

University of Tartu ICPC Team Notebook

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1	Setup
2	crc.sh
3	gcc ordered set
4	2D geometry
5	3D geometry
6	Triangle centers
7	Seg-Seg intersection, halfplane intersection area
8	Convex polygon algorithms
9	Delaunay triangulation $\mathcal{O}(n \log n)$
10	Aho Corasick $\mathcal{O}(\alpha \sum \text{len})$
11	Suffix automaton and tree $\mathcal{O}((n+q) \log(\alpha))$
12	Dinic
13	Min Cost Max Flow with successive dijkstra $\mathcal{O}(\text{flow} \cdot n^2)$
14	Min Cost Max Flow with Cycle Cancelling $\mathcal{O}(\text{flow} \cdot nm)$
15	DMST $\mathcal{O}(E \log V)$
16	Bridges $\mathcal{O}(n)$
17	2-Sat $\mathcal{O}(n)$ and SCC $\mathcal{O}(n)$
18	Generic persistent compressed lazy segment tree
19	Templated HLD $\mathcal{O}(M(n) \log n)$ per query
20	Templated multi dimensional BIT $\mathcal{O}(\log(n)^{\text{dim}})$ per query
21	Treap $\mathcal{O}(\log n)$ per query
22	Radixsort 50M 64 bit integers as single array in 1 sec

23	FFT 5M length/sec	22	University of Tartu
24	Fast mod mult, Rabbin Miller prime check, Pollard rho factorization $\mathcal{O}(\sqrt{p})$	23	
25	Symmetric Submodular Functions; Queyrannes's algorithm	24	
26	Berlekamp-Massey $\mathcal{O}(\mathcal{L}N)$	25	
1	1 Setup		
3	<pre> 1 set smartindent cindent 2 set ts=4 sw=4 expandtab 3 syntax enable 4 set clipboard=unnamedplus 5 # setxkbmap -option caps:escape 6 # valgrind --vgdb-error=0 ./a <inp & 7 # gdb a 8 # target remote vgdb </pre>		
7	2 crc.sh		
9	<pre> 1 #!/bin/envbash 2 for j in `seq 5 5 200`; do 3 sed '/~\s*\$/d' \$1 head -\$j tr -d '[:space:]' cksum cut -f1 4 ↪ -d ' ' tail -c 4 #whistespaces don't matter. 5 done #there shouldn't be any COMMENTS. 6 #copy lines being checked to separate file. 7 # \$./crc.sh tmp.cpp </pre>		
11	3 gcc ordered set		
12	<pre> 1 #define DEBUG(...) cerr << __VA_ARGS__ << endl; 2 #ifndef CDEBUG 3 #undef DEBUG 4 #define DEBUG(...) ((void)0); 5 #define NDEBUG@ 6 #endif 7 #define ran(i, a, b) for (auto i = (a); i < (b); i++) 8 #include <bits/stdc++.h> 9 typedef long long ll; 10 typedef long double ld 11 using namespace std; #include <ext/pb_ds/assoc_container.hpp> 12 #include <ext/pb_ds/tree_policy.hpp> 13 using namespace __gnu_pbds; 14 template <typename T 15 using ordered_set = tree<T, null_type, less<T>, rb_tree_tag, 16 tree_order_statistics_node_update>; 17 intmain({ 18 ordered_set<int> cur; 19 cur.insert(1) 20 cur.insert(3); 21 cout << cur.order_of_key(2) 22 << endl; // the number of elements in the set less than 2 </pre>	#438 @	
16		#546	
17		#822	
20		#325	
21			
22			

```
23  cout << *cur.find_by_order(0)
24      << endl; // the 0-th smallest number in the set(0-based)    #478
25  cout << *cur.find_by_order(1)
26      << endl; // the 1-th smallest number in the set(0-based)
```

4 2D geometry

Define $\text{orient}(A, B, C) = \overline{AB} \times \overline{AC}$. CCW iff > 0 .
Define $\text{perp}((a, b)) = (-b, a)$. The vectors are orthogonal.

For line $ax + by = c$ def $\bar{v} = (-b, a)$.

Line through P and Q has $\bar{v} = \overline{PQ}$ and $c = \bar{v} \times P$.

$\text{side}_l(P) = \bar{v}_l \times P - c_l$ sign determines which side P is on from l .

$\text{dist}_l(P) = \text{side}_l(P) / \|\bar{v}_l\|$ squared is integer.

Sorting points along a line: comparator is $\bar{v} \cdot A < \bar{v} \cdot B$.

Translating line by \bar{t} : new line has $c' = c + \bar{v} \times \bar{t}$.

Line intersection: is $(c_l \bar{v}_m - c_m \bar{v}_l) / (\bar{v}_l \times \bar{v}_m)$.

Project P onto l : is $P - \text{perp}(v) \text{side}_l(P) / \|v\|^2$.

Angle bisectors: $\bar{v} = \bar{v}_l / \|\bar{v}_l\| + \bar{v}_m / \|\bar{v}_m\|$

$c = c_l / \|\bar{v}_l\| + c_m / \|\bar{v}_m\|$.

P is on segment AB iff $\text{orient}(A, B, P) = 0$ and $\overline{PA} \cdot \overline{PB} \leq 0$.

Proper intersection of AB and CD exists iff $\text{orient}(C, D, A)$ and $\text{orient}(C, D, B)$ have opp. signs and $\text{orient}(A, B, C)$ and $\text{orient}(A, B, D)$ have opp. signs. Coordinates:

$$\frac{A \text{ orient}(C, D, B) - B \text{ orient}(C, D, A)}{\text{orient}(C, D, B) - \text{orient}(C, D, A)}.$$

Circumcircle center:

```
pt circumCenter(pt a, pt b, pt c) {
    b = b-a, c = c-a; // consider coordinates
    relative to A
    assert(cross(b,c) != 0); // no circumcircle if
    A,B,C aligned
    return a + perp(b*sq(c) - c*sq(b))/cross(b,c)
    /2;
```

Circle-line intersect:

```
int circleLine(pt o, double r, line l, pair<pt,
    pt> &out) {
    double h2 = r*r - l.sqDist(o);
    if (h2 >= 0) { // the line touches the circle
        pt p = l.proj(o); // point P
        pt h = l.v*sqrt(h2)/abs(l.v); // vector
        paral to l, of len h
        out = {p-h, p+h};
    }
    return 1 + sgn(h2);
```

Circle-circle intersect:

```
int circleCircle(pt o1, double r1, pt o2, double
    r2, pair<pt,pt> &out) {
    pt d=o2-o1; double d2=sq(d);
```

```
if (d2 == 0) {assert(r1 != r2); return 0;} //
    concentric circles
double pd = (d2 + r1*r1 - r2*r2)/2; // = |O_1P
    | * d
double h2 = r1*r1 - pd*pd/d2; // = h^2
if (h2 >= 0) {
    pt p = o1 + d*pd/d2, h = perp(d)*sqrt(h2/d2)
    ;
    out = {p-h, p+h};}
return 1 + sgn(h2);
```

Tangent lines:

```
int tangents(pt o1, double r1, pt o2, double r2,
    bool inner, vector<pair<pt,pt>> &out) {
    if (inner) r2 = -r2;
    pt d = o2-o1;
    double dr = r1-r2, d2 = sq(d), h2 = d2-dr*dr;
    if (d2 == 0 || h2 < 0) {assert(h2 != 0);
        return 0;}
    for (double sign : {-1,1}) {
        pt v = (d*dr + perp(d)*sqrt(h2)*sign)/d2;
        out.push_back({o1 + v*r1, o2 + v*r2});}
    return 1 + (h2 > 0);
```

5 3D geometry

$\text{orient}(P, Q, R, S) = (\overline{PQ} \times \overline{PR}) \cdot \overline{PS}$.

S above PQR iff > 0 .

For plane $ax + by + cz = d$ def $\bar{n} = (a, b, c)$.

Line with normal \bar{n} through point P has $d = \bar{n} \cdot P$.

$\text{side}_\Pi(P) = \bar{n} \cdot P - d$ sign determines side from Π .

$\text{dist}_\Pi(P) = \text{side}_\Pi(P) / \|\bar{n}\|$.

Translating plane by \bar{t} makes $d' = d + \bar{n} \cdot \bar{t}$.

Plane-plane intersection of has direction $\bar{n}_1 \times \bar{n}_2$ and goes

through $((d_1 \bar{n}_2 - d_2 \bar{n}_1) \times \bar{d}) / \|\bar{d}\|^2$.

Line-line distance:

```
double dist(line3d l1, line3d l2) {
    p3 n = l1.d*l2.d;
    if (n == zero) // parallel
        return l1.dist(l2.o);
    return abs((l2.o-l1.o)|n)/abs(n);
```

Spherical to Cartesian:

$(r \cos \varphi \cos \lambda, r \cos \varphi \sin \lambda, r \sin \varphi)$.

Sphere-line intersection:

```
int sphereLine(p3 o, double r, line3d l, pair<p3
    ,p3> &out) {
    double h2 = r*r - l.sqDist(o);
    if (h2 < 0) return 0; // the line doesn't
    touch the sphere
    p3 p = l.proj(o); // point P
    p3 h = l.d*sqrt(h2)/abs(l.d); // vector
    parallel to l, of length h
    out = {p-h, p+h};
```

```
return 1 + (h2 > 0);
```

Great-circle distance between points A and B is $r \angle AOB$.

Spherical segment intersection:

```
bool properInter(p3 a, p3 b, p3 c, p3 d, p3 &out
    ) {
    p3 ab = a*b, cd = c*d; // normals of planes
    OAB and OCD
    int oa = sgn(cd|a),
        ob = sgn(cd|b),
        oc = sgn(ab|c),
        od = sgn(ab|d);
    out = ab*cd*od; // four multiplications =>
    careful with overflow !
    return (oa != ob && oc != od && oa != oc);
}
bool onSphSegment(p3 a, p3 b, p3 p) {
    p3 n = a*b;
    if (n == zero)
        return a*p == zero && (a|p) > 0;
    return (n|p) == 0 && (n|a*p) >= 0 && (n|b*p)
        <= 0;
}
struct directionSet : vector<p3> {
    using vector::vector; // import constructors
    void insert(p3 p) {
        for (p3 q : *this) if (p*q == zero) return;
        push_back(p);
    }
};
directionSet intersSph(p3 a, p3 b, p3 c, p3 d) {
    assert(validSegment(a, b) && validSegment(c, d
        ));
    p3 out;
    if (properInter(a, b, c, d, out)) return {out
        };
    directionSet s;
    if (onSphSegment(c, d, a)) s.insert(a);
    if (onSphSegment(c, d, b)) s.insert(b);
    if (onSphSegment(a, b, c)) s.insert(c);
    if (onSphSegment(a, b, d)) s.insert(d);
    return s;
}
```

Angle between spherical segments AB and AC is angle between $A \times B$ and $A \times C$.

Oriented angle: subtract from 2π if mixed product is negative.

