	ME	-1.448	0.263	13301.000
VC	1.930	0.356	Alpha	-0.005	0.001	17723.000
VC	0.804	0.363	MKT	0.804	0.363	21852.000
VC	1.527	0.517	ROE	-0.972	0.679	26680.000
VC	1.646	0.678	EG	-0.644	0.556	32730.000
PD	0.887	0.039	MKT	0.887	0.039	7368.000
PD	0.567	0.202	Alpha	0.003	0.001	7917.000
PD	0.763	0.113	EG	0.229	0.141	8758.000
PD	0.862	0.103	ME	0.342	0.256	9834.000
PD	0.812	0.153	ROE	0.258	0.394	11522.000
PD	0.914	0.211	IA	0.472	0.424	18096.000
RE	0.722	0.392	MKT	0.722	0.392	50900.000
RE	1.288	0.345	Alpha	-0.004	0.005	51437.000
RE	0.389	0.446	ROE	2.333	1.507	54689.000
RE	0.465	0.470	EG	0.448	0.629	59316.000
RE	0.847	0.411	IA	-1.262	1.160	65835.000
RE	0.983	0.350	ME	-1.467	1.298	66827.000
NR	-0.047	0.421	EG	0.657	0.557	10559.000
NR	0.318	0.321	MKT	0.318	0.321	11480.000
NR	-0.335	0.763	Alpha	0.006	0.005	11854.000
NR	0.136	0.466	ROE	0.844	1.062	13296.000
NR	0.270	0.508	IA	-0.288	1.124	14479.000
NR	0.416	0.587	ME	0.032	1.079	15789.000
INF	0.862	0.320	MKT	0.862	0.320	14551.000
INF	0.639	0.753	Alpha	0.002	0.004	15069.000
INF	0.766	0.626	EG	0.258	0.495	16004.000
INF	0.837	0.504	ROE	0.090	0.939	18472.000
INF	0.868	0.412	ME	0.078	0.643	18514.000
INF	0.892	0.561	IA	0.081	1.073	23162.000

Table 6: hv-block cross-validation with FW-VYP-SL weighting and max month 180.

Type Estim. SE SE.indep Factor Estim. SE SE.indep PE 0.775 0.638 0.550 EG 0.667 5.558 2.125 PE 0.610 1.064 0.387 Alpha 0.004 0.006 0.002 PE 0.826 20.352 8.308 ROE 1.087 33.514 12.143 PE 1.146 1.001 0.638 IA -0.386 1.909 0.813 PE 1.144 1.048 0.702 ME -0.014 1.797 0.736 VC 1.181 24.418 16.693 ME -1.277 4.928 4.352 VC 1.137 7.259 6.057 IA -1.553 3.716 2.139 VC 1.138 1.819 1.520 Alpha -0.006 0.335 0.117 VC 1.034 2.205 1.758 MKT 1.034 2.205 1.758 VC 1.488 </th <th></th> <th>MKT F</th> <th>actor</th> <th></th> <th colspan="4">2nd Factor</th>		MKT F	actor		2nd Factor			
PE 0.610 1.064 0.387 Alpha 0.004 0.006 0.002 PE 0.826 20.352 8.308 ROE 1.087 33.514 12.143 PE 1.134 1.050 0.694 MKT 1.134 1.050 0.694 PE 1.146 1.001 0.638 IA -0.386 1.909 0.813 PE 1.134 1.048 0.702 ME -0.014 1.797 0.736 VC 1.181 24.418 16.693 ME -1.277 4.928 4.352 VC 1.956 4.189 1.520 Alpha -0.006 0.335 0.117 VC 1.956 4.189 1.520 Alpha -0.006 0.335 0.117 VC 1.956 4.189 1.520 Alpha -0.006 0.335 0.117 VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.535<	Type	Estim.	SE	SE.indep	Factor	Estim.	SE	SE.indep
PE 0.826 20.352 8.308 ROE 1.087 33.514 12.143 PE 1.134 1.050 0.694 MKT 1.134 1.050 0.694 PE 1.146 1.001 0.638 IA -0.386 1.909 0.813 PE 1.134 1.048 0.702 ME -0.014 1.797 0.736 VC 1.181 24.418 16.693 ME -1.277 4.928 4.352 VC 1.137 7.259 6.057 IA -1.553 3.716 2.139 VC 1.956 4.189 1.520 Alpha -0.006 0.335 0.117 VC 1.034 2.205 1.758 MKT 1.034 2.205 1.758 VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.535 2.821 1.336 EG -0.754 3.626 1.260 PD 0.844	PE	0.775	0.638	0.550	EG	0.667	5.558	2.125
