Fast 3D Magnetic Resonance Fingerprinting for a Whole-Brain Coverage

Dan Ma, Yun Jiang, Yong Chen, Debra McGivney, Bhairav Mehta, Vikas Gulani, and Mark Griswold*

Purpose: The purpose of this study was to accelerate the acquisition and reconstruction time of 3D magnetic resonance fingerprinting scans.

Methods: A 3D magnetic resonance fingerprinting scan was accelerated by using a single-shot spiral trajectory with an undersampling factor of 48 in the x-y plane, and an interleaved sampling pattern with an undersampling factor of 3 through plane. Further acceleration came from reducing the waiting time between neighboring partitions. The reconstruction time was accelerated by applying singular value decomposition compression in k-space. Finally, a 3D premeasured $B_{\rm 1}$ map was used to correct for the $B_{\rm 1}$ inhomogeneity.

Results: The T_1 and T_2 values of the International Society for Magnetic Resonance in Medicine/National Institute of Standards and Technology MRI phantom showed a good agreement with the standard values, with an average concordance correlation coefficient of 0.99, and coefficient of variation of 7% in the repeatability scans. The results from in vivo scans also showed high image quality in both transverse and coronal views.

Conclusions: This study applied a fast acquisition scheme for a fully quantitative 3D magnetic resonance fingerprinting scan with a total acceleration factor of 144 as compared with the Nyquist rate, such that 3D T_1 , T_2 , and proton density maps can be acquired with whole-brain coverage at clinical resolution in less than 5 min. **Magn Reson Med 79:2190–2197, 2018.** © **2017 International Society for Magnetic Resonance in Medicine.**

Key words: MR fingerprinting; 3D; T₁; T₂; relaxometry

INTRODUCTION

Magnetic resonance fingerprinting (MRF) (1) is an acquisition and processing framework that uses a variable acquisition scheme to enable simultaneous quantification of multiple tissue properties, such as T_1 and T_2 . Currently, most MRF implementations and in vivo applications use 2D (2–10) and multislice acquisitions (11–13). However, to achieve higher through-plane resolution and better tissue characterization, extension to a 3D acquisition is desirable.

Department of Radiology, Case Western Reserve University, Cleveland, Ohio. USA.

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*Correspondence to: Mark Griswold, Ph.D., Department of Radiology, Case Western Reserve University, 11100 Euclid Avenue, Bolwell B121, Cleveland, OH 44106, USA. E-mail: mark.griswold@case.edu.

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In general, the two main concerns of a 3D MRF scan are (i) long acquisition time due to the increased number of excitations necessary to acquire the data; and (ii) signal intensity inhomogeneity across the 3D volume due to excitation profile imperfections and local changes in the B₁ field. Because 3D acquisitions potentially allow a higher acceleration factor and more flexible undersampling schemes as compared with 2D acquisitions, several fast 3D methods have been proposed previously by using non-Cartesian trajectories (14-19), fast sampling schemes (20-22), and incorporating parallel imaging and compressed sensing methods (23-25). Any inhomogeneity in the flip angle (FA) can cause errors, which lead to inaccurate T₁ and T₂ results for many quantitative measurements including MRF scans (26-28). The two common ways to correct for the FA error are to premeasure the B₁ or FA map (3,29,30), or to quantify B₁ at the same time as the tissue parameters (28,31,32).