Area of a spherical polygon:

$$r^2 [\text{sum of interior angles} - (n - 2)\pi].$$

6 Triangle centers

```

1 const double min_delta = 1e-13;
2 const double coord_max = 1e6;
3 typedef complex<double> point;
4 point A, B, C; // vertices of the triangle
5 bool collinear(                                     #823
6     double min_diff = min(abs(A - B), min(abs(A - C), abs(B - C)));
7     if (min_diff < coord_max * min_delta) return true;
8     point sp = (B - A) / (C - A);
9     double ang =
10         M_PI / 2                                     #638
11         abs(abs(arg(sp)) - M_PI / 2); // positive angle with the real line
12     return ang < min_delta;                         %446
13
14 point circum_center({
15     if (collinear()) return point(NAN, NAN);
16     // squared lengths of sides
17     double a2 = norm(B - C);
18     double b2 = norm(A - C);
19     double c2 = norm(A - B)                         #715
20     // barycentric coordinates of the circumcenter
21     double c_A = a2 * (b2 + c2 - a2); // sin(2 * alpha) works also
22     double c_B = b2 * (a2 + c2 - b2);
23     double c_C = c2 * (a2 + b2 - c2);
24     double sum = c_A + c_B + c_C;
25     c_A /= sum                                       #407
26     c_B /= sum;
27     c_C /= sum;
28     return c_A * A + c_B * B + c_C * C; // cartesian
29                                                     %856
30 point centroid({ // center of mass
31     return (A + B + C) / 3.0;
32 }
33 point ortho_center() { // euler line
34     point O = circum_center()
35     return O + 3.0 * (centroid() - O);              #895
36 };
37 point nine_point_circle_center({ // euler line
38     point O = circum_center();
39     return O + 1.5 * (centroid() - O)               #193
40 }                                     %031
41 point in_center({
42     if (collinear()) return point(NAN, NAN);
43     double a = abs(B - C); // side lengths
44     double b = abs(A - C);
45     double c = abs(A - B)                           #954
46     // trilinear coordinates are (1,1,1)
47     double sum = a + b + c;
48     a /= sum;
49     b /= sum;
50     c /= sum;                                     // barycentric

```

```

51 return a * A + b * B + c * C; // cartesian          #596

```

7 Seg-Seg intersection, halfplane intersection area

```

1 struct Seg {
2     Vec a, b;
3     Vecd({ return b - a; }
4 };
5 Vec intersection(Seg l, Seg r                                     #327
6     Vec dl = l.d(), dr = r.d();
7     if (cross(dl, dr) == 0) return {nanl(""), nanl("")};
8     double h = cross(dr, l.a - r.a) / len(dr);
9     double dh = cross(dr, dl) / len(dr);
10    return l.a + dl * (h / -dh)                               #893
11 } // Returns the area bounded by halfplanes
12 double calc_area(vector<Seg> lines{
13     double lb = -HUGE_VAL, ub = HUGE_VAL;
14     vector<Seg> linesBySide[2];
15     for (auto line : lines)                                   #454
16         if (line.b.y == line.a.y) {
17             if (line.a.x < line.b.x) {
18                 lb = max(lb, line.a.y);
19             } else {
20                 ub = min(ub, line.a.y)                       #029
21             }
22         } else if (line.a.y < line.b.y) {
23             linesBySide[1].push_back(line);
24         } else {
25             linesBySide[0].push_back({line.b, line.a})       #613
26         }
27     }
28     sort(
29         linesBySide[0].begin(), linesBySide[0].end(), [](Seg l, Seg r) {
30             if (cross(l.d(), r.d()) == 0                     #123
31                 return normal(l.d()) * l.a > normal(r.d()) * r.;
32             return cross(l.d(), r.d()) < ;
33         });
34     sort(
35         linesBySide[1].begin(), linesBySide[1].end(), [](Seg l, Seg r)
36         → #115
37         if (cross(l.d(), r.d()) == 0)
38             return normal(l.d()) * l.a < normal(r.d()) * r.a;
39         return cross(l.d(), r.d()) > ;
40     });
41     // Now find the application area of the lines and clean up redundant
42     // ones
43     vector<double> applyStart[2]                               #597
44     for (int side = 0; side < 2; side++) {
45         vector<double> &apply = applyStart[side];
46         vector<Seg> curLines;
47         for (auto line : linesBySide[side]) {
48             while (curLines.size() > 0)                       #412
49                 Seg other = curLines.back();

```

```

49     if (cross(line.d(), other.d()) != 0) {
50         double start = intersection(line, other).y;
51         if (start > apply.back()) break;
52
53         curLines.pop_back();
54         apply.pop_back();
55     }
56     if (curLines.size() == 0) {
57         apply.push_back(-HUGE_VAL)
58     } else {
59         apply.push_back(intersection(line, curLines.back()).y);
60     }
61     curLines.push_back(line);
62
63     linesBySide[side] = curLines;
64 }
65 applyStart[0].push_back(HUGE_VALL);
66 applyStart[1].push_back(HUGE_VALL);
67 double result = 0
68 {
69     double lb = -HUGE_VALL, ub;
70     for (int i = 0, j = 0; i < (int)linesBySide[0].size() &&
71         j < (int)linesBySide[1].size();
72         lb = ub)
73         ub = min(applyStart[0][i + 1], applyStart[1][j + 1]);
74     double alb = lb, aub = ub;
75     Seg l0 = linesBySide[0][i], l1 = linesBySide[1][j];
76     if (cross(l1.d(), l0.d()) > 0) {
77         alb = max(alb, intersection(l0, l1).y)
78     } else if (cross(l1.d(), l0.d()) < 0) {
79         aub = min(aub, intersection(l0, l1).y);
80     }
81     alb = max(alb, lb);
82     aub = min(aub, ub)
83     aub = max(aub, alb);
84     {
85         double x1 = l0.a.x + (alb - l0.a.y) / l0.d().y * l0.d().x;
86         double x2 = l1.a.x + (aub - l1.a.y) / l1.d().y * l1.d().x;
87         result -= (aub - alb) * (x1 + x2) / 2
88     }
89     {
90         double x1 = l1.a.x + (alb - l1.a.y) / l1.d().y * l1.d().x;
91         double x2 = l1.a.x + (aub - l1.a.y) / l1.d().y * l1.d().x;
92         result += (aub - alb) * (x1 + x2) / 2
93     }
94     if (applyStart[0][i + 1] < applyStart[1][j + 1]) {
95         i++;
96     } else {
97         j++
98     }
99 }
100 }

```

```

101 return result;

```

8 Convex polygon algorithms

```

1 typedef pair<int, int> Vec;
2 typedef pair<Vec, Vec> Seg;
3 typedef vector<Seg>::iterator SegIt; #define F first
4 #define S second @ #608 @
5 #define MP(x, y) make_pair(x, y)
6 lldot(Vec &v1, Vec &v2 { return (l1)v1.F * v2.F + (l1)v1.S * v2.S; }
7 lldcross(Vec &v1, Vec &v2 {
8     return (l1)v1.F * v2.S - (l1)v2.F * v1.S;
9 } #541
10 lldist_sq(Vec &p1, Vec &p2 {
11     return (l1)(p2.F - p1.F) * (p2.F - p1.F) +
12         (l1)(p2.S - p1.S) * (p2.S - p1.S);
13 } %008
14 struct Hull {
15     vector<Seg> hull;
16     SegIt up_beg;
17     template <typename It>
18     void extend(It beg, It end) { // O(n) #096
19         vector<Vec> r;
20         for (auto it = beg; it != end; ++it) {
21             if (r.empty() || *it != r.back()) {
22                 while (r.size() >= 2) {
23                     int n = r.size() #442
24                     Vec v1 = {r[n - 1].F - r[n - 2].F, r[n - 1].S - r[n - 2].S};
25                     Vec v2 = {it->F - r[n - 2].F, it->S - r[n - 2].S};
26                     if (cross(v1, v2) > 0) break;
27                     r.pop_back();
28 } #605
29         r.push_back(*it);
30     }
31 }
32 ran(i, 0, (int)r.size() - 1) hull.emplace_back(r[i], r[i + 1]);
33 #572
34 Hull(vector<Vec> &vert) { // at least 2 distinct points
35     sort(vert.begin(), vert.end()); // O(n log(n))
36     extend(vert.begin(), vert.end());
37     int diff = hull.size();
38     extend(vert.rbegin(), vert.rend()) #964
39     up_beg = hull.begin() + diff;
40 } %722
41 bool contains(Vec p { // O(log(n))
42     if (p < hull.front().F || p > up_beg->F) return false;
43 }
44     auto it_low = lower_bound(
45         hull.begin(), up_beg, MP(MP(p.F, (int)-2e9), MP(0, 0))) #542
46     if (it_low != hull.begin()) --it_low;
47     Vec a = {it_low->S.F - it_low->F.F, it_low->S.S - it_low->F.S};
48     Vec b = {p.F - it_low->F.F, p.S - it_low->F.S};

```

```

49     if (cross(a, b) < 0) // < 0 is inclusive, <=0 is exclusive
50         return false
51     }
52     {
53         auto it_up = lower_bound(hull.rbegin(),
54             hull.rbegin() + (hull.end() - up_beg),
55             MP(MP(p.F, (int)2e9), MP(0, 0)))
56         if (it_up - hull.rbegin() == hull.end() - up_beg) --it_up;
57         Vec a = {it_up->F.F - it_up->S.F, it_up->F.S - it_up->S.S};
58         Vec b = {p.F - it_up->S.F, p.S - it_up->S.S};
59         if (cross(a, b) > 0) // > 0 is inclusive, >=0 is exclusive
60             return false
61     }
62     return true;
63
64     // The function can have only one local min and max
65     // and may be constant only at min and max.
66     template <typename T>
67     SegIt max(function<T(Seg &)> f) // O(log(n))
68     {
69         auto l = hull.begin();
70         auto r = hull.end();
71         SegIt b = hull.end();
72         T b_v;
73         while (r - l > 2) {
74             auto m = l + (r - l) / 2;
75             T l_v = f(*l);
76             T l_n_v = f(*(l + 1));
77             T m_v = f(*m);
78             T m_n_v = f(*(m + 1));
79             if (b == hull.end() || l_v > b_v) {
80                 b = l; // If max is at l we may remove it from the range.
81                 b_v = l_v
82             }
83             if (l_n_v > l_v) {
84                 if (m_v < l_v) {
85                     r = m;
86                 } else
87                 if (m_n_v > m_v) {
88                     l = m + 1;
89                 } else {
90                     r = m + 1;
91                 }
92             } else {
93                 if (m_v < l_v) {
94                     l = m + 1;
95                 } else
96                 if (m_n_v > m_v) {
97                     l = m + 1;
98                 } else {
99                     r = m + 1;
100
101     }
102     }
103     }
104     T l_v = f(*l);
105     if (b == hull.end() || l_v > b_v)
106         b = l;
107     b_v = l_v;
108 }
109 if (r - l > 1) {
110     T l_n_v = f(*(l + 1));
111     if (b == hull.end() || l_n_v > b_v) {
112         b = l + 1;
113         b_v = l_n_v;
114     }
115     return b;
116
117 SegIt closest(Vec p // p can't be internal (can be on border),
118             // hull must have at least 3 points
119 Seg &ref_p = hull.front(); // O(log(n))
120 return max(function<double>(Seg &>(&p, &ref_p) {
121     Seg &seg) // accuracy of used type should be coord^2
122     if (p == seg.F) return 10 - M_PI;
123     Vec v1 = {seg.S.F - seg.F.F, seg.S.S - seg.F.S};
124     Vec v2 = {p.F - seg.F.F, p.S - seg.F.S};
125     ll c_p = cross(v1, v2);
126     if (c_p > 0) // order the backside by angle
127         Vec v1 = {ref_p.F.F - p.F, ref_p.F.S - p.S};
128         Vec v2 = {seg.F.F - p.F, seg.F.S - p.S};
129         ll d_p = dot(v1, v2);
130         ll c_p = cross(v2, v1);
131         return atan2(c_p, d_p /
132     }
133     ll d_p = dot(v1, v2);
134     double res = atan2(d_p, c_p);
135     if (d_p <= 0 && res > 0) res = -M_PI;
136     if (res > 0)
137         res += 20;
138     } else {
139         res = 10 - res;
140     }
141     return res
142 }));
143
144 template <int DIRECTION> // 1 or -1
145 Vectan_point(Vec p // can't be internal or on border
146             // -1 iff CCW rotation of ray from p to res takes it away from
147             // polygon?
148 Seg &ref_p = hull.front(); // O(log(n))

