

University of Tartu ICPC Team Notebook

(2018-2019) March 10, 2019

- 1 Setup
- 2 crc.sh
- 3 gcc ordered set
- 4 2D geometry
- 5 3D geometry
- 6 Triangle centers
- 7 Seg-Seg intersection, halfplane intersection area
- 8 Convex polygon algorithms
- 9 Delaunay triangulation $\mathcal{O}(n \log n)$
- 10 Aho Corasick $\mathcal{O}(|\alpha| \sum \text{len})$
- 11 Suffix automaton and tree $\mathcal{O}((n+q) \log(|\alpha|))$
- 12 Dinic
- 13 Min Cost Max Flow with successive dijkstra $\mathcal{O}(\text{flow} \cdot n^2)$
- 14 Min Cost Max Flow with Cycle Cancelling $\mathcal{O}(\text{flow} \cdot nm)$
- 15 DMST $\mathcal{O}(E \log V)$
- 16 Bridges $\mathcal{O}(n)$
- 17 2-Sat $\mathcal{O}(n)$ and SCC $\mathcal{O}(n)$
- 18 Generic persistent compressed lazy segment tree
- 19 Templatized HLD $\mathcal{O}(M(n) \log n)$ per query
- 20 Templatized multi dimensional BIT $\mathcal{O}(\log(n)^{\dim})$ per query
- 21 Treap $\mathcal{O}(\log n)$ per query
- 22 Radixsort 50M 64 bit integers as single array in 1 sec

<pre> 23 FFT 5M length/sec 24 Fast mod mult, Rabbin Miller prime check, Pollard rho factorization 25 Symmetric Submodular Functions; Queyranne's algorithm 26 Berlekamp-Massey $\mathcal{O}(\mathcal{L}N)$ </pre> <hr/> <pre> 1 1 Setup 1 2 1 3 1 4 1 5 1 6 1 7 1 8 1 9 1 10 1 11 1 12 1 13 1 14 1 15 1 16 1 17 1 18 1 19 1 20 1 21 1 22 </pre> <hr/> <pre> 1 set smartindent cindent 2 set ts=4 sw=4 expandtab 3 syntax enable 4 set clipboard=unnamedplus 5 # setakbmap -option caps:escape 6 # valgrind --vgdb-error=0 ./a <inp & 7 # gdb a 8 # target remote / vgdb </pre> <hr/> <pre> 1 2 crc.sh 1 #!/bin/env bash 2 for j in `seq 5 5 200`; do 3 sed '/^\s*\$/d' \$1 head -\$j tr -d '[:space:]' cksum cut -f1 4 -d ' ' tail -c 4 #whitespace don't matter. 5 done #there shouldn't be any COMMENTS. 6 #copy lines being checked to separate file. 6 # \$./crc.sh tmp.cpp </pre> <hr/> <pre> 1 3 gcc ordered set 1 #define DEBUG(...) cerr << __VA_ARGS__ << endl; 2 #ifndef CDEBUG 3 #undef DEBUG 4 #define DEBUG(...) ((void)0); 5 #define NDEBUG@#438 @ 6 #endif 7 #define ran(i, a, b) for (auto i = (a); i < (b); i++) 8 #include<bits/stdc++.h> 9 typedef long long ll; 10 typedef long double ld 11 using namespace std;# include<ext/pb_ds/assoc_container.hpp> 12 # include<ext/pb_ds/tree_policy.hpp> 13 using namespace __gnu_pbds; 14 template <typename T 15 using ordered_set = tree<T, null_type, less<T>, rb_tree_tag, 16 tree_order_statistics_node_update>; 17 intmain({ 18 ordered_set<int> cur; 19 cur.insert(1) 20 cur.insert(3); 21 cout << cur.order_of_key(2) 22 << endl;// the number of elements in the set less than 2 </pre>	<p>22 University of Tartu</p> <p>23</p> <p>24</p> <p>25</p> <p>26</p> <p>27</p> <p>28</p> <p>29</p> <p>30</p> <p>31</p> <p>32</p> <p>33</p> <p>34</p> <p>35</p> <p>36</p> <p>37</p> <p>38</p> <p>39</p> <p>40</p> <p>41</p> <p>42</p> <p>43</p> <p>44</p> <p>45</p> <p>46</p> <p>47</p> <p>48</p> <p>49</p> <p>50</p> <p>51</p> <p>52</p> <p>53</p> <p>54</p> <p>55</p> <p>56</p> <p>57</p> <p>58</p> 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23 cout << *cur.find_by_order(0)
24     << endl;// the 0-th smallest number in the set(0-based)      #478
25 cout << *cur.find_by_order(1)
26     << endl;// the 1-th smallest number in the set(0-based)
```

4 2D geometry

Define $\text{orient}(A, B, C) = \overline{AB} \times \overline{AC}$. CCW iff > 0 . Define $\text{perp}((a, b)) = (-b, a)$. The vectors are orthogonal.

For line $ax + by = c$ def $\bar{v} = (-b, a)$.

Line through P and Q has $\bar{v} = \overline{PQ}$ and $c = \bar{v} \times P$. $\text{side}_l(P) = \bar{v}_l \times P - c_l$ sign determines which side P is on from l .

$\text{dist}_l(P) = \text{side}_l(P)/\|\bar{v}_l\|$ squared is integer.

Sorting points along a line: comparator is $\bar{v} \cdot A < \bar{v} \cdot B$.

Translating line by \bar{t} : new line has $c' = c + \bar{v} \times \bar{t}$.

Line intersection: is $(c_l \bar{v}_m - c_m \bar{v}_l)/(\bar{v}_l \times \bar{v}_m)$.

Project P onto l : is $P - \text{perp}(v) \text{side}_l(P)/\|v\|^2$.

Angle bisectors: $\bar{v} = \bar{v}_l/\|\bar{v}_l\| + \bar{v}_m/\|\bar{v}_m\|$

$c = c_l/\|\bar{v}_l\| + c_m/\|\bar{v}_m\|$.

P is on segment AB iff $\text{orient}(A, B, P) = 0$ and $\overline{PA} \cdot \overline{PB} \leq 0$.

Proper intersection of AB and CD exists iff $\text{orient}(C, D, A)$ and $\text{orient}(C, D, B)$ have opp. signs and $\text{orient}(A, B, C)$ and $\text{orient}(A, B, D)$ have opp. signs. Coordinates:

$$\frac{A \text{orient}(C, D, B) - B \text{orient}(C, D, A)}{\text{orient}(C, D, B) - \text{orient}(C, D, A)}.$$

Circumcircle center:

```
pt circumCenter(pt a, pt b, pt c) {
    b = b-a, c = c-a; // consider coordinates relative to A
    assert(cross(b,c) != 0); // no circumcircle if A,B,C aligned
    return a + perp(b*sq(c) - c*sq(b))/cross(b,c)/2;
```

Circle-line intersect:

```
int circleLine(pt o, double r, line l, pair<pt, pt> &out) {
    double h2 = r*r - l.sqDist(o);
    if (h2 >= 0) { // the line touches the circle
        pt p = l.proj(o); // point P
        pt h = l.v*sqrt(h2)/abs(l.v); // vector parallel to l, of len h
        out = {p-h, p+h};
    }
    return 1 + sgn(h2);
```

Circle-circle intersect:

```
int circleCircle(pt o1, double r1, pt o2, double r2, pair<pt, pt> &out) {
    pt d=o2-o1; double d2=sq(d);
```

```
if (d2 == 0) {assert(r1 != r2); return 0;} // concentric circles
double pd = (d2 + r1*r1 - r2*r2)/2; // = |0_1P| * d
double h2 = r1*r1 - pd*pd/d2; // = h^2
if (h2 >= 0) {
    pt p = o1 + d*pd/d2, h = perp(d)*sqrt(h2/d2);
    ;
    out = {p-h, p+h};}
return 1 + sgn(h2);
```

Tangent lines:

```
int tangents(pt o1, double r1, pt o2, double r2,
    bool inner, vector<pair<pt, pt>> &out) {
    if (inner) r2 = -r2;
    pt d = o2-o1;
    double dr = r1-r2, d2 = sq(d), h2 = d2-dr*dr;
    if (d2 == 0 || h2 < 0) {assert(h2 != 0);
        return 0;}
    for (double sign : {-1,1}) {
        pt v = (d*dr + perp(d)*sqrt(h2)*sign)/d2;
        out.push_back({o1 + v*r1, o2 + v*r2});}
    return 1 + (h2 > 0);
```

5 3D geometry

$\text{orient}(P, Q, R, S) = (\overline{PQ} \times \overline{PR}) \cdot \overline{PS}$.

S above PQR iff > 0 .

For plane $ax + by + cz = d$ def $\bar{n} = (a, b, c)$.

Line with normal \bar{n} through point P has $d = \bar{n} \cdot P$.

$\text{side}_\Pi(P) = \bar{n} \cdot P - d$ sign determines side from Π .

$\text{dist}_\Pi(P) = \text{side}_\Pi(P)/\|\bar{n}\|$.

Translating plane by \bar{t} makes $d' = d + \bar{n} \cdot \bar{t}$.

Plane-plane intersection of has direction $\bar{n}_1 \times \bar{n}_2$ and goes through $((d_1 \bar{n}_2 - d_2 \bar{n}_1) \times \bar{d})/\|\bar{d}\|^2$.

Line-line distance:

```
double dist(line3d l1, line3d l2) {
    p3 n = l1.d*l2.d;
    if (n == zero) // parallel
        return l1.dist(l2.o);
    return abs((l2.o-l1.o)|n)/abs(n);
```

Spherical to Cartesian:

$(r \cos \varphi \cos \lambda, r \cos \varphi \sin \lambda, r \sin \varphi)$.

Sphere-line intersection:

```
int sphereLine(p3 o, double r, line3d l, pair<p3, p3> &out) {
    double h2 = r*r - l.sqDist(o);
    if (h2 < 0) return 0; // the line doesn't touch the sphere
    p3 p = l.proj(o); // point P
    p3 h = l.d*sqrt(h2)/abs(l.d); // vector parallel to l, of length h
    out = {p-h, p+h};
```

```
return 1 + (h2 > 0);
```

Great-circle distance between points A and B is $r\angle AOB$.

Spherical segment intersection:

```
bool properInter(p3 a, p3 b, p3 c, p3 d, p3 &out)
    ) {
    p3 ab = a*b, cd = c*d; // normals of planes OAB and OCD
    int oa = sgn(cd|a),
        ob = sgn(cd|b),
        oc = sgn(ab|c),
        od = sgn(ab|d);
    out = ab*cd*od; // four multiplications => careful with overflow !
    return (oa != ob && oc != od && oa != oc);
}
bool onSphSegment(p3 a, p3 b, p3 p) {
    p3 n = a*b;
    if (n == zero)
        return a*p == zero && (a|p) > 0;
    return (n|p) == 0 && (n|a*p) >= 0 && (n|b*p) <= 0;
}
```

```
struct directionSet : vector<p3> {
    using vector::vector; // import constructors
    void insert(p3 p) {
        for (p3 q : *this) if (p*q == zero) return;
        push_back(p);
    }
};
```

