

University of Tartu ICPC Team Notebook

(2018-2019) November 22, 2018

Contents

1	Setup
2	crc.sh
3	gcc ordered set
4	2D geometry
5	3D geometry
6	Numerical integration with Simpson's rule
7	Triangle centers
8	Seg-Seg intersection, halfplane intersection area
9	Convex polygon algorithms
10	Aho Corasick $\mathcal{O}(\alpha \sum \text{len})$
11	Suffix automaton and tree $\mathcal{O}((n+q) \log(\alpha))$
12	Dinic
13	Min Cost Max Flow with successive dijkstra $\mathcal{O}(\text{flow} \cdot n^2)$
14	Min Cost Max Flow with Cycle Cancelling $\mathcal{O}(\text{flow} \cdot nm)$
15	DMST $\mathcal{O}(E \log V)$
16	Bridges $\mathcal{O}(n)$
17	2-Sat $\mathcal{O}(n)$ and SCC $\mathcal{O}(n)$
18	Generic persistent compressed lazy segment tree
19	Templated HLD $\mathcal{O}(M(n) \log n)$ per query
20	Templated multi dimensional BIT $\mathcal{O}(\log(n)^{\text{dim}})$ per query
21	Treap $\mathcal{O}(\log n)$ per query
22	Radixsort 50M 64 bit integers as single array in 1 sec

23	FFT 5M length/sec	20
24	Fast mod mult, Rabbin Miller prime check, Pollard rho factorization $\mathcal{O}(\sqrt{p})$	21
25	Symmetric Submodular Functions; Queyrannes's algorithm	22

1 Setup

```
1 set smartindent cindent set ts = 4 sw =
2 4 expandtab syntax enable set clipboard = unnamedplus
3 "setxkbmap -option caps:escape
4 "valgrind --vgdb-error=0 ./a <inp &
5 "gdb a
6 "target remote | vgdb
```

2 crc.sh

```
1 #!/bin/envbash
2 for j in `seq 10 10 200`; do
3   sed '/^\s*$/d' $1 | head -$j | tr -d '[:space:]' | cksum | cut -f1
4   ↪ -d ' ' | tail -c 4 #whistespaces don't matter.
5 done #there shouldn't be any COMMENTS.
6 #copy lines being checked to separate file.
7 # $ ./crc.sh tmp.cpp
```

3 gcc ordered set

```
1 #include <bits/stdc++.h>
2 typedef long long ll;
3 using namespace std;
4 #include <ext/pb_ds/assoc_container.hpp>
5 #include <ext/pb_ds/tree_policy.hpp>
6 using namespace __gnu_pbds;
7 template <typename T>
8 using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
9   tree_order_statistics_node_update>;
10 int main() {
11   ordered_set<int> cur;
12   cur.insert(1);
13   cur.insert(3);
14   cout << cur.order_of_key(2)
15   << endl; // the number of elements in the set less than 2
16   cout << *cur.find_by_order(0)
17   << endl; // the 0-th smallest number in the set(0-based)
18   cout << *cur.find_by_order(1)
19   << endl; // the 1-th smallest number in the set(0-based)
20 }
```

#558

%574

4 2D geometry

Define **orient**(A, B, C) = $\overline{AB} \times \overline{AC}$. CCW iff > 0 .
 Define **perp**((a, b)) = $(-b, a)$. The vectors are orthogonal.

For line $ax + by = c$ def $\bar{v} = (-b, a)$.

Line through P and Q has $\bar{v} = \overline{PQ}$ and $c = \bar{v} \times P$.

side_l(P) = $\bar{v}_l \times P - c_l$ sign determines which side P is on from l .

dist_l(P) = **side_l**(P)/ $\|\bar{v}_l\|$ squared is integer.

Sorting points along a line: comparator is $\bar{v} \cdot A < \bar{v} \cdot B$.

Translating line by \bar{t} : new line has $c' = c + \bar{v} \times \bar{t}$.

Line intersection: is $(c_l \bar{v}_m - c_m \bar{v}_l) / (\bar{v}_l \times \bar{v}_m)$.

Project P onto l : is $P - \text{perp}(v) \text{side}_l(P) / \|\bar{v}\|^2$.

Angle bisectors: $\bar{v} = \bar{v}_l / \|\bar{v}_l\| + \bar{v}_m / \|\bar{v}_m\|$

$c = c_l / \|\bar{v}_l\| + c_m / \|\bar{v}_m\|$.

P is on segment AB iff **orient**(A, B, P) = 0 and $\overline{PA} \cdot \overline{PB} \leq 0$.

Proper intersection of AB and CD exists iff **orient**(C, D, A) and **orient**(C, D, B) have opp. signs and **orient**(A, B, C) and **orient**(A, B, D) have opp. signs. Coordinates:

$$\frac{A \text{orient}(C, D, B) - B \text{orient}(C, D, A)}{\text{orient}(C, D, B) - \text{orient}(C, D, A)}.$$

Circumcircle center:

```
pt circumCenter(pt a, pt b, pt c) {
    b = b-a, c = c-a; // consider coordinates
    relative to A
    assert(cross(b,c) != 0); // no circumcircle if
    A,B,C aligned
    return a + perp(b*sq(c) - c*sq(b))/cross(b,c)
    /2;
```

Circle-line intersect:

```
int circleLine(pt o, double r, line l, pair<pt,
pt> &out) {
    double h2 = r*r - l.sqDist(o);
    if (h2 >= 0) { // the line touches the circle
        pt p = l.proj(o); // point P
        pt h = l.v*sqrt(h2)/abs(l.v); // vector
        paral to l, of len h
        out = {p-h, p+h};
    }
    return 1 + sgn(h2);
```

Circle-circle intersect:

```
int circleCircle(pt o1, double r1, pt o2, double
r2, pair<pt,pt> &out) {
```

```
pt d=o2-o1; double d2=sq(d);
if (d2 == 0) {assert(r1 != r2); return 0;} //
concentric circles
double pd = (d2 + r1*r1 - r2*r2)/2; // = |O1P
| * d
double h2 = r1*r1 - pd*pd/d2; // = h^2
if (h2 >= 0) {
    pt p = o1 + d*pd/d2, h = perp(d)*sqrt(h2/d2)
    ;
    out = {p-h, p+h};}
return 1 + sgn(h2);
```

Tangent lines:

```
int tangents(pt o1, double r1, pt o2, double r2,
bool inner, vector<pair<pt,pt>> &out) {
    if (inner) r2 = -r2;
    pt d = o2-o1;
    double dr = r1-r2, d2 = sq(d), h2 = d2-dr*dr;
    if (d2 == 0 || h2 < 0) {assert(h2 != 0);
        return 0;}
    for (double sign : {-1,1}) {
        pt v = (d*dr + perp(d)*sqrt(h2)*sign)/d2;
        out.push_back({o1 + v*r1, o2 + v*r2});}
    return 1 + (h2 > 0);
```

5 3D geometry

orient(P, Q, R, S) = $(\overline{PQ} \times \overline{PR}) \cdot \overline{PS}$.

S above PQR iff > 0 .

For plane $ax + by + cz = d$ def $\bar{n} = (a, b, c)$.

Line with normal \bar{n} through point P has $d = \bar{n} \cdot P$.

side_Π(P) = $\bar{n} \cdot P - d$ sign determines side from Π .

dist_Π(P) = **side_Π**(P)/ $\|\bar{n}\|$.

Translating plane by \bar{t} makes $d' = d + \bar{n} \cdot \bar{t}$.

Plane-plane intersection has direction $\bar{n}_1 \times \bar{n}_2$ and goes

through $((d_1 \bar{n}_2 - d_2 \bar{n}_1) \times \bar{d}) / \|\bar{d}\|^2$.

Line-line distance:

```
double dist(line3d l1, line3d l2) {
    p3 n = l1.d*l2.d;
    if (n == zero) // parallel
        return l1.dist(l2.o);
    return abs((l2.o-l1.o)|n)/abs(n);
```

Spherical to Cartesian:

$(r \cos \varphi \cos \lambda, r \cos \varphi \sin \lambda, r \sin \varphi)$.

Sphere-line intersection:

```
int sphereLine(p3 o, double r, line3d l, pair<p3
,p3> &out) {
    double h2 = r*r - l.sqDist(o);
    if (h2 < 0) return 0; // the line doesn't
    touch the sphere
    p3 p = l.proj(o); // point P
```

```
p3 h = l.d*sqrt(h2)/abs(l.d); // vector
parallel to l, of length h
out = {p-h, p+h};
return 1 + (h2 > 0);
```

Great-circle distance between points A and B is $r \angle AOB$.

Spherical segment intersection:

```
bool properInter(p3 a, p3 b, p3 c, p3 d, p3 &out
) {
    p3 ab = a*b, cd = c*d; // normals of planes
    OAB and OCD
    int oa = sgn(cd|a),
    ob = sgn(cd|b),
    oc = sgn(ab|c),
    od = sgn(ab|d);
    out = ab*cd*od; // four multiplications =>
    careful with overflow !
    return (oa != ob && oc != od && oa != oc);
}
bool onSphSegment(p3 a, p3 b, p3 p) {
    p3 n = a*b;
    if (n == zero)
        return a*p == zero && (a|p) > 0;
    return (n|p) == 0 && (n|a*p) >= 0 && (n|b*p)
    <= 0;
}
struct directionSet : vector<p3> {
    using vector::vector; // import constructors
    void insert(p3 p) {
        for (p3 q : *this) if (p*q == zero) return;
        push_back(p);
    }
};
directionSet intersSph(p3 a, p3 b, p3 c, p3 d) {
    assert(validSegment(a, b) && validSegment(c, d
));
    p3 out;
    if (properInter(a, b, c, d, out)) return {out
};
    directionSet s;
    if (onSphSegment(c, d, a)) s.insert(a);
    if (onSphSegment(c, d, b)) s.insert(b);
    if (onSphSegment(a, b, c)) s.insert(c);
    if (onSphSegment(a, b, d)) s.insert(d);
    return s;
}
```

Angle between spherical segments AB and AC is angle between $A \times B$ and $A \times C$.