```

#864

#972

#086

%504

#566

#586

#332

#279

#656

#311

#469

#864

#972

#086

%504

#566

#586

#332

#279

#656

#311

#469

#864

#972

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```

151 auto best_seg = max(function<double>(Seg &)>(<
152   [&p, &ref_p]                                     #209
153   Seg &seg) {// accuracy of used type should be coord^2
154   Vec v1 = {ref_p.F.F - p.F, ref_p.F.S - p.S};
155   Vec v2 = {seg.F.F - p.F, seg.F.S - p.S};
156   ll d_p = dot(v1, v2);
157   ll c_p = DIRECTION * cross(v2, v1)               #762
158   return atan2(c_p, d_p; // order by signed angle
159   ));
160 return best_seg->F;
161
162 SegIt max_in_dir(Vec v {// first is the ans. O(log(n))
163   return max(
164     function<ll>(Seg &)>([&v](Seg &seg){ return dot(v, seg.F); }));
165   #596
166 pair<SegIt, SegIt> intersections(Seg l) {// O(log(n))
167   int x = l.S.F - l.F.F;
168   int y = l.S.S - l.F.S;
169   Vec dir = {-y, x};
170   auto it_max = max_in_dir(dir)                     #740
171   auto it_min = max_in_dir(MP(y, -x));
172   ll opt_val = dot(dir, l.F);
173   if (dot(dir, it_max->F) < opt_val ||
174       dot(dir, it_min->F) > opt_val)
175     return MP(hull.end(), hull.end())                #276
176   SegIt it_r1, it_r2;
177   function<bool>(Seg &, Seg &)> inc_c([&dir](Seg &lft, Seg &rgt) {
178     return dot(dir, lft.F) < dot(dir, rgt.F);
179   });
180   function<bool>(Seg &, Seg &)> dec_c([&dir](Seg &lft, Seg &rgt)
181     ↪ #431
182     return dot(dir, lft.F > dot(dir, rgt.F;
183   ));
184   if (it_min <= it_max) {
185     it_r1 = upper_bound(it_min, it_max + 1, l, inc_c) - 1;
186     if (dot(dir, hull.front().F) >= opt_val)           #689
187       it_r2 = upper_bound(hull.begin(), it_min + 1, l, dec_c) - 1;
188     } else {
189       it_r2 = upper_bound(it_max, hull.end(), l, dec_c) - 1;
190     }
191   } else
192     it_r1 = upper_bound(it_max, it_min + 1, l, dec_c) - 1;           #552
193   if (dot(dir, hull.front().F) <= opt_val) {
194     it_r2 = upper_bound(hull.begin(), it_max + 1, l, inc_c) - 1;
195   } else {
196     it_r2 = upper_bound(it_min, hull.end(), l, inc_c) - 1           #220
197   }
198   return MP(it_r1, it_r2);
199
200 Seg diameter({// O(n)

```

%037

%596

#740

#276

#689

#552

#220

%498

```

201 Seg res;
202 ll dia_sq = 0;
203 auto it1 = hull.begin();
204 auto it2 = up_beg                                     #632
205 Vec v1 = {hull.back().S.F - hull.back().F.F,
206   hull.back().S.S - hull.back().F.S};
207 while (it2 != hull.begin()) {
208   Vec v2 = {(it2 - 1)->S.F - (it2 - 1)->F.F,
209     (it2 - 1)->S.S - (it2 - 1)->F.S}
210   if (cross(v1, v2) > 0) break;
211   --it2;
212 }
213 while (it2 != hull.end()) {// check all antipodal pairs
214   if (dist_sq(it1->F, it2->F) > dia_sq)                 #246
215     res = {it1->F, it2->F};
216     dia_sq = dist_sq(res.F, res.S);
217   }
218   Vec v1 = {it1->S.F - it1->F.F, it1->S.S - it1->F.S};
219   Vec v2 = {it2->S.F - it2->F.F, it2->S.S - it2->F.S}
220   if (cross(v1, v2) == 0) {
221     if (dist_sq(it1->S, it2->F) > dia_sq) {
222       res = {it1->S, it2->F};
223       dia_sq = dist_sq(res.F, res.S);
224     }
225     if (dist_sq(it1->F, it2->S) > dia_sq) {
226       res = {it1->F, it2->S};
227       dia_sq = dist_sq(res.F, res.S);
228     }// report cross pairs at parallel lines.
229     ++it1
230     ++it2;
231   } else if (cross(v1, v2) < 0) {
232     ++it1;
233   } else {
234     ++it2
235   }
236 }
237 return res;
238 }

```

#150

#246

#529

#406

#362

#936

9 Delaunay triangulation $\mathcal{O}(n \log n)$

```

1 const int max_co = (1 << 28) - 5;
2 struct Vec {
3   int x, y;
4   bool operator==(const Vec &oth) { return x == oth.x && y == oth.y; }
5   bool operator!=(const Vec &oth) { return !operator==(oth); }           #679
6   Vec operator-(const Vec &oth) { return {x - oth.x, y - oth.y}; }
7 };
8 lldot(Vec a, Vec b { return (ll)a.x * b.y - (ll)a.y * b.x; }
9 lldot(Vec a, Vec b { return (ll)a.x * b.x + (ll)a.y * b.y; }
10 struct Edge
11   Vec tar;
12   Edge *nxt;

```

#732

```

13  Edge *inv = NULL;
14  Edge *rep = NULL;
15  bool vis = false
16 };
17 struct Seg {
18     Vec a, b;
19     bool operator==(const Seg &oth) { return a == oth.a && b == oth.b; }
20     bool operator!=(const Seg &oth) { return !operator==(oth); }
21 };
22 llorient(Vec a, Vec b, Vec c{
23     return (ll)a.x * (b.y - c.y) + (ll)b.x * (c.y - a.y) +
24         (ll)c.x * (a.y - b.y);
25 }
26 boolin_c_circle(Vec *arr, Vec d{
27     if (cross(arr[1] - arr[0], arr[2] - arr[0]) == 0)
28         return true; // degenerate
29     ll m[3][3];
30     ran(i, 0, 3)
31         m[i][0] = arr[i].x - d.x;
32         m[i][1] = arr[i].y - d.y;
33         m[i][2] = m[i][0] * m[i][0];
34         m[i][2] += m[i][1] * m[i][1];
35 }
36 __int128 res = 0;
37 res += (__int128)(m[0][0] * m[1][1] - m[0][1] * m[1][0]) * m[2][2];
38 res += (__int128)(m[1][0] * m[2][1] - m[1][1] * m[2][0]) * m[0][2];
39 res -= (__int128)(m[0][0] * m[2][1] - m[0][1] * m[2][0]) * m[1][2];
40 return res > 0
41 }
42 Edge add_triangle(Edge *a, Edge *b, Edge *c{
43     Edge *old[] = {a, b, c};
44     Edge *tmp = new Edge[3];
45     ran(i, 0, 3) {
46         old[i]->rep = tmp + i
47         tmp[i] = {old[i]->tar, tmp + (i + 1) % 3, old[i]->inv};
48         if (tmp[i].inv) tmp[i].inv->inv = tmp + i;
49     }
50     return tmp;
51 }
52 Edge add_point(Vec p, Edge *cur{ // returns outgoing edge
53     Edge *triangle[] = {cur, cur->nxt, cur->nxt->nxt};
54     ran(i, 0, 3) {
55         if (orient(triangle[i]->tar, triangle[(i + 1) % 3]->tar, p) < 0)
56             return NULL
57     }
58     ran(i, 0, 3) {
59         if (triangle[i]->rep) {
60             Edge *res = add_point(p, triangle[i]->rep);
61             if (res
62                 return res; // unless we are on last layer we must exit here
63     }
64 }
65 Edge p_as_e{p};
66 Edge tmp{cur->tar}
67 tmp.inv = add_triangle(&p_as_e, &tmp, cur = cur->nxt);
68 Edge *res = tmp.inv->nxt;
69 tmp.tar = cur->tar;
70 tmp.inv = add_triangle(&p_as_e, &tmp, cur = cur->nxt);
71 tmp.tar = cur->tar
72 res->inv = add_triangle(&p_as_e, &tmp, cur = cur->nxt);
73 res->inv->inv = res;
74 return res;
75 }
76 Edge *delaunay(vector<Vec> &points)
77     random_shuffle(points.begin(), points.end());
78     Vec arr[] = {{4 * max_co, 4 * max_co}, {-4 * max_co, max_co},
79         {max_co, -4 * max_co}};
80     Edge *res = new Edge[3];
81     ran(i, 0, 3) res[i] = {arr[i], res + (i + 1) % 3}
82     for (Vec &cur : points) {
83         Edge *loc = add_point(cur, res);
84         Edge *out = loc;
85         arr[0] = cur;
86         while (true)
87             arr[1] = out->tar;
88             arr[2] = out->nxt->tar;
89             Edge *e = out->nxt->inv;
90             if (e && in_c_circle(arr, e->nxt->tar)) {
91                 Edge tmp{cur}
92                 tmp.inv = add_triangle(&tmp, out, e->nxt);
93                 tmp.tar = e->nxt->tar;
94                 tmp.inv->inv = add_triangle(&tmp, e->nxt->nxt, out->nxt->nxt);
95                 out = tmp.inv->nxt;
96                 continue
97             }
98             out = out->nxt->nxt->inv;
99             if (out->tar == loc->tar) break;
100     }
101     return res;
102 }
103 void extract_triangles(Edge *cur, vector<vector<Seg> > &res{
104     if (!cur->vis) {
105         bool inc = true;
106         Edge *it = cur;
107         do
108             it->vis = true;
109             if (it->rep) {
110                 extract_triangles(it->rep, res);
111                 inc = false;
112             }
113         while (it = it->nxt;

```



```

115 } while (it != cur);
116 if (inc) {
117     Edge *triangle[3] = {cur, cur->nxt, cur->nxt->nxt};
118     res.resize(res.size() + 1)
119     vector<Seg> &tar = res.back();
120     ran(i, 0, 3) {
121         if ((abs(triangle[i]->tar.x) < max_co &&
122             abs(triangle[(i + 1) % 3]->tar.x) < max_co))
123             tar.push_back
124             {triangle[i]->tar, triangle[(i + 1) % 3]->tar});
125     }
126     if (tar.empty()) res.pop_back();
127 }
128

```

#207

#011

#602

10 Aho Corasick $O(|\alpha| \sum \text{len})$

```

1 const int alpha_size = 26;
2 struct Node {
3     Node *nxt[alpha_size]; // May use other structures to move in trie
4     Node *suffix;
5     Node() { memset(nxt, 0, alpha_size * sizeof(Node *));
6     int cnt = 0;
7 };
8 Node aho_corasick(vector<vector<char> > &dict{
9     Node *root = new Node;
10    root->suffix = 0
11    vector<pair<vector<char> *, Node *> > state;
12    for (vector<char> &s : dict) state.emplace_back(&s, root);
13    for (int i = 0; !state.empty(); ++i) {
14        vector<pair<vector<char> *, Node *> > nstate;
15        for (auto &cur : state)
16            Node *nxt = cur.second->nxt[(cur.first)[i]];
17            if (nxt) {
18                cur.second = nxt;
19            } else {
20                nxt = new Node
21                cur.second->nxt[(cur.first)[i]] = nxt;
22                Node *suf = cur.second->suffix;
23                cur.second = nxt;
24                nxt->suffix = root; // set correct suffix link
25                while (suf)
26                    if (suf->nxt[(cur.first)[i]]) {
27                        nxt->suffix = suf->nxt[(cur.first)[i]];
28                        break;
29                    }
30                suf = suf->suffix
31            }
32        }
33        if (cur.first->size() > i + 1) nstate.push_back(cur);
34    }
35    state = nstate
36 }

```

#248

#292

#306

#266

#249

#562

#417