```
directionSet intersSph(p3 a, p3 b, p3 c, p3 d) {
    assert(validSegment(a, b) && validSegment(c, d));
    p3 out;
    if (properInter(a, b, c, d, out)) return {out};
    directionSet s;
    if (onSphSegment(c, d, a)) s.insert(a);
    if (onSphSegment(c, d, b)) s.insert(b);
    if (onSphSegment(a, b, c)) s.insert(c);
    if (onSphSegment(a, b, d)) s.insert(d);
    return s;
}
```

Angle between spherical segments AB and AC is angle between $A \times B$ and $A \times C$.

Oriented angle: subtract from 2π if mixed product is negative.

Area of a spherical polygon:

$$r^2[\text{sum of interior angles} - (n-2)\pi].$$

6 Triangle centers

```

1 const double min_delta = 1e-13;
2 const double coord_max = 1e6;
3 typedef complex<double> point;
4 point A, B, C;// vertexes of the triangle
5 bool collinear() #823
6     double min_diff = min(abs(A - B), min(abs(A - C), abs(B - C)));
7     if (min_diff < coord_max * min_delta) return true;
8     point sp = (B - A) / (C - A);
9     double ang = #638
10        M_PI / 2
11        abs(arg(sp)) - M_PI / 2;// positive angle with the real line
12     return ang < min_delta; %0446
13
14 point circum_center(){
15     if (collinear()) return point(NAN, NAN);
16     // squared lengths of sides
17     double a2 = norm(B - C);
18     double b2 = norm(A - C);
19     double c2 = norm(A - B) #715
20     // barycentric coordinates of the circumcenter
21     double c_A = a2 * (b2 + c2 - a2); // sin(2 * alpha) works also
22     double c_B = b2 * (a2 + c2 - b2);
23     double c_C = c2 * (a2 + b2 - c2);
24     double sum = c_A + c_B + c_C;
25     c_A /= sum
26     c_B /= sum; #407
27     c_C /= sum;
28     return c_A * A + c_B * B + c_C * C;// cartesian
29
30 point centroid(){// center of mass
31     return (A + B + C) / 3.0;
32 }
33 point ortho_center() {// euler line
34     point O = circum_center()
35     return O + 3.0 * (centroid() - O); #895
36 };
37 point nine_point_circle_center(){// euler line
38     point O = circum_center();
39     return O + 1.5 * (centroid() - O)
40 }
41 point in_center(){
42     if (collinear()) return point(NAN, NAN);
43     double a = abs(B - C); // side lengths
44     double b = abs(A - C);
45     double c = abs(A - B)
46     // trilinear coordinates are (1,1,1) #193
47     double sum = a + b + c;
48     a /= sum;
49     b /= sum; %031
50     c /= sum; // barycentric

```

```

51     return a * A + b * B + c * C;// cartesian #596
52
53     7 Seg-Seg intersection, halfplane intersection area
54     struct Seg {
55         Vec a, b;
56         Vecd({ return b - a; })
57     };
58     Vec intersection(Seg l, Seg r) #327
59         Vec dl = l.d(), dr = r.d();
60         if (cross(dl, dr) == 0) return {nanl "", nanl ""};
61         double h = cross(dr, l.a - r.a) / len(dr);
62         double dh = cross(dr, dl) / len(dr);
63         return l.a + dl * (h / -dh) #893
64     }// Returns the area bounded by halfplanes
65     double calc_area(vector<Seg> lines{
66         double lb = -HUGE_VAL, ub = HUGE_VAL; #454
67         vector<Seg> linesBySide[2];
68         for (auto line : lines)
69             if (line.b.y == line.a.y) {
70                 if (line.a.x < line.b.x) {
71                     lb = max(lb, line.a.y); #029
72                 } else {
73                     ub = min(ub, line.a.y)
74                 }
75             } else if (line.a.y < line.b.y) {
76                 linesBySide[1].push_back(line);
77             } else {
78                 linesBySide[0].push_back({line.b, line.a}) #613
79             }
80         }
81         sort(
82             linesBySide[0].begin(), linesBySide[0].end(), [] (Seg l, Seg r) {
83                 if (cross(l.d(), r.d()) == 0) #123
84                     return normal(l.d()) * l.a > normal(r.d()) * r.; #115
85                 return cross(l.d(), r.d()) < ;
86             });
87         sort(
88             linesBySide[1].begin(), linesBySide[1].end(), [] (Seg l, Seg r) {
89                 if (cross(l.d(), r.d()) == 0)
90                     return normal(l.d()) * l.a < normal(r.d()) * r.a;
91                 return cross(l.d(), r.d()) > ;
92             });
93         // Now find the application area of the lines and clean up redundant
94         // ones
95         vector<double> applyStart[2] #597
96         for (int side = 0; side < 2; side++) {
97             vector<double> &apply = applyStart[side];
98             vector<Seg> curLines;
99             for (auto line : linesBySide[side]) {
100                 while (curLines.size() > 0) #412
101                     Seg other = curLines.back();
102                     if (cross(other.d(), line.d()) < 0)
103                         curLines.pop_back();
104                     else
105                         apply.push_back(cross(other.d(), line.d()));
106             }
107         }
108     }

```

```

49     if (cross(line.d(), other.d()) != 0) {
50         double start = intersection(line, other).y;
51         if (start > apply.back()) break;
52
53         curLines.pop_back();
54         apply.pop_back();
55     }
56     if (curLines.size() == 0) {
57         apply.push_back(-HUGE_VAL)
58     } else {
59         apply.push_back(intersection(line, curLines.back()).y);
60     }
61     curLines.push_back(line);
62
63     linesBySide[side] = curLines;
64 }
65 applyStart[0].push_back(HUGE_VALL);
66 applyStart[1].push_back(HUGE_VALL);
67 double result = 0
68 {
69     double lb = -HUGE_VALL, ub;
70     for (int i = 0, j = 0; i < (int)linesBySide[0].size() &&
71             j < (int)linesBySide[1].size();
72         lb = ub)
73         ub = min(applyStart[0][i + 1], applyStart[1][j + 1]);
74         double alb = lb, aub = ub;
75         Seg 10 = linesBySide[0][i], 11 = linesBySide[1][j];
76         if (cross(11.d(), 10.d()) > 0) {
77             alb = max(alb, intersection(10, 11).y)
78         } else if (cross(11.d(), 10.d()) < 0) {
79             aub = min(aub, intersection(10, 11).y);
80         }
81         alb = max(alb, lb);
82         aub = min(aub, ub)
83         aub = max(aub, alb);
84     {
85         double x1 = 10.a.x + (alb - 10.a.y) / 10.d().y * 10.d().x;
86         double x2 = 10.a.x + (aub - 10.a.y) / 10.d().y * 10.d().x;
87         result -= (aub - alb) * (x1 + x2) / 2
88     }
89     {
90         double x1 = 11.a.x + (alb - 11.a.y) / 11.d().y * 11.d().x;
91         double x2 = 11.a.x + (aub - 11.a.y) / 11.d().y * 11.d().x;
92         result += (aub - alb) * (x1 + x2) / 2
93     }
94     if (applyStart[0][i + 1] < applyStart[1][j + 1]) {
95         i++;
96     } else {
97         j++
98     }
99 }
100 
```

```

101     return result;

```

8 Convex polygon algorithms

```

1 typedef pair<int, int> Vec;
2 typedef pair<Vec, Vec> Seg;
3 typedef vector<Seg>::iterator SegIt; #define F first
4 #define S second
5 #define MP(x, y) make_pair(x, y)
6 lldot(Vec &v1, Vec &v2){ return (ll)v1.F * v2.F + (ll)v1.S * v2.S; }
7 llcross(Vec &v1, Vec &v2){
8     return (ll)v1.F * v2.S - (ll)v2.F * v1.S;
9 }
10 lldist_sq(Vec &p1, Vec &p2{
11     return (ll)(p2.F - p1.F) * (p2.F - p1.F) +
12         (ll)(p2.S - p1.S) * (p2.S - p1.S);
13 }
14 struct Hull {
15     vector<Seg> hull;
16     SegIt up_beg;
17     template <typename It>
18     void extend(It beg, It end) { // O(n)
19         vector<Vec> r;
20         for (auto it = beg; it != end; ++it) {
21             if (r.empty() || *it != r.back()) {
22                 while (r.size() >= 2) {
23                     int n = r.size()
24                     Vec v1 = {r[n - 1].F - r[n - 2].F, r[n - 1].S - r[n - 2].S};
25                     Vec v2 = {it->F - r[n - 2].F, it->S - r[n - 2].S};
26                     if (cross(v1, v2) > 0) break;
27                     r.pop_back();
28                 }
29                 r.push_back(*it);
30             }
31         }
32         ran(i, 0, (int)r.size() - 1) hull.emplace_back(r[i], r[i + 1]);
33     }
34 Hull(vector<Vec> &vert) { // atleast 2 distinct points
35     sort(vert.begin(), vert.end()); // O(n log(n))
36     extend(vert.begin(), vert.end());
37     int diff = hull.size();
38     extend(vert.rbegin(), vert.rend())
39     up_beg = hull.begin() + diff;
40 }
41 bool contains(Vec p{// O(log(n))
42     if (p < hull.front().F || p > up_beg->F) return false;
43     {
44         auto it_low = lower_bound(
45             hull.begin(), up_beg, MP(MP(p.F, (int)-2e9), MP(0, 0))) #542
46         if (it_low != hull.begin()) --it_low;
47         Vec a = {it_low->S.F - it_low->F.F, it_low->S.S - it_low->F.S};
48         Vec b = {p.F - it_low->F.F, p.S - it_low->F.S};

```



```

151 auto best_seg = max(function<double>(Seg &)>
152   [&p, &ref_p]
153   Seg &seg) { // accuracy of used type should be coord-2
154   Vec v1 = {ref_p.F.F - p.F, ref_p.F.S - p.S};
155   Vec v2 = {seg.F.F - p.F, seg.F.S - p.S};
156   ll d_p = dot(v1, v2);
157   ll c_p = DIRECTION * cross(v2, v1)
158   return atan2(c_p, d_p); // order by signed angle
159 });
160 return best_seg->F;
161
162 SegItmax_in_dir(Vec v{ // first is the ans. O(log(n))
163   return max(
164     function<ll>(&Seg &>)([&v](Seg &seg){ return dot(v, seg.F); }));
165   } %596
166 pair<SegIt, SegIt> intersections(Seg l) { // O(log(n))
167   int x = l.S.F - l.F.F;
168   int y = l.S.S - l.F.S;
169   Vec dir = {-y, x};
170   auto it_max = max_in_dir(dir)
171   auto it_min = max_in_dir(MP(y, -x));
172   ll opt_val = dot(dir, l.F);
173   if (dot(dir, it_max->F) < opt_val ||
174       dot(dir, it_min->F) > opt_val)
175     return MP(hull.end(), hull.end()); #276
176 SegIt it_r1, it_r2;
177 function<bool>(Seg &, Seg &) > inc_c([&dir](Seg &lft, Seg &rgt) {
178   return dot(dir, lft.F) < dot(dir, rgt.F);
179 });
180 function<bool>(Seg &, Seg &) > dec_c([&dir](Seg &lft, Seg &rgt)
181   ↵ #431
182   return dot(dir, lft.F) > dot(dir, rgt.F);
183 );
183 if (it_min <= it_max) {
184   it_r1 = upper_bound(it_min, it_max + 1, l, inc_c) - 1;
185   if (dot(dir, hull.front().F) >= opt_val) #689
186     it_r2 = upper_bound(hull.begin(), it_min + 1, l, dec_c) - 1;
187   } else {
188     it_r2 = upper_bound(it_max, hull.end(), l, dec_c) - 1;
189   }
190 } else #552
191   it_r1 = upper_bound(it_max, it_min + 1, l, dec_c) - 1;
192   if (dot(dir, hull.front().F) <= opt_val) {
193     it_r2 = upper_bound(hull.begin(), it_max + 1, l, inc_c) - 1;
194   } else {
195     it_r2 = upper_bound(it_min, hull.end(), l, inc_c) - 1 #220
196   }
197 return MP(it_r1, it_r2);
198
199 Segdiameter({ // O(n)
200

```

