

Forces of the Quantum Vacuum presents a number of approaches to Casimir, van der Waals and Casimir-Polder forces that have been fruitfully employed in mainstream research, and reviews the experimental evidence for Casimir forces.

Beginning with basic ideas in quantum mechanics and building its way to a sophisticated form of macroscopic QED, *Forces of the Quantum Vacuum* provides an inspiring training manual for graduate students that develops the ideas needed for modern research on Casimir forces in a natural progression, with a strong emphasis on physical understanding.

Contributing editors

William Simpson is a Research Fellow in Theoretical Physics at the Weizmann Institute of Science, and a Research Associate in Theology at the University of St Andrews.

Ulf Leonhardt is a Professor of Physics at The Weizmann Institute of Science. His research interests include quantum electrodynamics in media, Hawking radiation, and transformation optics.

"... a refreshingly readable introduction to Casimir physics. The contributing experts have introduced the concepts and techniques needed for students and nonspecialists to learn the essential physics of van der Waals and Casimir forces."

Peter Milonni, Professor of Physics,
University of Rochester

William M.R. Simpson
Ulf Leonhardt

FORCES OF THE QUANTUM VACUUM

An introduction
to Casimir Physics

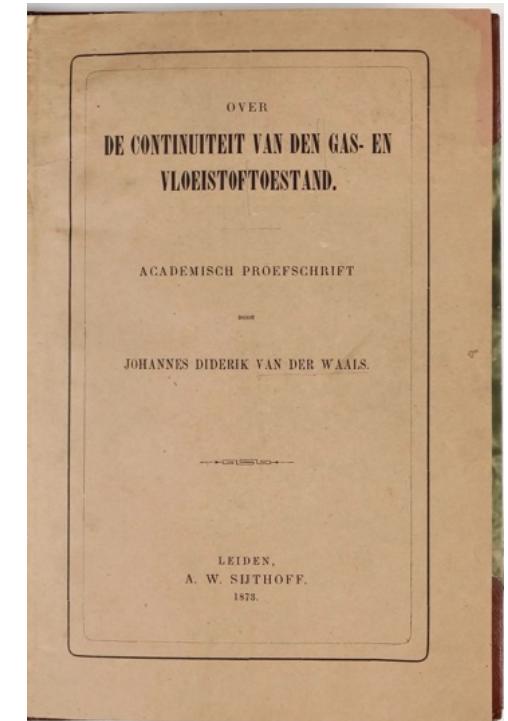
van der Waals: molecular forces 1873



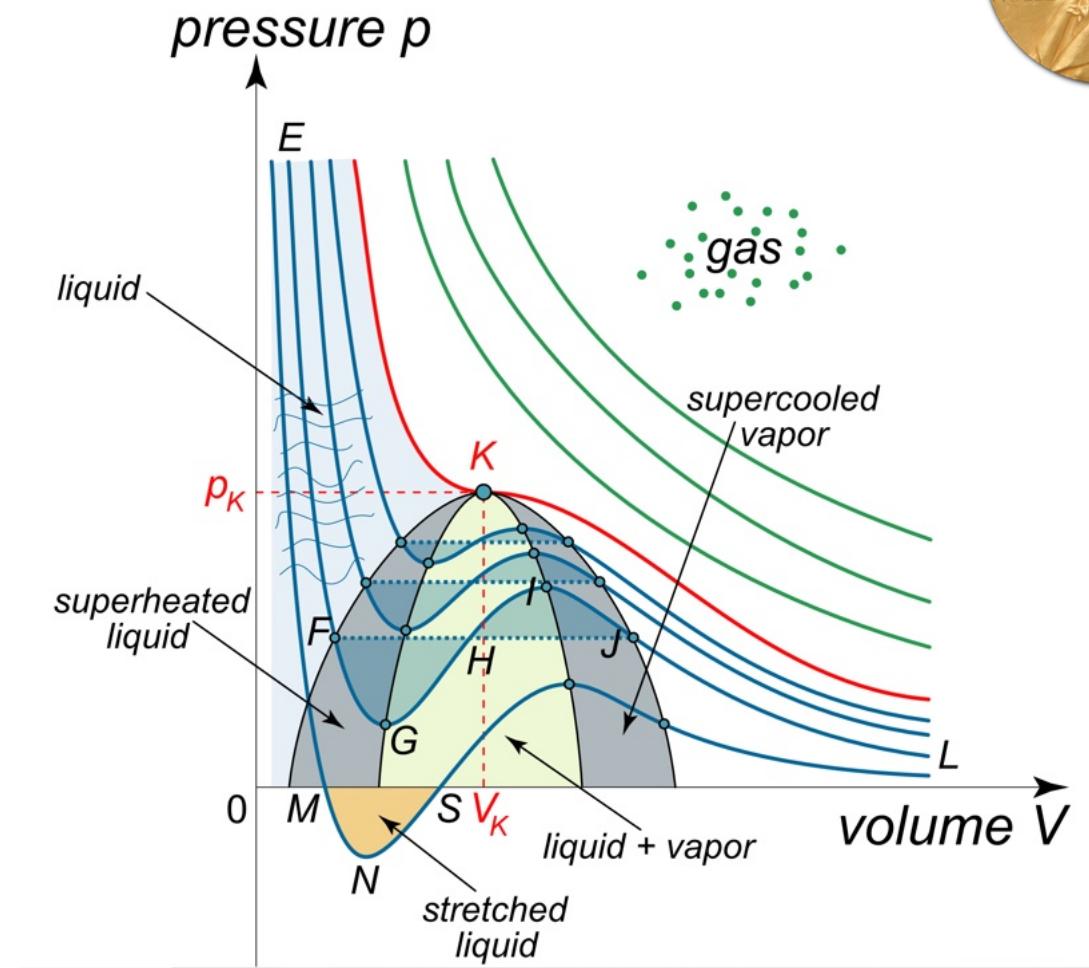
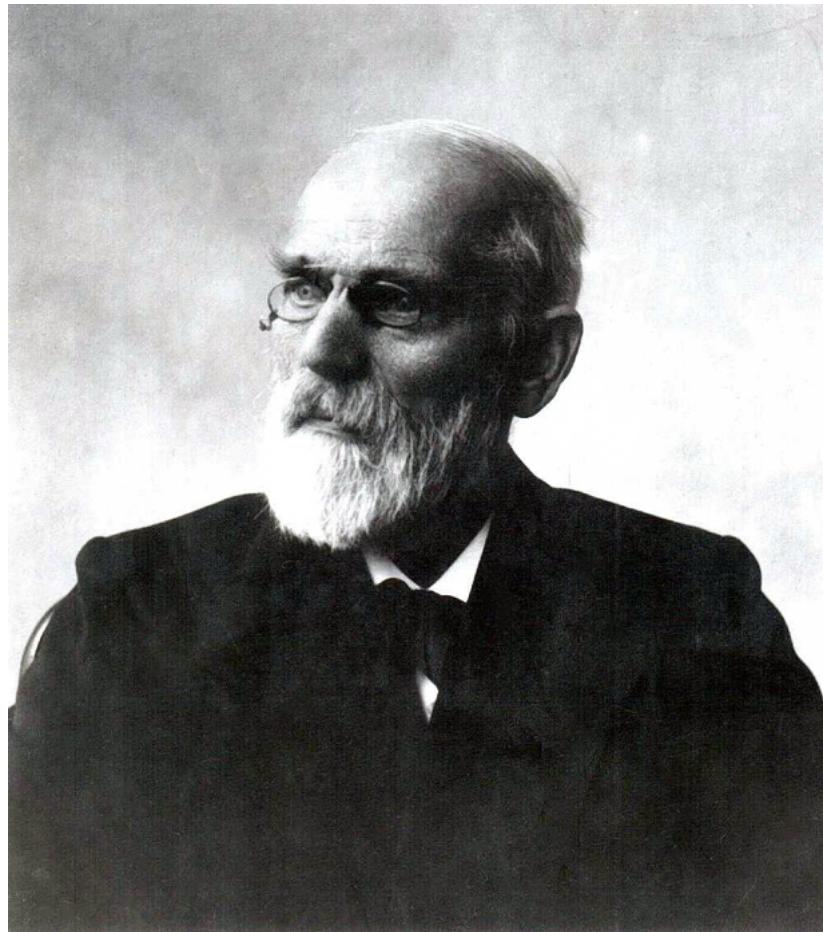
$$(p + an^2/V^2)(V - nb) = nRT$$