```

37 return root;
38 //882 // auxiliary functions for searhing and counting
39 Node walk(Node *cur,
40     char c{// longest prefix in dict that is suffix of walked string.
41     while (true) {
42         if (cur->nxt[c]) return cur->nxt[c];
43         if (!cur->suffix) return cur
44         cur = cur->suffix;
45     }
46
47 void cnt_matches(Node *root, vector<char> &match_in{
48     Node *cur = root;
49     for (char c : match_in) {
50         cur = walk(cur, c);
51         ++cur->cnt
52     }
53
54 void add_cnt(Node *root{// After counting matches propagete ONCE to
55     // suffixes for final counts
56     vector<Node *> to_visit = {root};
57     ran(i, 0, to_visit.size()) {
58         Node *cur = to_visit[i];
59         ran(j, 0, alpha_size)
60             if (cur->nxt[j]) to_visit.push_back(cur->nxt[j]);
61     }
62 }
63 for (int i = to_visit.size() - 1; i > 0; --i)
64     to_visit[i]->suffix->cnt += to_visit[i]->cnt
65
66 int main({
67     int n, len;
68     scanf("%d %d", &len, &n);
69     vector<char> a(len + 1);
70     scanf("%s", a.data());
71     a.pop_back();
72     for (char &c : a) c -= 'a';
73     vector<vector<char> > dict(n);
74     ran(i, 0, n) {
75         scanf("%d", &len);
76         dict[i].resize(len + 1);
77         scanf("%s", dict[i].data());
78         dict[i].pop_back();
79         for (char &c : dict[i]) c -= 'a';
80     }
81     Node *root = aho_corasick(dict);
82     cnt_matches(root, a);
83     add_cnt(root);
84     ran(i, 0, n) {
85         Node *cur = root;
86         for (char c : dict[i]) cur = walk(cur, c);
87         printf("%d\n", cur->cnt);

```

#414

#529

#015

#156

#662

#950

#488

88 }

11 Suffix automaton and tree $O((n + q) \log(|\alpha|))$

```

1 class Node {
2     private:
3         map<char, Node *>
4         nxt_char; // Map is faster than hashtable and unsorted arrays
5     public
6         int len; // Length of longest suffix in equivalence class.
7         Node *suf;
8         bool has_nxt(char c) const { return nxt_char.count(c); }
9         Node nxt(char c {
10             if (!has_nxt(c)) return NULL
11             return nxt_char[c];
12         }
13         void set_nxt(char c, Node *node { nxt_char[c] = node; }
14         Node split(int new_len, char c {
15             Node *new_n = new Node
16             new_n->nxt_char = nxt_char;
17             new_n->len = new_len;
18             new_n->suf = suf;
19             suf = new_n;
20             return new_n
21         }
22         // Extra functions for matching and counting
23         Node lower_depth(int depth { // move to longest suffix of current
24                                     // with a maximum length of depth.
25             if (suf->len >= depth) return suf->lower_depth(depth);
26             return this;
27         }
28         Node *walk(char c, int depth
29                   int &match_len) { // move to longest suffix of walked path that is
30                                     // a substring
31             match_len = min(match_len,
32                             len); // includes depth limit (needed for finding matches)
33             if (has_nxt(c)) { // as suffixes are in classes match_len must be
34                             // tracked externally
35                 ++match_len
36                 return nxt(c->lower_depth(depth);
37             }
38             if (suf) return suf->walk(c, depth, match_len);
39             return this;
40         }
41         int paths_to_end = 0;
42         void set_as_end({ // All suffixes of current node are marked as
43                         // ending nodes.
44             paths_to_end += 1;
45             if (suf) suf->set_as_end();
46         }
47         bool vis = false;
48         void calc_paths_to_end({ // Call ONCE from ROOT. For each node
49                                // calculates number of ways to reach an

```

```

50                                     // end node.
51         if (!vis) { // paths_to_end is occurrence count for any strings in
52                     // current suffix equivalence class.
53             vis = true;
54             for (auto cur : nxt_char)
55                 cur.second->calc_paths_to_end();
56             paths_to_end += cur.second->paths_to_end;
57         }
58     }
59 }
60 // Transform into suffix tree of reverse string
61 map<char, Node *> tree_links;
62 int end_dist = 1 << 30;
63 int calc_end_dist({
64     if (end_dist == 1 << 30) {
65         if (nxt_char.empty()) end_dist = 0
66         for (auto cur : nxt_char)
67             end_dist = min(end_dist, 1 + cur.second->calc_end_dist());
68     }
69     return end_dist;
70 }
71 bool vis_t = false;
72 void build_suffix_tree(string &s { // Call ONCE from ROOT.
73     if (!vis_t) {
74         vis_t = true;
75         if (suf
76             suf->tree_links[s[s.size() - end_dist - suf->len - 1]] = this;
77         for (auto cur : nxt_char) cur.second->build_suffix_tree(s);
78     }
79 }
80 }
81 struct SufAuto {
82     Node *last;
83     Node *root;
84     void extend(char new_c {
85         Node *new_end = new Node
86         new_end->len = last->len + 1;
87         Node *suf_w_nxt = last;
88         while (suf_w_nxt && !suf_w_nxt->has_nxt(new_c)) {
89             suf_w_nxt->set_nxt(new_c, new_end);
90             suf_w_nxt = suf_w_nxt->suf
91         }
92         if (!suf_w_nxt) {
93             new_end->suf = root;
94         } else {
95             Node *max_sbstr = suf_w_nxt->nxt(new_c)
96             if (suf_w_nxt->len + 1 == max_sbstr->len) {
97                 new_end->suf = max_sbstr;
98             } else {
99                 Node *eq_sbstr = max_sbstr->split(suf_w_nxt->len + 1, new_c);
100                 new_end->suf = eq_sbstr

```

```

101     Node *w_edge_to_eq_sbstr = suf_w_nxt;
102     while (w_edge_to_eq_sbstr != 0 &&
103            w_edge_to_eq_sbstr->nxt(new_c) == max_sbstr) {
104         w_edge_to_eq_sbstr->set_nxt(new_c, eq_sbstr);
105         w_edge_to_eq_sbstr = w_edge_to_eq_sbstr->suf #678
106     }
107 }
108 }
109 last = new_end;
110
111 SufAuto(string &s) {
112     root = new Node;
113     root->len = 0;
114     root->suf = NULL;
115     last = root #604
116     for (char c : s) extend(c);
117     root->calc_end_dist(); // To build suffix tree use reversed string
118     root->build_suffix_tree(s);
119 }

```

12 Dinic

```

1 struct MaxFlow {
2     typedef long long ll;
3     const ll INF = 1e18;
4     struct Edge {
5         int u, v #295
6         ll c, rc;
7         shared_ptr<ll> flow;
8         Edge(int _u, int _v, ll _c, ll _rc = 0)
9             : u(_u), v(_v), c(_c), rc(_rc) {} #787
10    }
11    struct FlowTracker {
12        shared_ptr<ll> flow;
13        ll cap, rcap;
14        bool dir;
15        FlowTracker(ll _cap, ll _rcap, shared_ptr<ll> _flow, int _dir #418
16            : cap(_cap), rcap(_rcap), flow(_flow), dir(_dir) {}
17        ll rem() const {
18            if (dir == 0) {
19                return cap - *flow;
20            } else #844
21                return rcap + *flow;
22        }
23    }
24    void add_flow(ll f) {
25        if (dir == 0 #920
26            *flow += f;
27        else
28            *flow -= f;
29        assert(*flow <= cap);
30        assert(*flow <= rcap) #287

```

```

31    }
32    operator ll() const { return rem(); }
33    void operator--(ll x) { add_flow(x); }
34    void operator+=(ll x) { add_flow(-x); } #789
35 }
36 int source, sink;
37 vector<vector<int>> > adj;
38 vector<vector<FlowTracker>> > cap;
39 vector<Edge> edges;
40 MaxFlow(int _source, int _sink) : source(_source), sink(_sink) #080
41     ↪ assert(source != sink);
42 }
43 int add_edge(int u, int v, ll c, ll rc = 0) {
44     edges.push_back(Edge(u, v, c, rc));
45     return edges.size() - 1 #659
46 }
47 vector<int> now, lvl;
48 void prep({
49     int max_id = max(source, sink);
50     for (auto edge : edges) max_id = max(max_id, max(edge.u, edge.v))
51     ↪ #638
52     adj.resize(max_id + 1);
53     cap.resize(max_id + 1);
54     now.resize(max_id + 1);
55     lvl.resize(max_id + 1);
56     for (auto &edge : edges) #604
57         auto flow = make_shared<ll>(0);
58         adj[edge.u].push_back(edge.v);
59         cap[edge.u].push_back(FlowTracker(edge.c, edge.rc, flow, 0));
60         if (edge.u != edge.v) { #789
61             adj[edge.v].push_back(edge.u) #789
62             cap[edge.v].push_back(FlowTracker(edge.c, edge.rc, flow, 1));
63         }
64         assert(cap[edge.u].back() == edge.c);
65         edge.flow = flow; #131
66     }
67 bool dinic_bfs({
68     fill(now.begin(), now.end(), 0);
69     fill(lvl.begin(), lvl.end(), 0); #448
70     lvl[source] = 1
71     vector<int> bfs(1, source);
72     for (int i = 0; i < bfs.size(); ++i) {
73         int u = bfs[i];
74         for (int j = 0; j < adj[u].size(); ++j) {
75             int v = adj[u][j] #227
76             if (cap[u][j] > 0 && lvl[v] == 0) {
77                 lvl[v] = lvl[u] + 1;
78                 bfs.push_back(v);
79             }

```

```

80     }
81     }
82     return lvl[sink] > 0;
83 }
84 lldinic_dfs(int u, ll flow{
85     if (u == sink) return flow
86     while (now[u] < adj[u].size()) {
87         int v = adj[u][now[u]];
88         if (lvl[v] == lvl[u] + 1 && cap[u][now[u]] != 0) {
89             ll res = dinic_dfs(v, min(flow, (ll)cap[u][now[u]]));
90             if (res > 0)
91                 cap[u][now[u]] -= res;
92             return res;
93         }
94     }
95     ++now[u]
96 }
97 return 0;
98 }
99 llcalc_max_flow({
100     prep()
101     ll ans = 0;
102     while (dinic_bfs()) {
103         ll cur = 0;
104         do {
105             cur = dinic_dfs(source, INF)
106             ans += cur;
107         } while (cur > 0);
108     }
109     return ans;
110 }
111 llflow_on_edge(int edge_index{
112     assert(edge_index < edges.size());
113     return *edges[edge_index].flow;
114 }
115 }
116 intmain({
117     int n, m;
118     cin >> n >> m;
119     auto mf = MaxFlow(
120         1, n); // arguments source and sink, memory usage O(largest node
121                // index + input size), sink doesn't need to be last index
122     int edge_index;
123     for (int i = 0; i < m; ++i) {
124         int a, b, c;
125         cin >> a >> b >> c;
126         // mf.add_edge(a,b,c); // for directed edges
127         edge_index = mf.add_edge(
128             a, b, c, c); // store edge index if care about flow value
129     }
130     cout << mf.calc_max_flow() << '\n';
131     // cout << mf.flow_on_edge(edge_index) << endl; // return flow on

```

#722

#725

#459

#460

#054

#052

#346

%583

132 // this edge

13 Min Cost Max Flow with successive dijkstra $O(\text{flow} \cdot n^2)$

```

1 const int nmax = 1055;
2 const ll inf = 1e14;
3 int t, n, v; // 0 is source, v-1 sink
4 ll rem_flow[nmax][nmax]; // set [x][y] for directed capacity from x to
   ↪ y.
5 ll cost[nmax][nmax]; // set [x][y] for directed cost from x to y.
   ↪ SET #497
6 // TO inf IF NOT USED
7 ll min_dist[nmax];
8 int prev_node[nmax];
9 ll node_flow[nmax];
10 bool visited[nmax] %576
11 ll tot_cost, tot_flow; // output
12 voidmin_cost_max_flow({
13     tot_cost = 0; // Does not work with negative cycles.
14     tot_flow = 0;
15     ll sink_pot = 0 #614
16     min_dist[0] = 0 %927
17     for (int i = 1; i <= v; ++i) { // incase of no negative edges
18                                     // Bellman-Ford can be removed.
19         min_dist[i] = inf;
20     }
21     for (int i = 0; i < v - 1; ++i) {
22         for (int j = 0; j < v; ++j) #654
23             for (int k = 0; k < v; ++k) {
24                 if (rem_flow[j][k] > 0 &&
25                     min_dist[j] + cost[j][k] < min_dist[k])
26                     min_dist[k] = min_dist[j] + cost[j][k];
27             }
28         }
29     }
30     for (int i = 0; i < v; ++i) { // Apply potentials to edge costs.
31         for (int j = 0; j < v; ++j) {
32             if (cost[i][j] != inf) #037
33                 cost[i][j] += min_dist[i];
34                 cost[i][j] -= min_dist[j];
35             }
36         }
37     }
38     sink_pot += min_dist[v - 1]; // Bellman-Ford end. %849
39     while (true) {
40         for (int i = 0; i <= v; ++i) { // node after sink is used as start
41                                     // value for Dijkstra.
42             min_dist[i] = inf;
43             visited[i] = false;
44         }
45         min_dist[0] = 0;
46         node_flow[0] = inf;

```

#497

%576

#614

%927

#654

#040

#037

#630

%849

#827