PE 1.134 1.050 0.694 MKT 1.134 1.050 0.694 PE 1.146 1.001 0.638 IA -0.386 1.909 0.813 PE 1.134 1.048 0.702 ME -0.014 1.797 0.736 VC 1.181 24.418 16.693 ME -1.277 4.928 4.352 VC 1.137 7.259 6.057 IA -1.553 3.716 2.139 VC 1.956 4.189 1.520 Alpha -0.006 0.335 0.117 VC 1.034 2.205 1.758 MKT 1.034 2.205 1.758 VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.535 2.821 1.336 EG -0.754 3.626 1.265 PD 0.844	PE	0.610	1.064	0.387	Alpha	0.004	0.006	0.002
PE 1.146 1.001 0.638 IA -0.386 1.909 0.813 PE 1.134 1.048 0.702 ME -0.014 1.797 0.736 VC 1.181 24.418 16.693 ME -1.277 4.928 4.352 VC 1.137 7.259 6.057 IA -1.553 3.716 2.139 VC 1.956 4.189 1.520 Alpha -0.006 0.335 0.117 VC 1.034 2.205 1.758 MKT 1.034 2.205 1.758 VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.535 2.821 1.336 EG -0.754 3.626 1.260 PD 0.844 1.245 0.856 MKT 0.03 0.000 0.000 PD 0.791 2.478 1.557 ROE 0.222 5.024 1.966 PD 0.736	PE	0.826	20.352	8.308	ROE	1.087	33.514	12.143
PE 1.134 1.048 0.702 ME -0.014 1.797 0.736 VC 1.181 24.418 16.693 ME -1.277 4.928 4.352 VC 1.137 7.259 6.057 IA -1.553 3.716 2.139 VC 1.956 4.189 1.520 Alpha -0.006 0.335 0.117 VC 1.034 2.205 1.758 MKT 1.034 2.205 1.758 VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.535 2.821 1.336 EG -0.754 3.626 1.260 PD 0.844 1.245 0.856 MKT 0.844 1.245 0.856 PD 0.791 2.478 1.557 ROE 0.222 5.024 1.966 PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844	PE	1.134	1.050	0.694	MKT	1.134	1.050	0.694
VC 1.181 24.418 16.693 ME -1.277 4.928 4.352 VC 1.137 7.259 6.057 IA -1.553 3.716 2.139 VC 1.956 4.189 1.520 Alpha -0.006 0.335 0.117 VC 1.034 2.205 1.758 MKT 1.034 2.205 1.758 VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.535 2.821 1.336 EG -0.754 3.626 1.260 PD 0.844 1.245 0.856 MKT 0.844 1.245 0.856 PD 0.502 0.044 0.015 Alpha 0.003 0.000 0.000 PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833	PE	1.146	1.001	0.638	IA	-0.386	1.909	0.813
VC 1.137 7.259 6.057 IA -1.553 3.716 2.139 VC 1.956 4.189 1.520 Alpha -0.006 0.335 0.117 VC 1.034 2.205 1.758 MKT 1.034 2.205 1.758 VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.535 2.821 1.336 EG -0.754 3.626 1.260 PD 0.844 1.245 0.856 MKT 0.844 1.245 0.856 PD 0.502 0.044 0.015 Alpha 0.003 0.000 0.000 PD 0.791 2.478 1.557 ROE 0.222 5.024 1.966 PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833	PE	1.134	1.048	0.702	ME	-0.014	1.797	0.736
