



Edge

CS172 Computer Vision I

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Agenda

- Edge
 - Image gradient
 - Derivatives with convolution
 - Gaussian derivative filter
- Texture

Edge Detection



[Winter in Kraków photographed by Marcin Ryczek](#)

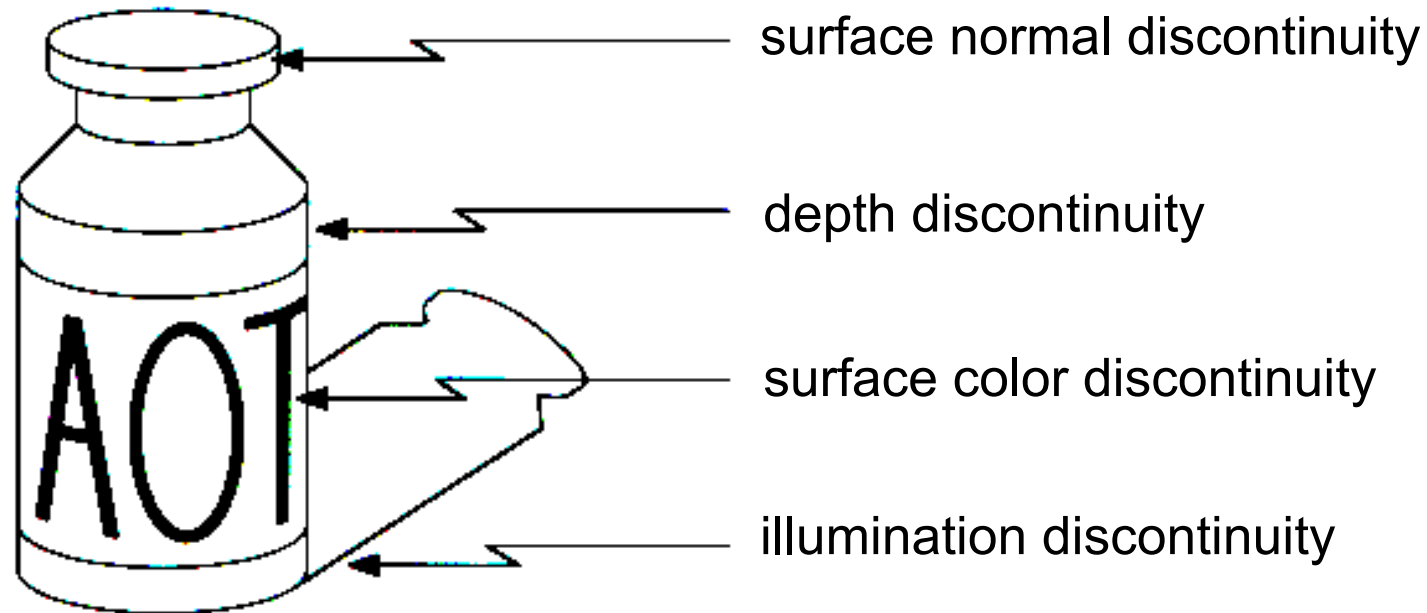
Edge Detection

- **Goal:** Identify sudden changes (**discontinuities**) in an image.
 - Intuitively, most semantic and shape information from the image can be encoded in the edges
 - More compact than pixels
- **Ideal:** artist's line drawing (but artist is also using object-level knowledge)