```

201 Seg res;
202 ll dia_sq = 0;
203 auto it1 = hull.begin();
204 auto it2 = up_beg
205 Vec v1 = {hull.back().S.F - hull.back().F.F,
206   hull.back().S.S - hull.back().F.S};
207 while (it2 != hull.begin()) {
208   Vec v2 = {(it2 - 1)->S.F - (it2 - 1)->F.F,
209   (it2 - 1)->S.S - (it2 - 1)->F.S} #150
210   if (cross(v1, v2) > 0) break;
211   --it2;
212 }
213 while (it2 != hull.end()) { // check all antipodal pairs
214   if (dist_sq(it1->F, it2->F) > dia_sq) #246
215     res = {it1->F, it2->F};
216   dia_sq = dist_sq(res.F, res.S);
217 }
218 Vec v1 = {it1->S.F - it1->F.F, it1->S.S - it1->F.S};
219 Vec v2 = {it2->S.F - it2->F.F, it2->S.S - it2->F.S} #529
220 if (cross(v1, v2) == 0) {
221   if (dist_sq(it1->S, it2->F) > dia_sq) {
222     res = {it1->S, it2->F};
223     dia_sq = dist_sq(res.F, res.S);
224   }
225   if (dist_sq(it1->F, it2->S) > dia_sq) {
226     res = {it1->F, it2->S};
227     dia_sq = dist_sq(res.F, res.S);
228 } // report cross pairs at parallel lines. #406
229 ++it1
230 ++it2;
231 } else if (cross(v1, v2) < 0) {
232   ++it1;
233 } else {
234   ++it2
235 }
236 }
237 return res;
238 }

#362
#936
#732

```

9 Delaunay triangulation $\mathcal{O}(n \log n)$

```

1 const int max_co = (1 << 28) - 5;
2 struct Vec {
3   int x, y;
4   bool operator==(const Vec &oth) { return x == oth.x && y == oth.y; }
5   bool operator!=(const Vec &oth) { return !operator==(oth); } #679
6   Vec operator-(const Vec &oth) { return {x - oth.x, y - oth.y}; }
7 };
8 llcross(Vec a, Vec b{ return (ll)a.x * b.y - (ll)a.y * b.x; }
9 lldot(Vec a, Vec b{ return (ll)a.x * b.x + (ll)a.y * b.y; }
10 struct Edge
11   Vec tar;
12   Edge *nxt;

```

```

13 Edge *inv = NULL;
14 Edge *rep = NULL;
15 bool vis = false
16 };
17 struct Seg {
18 Vec a, b;
19 bool operator==(const Seg &oth) { return a == oth.a && b == oth.b; }
20 bool operator!=(const Seg &oth) { return !operator==(oth); } #245
21 };
22 llorient(Vec a, Vec b, Vec c{
23 return (ll)a.x * (b.y - c.y) + (ll)b.x * (c.y - a.y) +
24 (ll)c.x * (a.y - b.y);
25
26 bool in_c_circle(Vec *arr, Vec d{
27 if (cross(arr[1] - arr[0], arr[2] - arr[0]) == 0)
28 return true; // degenerate
29 ll m[3][3];
30 ran(i, 0, 3) #264
31 m[i][0] = arr[i].x - d.x;
32 m[i][1] = arr[i].y - d.y;
33 m[i][2] = m[i][0] * m[i][0];
34 m[i][2] += m[i][1] * m[i][1];
35
36 __int128 res = 0;
37 res += (__int128)(m[0][0] * m[1][1] - m[0][1] * m[1][0]) * m[2][2];
38 res += (__int128)(m[1][0] * m[2][1] - m[1][1] * m[2][0]) * m[0][2];
39 res -= (__int128)(m[0][0] * m[2][1] - m[0][1] * m[2][0]) * m[1][2];
40 return res > 0 #845
41
42 Edge add_triangle(Edge *a, Edge *b, Edge *c{
43 Edge *old[] = {a, b, c};
44 Edge *tmp = new Edge[3];
45 ran(i, 0, 3) {
46 old[i]->rep = tmp + i #219
47 tmp[i] = {old[i]->tar, tmp + (i + 1) % 3, old[i]->inv};
48 if (tmp[i].inv) tmp[i].inv->inv = tmp + i;
49 }
50 return tmp;
51
52 Edge add_point(Vec p, Edge *cur{ // returns outgoing edge
53 Edge *triangle[] = {cur, cur->nxt, cur->nxt->nxt};
54 ran(i, 0, 3) {
55 if (orient(triangle[i]->tar, triangle[(i + 1) % 3]->tar, p) < 0)
56 return NULL #233
57 }
58 ran(i, 0, 3) {
59 if (triangle[i]->rep) {
60 Edge *res = add_point(p, triangle[i]->rep);
61 if (res
62 return res; // unless we are on last layer we must exit here #636
63 }

64 }
65 Edge p_as_e[p];
66 Edge tmp{cur->tar}
67 tmp.inv = add_triangle(&p_as_e, &tmp, cur = cur->nxt); #432
68 Edge *res = tmp.inv->nxt;
69 tmp.tar = cur->tar;
70 tmp.inv = add_triangle(&p_as_e, &tmp, cur = cur->nxt);
71 tmp.tar = cur->tar #359
72 res->inv = add_triangle(&p_as_e, &tmp, cur = cur->nxt);
73 res->inv->inv = res;
74 return res;
75 }
76 Edge *delaunay(vector<Vec> &points) #029
77 random_shuffle(points.begin(), points.end());
78 Vec arr[] = {{4 * max_co, 4 * max_co}, {-4 * max_co, max_co},
79 {max_co, -4 * max_co}};
80 Edge *res = new Edge[3];
81 ran(i, 0, 3) res[i] = {arr[i], res + (i + 1) % 3} #480
82 for (Vec &cur : points) {
83 Edge *loc = add_point(cur, res);
84 Edge *out = loc;
85 arr[0] = cur;
86 while (true) #601
87 arr[1] = out->tar;
88 arr[2] = out->nxt->tar;
89 Edge *e = out->nxt->inv;
90 if (e && in_c_circle(arr, e->nxt->tar)) { #056
91 Edge tmp{cur}
92 tmp.inv = add_triangle(&tmp, out, e->nxt);
93 tmp.tar = e->nxt->tar;
94 tmp.inv->inv = add_triangle(&tmp, e->nxt->nxt, out->nxt->nxt);
95 out = tmp.inv->nxt;
96 continue #173
97 }
98 out = out->nxt->nxt->inv;
99 if (out->tar == loc->tar) break;
100 }
101
102 return res; #032
103
104 void extract_triangles(Edge *cur, vector<vector<Seg> > &res{ #769
105 if (!cur->vis) {
106 bool inc = true;
107 Edge *it = cur;
108 do
109 it->vis = true;
110 if (it->rep) {
111 extract_triangles(it->rep, res);
112 inc = false;
113
114 it = it->nxt; #104
}

```

```

115 } while (it != cur);
116 if (inc) {
117     Edge *triangle[3] = {cur, cur->nxt, cur->nxt->nxt};
118     res.resize(res.size() + 1) #207
119     vector<Seg> &tar = res.back();
120     ran(i, 0, 3) {
121         if ((abs(triangle[i]->tar.x) < max_co &&
122             abs(triangle[(i + 1) % 3]->tar.x) < max_co))
123             tar.push_back #011
124             {triangle[i]->tar, triangle[(i + 1) % 3]->tar};
125     }
126     if (tar.empty()) res.pop_back();
127 }
128 #602

```

10 Aho Corasick $\mathcal{O}(|\alpha| \sum \text{len})$

```

1 const int alpha_size = 26;
2 struct Node {
3     Node *nxt[alpha_size]; // May use other structures to move in trie
4     Node *suffix;
5     Node() { memset(nxt, 0, alpha_size * sizeof(Node *)); #248
6         int cnt = 0;
7     };
8     Node aho_corasick(vector<vector<char> > &dict{
9         Node *root = new Node;
10        root->suffix = 0 #292
11        vector<pair<vector<char> *, Node *> > state;
12        for (vector<char> &s : dict) state.emplace_back(&s, root);
13        for (int i = 0; !state.empty(); ++i) {
14            vector<pair<vector<char> *, Node *> > nstate;
15            for (auto &cur : state) #306
16                Node *nxt = cur.second->nxt[(*cur.first)[i]];
17                if (nxt) {
18                    cur.second = nxt;
19                } else {
20                    nxt = new Node #266
21                    cur.second->nxt[(*cur.first)[i]] = nxt;
22                    Node *suf = cur.second->suffix;
23                    cur.second = nxt;
24                    nxt->suffix = root; // set correct suffix link
25                    while (suf) #249
26                        if (suf->nxt[(*cur.first)[i]]) {
27                            nxt->suffix = suf->nxt[(*cur.first)[i]];
28                            break;
29                        }
30                        suf = suf->suffix #562
31                    }
32                if (cur.first->size() > i + 1) nstate.push_back(cur);
33            }
34            state = nstate #417
35        }
36    }

```

```

37     return root; #882 // auxilary functions for searching and counting
38
39 Node walk(Node *cur, char c{// longest prefix in dict that is suffix of walked string.
40     while (true) {
41         if (cur->nxt[c]) return cur->nxt[c];
42         if (!cur->suffix) return cur #414
43         cur = cur->suffix;
44     }
45 }
46
47 void cnt_matches(Node *root, vector<char> &match_in{ #529
48     Node *cur = root;
49     for (char c : match_in) {
50         cur = walk(cur, c);
51         ++cur->cnt
52     }
53 }
54 void add_cnt(Node *root{// After counting matches propagate ONCE to #156
55     // suffixes for final counts
56     vector<Node *> to_visit = {root};
57     ran(i, 0, to_visit.size()) {
58         Node *cur = to_visit[i];
59         ran(j, 0, alpha_size);
60         if (cur->nxt[j]) to_visit.push_back(cur->nxt[j]); #662
61     }
62 }
63 for (int i = to_visit.size() - 1; i > 0; --i)
64     to_visit[i]->suffix->cnt += to_visit[i]->cnt #950
65
66 int main(){ #488
67     int n, len;
68     scanf "%d %d", &len, &n);
69     vector<char> a(len + 1);
70     scanf "%s", a.data());
71     a.pop_back();
72     for (char &c : a) c -= 'a';
73     vector<vector<char> > dict(n);
74     ran(i, 0, n) {
75         scanf "%d", &len);
76         dict[i].resize(len + 1);
77         scanf "%s", dict[i].data());
78         dict[i].pop_back();
79         for (char &c : dict[i]) c -= 'a';
80     }
81     Node *root = aho_corasick(dict);
82     cnt_matches(root, a);
83     add_cnt(root);
84     ran(i, 0, n) {
85         Node *cur = root;
86         for (char c : dict[i]) cur = walk(cur, c);
87         printf "%d\n", cur->cnt);

```