b : molecular volume

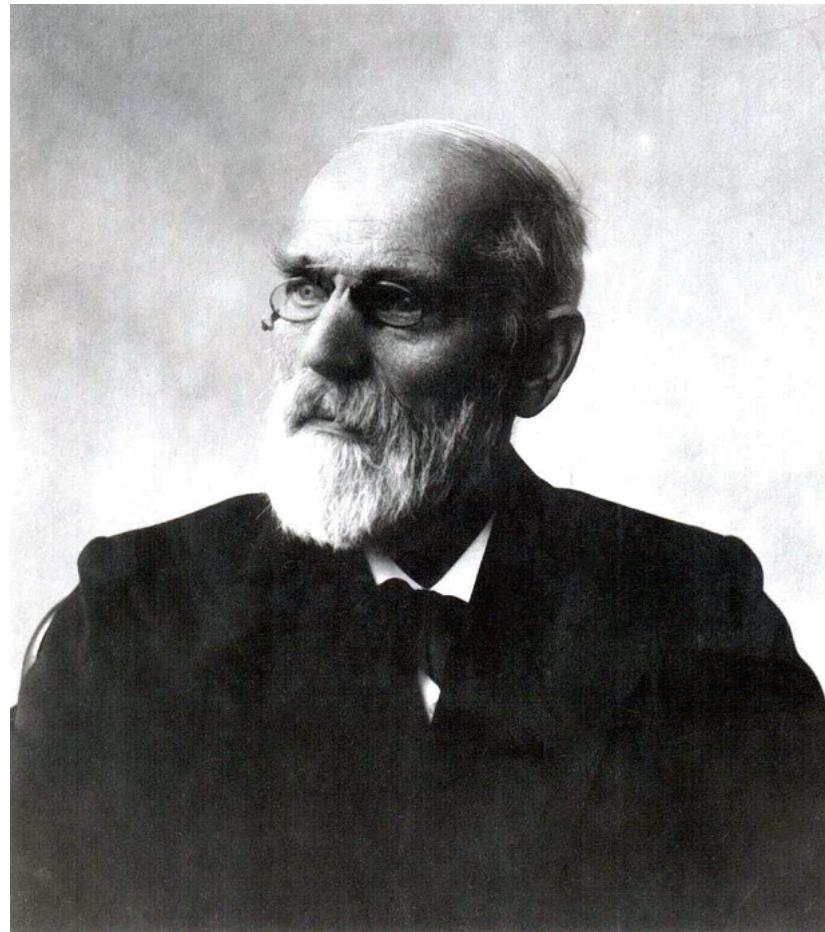
$$\varrho = n/V$$



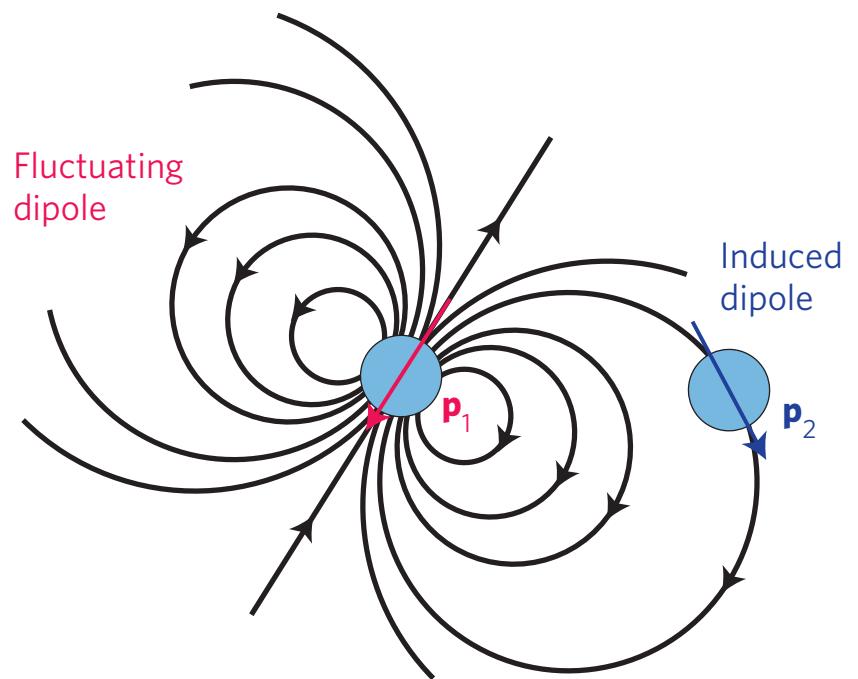
van der Waals: molecular forces 1873



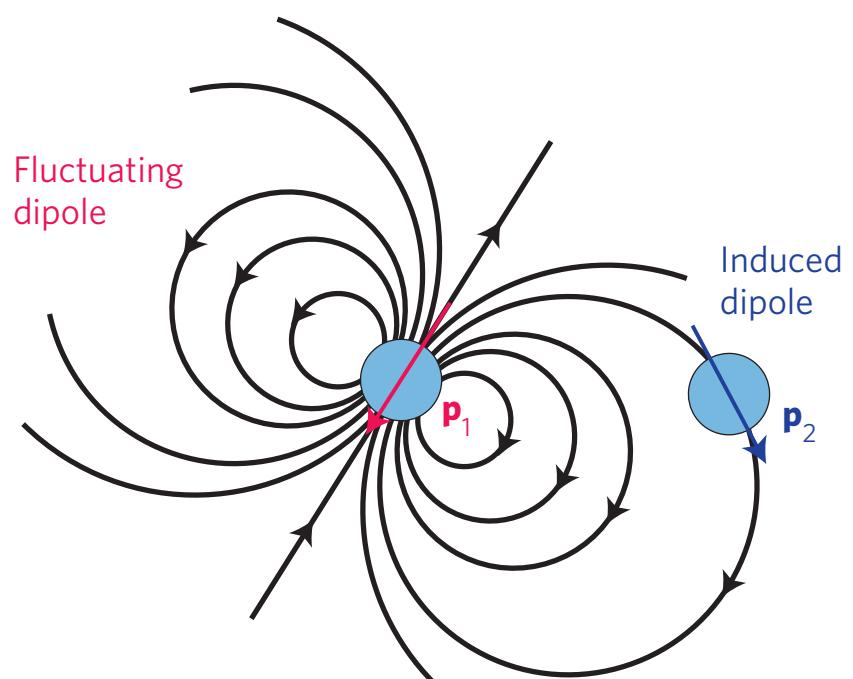
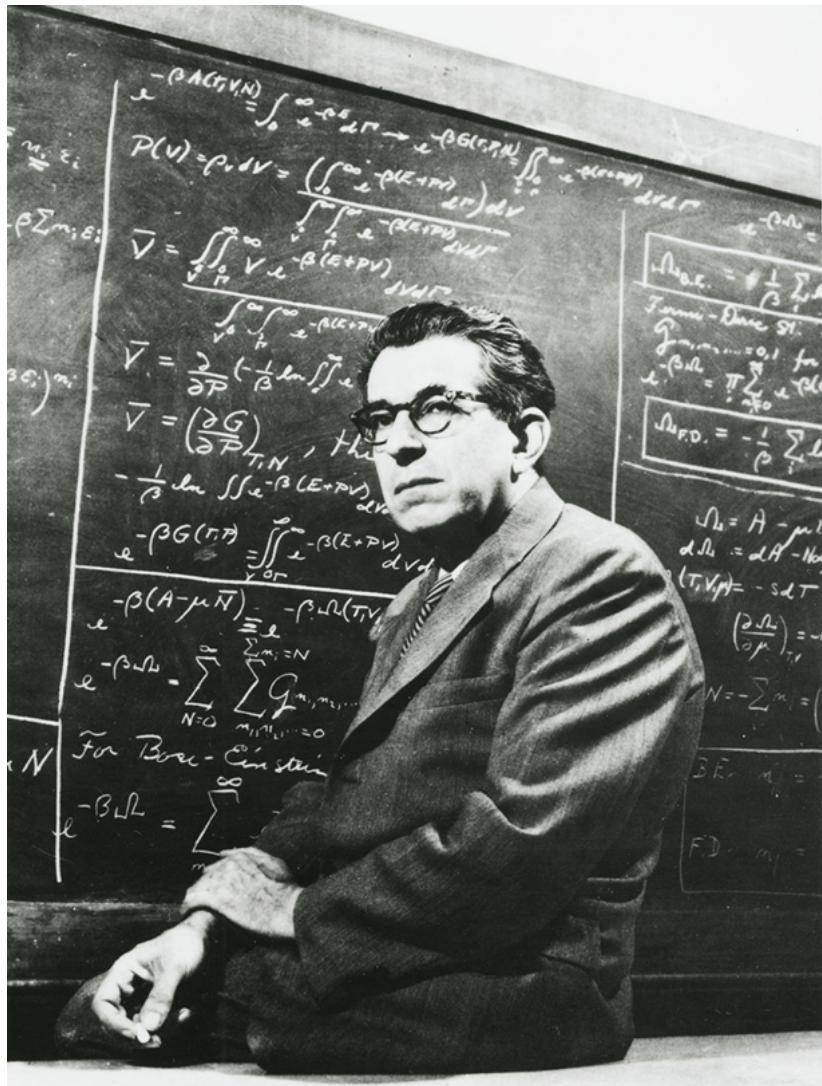
van der Waals: molecular forces 1873



$$(p + an^2/V^2)(V - nb) = nRT$$



Fritz London: dispersion forces 1930



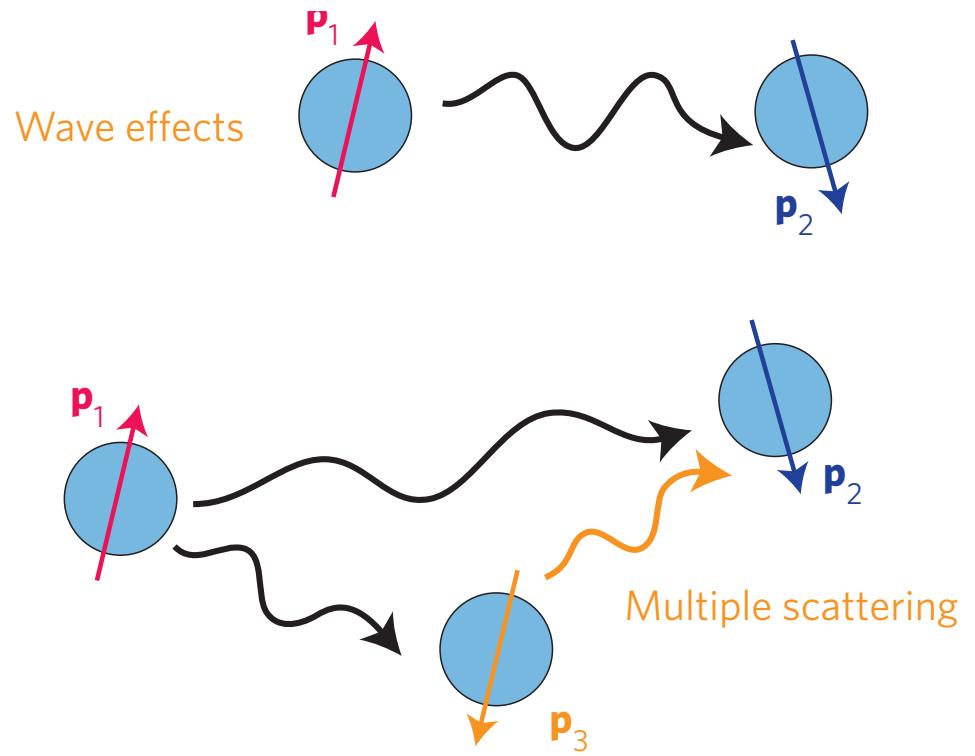
Hendrik Casimir: chief scientist 1946-1972



Hendrik Casimir: liquid paint 1940s



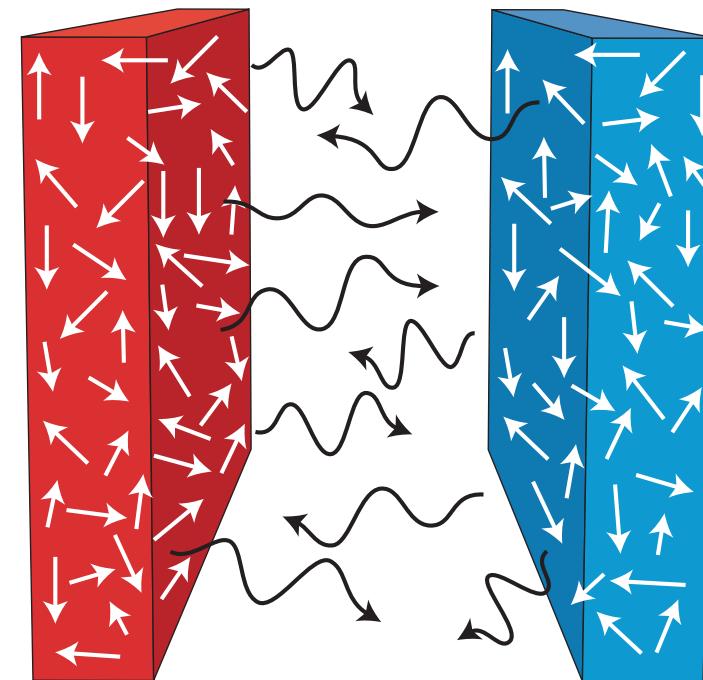
Casimir & Polder: waves & retardation 1948