```

47 int min_node;
48 while (true) {// Use Dijkstra to calculate potentials
49     int min_node = v
50     for (int i = 0; i < v; ++i) {
51         if ((!visited[i]) && min_dist[i] < min_dist[min_node])
52             min_node = i;
53     }
54     if (min_node == v) break visited[min_node] = true
55     for (int i = 0; i < v; ++i) {
56         if ((!visited[i]) &&
57             min_dist[min_node] + cost[min_node][i] < min_dist[i]) {
58             min_dist[i] = min_dist[min_node] + cost[min_node][i];
59             prev_node[i] = min_node
60             node_flow[i] =
61                 min(node_flow[min_node], rem_flow[min_node][i]);
62         }
63     }
64
65     if (min_dist[v - 1] == inf)
66         break for (int i = 0; i < v;
67             ++i) {// Apply potentials to edge costs.
68             for (int j = 0; j < v;
69                 ++j) {// Found path from source to sink becomes 0
70                 cost.
71                 if (cost[i][j] != inf) {
72                     cost[i][j] += min_dist[i];
73                     cost[i][j] -= min_dist[j];
74                 }
75             }
76             sink_pot += min_dist[v - 1];
77             tot_flow += node_flow[v - 1];
78             tot_cost += sink_pot * node_flow[v - 1];
79             int cur = v - 1
80             while (cur != 0) {
81                 // Backtrack along found path that now has 0 cost.
82                 rem_flow[prev_node[cur]][cur] -= node_flow[v - 1];
83                 rem_flow[cur][prev_node[cur]] += node_flow[v - 1];
84                 cost[cur][prev_node[cur]] = 0;
85                 if (rem_flow[prev_node[cur]][cur] == 0
86                     cost[prev_node[cur]][cur] = inf;
87                 cur = prev_node[cur];
88             }
89         }
90
91 intmain({// http://www.spoj.com/problems/GREED/
92     cin >> t;
93     for (int i = 0; i < t; ++i) {
94         cin >> n;
95         for (int j = 0; j < nmax; ++j) {
96             for (int k = 0; k < nmax; ++k) {
97                 cost[j][k] = inf;

```

#782

#281

#881

#046

#664

#983

#946

#446

%803

```

98     rem_flow[j][k] = 0;
99 }
100 }
101 for (int j = 1; j <= n; ++j) {
102     cost[j][2 * n + 1] = 0;
103     rem_flow[j][2 * n + 1] = 1;
104 }
105 for (int j = 1; j <= n; ++j) {
106     int card;
107     cin >> card;
108     ++rem_flow[0][card];
109     cost[0][card] = 0;
110 }
111 int ex_c;
112 cin >> ex_c;
113 for (int j = 0; j < ex_c; ++j) {
114     int a, b;
115     cin >> a >> b;
116     if (b < a) swap(a, b);
117     cost[a][b] = 1;
118     rem_flow[a][b] = nmax;
119     cost[b][n + b] = 0;
120     rem_flow[b][n + b] = nmax;
121     cost[n + b][a] = 1;
122     rem_flow[n + b][a] = nmax;
123 }
124 v = 2 * n + 2;
125 min_cost_max_flow();
126 cout << tot_cost << '\n';
127 }

```

14 Min Cost Max Flow with Cycle Cancelling $\mathcal{O}(\text{flow} \cdot nm)$

```

1 struct Network {
2     struct Node;
3     struct Edge {
4         Node *u, *v;
5         int f, c, cost
6         Node*from(Node* pos{
7             if (pos == u) return v;
8             return u;
9         }
10        intgetCap(Node* pos
11            if (pos == u) return c - f;
12            return f;
13        }
14        int addFlow(Node* pos, int toAdd) {
15            if (pos == u)
16                f += toAdd;
17                return toAdd * cost;
18            } else {
19                f -= toAdd;

```

#965

#145

#369

```

20     return -toAdd * cost; #987
21 }
22 }
23 };
24 struct Node {
25     vector<Edge*> conn; #577
26     int index;
27 };
28 deque<Node> nodes;
29 deque<Edge> edges;
30 Node*addNode( #057
31     nodes.push_back(Node());
32     nodes.back().index = nodes.size() - 1;
33     return &nodes.back();
34 }
35 Edge*addEdge(Node* u, Node* v, int f, int c, int cost #518
36     edges.push_back({u, v, f, c, cost});
37     u->conn.push_back(&edges.back());
38     v->conn.push_back(&edges.back());
39     return &edges.back();
40
41 // Assumes all needed flow has already been added #692
42 intminCostMaxFlow({
43     int n = nodes.size();
44     int result = 0;
45     struct State {
46         int p; #091
47         Edge* used;
48     };
49     while (1) {
50         vector<vector<State>> state(1, vector<State>(n, {0, 0})); #158
51         for (int lev = 0; lev < n; lev++)
52             state.push_back(state[lev]);
53         for (int i = 0; i < n; i++) {
54             if (lev == 0 || state[lev][i].p < state[lev - 1][i].p) {
55                 for (Edge* edge : nodes[i].conn) {
56                     if (edge->getCap(&nodes[i]) > 0) #760
57                         int np =
58                             state[lev][i].p +
59                             (edge->u == &nodes[i] ? edge->cost : -edge->cost);
60                     int ni = edge->from(&nodes[i])->index;
61                     if (np < state[lev + 1][ni].p) #281
62                         state[lev + 1][ni].p = np;
63                     state[lev + 1][ni].used = edge;
64                 }
65             }
66         } #460
67     }
68 }
69 }
70 // Now look at the last level
71 bool valid = false;

```

```

72 for (int i = 0; i < n; i++) #283
73     if (state[n - 1][i].p > state[n][i].p) {
74         valid = true;
75         vector<Edge*> path;
76         int cap = 1000000000;
77         Node* cur = &nodes[i] #352
78         int clef = n;
79         vector<bool> explr(n, false);
80         while (!explr[cur->index]) {
81             explr[cur->index] = true;
82             State cstate = state[clef][cur->index] #954
83             cur = cstate.used->from(cur);
84             path.push_back(cstate.used);
85         }
86         reverse(path.begin(), path.end()); #592
87
88         int i = 0;
89         Node* cur2 = cur;
90         do {
91             cur2 = path[i]->from(cur2);
92             i++; #990
93         } while (cur2 != cur);
94         path.resize(i);
95     }
96     for (auto edge : path) {
97         cap = min(cap, edge->getCap(cur)) #297
98         cur = edge->from(cur);
99     }
100     for (auto edge : path) {
101         result += edge->addFlow(cur, cap);
102         cur = edge->from(cur) #599
103     }
104 }
105 if (!valid) break;
106 }
107 return result #550
108 }

```

15 DMST $\mathcal{O}(E \log V)$

```

1 struct EdgeDesc {
2     int from, to, w;
3 };
4 struct DMST {
5     struct Node #091
6     struct Edge {
7         Node *from;
8         Node *tar;
9         int w;
10        bool inc #186
11    };
12    struct Circle {

```


13	bool vis = false;		
14	vector<Edge *> contents;		
15	voidclean(int idx	#946	
16	};		
17	const static greater<pair<ll, Edge *> >		
18	comp; <i>// Can use inline static since C++17</i>		
19	static vector<Circle> to_process;		
20	static bool no_dmst	#478	
21	static Node *root;		
22	struct Node {		
23	Node *par = NULL;		
24	vector<pair<int, int> > out_cands; <i>// Circ, edge idx</i>		
25	vector<pair<ll, Edge *> > con	#608	
26	bool in_use = false;		
27	ll w = 0; <i>// extra to add to edges in con</i>		
28	Nodeanc({		
29	if (!par return thi;		
30	while (par->par) par = par->par	#721	
31	return par;		
32	}		
33	voidclean({		
34	if (!no_dmst) {		
35	in_use = false	#465	
36	for (auto &cur : out_cands)		
37	to_process[cur.first].clean(cur.second);		
38	}		
39	}		
40	Node con_to_root(#488	
41	if (anc() == root) return root;		
42	in_use = true;		
43	Node *super = this; <i>// Will become root or the first Node</i>		
44	<i>// encountered in a loop.</i>		
45	while (super == this) {		
46	while	#363	
47	!con.empty() && con.front().second->tar->anc() == anc()) {		
48	pop_heap(con.begin(), con.end(), comp);		
49	con.pop_back();		
50	}		
51	if (con.empty())	#506	
52	no_dmst = true;		
53	return root;		
54	}		
55	pop_heap(con.begin(), con.end(), comp);		
56	auto nxt = con.back()	#541	
57	con.pop_back();		
58	w = -nxt.first;		
59	if (nxt.second->tar		
60	->in_use) <i>// anc() wouldn't change anything</i>	#174	
61	super = nxt.second->tar->anc()		
62	to_process.resize(to_process.size() + 1);		
63	} else {		
64	super = nxt.second->tar->con_to_root();		
65	}		
66	if (super != root)	#595	
67	to_process.back().contents.push_back(nxt.second);		
68	out_cands.emplace_back(to_process.size() - 1,		
69	to_process.back().contents.size() - 1);		
70	} else <i>// Clean circles</i>	#848	
71	nxt.second->inc = true		
72	nxt.second->from->clean();		
73	}		
74	}		
75	if (super != root) <i>// we are some loops non first Node.</i>		
76	if (con.size() > super->con.size())	#860	
77	swap(con,		
78	super->con); <i>// Largest con in loop should not be copied.</i>		
79	swap(w, super->w);		
80	}		
81	for (auto cur : con)	#064	
82	super->con.emplace_back(
83	cur.first - super->w + w, cur.second);		
84	push_heap(super->con.begin(), super->con.end(), comp);		
85	}		
86		#295	
87	par = super; <i>// root or anc() of first Node encountered in a</i>		
88	<i>// loop</i>		
89	return super;		
90	}		
91	};		
92	Node *cur_root	#995	
93	vector<Node> graph;		
94	vector<Edge> edges;		
95	DMST(int n, vector<EdgeDesc> &desc,		
96	int r) <i>// Self loops and multiple edges are okay.</i>	#989	
97	graph.resize(n)		
98	cur_root = &graph[r];		
99	for (auto &cur : desc) <i>// Edges are reversed internally</i>		
100	edges.push_back(Edge{&graph[cur.to], &graph[cur.from], cur.w});		
101	for (int i = 0; i < desc.size(); ++i)		
102	graph[desc[i].to].con.emplace_back(desc[i].w, &edges[i])	#895	
103	for (int i = 0; i < n; ++i)		
104	make_heap(graph[i].con.begin(), graph[i].con.end(), comp);		
105	}		
106	bool find() {		
107	root = cur_root	#771	
108	no_dmst = false;		
109	for (auto &cur : graph) {		
110	cur.con_to_root();		
111	to_process.clear();		
112	if (no_dmst) return false	#405	
113	}		
114	return true;		
115		%732	