VC 1.956 4.189 1.520 Alpha -0.006 0.335 0.117 VC 1.034 2.205 1.758 MKT 1.034 2.205 1.758 VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.535 2.821 1.336 EG -0.754 3.626 1.260 PD 0.844 1.245 0.856 MKT 0.844 1.245 0.856 PD 0.502 0.044 0.015 Alpha 0.003 0.000 0.000 PD 0.791 2.478 1.557 ROE 0.222 5.024 1.966 PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833 1.978 1.362 ME 0.323 1.845 0.986 RE 0.743 <	VC	1.181	24.418	16.693	ME	-1.277	4.928	4.352
VC 1.034 2.205 1.758 MKT 1.034 2.205 1.758 VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.535 2.821 1.336 EG -0.754 3.626 1.260 PD 0.844 1.245 0.856 MKT 0.844 1.245 0.856 PD 0.502 0.044 0.015 Alpha 0.003 0.000 0.000 PD 0.791 2.478 1.557 ROE 0.222 5.024 1.966 PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833 1.978 1.362 ME 0.323 1.845 0.986 RE 0.743 3.471 2.075 MKT 0.743 3.471 2.075 RE 1.265	VC	1.137	7.259	6.057	IA	-1.553	3.716	2.139
VC 1.488 1.801 0.941 ROE -1.148 4.060 1.424 VC 1.535 2.821 1.336 EG -0.754 3.626 1.260 PD 0.844 1.245 0.856 MKT 0.844 1.245 0.856 PD 0.502 0.044 0.015 Alpha 0.003 0.000 0.000 PD 0.791 2.478 1.557 ROE 0.222 5.024 1.966 PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833 1.978 1.362 ME 0.323 1.845 0.986 RE 0.743 3.471 2.075 MKT 0.743 3.471 2.075 RE 1.265 7.581 3.331 Alpha -0.004 0.046 0.017 RE 0.145 <	VC	1.956	4.189	1.520	Alpha	-0.006	0.335	0.117
VC 1.535 2.821 1.336 EG -0.754 3.626 1.260 PD 0.844 1.245 0.856 MKT 0.844 1.245 0.856 PD 0.502 0.044 0.015 Alpha 0.003 0.000 0.000 PD 0.791 2.478 1.557 ROE 0.222 5.024 1.966 PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833 1.978 1.362 ME 0.323 1.845 0.986 RE 0.743 3.471 2.075 MKT 0.743 3.471 2.075 RE 1.265 7.581 3.331 Alpha -0.004 0.046 0.017 RE 0.145 3.486 1.614 ROE 3.202 17.447 7.413 RE 0.400 <	VC	1.034	2.205	1.758	MKT	1.034	2.205	1.758
PD 0.844 1.245 0.856 MKT 0.844 1.245 0.856 PD 0.502 0.044 0.015 Alpha 0.003 0.000 0.000 PD 0.791 2.478 1.557 ROE 0.222 5.024 1.966 PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833 1.978 1.362 ME 0.323 1.845 0.986 RE 0.743 3.471 2.075 MKT 0.743 3.471 2.075 RE 1.265 7.581 3.331 Alpha -0.004 0.046 0.017 RE 0.145 3.486 1.614 ROE 3.202 17.447 7.413 RE 0.400 50.493 31.818 EG 0.700 48.813 29.195 RE 0.884	VC	1.488	1.801	0.941	ROE	-1.148	4.060	1.424
PD 0.502 0.044 0.015 Alpha 0.003 0.000 0.000 PD 0.791 2.478 1.557 ROE 0.222 5.024 1.966 PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833 1.978 1.362 ME 0.323 1.845 0.986 RE 0.743 3.471 2.075 MKT 0.743 3.471 2.075 RE 1.265 7.581 3.331 Alpha -0.004 0.046 0.017 RE 0.145 3.486 1.614 ROE 3.202 17.447 7.413 RE 0.400 50.493 31.818 EG 0.700 48.813 29.195 RE 0.884 4.928 2.813 ME -1.782 1.474 0.605 RE 0.795	VC	1.535	2.821	1.336	EG	-0.754	3.626	1.260