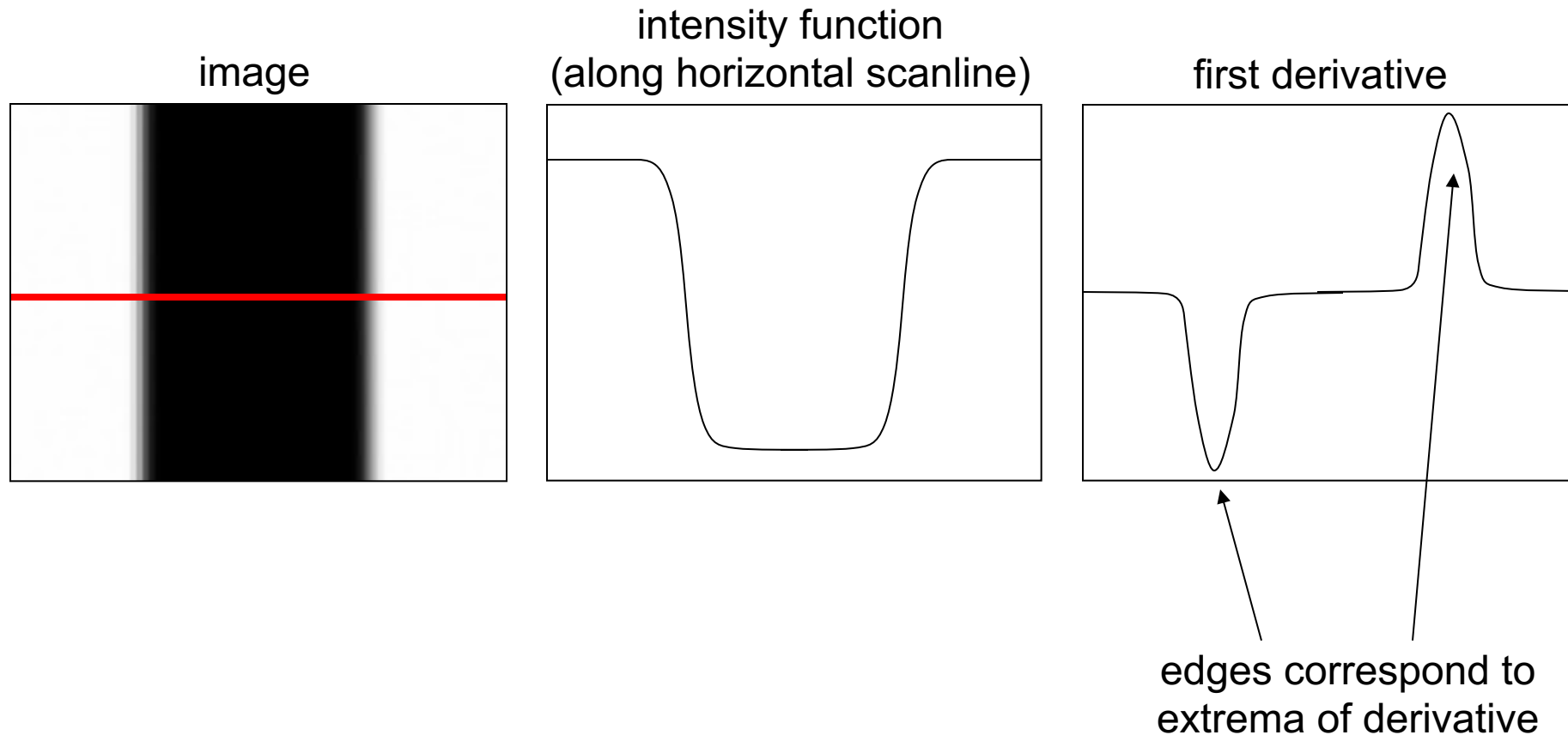
Origin of Edges

Edges are caused by a variety of factors:



Characterizing Edge

- An edge is a place of rapid change in the image intensity function



Derivatives with Convolution

For 2D function $f(x, y)$, the partial derivative is:

$$\frac{\partial f(x, y)}{\partial x} = \lim_{\varepsilon \rightarrow 0} \frac{f(x + \varepsilon, y) - f(x, y)}{\varepsilon}$$

For discrete data, we can approximate using finite differences:

$$\frac{\partial f(x, y)}{\partial x} \approx \frac{f(x + 1, y) - f(x, y)}{1}$$

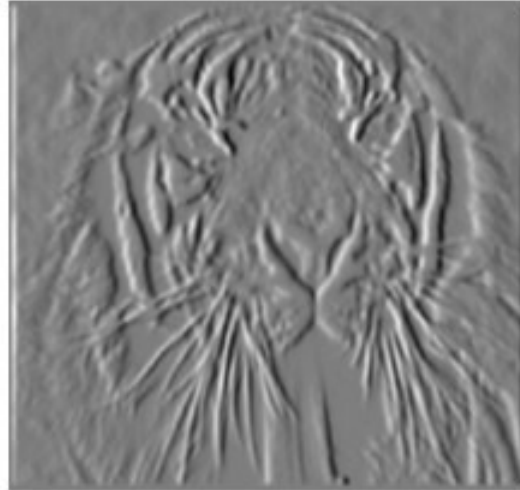
To implement the above as convolution, what would be the associated filter?

Partial Derivatives of an Image



$$\frac{\partial f(x, y)}{\partial x}$$

-1	1
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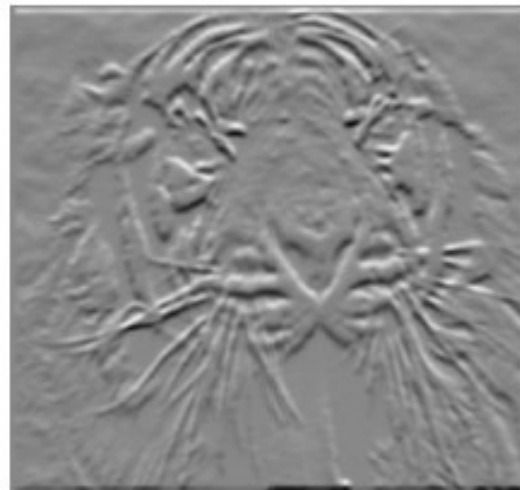


$$\frac{\partial f(x, y)}{\partial y}$$

-1
1

 or

1
-1



Which shows changes with respect to x?