Oriented angle: subtract from 2π if mixed product is negative.

Area of a spherical polygon:

$$r^2 [\text{sum of interior angles} - (n - 2)\pi].$$

6 Numerical integration with Simpson's rule

```

1 // computing power = how many times function integrate gets called
2 template <typename T>
3 double simps(T f, double a, double b) {
4     return (f(a) + 4 * f((a + b) / 2) + f(b)) * (b - a) / 6;
5 }
6 template <typename T>
7 double integrate(T f, double a, double b, double computing_power) {
8     double m = (a + b) / 2;
9     double l = simps(f, a, m), r = simps(f, m, b), tot = simps(f, a, b);
10    if (computing_power < 1) return tot;
11    return integrate(f, a, m, computing_power / 2) + #567
12           integrate(f, m, b, computing_power / 2);
13 } %360

```

7 Triangle centers

```

1 const double min_delta = 1e-13;
2 const double coord_max = 1e6;
3 typedef complex<double> point;
4 point A, B, C; // vertices of the triangle
5 bool collinear() {
6     double min_diff = min(abs(A - B), min(abs(A - C), abs(B - C)));
7     if (min_diff < coord_max * min_delta) return true;
8     point sp = (B - A) / (C - A);
9     double ang =
10         M_PI / 2 - #638
11         abs(abs(arg(sp)) - M_PI / 2); // positive angle with the real line
12     return ang < min_delta;
13 } %446
14 point circum_center() {
15     if (collinear()) return point(NAN, NAN);
16     // squared lengths of sides
17     double a2, b2, c2;
18     a2 = norm(B - C);
19     b2 = norm(A - C);
20     c2 = norm(A - B);
21     // barycentric coordinates of the circumcenter
22     double c_A, c_B, c_C;
23     c_A = a2 * (b2 + c2 - a2); // sin(2 * alpha) may be used as well
24     c_B = b2 * (a2 + c2 - b2);
25     c_C = c2 * (a2 + b2 - c2); #403
26     double sum = c_A + c_B + c_C;
27     c_A /= sum;
28     c_B /= sum;
29     c_C /= sum;
30     // cartesian coordinates of the circumcenter
31     return c_A * A + c_B * B + c_C * C;
32 } %742
33 point centroid() { // center of mass
34     return (A + B + C) / 3.0;
35 }
36 point ortho_center() { // euler line
37     point O = circum_center();
38     return O + 3.0 * (centroid() - O);

```

```

39 };
40 point nine_point_circle_center() { // euler line
41     point O = circum_center();
42     return O + 1.5 * (centroid() - O); #193
43 }; %031
44 point in_center() {
45     if (collinear()) return point(NAN, NAN);
46     double a, b, c; // side lengths
47     a = abs(B - C);
48     b = abs(A - C);
49     c = abs(A - B);
50     // trilinear coordinates are (1,1,1)
51     // barycentric coordinates
52     double c_A = a, c_B = b, c_C = c;
53     double sum = c_A + c_B + c_C;
54     c_A /= sum;
55     c_B /= sum; #812
56     c_C /= sum;
57     // cartesian coordinates of the incenter
58     return c_A * A + c_B * B + c_C * C;
59 } %980

```

8 Seg-Seg intersection, halfplane intersection area

```

1 struct Seg {
2     Vec a, b;
3     Vec d() { return b - a; }
4 };
5 Vec intersection(Seg l, Seg r) {
6     Vec dl = l.d(), dr = r.d();
7     if (cross(dl, dr) == 0) return {nanl(""), nanl("")};
8     double h = cross(dr, l.a - r.a) / len(dr);
9     double dh = cross(dr, dl) / len(dr);
10    return l.a + dl * (h / -dh); #893
11 }
12 // Returns the area bounded by halfplanes
13 double calc_area(vector<Seg> lines) {
14     double lb = -HUGE_VAL, ub = HUGE_VAL;
15     vector<Seg> linesBySide[2];
16     for (auto line : lines) {
17         if (line.b.y == line.a.y) {
18             if (line.a.x < line.b.x) {
19                 lb = max(lb, line.a.y);
20             } else {
21                 ub = min(ub, line.a.y); #029
22             }
23         } else if (line.a.y < line.b.y) {
24             linesBySide[1].push_back(line);
25         } else {
26             linesBySide[0].push_back({line.b, line.a});
27         }
28     }
29     sort(
30         linesBySide[0].begin(), linesBySide[0].end(), [](Seg l, Seg r) {
31             if (cross(l.d(), r.d()) == 0)

```

```

32     return normal(l.d()) * l.a > normal(r.d()) * r.a;
33     return cross(l.d(), r.d()) < 0;
34 });
35 sort(
36     linesBySide[1].begin(), linesBySide[1].end(), [](Seg l, Seg r) {
37         if (cross(l.d(), r.d()) == 0)
38             return normal(l.d()) * l.a < normal(r.d()) * r.a;
39         return cross(l.d(), r.d()) > 0;
40 });
41 // Now find the application area of the lines and clean up redundant
42 // ones
43 vector<double> applyStart[2];
44 for (int side = 0; side < 2; side++) {
45     vector<double> &apply = applyStart[side];
46     vector<Seg> curLines;
47     for (auto line : linesBySide[side]) {
48         while (curLines.size() > 0) {
49             Seg other = curLines.back();
50             if (cross(line.d(), other.d()) != 0) {
51                 double start = intersection(line, other).y;
52                 if (start > apply.back()) break;
53             }
54             curLines.pop_back();
55             apply.pop_back();
56         }
57         if (curLines.size() == 0) {
58             apply.push_back(-HUGE_VAL);
59         } else {
60             apply.push_back(intersection(line, curLines.back()).y);
61         }
62         curLines.push_back(line);
63     }
64     linesBySide[side] = curLines;
65 }
66 applyStart[0].push_back(HUGE_VALL);
67 applyStart[1].push_back(HUGE_VALL);
68 double result = 0;
69 {
70     double lb = -HUGE_VALL, ub;
71     for (int i = 0, j = 0; i < (int)linesBySide[0].size() &&
72         j < (int)linesBySide[1].size();
73         lb = ub) {
74         ub = min(applyStart[0][i + 1], applyStart[1][j + 1]);
75         double alb = lb, aub = ub;
76         Seg l0 = linesBySide[0][i], l1 = linesBySide[1][j];
77         if (cross(l1.d(), l0.d()) > 0) {
78             alb = max(alb, intersection(l0, l1).y);
79         } else if (cross(l1.d(), l0.d()) < 0) {
80             aub = min(aub, intersection(l0, l1).y);
81         }
82         alb = max(alb, lb);
83         aub = min(aub, ub);
84         aub = max(aub, alb);
85     }

```

#597

#503

#047

#251

#839

```

86     double x1 = 10.a.x + (alb - 10.a.y) / 10.d().y * 10.d().x;
87     double x2 = 10.a.x + (aub - 10.a.y) / 10.d().y * 10.d().x;
88     result -= (aub - alb) * (x1 + x2) / 2;
89 }
90 {
91     double x1 = 11.a.x + (alb - 11.a.y) / 11.d().y * 11.d().x;
92     double x2 = 11.a.x + (aub - 11.a.y) / 11.d().y * 11.d().x;
93     result += (aub - alb) * (x1 + x2) / 2;
94 }
95 if (applyStart[0][i + 1] < applyStart[1][j + 1]) {
96     i++;
97 } else {
98     j++;
99 }
100 }
101 }
102 return result;
103 }

```

#717

%103

9 Convex polygon algorithms

```

1 typedef pair<int, int> Vec;
2 typedef pair<Vec, Vec> Seg;
3 typedef vector<Seg>::iterator SegIt;
4 #define F first
5 #define S second
6 #define MP(x, y) make_pair(x, y)
7 ll dot(const Vec &v1, const Vec &v2) {
8     return (ll)v1.F * v2.F + (ll)v1.S * v2.S;
9 }
10 ll cross(const Vec &v1, const Vec &v2) {
11     return (ll)v1.F * v2.S - (ll)v2.F * v1.S;
12 }
13 ll dist_sq(const Vec &p1, const Vec &p2) {
14     return (ll)(p2.F - p1.F) * (p2.F - p1.F) +
15         (ll)(p2.S - p1.S) * (p2.S - p1.S);
16 }
17 struct Hull {
18     vector<Seg> hull;
19     SegIt upper_begin;
20     template <typename It>
21     void extend_hull(It begin, It end) { // O(n)
22         vector<Vec> res;
23         for (auto it = begin; it != end; ++it) {
24             if (res.empty() || *it != res.back()) {
25                 while (res.size() >= 2) {
26                     Vec v1 = {res[res.size() - 1].F - res[res.size() - 2].F,
27                         ↪ #854
28                         res[res.size() - 1].S - res[res.size() - 2].S};
29                     Vec v2 = {it->F - res[res.size() - 2].F,
30                         it->S - res[res.size() - 2].S};
31                     if (cross(v1, v2) > 0) break;
32                     res.pop_back();
33                 }