PD 0.791 2.478 1.557 ROE 0.222 5.024 1.966 PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833 1.978 1.362 ME 0.323 1.845 0.986 RE 0.743 3.471 2.075 MKT 0.743 3.471 2.075 RE 1.265 7.581 3.331 Alpha -0.004 0.046 0.017 RE 0.145 3.486 1.614 ROE 3.202 17.447 7.413 RE 0.400 50.493 31.818 EG 0.700 48.813 29.195 RE 0.884 4.928 2.813 ME -1.782 1.474 0.605 RE 0.795 18.146 10.282 IA -1.712 13.199 7.657 NR 0.000	PD	0.844	1.245	0.856	MKT	0.844	1.245	0.856
PD 0.736 2.230 1.303 EG 0.213 6.296 2.374 PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833 1.978 1.362 ME 0.323 1.845 0.986 RE 0.743 3.471 2.075 MKT 0.743 3.471 2.075 RE 1.265 7.581 3.331 Alpha -0.004 0.046 0.017 RE 0.145 3.486 1.614 ROE 3.202 17.447 7.413 RE 0.400 50.493 31.818 EG 0.700 48.813 29.195 RE 0.884 4.928 2.813 ME -1.782 1.474 0.605 RE 0.795 18.146 10.282 IA -1.712 13.199 7.657 NR -0.056 3.693 1.897 ROE 1.934 3.154 2.287 NR 0.425	PD	0.502	0.044	0.015	Alpha	0.003	0.000	0.000
PD 0.844 1.150 0.837 IA 0.076 2.543 1.416 PD 0.833 1.978 1.362 ME 0.323 1.845 0.986 RE 0.743 3.471 2.075 MKT 0.743 3.471 2.075 RE 1.265 7.581 3.331 Alpha -0.004 0.046 0.017 RE 0.145 3.486 1.614 ROE 3.202 17.447 7.413 RE 0.400 50.493 31.818 EG 0.700 48.813 29.195 RE 0.884 4.928 2.813 ME -1.782 1.474 0.605 RE 0.795 18.146 10.282 IA -1.712 13.199 7.657 NR -0.056 3.693 1.897 ROE 1.934 3.154 2.287 NR 0.000 4.771 2.368 EG 0.814 1.368 1.753 NR 0.425	PD	0.791	2.478	1.557	ROE	0.222	5.024	1.966
PD 0.833 1.978 1.362 ME 0.323 1.845 0.986 RE 0.743 3.471 2.075 MKT 0.743 3.471 2.075 RE 1.265 7.581 3.331 Alpha -0.004 0.046 0.017 RE 0.145 3.486 1.614 ROE 3.202 17.447 7.413 RE 0.400 50.493 31.818 EG 0.700 48.813 29.195 RE 0.884 4.928 2.813 ME -1.782 1.474 0.605 RE 0.795 18.146 10.282 IA -1.712 13.199 7.657 NR -0.056 3.693 1.897 ROE 1.934 3.154 2.287 NR 0.000 4.771 2.368 EG 0.814 1.368 1.753 NR 0.425 3.370 5.178 MKT 0.425 3.370 5.178 NR 0.394	PD	0.736	2.230	1.303	EG	0.213	6.296	2.374
RE 0.743 3.471 2.075 MKT 0.743 3.471 2.075 RE 1.265 7.581 3.331 Alpha -0.004 0.046 0.017 RE 0.145 3.486 1.614 ROE 3.202 17.447 7.413 RE 0.400 50.493 31.818 EG 0.700 48.813 29.195 RE 0.884 4.928 2.813 ME -1.782 1.474 0.605 RE 0.795 18.146 10.282 IA -1.712 13.199 7.657 NR -0.056 3.693 1.897 ROE 1.934 3.154 2.287 NR 0.000 4.771 2.368 EG 0.814 1.368 1.753 NR 0.425 3.370 5.178 MKT 0.425 3.370 5.178 NR -0.272 39.463 16.698 Alpha 0.006 0.202 0.081 NR 0.394 <td>PD</td> <td>0.844</td> <td>1.150</td> <td>0.837</td> <td>IA</td> <td>0.076</td> <td>2.543</td> <td>1.416</td>	PD	0.844	1.150	0.837	IA	0.076	2.543	1.416
RE 1.265 7.581 3.331 Alpha -0.004 0.046 0.017 RE 0.145 3.486 1.614 ROE 3.202 17.447 7.413 RE 0.400 50.493 31.818 EG 0.700 48.813 29.195 RE 0.884 4.928 2.813 ME -1.782 1.474 0.605 RE 0.795 18.146 10.282 IA -1.712 13.199 7.657 NR -0.056 3.693 1.897 ROE 1.934 3.154 2.287 NR 0.000 4.771 2.368 EG 0.814 1.368 1.753 NR 0.425 3.370 5.178 MKT 0.425 3.370 5.178 NR -0.272 39.463 16.698 Alpha 0.006 0.202 0.081 NR 0.394 0.871 1.401 IA -0.319 1.734 1.169 NR 0.453 <td>PD</td> <td>0.833</td> <td>1.978</td> <td>1.362</td> <td>ME</td> <td>0.323</td> <td>1.845</td> <td>0.986</td>	PD	0.833	1.978	1.362	ME	0.323	1.845	0.986