```

116 llweight({
117     ll res = 0;
118     for (auto &cur : edges) {
119         if (cur.inc) res += cur.w;
120     }
121     return res;
122 };
123 };
124 void DMST::Circle::clean(int idx) {
125     if (!vis) {
126         vis = true;
127         for (int i = 0; i < contents.size(); ++i)
128             if (i != idx) {
129                 contents[i]->inc = true;
130                 contents[i]->from->clean();
131             }
132     }
133 }
134 }
135 const greater<pair<ll, DMST::Edge *> > DMST::comp;
136 vector<DMST::Circle> DMST::to_process;
137 bool DMST::no_dmst

```

16 Bridges $\mathcal{O}(n)$

```

1 struct vert;
2 struct edge {
3     bool exists = true;
4     vert *dest;
5     edge *rev
6     edge(vert *_dest) : dest(_dest) { rev = NULL; }
7     vert &operator*() { return *dest; }
8     vert *operator->() { return dest; }
9     bool is_bridge();
10 }
11 struct vert {
12     deque<edge> con;
13     int val = 0;
14     int seen;
15     intdfs(int upd, edge *ban{// handles multiple edges
16         if (!val) {
17             val = upd;
18             seen = val;
19             for (edge &nxt : con) {
20                 if (nxt.exists && (&nxt) != ban
21                     seen = min(seen, nxt->dfs(upd + 1, nxt.rev));
22             }
23         }
24         return seen;
25     }
26     voidremove_adj_bridges({
27         for (edge &nxt : con) {
28             if (nxt.is_bridge()) nxt.exists = false;

```

```

29     }
30 }
31 intcnt_adj_bridges({
32     int res = 0;
33     for (edge &nxt : con) res += nxt.is_bridge();
34     return res;
35 };
36 };
37 bool edge::is_bridge() {
38     return exists &&
39         (dest->seen > rev->dest->val || dest->val < rev->dest->seen);
40 }
41 vert graph[nmax];
42 intmain({// Mechanics Practice BRIDGES
43     int n, m;
44     cin >> n >> m;
45     for (int i = 0; i < m; ++i) {
46         int u, v;
47         scanf("%d %d", &u, &v);
48         graph[u].con.emplace_back(graph + v);
49         graph[v].con.emplace_back(graph + u);
50         graph[u].con.back().rev = &graph[v].con.back();
51         graph[v].con.back().rev = &graph[u].con.back();
52     }
53     graph[1].dfs(1, NULL);
54     int res = 0;
55     for (int i = 1; i <= n; ++i) res += graph[i].cnt_adj_bridges();
56     cout << res / 2 << endl;

```

17 2-Sat $\mathcal{O}(n)$ and SCC $\mathcal{O}(n)$

```

1 struct Graph {
2     int n;
3     vector<vector<int> > conn;
4     Graph(int nsize) {
5         n = nsize
6         conn.resize(n);
7     }
8     void add_edge(int u, int v) { conn[u].push_back(v); }
9     void _topsort_dfs(int pos, vector<int> &result, vector<bool> &explr,
10         vector<vector<int> > &revconn)
11         if (explr[pos]) return;
12         explr[pos] = true;
13         for (auto next : revconn[pos])
14             _topsort_dfs(next, result, explr, revconn);
15         result.push_back(pos)
16     }
17     vector<int> topsort() {
18         vector<vector<int> > revconn(n);
19         for (int u = 0; u < n; u++) {
20             for (auto v : conn[u]) revconn[v].push_back(u)
21         }
22         vector<int> result;

```

```

23     vector<bool> explr(n, false);
24     for (int i = 0; i < n; i++)
25         _topsort_dfs(i, result, explr, revconn)
26     reverse(result.begin(), result.end());
27     return result;
28 }
29 void dfs(int pos, vector<int> &result, vector<bool> &explr) {
30     if (explr[pos]) return
31     explr[pos] = true;
32     for (auto next : conn[pos]) dfs(next, result, explr);
33     result.push_back(pos);
34 }
35 vector<vector<int> > scc() {
36     vector<int> order = topsort();
37     reverse(order.begin(), order.end());
38     vector<bool> explr(n, false);
39     vector<vector<int> > results
40     for (auto it = order.rbegin(); it != order.rend(); ++it) {
41         vector<int> component;
42         _topsort_dfs(*it, component, explr, conn);
43         sort(component.begin(), component.end());
44         results.push_back(component)
45     }
46     sort(results.begin(), results.end());
47     return results;
48 }
49 }                                     %983 // Solution for:
50 // http://codeforces.com/group/PjzGiggT71/contest/221700/problem/C
51 int main() {
52     int n, m;
53     cin >> n >> m;
54     Graphg(2 * m;
55     for (int i = 0; i < n; i++) {
56         int a, sa, b, sb;
57         cin >> a >> sa >> b >> sb;
58         a--, b--;
59         g.add_edge(2 * a + 1 - sa, 2 * b + sb);
60         g.add_edge(2 * b + 1 - sb, 2 * a + sa);
61     }
62     vector<int> state(2 * m, 0);
63     {
64         vector<int> order = g.topsort();
65         vector<bool> explr(2 * m, false);
66         for (auto u : order) {
67             vector<int> traversed;
68             g.dfs(u, traversed, explr);
69             if (traversed.size() > 0 && !state[traversed[0] ^ 1]) {
70                 for (auto c : traversed) state[c] = 1;
71             }
72         }
73     }

```

#178

#591

%603

#020

#741

```

74     for (int i = 0; i < m; i++) {
75         if (state[2 * i] == state[2 * i + 1]) {
76             cout << "IMPOSSIBLE\n";
77             return 0;
78         }
79     }
80     for (int i = 0; i < m; i++) {
81         cout << state[2 * i + 1] << '\n';
82     }
83     return 0;

```

18 Generic persistent compressed lazy segment tree

```

1 struct Seg {
2     ll sum = 0;
3     void recalc(const Seg &lhs_seg, int lhs_len, const Seg &rhs_seg,
4         int rhs_len {
5         sum = lhs_seg.sum + rhs_seg.sum
6     }
7 } __attribute__((packed));
8 struct Lazy {
9     ll add;
10    ll assign_val; // LLONG_MIN if no assign;
11    void init() {
12        add = 0;
13        assign_val = LLONG_MIN;
14    }
15    Lazy() { init();
16    void split(Lazy &lhs_lazy, Lazy &rhs_lazy, int len {
17        lhs_lazy = *this;
18        rhs_lazy = *this;
19        init();
20    }
21    void merge(Lazy &oth, int len {
22        if (oth.assign_val != LLONG_MIN) {
23            add = 0;
24            assign_val = oth.assign_val;
25        }
26        add += oth.add;
27    }
28    void apply_to_seg(Seg &cur, int len) const {
29        if (assign_val != LLONG_MIN) {
30            cur.sum = len * assign_val
31        }
32        cur.sum += len * add;
33    }
34 } __attribute__((packed))
35 struct Node { // Following code should not need to be modified
36     int ver;
37     bool is_lazy = false;
38     Seg seg;
39     Lazy lazy
40     Node *lc = NULL, *rc = NULL;

```

#684

#529

#819

#953

#949

#204

%625

#321

```

41 voidinit({
42     if (!lc) {
43         lc = new Node{ver};
44         rc = new Node{ver}
45     }
46 }
47 Node upd(int L, int R, int l, int r, Lazy &val, int tar_ver{
48     if (ver != tar_ver) {
49         Node *rep = new Node(*this)
50         rep->ver = tar_ver;
51         return rep->upd(L, R, l, r, val, tar_ver);
52     }
53     if (L >= l && R <= r) {
54         val.apply_to_seg(seg, R - L)
55         lazy.merge(val, R - L);
56         is_lazy = true;
57     } else {
58         init();
59         int M = (L + R) / 2
60         if (is_lazy) {
61             Lazy l_val, r_val;
62             lazy.split(l_val, r_val, R - L);
63             lc = lc->upd(L, M, L, M, l_val, ver);
64             rc = rc->upd(M, R, M, R, r_val, ver)
65             is_lazy = false;
66         }
67         Lazy l_val, r_val;
68         val.split(l_val, r_val, R - L);
69         if (l < M) lc = lc->upd(L, M, l, r, l_val, ver)
70         if (M < r) rc = rc->upd(M, R, l, r, r_val, ver);
71         seg.recalc(lc->seg, M - L, rc->seg, R - M);
72     }
73     return this;
74 }
75 voidget(int L, int R, int l, int r, Seg *&lft_res, Seg *&tmp,
76     bool last_ver{
77     if (L >= l && R <= r) {
78         tmp->recalc(*lft_res, L - l, seg, R - L);
79         swap(lft_res, tmp)
80     } else {
81         init();
82         int M = (L + R) / 2;
83         if (is_lazy) {
84             Lazy l_val, r_val
85             lazy.split(l_val, r_val, R - L);
86             lc = lc->upd(L, M, L, M, l_val, ver + last_ver);
87             lc->ver = ver;
88             rc = rc->upd(M, R, M, R, r_val, ver + last_ver);
89             rc->ver = ver
90             is_lazy = false;
91         }
92         if (l < M) lc->get(L, M, l, r, lft_res, tmp, last_ver);

```

```

93         if (M < r) rc->get(M, R, l, r, lft_res, tmp, last_ver);
94     }
95 }
#313 } __attribute__((packed));
96 }
97 struct SegTree { // indexes start from 0, ranges are [beg, end)
98     vector<Node *> roots; // versions start from 0
99     int len
#873 SegTree(int len) : len(len) { roots.push_back(new Node{0}); }
100 int upd(int l, int r, Lazy &val, bool new_ver = false) {
101     Node *cur_root =
102         roots.back()->upd(0, len, l, r, val, roots.size() - !new_ver);
103     if (cur_root != roots.back()) roots.push_back(cur_root)
#700     return roots.size() - 1;
104 }
105 }
106 Seg get(int l, int r, int ver = -1) {
107     if (ver == -1) ver = roots.size() - 1;
108     Seg seg1, seg2
#751 Seg *pres = &seg1, *ptmp = &seg2;
109 roots[ver]->get(0, len, l, r, pres, ptmp, roots.size() - 1);
110 return *pres;
111 }
112 }
#542 }
113 }
114 }
115 intmain({
116     int n, m; // solves Mechanics Practice LAZY
117     cin >> n >> m;
118     SegTree seg_tree(1 << 17;
119     for (int i = 0; i < n; ++i) {
120         Lazy tmp;
121         scanf("%lld", &tmp.assign_val);
122         seg_tree.upd(i, i + 1, tmp);
123     }
124     for (int i = 0; i < m; ++i) {
125         int o;
126         int l, r;
127         scanf("%d %d %d", &o, &l, &r);
128         --l;
129         if (o == 1) {
130             Lazy tmp;
131             scanf("%lld", &tmp.add);
132             seg_tree.upd(l, r, tmp);
133         } else if (o == 2) {
134             Lazy tmp;
135             scanf("%lld", &tmp.assign_val);
136             seg_tree.upd(l, r, tmp);
137         } else {
138             Seg res = seg_tree.get(l, r);
139             printf("%lld\n", res.sum);
140         }
141     }

```

19 Templated HLD $\mathcal{O}(M(n)\log n)$ per query

```

1 class dummy {
2 public:
3   dummy() {}
4   dummy(int, int) {}
5   void set(int, int) {
6     intquery(int left, int right{
7       cout << this << ' ' << left << ' ' << right << endl;
8     }
9 }
10  %932 /* T should be the type of the data stored in each vertex;
11  * DS should be the underlying data structure that is used to perform
12  * the group operation. It should have the following methods:
13  * * DS () - empty constructor
14  * * DS (int size, T initial) - constructs the structure with the
15  * given size, initially filled with initial.
16  * * void set (int index, T value) - set the value at index `index` to
17  * `value`
18  * * T query (int left, int right) - return the "sum" of elements
19  * between left and right, inclusive.
20 */
21 template <typename T, class DS>
22 class HLD {
23   int vertexc;
24   vector<int> *adj;
25   vector<int> subtree_size
26   DS structure;
27   DS aux;
28   void build_sizes(int vertex, int parent{
29     subtree_size[vertex] = 1;
30     for (int child : adj[vertex])
31       if (child != parent) {
32         build_sizes(child, vertex);
33         subtree_size[vertex] += subtree_size[child];
34       }
35   }
36   int cur;
37   vector<int> ord;
38   vector<int> chain_root;
39   vector<int> par
40   void build_hld(int vertex, int parent, int chain_source{
41     cur++;
42     ord[vertex] = cur;
43     chain_root[vertex] = chain_source;
44     par[vertex] = parent
45     if (adj[vertex].size() > 1 ||
46         (vertex == 1 && adj[vertex].size() == 1)) {
47       int big_child, big_size = -1;
48       for (int child : adj[vertex]) {
49         if ((child != parent) && (subtree_size[child] > big_size))

```

#531

#178

#037

#759

#593

#432