```

#914

%623

```

33     res.push_back(*it);
34 }
35 }
36 for (int i = 0; i < res.size() - 1; ++i) #114
37     hull.emplace_back(res[i], res[i + 1]);
38 }
39 Hull(vector<Vec> &vert) { // at least 2 distinct points
40     sort(vert.begin(), vert.end()); // O(n log(n))
41     extend_hull(vert.begin(), vert.end());
42     int diff = hull.size();
43     extend_hull(vert.rbegin(), vert.rend());
44     upper_begin = hull.begin() + diff;
45 } %039
46 bool contains(Vec p) { // O(log(n))
47     if (p < hull.front().F || p > upper_begin->F) return false;
48     {
49         auto it_low = lower_bound(
50             hull.begin(), upper_begin, MP(MP(p.F, (int)-2e9), MP(0, 0)));
51         if (it_low != hull.begin()) --it_low;
52         Vec v1 = {it_low->S.F - it_low->F.F, it_low->S.S - it_low->F.S};
53         Vec v2 = {p.F - it_low->F.F, p.S - it_low->F.S};
54         if (cross(v1, v2) < 0) // < 0 is inclusive, <=0 is exclusive
55             return false; #287
56     }
57     {
58         auto it_up = lower_bound(hull.rbegin(),
59             hull.rbegin() + (hull.end() - upper_begin),
60             MP(MP(p.F, (int)2e9), MP(0, 0)));
61         if (it_up - hull.rbegin() == hull.end() - upper_begin) --it_up;
62         Vec v1 = {it_up->F.F - it_up->S.F, it_up->F.S - it_up->S.S};
63         Vec v2 = {p.F - it_up->S.F, p.S - it_up->S.S};
64         if (cross(v1, v2) > 0) // > 0 is inclusive, >=0 is exclusive
65             return false; #906
66     }
67     return true;
68 } %673
69 template <typename T> // The function can have only one local min
70 // and max and may be constant only at min and
71 // max.
72 SegIt max(
73     function<T(const Seg &)> f) { // O(log(n))
74     auto l = hull.begin();
75     auto r = hull.end();
76     SegIt best = hull.end();
77     T best_val;
78     while (r - l > 2) {
79         auto mid = l + (r - l) / 2;
80         T l_val = f(*l); #580
81         T l_nxt_val = f(*(l + 1));
82         T mid_val = f(*mid);
83         T mid_nxt_val = f(*(mid + 1));
84         if (best == hull.end() ||
85             l_val > best_val) { // If max is at l we may remove it from

```

```

86 // the range.
87     best = l;
88     best_val = l_val;
89 }
90 if (l_nxt_val > l_val) {
91     if (mid_val < l_val) { #146
92         r = mid;
93     } else {
94         if (mid_nxt_val > mid_val) {
95             l = mid + 1;
96         } else {
97             r = mid + 1;
98         }
99     }
100 } else {
101     if (mid_val < l_val) { #343
102         l = mid + 1;
103     } else {
104         if (mid_nxt_val > mid_val) {
105             l = mid + 1;
106         } else {
107             r = mid + 1;
108         }
109     }
110 }
111 } #951
112 T l_val = f(*l);
113 if (best == hull.end() || l_val > best_val) {
114     best = l;
115     best_val = l_val;
116 }
117 if (r - l > 1) {
118     T l_nxt_val = f(*(l + 1));
119     if (best == hull.end() || l_nxt_val > best_val) {
120         best = l + 1;
121         best_val = l_nxt_val; #886
122     }
123 }
124 return best;
125 } %053
126 SegIt closest(Vec p) { // p can't be internal(can be on border),
127 // hull must have atleast 3 points
128     const Seg &ref_p = hull.front(); // O(log(n))
129     return max(function<double(const Seg &)>(&p, &ref_p)(
130         const Seg &seg) { // accuracy of used type should be coord^2
131             if (p == seg.F) return 10 - M_PI;
132             Vec v1 = {seg.S.F - seg.F.F, seg.S.S - seg.F.S};
133             Vec v2 = {p.F - seg.F.F, p.S - seg.F.S};
134             ll cross_prod = cross(v1, v2);
135             if (cross_prod > 0) { // order the backside by angle #083
136                 Vec v1 = {ref_p.F.F - p.F, ref_p.F.S - p.S};
137                 Vec v2 = {seg.F.F - p.F, seg.F.S - p.S};

```



```

139     ll dot_prod = dot(v1, v2);
140     ll cross_prod = cross(v2, v1);
141     return atan2(cross_prod, dot_prod) / 2;
142 }
143 ll dot_prod = dot(v1, v2);
144 double res = atan2(dot_prod, cross_prod);
145 if (dot_prod <= 0 && res > 0) res = -M_PI;
146 if (res > 0) { #195
147     res += 20;
148 } else {
149     res = 10 - res;
150 }
151 return res;
152 }));
153 } %368
154 template <int DIRECTION> // 1 or -1
155 Vec tan_point(Vec p) { // can't be internal or on border
156     // -1 iff CCW rotation of ray from p to res takes it away from
157     // polygon?
158     const Seg &ref_p = hull.front(); // O(log(n))
159     auto best_seg = max(function<double(const Seg &)>(
160         [&p, &ref_p](
161             const Seg &seg) { // accuracy of used type should be coord^2
162                 Vec v1 = {ref_p.F.F - p.F, ref_p.F.S - p.S};
163                 Vec v2 = {seg.F.F - p.F, seg.F.S - p.S};
164                 ll dot_prod = dot(v1, v2);
165                 ll cross_prod = DIRECTION * cross(v2, v1); #867
166                 return atan2(cross_prod, dot_prod); // order by signed angle
167             });
168     return best_seg->F;
169 } %101
170 SegIt max_in_dir(Vec v) { // first is the ans. O(log(n))
171     return max(function<ll(const Seg &)>(
172         [&v](const Seg &seg) { return dot(v, seg.F); }));
173 } %861
174 pair<SegIt, SegIt> intersections(Seg line) { // O(log(n))
175     int x = line.S.F - line.F.F;
176     int y = line.S.S - line.F.S;
177     Vec dir = {-y, x};
178     auto it_max = max_in_dir(dir);
179     auto it_min = max_in_dir(MP(y, -x));
180     ll opt_val = dot(dir, line.F);
181     if (dot(dir, it_max->F) < opt_val ||
182         dot(dir, it_min->F) > opt_val)
183         return MP(hull.end(), hull.end()); #292
184     SegIt it_r1, it_r2;
185     function<bool(const Seg &, const Seg &)> inc_comp(
186         [&dir](const Seg &lft, const Seg &rgt) {
187             return dot(dir, lft.F) < dot(dir, rgt.F);
188         });
189     function<bool(const Seg &, const Seg &)> dec_comp(
190         [&dir](const Seg &lft, const Seg &rgt) {
191             return dot(dir, lft.F) > dot(dir, rgt.F);

```

```

192     });
193     if (it_min <= it_max) { #402
194         it_r1 = upper_bound(it_min, it_max + 1, line, inc_comp) - 1;
195         if (dot(dir, hull.front().F) >= opt_val) {
196             it_r2 =
197                 upper_bound(hull.begin(), it_min + 1, line, dec_comp) - 1;
198         } else {
199             it_r2 = upper_bound(it_max, hull.end(), line, dec_comp) - 1;
200         }
201     } else {
202         it_r1 = upper_bound(it_max, it_min + 1, line, dec_comp) - 1;
203         if (dot(dir, hull.front().F) <= opt_val) { #421
204             it_r2 =
205                 upper_bound(hull.begin(), it_max + 1, line, inc_comp) - 1;
206         } else {
207             it_r2 = upper_bound(it_min, hull.end(), line, inc_comp) - 1;
208         }
209     }
210     return MP(it_r1, it_r2);
211 } %567
212 Seg diameter() { // O(n)
213     Seg res;
214     ll dia_sq = 0;
215     auto it1 = hull.begin();
216     auto it2 = upper_begin;
217     Vec v1 = {hull.back().S.F - hull.back().F.F,
218             hull.back().S.S - hull.back().F.S};
219     while (it2 != hull.begin()) {
220         Vec v2 = {(it2 - 1)->S.F - (it2 - 1)->F.F,
221             (it2 - 1)->S.S - (it2 - 1)->F.S}; #386
222         ll decider = cross(v1, v2);
223         if (decider > 0) break;
224         --it2;
225     }
226     while (it2 != hull.end()) { // check all antipodal pairs
227         if (dist_sq(it1->F, it2->F) > dia_sq) {
228             res = {it1->F, it2->F};
229             dia_sq = dist_sq(res.F, res.S);
230         }
231         Vec v1 = {it1->S.F - it1->F.F, it1->S.S - it1->F.S}; #607
232         Vec v2 = {it2->S.F - it2->F.F, it2->S.S - it2->F.S};
233         ll decider = cross(v1, v2);
234         if (decider == 0) { // report cross pairs at parallel lines.
235             if (dist_sq(it1->S, it2->F) > dia_sq) {
236                 res = {it1->S, it2->F};
237                 dia_sq = dist_sq(res.F, res.S);
238             }
239             if (dist_sq(it1->F, it2->S) > dia_sq) {
240                 res = {it1->F, it2->S};
241                 dia_sq = dist_sq(res.F, res.S); #980
242             }
243             ++it1;
244             ++it2;

```

```

245     } else if (decider < 0) {
246         ++it1;
247     } else {
248         ++it2;
249     }
250 }
251 return res;
252 }
253 };