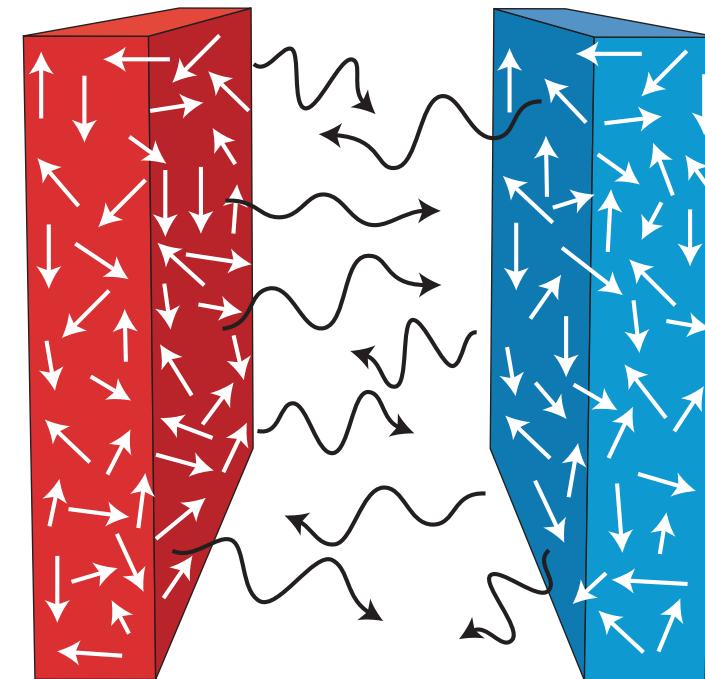
Bohr versus Pauli: quantum vacuum



Hendrik Casimir: macroscopic bodies 1948

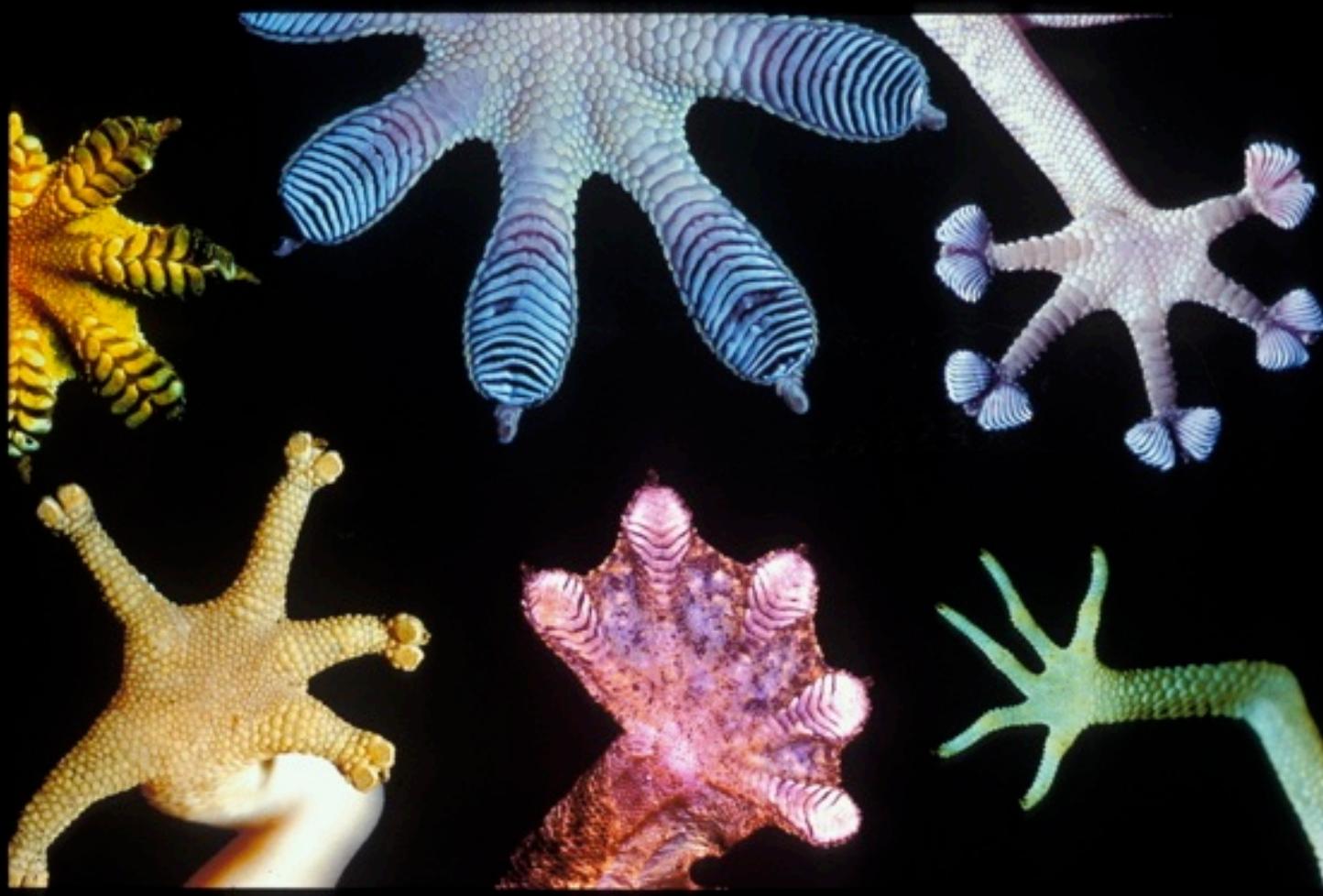


Hendrik Casimir: macroscopic bodies 1948



10nm corresponds to 1atm

Casimir/ van der Waals forces



Lifshitz theory



SOVIET PHYSICS

USPEKHI

A Translation of Uspekhi Fizicheskikh Nauk

SOVIET PHYSICS USPEKHI

(Russian Vol. 73, Nos. 3-4)

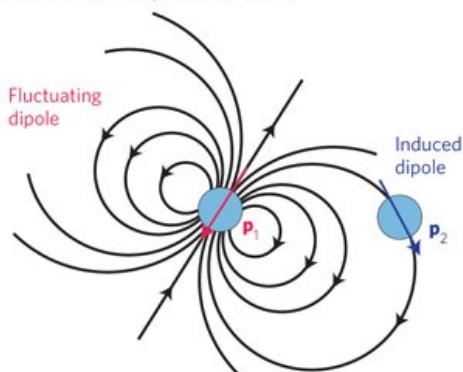
SEPTEMBER-OCTOBER 1961

GENERAL THEORY OF VAN DER WAALS' FORCES

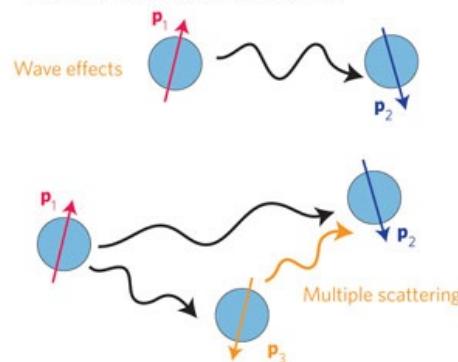
I. E. DZYALOSHINSKII, E. M. LIFSHITZ, and L. P. PITAEVSKII

Usp. Fiz. Nauk 73, 381-422 (March, 1961)

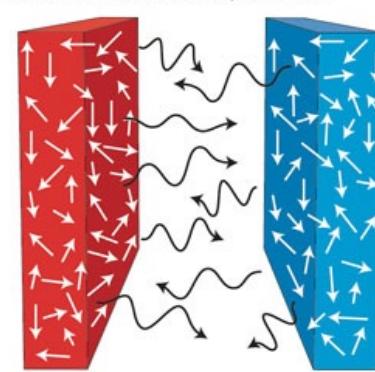
a van der Waals (quasistatic fields)



b Casimir-Polder (waves/retardation)

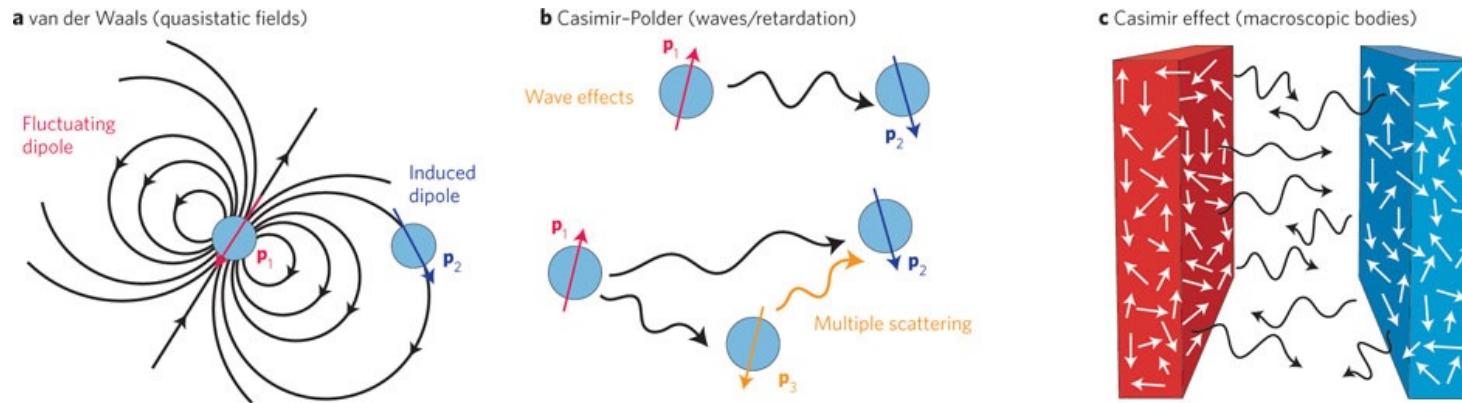


c Casimir effect (macroscopic bodies)



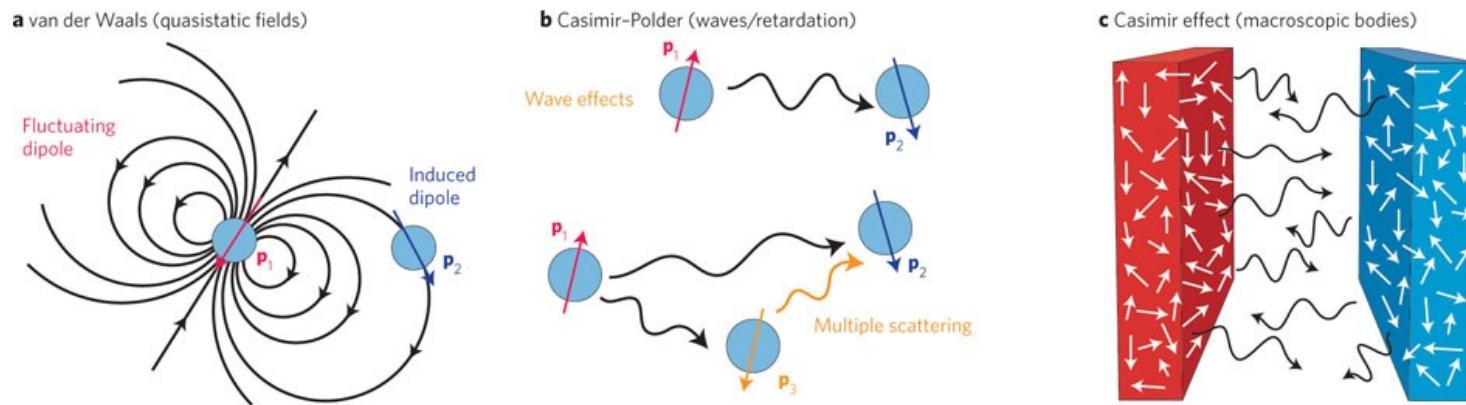
The Casimir effect in microstructured geometries

Alejandro W. Rodriguez^{1,2}, Federico Capasso^{1*} and Steven G. Johnson²



The Casimir effect in microstructured geometries

Alejandro W. Rodriguez^{1,2}, Federico Capasso^{1*} and Steven G. Johnson²



VOLUME 78, NUMBER 1

PHYSICAL REVIEW LETTERS

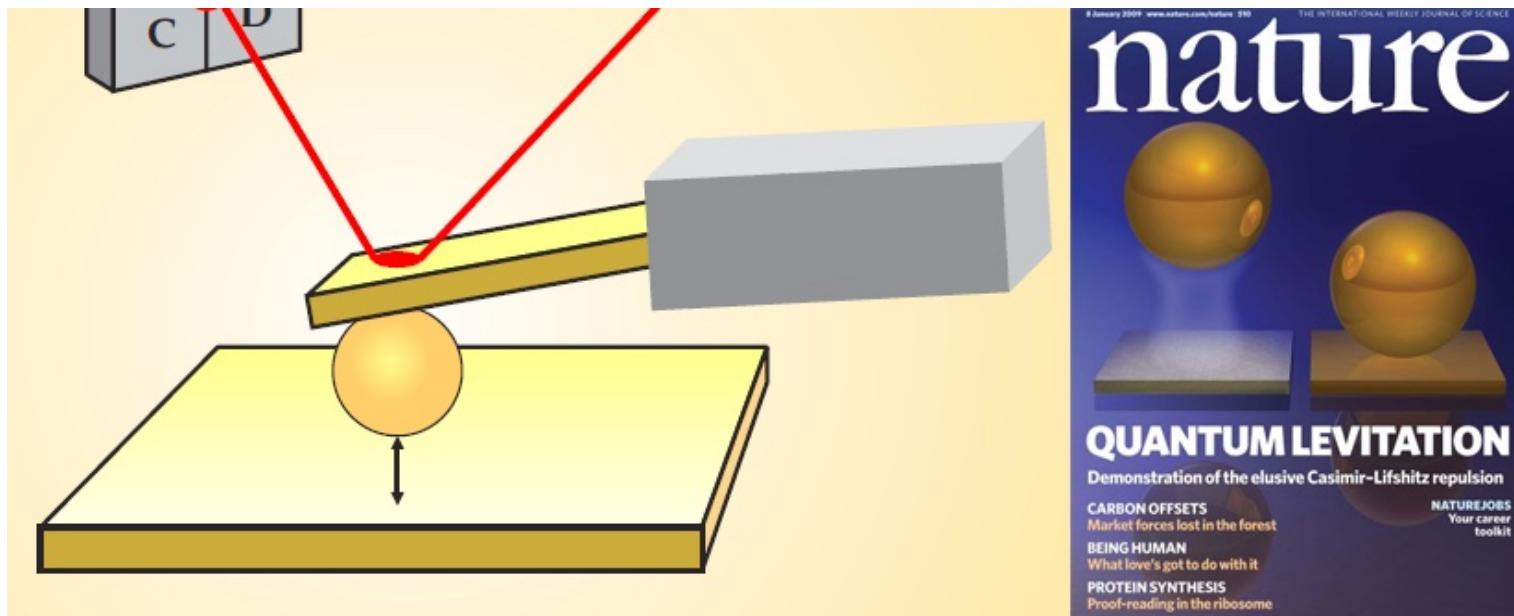
6 JANUARY 1997

Demonstration of the Casimir Force in the 0.6 to 6 μm Range

S. K. Lamoreaux*

Physics Department, University of Washington, Box 35160, Seattle, Washington 98195-1560
(Received 28 August 1996)

Precision measurements and manipulations of Casimir forces



RESEARCH

PHYSICS

Science 364, 984–987 (2019) 7 June 2019

Stable Casimir equilibria and quantum trapping

Rongkuo Zhao^{1*}, Lin Li^{1*}, Sui Yang^{1*}, Wei Bao^{1*}, Yang Xia¹, Paul Ashby²,
Yuan Wang¹, Xiang Zhang^{1,3†}