The purpose of this study was to accelerate the 3D MRF scan and to correct for the FA error, to provide accurate T1 and T2 maps of a whole-brain scan in a clinically acceptable time. Specifically, this study applied a simple accelerated acquisition scheme similar to the k-t broad-use linear acquisition speed-up technique (21) for the 3D MRF scan, to allow a total factor of 144 acceleration as compared with the Nyquist rate, so that 3D T₁, T₂, and proton density (M₀) maps can be acquired from a whole brain with a resolution of $1.2 \times 1.2 \times 3 \,\mathrm{mm}^3$ in less than 5 min. In addition, because the 3D MRF scan acquired over 1000 undersampled volumes, a singular value decomposition (SVD) compression (7) was applied in k-space before reconstruction, to substantially reduce the computing memory and accelerate the postprocessing time. To correct for the FA error, a 3D slab-selective radiofrequency (RF) pulse with an optimized excitation profile was used to minimize the excitation profile variation across partitions (or slices in a 3D volume), and a 3D B₁ map that was premeasured using the Bloch-Siegert method (3,29) was used to measure the B₁ inhomogeneity. The B₁ values were then simulated into the dictionary to correct for inaccurate FAs and improve the accuracy of the resulting T₁ and T₂ values.

METHODS

Three-Dimensional Acceleration Scheme

The 3D slab-selective MRF with the fast imaging with steady state precession (FISP) based readout (2) was implemented by adding phase-encoding lines along the k_z direction from the 2D MRF. As a quick summary of the 2D MRF sequence (1,2), the MRF sequence was

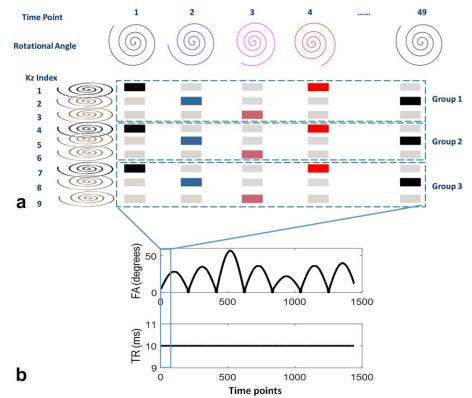


FIG. 1. Undersampling scheme (a) and FA and TR patterns (b) of the 3D MRF scan. a: Sampling scheme of a 3D MRF scan with nine partitions. The acquisition starts with the time domain first. Along the time points, the rotational angles of the spiral trajectories are changed with a step of 7.5°. With an acceleration factor of three, nine partitions are divided into three groups or repetitions. The colored kz lines are the ones that are acquired in the accelerated scan, whereas the gray kz lines are the ones that are skipped.

designed based on a TrueFISP or FISP sequence, but with randomized FAs and repetition times (TRs). To capture sufficient temporal information for multiparametric quantification, 1000 to 3000 time points (or TRs) were acquired, and one image was reconstructed at each time point. The resulting signal evolution in each pixel as a function of time was matched to a predefined dictionary to obtain multiple tissue properties (such as T₁, T₂, and M_0) simultaneously. In this study, the 3D acquisition acquired data along time points in the x-y plane first. After acquiring all of the time points at a certain phaseencoding line in kz, the kz increased and the same acquisition pattern (FA, TR, and spiral trajectories) was repeated. For each time point at each kz, a variable density spiral trajectory was used to sample the kx-ky data (note that spiral trajectory was designed to require 48 arms to fully sample the k-space) (2,33). After all sampling was complete, the spiral trajectory in kx-ky (in plane) and Cartesian phase encoding in kz (through plane) constitute a stack-of-spiral sampling pattern at each time point. However, to preserve the temporal fidelity of the rapidly changing MRF signals, the sampling order of this stack-of-spiral MRF acquisition is different from other time-resolved 3D acquisitions that acquire all kz lines for a time point before proceeding to the next time point.

If these data were acquired at the Nyquist rate, the scan duration would be prohibitively long. As shown in previous MRF studies, individual time points can be greatly undersampled to reduce imaging times. Here, the acceleration scheme, including both in-plane and through-plane acceleration, is proposed. In-plane acceleration was achieved by using a single spiral arm in each time point (or

TR) and for each kz. To improve spatial-temporal incoherence, a 7.5° (360/48) rotation of the trajectory was applied from one time point to the next, such that the aliasing artifacts from neighboring time points are different. This yielded an in-plane acceleration factor of 48. Throughplane acceleration was achieved by uniformly undersamping the kz lines in an interleaved fashion by a factor of three.