```

#686

%781

10 Aho Corasick $\mathcal{O}(|\alpha| \sum \text{len})$

```

1 const int alpha_size = 26;
2 struct node {
3     node *nxt[alpha_size]; // May use other structures to move in trie
4     node *suffix;
5     node() { memset(nxt, 0, alpha_size * sizeof(node *)); }
6     int cnt = 0;
7 };
8 node *aho_corasick(vector<vector<char> > &dict) {
9     node *root = new node;
10    root->suffix = 0;
11    vector<pair<vector<char> *, node *> > cur_state;
12    for (vector<char> &s : dict) cur_state.emplace_back(&s, root);
13    for (int i = 0; !cur_state.empty(); ++i) {
14        vector<pair<vector<char> *, node *> > nxt_state;
15        for (auto &cur : cur_state) {
16            node *nxt = cur.second->nxt[(cur.first)[i]];
17            if (nxt) {
18                cur.second = nxt;
19            } else {
20                nxt = new node;
21                cur.second->nxt[(cur.first)[i]] = nxt;
22                node *suf = cur.second->suffix;
23                cur.second = nxt;
24                nxt->suffix = root; // set correct suffix link
25                while (suf) {
26                    if (suf->nxt[(cur.first)[i]]) {
27                        nxt->suffix = suf->nxt[(cur.first)[i]];
28                        break;
29                    }
30                    suf = suf->suffix;
31                }
32            }
33            if (cur.first->size() > i + 1) nxt_state.push_back(cur);
34        }
35        cur_state = nxt_state;
36    }
37    return root;
38 }
39 // auxiliary functions for searching and counting
40 node *walk(node *cur,
41     char c) { // longest prefix in dict that is suffix of walked string.
42     while (true) {
43         if (cur->nxt[c]) return cur->nxt[c];

```

#911

#003

#378

%064

```

44     if (!cur->suffix) return cur;
45     cur = cur->suffix;
46 }
47 }
48 void cnt_matches(node *root, vector<char> &match_in) {
49     node *cur = root;
50     for (char c : match_in) {
51         cur = walk(cur, c);
52         ++cur->cnt;
53     }
54 }
55 void add_cnt(node *root) { // After counting matches propagate ONCE to
56                             // suffixes for final counts
57     vector<node *> to_visit = {root};
58     for (int i = 0; i < to_visit.size(); ++i) {
59         node *cur = to_visit[i];
60         for (int j = 0; j < alpha_size; ++j) {
61             if (cur->nxt[j]) to_visit.push_back(cur->nxt[j]);
62         }
63     }
64     for (int i = to_visit.size() - 1; i > 0; --i)
65         to_visit[i]->suffix->cnt += to_visit[i]->cnt;
66 }
67 int main() { //
68     ↪ http://codeforces.com/group/s3etJR5zZK/contest/212916/problem/4
69     int n, len;
70     scanf("%d %d", &n, &len);
71     vector<char> a(len + 1);
72     scanf("%s", a.data());
73     a.pop_back();
74     for (char &c : a) c -= 'a';
75     vector<vector<char> > dict(n);
76     for (int i = 0; i < n; ++i) {
77         scanf("%d", &len);
78         dict[i].resize(len + 1);
79         scanf("%s", dict[i].data());
80         dict[i].pop_back();
81         for (char &c : dict[i]) c -= 'a';
82     }
83     node *root = aho_corasick(dict);
84     cnt_matches(root, a);
85     add_cnt(root);
86     for (int i = 0; i < n; ++i) {
87         node *cur = root;
88         for (char c : dict[i]) cur = walk(cur, c);
89         printf("%d\n", cur->cnt);
90     }

```

%127

%286

#354

%313

11 Suffix automaton and tree $\mathcal{O}((n + q) \log(|\alpha|))$

```

1 class AutoNode {
2     private:
3     map<char, AutoNode *>
4     nxt_char; // Map is faster than hashtable and unsorted arrays

```

```

5 public:
6     int len; // Length of longest suffix in equivalence class.
7     AutoNode *suf;
8     bool has_nxt(char c) const { return nxt_char.count(c); }
9     AutoNode *nxt(char c) {
10         if (!has_nxt(c)) return NULL;
11         return nxt_char[c];
12     }
13     void set_nxt(char c, AutoNode *node) { nxt_char[c] = node; }
14     AutoNode *split(int new_len, char c) {
15         AutoNode *new_n = new AutoNode;
16         new_n->nxt_char = nxt_char;
17         new_n->len = new_len;
18         new_n->suf = suf;
19         suf = new_n;
20         return new_n;
21     }
22     // Extra functions for matching and counting
23     AutoNode *lower_depth(
24         int depth) { // move to longest suffix of current with a maximum
25                     // length of depth.
26         if (suf->len >= depth) return suf->lower_depth(depth);
27         return this;
28     }
29     AutoNode *walk(char c, int depth,
30         int &match_len) { // move to longest suffix of walked path that is
31                          // a substring
32         match_len = min(match_len,
33             len); // includes depth limit (needed for finding matches)
34         if (has_nxt(c)) { // as suffixes are in classes match_len must
35             ↪ be
36                 // tracked externally
37             ++match_len;
38             return nxt(c)->lower_depth(depth);
39         }
40         if (suf) return suf->walk(c, depth, match_len);
41         return this;
42     }
43     int paths_to_end = 0;
44     void set_as_end() { // All suffixes of current node are marked as
45                       // ending nodes.
46         paths_to_end += 1;
47         if (suf) suf->set_as_end();
48     }
49     bool vis = false;
50     void calc_paths_to_end() { // Call ONCE from ROOT. For each node
51                              // calculates number of ways to reach an
52                              // end node.
53         if (!vis) { // paths_to_end is occurrence count for any strings in
54                     // current suffix equivalence class.
55             vis = true;
56             for (auto cur : nxt_char) {

```

#308

#890
%677

#091

%955

#035

```

57         paths_to_end += cur.second->paths_to_end;
58     }
59 }
60 // Transform into suffix tree of reverse string
61 map<char, AutoNode *> tree_links;
62 int end_dist = 1 << 30;
63 int calc_end_dist() {
64     if (end_dist == 1 << 30) {
65         if (nxt_char.empty()) end_dist = 0;
66         for (auto cur : nxt_char)
67             end_dist = min(end_dist, 1 + cur.second->calc_end_dist());
68     }
69     return end_dist;
70 }
71 bool vis_t = false;
72 void build_suffix_tree(string &s) { // Call ONCE from ROOT.
73     if (!vis_t) {
74         vis_t = true;
75         if (suf)
76             suf->tree_links[s[s.size() - end_dist - suf->len - 1]] = this;
77         for (auto cur : nxt_char) cur.second->build_suffix_tree(s);
78     }
79 }
80 };
81 struct SufAutomaton {
82     AutoNode *last;
83     AutoNode *root;
84     void extend(char new_c) {
85         AutoNode *new_end = new AutoNode;
86         new_end->len = last->len + 1;
87         AutoNode *suf_w_nxt = last;
88         while (suf_w_nxt && !suf_w_nxt->has_nxt(new_c)) {
89             suf_w_nxt->set_nxt(new_c, new_end);
90             suf_w_nxt = suf_w_nxt->suf;
91         }
92         if (!suf_w_nxt) {
93             new_end->suf = root;
94         } else {
95             AutoNode *max_sbstr = suf_w_nxt->nxt(new_c);
96             if (suf_w_nxt->len + 1 == max_sbstr->len) {
97                 new_end->suf = max_sbstr;
98             } else {
99                 AutoNode *eq_sbstr =
100                     max_sbstr->split(suf_w_nxt->len + 1, new_c);
101                 new_end->suf = eq_sbstr;
102                 AutoNode *w_edge_to_eq_sbstr = suf_w_nxt;
103                 while (w_edge_to_eq_sbstr != 0 &&
104                     w_edge_to_eq_sbstr->nxt(new_c) == max_sbstr) {
105                     w_edge_to_eq_sbstr->set_nxt(new_c, eq_sbstr);
106                     w_edge_to_eq_sbstr = w_edge_to_eq_sbstr->suf;
107                 }
108             }
109         }

```

%996

#188

#748

#705

#169


```
#356
%628
```

%034

#787

#448

#722

#459

```

91     cap[u][now[u]] -= res;
92     return res;
93 }
94 }
95 ++now[u];
96 }
97 return 0;
98 }
99 ll calc_max_flow() {
100     prep();
101     ll ans = 0;
102     while (dinic_bfs()) {
103         ll cur = 0;
104         do {
105             cur = dinic_dfs(source, INF);
106             ans += cur;
107         } while (cur > 0);
108     }
109     return ans;
110 }
111 ll flow_on_edge(int edge_index) {
112     assert(edge_index < edges.size());
113     return *edges[edge_index].flow;
114 }
115 };
116 int main() {
117     int n, m;
118     cin >> n >> m;
119     vector<pair<int, pair<int, int> > > graph(m);
120     for (int i = 0; i < m; ++i) {
121         cin >> graph[i].second.first >> graph[i].second.second >>
122             graph[i].first;
123     }
124     ll res = 0;
125     for (auto cur : graph) {
126         auto mf = MaxFlow(cur.second.first,
127             cur.second.second); // arguments source and sink, memory usage
128                                 // 0(largest node index + input size), sink
129                                 // doesn't need to be last index
130         for (int i = 0; i < m; ++i) {
131             if (graph[i].first > cur.first) {
132                 mf.add_edge(graph[i].second.first, graph[i].second.second, 1,
133                     1); // store edge index if care about flow value
134             }
135         }
136         res += mf.calc_max_flow();
137     }
138     cout << res << endl;
139 }

```

13 Min Cost Max Flow with successive dijkstra $\mathcal{O}(\text{flow} \cdot n^2)$

```

1 const int nmax = 1055;
2 const ll inf = 1e14;
3 int t, n, v; // 0 is source, v-1 sink