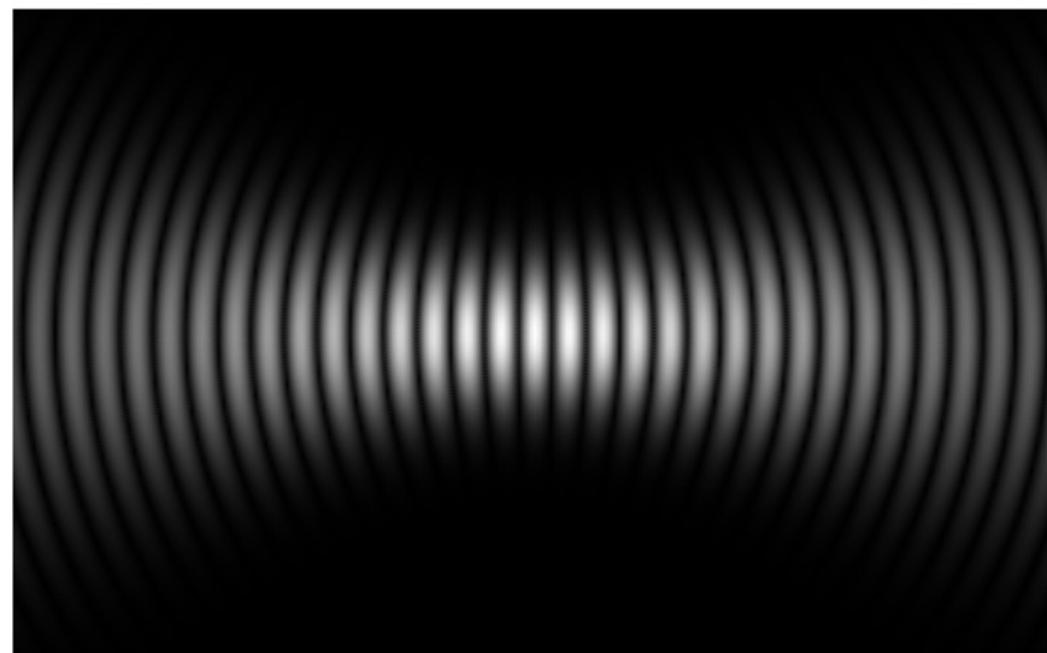
Quantum fields: mode expansion

$$\hat{A} = \sum_k \hat{a}_k A_k(x, t) + \hat{a}_k^\dagger A_k^*(x, t)$$

Quantum fields: mode expansion

$$\hat{A} = \sum_k \hat{a}_k A_k(x, t) + \hat{a}_k^\dagger A_k^*(x, t)$$

$A_k(x, t) :$



Quantum fields: mode expansion

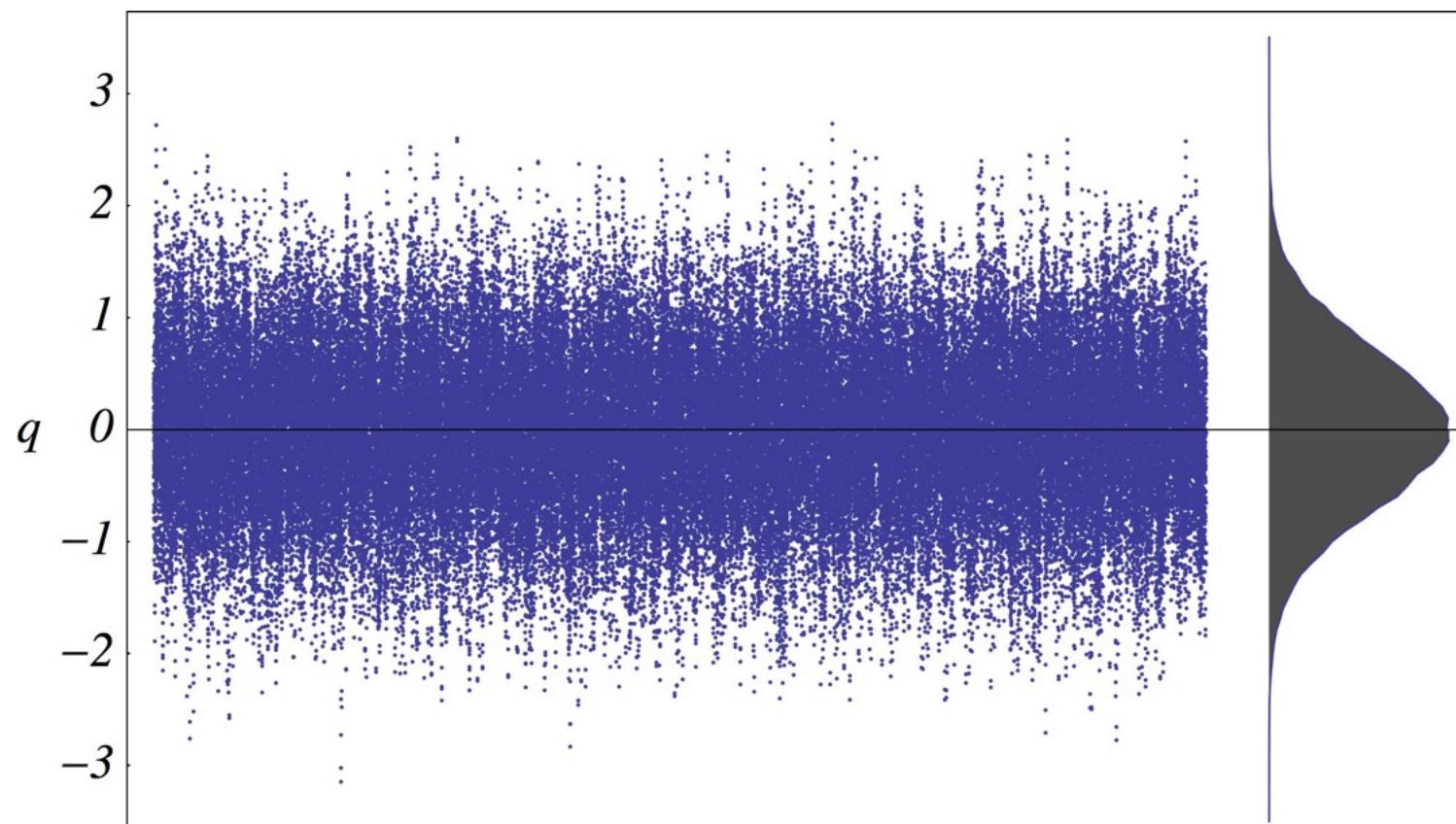
$$\hat{A} = \sum_k \hat{a}_k A_k(x, t) + \hat{a}_k^\dagger A_k^*(x, t)$$

$$[\hat{a}_k, \hat{a}_{k'}^\dagger] = \delta_{kk'}$$

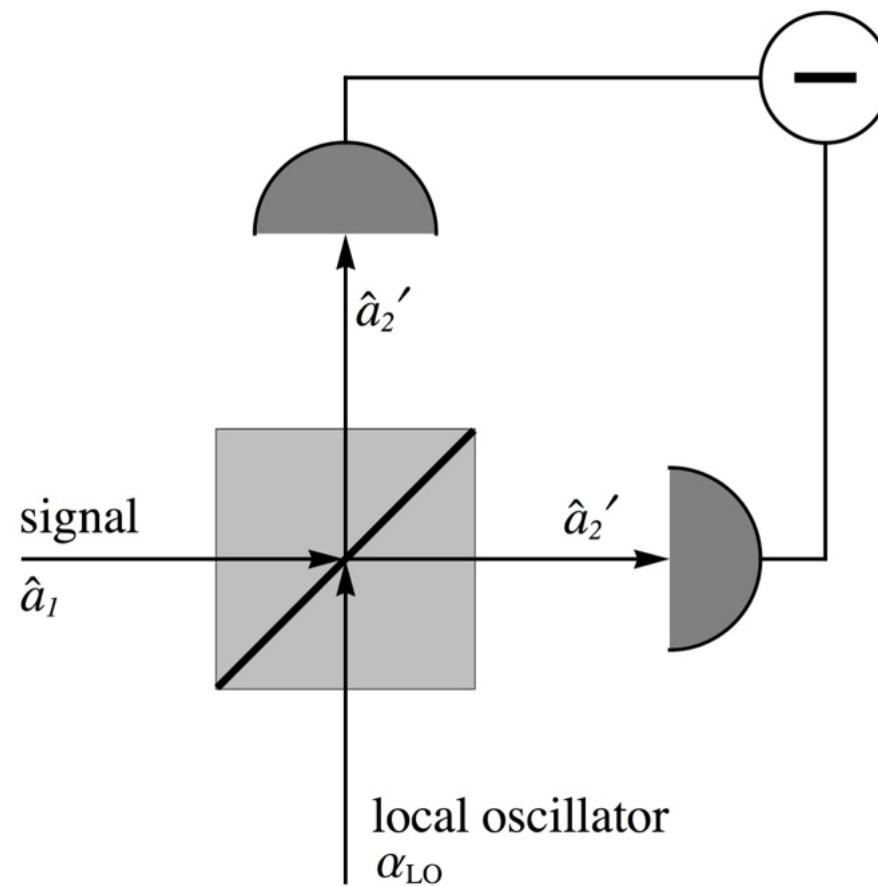
$$\hat{a} = 2^{-1/2}(\hat{q} + i\hat{p})$$