```

50     big_child = child;
51     big_size = subtree_size[child];
52   }
53 }
54 build_hld(big_child, vertex, chain_source)
55 for (int child : adj[vertex]) {
56   if ((child != parent) && (child != big_child))
57     build_hld(child, vertex, child);
58 }
59 }
60 public:
61 HLD(int _vertexc) {
62   vertexc = _vertexc;
63   adj = new vector<int>[vertexc + 5]
64 }
65 void add_edge(int u, int v) {
66   adj[u].push_back(v);
67   adj[v].push_back(u);
68 }
69 void build(T initial{
70   subtree_size = vector<int>(vertexc + 5);
71   ord = vector<int>(vertexc + 5);
72   chain_root = vector<int>(vertexc + 5);
73   par = vector<int>(vertexc + 5)
74   cur = 0;
75   build_sizes(1, -1);
76   build_hld(1, -1, 1);
77   structure = DS(vertexc + 5, initial);
78   aux = DS(50, initial)
79 }
80 void set(int vertex, int value) {
81   structure.set(ord[vertex], value);
82 }
83 T query_path
84 int u, int v) { /* returns the "sum" of the path u->v */
85   int cur_id = 0;
86   while (chain_root[u] != chain_root[v]) {
87     if (ord[u] > ord[v]) {
88       cur_id++
89       aux.set(cur_id, structure.query(ord[chain_root[u]], ord[u]));
90       u = par[chain_root[u]];
91     } else {
92       cur_id++;
93       aux.set(cur_id, structure.query(ord[chain_root[v]], ord[v]))
94       ↪ #485
95       v = par[chain_root[v]];
96     }
97   }
98   cur_id++;
99   aux.set(cur_id

```

#254

#461

#800

#587

#976

#638

#325

#052

#041

```

100     structure.query(min(ord[u], ord[v]), max(ord[u], ord[v]));
101     return aux.query(1, cur_id);
102                                     %905
103 voidprint({
104     for (int i = 1; i <= vertexc; i++)
105         cout << i << ' ' << ord[i] << ' ' << chain_root[i] << ' '
106             << par[i] << endl;
107 }
108 };
109 intmain({
110     int vertexc;
111     cin >> vertexc;
112     HLD<int, dummy> hld(vertexc);
113     for (int i = 0; i < vertexc - 1; i++) {
114         int u, v;
115         cin >> u >> v;
116         hld.add_edge(u, v);
117     }
118     hld.build(0);
119     hld.print();
120     int queryc;
121     cin >> queryc;
122     for (int i = 0; i < queryc; i++) {
123         int u, v;
124         cin >> u >> v;
125         hld.query_path(u, v);
126         cout << endl;
127     }

```

20 Templated multi dimensional BIT $\mathcal{O}(\log(n)^{\dim})$ per query

```

1 // Fully overloaded any dimensional BIT, use any type for coordinates,
2 // elements, return_value. Includes coordinate compression.
3 template <typename elem_t, typename coord_t, coord_t n_inf,
4     typename ret_t>
5 class BIT {
6     vector<coord_t> positions;
7     vector<elem_t> elems
8     bool initiated = false;
9 public:
10     BIT() { positions.push_back(n_inf); }
11     void initiate() {
12         if (initiated)
13             for (elem_t &c_elem : elems) c_elem.initiate();
14         else {
15             initiated = true;
16             sort(positions.begin(), positions.end());
17             positions.resize(unique(positions.begin(), positions.end())
18                               ↪ #822
19                               positions.begin());
19             elems.resize(positions.size());
20         }
21     }

```

```

22 template <typename... loc_form
23 voidupdate(coord_t cord, loc_form... args{
24     if (initiated) {
25         int pos =
26             lower_bound(positions.begin(), positions.end(), cord) -
27             positions.begin()
28         for (; pos < positions.size(); pos += pos & -pos)
29             elems[pos].update(args...);
30     } else {
31         positions.push_back(cord);
32     }
33 }
34 template <typename... loc_form>
35 ret_t query(coord_t cord,
36     loc_form... args) {// sum in open interval (-inf, cord)
37     ret_t res = 0
38     int pos = (lower_bound(positions.begin(), positions.end(), cord) -
39             positions.begin()) -
40             1;
41     for (; pos > 0; pos -= pos & -pos)
42         res += elems[pos].query(args...)
43     return res;
44 }
45 };
46 template <typename internal_type>
47 struct wrapped
48     internal_type a = 0;
49     voidupdate(internal_type b{ a += b; }
50     internal_typequery({ return a; }
51     // Should never be called, needed for compilation
52     voidinitiate({ cerr << 'i' << endl; }
53     voidupdate({ cerr << 'u' << endl;
54 }
55 intmain({
56     // return type should be same as type inside wrapped
57     BIT<BIT<wrapped<ll>, int, INT_MIN, ll>, int, INT_MIN, ll> fenwick;
58     int dim = 2;
59     vector<tuple<int, int, ll> > to_insert;
60     to_insert.emplace_back(1, 1, 1);
61     // set up all positions that are to be used for update
62     for (int i = 0; i < dim; ++i) {
63         for (auto &cur : to_insert)
64             fenwick.update(get<0>(cur),
65                 get<1>(cur)); // May include value which won't be used
66         fenwick.initiate();
67     }
68     // actual use
69     for (auto &cur : to_insert)
70         fenwick.update(get<0>(cur), get<1>(cur), get<2>(cur));
71     cout << fenwick.query(2, 2) << '\n';

```

#620

#346

#542

#326

#549

#616

#636

%714

21 Treap $\mathcal{O}(\log n)$ per query

```

1 mt19937 randgen;
2 struct Treap {
3     struct Node {
4         int key;
5         int value
6         unsigned int priority;
7         long long total;
8         Node* lch;
9         Node* rch;
10        Node(int new_key, int new_value)
11            key = new_key;
12            value = new_value;
13            priority = randgen();
14            total = new_value;
15            lch = 0;
16            rch = 0;
17        }
18        void update() {
19            total = value;
20            if (lch) total += lch->total;
21            if (rch) total += rch->total;
22        }
23    };
24    deque<Node> nodes;
25    Node* root = 0
26    pair<Node*, Node*> split(int key, Node* cur) {
27        if (cur == 0) return {0, 0};
28        pair<Node*, Node*> result;
29        if (key <= cur->key) {
30            auto ret = split(key, cur->lch);
31            cur->lch = ret.second;
32            result = {ret.first, cur};
33        } else {
34            auto ret = split(key, cur->rch);
35            cur->rch = ret.first;
36            result = {cur, ret.second};
37        }
38        cur->update();
39        return result;
40    }
41    Node* merge(Node* left, Node* right) {
42        if (left == 0) return right;
43        if (right == 0) return left;
44        Node* top;
45        if (left->priority < right->priority)
46            left->rch = merge(left->rch, right);
47            top = left;
48        } else {
49            right->lch = merge(left, right->lch);
50            top = right

```

#615

#698

#232

#295

#633

#233

#988

#230

#282

#510

```

51     }
52     top->update();
53     return top;
54 }
55 void insert(int key, int value)
56     nodes.push_back(Node(key, value));
57     Node* cur = &nodes.back();
58     pair<Node*, Node*> ret = split(key, root);
59     cur = merge(ret.first, cur);
60     cur = merge(cur, ret.second)
61     root = cur;
62 }
63 void erase(int key) {
64     Node *left, *mid, *right;
65     tie(left, mid) = split(key, root)
66     tie(mid, right) = split(key + 1, mid);
67     root = merge(left, right);
68 }
69 long long sum_upto(int key, Node* cur) {
70     if (cur == 0) return 0
71     if (key <= cur->key) {
72         return sum_upto(key, cur->lch);
73     } else {
74         long long result = cur->value + sum_upto(key, cur->rch);
75         if (cur->lch) result += cur->lch->total
76         return result;
77     }
78 }
79 long long get(int l, int r) {
80     return sum_upto(r + 1, root) - sum_upto(l, root)
81 }
82 }
83 // http://codeforces.com/group/U01GDa2Gwb/contest/219104/problem/TREAP
84 int main() {
85     ios_base::sync_with_stdio(false);
86     cin.tie(0);
87     int m;
88     Treap treap;
89     cin >> m;
90     for (int i = 0; i < m; i++) {
91         int type;
92         cin >> type;
93         if (type == 1) {
94             int x, y;
95             cin >> x >> y;
96             treap.insert(x, y);
97         } else if (type == 2) {
98             int x;
99             cin >> x;
100             treap.erase(x);
101         } else {

```

#918

#760

#416

#634

#122

#509

```

102     int l, r;
103     cin >> l >> r;
104     cout << treap.get(l, r) << endl;
105 }
106 }
107 return 0;

```

22 Radixsort 50M 64 bit integers as single array in 1 sec

```

1 typedef unsigned char uchar;
2 template <typename T>
3 void msd_radixsort(
4     T *start, T *sec_start, int arr_size, int d = sizeof(T) - 1) { #866
5     const int msd_radix_lim = 100
6     const T mask = 255;
7     int bucket_sizes[256]{};
8     for (T *it = start; it != start + arr_size; ++it) {
9         ++bucket_sizes[((*it) >> (d * 8)) & mask];
10        //++bucket_sizes[*((uchar*)it + d)];
11    }
12    T *locs_mem[257];
13    locs_mem[0] = sec_start;
14    T **locs = locs_mem + 1;
15    locs[0] = sec_start;
16    for (int j = 0; j < 255; ++j) #818
17        locs[j + 1] = locs[j] + bucket_sizes[j];
18    }
19    for (T *it = start; it != start + arr_size; ++it) {
20        uchar bucket_id = ((*it) >> (d * 8)) & mask;
21        *(locs[bucket_id]++) = *it #361
22    }
23    locs = locs_mem;
24    if (d) {
25        T *locs_old[256];
26        locs_old[0] = start #153
27        for (int j = 0; j < 255; ++j) {
28            locs_old[j + 1] = locs_old[j] + bucket_sizes[j];
29        }
30        for (int j = 0; j < 256; ++j) {
31            if (locs[j + 1] - locs[j] < msd_radix_lim) #867
32                std::sort(locs[j], locs[j + 1]);
33            if (d & 1) {
34                copy(locs[j], locs[j + 1], locs_old[j]);
35            }
36            } else #946
37                msd_radixsort(locs[j], locs_old[j], bucket_sizes[j], d - 1);
38        }
39    }
40    }
41    %225
42    const int nmax = 5e7;
43    ll arr[nmax], tmp[nmax];
44    intmain({

```

```

45     for (int i = 0; i < nmax; ++i) arr[i] = ((ll)rand() << 32) | rand();
46     msd_radixsort(arr, tmp, nmax);
47     assert(is_sorted(arr, arr + nmax));

```

23 FFT 5M length/sec

integer $c = a * b$ is accurate if $c_i < 2^{49}$