```

```

4 ll rem_flow[nmax][nmax];
5 // set [x][y] for directed capacity from x to y.
6 ll cost[nmax][nmax]; // set [x][y] for directed cost from x to y. SET
7                       // TO inf IF NOT USED
8 ll min_dist[nmax];
9 int prev_node[nmax];
10 ll node_flow[nmax];
11 bool visited[nmax];
12 ll tot_cost, tot_flow; // output
13 void min_cost_max_flow() {
14     tot_cost = 0; // Does not work with negative cycles.
15     tot_flow = 0;
16     ll sink_pot = 0;
17     min_dist[0] = 0;
18     for (int i = 1; i <= v; ++i) { // incase of no negative edges
19                                     // Bellman-Ford can be removed.
20         min_dist[i] = inf;
21     }
22     for (int i = 0; i < v - 1; ++i) {
23         for (int j = 0; j < v; ++j) {
24             for (int k = 0; k < v; ++k) {
25                 if (rem_flow[j][k] > 0 &&
26                     min_dist[j] + cost[j][k] < min_dist[k])
27                     min_dist[k] = min_dist[j] + cost[j][k];
28             }
29         }
30     }
31     for (int i = 0; i < v; ++i) { // Apply potentials to edge costs.
32         for (int j = 0; j < v; ++j) {
33             if (cost[i][j] != inf) {
34                 cost[i][j] += min_dist[i];
35                 cost[i][j] -= min_dist[j];
36             }
37         }
38     }
39     sink_pot += min_dist[v - 1]; // Bellman-Ford end.
40     while (true) {
41         for (int i = 0; i <= v; ++i) { // node after sink is used as start
42                                         // value for Dijkstra.
43             min_dist[i] = inf;
44             visited[i] = false;
45         }
46         min_dist[0] = 0;
47         node_flow[0] = inf;
48         int min_node;
49         while (true) { // Use Dijkstra to calculate potentials
50             min_node = v;
51             for (int i = 0; i < v; ++i) {
52                 if ((!visited[i]) && min_dist[i] < min_dist[min_node])
53                     min_node = i;
54             }
55             if (min_node == v) break;
56             visited[min_node] = true;
57             for (int i = 0; i < v; ++i) {

```

%576

%927

#040

#630

%849

#782

```

57     if ((!visited[i]) &&
58         min_dist[min_node] + cost[min_node][i] < min_dist[i]) {
59         min_dist[i] = min_dist[min_node] + cost[min_node][i];
60         prev_node[i] = min_node;
61         node_flow[i] =
62             min(node_flow[min_node], rem_flow[min_node][i]);
63     }
64 }
65 }
66 if (min_dist[v - 1] == inf)
67     break for (int i = 0; i < v;
68             ++i) { // Apply potentials to edge costs.
69     for (int j = 0; j < v;
70         ++j) { // Found path from source to sink becomes 0
71                 ↪ cost.
72                 if (cost[i][j] != inf) {
73                     cost[i][j] += min_dist[i];
74                     cost[i][j] -= min_dist[j];
75                 }
76             }
77 sink_pot += min_dist[v - 1];
78 tot_flow += node_flow[v - 1];
79 tot_cost += sink_pot * node_flow[v - 1];
80 int cur = v - 1;
81 while (cur != 0) {
82     // Backtrack along found path that now has 0 cost.
83     rem_flow[prev_node[cur]][cur] -= node_flow[v - 1];
84     rem_flow[cur][prev_node[cur]] += node_flow[v - 1];
85     cost[cur][prev_node[cur]] = 0;
86     if (rem_flow[prev_node[cur]][cur] == 0)
87         cost[prev_node[cur]][cur] = inf;
88     cur = prev_node[cur];
89 }
90 }
91 }
92 int main() { // http://www.spoj.com/problems/GREED/
93     cin >> t;
94     for (int i = 0; i < t; ++i) {
95         cin >> n;
96         for (int j = 0; j < nmax; ++j) {
97             for (int k = 0; k < nmax; ++k) {
98                 cost[j][k] = inf;
99                 rem_flow[j][k] = 0;
100             }
101         }
102         for (int j = 1; j <= n; ++j) {
103             cost[j][2 * n + 1] = 0;
104             rem_flow[j][2 * n + 1] = 1;
105         }
106         for (int j = 1; j <= n; ++j) {
107             int card;
108             cin >> card;
109             ++rem_flow[0][card];

```

#881

#664

#946

%803

```

110     cost[0][card] = 0;
111 }
112 int ex_c;
113 cin >> ex_c;
114 for (int j = 0; j < ex_c; ++j) {
115     int a, b;
116     cin >> a >> b;
117     if (b < a) swap(a, b);
118     cost[a][b] = 1;
119     rem_flow[a][b] = nmax;
120     cost[b][n + b] = 0;
121     rem_flow[b][n + b] = nmax;
122     cost[n + b][a] = 1;
123     rem_flow[n + b][a] = nmax;
124 }
125 v = 2 * n + 2;
126 min_cost_max_flow();
127 cout << tot_cost << '\n';
128 }
129 }

```

14 Min Cost Max Flow with Cycle Cancelling $\mathcal{O}(\text{flow} \cdot nm)$

```

1 struct Network {
2     struct Node;
3     struct Edge {
4         Node *u, *v;
5         int f, c, cost;
6         Node* from(Node* pos) {
7             if (pos == u) return v;
8             return u;
9         }
10        int getCap(Node* pos) {
11            if (pos == u) return c - f;
12            return f;
13        }
14        int addFlow(Node* pos, int toAdd) {
15            if (pos == u) {
16                f += toAdd;
17                return toAdd * cost;
18            } else {
19                f -= toAdd;
20                return -toAdd * cost;
21            }
22        }
23    };
24    struct Node {
25        vector<Edge*> conn;
26        int index;
27    };
28    deque<Node> nodes;
29    deque<Edge> edges;
30    Node* addNode() {
31        nodes.push_back(Node());

```

#145

#987

#057

```

32     nodes.back().index = nodes.size() - 1;
33     return &nodes.back();
34 }
35 Edge* addEdge(Node* u, Node* v, int f, int c, int cost) {
36     edges.push_back({u, v, f, c, cost});
37     u->conn.push_back(&edges.back());
38     v->conn.push_back(&edges.back());
39     return &edges.back();
40 }
41 // Assumes all needed flow has already been added
42 int minCostMaxFlow() {
43     int n = nodes.size();
44     int result = 0;
45     struct State {
46         int p;
47         Edge* used;
48     };
49     while (1) {
50         vector<vector<State> > state(1, vector<State>(n, {0, 0}));
51         for (int lev = 0; lev < n; lev++) {
52             state.push_back(state[lev]);
53             for (int i = 0; i < n; i++) {
54                 if (lev == 0 || state[lev][i].p < state[lev - 1][i].p) {
55                     for (Edge* edge : nodes[i].conn) {
56                         if (edge->getCap(&nodes[i]) > 0) {
57                             int np =
58                                 state[lev][i].p +
59                                 (edge->u == &nodes[i] ? edge->cost : -edge->cost);
60                             int ni = edge->from(&nodes[i])->index;
61                             if (np < state[lev + 1][ni].p) {
62                                 state[lev + 1][ni].p = np;
63                                 state[lev + 1][ni].used = edge;
64                             }
65                         }
66                     }
67                 }
68             }
69         }
70         // Now look at the last level
71         bool valid = false;
72         for (int i = 0; i < n; i++)
73             if (state[n - 1][i].p > state[n][i].p) {
74                 valid = true;
75                 vector<Edge*> path;
76                 int cap = 1000000000;
77                 Node* cur = &nodes[i];
78                 int clev = n;
79                 vector<bool> explr(n, false);
80                 while (!explr[cur->index]) {
81                     explr[cur->index] = true;
82                     State cstate = state[clev][cur->index];
83                     cur = cstate.used->from(cur);
84                     path.push_back(cstate.used);
85                 }

```

#692

#158

#281

#283

#954

```

86     reverse(path.begin(), path.end());
87     {
88         int i = 0;
89         Node* cur2 = cur;
90         do {
91             cur2 = path[i]->from(cur2);
92             i++;
93         } while (cur2 != cur);
94         path.resize(i);
95     }
96     for (auto edge : path) {
97         cap = min(cap, edge->getCap(cur));
98         cur = edge->from(cur);
99     }
100     for (auto edge : path) {
101         result += edge->addFlow(cur, cap);
102         cur = edge->from(cur);
103     }
104 }
105 if (!valid) break;
106 }
107 return result;
108 }
109 };

```

#990

#599

%900

15 DMST $\mathcal{O}(E \log V)$

```

1 struct EdgeDesc {
2     int from, to, w;
3 };
4 struct DMST {
5     struct Node;
6     struct Edge {
7         Node *from;
8         Node *tar;
9         int w;
10        bool inc;
11    };
12    struct Circle {
13        bool vis = false;
14        vector<Edge*> contents;
15        void clean(int idx);
16    };
17    const static greater<pair<ll, Edge*> >
18        comp; // Can use inline static since C++17
19    static vector<Circle> to_process;
20    static bool no_dmst;
21    static Node *root;
22    struct Node {
23        Node *par = NULL;
24        vector<pair<int, int> > out_cands; // Circ, edge idx
25        vector<pair<ll, Edge*> > con;
26        bool in_use = false;
27        ll w = 0; // extra to add to edges in con