Quantum vacuum: zero amplitude

$$\hat{a}_k |0\rangle = 0$$

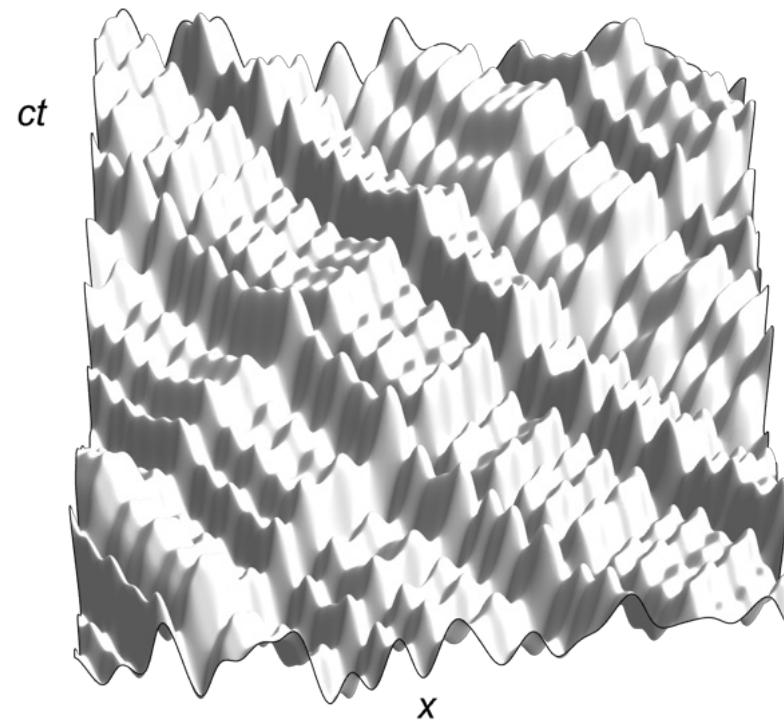


Amplitude measurements: homodyne detection



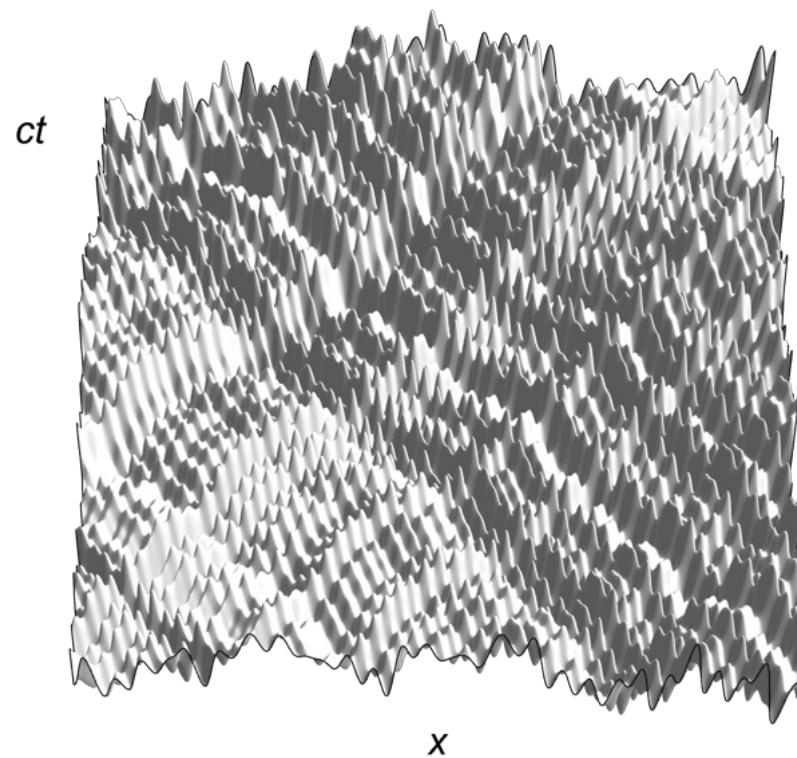
Quantum fields: 32 plane waves

$$\hat{A} = \sum_k \hat{a}_k A_k(x, t) + \hat{a}_k^\dagger A_k^*(x, t)$$



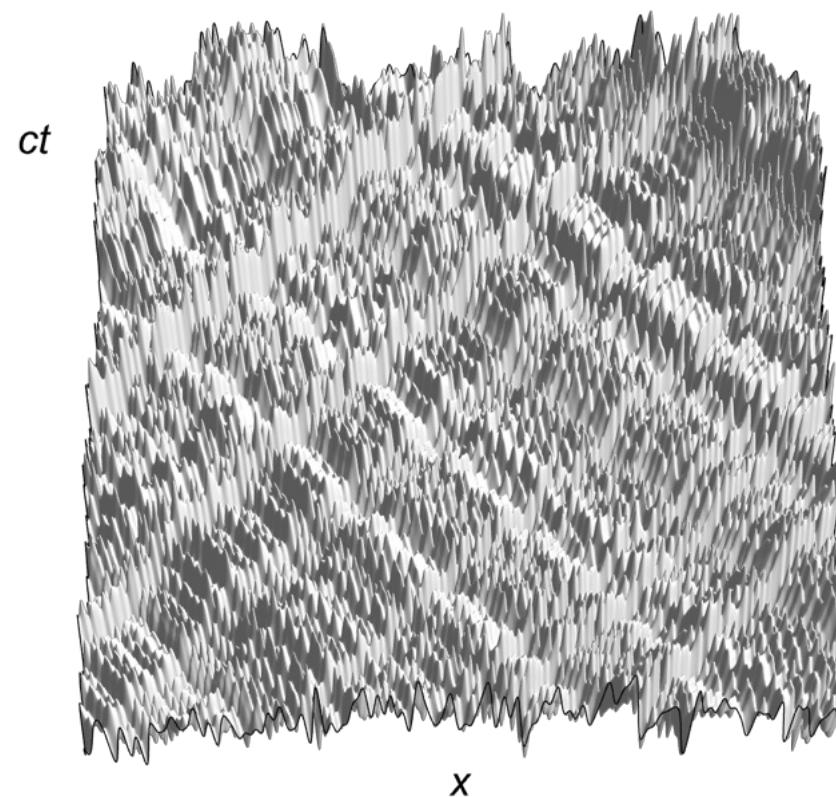
Quantum fields: 64 plane waves

$$\hat{A} = \sum_k \hat{a}_k A_k(x, t) + \hat{a}_k^\dagger A_k^*(x, t)$$



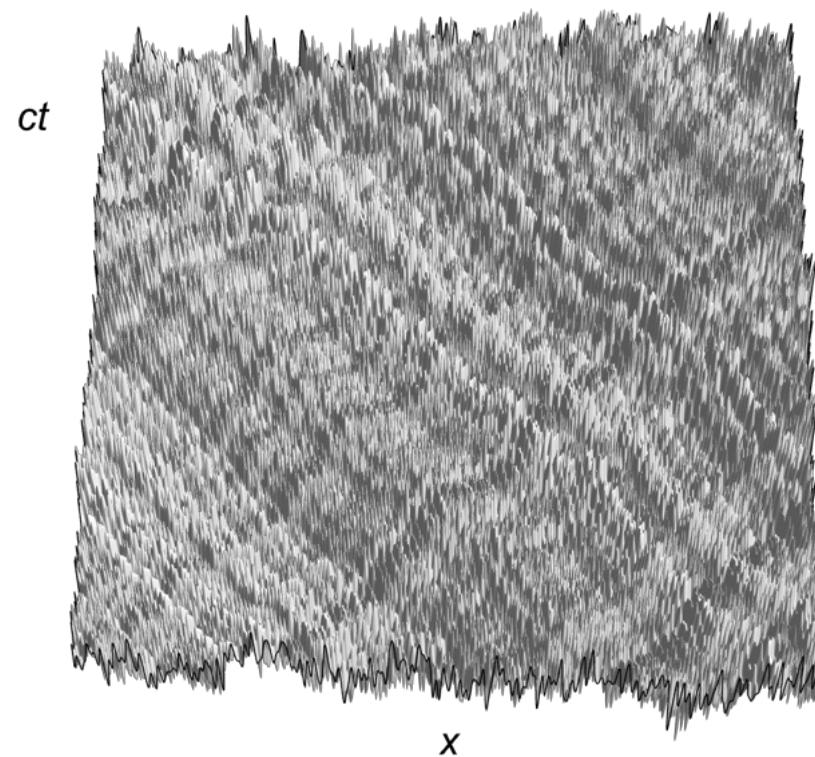
Quantum fields: 128 plane waves

$$\hat{A} = \sum_k \hat{a}_k A_k(x, t) + \hat{a}_k^\dagger A_k^*(x, t)$$



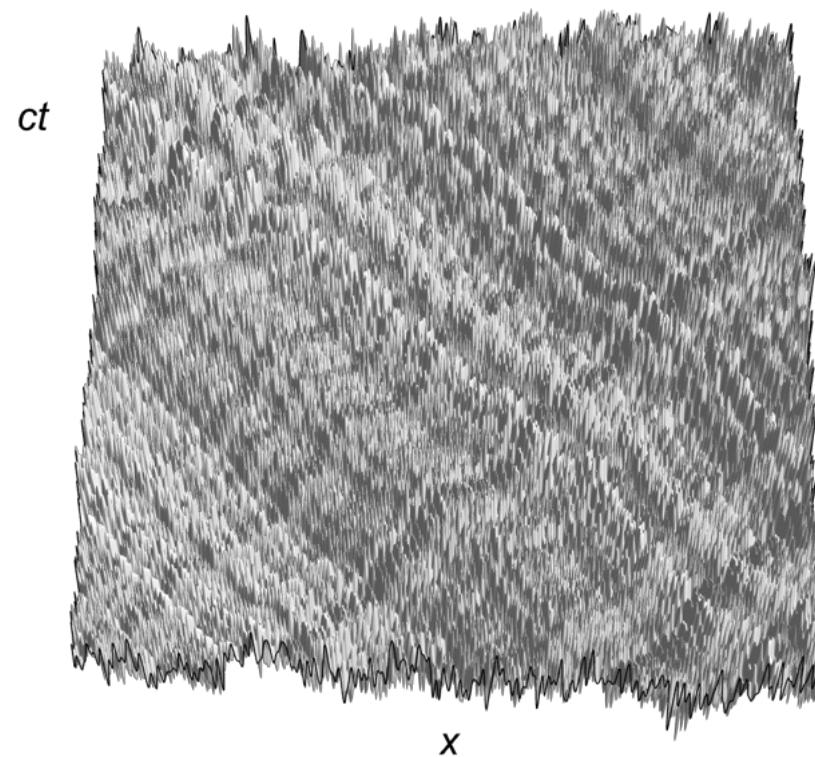
Quantum fields: 256 plane waves

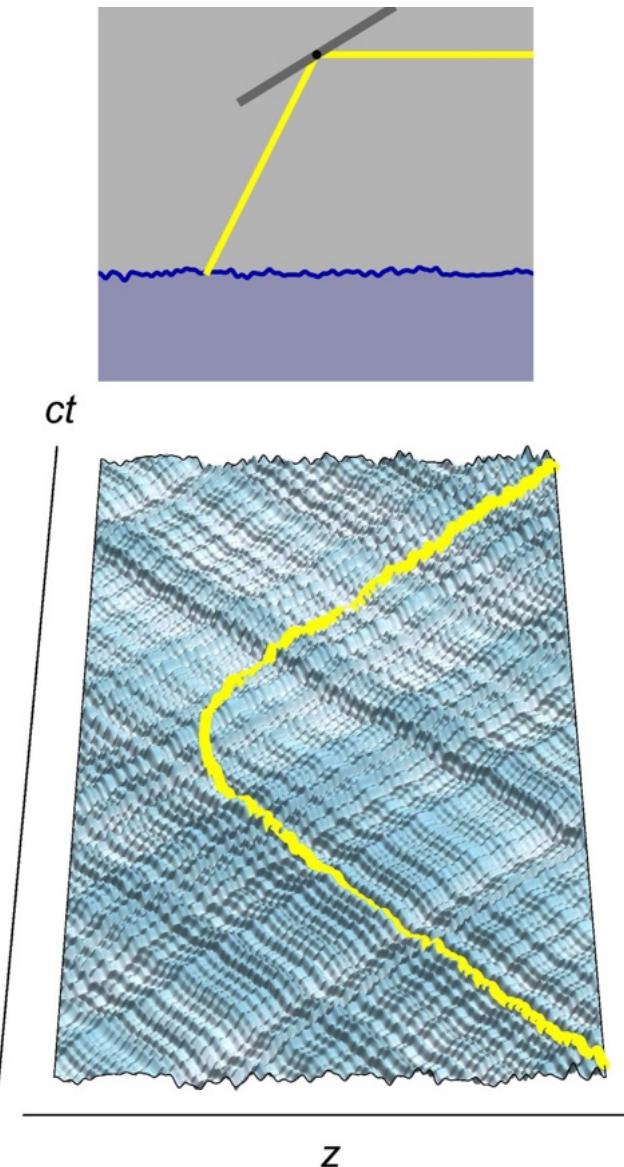
$$\hat{A} = \sum_k \hat{a}_k A_k(x, t) + \hat{a}_k^\dagger A_k^*(x, t)$$



Vacuum noise is organised

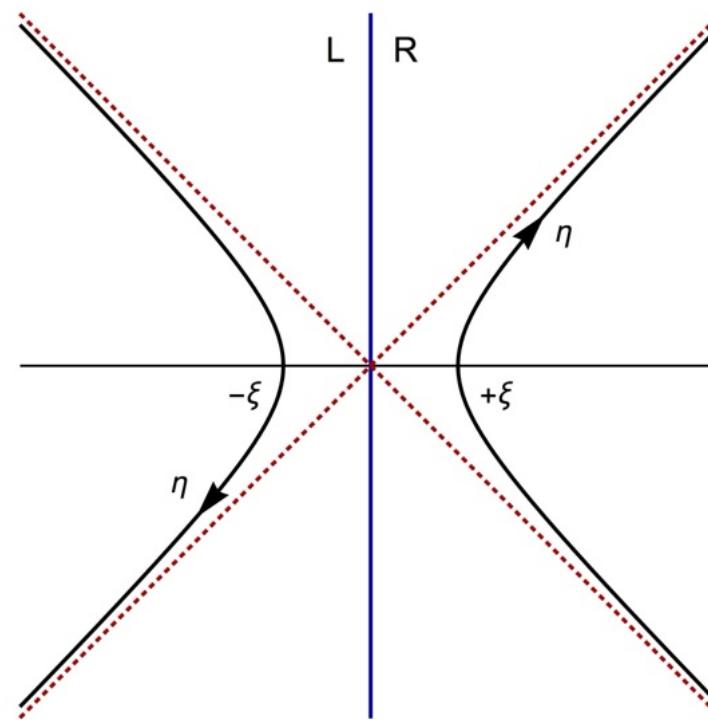
$$\hat{A} = \sum_k \hat{a}_k A_k(x, t) + \hat{a}_k^\dagger A_k^*(x, t)$$





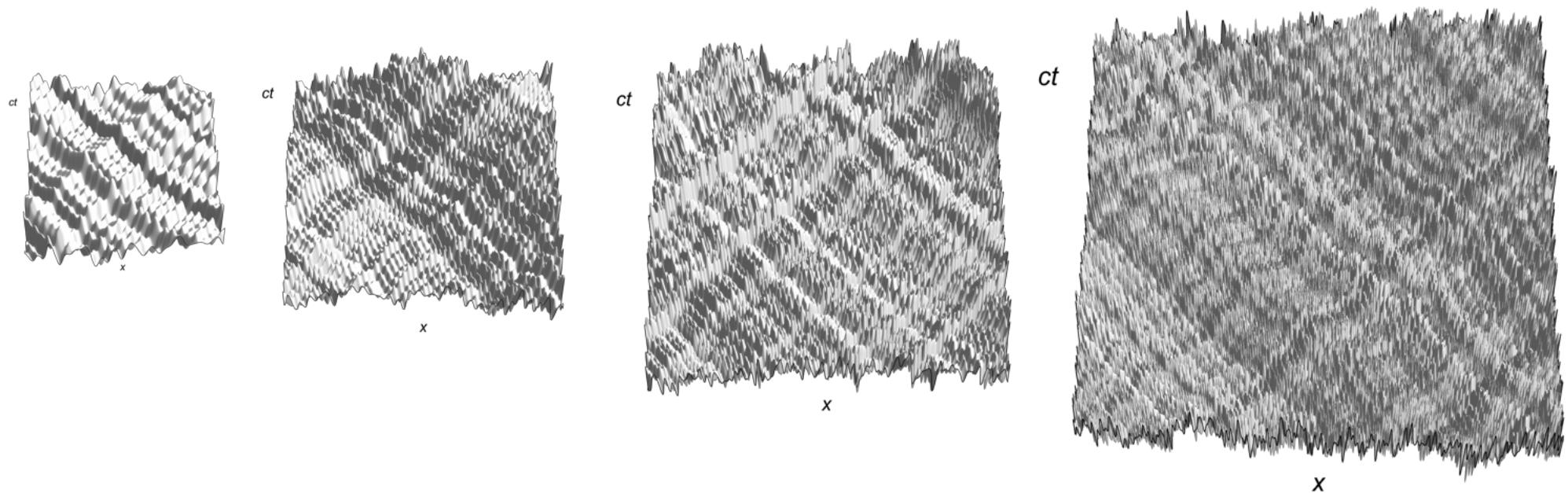
Classical analog of the Unruh effect

Ulf Leonhardt,¹ Itay Griniasty,¹ Sander Wildeman,² Emmanuel Fort,² and Mathias Fink²