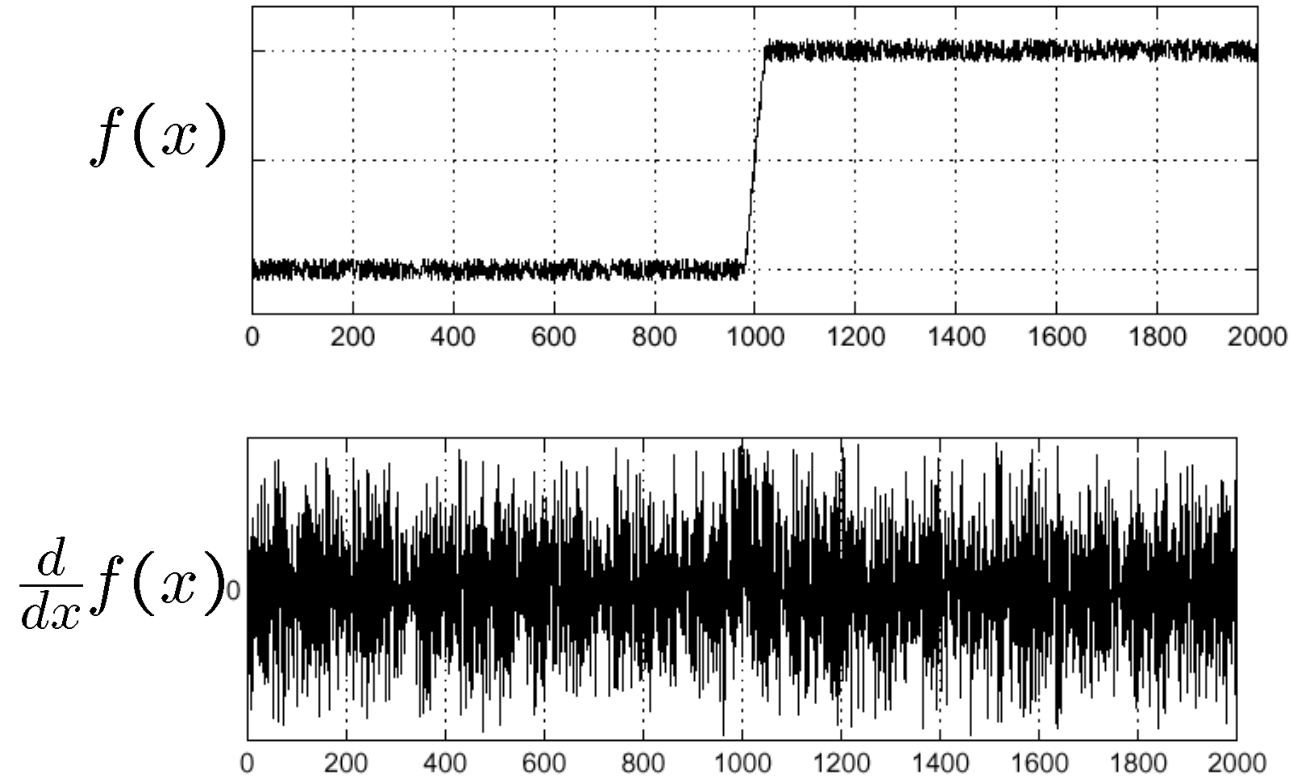
Gradient Magnitude



$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

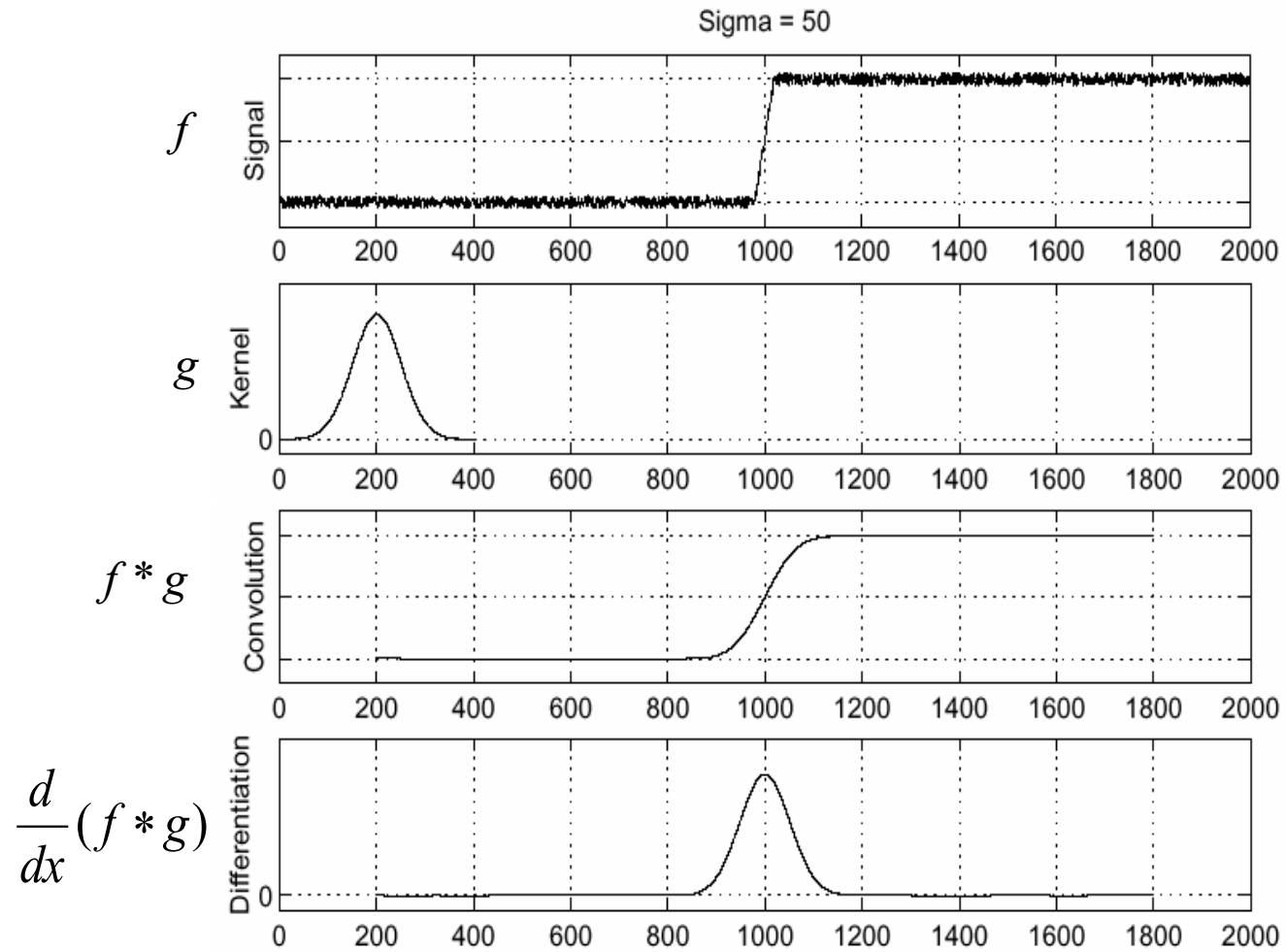
Effects of Noise

- Consider a single row or column of the image



Where is the edge?