```

#186

#478

```

28 Node *anc() {
29     if (!par) return this;
30     while (par->par) par = par->par;
31     return par;
32 }
33 void clean() {
34     if (!no_dmst) {
35         in_use = false;
36         for (auto &cur : out_cands)
37             to_process[cur.first].clean(cur.second);
38     }
39 }
40 Node *con_to_root() {
41     if (anc() == root) return root;
42     in_use = true;
43     Node *super = this; // Will become root or the first Node
44                        // encountered in a loop.
45     while (super == this) {
46         while (
47             !con.empty() && con.front().second->tar->anc() == anc()) {
48             pop_heap(con.begin(), con.end(), comp);
49             con.pop_back();
50         }
51         if (con.empty()) {
52             no_dmst = true;
53             return root;
54         }
55         pop_heap(con.begin(), con.end(), comp);
56         auto nxt = con.back();
57         con.pop_back();
58         w = -nxt.first;
59         if (nxt.second->tar
60             ->in_use) { // anc() wouldn't change anything
61             super = nxt.second->tar->anc();
62             to_process.resize(to_process.size() + 1);
63         } else {
64             super = nxt.second->tar->con_to_root();
65         }
66         if (super != root) {
67             to_process.back().contents.push_back(nxt.second);
68             out_cands.emplace_back(to_process.size() - 1,
69                                   to_process.back().contents.size() - 1);
70         } else { // Clean circles
71             nxt.second->inc = true;
72             nxt.second->from->clean();
73         }
74     }
75     if (super != root) { // we are some loops non first Node.
76         if (con.size() > super->con.size()) {
77             swap(con,
78                 super->con); // Largest con in loop should not be copied.
79             swap(w, super->w);
80         }
81         for (auto cur : con) {
82             super->con.emplace_back(
83                 cur.first - super->w + w, cur.second);
84             push_heap(super->con.begin(), super->con.end(), comp);
85         }
86     }
87     par = super; // root or anc() of first Node encountered in a
88                // loop
89     return super;
90 }
91 };
92 Node *cur_root;
93 vector<Node> graph;
94 vector<Edge> edges;
95 DMST(int n, vector<EdgeDesc> &desc,
96      int r) { // Self loops and multiple edges are okay.
97     graph.resize(n);
98     cur_root = &graph[r];
99     for (auto &cur : desc) // Edges are reversed internally
100         edges.push_back(Edge(&graph[cur.to], &graph[cur.from], cur.w));
101     for (int i = 0; i < desc.size(); ++i)
102         graph[desc[i].to].con.emplace_back(desc[i].w, &edges[i]);
103     for (int i = 0; i < n; ++i)
104         make_heap(graph[i].con.begin(), graph[i].con.end(), comp);
105 }
106 bool find() {
107     root = cur_root;
108     no_dmst = false;
109     for (auto &cur : graph) {
110         cur.con_to_root();
111         to_process.clear();
112         if (no_dmst) return false;
113     }
114     return true;
115 }
116 ll weight() {
117     ll res = 0;
118     for (auto &cur : edges) {
119         if (cur.inc) res += cur.w;
120     }
121     return res;
122 }
123 };
124 void DMST::Circle::clean(int idx) {
125     if (!vis) {
126         vis = true;
127         for (int i = 0; i < contents.size(); ++i) {
128             if (i != idx) {
129                 contents[i]->inc = true;
130                 contents[i]->from->clean();
131             }
132         }
133     }
134 }

```

#995

#405

%732

%477

#711


```

135 const greater<pair<ll, DMST::Edge *> > DMST::comp;
136 vector<DMST::Circle> DMST::to_process;
137 bool DMST::no_dmst;
138 DMST::Node *DMST::root;

```

%771

16 Bridges $\mathcal{O}(n)$

```

1 struct vert;
2 struct edge {
3     bool exists = true;
4     vert *dest;
5     edge *rev;
6     edge(vert *_dest) : dest(_dest) { rev = NULL; }
7     vert &operator*() { return *dest; }
8     vert *operator->() { return dest; }
9     bool is_bridge();
10 };
11 struct vert {
12     deque<edge> con;
13     int val = 0;
14     int seen;
15     int dfs(int upd, edge *ban) { // handles multiple edges
16         if (!val) {
17             val = upd;
18             seen = val;
19             for (edge &nxt : con) {
20                 if (nxt.exists && (&nxt) != ban)
21                     seen = min(seen, nxt->dfs(upd + 1, nxt.rev));
22             }
23         }
24         return seen;
25     }
26     void remove_adj_bridges() {
27         for (edge &nxt : con) {
28             if (nxt.is_bridge()) nxt.exists = false;
29         }
30     }
31     int cnt_adj_bridges() {
32         int res = 0;
33         for (edge &nxt : con) res += nxt.is_bridge();
34         return res;
35     }
36 };
37 bool edge::is_bridge() {
38     return exists &&
39         (dest->seen > rev->dest->val || dest->val < rev->dest->seen);
40 }
41 vert graph[nmax];
42 int main() { // Mechanics Practice BRIDGES
43     int n, m;
44     cin >> n >> m;
45     for (int i = 0; i < m; ++i) {
46         int u, v;
47         scanf("%d %d", &u, &v);
48         graph[u].con.emplace_back(graph + v);

```

#116

#866

%624

%106

%056

%223

```

49     graph[v].con.emplace_back(graph + u);
50     graph[u].con.back().rev = &graph[v].con.back();
51     graph[v].con.back().rev = &graph[u].con.back();
52 }
53 graph[1].dfs(1, NULL);
54 int res = 0;
55 for (int i = 1; i <= n; ++i) res += graph[i].cnt_adj_bridges();
56 cout << res / 2 << endl;
57 }

```

17 2-Sat $\mathcal{O}(n)$ and SCC $\mathcal{O}(n)$

```

1 struct Graph {
2     int n;
3     vector<vector<int> > conn;
4     Graph(int nsize) {
5         n = nsize;
6         conn.resize(n);
7     }
8     void add_edge(int u, int v) { conn[u].push_back(v); }
9     void _topsort_dfs(int pos, vector<int> &result, vector<bool> &explr,
10         vector<vector<int> > &revconn) { // #592
11         if (explr[pos]) return;
12         explr[pos] = true;
13         for (auto next : revconn[pos])
14             _topsort_dfs(next, result, explr, revconn);
15         result.push_back(pos);
16     }
17     vector<int> topsort() {
18         vector<vector<int> > revconn(n);
19         for (int u = 0; u < n; u++) {
20             for (auto v : conn[u]) revconn[v].push_back(u); // #775
21         }
22         vector<int> result;
23         vector<bool> explr(n, false);
24         for (int i = 0; i < n; i++)
25             _topsort_dfs(i, result, explr, revconn);
26         reverse(result.begin(), result.end());
27         return result;
28     }
29     void dfs(int pos, vector<int> &result, vector<bool> &explr) { // #591
30         if (explr[pos]) return;
31         explr[pos] = true;
32         for (auto next : conn[pos]) dfs(next, result, explr);
33         result.push_back(pos); // #603
34     }
35     vector<vector<int> >
36     scc() { // tested on
37         //
38         ↪ https://www.hackerearth.com/practice/algorithms/graphs/strongly
39         vector<int> order = topsort();
40         reverse(order.begin(), order.end());
41         vector<bool> explr(n, false);
42         vector<vector<int> > results;
43         for (auto it = order.rbegin(); it != order.rend(); ++it) {

```

```

43     vector<int> component;
44     _topsort_dfs(*it, component, explr, conn);
45     sort(component.begin(), component.end());           #688
46     results.push_back(component);
47 }
48 sort(results.begin(), results.end());
49 return results;
50 }
51 };                                                    %983
52 // Solution for:
53 // http://codeforces.com/group/PjzGiggT71/contest/221700/problem/C
54 int main() {
55     int n, m;
56     cin >> n >> m;
57     Graph g(2 * m);
58     for (int i = 0; i < n; i++) {
59         int a, sa, b, sb;
60         cin >> a >> sa >> b >> sb;
61         a--, b--;
62         g.add_edge(2 * a + 1 - sa, 2 * b + sb);
63         g.add_edge(2 * b + 1 - sb, 2 * a + sa);
64     }
65     vector<int> state(2 * m, 0);
66     {
67         vector<int> order = g.topsort();
68         vector<bool> explr(2 * m, false);
69         for (auto u : order) {
70             vector<int> traversed;
71             g.dfs(u, traversed, explr);
72             if (traversed.size() > 0 && !state[traversed[0] ^ 1]) {
73                 for (auto c : traversed) state[c] = 1;
74             }
75         }
76     }
77     for (int i = 0; i < m; i++) {
78         if (state[2 * i] == state[2 * i + 1]) {
79             cout << "IMPOSSIBLE\n";
80             return 0;
81         }
82     }
83     for (int i = 0; i < m; i++) {
84         cout << state[2 * i + 1] << '\n';
85     }
86     return 0;
87 }

```

18 Generic persistent compressed lazy segment tree

```

1 struct Seg {
2     ll sum = 0;
3     void recalc(const Seg &lhs_seg, int lhs_len, const Seg &rhs_seg,
4                 int rhs_len) {
5         sum = lhs_seg.sum + rhs_seg.sum;
6     }
7 } __attribute__((packed));

```

```

8 struct Lazy {
9     ll add;
10    ll assign_val; // LLONG_MIN if no assign;           #529
11    void init() {
12        add = 0;
13        assign_val = LLONG_MIN;
14    }
15    Lazy() { init(); }
16    void split(Lazy &lhs_lazy, Lazy &rhs_lazy, int len) {
17        lhs_lazy = *this;
18        rhs_lazy = *this;
19        init();
20    }
21    void merge(Lazy &oth, int len) {
22        if (oth.assign_val != LLONG_MIN) {
23            add = 0;
24            assign_val = oth.assign_val;
25        }
26        add += oth.add;
27    }
28    void apply_to_seg(Seg &cur, int len) const {
29        if (assign_val != LLONG_MIN) {
30            cur.sum = len * assign_val;
31        }
32        cur.sum += len * add;
33    }
34 } __attribute__((packed));
35 struct Node { // Following code should not need to be modified
36     int ver;
37     bool is_lazy = false;
38     Seg seg;
39     Lazy lazy;
40     Node *lc = NULL, *rc = NULL;
41     void init() {
42         if (!lc) {
43             lc = new Node{ver};
44             rc = new Node{ver};
45         }
46     }
47     Node *upd(int L, int R, int l, int r, Lazy &val, int tar_ver) {
48         if (ver != tar_ver) {
49             Node *rep = new Node(*this);
50             rep->ver = tar_ver;
51             return rep->upd(L, R, l, r, val, tar_ver);
52         }
53         if (L >= l && R <= r) {
54             val.apply_to_seg(seg, R - L);
55             lazy.merge(val, R - L);
56             is_lazy = true;
57         } else {
58             init();
59             int M = (L + R) / 2;
60             if (is_lazy) {