```

88 }


---


11 Suffix automaton and tree  $\mathcal{O}((n+q)\log(|\alpha|))$ 


---


1 class Node {
2     private:
3         map<char, Node *>
4             nxt_char; // Map is faster than hashtable and unsorted arrays
5     public:
6         int len; // Length of longest suffix in equivalence class. #994
7         Node *suf;
8         bool has_nxt(char c) const { return nxt_char.count(c); }
9         Node *nxt(char c){ #788
10             if (!has_nxt(c)) return NULL;
11             return nxt_char[c];
12         }
13         void set_nxt(char c, Node *node){ nxt_char[c] = node; }
14         Node *split(int new_len, char c{ #449
15             Node *new_n = new Node;
16             new_n->nxt_char = nxt_char;
17             new_n->len = new_len;
18             new_n->suf = suf;
19             suf = new_n;
20             return new_n
21         } #130
22         %044
23         // Extra functions for matching and counting
24         Node *lower_depth(int depth{ // move to longest suffix of current #736
25             // with a maximum length of depth.
26             if (suf->len >= depth) return suf->lower_depth(depth);
27             return this;
28         }
29         Node *walk(char c, int depth #736
30             int &match_len) { // move to longest suffix of walked path that is
31             // a substring
32             match_len = min(match_len,
33                 len); // includes depth limit(needed for finding matches)
34             if (has_nxt(c)) { // as suffixes are in classes match_len must be
35                 // tracked externally
36                 ++match_len
37                 return nxt(c->lower_depth(depth);
38             }
39             if (suf) return suf->walk(c, depth, match_len);
40             return this;
41         } #153
42         %969
43         int paths_to_end = 0;
44         void set_as_end({ // All suffixes of current node are marked as
45             // ending nodes.
46             paths_to_end += 1;
47             if (suf) suf->set_as_end();
48         } #041
49         bool vis = false;
50         void calc_paths_to_end({ // Call ONCE from ROOT. For each node
51             // calculates number of ways to reach an

```

```

52             // end node.
53             if (!vis) { // paths_to_end is occurrence count for any strings in
54                 // current suffix equivalence class. #035
55                 vis = true;
56                 for (auto cur : nxt_char)
57                     cur.second->calc_paths_to_end();
58                 paths_to_end += cur.second->paths_to_end;
59             }
59             // Transform into suffix tree of reverse string
60             map<char, Node *> tree_links;
61             int end_dist = 1 << 30;
62             int calc_end_dist({ #996
63                 if (end_dist == 1 << 30) {
64                     if (nxt_char.empty()) end_dist = 0
65                     for (auto cur : nxt_char)
66                         end_dist = min(end_dist, 1 + cur.second->calc_end_dist());
67                 }
68                 return end_dist;
69             } #021
70             bool vis_t = false;
71             void build_suffix_tree(string &s{ // Call ONCE from ROOT.
72                 if (!vis_t) {
73                     vis_t = true;
74                     if (suf
75                         suf->tree_links[s.size() - end_dist - suf->len - 1]] = this;
76                         for (auto cur : nxt_char) cur.second->build_suffix_tree(s);
77                     }
78                 }
79             } #268
80             struct SufAuto {
81                 Node *last;
82                 Node *root;
83                 void extend(char new_c{ #340
84                     Node *new_end = new Node
85                     new_end->len = last->len + 1;
86                     Node *suf_w_nxt = last;
87                     while (suf_w_nxt && !suf_w_nxt->has_nxt(new_c)) {
88                         suf_w_nxt->set_nxt(new_c, new_end);
89                         suf_w_nxt = suf_w_nxt->suf
90                     }
91                     if (!suf_w_nxt) {
92                         new_end->suf = root;
93                     } else {
94                         Node *max_sbstr = suf_w_nxt->nxt(new_c)
95                         if (suf_w_nxt->len + 1 == max_sbstr->len) {
96                             new_end->suf = max_sbstr;
97                         } else {
98                             Node *eq_sbstr = max_sbstr->split(suf_w_nxt->len + 1, new_c);
99                             new_end->suf = eq_sbstr
100                         }
100                     }
100                 } #217
100             } #618
100             #295
100         }
100     }
100 
```

```

101     Node *w_edge_to_eq_sbstr = suf_w_nxt;
102     while (w_edge_to_eq_sbstr != 0 &&
103             w_edge_to_eq_sbstr->nxt(new_c) == max_sbstr) {
104         w_edge_to_eq_sbstr->set_nxt(new_c, eq_sbstr);
105         w_edge_to_eq_sbstr = w_edge_to_eq_sbstr->suf
106     }
107 }
108 }
109 last = new_end;
110
111 SufAuto(string &s) {
112     root = new Node;
113     root->len = 0;
114     root->suf = NULL;
115     last = root
116     for (char c : s) extend(c);
117     root->calc_end_dist(); // To build suffix tree use reversed string
118     root->build_suffix_tree(s);
119 }
#135



---



## 12 Dinic



---


1 struct MaxFlow {
2     typedef long long ll;
3     const ll INF = 1e18;
4     struct Edge {
5         int u, v
6         ll c, rc;
7         shared_ptr<ll> flow;
8         Edge(int _u, int _v, ll _c, ll _rc = 0)
9             : u(_u), v(_v), c(_c), rc(_rc) {}
10    }
#295
11    struct FlowTracker {
12        shared_ptr<ll> flow;
13        ll cap, rcap;
14        bool dir;
15        FlowTracker(ll _cap, ll _rcap, shared_ptr<ll> _flow, int _dir
#418
16            : cap(_cap), rcap(_rcap), flow(_flow), dir(_dir) {}
17        ll rem() const {
18            if (dir == 0) {
19                return cap - *flow;
20            } else
21                return rcap + *flow;
22        }
23    }
24    void add_flow(ll f) {
25        if (dir == 0
26            *flow += f;
27        else
28            *flow -= f;
29        assert(*flow <= cap);
30        assert(-*flow <= rcap)
#287

```

```

31 }
32     operator ll() const { return rem(); }
33     void operator-=(ll x) { add_flow(x); }
34     void operator+=(ll x) { add_flow(-x); }
35 } #789
36 int source, sink;
37 vector<vector<int>> adj;
38 vector<vector<FlowTracker>> cap;
39 vector<Edge> edges;
40 MaxFlow(int _source, int _sink) : source(_source), sink(_sink) #080
41     ← assert(source != sink);
42 }
43 int add_edge(int u, int v, ll c, ll rc = 0) {
44     edges.push_back(Edge(u, v, c, rc));
45     return edges.size() - 1 #659
46 }
47 vector<int> now, lvl;
48 void prep() {
49     int max_id = max(source, sink);
50     for (auto edge : edges) max_id = max(max_id, max(edge.u, edge.v))
51     ← #638
52     adj.resize(max_id + 1);
53     cap.resize(max_id + 1);
54     now.resize(max_id + 1);
55     lvl.resize(max_id + 1);
56     for (auto &edge : edges) #604
57         auto flow = make_shared<ll>(0);
58         adj[edge.u].push_back(edge.v);
59         cap[edge.u].push_back(FlowTracker(edge.c, edge.rc, flow, 0));
60         if (edge.u != edge.v) {
61             adj[edge.v].push_back(edge.u) #789
62             cap[edge.v].push_back(FlowTracker(edge.c, edge.rc, flow, 1));
63         }
64         assert(cap[edge.u].back() == edge.c);
65         edge.flow = flow; #131
66     }
67     booldinic_bfs({
68         fill(now.begin(), now.end(), 0);
69         fill(lvl.begin(), lvl.end(), 0);
70         lvl[source] = 1 #448
71         vector<int> bfs(1, source);
72         for (int i = 0; i < bfs.size(); ++i) {
73             int u = bfs[i];
74             for (int j = 0; j < adj[u].size(); ++j) {
75                 int v = adj[u][j];
76                 if (cap[u][j] > 0 && lvl[v] == 0) {
77                     lvl[v] = lvl[u] + 1;
78                     bfs.push_back(v);
79                 }
80             }
81         }
82     }
83 }
```

```

80
81     }
82     return lvl[sink] > 0;
83 }
84 lldinic_dfs(int u, ll flow{
85     if (u == sink) return flow;
86     while (now[u] < adj[u].size()) {
87         int v = adj[u][now[u]];
88         if (lvl[v] == lvl[u] + 1 && cap[u][now[u]] != 0) {
89             ll res = dinic_dfs(v, min(flow, (ll)cap[u][now[u]]));
90             if (res > 0)
91                 cap[u][now[u]] -= res;
92             return res;
93         }
94         ++now[u];
95     }
96     return 0;
97 }
98 llcalc_max_flow({
99     prep()
100    ll ans = 0;
101    while (dinic_bfs()) {
102        ll cur = 0;
103        do {
104            cur = dinic_dfs(source, INF)
105            ans += cur;
106        } while (cur > 0);
107    }
108    return ans;
109 }
110 llflow_on_edge(int edge_index{
111     assert(edge_index < edges.size());
112     return *edges[edge_index].flow;
113 }
114 }
115 intmain(){
116     int n, m;
117     cin >> n >> m;
118     auto mf = MaxFlow(
119         1, n); // arguments source and sink, memory usage O(largest node
120         // index + input size), sink doesn't need to be last index
121     int edge_index;
122     for (int i = 0; i < m; ++i) {
123         int a, b, c;
124         cin >> a >> b >> c;
125         // mf.add_edge(a,b,c); // for directed edges
126         edge_index = mf.add_edge(
127             a, b, c, c); // store edge index if care about flow value
128     }
129     cout << mf.calc_max_flow() << '\n';
130     // cout << mf.flow_on_edge(edge_index) << endl; // return flow on
131 }
```