Solution: Smooth First



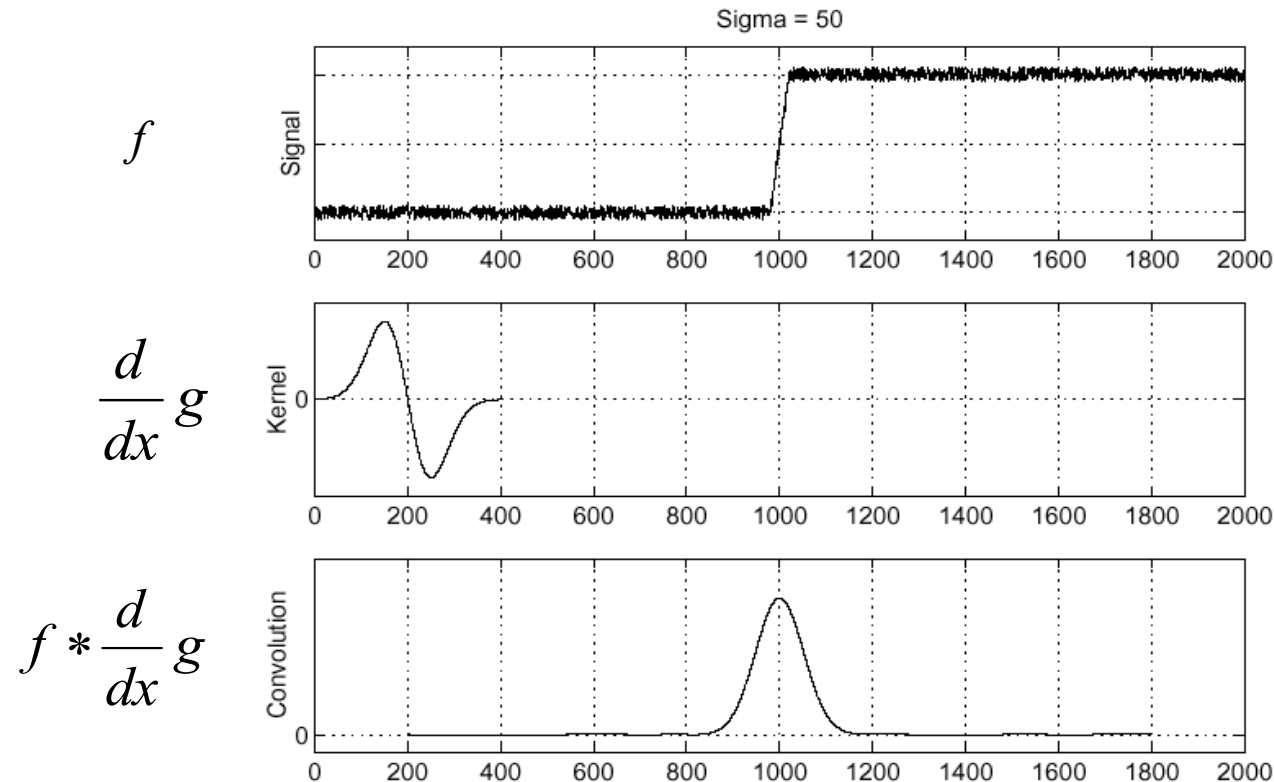
To find edges, look for peaks in $\frac{d}{dx}(f * g)$

Derivative Theorem of Convolution

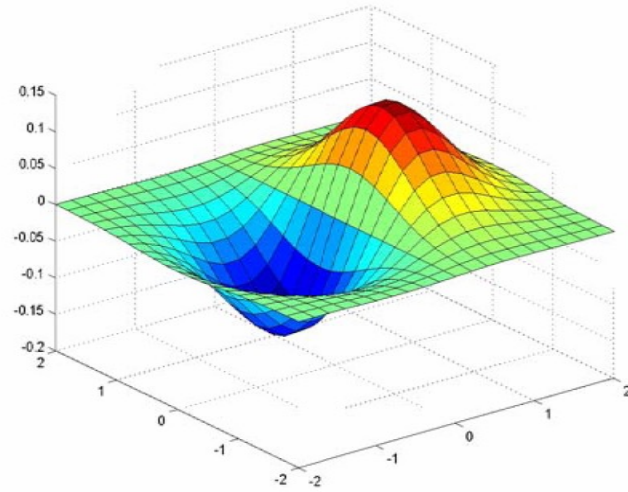
- Differentiation is convolution, and convolution is associative:

$$\frac{d}{dx}(f * g) = f * \frac{d}{dx}g$$

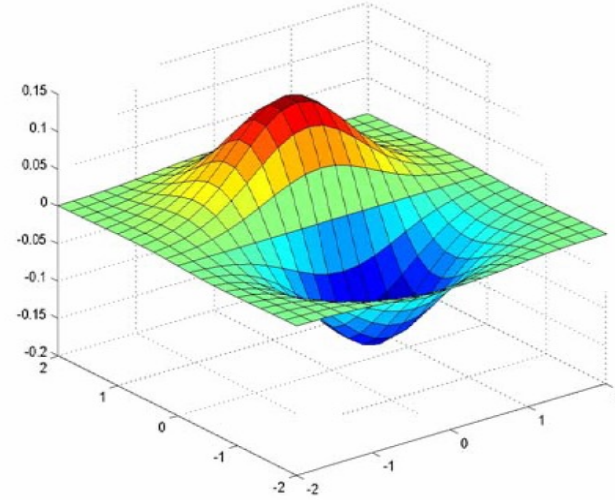
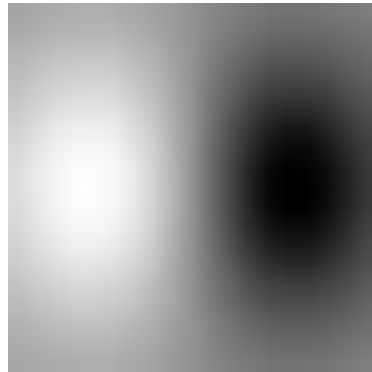
- This saves us one operation:



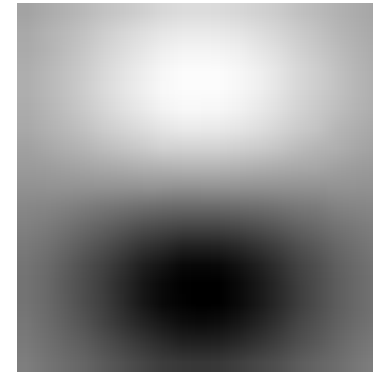
Derivative of Gaussian Filters



x-direction



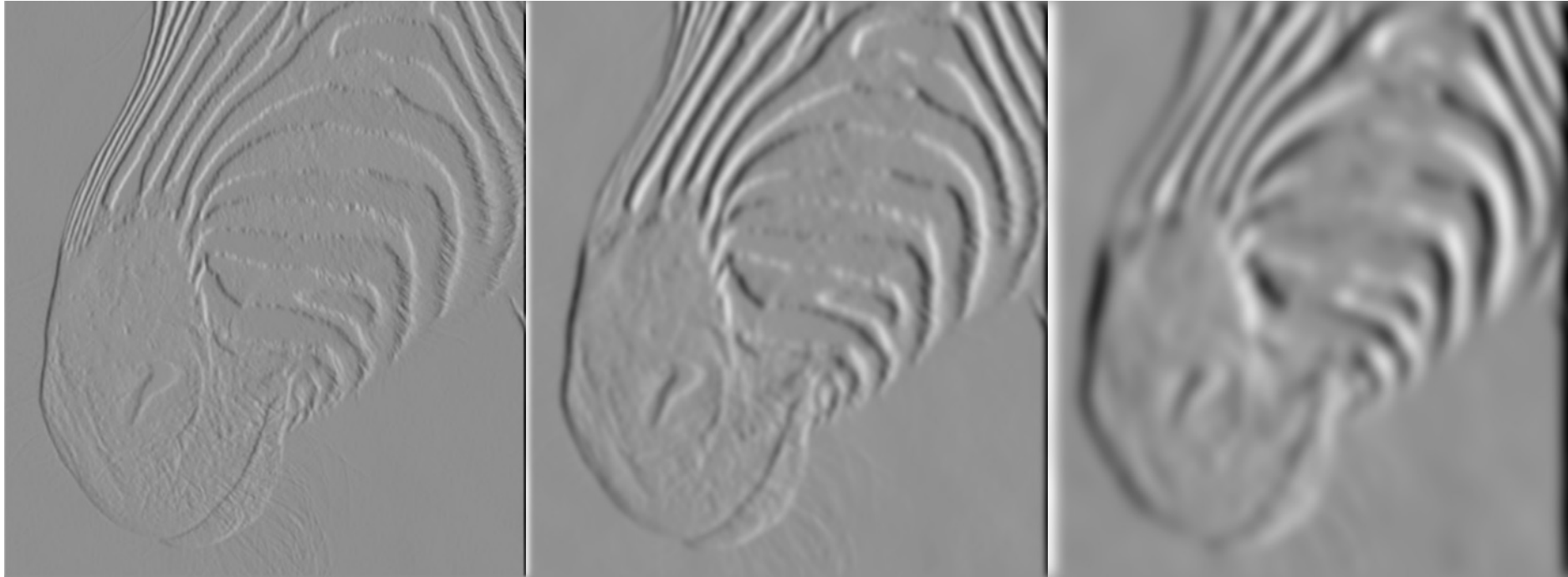
y-direction



Which one finds horizontal/vertical edges?

Are these filters separable?

Scale of Gaussian Derivative Filter



1 pixel

3 pixels

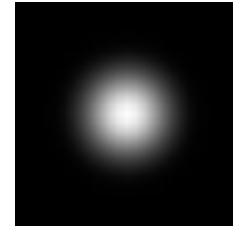
7 pixels

Smoothed derivative removes noise, but blurs edge.
Also finds edges at different “scales”

Review: Smoothing vs. Derivative Filters

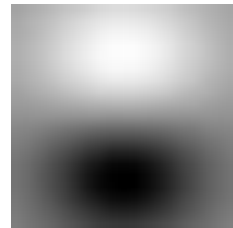
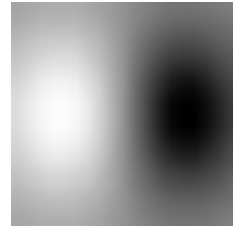
- Smoothing filters

- Gaussian: remove “high-frequency” components; “low-pass” filter
- Can the values of a smoothing filter be negative?
- What should the values sum to?
 - **One:** constant regions are not affected by the filter



- Derivative filters

- Derivatives of Gaussian
- Can the values of a derivative filter be negative?
- What should the values sum to?
 - **Zero:** no response in constant regions



Sobel Operator

$$g_x = \begin{bmatrix} -1 & 0 & 1 \end{bmatrix} * \frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

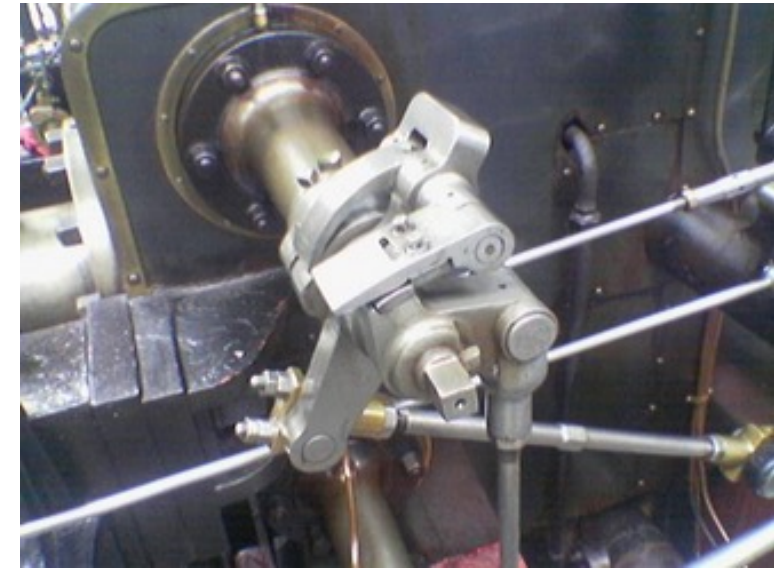
$$g_x = \begin{array}{|c|c|c|} \hline -1 & 0 & 1 \\ \hline -2 & 0 & 2 \\ \hline -1 & 0 & 1 \\ \hline \end{array}$$

$$g_y = \begin{array}{|c|c|c|} \hline -1 & -2 & -1 \\ \hline 0 & 0 & 0 \\ \hline 1 & 2 & 1 \\ \hline \end{array}$$

