### 1 Motivations

- 1. A policy should accomplish diverse and unknown user-specified goal at test time.
- 2. If the goal specified at test time is unknown, then the policy needs to perform well on all possible goals.
- 3. Then, the goal proposal distribution, from which we sample goals for the policy to practice, should be the uniform distribution over the set of possible goals.
- 4. However, we do not know this set a prior and can only observe sample from the set.
- 5. State and goal are assumed to be equivalent in this paper.
- 6. At each iteration, we can sample state by performing goal-directed exploration. How do we construct the goal proposal distribution at each iteration such that it converges to the uniform dist. over the set of possible goals over time?

### 2 Abstraction

- 1. To analyze the setting, we abstract away needless details of this process.
- 2. A goal  $\mathbf{G} \sim p_{\phi}$  is sampled from the goal dist., and then the agent attempts to achieve this goal, which results in a distribution of states  $\mathbf{S} \in \mathcal{S}$  seen along the trajectory.
- 3. The marginal dist. over **S** is written as  $p(\mathbf{S}|p_{\phi})$

# 3 Skew Fit Algorithm

- 1. Given a generative model  $p_{\phi_t}$  at iteration t, they want to obtain  $p_{\phi_{t+1}}$  such that  $p_{\phi_t}$  has higher entropy than  $p_{\phi_t}$  over the set of possible goal.
- 2. While they do not know the set of valid states, they can sample state from  $p(\mathbf{S}|p_{\phi})$ , resulting in an empirical distribution over the states

$$p_{\text{emp}_t}(\mathbf{s}) \triangleq \frac{1}{N} \sum_{n=1}^{N} \mathbf{1} \left\{ \mathbf{s} = \mathbf{S}_n \right\}, \quad \mathbf{S}_n \sim p\left(\mathbf{S}|p_{\phi_t}\right)$$

- 3. They use this empirical dist. to train the next generative model  $p_{\phi_{t+1}}$ .
- 4. However, doing this does not guarantee that the entropy of  $p_{\phi_{t+1}}$  is higher than the entropy of  $p_{\phi_t}$
- 5. They thus train the generative model to approximate the uniform dist.

$$argmax_{\phi} \mathbb{E}_{\mathbf{S} \sim U_{\mathcal{S}}} \left[ \log p_{\phi}(\mathbf{S}) \right]$$

6. To get an unbiased estimate of the obj, they invoke importance sampling

$$\mathbb{E}_{\mathbf{S} \sim U_{\mathcal{S}}} \left[ \log p_{\phi}(\mathbf{S}) \right] = \mathbb{E}_{\mathbf{S} \sim p_{\text{emp } t}} \left[ \frac{U_{\mathcal{S}}(\mathbf{S})}{p_{\text{emp } t}(\mathbf{S})} \log p_{\phi}(\mathbf{S}) \right] \propto \mathbb{E}_{\mathbf{S} \sim p_{\text{emp } t}} \left[ \frac{1}{p_{\text{emp } t}(\mathbf{S})} \log p_{\phi}(\mathbf{S}) \right]$$

- 7. They argue that computing  $p_{\text{emp}_t}$  requires marginalizing out the MDP dynamics, they thus approximate it with  $p_{\phi_t}$ .
- 8. Presumably to trade off bias for lower variance, they introduce a new hyper-param  $\alpha$  and weight each state by

$$w_{t,\alpha}(\mathbf{S}) \triangleq p_{\phi_t}(\mathbf{S})^{\alpha}, \quad \alpha < 0$$

9. To further reduce variance, they invoke sampling importance sampling (SIR), rather than sampling from the empirical distribution and weighting each sample, SIR explicitly defines each dist. as

$$p_{\text{skewed }t}(\mathbf{s}) \triangleq \frac{1}{Z_{\alpha}} p_{\text{emp }t}(\mathbf{s}) w_{t,\alpha}(\mathbf{s}), \quad Z_{\alpha} = \sum_{n=1}^{N} p_{\text{emp }t}(\mathbf{S}_{n}) w_{t,\alpha}(\mathbf{S}_{n})$$

- 10. They then fit  $p_{\phi_{t+1}}$  to  $p_{\text{skewed }t}$  with MLE.
- 11. At iteration t+1, to sample goal for the goal-conditioned policy, they can either use  $p_{\text{skewed }t}$  or  $p_{\phi_{t+1}}$ .

# 4 Skew Fit analysis

- 1. They first show that if the entropy of  $p_{\phi_{t+1}}$  is always larger than the entropy of  $p_{\phi_t}$  and is equal iff  $p_{\phi_t}$  is the uniform dist., then  $p_{\phi}$  converges to the uniform dist.
- 2. They then show that the condition for the entropy of  $p_{\phi_{t+1}}$  to be larger than the entropy of  $p_{\phi_t}$  is that the log density of  $p_{\text{emp}_t}$  and  $p_{\phi_t}$  should be correlated.
- 3. They argue that this should happen for a high performing goal-conditioned policy, since  $p_{\text{emp}_t}$  is the distribution resulting from trying to reach goals sampled from  $p_{\phi_t}$ .

# 5 Interesting bits from experimental section

- 1. They argue that their methods lead to diverse goals proposed to the goal-condition policy, while previous methods only propose goals closed to the initial state distribution.
- 2. They argue that the most common failure of prior methods is that the goal distribution collapse, resulting in the agent only learning to reach a fraction of the state.