RE 0.145 3.486 1.614 ROE 3.202 17.447 7.413 RE 0.400 50.493 31.818 EG 0.700 48.813 29.195 RE 0.884 4.928 2.813 ME -1.782 1.474 0.605 RE 0.795 18.146 10.282 IA -1.712 13.199 7.657 NR -0.056 3.693 1.897 ROE 1.934 3.154 2.287 NR 0.000 4.771 2.368 EG 0.814 1.368 1.753 NR 0.425 3.370 5.178 MKT 0.425 3.370 5.178 NR -0.272 39.463 16.698 Alpha 0.006 0.202 0.081 NR 0.394 0.871 1.401 IA -0.319 1.734 1.169 NR 0.453 15.719 24.377 ME 0.432 5.574 8.016 INF 0.280 <td>RE</td> <td>0.743</td> <td>3.471</td> <td>2.075</td> <td>MKT</td> <td>0.743</td> <td>3.471</td> <td>2.075</td>	RE	0.743	3.471	2.075	MKT	0.743	3.471	2.075
RE 0.400 50.493 31.818 EG 0.700 48.813 29.195 RE 0.884 4.928 2.813 ME -1.782 1.474 0.605 RE 0.795 18.146 10.282 IA -1.712 13.199 7.657 NR -0.056 3.693 1.897 ROE 1.934 3.154 2.287 NR 0.000 4.771 2.368 EG 0.814 1.368 1.753 NR 0.425 3.370 5.178 MKT 0.425 3.370 5.178 NR -0.272 39.463 16.698 Alpha 0.006 0.202 0.081 NR 0.394 0.871 1.401 IA -0.319 1.734 1.169 NR 0.453 15.719 24.377 ME 0.432 5.574 8.016 INF 0.098 0.055 0.025 Alpha 0.006 0.001 0.000 INF 0.755 </td <td>RE</td> <td>1.265</td> <td>7.581</td> <td>3.331</td> <td>Alpha</td> <td>-0.004</td> <td>0.046</td> <td>0.017</td>	RE	1.265	7.581	3.331	Alpha	-0.004	0.046	0.017
RE 0.884 4.928 2.813 ME -1.782 1.474 0.605 RE 0.795 18.146 10.282 IA -1.712 13.199 7.657 NR -0.056 3.693 1.897 ROE 1.934 3.154 2.287 NR 0.000 4.771 2.368 EG 0.814 1.368 1.753 NR 0.425 3.370 5.178 MKT 0.425 3.370 5.178 NR -0.272 39.463 16.698 Alpha 0.006 0.202 0.081 NR 0.394 0.871 1.401 IA -0.319 1.734 1.169 NR 0.453 15.719 24.377 ME 0.432 5.574 8.016 INF 0.098 0.055 0.025 Alpha 0.006 0.001 0.000 INF 0.280 20.158 8.983 EG 0.893 21.368 9.700 INF 0.469 <td>RE</td> <td>0.145</td> <td>3.486</td> <td>1.614</td> <td>ROE</td> <td>3.202</td> <td>17.447</td> <td>7.413</td>	RE	0.145	3.486	1.614	ROE	3.202	17.447	7.413
RE 0.795 18.146 10.282 IA -1.712 13.199 7.657 NR -0.056 3.693 1.897 ROE 1.934 3.154 2.287 NR 0.000 4.771 2.368 EG 0.814 1.368 1.753 NR 0.425 3.370 5.178 MKT 0.425 3.370 5.178 NR -0.272 39.463 16.698 Alpha 0.006 0.202 0.081 NR 0.394 0.871 1.401 IA -0.319 1.734 1.169 NR 0.453 15.719 24.377 ME 0.432 5.574 8.016 INF 0.098 0.055 0.025 Alpha 0.006 0.001 0.000 INF 0.280 20.158 8.983 EG 0.893 21.368 9.700 INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0.7	RE	0.400	50.493	31.818	EG	0.700	48.813	29.195