```

#953

#204

%625

#313

#138

```

61     Lazy l_val, r_val;
62     lazy.split(l_val, r_val, R - L);
63     lc = lc->upd(L, M, L, M, l_val, ver);
64     rc = rc->upd(M, R, M, R, r_val, ver);
65     is_lazy = false;
66 }
67 Lazy l_val, r_val;
68 val.split(l_val, r_val, R - L);
69 if (l < M) lc = lc->upd(L, M, l, r, l_val, ver);
70 if (M < r) rc = rc->upd(M, R, l, r, r_val, ver);
71 seg.recalc(lc->seg, M - L, rc->seg, R - M);
72 }
73 return this;
74 }
75 void get(int L, int R, int l, int r, Seg *&lft_res, Seg *&tmp,
76 bool last_ver) {
77     if (L >= l && R <= r) {
78         tmp->recalc(*lft_res, L - l, seg, R - L);
79         swap(lft_res, tmp);
80     } else {
81         init();
82         int M = (L + R) / 2;
83         if (is_lazy) {
84             Lazy l_val, r_val;
85             lazy.split(l_val, r_val, R - L);
86             lc = lc->upd(L, M, L, M, l_val, ver + last_ver);
87             lc->ver = ver;
88             rc = rc->upd(M, R, M, R, r_val, ver + last_ver);
89             rc->ver = ver;
90             is_lazy = false;
91         }
92         if (l < M) lc->get(L, M, l, r, lft_res, tmp, last_ver);
93         if (M < r) rc->get(M, R, l, r, lft_res, tmp, last_ver);
94     }
95 }
96 } __attribute__((packed));
97 struct SegTree {
98     // indexes start from 0, ranges are [beg, end)
99     vector<Node *> roots; // versions start from 0
100     int len;
101     SegTree(int _len) : len(_len) { roots.push_back(new Node{0}); }
102     int upd(int l, int r, Lazy &val, bool new_ver = false) {
103         Node *cur_root =
104             roots.back()->upd(0, len, l, r, val, roots.size() - 1, new_ver);
105         if (cur_root != roots.back()) roots.push_back(cur_root);
106         return roots.size() - 1;
107     }
108     Seg get(int l, int r, int ver = -1) {
109         if (ver == -1) ver = roots.size() - 1;
110         Seg seg1, seg2;
111         Seg *pres = &seg1, *ptmp = &seg2;
112         roots[ver]->get(0, len, l, r, pres, ptmp, roots.size() - 1);
113         return *pres;
114 }
115 };

```

#104

#441

#803

#770

#542

```

115 int main() {
116     int n, m; // solves Mechanics Practice LAZY
117     cin >> n >> m;
118     SegTree seg_tree(1 << 17);
119     for (int i = 0; i < n; ++i) {
120         Lazy tmp;
121         scanf("%lld", &tmp.assign_val);
122         seg_tree.upd(i, i + 1, tmp);
123     }
124     for (int i = 0; i < m; ++i) {
125         int o;
126         int l, r;
127         scanf("%d %d %d", &o, &l, &r);
128         --l;
129         if (o == 1) {
130             Lazy tmp;
131             scanf("%lld", &tmp.add);
132             seg_tree.upd(l, r, tmp);
133         } else if (o == 2) {
134             Lazy tmp;
135             scanf("%lld", &tmp.assign_val);
136             seg_tree.upd(l, r, tmp);
137         } else {
138             Seg res = seg_tree.get(l, r);
139             printf("%lld\n", res.sum);
140         }
141     }
142 }

```

19 Templated HLD $\mathcal{O}(M(n) \log n)$ per query

```

1 class dummy {
2 public:
3     dummy() {}
4     dummy(int, int) {}
5     void set(int, int) {}
6     int query(int left, int right) {
7         cout << this << ' ' << left << ' ' << right << endl;
8     }
9 };
10 /* T should be the type of the data stored in each vertex;
11 * DS should be the underlying data structure that is used to perform
12 * the group operation. It should have the following methods:
13 * * DS () - empty constructor
14 * * DS (int size, T initial) - constructs the structure with the
15 * given size, initially filled with initial.
16 * * void set (int index, T value) - set the value at index `index` to
17 * `value`
18 * * T query (int left, int right) - return the "sum" of elements
19 * between left and right, inclusive.
20 */
21 template <typename T, class DS>
22 class HLD {
23     int vertexc;

```

%932

```

24 vector<int> *adj;
25 vector<int> subtree_size;
26 DS structure;
27 DS aux;
28 void build_sizes(int vertex, int parent) {
29     subtree_size[vertex] = 1;
30     for (int child : adj[vertex]) {
31         if (child != parent) {
32             build_sizes(child, vertex);
33             subtree_size[vertex] += subtree_size[child];
34         }
35     }
36 }
37 int cur;
38 vector<int> ord;
39 vector<int> chain_root;
40 vector<int> par;
41 void build_hld(int vertex, int parent, int chain_source) {
42     cur++;
43     ord[vertex] = cur;
44     chain_root[vertex] = chain_source;
45     par[vertex] = parent;
46     if (adj[vertex].size() > 1 ||
47         (vertex == 1 && adj[vertex].size() == 1)) {
48         int big_child, big_size = -1;
49         for (int child : adj[vertex]) {
50             if ((child != parent) && (subtree_size[child] > big_size)) {
51                 ↪ #042
52                 big_child = child;
53                 big_size = subtree_size[child];
54             }
55             build_hld(big_child, vertex, chain_source);
56             for (int child : adj[vertex]) {
57                 if ((child != parent) && (child != big_child))
58                     build_hld(child, vertex, child);
59             }
60         }
61     }
62 public:
63 HLD(int _vertexc) {
64     vertexc = _vertexc;
65     adj = new vector<int>[vertexc + 5];
66 }
67 void add_edge(int u, int v) {
68     adj[u].push_back(v);
69     adj[v].push_back(u);
70 }
71 void build(T initial) {
72     subtree_size = vector<int>(vertexc + 5);
73     ord = vector<int>(vertexc + 5);
74     chain_root = vector<int>(vertexc + 5);
75     par = vector<int>(vertexc + 5);
76     cur = 0;

```

#037

#593

#461

#587

```

77     build_sizes(1, -1);
78     build_hld(1, -1, 1);
79     structure = DS(vertexc + 5, initial);
80     aux = DS(50, initial);
81 }
82 void set(int vertex, int value) {
83     structure.set(ord[vertex], value);
84 }
85 T query_path(
86     int u, int v) { /* returns the "sum" of the path u->v */
87     int cur_id = 0;
88     while (chain_root[u] != chain_root[v]) {
89         if (ord[u] > ord[v]) {
90             cur_id++;
91             aux.set(cur_id, structure.query(ord[chain_root[u]], ord[u]));
92             u = par[chain_root[u]];
93         } else {
94             cur_id++;
95             aux.set(cur_id, structure.query(ord[chain_root[v]], ord[v]));
96             v = par[chain_root[v]];
97         }
98     }
99     cur_id++;
100     aux.set(cur_id,
101             structure.query(min(ord[u], ord[v]), max(ord[u], ord[v])));
102     return aux.query(1, cur_id);
103 }
104 void print() {
105     for (int i = 1; i <= vertexc; i++)
106         cout << i << ' ' << ord[i] << ' ' << chain_root[i] << ' '
107             << par[i] << endl;
108 }
109 };
110 int main() {
111     int vertexc;
112     cin >> vertexc;
113     HLD<int, dummy> hld(vertexc);
114     for (int i = 0; i < vertexc - 1; i++) {
115         int u, v;
116         cin >> u >> v;
117         hld.add_edge(u, v);
118     }
119     hld.build(0);
120     hld.print();
121     int queryc;
122     cin >> queryc;
123     for (int i = 0; i < queryc; i++) {
124         int u, v;
125         cin >> u >> v;
126         hld.query_path(u, v);
127         cout << endl;
128     }
129 }

```

#638

#052

#041

%905

20 Templated multi dimensional BIT $\mathcal{O}(\log(n)^{\text{dim}})$ per query

```

1 // Fully overloaded any dimensional BIT, use any type for coordinates,
2 // elements, return value. Includes coordinate compression.
3 template <typename elem_t, typename coord_t, coord_t n_inf,
4   typename ret_t>
5 class BIT {
6   vector<coord_t> positions;
7   vector<elem_t> elems;
8   bool initiated = false;
9 public:
10  BIT() { positions.push_back(n_inf); }
11  void initiate() {
12      if (initiated) {
13          for (elem_t &c_elem : elems) c_elem.initiate();
14      } else {
15          initiated = true;
16          sort(positions.begin(), positions.end());
17          positions.resize(unique(positions.begin(), positions.end()) -
18                          positions.begin());
19          elems.resize(positions.size());
20      }
21  }
22  template <typename... loc_form>
23  void update(coord_t cord, loc_form... args) {
24      if (initiated) {
25          int pos =
26              lower_bound(positions.begin(), positions.end(), cord) -
27              positions.begin();
28          for (; pos < positions.size(); pos += pos & -pos)
29              elems[pos].update(args...);
30      } else {
31          positions.push_back(cord);
32      }
33  }
34  template <typename... loc_form>
35  ret_t query(coord_t cord,
36             loc_form... args) { // sum in open interval (-inf, cord)
37      ret_t res = 0;
38      int pos = (lower_bound(positions.begin(), positions.end(), cord) -
39                positions.begin()) -
40                1;
41      for (; pos > 0; pos -= pos & -pos)
42          res += elems[pos].query(args...);
43      return res;
44  }
45 };
46 template <typename internal_type>
47 struct wrapped {
48     internal_type a = 0;
49     void update(internal_type b) { a += b; }
50     internal_type query() { return a; }
51     // Should never be called, needed for compilation
52     void initiate() { cerr << 'i' << endl; }