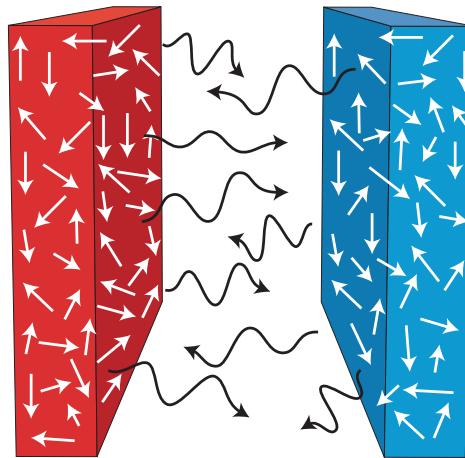


Vacuum noise is infinite

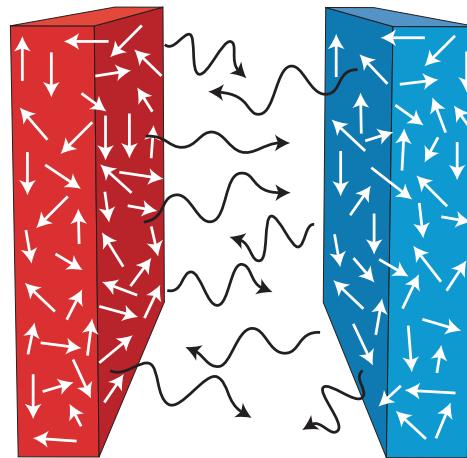
$$\hat{A} = \sum_k \hat{a}_k A_k(x, t) + \hat{a}_k^\dagger A_k^*(x, t)$$



Renormalization: bare vacuum energy is infinite

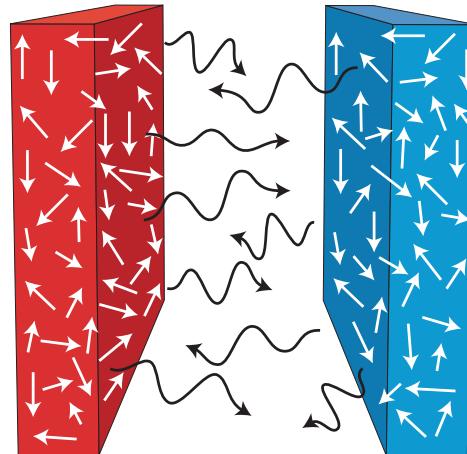


Renormalization: compare vacuum energy at finite distance

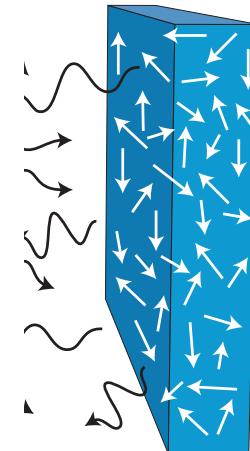
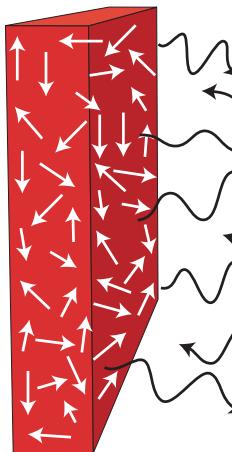


with

Renormalization: compare vacuum energy at finite distance



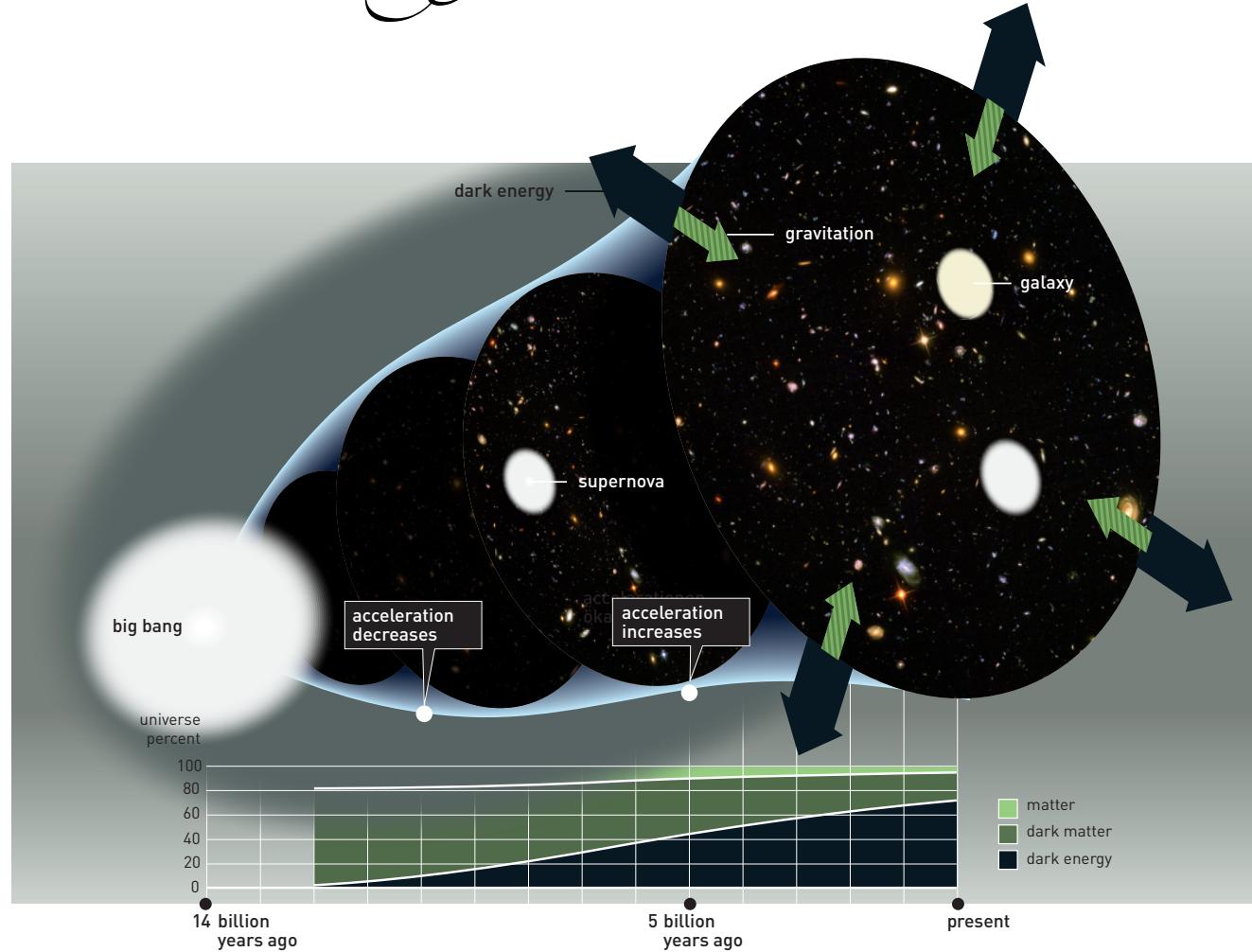
with

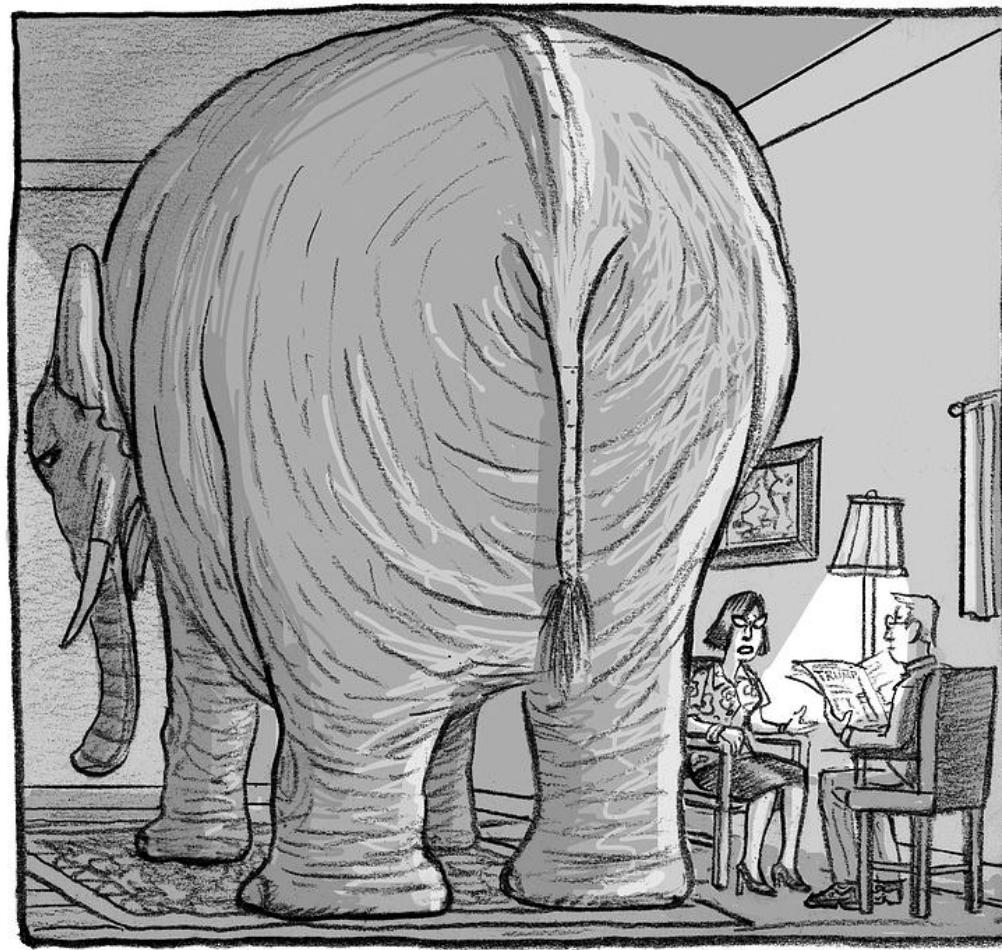


Dark energy – cosmological constant



2011

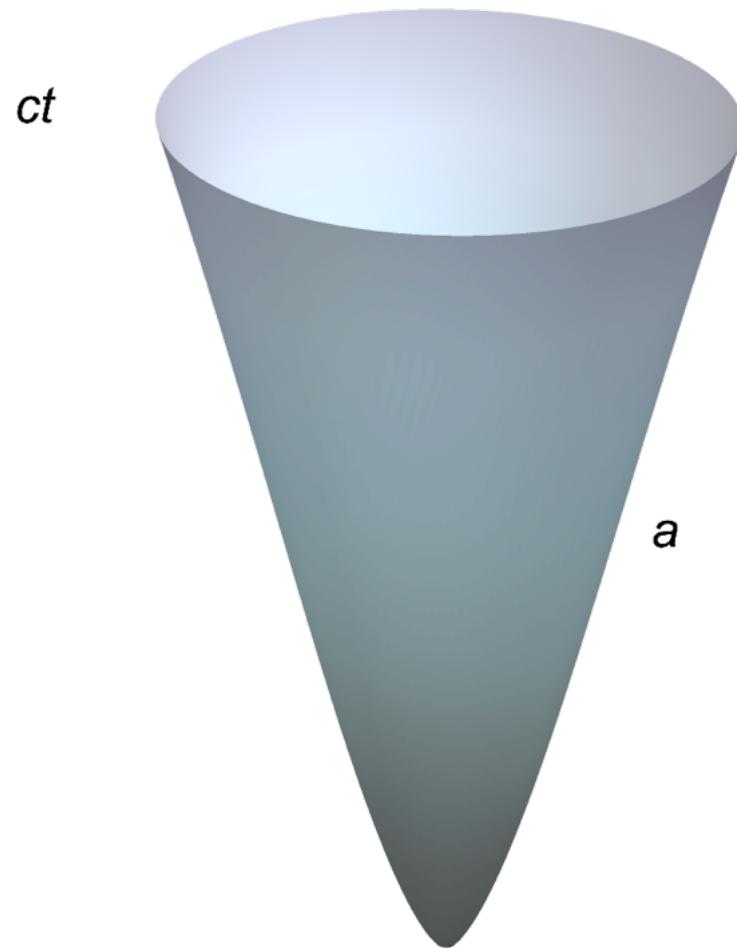




KUPER

"Actually, it's all we ever talk about."