An example of this undersampled 3D MRF acquisition is shown in Figure 1 for a scan using nine kz lines. These nine kz lines were divided into groups based on the through-plane acceleration factor (in this case there are three groups for the undersampling factor of three). Specifically, in the first repetition, the first kz line was acquired at the first time point, then the second kz line was acquired at the second time point, then the third kz line at third time point, followed by the first kz line at the fourth time point, and so on. Additionally, because the rotational angle of the spiral trajectory was repeated in every 48th time point, at the 49th time point, instead of acquiring the first kz line, the second kz line was acquired in group 1. Thus, in addition to shifting the kz line by one for each time point, the index of the kz line was shifted by one at each multiple of 48 time points. After the kz lines at all time points were acquired in the first group, a waiting time with no excitation was applied to allow for the signal recovery, followed by the acquisition of the second group of kz lines, starting with the first kz line at the first time point again. After all undersampled 3D MRF data were acquired, this resulted in an undersampled, interleaved, stack-of-spirals sampling. This sampling pattern is similar to k-t broad-use linear acquisition speed-up technique and k-t sensitivity 2192 Ma et al.

encoding (21), which was used to shift the aliasing artifacts. The additional benefit of this sampling scheme was that the sampling density of each kz line as well as the sampling times of each rotational angle of the spiral trajectory were the same after the entire acquisition.

The scan time is further reduced by shortening the waiting time between neighboring groups. Although traditional relaxometry methods require spins to be fully relaxed before sampling each kz, MRF can account for partial relaxation of the spins by simulating the known waiting time between neighboring kz lines in the dictionary. This property of MRF provides some inherent acceleration, as it allows the minimization of the waiting time between neighboring groups.

Data Acquisition

All scans were performed in a 3T scanner system (Skyra, Siemens Healthcare, Erlangen, Germany). For both phantom and in vivo studies, a field of view of 300 imes 300 imes $144 \, \mathrm{mm}^3$ with a matrix of $256 \times 256 \times 48$ and an image resolution of $1.2 \times 1.2 \times 3 \, \text{mm}^3$ was acquired. Under an acceleration factor of three, 16 acquisition groups (or repetitions) were acquired. For each group, 1440 time points (30 repetitions of 48 rotation angles) were acquired with an acquisition time of 14 s, followed by a 3-s waiting time before the next group, to allow for relaxation and to improve signal-to-noise ratio. The FA and TR patterns are shown in Figure 1b. An asymmetric 3D slab-selective RF pulse with a duration of 2048 µs was used for excitation. Adiabatic inversion pulses were added at the first and the 1201th time points at each repetition, to improve sensitivity to T_1 . The total acquisition time was 4.6 min.

A 3D B_1 map was acquired separately using the Bloch-Siegert method before each MRF scan (3,29). To accelerate the scan, a B_1 map with a spatial resolution of 2.3 \times 2.3 \times 3 mm³ was first acquired. The B_1 map in each partition was then interpolated to a spatial resolution of 1.2 \times 1.2 mm² to match the spatial resolution of the tissue maps. The total acquisition time was 1.6 min.

The accuracy and repeatability of the 3D MRF scan were first validated using the International Society for Magnetic Resonance in Medicine/National Institute of Standards and Technology MRI phantom, which has T_1 and T_2 layers, each containing 14 spheres, with T_1 values ranging from 20 ms to 2 s, and T_2 values ranging from 8 to 600 ms (34,35). The phantom was scanned in 5 consecutive days by both B_1 and 3D MRF scans. The mean and standard deviations of the T_1 values in the T_1 layer as well as T_2 values from the T_2 layer were compared with those values measured by NMR experiment from the physical measurement laboratory at the National Institute of Standards and Technology (34).