```

#722 #132 // this edge


---


13 13 Min Cost Max Flow with successive dijkstra  $\mathcal{O}(\text{flow} \cdot n^2)$ 
1 const int nmax = 1055;
2 const ll inf = 1e14;
3 int t, n, v; // 0 is source, v-1 sink
4 ll rem_flow[nmax][nmax]; // set [x][y] for directed capacity from x to
5 ll cost[nmax][nmax]; // set [x][y] for directed cost from x to y.
6 ll min_dist[nmax]; // TO inf IF NOT USED
7 ll node_flow[nmax];
8 int prev_node[nmax];
9 bool visited[nmax];
10 ll tot_cost, tot_flow; // output
11 void min_cost_max_flow(){
12     tot_cost = 0; // Does not work with negative cycles.
13     tot_flow = 0;
14     ll sink_pot = 0;
15     min_dist[0] = 0
16     for (int i = 1; i <= v; ++i) { // incase of no negative edges
17         // Bellman-Ford can be removed.
18         min_dist[i] = inf;
19     }
20     for (int i = 0; i < v - 1; ++i) {
21         for (int j = 0; j < v; ++j)
22             for (int k = 0; k < v; ++k) {
23                 if (rem_flow[j][k] > 0 &&
24                     min_dist[j] + cost[j][k] < min_dist[k])
25                     min_dist[k] = min_dist[j] + cost[j][k];
26             }
27     }
28 }
29 for (int i = 0; i < v; ++i) { // Apply potentials to edge costs.
30     for (int j = 0; j < v; ++j) {
31         if (cost[i][j] != inf)
32             cost[i][j] += min_dist[i];
33             cost[i][j] -= min_dist[j];
34     }
35 }
36 }
37 sink_pot += min_dist[v - 1]; // Bellman-Ford end.
38 while (true) {
39     for (int i = 0; i <= v; ++i) { // node after sink is used as start
40         // value for Dijkstra.
41         min_dist[i] = inf;
42         visited[i] = false;
43     }
44     min_dist[0] = 0;
45     node_flow[0] = inf;
46 }
```

```

47 int min_node;
48 while (true) { // Use Dijkstra to calculate potentials
49     int min_node = v
50     for (int i = 0; i < v; ++i) {
51         if ((!visited[i]) && min_dist[i] < min_dist[min_node])
52             min_node = i;
53     }
54     if (min_node == v) break visited[min_node] = true #782
55     for (int i = 0; i < v; ++i) {
56         if ((!visited[i]) &&
57             min_dist[min_node] + cost[min_node][i] < min_dist[i]) {
58             min_dist[i] = min_dist[min_node] + cost[min_node][i];
59             prev_node[i] = min_node #881
60             node_flow[i] =
61                 min(node_flow[min_node], rem_flow[min_node][i]);
62     }
63 }
64 if (min_dist[v - 1] == inf)
65     break for (int i = 0; i < v;
66             ++i) { // Apply potentials to edge costs.
67     for (int j = 0; j < v;
68         ++j) { // Found path from source to sink becomes 0
69         → cost. #664
70         if (cost[i][j] != inf) {
71             cost[i][j] += min_dist[i];
72             cost[i][j] -= min_dist[j];
73         }
74     }
75     sink_pot += min_dist[v - 1];
76     tot_flow += node_flow[v - 1];
77     tot_cost += sink_pot * node_flow[v - 1];
78     int cur = v - 1
79     while (cur != 0) { #946
80         // Backtrack along found path that now has 0 cost.
81         rem_flow[prev_node[cur]][cur] -= node_flow[v - 1];
82         rem_flow[cur][prev_node[cur]] += node_flow[v - 1];
83         cost[cur][prev_node[cur]] = 0;
84         if (rem_flow[prev_node[cur]][cur] == 0 #446
85             cost[prev_node[cur]][cur] = inf;
86         cur = prev_node[cur];
87     }
88 }
89 }
90 intmain({ // http://www.spoj.com/problems/GREED/
91     cin >> t;
92     for (int i = 0; i < t; ++i) {
93         cin >> n;
94         for (int j = 0; j < nmax; ++j) {
95             for (int k = 0; k < nmax; ++k) {
96                 cost[j][k] = inf;
97             }

```

```

98     rem_flow[j][k] = 0;
99 }
100 }
101 for (int j = 1; j <= n; ++j) {
102     cost[j][2 * n + 1] = 0;
103     rem_flow[j][2 * n + 1] = 1;
104 }
105 for (int j = 1; j <= n; ++j) {
106     int card;
107     cin >> card;
108     ++rem_flow[0][card];
109     cost[0][card] = 0;
110 }
111 int ex_c;
112 cin >> ex_c;
113 for (int j = 0; j < ex_c; ++j) {
114     int a, b;
115     cin >> a >> b;
116     if (b < a) swap(a, b);
117     cost[a][b] = 1;
118     rem_flow[a][b] = nmax;
119     cost[b][n + b] = 0;
120     rem_flow[b][n + b] = nmax;
121     cost[n + b][a] = 1;
122     rem_flow[n + b][a] = nmax;
123 }
124 v = 2 * n + 2;
125 min_cost_max_flow();
126 cout << tot_cost << '\n';
127 }

```

14 Min Cost Max Flow with Cycle Cancelling $\mathcal{O}(\text{flow} \cdot nm)$

```

1 struct Network {
2     struct Node;
3     struct Edge {
4         Node *u, *v;
5         int f, c, cost
6         Node*from(Node* pos#965
7             if (pos == u) return v;
8             return u;
9         }
10        intgetCap(Node* pos#145
11            if (pos == u) return c - f;
12            return f;
13        }
14        int addFlow(Node* pos, int toAdd) {
15            if (pos == u) #369
16                f += toAdd;
17                return toAdd * cost;
18            } else {
19                f -= toAdd;

```

```

20     return -toAdd * cost
21 }
22 }
23 };
24 struct Node {
25     vector<Edge*> conn
26     int index;
27 };
28 deque<Node> nodes;
29 deque<Edge> edges;
30 Node* addNode()
31     nodes.push_back(Node());
32     nodes.back().index = nodes.size() - 1;
33     return &nodes.back();
34 }
35 Edge* addEdge(Node* u, Node* v, int f, int c, int cost
36     edges.push_back({u, v, f, c, cost});
37     u->conn.push_back(&edges.back());
38     v->conn.push_back(&edges.back());
39     return &edges.back();
40 }
41 // Assumes all needed flow has already been added
42 int minCostMaxFlow({
43     int n = nodes.size();
44     int result = 0;
45     struct State {
46         int p
47         Edge* used;
48     };
49     while (1) {
50         vector<vector<State>> state(1, vector<State>(n, {0, 0}));
51         for (int lev = 0; lev < n; lev++) #158
52             state.push_back(state[lev]);
53             for (int i = 0; i < n; i++) {
54                 if (lev == 0 || state[lev][i].p < state[lev - 1][i].p) {
55                     for (Edge* edge : nodes[i].conn) {
56                         if (edge->getCap(&nodes[i]) > 0) #760
57                             int np =
58                                 state[lev][i].p +
59                                 (edge->u == &nodes[i] ? edge->cost : -edge->cost);
60                         int ni = edge->from(&nodes[i])->index;
61                         if (np < state[lev + 1][ni].p) #281
62                             state[lev + 1][ni].p = np;
63                             state[lev + 1][ni].used = edge;
64                         }
65                     }
66                 }
67             }
68         }
69     }
70     // Now look at the last level
71     bool valid = false;

```

```

#987    72     for (int i = 0; i < n; i++)
#988     73         if (state[n - 1][i].p > state[n][i].p) {
#989             valid = true;
#990             vector<Edge*> path;
#991             int cap = 1000000000;
#992             Node* cur = &nodes[i]
#993             int clev = n;
#994             vector<bool> explr(n, false);
#995             while (!explr[cur->index]) {
#996                 explr[cur->index] = true;
#997                 State cstate = state[clev][cur->index] #954
#998                 cur = cstate.used->from(cur);
#999                 path.push_back(cstate.used);
#1000             }
#1001             reverse(path.begin(), path.end()); #592
#1002             int i = 0;
#1003             Node* cur2 = cur;
#1004             do {
#1005                 cur2 = path[i]->from(cur2); #990
#1006                 i++;
#1007             } while (cur2 != cur);
#1008             path.resize(i);
#1009             for (auto edge : path) {
#1010                 cap = min(cap, edge->getCap(cur)) #297
#1011                 cur = edge->from(cur);
#1012             }
#1013             for (auto edge : path) {
#1014                 result += edge->addFlow(cur, cap); #599
#1015                 cur = edge->from(cur)
#1016             }
#1017             if (!valid) break;
#1018         }
#1019         return result; #550
#1020     }

```

15 DMST $\mathcal{O}(E \log V)$

```

1 struct EdgeDesc {
2     int from, to, w;
3 };
4 struct DMST {
5     struct Node
6     struct Edge {
7         Node *from;
8         Node *tar;
9         int w;
10        bool inc
11    };
12    struct Circle {

```

```

13     bool vis = false;
14     vector<Edge *> contents;
15     void clean(int idx
16     );
17     const static greater<pair<ll, Edge *> >
18         comp; // Can use inline static since C++17
19     static vector<Circle> to_process;
20     static bool no_dmst
21     static Node *root;
22     struct Node {
23         Node *par = NULL;
24         vector<pair<int, int> > out_cands; // Circ, edge idx
25         vector<pair<ll, Edge *> > con
26         bool in_use = false;
27         ll w = 0; // extra to add to edges in con
28         Nodeanc() {
29             if (!par return thi;
30             while (par->par) par = par->par
31             return par;
32         }
33         void clean() {
34             if (!no_dmst) {
35                 in_use = false
36                 for (auto &cur : out_cands)
37                     to_process[cur.first].clean(cur.second);
38             }
39         }
40         Node con_to_root()
41             if (anc() == root) return root;
42             in_use = true;
43             Node *super = this; // Will become root or the first Node
44                 // encountered in a loop.
45             while (super == this) {
46                 while
47                     !con.empty() && con.front().second->tar->anc() == anc() {
48                         pop_heap(con.begin(), con.end(), comp);
49                         con.pop_back();
50                     }
51                     if (con.empty())
52                         no_dmst = true;
53                         return root;
54                     }
55                     pop_heap(con.begin(), con.end(), comp);
56                     auto nxt = con.back()
57                     con.pop_back();
58                     w = -nxt.first;
59                     if (nxt.second->tar
60                         ->in_use) { // anc() wouldn't change anything
61                         super = nxt.second->tar->anc()
62                         to_process.resize(to_process.size() + 1);
63                     } else {
64                         super = nxt.second->tar->con_to_root();
65
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#946 #478 #608 #721 #465 #488 #363 #506 #541 #174 #595 #848 #860 #064 #295 #995 #989 #895 #771 #405 #732
}
if (super != root)
    to_process.back().contents.push_back(nxt.second);
    out_cands.emplace_back(to_process.size() - 1,
        to_process.back().contents.size() - 1);
} else { // Clean circles
    nxt.second->inc = true
    nxt.second->from->clean();
}
}
if (super != root) { // we are some loops non first Node.
    if (con.size() > super->con.size())
        swap(con,
            super->con); // Largest con in loop should not be copied.
    swap(w, super->w);
}
for (auto cur : con)
    super->con.emplace_back(
        cur.first - super->w + w, cur.second);
    push_heap(super->con.begin(), super->con.end(), comp);
}
par = super; // root or anc() of first Node encountered in a
// loop
return super;
};
Node *cur_root
vector<Node> graph;
vector<Edge> edges;
DMST(int n, vector<EdgeDesc> &desc,
    int r) { // Self loops and multiple edges are okay.
graph.resize(n)
cur_root = &graph[r];
for (auto &cur : desc) // Edges are reversed internally
    edges.push_back(Edge{&graph[cur.to], &graph[cur.from], cur.w});
for (int i = 0; i < desc.size(); ++i)
    graph[desc[i].to].con.emplace_back(desc[i].w, &edges[i])
make_heap(graph[i].con.begin(), graph[i].con.end(), comp);
}
bool find() {
    root = cur_root
    no_dmst = false;
    for (auto &cur : graph) {
        cur.con_to_root();
        to_process.clear();
        if (no_dmst) return false
    }
    return true;
}
#595 #848 #860 #064 #295 #995 #989 #895 #771 #405 #732
%
```