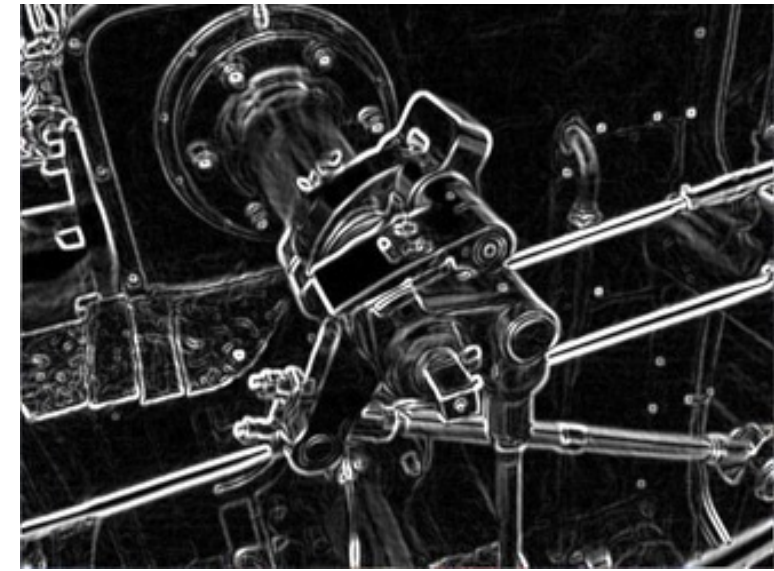
Magnitude:

$$g = \sqrt{g_x^2 + g_y^2}$$

The kernel is already flipped for simplicity



An example image from [wiki](#)

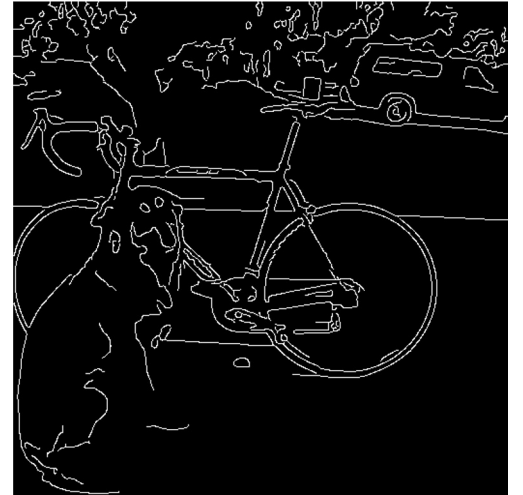


The Sobel operator applied to that image

Canny Edge Detection

Algorithm:

- 1. Smooth image (only want “real” edges, not noise)
- 2. Calculate gradient direction and magnitude
- 3. Non-maximum suppression perpendicular to edge
- 4. Threshold into strong, weak, no edge
- 5. Connect together components



Canny Edge Detection: Smooth



Gaussian filter



Canny Edge Detection: Gradient



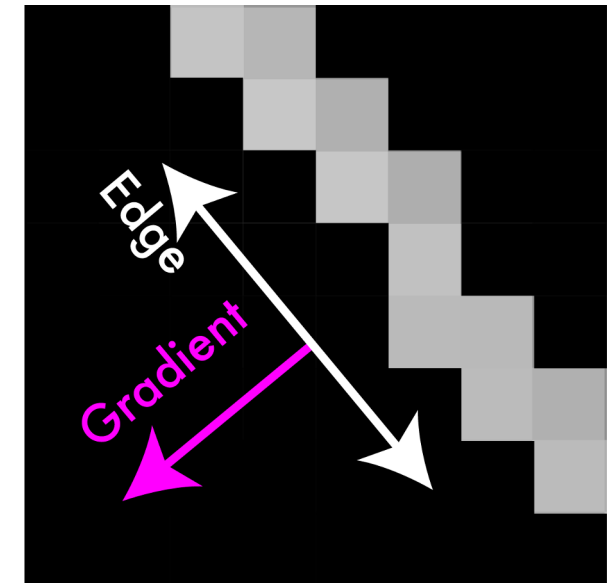
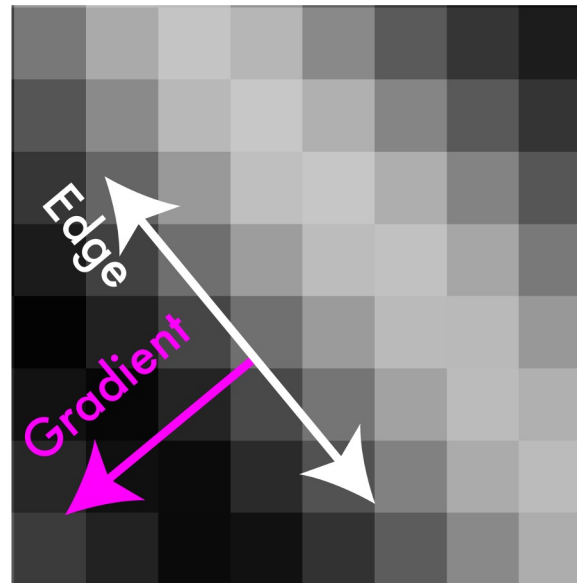
Sobel operator