Optical analogue of expanding, spatially flat universe



$$d\ell = a(t) d\sqrt{r}$$

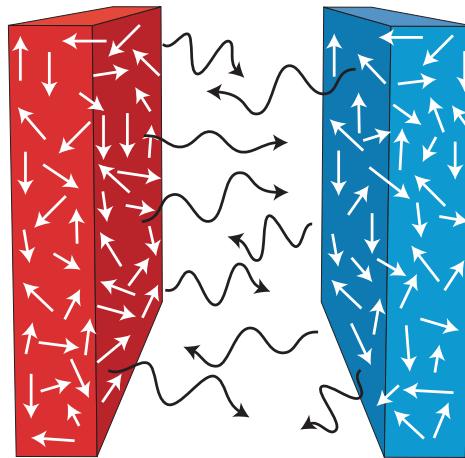
$$n = a$$



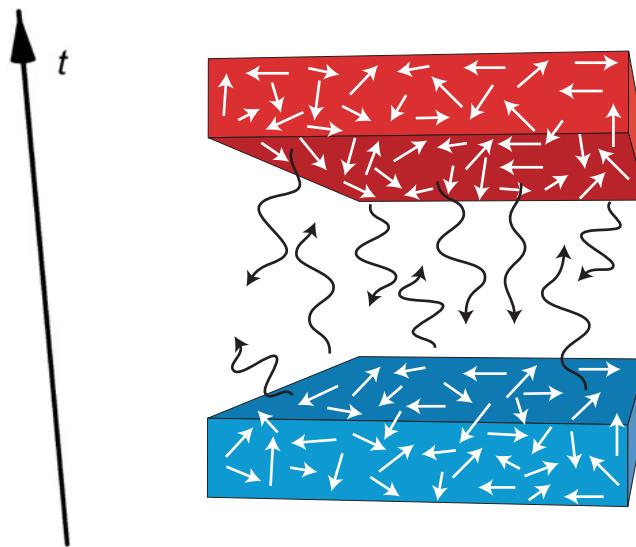
ct

r

Casimir cosmology: turn from space



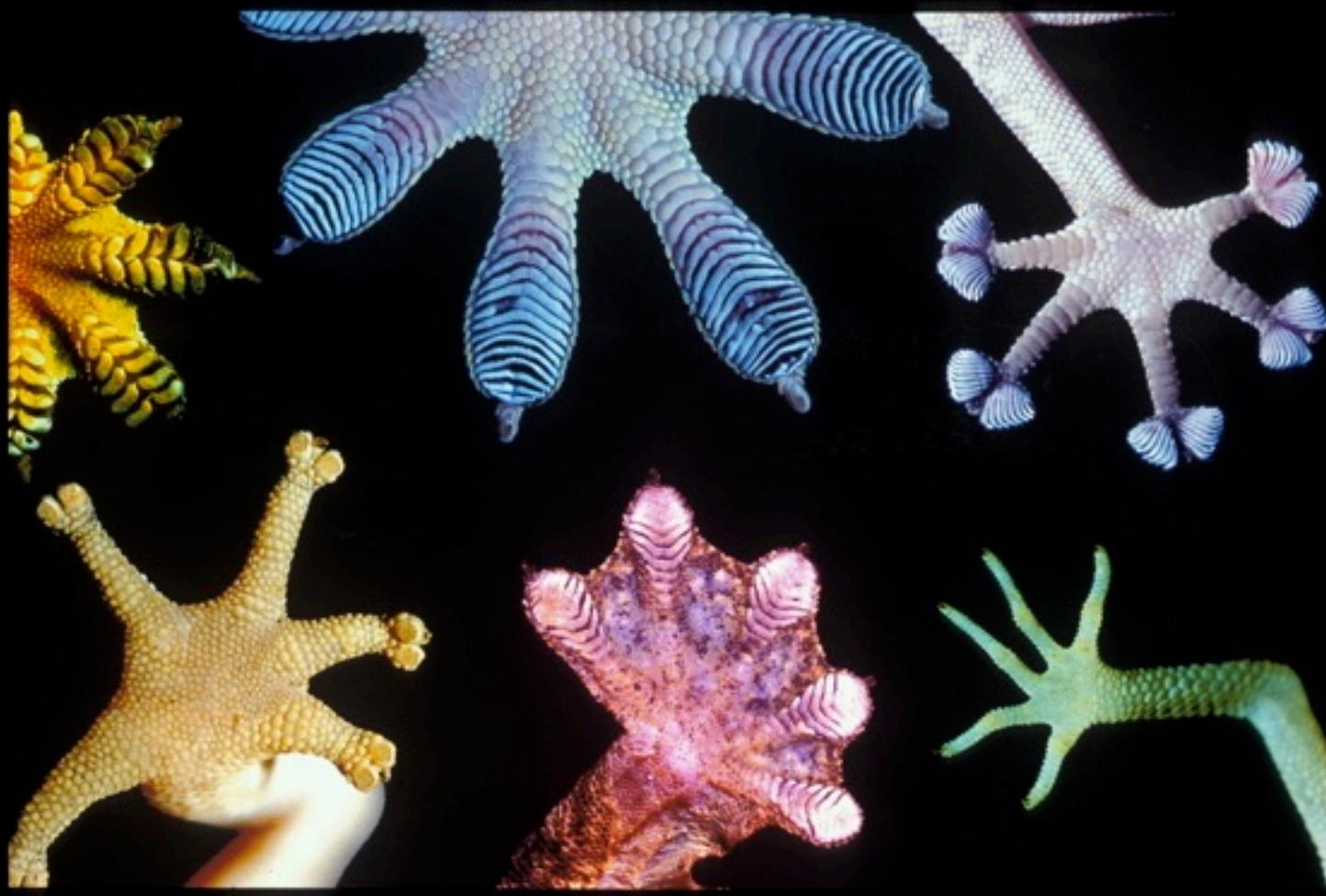
Casimir cosmology: turn from space to time



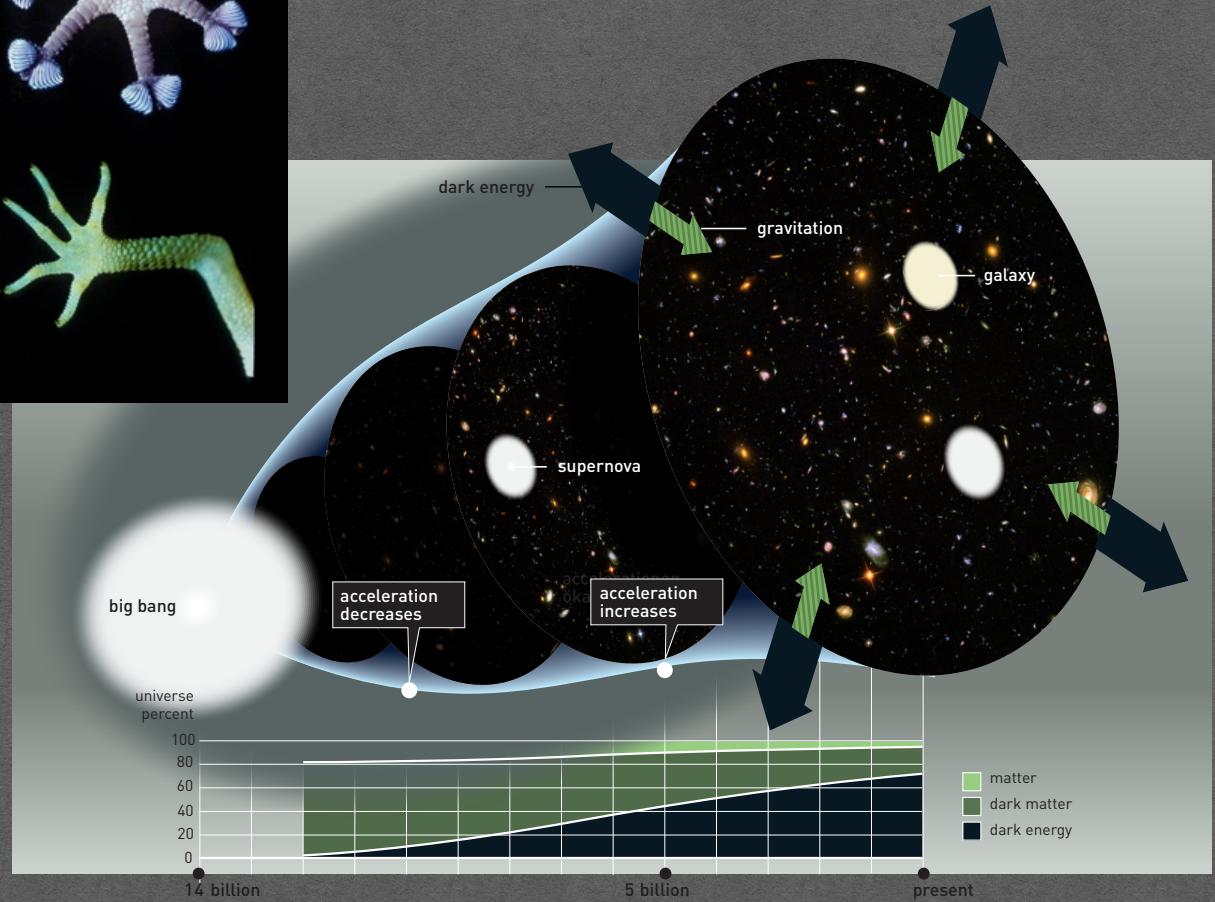
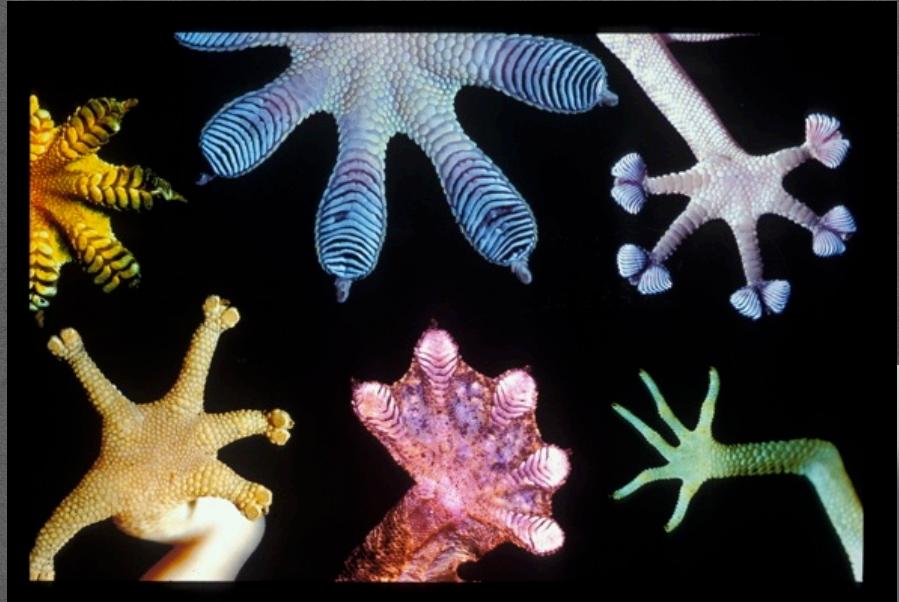
Casimir cosmology: continuous $n(t)$



Casimir force in cosmology?