```

116     llweight({
117         ll res = 0;
118         for (auto &cur : edges) {
119             if (cur.inc) res += cur.w;
120
121         return res;
122     };
123 }
124 void DMST::Circle::clean(int idx) {
125     if (!vis) {
126         vis = true;
127         for (int i = 0; i < contents.size(); ++i)
128             if (i != idx) {
129                 contents[i]->inc = true;
130                 contents[i]->from->clean();
131             }
132     }
133 }
134 }
135 const greater<pair<ll, DMST::Edge *>> DMST::comp;
136 vector<DMST::Circle> DMST::to_process;
137 bool DMST::no_dmst
#417

```

16 Bridges $\mathcal{O}(n)$

```

1 struct vert;
2 struct edge {
3     bool exists = true;
4     vert *dest;
5     edge *rev
6     edge(vert *_dest) : dest(_dest) { rev = NULL; }
7     vert &operator*() { return *dest; }
8     vert *operator->() { return dest; }
9     bool is_bridge();
10 }
11 struct vert {
12     deque<edge> con;
13     int val = 0;
14     int seen;
15     int ddfs(int upd, edge *ban{// handles multiple edges
16         if (!val) {
17             val = upd;
18             seen = val;
19             for (edge &nxt : con) {
20                 if (nxt.exists && (&nxt) != ban
21                     seen = min(seen, nxt->dfs(upd + 1, nxt.rev));
22             }
23         }
24         return seen;
25     }
26     void remove_adj_bridges(){
27         for (edge &nxt : con) {
28             if (nxt.is_bridge()) nxt.exists = false;
#369
#477
#814
#711
#922
#116
#331
#866
#624

```

```

29     }
30
31     intcnt_adj_bridges(){
32         int res = 0;
33         for (edge &nxt : con) res += nxt.is_bridge();
34         return res;
35     };
36     bool edge::is_bridge() {
37         return exists &&
38             (dest->seen > rev->dest->val || dest->val < rev->dest->seen);
39             %223
40
41     vert graph[nmax];
42     intmain{// Mechanics Practice BRIDGES
43         int n, m;
44         cin >> n >> m;
45         for (int i = 0; i < m; ++i) {
46             int u, v;
47             scanf "%d %d", &u, &v);
48             graph[u].con.emplace_back(graph + v);
49             graph[v].con.emplace_back(graph + u);
50             graph[u].con.back().rev = &graph[v].con.back();
51             graph[v].con.back().rev = &graph[u].con.back();
52         }
53         graph[1].dfs(1, NULL);
54         int res = 0;
55         for (int i = 1; i <= n; ++i) res += graph[i].cnt_adj_bridges();
56         cout << res / 2 << endl;
#987
#592
#810
#775

```

17 2-Sat $\mathcal{O}(n)$ and SCC $\mathcal{O}(n)$

```

1 struct Graph {
2     int n;
3     vector<vector<int>> conn;
4     Graph(int nsize) {
5         n = nsize
6         conn.resize(n);
7     }
8     void add_edge(int u, int v) { conn[u].push_back(v); }
9     void _topsort_dfs(int pos, vector<int> &result, vector<bool> &explr,
10                     vector<vector<int>> &revconn)
11         if (explr[pos]) return;
12         explr[pos] = true;
13         for (auto next : revconn[pos])
14             _topsort_dfs(next, result, explr, revconn);
15         result.push_back(pos)
16     }
17     vector<int> topsort() {
18         vector<vector<int>> revconn(n);
19         for (int u = 0; u < n; u++) {
20             for (auto v : conn[u]) revconn[v].push_back(u)
21         }
22         vector<int> result;
#775

```

```

23     vector<bool> exprl(n, false);
24     for (int i = 0; i < n; i++)
25         _topsort_dfs(i, result, exprl, revconn)           #178
26     reverse(result.begin(), result.end());
27     return result;
28 }
29 void dfs(int pos, vector<int> &result, vector<bool> &exprl) {
30     if (exprl[pos]) return                                #591
31     exprl[pos] = true;
32     for (auto next : conn[pos]) dfs(next, result, exprl);
33     result.push_back(pos);
34 }
35 vector<vector<int>> scc() {
36     vector<int> order = topsort();
37     reverse(order.begin(), order.end());
38     vector<bool> exprl(n, false);
39     vector<vector<int>> results                      #020
40     for (auto it = order.rbegin(); it != order.rend(); ++it) {
41         vector<int> component;
42         _topsort_dfs(*it, component, exprl, conn);
43         sort(component.begin(), component.end());
44         results.push_back(component)                   #741
45     }
46     sort(results.begin(), results.end());
47     return results;
48 }                                                 %983 // Solution for:
49 // http://codeforces.com/group/PjzGiggT71/contest/221700/problem/C
50 intmain(){
51     int n, m;
52     cin >> n >> m;
53     Graphg(2 * m);
54     for (int i = 0; i < n; i++) {
55         int a, sa, b, sb;
56         cin >> a >> sa >> b >> sb;
57         a--;
58         b--;
59         g.add_edge(2 * a + 1 - sa, 2 * b + sb);
60         g.add_edge(2 * b + 1 - sb, 2 * a + sa);
61     }
62     vector<int> state(2 * m, 0);
63     {
64         vector<int> order = g.topsort();
65         vector<bool> exprl(2 * m, false);
66         for (auto u : order) {
67             vector<int> traversed;
68             g.dfs(u, traversed, exprl);
69             if (traversed.size() > 0 && !state[traversed[0] ^ 1]) {
70                 for (auto c : traversed) state[c] = 1;
71             }
72         }
73     }

```

```

74     for (int i = 0; i < m; i++) {
75         if (state[2 * i] == state[2 * i + 1]) {
76             cout << "IMPOSSIBLE\n";
77             return 0;
78         }
79     }
80     for (int i = 0; i < m; i++) {
81         cout << state[2 * i + 1] << '\n';
82     }
83     return 0;

```

18 Generic persistent compressed lazy segment tree

```

1 struct Seg {
2     ll sum = 0;
3     void recalc(const Seg &lhs_seg, int lhs_len, const Seg &rhs_seg,
4                 int rhs_len)                                #684
5         sum = lhs_seg.sum + rhs_seg.sum
6     }
7 } __attribute__((packed));
8 struct Lazy {
9     ll add;
10    ll assign_val; // LLONG_MIN if no assign;          #529
11    void init() {
12        add = 0;
13        assign_val = LLONG_MIN;
14    }
15    Lazy() { init(); }
16    void split(Lazy &lhs_lazy, Lazy &rhs_lazy, int len{      #819
17        lhs_lazy = *this;
18        rhs_lazy = *this;
19        init();
20    }
21    void merge(Lazy &oth, int len{                         #953
22        if (oth.assign_val != LLONG_MIN) {
23            add = 0;
24            assign_val = oth.assign_val;
25        }
26        add += oth.add;
27    }
28    void apply_to_seg(Seg &cur, int len) const {           #204
29        if (assign_val != LLONG_MIN) {
30            cur.sum = len * assign_val
31        }
32        cur.sum += len * add;
33    }
34 } __attribute__((packed))                                %625
35 struct Node { // Following code should not need to be modified
36     int ver;
37     bool is_lazy = false;
38     Seg seg;
39     Lazy lazy;
40     Node *lc = NULL, *rc = NULL;                          #321

```

```

41 void init() {
42     if (!lc) {
43         lc = new Node{ver};
44         rc = new Node{ver}
45     }
46 }
47 Node upd(int L, int R, int l, int r, Lazy &val, int tar_ver{
48     if (ver != tar_ver) {
49         Node *rep = new Node(*this)
50         rep->ver = tar_ver;
51         return rep->upd(L, R, l, r, val, tar_ver);
52     }
53     if (L >= l && R <= r) {
54         val.apply_to_seg(seg, R - L)
55         lazy.merge(val, R - L);
56         is_lazy = true;
57     } else {
58         init();
59         int M = (L + R) / 2
60         if (is_lazy) {
61             Lazy l_val, r_val;
62             lazy.split(l_val, r_val, R - L);
63             lc = lc->upd(L, M, l, M, l_val, ver);
64             rc = rc->upd(M, R, M, r_val, r_val, ver)
65             is_lazy = false;
66         }
67         Lazy l_val, r_val;
68         val.split(l_val, r_val, R - L);
69         if (l < M) lc = lc->upd(L, M, l, r, l_val, ver)
70         if (M < r) rc = rc->upd(M, R, l, r, r_val, ver);
71         seg.recalc(lc->seg, M - L, rc->seg, R - M);
72     }
73     return this;
74 }
75 void get(int L, int R, int l, int r, Seg *&lft_res, Seg *&tmp,
76          bool last_ver{
77     if (L >= l && R <= r) {
78         tmp->recalc(*lft_res, L - l, seg, R - L);
79         swap(lft_res, tmp)
80     } else {
81         init();
82         int M = (L + R) / 2;
83         if (is_lazy) {
84             Lazy l_val, r_val
85             lazy.split(l_val, r_val, R - L);
86             lc = lc->upd(L, M, l, M, l_val, ver + last_ver);
87             lc->ver = ver;
88             rc = rc->upd(M, R, M, r_val, r_val, ver + last_ver);
89             rc->ver = ver
90             is_lazy = false;
91         }
92         if (l < M) lc->get(L, M, l, r, lft_res, tmp, last_ver);

```

```

93         if (M < r) rc->get(M, R, l, r, lft_res, tmp, last_ver); #770
94     }
95 }
96 } __attribute__((packed));
97 struct SegTree { // indexes start from 0, ranges are [beg, end)
98     vector<Node *> roots; // versions start from 0
99     int len; #873
100    SegTree(int _len) : len(_len) { roots.push_back(new Node{0}); }
101    int upd(int l, int r, Lazy &val, bool new_ver = false) {
102        Node *cur_root =
103            roots.back()->upd(0, len, l, r, val, roots.size() - !new_ver);
104        if (cur_root != roots.back()) roots.push_back(cur_root); #700
105        return roots.size() - 1;
106    }
107    Seg get(int l, int r, int ver = -1) {
108        if (ver == -1) ver = roots.size() - 1;
109        Seg seg1, seg2; #751
110        Seg *pres = &seg1, *ptmp = &seg2;
111        roots[ver]->get(0, len, l, r, pres, ptmp, roots.size() - 1);
112        return *pres;
113    }
114 } #542
115 int main(){ %542
116     int n, m;// solves Mechanics Practice LAZY
117     cin >> n >> m;
118     SegTree seg_tree(1 << 17);
119     for (int i = 0; i < n; ++i) {
120         Lazy tmp;
121         scanf("%lld", &tmp.assign_val);
122         seg_tree.upd(i, i + 1, tmp);
123     }
124     for (int i = 0; i < m; ++i) {
125         int o;
126         int l, r;
127         scanf("%d %d %d", &o, &l, &r);
128         --l;
129         if (o == 1) {
130             Lazy tmp;
131             scanf("%lld", &tmp.add);
132             seg_tree.upd(l, r, tmp);
133         } else if (o == 2) {
134             Lazy tmp;
135             scanf("%lld", &tmp.assign_val);
136             seg_tree.upd(l, r, tmp);
137         } else {
138             Seg res = seg_tree.get(l, r);
139             printf("%lld\n", res.sum);
140         }
141     }

```

19 Templatized HLD $\mathcal{O}(M(n) \log n)$ per query