NR -0.056 3.693 1.897 ROE 1.934 3.154 2.287 NR 0.000 4.771 2.368 EG 0.814 1.368 1.753 NR 0.425 3.370 5.178 MKT 0.425 3.370 5.178 NR -0.272 39.463 16.698 Alpha 0.006 0.202 0.081 NR 0.394 0.871 1.401 IA -0.319 1.734 1.169 NR 0.453 15.719 24.377 ME 0.432 5.574 8.016 INF 0.098 0.055 0.025 Alpha 0.006 0.001 0.000 INF 0.280 20.158 8.983 EG 0.893 21.368 9.700 INF 0.775 19.273 22.509 MKT 0.775 19.273 22.509 INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0	RE	0.884	4.928	2.813	ME	-1.782	1.474	0.605
NR 0.000 4.771 2.368 EG 0.814 1.368 1.753 NR 0.425 3.370 5.178 MKT 0.425 3.370 5.178 NR -0.272 39.463 16.698 Alpha 0.006 0.202 0.081 NR 0.394 0.871 1.401 IA -0.319 1.734 1.169 NR 0.453 15.719 24.377 ME 0.432 5.574 8.016 INF 0.098 0.055 0.025 Alpha 0.006 0.001 0.000 INF 0.280 20.158 8.983 EG 0.893 21.368 9.700 INF 0.775 19.273 22.509 MKT 0.775 19.273 22.509 INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0.758 33.453 36.239 ME -0.804 16.214 16.161	RE	0.795	18.146	10.282	IA	-1.712	13.199	7.657
NR 0.425 3.370 5.178 MKT 0.425 3.370 5.178 NR -0.272 39.463 16.698 Alpha 0.006 0.202 0.081 NR 0.394 0.871 1.401 IA -0.319 1.734 1.169 NR 0.453 15.719 24.377 ME 0.432 5.574 8.016 INF 0.098 0.055 0.025 Alpha 0.006 0.001 0.000 INF 0.280 20.158 8.983 EG 0.893 21.368 9.700 INF 0.775 19.273 22.509 MKT 0.775 19.273 22.509 INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0.758 33.453 36.239 ME -0.804 16.214 16.161	NR	-0.056	3.693	1.897		1.934	3.154	2.287
NR -0.272 39.463 16.698 Alpha 0.006 0.202 0.081 NR 0.394 0.871 1.401 IA -0.319 1.734 1.169 NR 0.453 15.719 24.377 ME 0.432 5.574 8.016 INF 0.098 0.055 0.025 Alpha 0.006 0.001 0.000 INF 0.280 20.158 8.983 EG 0.893 21.368 9.700 INF 0.775 19.273 22.509 MKT 0.775 19.273 22.509 INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0.758 33.453 36.239 ME -0.804 16.214 16.161		0.000	4.771	2.368		0.814	1.368	1.753
NR 0.394 0.871 1.401 IA -0.319 1.734 1.169 NR 0.453 15.719 24.377 ME 0.432 5.574 8.016 INF 0.098 0.055 0.025 Alpha 0.006 0.001 0.000 INF 0.280 20.158 8.983 EG 0.893 21.368 9.700 INF 0.775 19.273 22.509 MKT 0.775 19.273 22.509 INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0.758 33.453 36.239 ME -0.804 16.214 16.161	NR	0.425	3.370	5.178	MKT	0.425	3.370	5.178
NR 0.453 15.719 24.377 ME 0.432 5.574 8.016 INF 0.098 0.055 0.025 Alpha 0.006 0.001 0.000 INF 0.280 20.158 8.983 EG 0.893 21.368 9.700 INF 0.775 19.273 22.509 MKT 0.775 19.273 22.509 INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0.758 33.453 36.239 ME -0.804 16.214 16.161	NR	-0.272	39.463	16.698	Alpha	0.006	0.202	0.081
INF 0.098 0.055 0.025 Alpha 0.006 0.001 0.000 INF 0.280 20.158 8.983 EG 0.893 21.368 9.700 INF 0.775 19.273 22.509 MKT 0.775 19.273 22.509 INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0.758 33.453 36.239 ME -0.804 16.214 16.161	NR	0.394	0.871	1.401	IA	-0.319	1.734	1.169