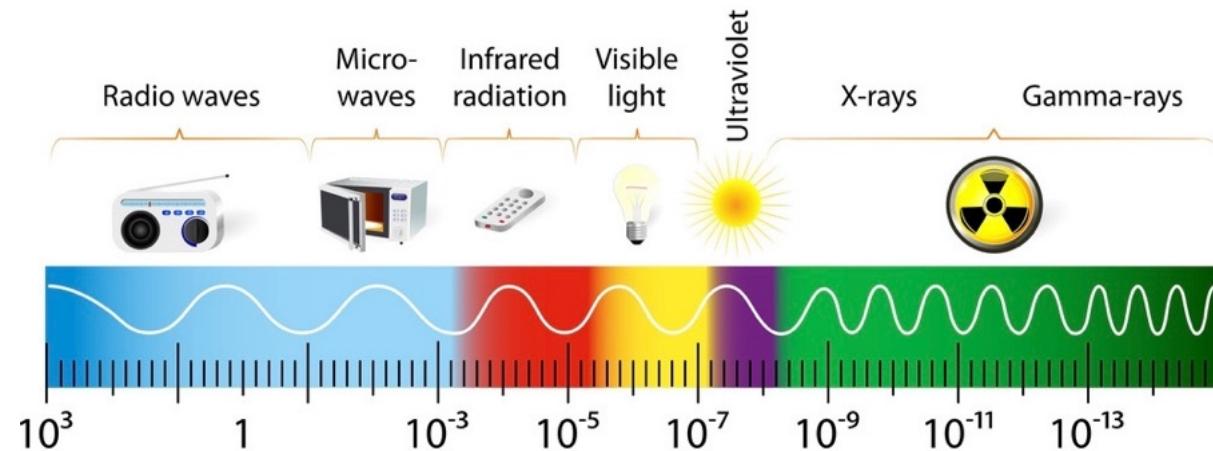


What's the difference?

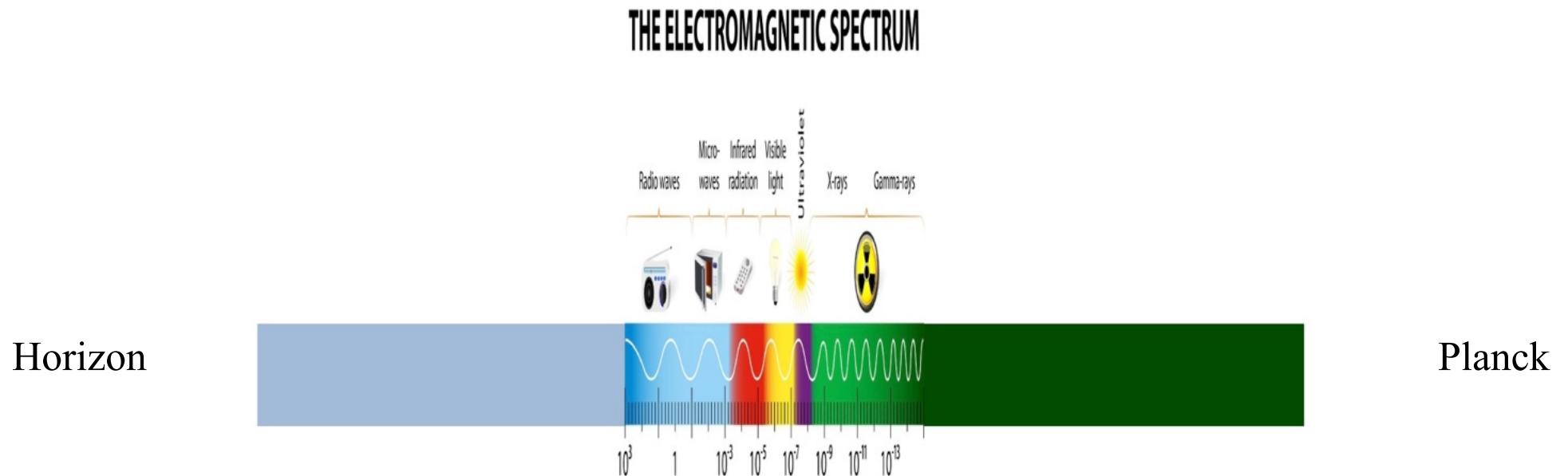


Equivalence principle: space-time is the same for everything

THE ELECTROMAGNETIC SPECTRUM



Equivalence principle: space-time is the same for everything



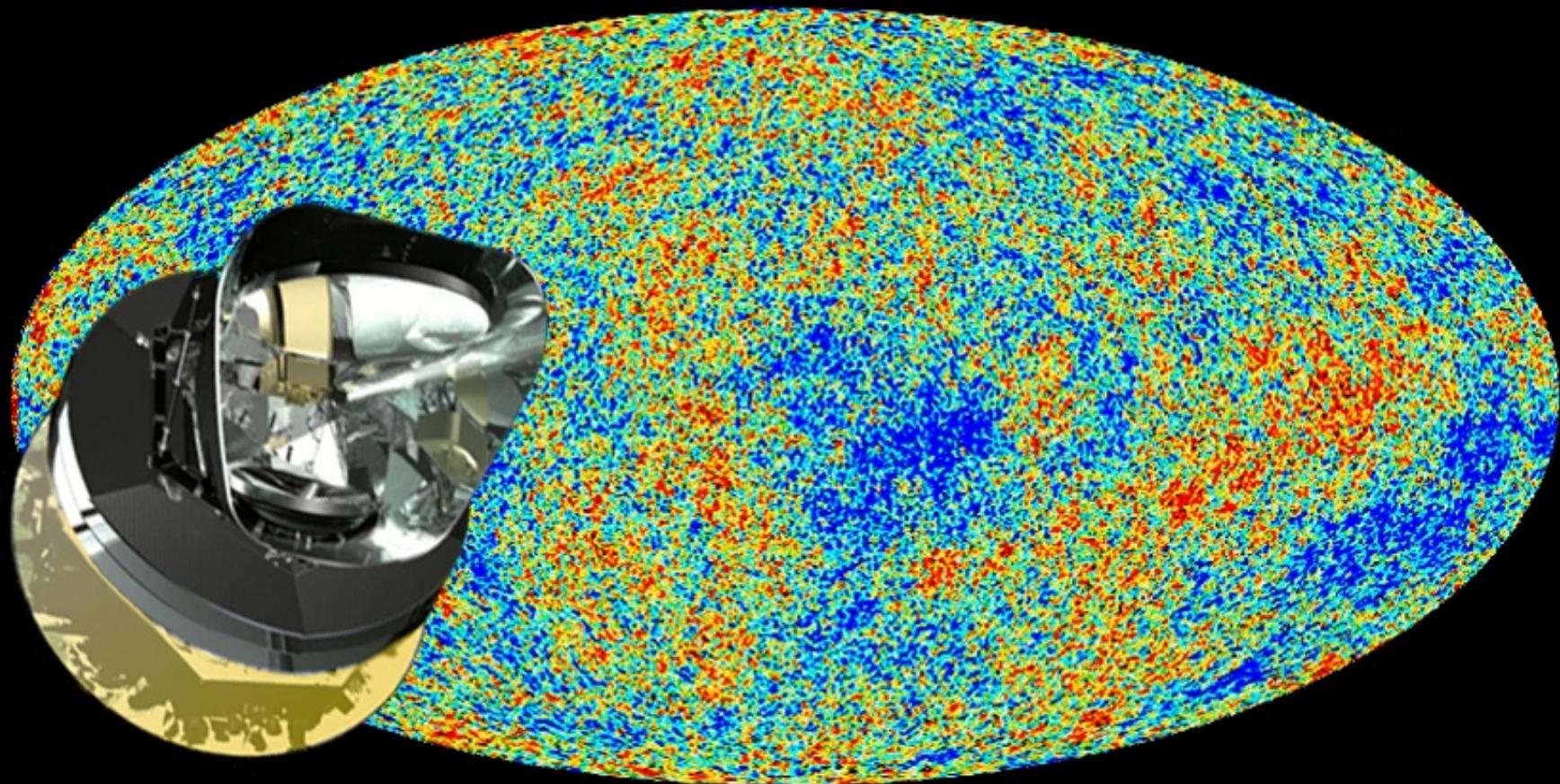
A Comprehensive Measurement of the Local Value of the Hubble Constant with $1 \text{ km s}^{-1} \text{ Mpc}^{-1}$ Uncertainty from the *Hubble Space Telescope* and the SH0ES Team

ADAM G. RIESS,^{1,2} WENLONG YUAN,² LUCAS M. MACRI,³ DAN SCOLNIC,⁴ DILLON BROUT,⁵ STEFANO CASERTANO,¹ DAVID O. JONES,⁶ YUKEI MURAKAMI,² GAGANDEEP S. ANAND,¹ LOUISE BREUVAL,² THOMAS G. BRINK,⁷ ALEXEY V. FILIPPENKO,^{7,8} SAMANTHA HOFFMANN,¹ SAURABH W. JHA,⁹ W. D'ARCY KENWORTHY,² JOHN MACKENTY,¹ BENJAMIN E. STAHL,⁷ AND WEIKANG ZHENG⁷

Astrophys. J. Lett. **934**, L7 (2022)



Indirect determination of Hubble constant from Cosmic Microwave Background



Quantum noise in time-dependent media and cosmic expansion

Ziv Landau^{1,2,*} and Ulf Leonhardt^{1,†}

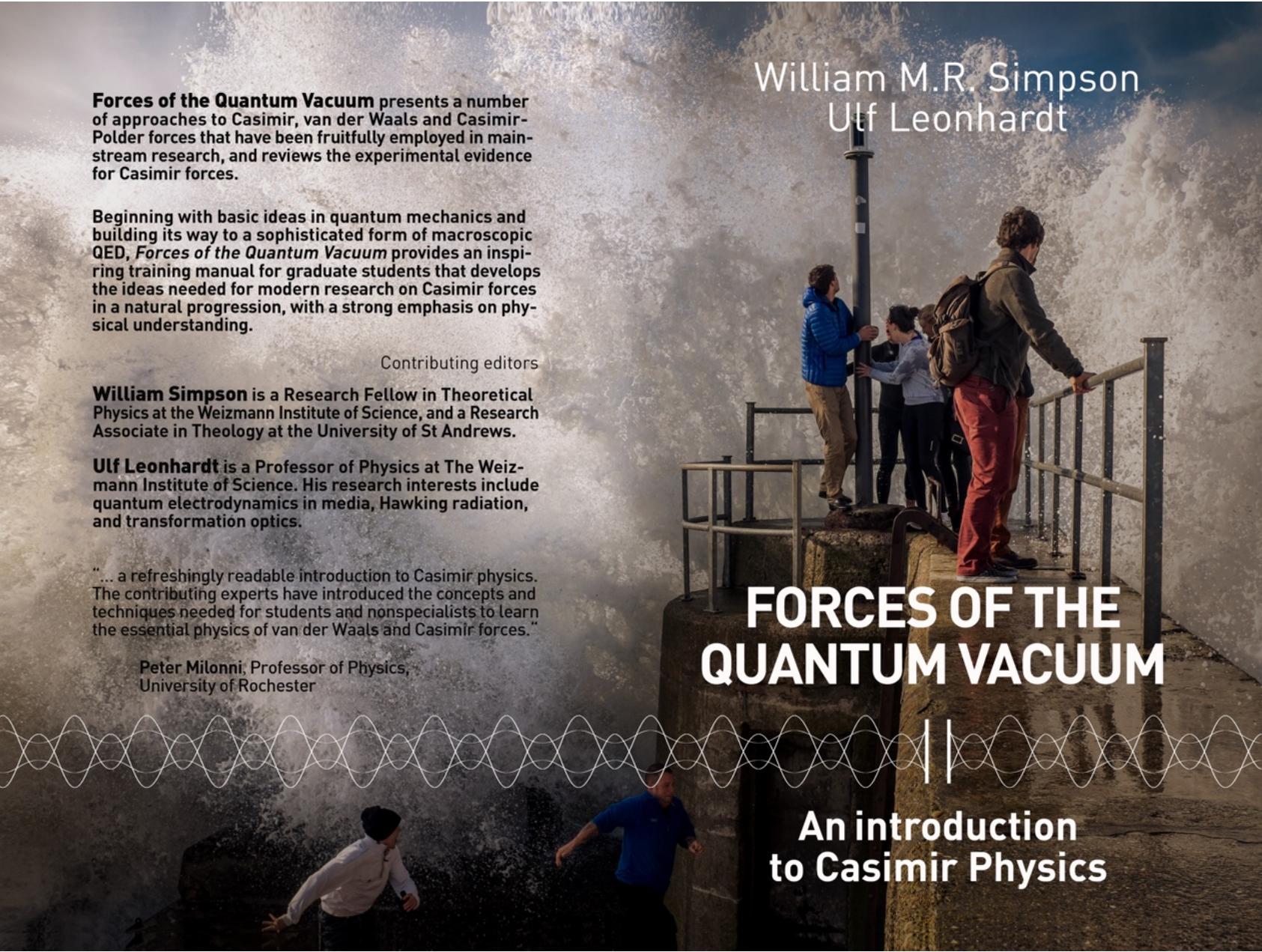
¹*Department of Physics of Complex Systems, Weizmann Institute of Science, Rehovot 761001, Israel*

²*St John's College, University of Cambridge, St John's St., Cambridge CB2 1TP, United Kingdom*

Quantum buoyancy:

**Observed Hubble
constant is
consistent with
Lifshitz theory**





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Contributing editors

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