```

1 class dummy {
2 public:
3     dummy() {}
4     dummy(int, int) {}
5     void set(int, int) { #531
6         intquery(int left, int right{
7             cout << this << ' ' << left << ' ' << right << endl;
8         }
9     } /* T should be the type of the data stored in each vertex;
10    * DS should be the underlying data structure that is used to perform
11    * the group operation. It should have the following methods:
12    * * DS () - empty constructor
13    * * DS (int size, T initial) - constructs the structure with the
14    * given size, initially filled with initial.
15    * * void set (int index, T value) - set the value at index `index` to
16    * `value`
17    * * T query (int left, int right) - return the "sum" of elements
18    * between left and right, inclusive.
19 */
20 template <typename T, class DS>
21 class HLD {
22     int vertexc;
23     vector<int> *adj;
24     vector<int> subtree_size #178
25     DS structure;
26     DS aux;
27     void build_sizes(int vertex, int parent{
28         subtree_size[vertex] = 1;
29         for (int child : adj[vertex]) #037
30             if (child != parent) {
31                 build_sizes(child, vertex);
32                 subtree_size[vertex] += subtree_size[child];
33             }
34     }
35     int cur;
36     vector<int> ord;
37     vector<int> chain_root;
38     vector<int> par #593
39     void build_hld(int vertex, int parent, int chain_source{
40         cur++;
41         ord[vertex] = cur;
42         chain_root[vertex] = chain_source;
43         par[vertex] = parent
44         if (adj[vertex].size() > 1 ||
45             (vertex == 1 && adj[vertex].size() == 1)) {
46             int big_child, big_size = -1;
47             for (int child : adj[vertex]) {
48                 if ((child != parent) && (subtree_size[child] > big_size))
49                     #042

```

```

50                     big_child = child;
51                     big_size = subtree_size[child];
52                 }
53             }
54             build_hld(big_child, vertex, chain_source) #254
55             for (int child : adj[vertex]) {
56                 if ((child != parent) && (child != big_child))
57                     build_hld(child, vertex, child);
58             }
59         }
60     }
61     public:
62     HLD(int _vertexc) {
63         vertexc = _vertexc;
64         adj = new vector<int>[vertexc + 5] #800
65     }
66     void add_edge(int u, int v) {
67         adj[u].push_back(v);
68         adj[v].push_back(u);
69     }
70     void build(T initial) #587
71         subtree_size = vector<int>(vertexc + 5);
72         ord = vector<int>(vertexc + 5);
73         chain_root = vector<int>(vertexc + 5);
74         par = vector<int>(vertexc + 5) #976
75         cur = 0;
76         build_sizes(1, -1);
77         build_hld(1, -1, 1);
78         structure = DS(vertexc + 5, initial);
79         aux = DS(50, initial) #638
80     }
81     void set(int vertex, int value) {
82         structure.set(ord[vertex], value);
83     }
84     T query_path #325
85     int u, int v) /* returns the "sum" of the path u->v */
86     int cur_id = 0;
87     while (chain_root[u] != chain_root[v]) {
88         if (ord[u] > ord[v]) { #052
89             cur_id++;
90             aux.set(cur_id, structure.query(ord[chain_root[u]], ord[u]));
91             u = par[chain_root[u]];
92         } else {
93             cur_id++;
94             aux.set(cur_id, structure.query(ord[chain_root[v]], ord[v])) #485
95             v = par[chain_root[v]];
96         }
97     }
98     cur_id++;
99     aux.set(cur_id) #041

```

```

100     structure.query(min(ord[u], ord[v]), max(ord[u], ord[v]))); #905
101     return aux.query(1, cur_id);
102
103 voidprint(){
104     for (int i = 1; i <= vertexc; i++)
105         cout << i << ' ' << ord[i] << ' ' << chain_root[i] << ' '
106         << par[i] << endl;
107 }
108 };
109 intmain{
110     int vertexc;
111     cin >> vertexc;
112     HLD<int, dummy> hld(vertexc);
113     for (int i = 0; i < vertexc - 1; i++) {
114         int u, v;
115         cin >> u >> v;
116         hld.add_edge(u, v);
117     }
118     hld.build();
119     hld.print();
120     int queryc;
121     cin >> queryc;
122     for (int i = 0; i < queryc; i++) {
123         int u, v;
124         cin >> u >> v;
125         hld.query_path(u, v);
126         cout << endl;
127     }

```

20 Templatized multi dimensional BIT $\mathcal{O}(\log(n)^{\dim})$ per query

```

1 // Fully overloaded any dimensional BIT, use any type for coordinates,
2 // elements, return_value. Includes coordinate compression.
3 template <typename elem_t, typename coord_t, coord_t n_inf,
4           typename ret_t>
5 class BIT {
6     vector<coord_t> positions;
7     vector<elem_t> elems;
8     bool initiated = false;
9 public:
10    BIT() { positions.push_back(n_inf); } #324
11    void initiate() {
12        if (initiated)
13            for (elem_t &c_ele : elems) c_ele.initiate(); #330
14        else {
15            initiated = true;
16            sort(positions.begin(), positions.end());
17            positions.resize(unique(positions.begin(), positions.end()))
18            ← #822
19            positions.begin());
20            elems.resize(positions.size());
21        }

```

```

22     template <typename... loc_form> #620
23     voidupdate(coord_t cord, loc_form... args{
24         if (initiated) {
25             int pos =
26                 lower_bound(positions.begin(), positions.end(), cord) - #346
27                 positions.begin()
28             for (; pos < positions.size(); pos += pos & -pos)
29                 elems[pos].update(args...);
30         } else {
31             positions.push_back(cord);
32         }
33     }
34     template <typename... loc_form>
35     ret_t query(coord_t cord, #542
36                 loc_form... args) { // sum in open interval (-inf, cord)
37         ret_t res = 0 #326
38         int pos = (lower_bound(positions.begin(), positions.end(), cord) - #549
39                     positions.begin()) -
40                     1;
41         for (; pos > 0; pos -= pos & -pos)
42             res += elems[pos].query(args...)
43         return res;
44     }
45 };
46 template <typename internal_type> #616
47 struct wrapped
48     internal_type a = 0;
49     voidupdate(internal_type b{ a += b; })
50     internal_typequery({ return a; })
51 // Should never be called, needed for compilation
52     voidinitiate({ cerr << 'i' << endl; })
53     voidupdate({ cerr << 'u' << endl; }) #636
54 }
55 intmain{ #714
56     // return type should be same as type inside wrapped
57     BIT<BIT<wrapped<ll>, int, INT_MIN, ll>, int, INT_MIN, ll> fenwick;
58     int dim = 2;
59     vector<tuple<int, int, ll> > to_insert;
60     to_insert.emplace_back(1, 1, 1);
61     // set up all positions that are to be used for update
62     for (int i = 0; i < dim; ++i) {
63         for (auto &cur : to_insert)
64             fenwick.update(get<0>(cur),
65                           get<1>(cur)); // May include value which won't be used
66         fenwick.initiate();
67     }
68     // actual use
69     for (auto &cur : to_insert)
70         fenwick.update(get<0>(cur), get<1>(cur), get<2>(cur));
71     cout << fenwick.query(2, 2) << '\n';

```

21 Treap $\mathcal{O}(\log n)$ per query

```

1 mt19937 randgen;
2 struct Treap {
3     struct Node {
4         int key;
5         int value;
6         unsigned int priority;
7         long long total;
8         Node* lch;
9         Node* rch;
10    Node(int new_key, int new_value)
11        key = new_key;
12        value = new_value;
13        priority = randgen();
14        total = new_value;
15        lch = 0
16        rch = 0;
17    }
18    void update() {
19        total = value;
20        if (lch) total += lch->total
21        if (rch) total += rch->total;
22    }
23};
24 deque<Node> nodes;
25 Node* root = 0
26 pair<Node*, Node*> split(int key, Node* cur) {
27    if (cur == 0) return {0, 0};
28    pair<Node*, Node*> result;
29    if (key <= cur->key) {
30        auto ret = split(key, cur->lch)
31        cur->lch = ret.second;
32        result = {ret.first, cur};
33    } else {
34        auto ret = split(key, cur->rch);
35        cur->rch = ret.first
36        result = {cur, ret.second};
37    }
38    cur->update();
39    return result;
40}
41 Node* merge(Node* left, Node* right{
42    if (left == 0) return right;
43    if (right == 0) return left;
44    Node* top;
45    if (left->priority < right->priority)
46        left->rch = merge(left->rch, right);
47        top = left;
48    } else {
49        right->lch = merge(left, right->lch);
50        top = right
51    }
52    top->update();
53    return top;
54}
55 void insert(int key, int value) #918
56     nodes.push_back(Node(key, value));
57     Node* cur = &nodes.back();
58     pair<Node*, Node*> ret = split(key, root);
59     cur = merge(ret.first, cur);
60     cur = merge(cur, ret.second)
61     root = cur;
62}
63 void erase(int key) { #760
64    Node *left, *mid, *right;
65    tie(left, mid) = split(key, root)
66    tie(mid, right) = split(key + 1, mid);
67    root = merge(left, right);
68}
69 long long sum_upto(int key, Node* cur) { #416
70    if (cur == 0) return 0
71    if (key <= cur->key) {
72        return sum_upto(key, cur->lch);
73    } else {
74        long long result = cur->value + sum_upto(key, cur->rch);
75        if (cur->lch) result += cur->lch->total
76        return result;
77    }
78}
79 long long get(int l, int r) { #634
80    return sum_upto(r + 1, root) - sum_upto(l, root)
81}
82} %959 // Solution for:
83 // http://codeforces.com/group/U01GDa2Gwb/contest/219104/problem/TREAP
84 int main(){
85    ios_base::sync_with_stdio(false);
86    cin.tie(0);
87    int m;
88    Treap treap;
89    cin >> m;
90    for (int i = 0; i < m; i++) {
91        int type;
92        cin >> type;
93        if (type == 1) {
94            int x, y;
95            cin >> x >> y;
96            treap.insert(x, y);
97        } else if (type == 2) {
98            int x;
99            cin >> x;
100           treap.erase(x);
101    }

```

```

102     int l, r;
103     cin >> l >> r;
104     cout << treap.get(l, r) << endl;
105   }
106 }
107 return 0;