The in vivo experiments were performed in five asymptomatic volunteers in an internal review board–approved study, including written informed consent before each scan. B_1 measurement and MRF scans were performed at the same 3D location. In the T_1 and T_2 maps from each volunteer, six regions including caudate nucleus, centrum semiovale, middle cerebellar pedencle, putamen, frontal white matter, and parietal white matter were selected. The T_1 and T_2 values in each tissue type

were first averaged for each volunteer, and then the mean and standard deviation of T_1 and T_2 values among five volunteers were calculated.

Dictionary Simulation

The dictionary used in the matching algorithm was simulated using the Bloch equations in MATLAB (The Math-Works, Natick, MA) and was introduced previously (1). In each TR, signal evolutions caused by RF excitation with nominal FAs, relaxation during echo time and TR times, and a 2π dephasing at the end of the TR from 200 isochromats were simulated. Because a 3D slab-selective RF pulse with an optimized excitation profile was applied, the RF profile was not simulated in the dictionary. To simulate the waiting time, the entire acquisition was simulated twice. At the end of the first repetition, relaxation during the waiting time was simulated. The resulting magnetization became the starting magnetization of the second repetition, in which the entire acquisition was simulated again. Based on the simulation from a wide range of T₁ and T₂ combinations, the starting magnetization was stable after the second repetition. Each isochromat was simulated independently for the whole sequence before summing over the voxel.

The B_1 values were simulated as an additional dimension of the dictionary, with a range between 0.7 and 1.5 in steps of 0.02. The actual FAs were calculated as nominal FAs multiplied by B_1 . For each B_1 value, a total of 12001 signal evolutions, each with 1440 time points, were simulated for a range of possible T_1 values (2 to 100 ms in steps of 2, 120 to 2000 ms in steps of 20, and 2000 to 3000 ms in steps of 40 ms) and T_2 values (2 to 130 ms in steps of 2 ms, 140 to 200 ms in steps of 10 ms, 200 to 1000 ms in steps of 20 ms, and 1040 to 2000 in steps of 40 ms). The simulation time was 5.7 min for each B_1 value and 3.4 h for the entire dictionary on a standalone personal computer.

Accelerated Postprocessing

Because 1440 undersampled 3D volumes were acquired, which could lead to a large memory requirement and long computing time for both reconstruction and template matching, a SVD compression method (7) was applied to the k-space data before the reconstruction. Specifically, the SVD of the full dictionary was first computed, which takes 4 min.

$$D = U\Sigma V^*$$
 [1]

The first k = 25 of the singular vectors were used to project the raw data and the full dictionary to the SVD space.

$$D \approx U_k \Sigma_k V_k^*$$
 [2]

$$Y_k = U_k^* Y ag{3}$$

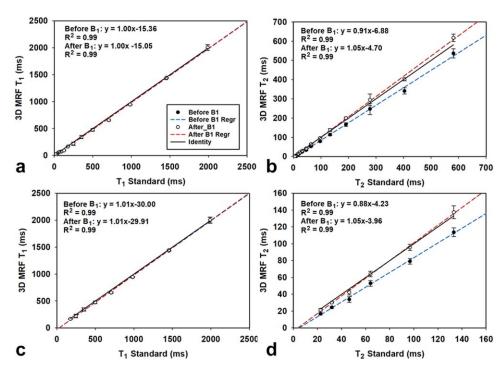
$$X_k = G^* Y_k \tag{4}$$

$$D_k = U_k^* D [5]$$

where in Equation [2], $U_k \in \mathbb{C}^{t \times N_k}$ is the first N_k of the left singular vector of the dictionary, and t is the number of TRs. In Equation [3], $Y \in \mathbb{C}^{t \times M}$ is the sampled k-space data,

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FIG. 2. Accuracy and repeatability of the qMRI phantom scan. a, b: T₁ and T₂ values from 14 spheres from the International Society for Magnetic Resonance in Medicine/ National Institute of Standards and Technology phantom are compared with the values from the spin-echo measurement. c, d: The same results but with a reduced T₁ range between 181 and 2038 ms, and a reduced T2 range between 26 and 143 ms. The blue line and red line in each plot are the linear regression results before and after B₁ correction, respectively.