```

1 struct Complex {
2     double a = 0, b = 0;
3     Complex &operator/=(const int &oth) {
4         a /= oth;
5         b /= oth #139
6         return *this;
7     }
8 };
9 Complex operator+(const Complex &lft, const Complex &rgt) {
10     return Complex{lft.a + rgt.a, lft.b + rgt.b} #384
11 }
12 Complex operator-(const Complex &lft, const Complex &rgt) {
13     return Complex{lft.a - rgt.a, lft.b - rgt.b};
14 }
15 Complex operator*(const Complex &lft, const Complex &rgt) #560
16     return Complex{
17         lft.a * rgt.a - lft.b * rgt.b, lft.a * rgt.b + lft.b * rgt.a;
18     };
19 Complex conj(const Complex &cur) { return Complex{cur.a, -cur.b}; }
20 void fft_rec(Complex *arr, Complex *root_pow, int len) #385
21     if (len != 1) {
22         fft_rec(arr, root_pow, len >> 1);
23         fft_rec(arr + len, root_pow, len >> 1);
24     }
25     root_pow += len #216
26     for (int i = 0; i < len; ++i) {
27         Complex tmp = arr[i] + root_pow[i] * arr[i + len];
28         arr[i + len] = arr[i] - root_pow[i] * arr[i + len];
29         arr[i] = tmp;
30     } #249
31 }
32 void fft(vector<Complex> &arr, int ord, bool invert) {
33     assert(arr.size() == 1 << ord);
34     static vector<Complex> root_pow(1);
35     static int inc_pow = 1 #669
36     static bool is_inv = false;
37     if (inc_pow <= ord) {
38         int idx = root_pow.size();
39         root_pow.resize(1 << ord);
40         for (; inc_pow <= ord; ++inc_pow) #517
41             for (int idx_p = 0; idx_p < 1 << (ord - 1);
42                 idx_p += 1 << (ord - inc_pow), ++idx) {
43                 root_pow[idx] = Complex{cos(-idx_p * M_PI / (1 << (ord - 1))),
44                     sin(-idx_p * M_PI / (1 << (ord - 1)))};
45                 if (is_inv) root_pow[idx].b = -root_pow[idx].b #105

```

```

46     }
47 }
48 }
49 if (invert != is_inv) {
50     is_inv = invert
51     for (Complex &cur : root_pow) cur.b = -cur.b;
52 }
53 for (int i = 1, j = 0; i < (1 << ord); ++i) {
54     int m = 1 << (ord - 1);
55     bool cont = true
56     while (cont) {
57         cont = j & m;
58         j ^= m;
59         m >>= 1;
60
61         if (i < j) swap(arr[i], arr[j]);
62     }
63     fft_rec(arr.data(), root_pow.data(), 1 << (ord - 1));
64     if (invert)
65         for (int i = 0; i < (1 << ord); ++i) arr[i] /= (1 << ord)
66
67 void mult_poly_mod(
68     vector<int> &a, vector<int> &b, vector<int> &c{// c += a*b
69     static vector<Complex>
70     arr[4]; // correct upto 0.5-2M elements(mod ~= 1e9)
71     if (c.size() < 400)
72         for (int i = 0; i < a.size(); ++i)
73             for (int j = 0; j < b.size() && i + j < c.size(); ++j)
74                 c[i + j] = ((ll)a[i] * b[j] + c[i + j]) % mod;
75     } else {
76         int fft_ord = 32 - __builtin_clz(c.size())
77         if (arr[0].size() != 1 << fft_ord)
78             for (int i = 0; i < 4; ++i) arr[i].resize(1 << fft_ord);
79         for (int i = 0; i < 4; ++i)
80             fill(arr[i].begin(), arr[i].end(), Complex{});
81         for (int &cur : a)
82             if (cur < 0) cur += mod;
83         for (int &cur : b)
84             if (cur < 0) cur += mod;
85         const int shift = 15;
86         const int mask = (1 << shift) - 1
87         for (int i = 0; i < min(a.size(), c.size()); ++i) {
88             arr[0][i].a = a[i] & mask;
89             arr[1][i].a = a[i] >> shift;
90         }
91         for (int i = 0; i < min(b.size(), c.size()); ++i)
92             arr[0][i].b = b[i] & mask;
93             arr[1][i].b = b[i] >> shift;
94     }
95     for (int i = 0; i < 2; ++i) fft(arr[i], fft_ord, false);
96     for (int i = 0; i < 2; ++i)
97         for (int j = 0; j < 2; ++j) {

```

#750

#122

#844

#343
%380

#811

#629

#591

#625

#528

#644

```

98     int tar = 2 + (i + j) / 2;
99     Complex mult = {0, -0.25};
100     if (i ^ j) mult = {0.25, 0};
101     for (int k = 0; k < (1 << fft_ord); ++k)
102         int rev_k = ((1 << fft_ord) - k) % (1 << fft_ord);
103         Complex ca = arr[i][k] + conj(arr[i][rev_k]);
104         Complex cb = arr[j][k] - conj(arr[j][rev_k]);
105         arr[tar][k] = arr[tar][k] + mult * ca * cb;
106
107     }
108 }
109 for (int i = 2; i < 4; ++i) {
110     fft(arr[i], fft_ord, true);
111     for (int k = 0; k < (int)c.size(); ++k)
112         c[k] = (c[k] + (((ll)(arr[i][k].a + 0.5) % mod)
113             << (shift * 2 * (i - 2)))) %
114             mod;
115         c[k] = (c[k] + (((ll)(arr[i][k].b + 0.5) % mod)
116             << (shift * (2 * (i - 2) + 1))))
117             mod;
118     }
119 }
120 }

```

#983

#471

#403

#108

24 Fast mod mult, Rabbin Miller prime check, Pollard rho factorization $O(\sqrt{p})$

```

1 struct ModArithm {
2     ull n;
3     ld rec;
4     ModArithm(ull _n) : n(_n) { // n in [2, 1<<63]
5         rec = 1.0L / n
6     }
7     ull multf(ull a, ull b) { // a, b in [0, min(2*n, 1<<63))
8         ull mult = (ld)a * b * rec + 0.5L;
9         ll res = a * b - mult * n;
10        if (res < 0) res += n
11        return res; // in [0, n-1]
12    }
13    ull sqp1(ull a) { return multf(a, a) + 1; }
14 }
15 ull pow_mod(ull a, ull n, ModArithm &arithm{
16     ull res = 1;
17     for (ull i = 1; i <= n; i <= 1) {
18         if (n & i) res = arithm.multf(res, a);
19         a = arithm.multf(a, a)
20     }
21     return res;
22 }
23 vector<char> small_primes = {
24     2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
25 bool is_prime(ull n { // n <= 1<<63, 1M rand/s

```

#237

#780

%493

#758

%144

```

26  ModArithmarithm(n;
27  if (n == 2 || n == 3) return true
28  if (!(n & 1) || n == 1) return false;
29  ull s = __builtin_ctz(n - 1);
30  ull d = (n - 1) >> s;
31  for (ull a : small_primes) {
32      if (a >= n) break
33      a = pow_mod(a, d, arithm);
34      if (a == 1 || a == n - 1) continue;
35      for (ull r = 1; r < s; ++r) {
36          a = arithm.multf(a, a);
37          if (a == 1) return false
38          if (a == n - 1) break;
39      }
40      if (a != n - 1) return false;
41  }
42  return true
43
44  ll pollard_rho(ll n{
45      ModArithm arithm(n);
46      int cum_cnt = 64 - __builtin_clz(n);
47      cum_cnt *= cum_cnt / 5 + 1;
48      while (true)
49          ll lv = rand() % n;
50          ll v = arithm.sqp1(lv);
51          int idx = 1;
52          int tar = 1;
53          while (true)
54              ll cur = 1;
55              ll v_cur = v;
56              int j_stop = min(cum_cnt, tar - idx);
57              for (int j = 0; j < j_stop; ++j) {
58                  cur = arithm.multf(cur, abs(v_cur - lv))
59                  v_cur = arithm.sqp1(v_cur);
60                  ++idx;
61              }
62              if (!cur) {
63                  for (int j = 0; j < cum_cnt; ++j)
64                      ll g = __gcd(abs(v - lv), n);
65                      if (g == 1) {
66                          v = arithm.sqp1(v);
67                      } else if (g == n) {
68                          break
69                      } else {
70                          return g;
71                      }
72              }
73              break
74          } else {
75              ll g = __gcd(cur, n);
76              if (g != 1) return g;
77          }

```

```

#104 78      v = v_cur
79      idx += j_stop;
80      if (idx == tar) {
81          lv = v;
82          tar *= 2;
83          v = arithm.sqp1(v)
84          ++idx;
85      }
86  }
87  }
#402
#876 88
89  map<ll, int> prime_factor(ll n,
90  map<ll, int> *res = NULL) {// n <= 1<<61, ~1000/s (<500/s on CF)
91  if (!res) {
92      map<ll, int> res_act;
93      for (int p : small_primes)
94          while (!(n % p)) {
95              ++res_act[p];
96              n /= p;
97          }
98
99      if (n != 1) prime_factor(n, &res_act);
100      return res_act;
101  }
102  if (is_prime(n)) {
103      ++(*res)[n]
104  } else {
#290 105      ll factor = pollard_rho(n);
106      prime_factor(factor, res);
107      prime_factor(n / factor, res);
108
109      return map<ll, int>();
#468
#912

```

25 Symmetric Submodular Functions; Queyrannes's algorithm

SSF: such function $f : V \rightarrow R$ that satisfies $f(A) = f(V/A)$ and for all $x \in V, X \subseteq Y \subseteq V$ it holds that $f(X + x) - f(X) \leq f(Y + x) - f(Y)$. **Hereditary family:** such set $I \subseteq 2^V$ so that $X \subset Y \wedge Y \in I \Rightarrow X \in I$. **Loop:** such $v \in V$ so that $v \notin I$.
breaklines

```

#906 1 def minimize():
2     s = merge_all_loops()
3     while size >= 3:
4         t, u = find_pp()
5         {u} is a possible minimizer
6         tu = merge(t, u)
7         if tu not in I:
8             s = merge(tu, s)
9         for x in V:
10             {x} is a possible minimizer
#208 11 def find_pp():
12     W = {s} # s as in minimizer()

```

```

13  todo = V/W
14  ord = []
15  while len(todo) > 0:
16      x = min(todo, key=lambda x: f(W+{x}) - f({x}))
17      W += {x}
18      todo -= {x}
19      ord.append(x)
20  return ord[-1], ord[-2]
21 def enum_all_minimal_minimizers(X):
22     # X is a inclusionwise minimal minimizer
23     s = merge(s, X)
24     yield X
25     for {v} in I:
26         if f({v}) == f(X):
27             yield X
28             s = merge(v, s)
29     while size(V) >= 3:
30         t, u = find_pp()
31         tu = merge(t, u)
32         if tu not in I:
33             s = merge(tu, s)
34     elif f({tu}) = f(X):
35         yield tu
36         s = merge(tu, s)

```

26 Berlekamp-Massey $O(\mathcal{L}N)$

```

1  template <typename K>
2  static vector<K> berlekamp_massey(vector<K> ss) {
3      vector<K> ts(ss.size());
4      vector<K> cs(ss.size());
5      cs[0] = K::unity                                #349
6      fill(cs.begin() + 1, cs.end(), K::zero);
7      vector<K> bs = cs;
8      int l = 0, m = 1;
9      K b = K::unity;
10     for (int k = 0; k < (int)ss.size(); k++)          #390
11         K d = ss[k];
12         assert(l <= k);
13         for (int i = 1; i <= l; i++) d += cs[i] * ss[k - i];
14         if (d == K::zero) {
15             m++;                                       #445
16         } else if (2 * l <= k) {
17             K w = d / b;
18             ts = cs;
19             for (int i = 0; i < (int)cs.size() - m; i++)
20                 cs[i + m] -= w * bs[i]                #661
21             l = k + 1 - l;
22             swap(bs, ts);
23             b = d;
24             m = 1;
25         } else                                       #815
26             K w = d / b;

```

```

27     for (int i = 0; i < (int)cs.size() - m; i++)
28         cs[i + m] -= w * bs[i];
29     m++;
30 }
31 }
32 cs.resize(l + 1);
33 while (cs.back() == K::zero) cs.pop_back();
34 return cs;

```