Canny Edge Detection: Non-Maximum Suppression



- Want single pixel edges, not thick blurry lines
- Need to check nearby pixels
- See if response is highest

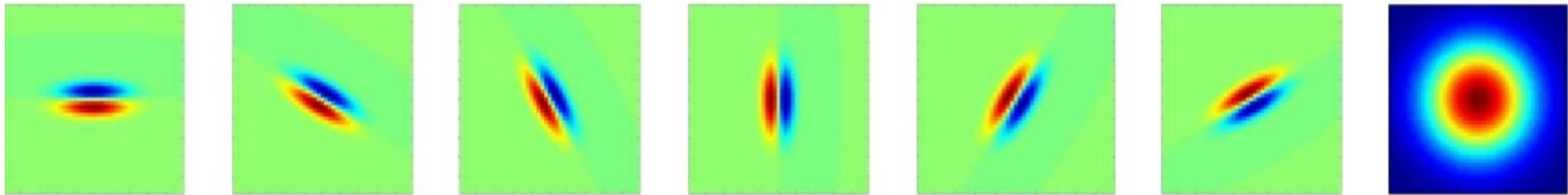


Texture



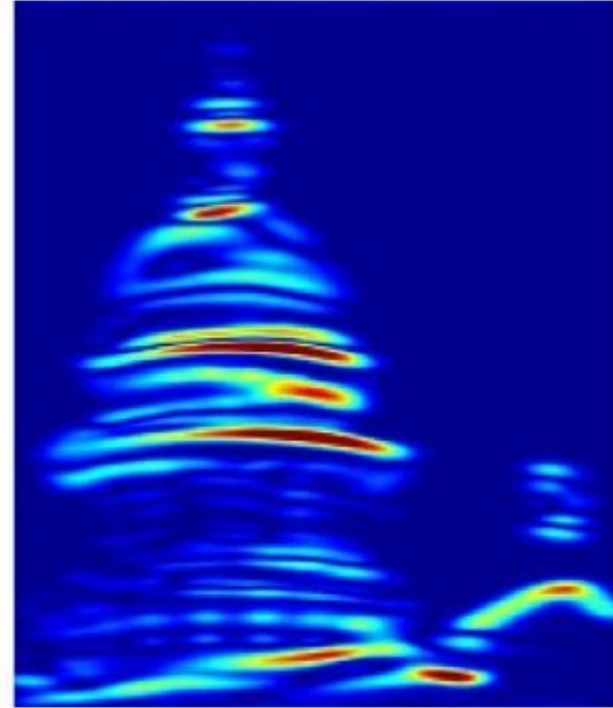
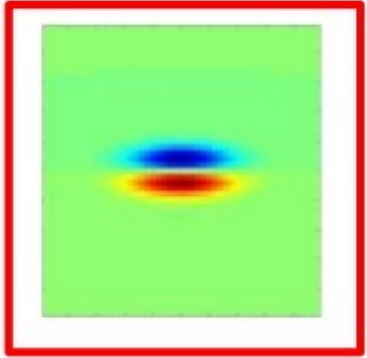
An **image texture** is the small-scale structure perceived on an image, based on the **spatial arrangement of color or intensities**.