in which $M = N_{coils} \times N_{samples_per_spiral} \times N_{spirals} \times N_{kz}$, and $Y_k \in \mathbb{C}^{N_k \times M}$ is the compressed k-space data in the SVD space. After projecting the raw data to the SVD space, instead of reconstructing 1440 undersampled 3D volumes, only 25 3D volumes with the compressed k-space data were reconstructed, which substantially reduced the computational effort. Each 3D volume was reconstructed using the GPU-NUFFT toolbox (36) with separately measured spiral trajectories (37). In Equation [4], X_k is the reconstructed images, with the size of $25 \times 256 \times 256 \times 48$, and G is the NUFFT operator. To correct for B₁ inhomogeneity, the same U_k as to compress the raw data were also used to project the full dictionary with different B₁ values to the SVD space. In Equation [5], $D \in \mathbb{C}^{t \times N_{t1t2} \times N_{B1}}$ is the full dictionary and D_k $\in \mathbb{C}^{N_k \times N_{t1t2} \times N_{B1}}$ is the compressed dictionary. In this way, pattern recognition could be performed between X_k and D_k , which are much smaller than the original full matrix X and D. Based on the measured B₁ map, the compressed signal evolution in each pixel was matched to those entries in the compressed dictionary that have the closest B₁ values as measured. The maximum inner-product value from the match gave rise to T₁, T₂, and M₀ values. The postprocessing time of generating B_1 -corrected T_1 , T_2 , and M_0 maps for a matrix size of $256 \times 256 \times 48$ was $48 \, \text{min}$ in MATLAB (The MathWorks Inc, Natick, MA).

RESULTS

Figure 2 shows the accuracy and repeatability results of the 3D MRF scan before and after the B_1 correction, with bidirectional error bars representing the standard deviation of five measurements. Figures 2a and 2b show the results from all 14 spheres of each layer, and Figures 2c and 2d show the same results but with a reduced T_1 range between 181 and 2038 ms and a reduced T_2 range between 26 and 143 ms, which correspond to the main physiological range

of the brain tissues. The linear regression and R^2 of the results before and after the B_1 correction are also listed in each plot. As shown in the figure, although the B_1 correction has little effect on the T_1 results, it greatly improves the accuracy of the T_2 results. After the B_1 correction, MRF results are generally in good agreement with the results from the reference values, with a concordance correlation coefficient (38) of 0.99 for both T_1 and T_2 . The MRF scans also demonstrate high repeatability, with an average coefficient of variation of 6.9% for T_1 and 6.6% for T_2 .

Figures 3 and 4 illustrate the T_1 and T_2 maps in the axial view and coronal view, respectively, from one of the volunteer scans. To illustrate the B_1 effects, Figure 3 shows the B_1 maps, as well as T_1 and T_2 maps before and after B_1 correction. Similar to the phantom results, the B_1 effects are more visible from T_2 maps. Table 1 summarizes the T_1 and T_2 values from six regions of the brain maps. The T_1 and T_2 values, along with the size of the regions of interest, and the mean \pm standard deviation of the T_1 and T_2 values among the five volunteers, are listed. Based on Table 1, the T_1 and T_2 values from each region are relatively consistent among these five healthy volunteers.