INF 0.280 20.158 8.983 EG 0.893 21.368 9.700 INF 0.775 19.273 22.509 MKT 0.775 19.273 22.509 INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0.758 33.453 36.239 ME -0.804 16.214 16.161	NR	0.453	15.719	24.377	ME	0.432	5.574	8.016
INF 0.775 19.273 22.509 MKT 0.775 19.273 22.509 INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0.758 33.453 36.239 ME -0.804 16.214 16.161	INF	0.098	0.055	0.025	Alpha	0.006	0.001	0.000
INF 0.469 26.226 12.751 ROE 1.030 30.728 16.129 INF 0.758 33.453 36.239 ME -0.804 16.214 16.161	INF	0.280	20.158	8.983	EG	0.893	21.368	9.700
INF 0.758 33.453 36.239 ME -0.804 16.214 16.161		0.775	19.273	22.509		0.775	19.273	22.509
	INF	0.469	26.226	12.751	ROE	1.030	30.728	16.129
IND 0.004 000 001 001 000 IA 0.000 100 000 000	INF	0.758	33.453		ME	-0.804	16.214	
INF 0.604 630.801 351.730 IA -0.929 137.937 75.628	INF	0.664	630.801	351.730	IA	-0.929	137.937	75.628

Table 7: Asymptotic inference with EW-VYP-SL max month 180, and D=12.

	MKT I	Factor	2nd Factor			
Type	Mean	SD	Factor	Mean	SD	CV-error
PE	0.886	0.262	EG	0.614	0.217	101444.000
PE	0.719	0.205	Alpha	0.004	0.001	105842.000
PE	0.948	0.267	ROE	0.975	0.407	110926.000
PE	1.250	0.262	MKT	1.250	0.262	127589.000
PE	1.247	0.274	IA	-0.183	0.598	157037.000
PE	1.281	0.323	ME	0.048	0.644	169552.000
VC	1.250	0.153	ME	-1.292	0.234	16305.000
VC	1.183	0.169	IA	-1.507	0.327	16449.000
VC	2.052	0.257	Alpha	-0.006	0.001	18666.000
VC	1.138	0.341	MKT	1.138	0.341	25321.000
VC	1.610	0.431	ROE	-0.946	0.426	26618.000
VC	1.688	0.505	EG	-0.616	0.331	30392.000
PD	0.838	0.029	MKT	0.838	0.029	11290.000
PD	0.458	0.151	Alpha	0.003	0.001	11568.000
PD	0.770	0.058	ROE	0.232	0.111	11572.000
PD	0.707	0.086	EG	0.224	0.091	12194.000
PD	0.825	0.083	IA	0.158	0.305	15071.000
PD	0.837	0.098	ME	0.358	0.328	15441.000
RE	0.803	0.336	MKT	0.803	0.336	43486.000
RE	1.191	0.363	Alpha	-0.003	0.004	45310.000
RE	0.341	0.402	ROE	2.275	1.558	52822.000
RE	0.559	0.379	EG	0.397	0.503	52867.000
RE	0.929	0.339	ME	-1.287	1.174	57341.000
RE	0.852	0.372	IA	-1.129	1.025	57662.000
NR	-0.009	0.203	ROE	1.880	0.562	15631.000
NR	0.200	0.510	EG	0.681	0.372	18981.000
NR	0.572	0.400	MKT	0.572	0.400	20006.000
NR	-0.065	0.729	Alpha	0.006	0.004	20880.000
NR	0.596	0.567	IA	-0.060	0.869	24766.000
NR	0.769	0.771	ME	0.666	1.062	27238.000
INF	0.124	0.608	Alpha	0.007	0.006	14995.000
INF	0.613	0.393	EG	0.402	0.496	15758.000
INF	0.862	0.281	MKT	0.862	0.281	15820.000
INF	0.627	0.360	ROE	0.577	1.374	18297.000
INF	0.810	0.315	ME	-0.129	1.109	19641.000
INF	0.797	0.842	IA	0.051	2.180	33661.000

Table 8: hv-block cross-validation with EW-VYP-SL weighting and max month 180.