Kernels to Detect Texture

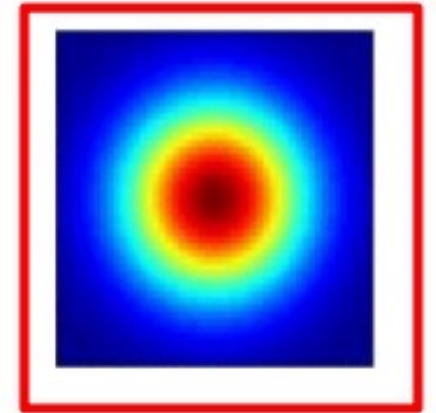


Describe what kind of pattern should be detected

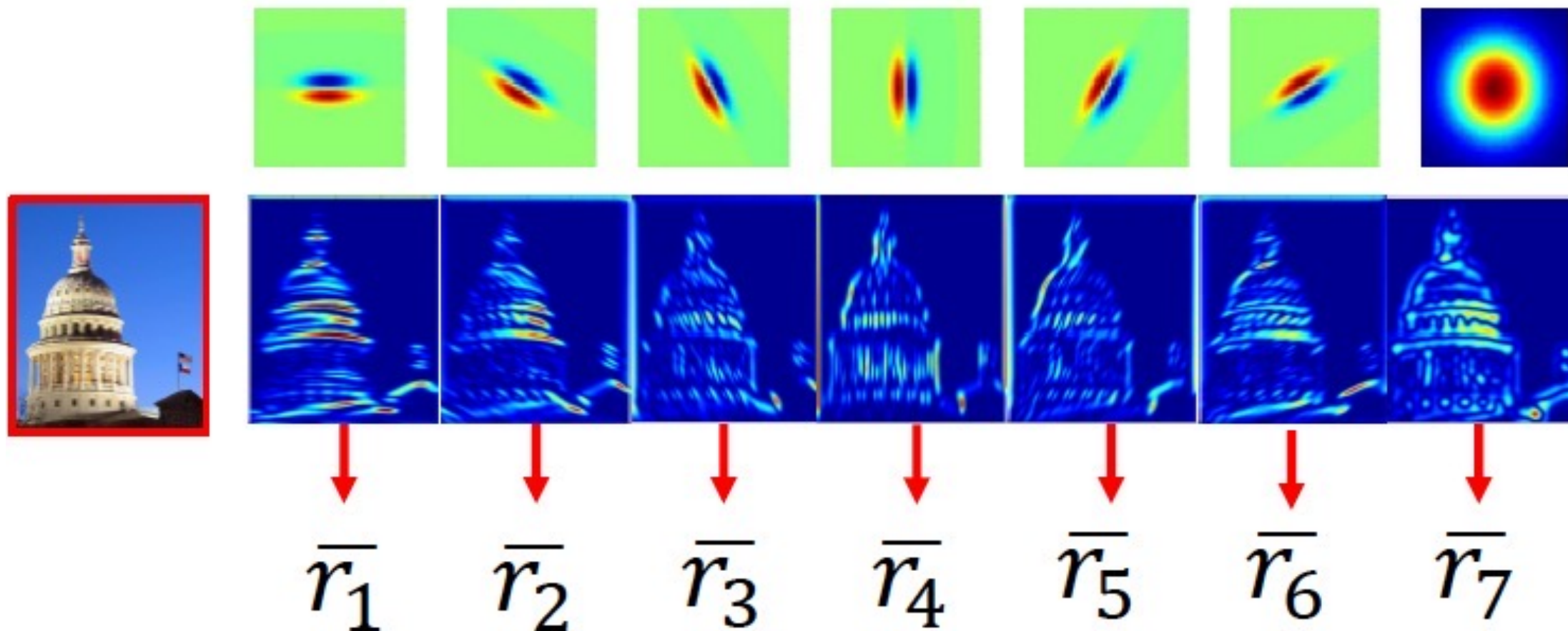
Response of One Kernel



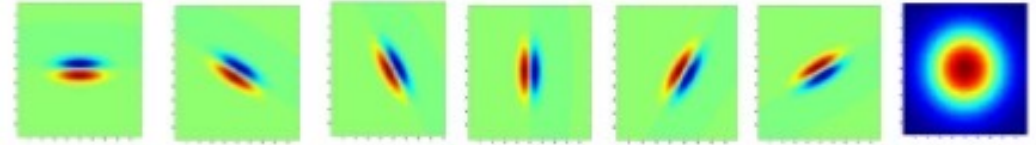
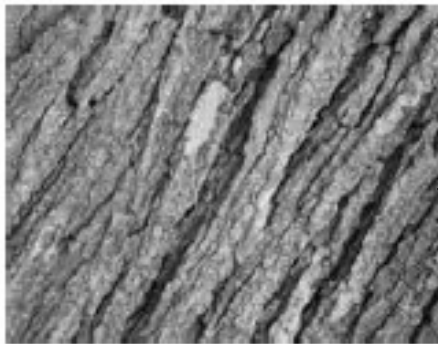
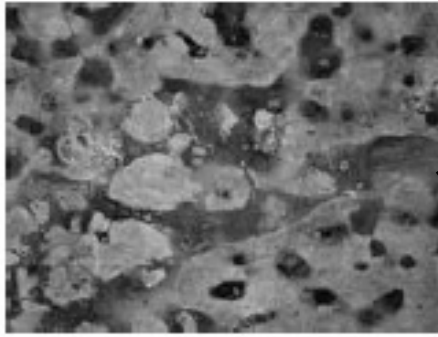
Response of One Kernel



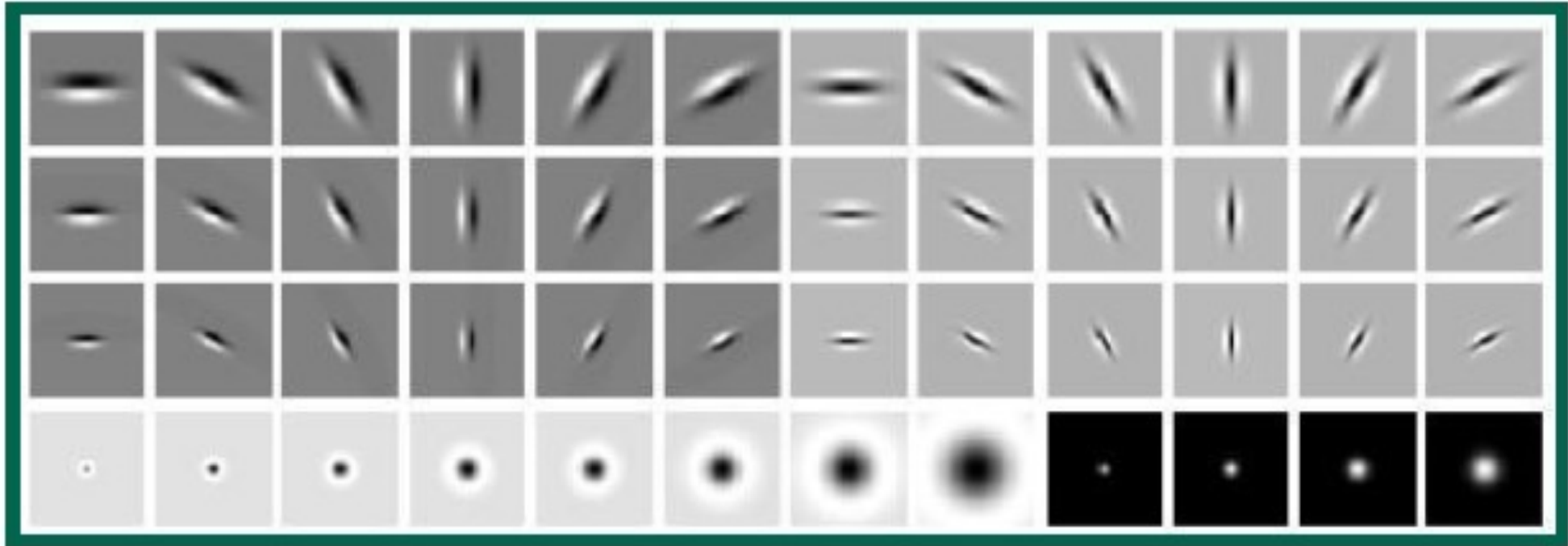
Feature: Response Pattern



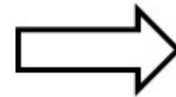
Feature can be Used for Recognition



More Kernels



...



$[\bar{r}_1 \quad \dots \quad \bar{r}_{48}]$

How to design kernels?