DISCUSSION

In this study, a fast acquisition scheme was applied for a fully quantitative 3D MRF scan in less than 5 min of acquisition time, demonstrating T_1 , T_2 , and M_0 maps with $1.2 \times 1.2 \times 3 \, \text{mm}^3$ resolution and a whole-brain coverage. A separate 1.6-min B_1 measurement scan was performed before the 3D scan. The resulting B_1 map was used to correct for B_1 inhomogeneity effects and improve the accuracy of T_1 and T_2 estimates. In fact, both B_1 and 3D MRF scans can be further accelerated. A fast Bloch-Siegert scan has been proposed to measure the 3D B_1 maps in only 32 s (39,40). By incorporating advanced reconstruction methods,

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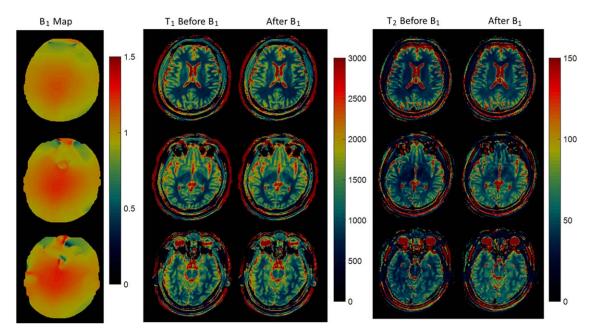


FIG. 3. B₁, T₁, and T₂ maps from a 3D in vivo scan in axial view.

substantial reduction of the scan time and/or further improvement of the spatial resolution can be achieved for 3D MRF scans. For example, by using low-rank reconstruction methods (41,42), the scan time of the 3D MRF scan with the same spatial resolution and tissue coverage can be reduced to only 2.7 min. The same method has also been used to achieve a higher isotropic image resolution $(1.2 \times 1.2 \times 1.2 \text{ mm}^3)$ (43). Optimization of the MRF scan could also lead to a reduction of the scan time (44,45). In addition, a method has been proposed to simultaneously

quantifying B_1 as well as tissue properties without compromising the scan time (46).

Acceleration of the acquisition was achieved in three steps: (i) intrinsic acceleration using short waiting times between neighboring phase-encoding lines, (ii) in-plane acceleration factor of 48, and (iii) through-plane acceleration factor of 3. The in-plane acceleration has been demonstrated previously in 2D MRF scans, which took the advantage of the variable density spiral sampling pattern to generate incoherent aliasing artifacts both in each image

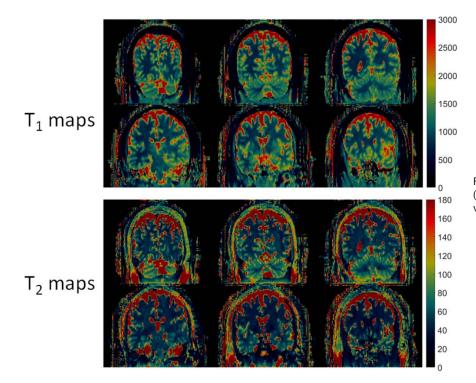


FIG. 4. Three-dimensional T_1 (ms) and T_2 (ms) maps from an in vivo scan in coronal view.

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Table 1 In Vivo T_1 and T_2 Values and the Size of the Regions of Interest From Five Volunteers Scanned From a 3T Scanner.

		v1	v2	v3	v4	v5	mean±std
Caudate Nucleus	T ₁	1397.2	1493.5	1293.5	1397.9	1368.9	1390.2±71.7
	T_2	42.1	38.9	53.4	40.9	44.7	44.0±5.6
	ROI	38	27	17	23	24	
Centrum Semiovale	T ₁	875.9	866.6	823.1	863.1	866.4	859.0±20.6
	T_2	39.7	33.6	40.3	34.4	41.2	37.8±3.5
	ROI	108	102	145	149	207	
Middle Cerebellar	T ₁	874.7	942.5	906.1	918.9	881.5	904.7±27.7
Pedencle	T_2	52.7	38.7	25.7	37.8	49.0	40.8
	ROI	72	54	47	75	87	
Putamen	T ₁	1285.9	1314.0	1169.5	1238.4	1234.3	1248.5±55.3
	T_2	40.7	36.9	43.0	38.6	39.1	39.7 ± 2.3
	ROI	37	52	24	32	55	
Frontal_wm	T ₁	843.1	854.3	794.8	809.1	818.1	823.9 ± 24.5
	T_2	30.8	29.1	42.6	35.1	35.6	34.6 ± 5.3
	ROI	51	68	61	78	85	
Parietal_wm	T ₁	783.3	817.9	904.5	793.7	781.2	816.1±51.5
	T ₂	46.8	37.7	36.8	36.1	43.1	40.1 ± 4.6
	ROI	79	85	45	31	100	