22 Radixsort 50M 64 bit integers as single array in 1 sec

1 typedef unsigned char uchar;
2 template <typename T>
3 void msd_radixsort(
4   T *start, T *sec_start, int arr_size, int d = sizeof(T) - 1 {           #866
5     const int msd_radix_lim = 100
6     const T mask = 255;
7     int bucket_sizes[256]{};
8     for (T *it = start; it != start + arr_size; ++it) {
9       ++bucket_sizes[((*it) >> (d * 8)) & mask];
10      //++bucket_sizes[*((uchar*)it + d)];                                #772
11
12     T *locs_mem[257];
13     locs_mem[0] = sec_start;
14     T **locs = locs_mem + 1;
15     locs[0] = sec_start;
16     for (int j = 0; j < 255; ++j)                                         #818
17       locs[j + 1] = locs[j] + bucket_sizes[j];
18   }
19   for (T *it = start; it != start + arr_size; ++it) {
20     uchar bucket_id = ((*it) >> (d * 8)) & mask;
21     *(locs[bucket_id]++) = *it                                         #361
22   }
23   locs = locs_mem;
24   if (d) {
25     T *locs_old[256];
26     locs_old[0] = start                                                 #153
27     for (int j = 0; j < 255; ++j) {
28       locs_old[j + 1] = locs_old[j] + bucket_sizes[j];
29     }
30     for (int j = 0; j < 256; ++j) {                                         #867
31       if (locs[j + 1] - locs[j] < msd_radix_lim)
32         std::sort(locs[j], locs[j + 1]);
33       if (d & 1) {
34         copy(locs[j], locs[j + 1], locs_old[j]);
35       }
36     } else                                                               #946
37     msd_radixsort(locs[j], locs_old[j], bucket_sizes[j], d - 1);
38   }
39 }
40 } %225
41 const int nmax = 5e7;
42 ll arr[nmax], tmp[nmax];
43 int main({
```

```

45   for (int i = 0; i < nmax; ++i) arr[i] = ((ll)rand() << 32) | rand();
46   msd_radixsort(arr, tmp, nmax);
47   assert(is_sorted(arr, arr + nmax));

23 FFT 5M length/sec
integer  $c = a * b$  is accurate if  $c_i < 2^{49}$ 

1 struct Complex {
2   double a = 0, b = 0;
3   Complex &operator=(const int &oth) {
4     a /= oth;
5     b /= oth                                         #139
6     return *this;
7   }
8 };
9 Complex operator+(const Complex &lft, const Complex &rgt) {          #384
10  return Complex{lft.a + rgt.a, lft.b + rgt.b};
11 }
12 Complex operator-(const Complex &lft, const Complex &rgt) {
13  return Complex{lft.a - rgt.a, lft.b - rgt.b};
14 }
15 Complex operator*(const Complex &lft, const Complex &rgt)           #560
16  return Complex{
17    lft.a * rgt.a - lft.b * rgt.b, lft.a * rgt.b + lft.b * rgt.a};
18 }
19 Complex conj(const Complex &cur) { return Complex{cur.a, -cur.b}; }
20 void fft_rec(Complex *arr, Complex *root_pow, int len)             #385
21  if (len != 1) {
22    fft_rec(arr, root_pow, len >> 1);
23    fft_rec(arr + len, root_pow, len >> 1);
24  }
25  root_pow += len                                         #216
26  for (int i = 0; i < len; ++i) {
27    Complex tmp = arr[i] + root_pow[i] * arr[i + len];
28    arr[i + len] = arr[i] - root_pow[i] * arr[i + len];
29    arr[i] = tmp;                                         #249
30  }
31 }
32 void fft(vector<Complex> &arr, int ord, bool invert) {
33  assert(arr.size() == 1 << ord);
34  static vector<Complex> root_pow(1);                  #669
35  static int inc_pow = 1;
36  static bool is_inv = false;
37  if (inc_pow <= ord) {
38    int idx = root_pow.size();
39    root_pow.resize(1 << ord);
40    for (; inc_pow <= ord; ++inc_pow)                      #517
41      for (int idx_p = 0; idx_p < 1 << (ord - 1);
42        idx_p += 1 << (ord - inc_pow), ++idx) {
43        root_pow[idx] = Complex{cos(-idx_p * M_PI / (1 << (ord - 1))), sin(-idx_p * M_PI / (1 << (ord - 1)))};
44        if (is_inv) root_pow[idx].b = -root_pow[idx].b      #105
45      }
```

```

46     }
47   }
48 }
49 if (invert != is_inv) {
50   is_inv = invert
51   for (Complex &cur : root_pow) cur.b = -cur.b;
52 }
53 for (int i = 1, j = 0; i < (1 << ord); ++i) {
54   int m = 1 << (ord - 1);
55   bool cont = true
56   while (cont) {
57     cont = j & m;
58     j ^= m;
59     m >>= 1;
60   }
61   if (i < j) swap(arr[i], arr[j]);
62 }
63 fft_rec(arr.data(), root_pow.data(), 1 << (ord - 1));
64 if (invert)
65   for (int i = 0; i < (1 << ord); ++i) arr[i] /= (1 << ord)
66
67 void mult_poly_mod(
68   vector<int> &a, vector<int> &b, vector<int> &c{ // c += a*b
69   static vector<Complex>
70   arr[4]; // correct upto 0.5-2M elements(mod ~ 1e9)
71   if (c.size() < 400)
72     for (int i = 0; i < a.size(); ++i)
73       for (int j = 0; j < b.size() && i + j < c.size(); ++j)
74         c[i + j] = ((ll)a[i] * b[j] + c[i + j]) % mod;
75   } else {
76     int fft_ord = 32 - __builtin_clz(c.size())
77     if (arr[0].size() != 1 << fft_ord)
78       for (int i = 0; i < 4; ++i) arr[i].resize(1 << fft_ord);
79     for (int i = 0; i < 4; ++i)
80       fill(arr[i].begin(), arr[i].end(), Complex{});
81     for (int &cur : a
82       if (cur < 0) cur += mod;
83     for (int &cur : b)
84       if (cur < 0) cur += mod;
85     const int shift = 15;
86     const int mask = (1 << shift) - 1
87     for (int i = 0; i < min(a.size(), c.size()); ++i) {
88       arr[0][i].a = a[i] & mask;
89       arr[1][i].a = a[i] >> shift;
90     }
91     for (int i = 0; i < min(b.size(), c.size()); ++i)
92       arr[0][i].b = b[i] & mask;
93       arr[1][i].b = b[i] >> shift;
94   }
95   for (int i = 0; i < 2; ++i) fft(arr[i], fft_ord, false);
96   for (int i = 0; i < 2; ++i)
97     for (int j = 0; j < 2; ++j) {
#750
#122
#844
#343
%380
#811
#629
#591
#625
#528
#528
#644

```

```

98   int tar = 2 + (i + j) / 2;
99   Complex mult = {0, -0.25};
100  if (i ^ j) mult = {0.25, 0};
101  for (int k = 0; k < (1 << fft_ord); ++k)
102    int rev_k = ((1 << fft_ord) - k) % (1 << fft_ord);
103    Complex ca = arr[i][k] + conj(arr[i][rev_k]);
104    Complex cb = arr[j][k] - conj(arr[j][rev_k]);
105    arr[tar][k] = arr[tar][k] + mult * ca * cb;
106
107  }
108 }
109 for (int i = 2; i < 4; ++i) {
110   fft(arr[i], fft_ord, true);
111   for (int k = 0; k < (int)c.size(); ++k)
112     c[k] = (c[k] + (((ll)(arr[i][k].a + 0.5) % mod)
113                      << (shift * 2 * (i - 2)))) %
114                      mod;
115     c[k] = (c[k] + (((ll)(arr[i][k].b + 0.5) % mod)
116                      << (shift * (2 * (i - 2) + 1)))) %
117                      mod;
118   }
119 }
120
#983
#471
#403
#108
#108
#237
#780
#493
#758
#144
#144

```

24 Fast mod mult, Rabin Miller prime check, Pollard rho factorization $\mathcal{O}(\sqrt{p})$

```

1 struct ModArithm {
2   ull n;
3   ld rec;
4   ModArithm(ull _n) : n(_n) { // n in [2, 1<<63)
5     rec = 1.0L / n
6   }
7   ull multf(ull a, ull b) { // a, b in [0, min(2*n, 1<<63))
8     ull mult = (ld)a * b * rec + 0.5L;
9     ll res = a * b - mult * n;
10    if (res < 0) res += n
11    return res; // in [0, n-1)
12  }
13  ull sqp1(ull a) { return multf(a, a) + 1; }
14 }
15 ull pow_mod(ull a, ull n, ModArithm &arithm{
16   ull res = 1;
17   for (ull i = 1; i <= n; i <= 1) {
18     if (n & i) res = arithm.multf(res, a);
19     a = arithm.multf(a, a)
20   }
21   return res;
22
23 vector<char> small_primes = {
24   2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
25 bool is_prime(ull n){ // n <= 1<<63, 1M rand/s

```



```

13 todo = V/W
14 ord = []
15 while len(todo) > 0:
16     x = min(todo, key=lambda x: f(W+{x}) - f({x}))
17     W += {x}
18     todo -= {x}
19     ord.append(x)
20 return ord[-1], ord[-2]
21 def enum_all_minimal_minimizers(X):
22     # X is a inclusionwise minimal minimizer
23     s = merge(s, X)
24     yield X
25     for {v} in I:
26         if f({v}) == f(X):
27             yield X
28             s = merge(v, s)
29     while size(V) >= 3:
30         t, u = find_pp()
31         tu = merge(t, u)
32         if tu not in I:
33             s = merge(tu, s)
34         elif f({tu}) == f(X):
35             yield tu
36             s = merge(tu, s)

```

26 Berlekamp-Massey $O(\mathcal{LN})$

```

1 template <typename K>
2 static vector<K> berlekamp_massey(vector<K> ss) {
3     vector<K> ts(ss.size());
4     vector<K> cs(ss.size());
5     cs[0] = K::unity;                                #349
6     fill(cs.begin() + 1, cs.end(), K::zero);
7     vector<K> bs = cs;
8     int l = 0, m = 1;
9     K b = K::unity;
10    for (int k = 0; k < (int)ss.size(); k++)          #390
11        K d = ss[k];
12        assert(l <= k);
13        for (int i = 1; i <= l; i++) d += cs[i] * ss[k - i];
14        if (d == K::zero) {
15            m++;                                         #445
16        } else if (2 * l <= k) {
17            K w = d / b;
18            ts = cs;
19            for (int i = 0; i < (int)cs.size() - m; i++)   #661
20                cs[i + m] -= w * bs[i];
21            l = k + 1 - l;
22            swap(bs, ts);
23            b = d;
24            m = 1;
25        } else                                         #815
26            K w = d / b;

```

```

27     for (int i = 0; i < (int)cs.size() - m; i++)
28         cs[i + m] -= w * bs[i];
29     m++;
30 }
31 cs.resize(l + 1);
32 while (cs.back() == K::zero) cs.pop_back();
33 return cs;

```

#888