Note: Units are in ms.

std, standard deviation; ROI, region of interest.

and through time. The through-plane acceleration was achieved using a uniform undersampling pattern similar to the k-t sampling pattern. This pattern shifted the aliasing artifacts from one time point to the next, to create incoherent artifacts through time. This pattern also guaranteed that all 48 rotational angles of the spiral trajectory were used at the same rate (30 times for each spiral angle), and all kz lines were sampled at the same density. For this reason, no density compensation was needed along kz, although density compensation was still needed in the kx-ky plane for the image reconstruction. In this study, all maps were generated by direct reconstruction and template matching. Advanced reconstruction methods that have been recently proposed for the 2D MRF could be applied in 3D MRF, to further reduce the acquisition time or improve the image quality (47,48). Other sampling schemes such as variable density sampling can also be applied to the partition direction, to potentially improve the sampling efficiency and increase the undersampling factor (49,50).

For a 3D scan with large volume coverage, B₁ variation and its effect on the resulting T₁ and T₂ estimation are not negligible. In this study, the Bloch-Siegert B₁ mapping method was performed separately before each MRF scan, and the resulting B₁ map was used to correct for the B₁ effect. Other approaches to correct for the B₁ effect, such as quantifying B1 at the same time as T1 and T₂, can also be applied (28,31). However, none of these methods has been effectively applied to 3D scans with such a high undersampling ratio. Although a separate scan to measure B₁ takes additional time, it reduces the sensitivity to potential tissue or system parameters, and thus reduces the amount of information and acquisition time required for the MRF scan. In addition, previous knowledge of the B₁ map reduces the dimensionality of the dictionary in pattern matching to estimate the tissue properties, which can lower the risk of mismatch and error propagation, especially in the presence of strong aliasing artifacts and with low signal-to-noise ratio from accelerated scans.

Based on the results obtained from the International Society for Magnetic Resonance in Medicine/National Institute of Standards and Technology MRI phantom, the 3D MRF scan shows high accuracy and repeatability as compared with the reference measurement. As described in our previous 2D study (51), we have consistently seen T₂ difference between our results after B₁ correction and literature-reported values acquired using fast spin-echo methods (2,52,53). Many groups have shown similar T₂ reduction by correcting for stimulated echoes (54), slice profile (27,51), magnetization transfer (55), and finite RF pulse effects (56). The lower T2 values may also be related to tissue microstructure, intravoxel dephasing (57), and diffusion effect from the spoiling gradients used in the FISP sequence (58). These effects may also cause the T₂ variation between frontal and parietal white matter regions, as given in Table 1. An exact analysis of this phenomenon is the subject of a future investigation.

In this study, a 3D MRF scheme with the FISP readout was used, which is less sensitive to the B_0 inhomogeneity for large volume coverage. Therefore, this 3D MRF scheme has the potential to be used in other parts of the body. In addition, with a large flexibility on the MRF sequence design, navigation and magnetization preparation can be added to the sequence to make the 3D MRF scan robust to different applications.

CONCLUSIONS

A fast acquisition scheme for a 3D MRF scan with a whole-brain coverage was presented. Three-dimensional T_1 , T_2 , and M_0 maps with a spatial resolution of $1.2 \times 1.2 \times 3 \, \text{mm}^3$ can be generated in 4.6 min. An additional 1.6-min B_1 scan was used to reduce the system and subject-related variations, and thus improve the accuracy of quantitative estimates. Given that this FISP-based sequence is also insensitive to the B_0 inhomogeneity, the proposed MRF scan could have wide and robust clinical applications.

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