```

#330

#620

#542

#549

```

53 void update() { cerr << 'u' << endl; }
54 };
55 int main() {
56     // return type should be same as type inside wrapped
57     BIT<BIT<wrapped<ll>, int, INT_MIN, ll>, int, INT_MIN, ll> fenwick;
58     int dim = 2;
59     vector<tuple<int, int, ll> > to_insert;
60     to_insert.emplace_back(1, 1, 1);
61     // set up all positions that are to be used for update
62     for (int i = 0; i < dim; ++i) {
63         for (auto &cur : to_insert)
64             fenwick.update(get<0>(cur),
65                             get<1>(cur)); // May include value which won't be used
66     }
67     // actual use
68     for (auto &cur : to_insert)
69         fenwick.update(get<0>(cur), get<1>(cur), get<2>(cur));
70     cout << fenwick.query(2, 2) << '\n';
71 }
72 }

```

21 Treap $\mathcal{O}(\log n)$ per query

```

1 mt19937 randgen;
2 struct Treap {
3     struct Node {
4         int key;
5         int value;
6         unsigned int priority;
7         long long total;
8         Node* lch;
9         Node* rch;
10        Node(int new_key, int new_value) {
11            key = new_key;
12            value = new_value;
13            priority = randgen();
14            total = new_value;
15            lch = 0;
16            rch = 0;
17        }
18        void update() {
19            total = value;
20            if (lch) total += lch->total;
21            if (rch) total += rch->total;
22        }
23    };
24    deque<Node> nodes;
25    Node* root = 0;
26    pair<Node*, Node*> split(int key, Node* cur) {
27        if (cur == 0) return {0, 0};
28        pair<Node*, Node*> result;
29        if (key <= cur->key) {
30            auto ret = split(key, cur->lch);
31            cur->lch = ret.second;

```

#698

#295

#233


```

32     result = {ret.first, cur};
33 } else {
34     auto ret = split(key, cur->rch);
35     cur->rch = ret.first;
36     result = {cur, ret.second};
37 }
38 cur->update();
39 return result;
40 }
41 Node* merge(Node* left, Node* right) {
42     if (left == 0) return right;
43     if (right == 0) return left;
44     Node* top;
45     if (left->priority < right->priority) {
46         left->rch = merge(left->rch, right);
47         top = left;
48     } else {
49         right->lch = merge(left, right->lch);
50         top = right;
51     }
52     top->update();
53     return top;
54 }
55 void insert(int key, int value) {
56     nodes.push_back(Node(key, value));
57     Node* cur = &nodes.back();
58     pair<Node*, Node*> ret = split(key, root);
59     cur = merge(ret.first, cur);
60     cur = merge(cur, ret.second);
61     root = cur;
62 }
63 void erase(int key) {
64     Node *left, *mid, *right;
65     tie(left, mid) = split(key, root);
66     tie(mid, right) = split(key + 1, mid);
67     root = merge(left, right);
68 }
69 long long sum_upto(int key, Node* cur) {
70     if (cur == 0) return 0;
71     if (key <= cur->key) {
72         return sum_upto(key, cur->lch);
73     } else {
74         long long result = cur->value + sum_upto(key, cur->rch);
75         if (cur->lch) result += cur->lch->total;
76         return result;
77     }
78 }
79 long long get(int l, int r) {
80     return sum_upto(r + 1, root) - sum_upto(l, root);
81 }
82 };
83 // Solution for:
84 // http://codeforces.com/group/U01GDa2Gwb/contest/219104/problem/TREAP
85 int main() {

```

#230

#510

#760

#634

#509

%959

```

86 ios_base::sync_with_stdio(false);
87 cin.tie(0);
88 int m;
89 Treap treap;
90 cin >> m;
91 for (int i = 0; i < m; i++) {
92     int type;
93     cin >> type;
94     if (type == 1) {
95         int x, y;
96         cin >> x >> y;
97         treap.insert(x, y);
98     } else if (type == 2) {
99         int x;
100        cin >> x;
101        treap.erase(x);
102    } else {
103        int l, r;
104        cin >> l >> r;
105        cout << treap.get(l, r) << endl;
106    }
107 }
108 return 0;
109 }

```

22 Radixsort 50M 64 bit integers as single array in 1 sec

```

1 typedef unsigned char uchar;
2 template <typename T>
3 void msd_radixsort(
4     T *start, T *sec_start, int arr_size, int d = sizeof(T) - 1) {
5     const int msd_radix_lim = 100;
6     const T mask = 255;
7     int bucket_sizes[256]{};
8     for (T *it = start; it != start + arr_size; ++it) {
9         ++bucket_sizes[((*it) >> (d * 8)) & mask];
10        //++bucket_sizes[*(uchar*)it + d];
11    }
12    T *locs_mem[257];
13    locs_mem[0] = sec_start;
14    T **locs = locs_mem + 1;
15    locs[0] = sec_start;
16    for (int j = 0; j < 255; ++j) {
17        locs[j + 1] = locs[j] + bucket_sizes[j];
18    }
19    for (T *it = start; it != start + arr_size; ++it) {
20        uchar bucket_id = ((*it) >> (d * 8)) & mask;
21        *(locs[bucket_id]++) = *it;
22    }
23    locs = locs_mem;
24    if (d) {
25        T *locs_old[256];
26        locs_old[0] = start;
27        for (int j = 0; j < 255; ++j) {

```

#772

#361

```

28     locs_old[j + 1] = locs_old[j] + bucket_sizes[j];
29 }
30 for (int j = 0; j < 256; ++j) {
31     if (locs[j + 1] - locs[j] < msd_radix_lim) { #867
32         std::sort(locs[j], locs[j + 1]);
33         if (d & 1) {
34             copy(locs[j], locs[j + 1], locs_old[j]);
35         }
36     } else {
37         msd_radixsort(locs[j], locs_old[j], bucket_sizes[j], d - 1);
38     }
39 }
40 }
41 } %225
42 const int nmax = 5e7;
43 ll arr[nmax], tmp[nmax];
44 int main() {
45     for (int i = 0; i < nmax; ++i) arr[i] = ((ll)rand() << 32) | rand();
46     msd_radixsort(arr, tmp, nmax);
47     assert(is_sorted(arr, arr + nmax));
48 }

```

23 FFT 5M length/sec

integer $c = a * b$ is accurate if $c_i < 2^{49}$

```

1 struct Complex {
2     double a = 0, b = 0;
3     Complex &operator/=(const int &oth) {
4         a /= oth;
5         b /= oth;
6         return *this;
7     }
8 };
9 Complex operator+(const Complex &lft, const Complex &rgt) {
10     return Complex{lft.a + rgt.a, lft.b + rgt.b}; #384
11 }
12 Complex operator-(const Complex &lft, const Complex &rgt) {
13     return Complex{lft.a - rgt.a, lft.b - rgt.b};
14 }
15 Complex operator*(const Complex &lft, const Complex &rgt) {
16     return Complex{
17         lft.a * rgt.a - lft.b * rgt.b, lft.a * rgt.b + lft.b * rgt.a;
18     }
19 }
20 Complex conj(const Complex &cur) { return Complex{cur.a, -cur.b}; }
21 void fft_rec(Complex *arr, Complex *root_pow, int len) { #385
22     if (len != 1) {
23         fft_rec(arr, root_pow, len >> 1);
24         fft_rec(arr + len, root_pow, len >> 1);
25     }
26     root_pow += len;
27     for (int i = 0; i < len; ++i) {
28         Complex tmp = arr[i] + root_pow[i] * arr[i + len];
29         arr[i + len] = arr[i] - root_pow[i] * arr[i + len];
30         arr[i] = tmp;

```

```

30     }
31 } #249
32 void fft(vector<Complex> &arr, int ord, bool invert) {
33     assert(arr.size() == 1 << ord);
34     static vector<Complex> root_pow(1);
35     static int inc_pow = 1;
36     static bool is_inv = false;
37     if (inc_pow <= ord) {
38         int idx = root_pow.size();
39         root_pow.resize(1 << ord);
40         for (; inc_pow <= ord; ++inc_pow) { #517
41             for (int idx_p = 0; idx_p < 1 << (ord - 1);
42                 idx_p += 1 << (ord - inc_pow), ++idx) {
43                 root_pow[idx] = Complex{cos(-idx_p * M_PI / (1 << (ord - 1))),
44                     sin(-idx_p * M_PI / (1 << (ord - 1)))};
45                 if (is_inv) root_pow[idx].b = -root_pow[idx].b;
46             }
47         }
48     }
49     if (invert != is_inv) {
50         is_inv = invert; #750
51         for (Complex &cur : root_pow) cur.b = -cur.b;
52     }
53     for (int i = 1, j = 0; i < (1 << ord); ++i) {
54         int m = 1 << (ord - 1);
55         bool cont = true;
56         while (cont) {
57             cont = j & m;
58             j ^= m;
59             m >>= 1;
60         }
61         if (i < j) swap(arr[i], arr[j]);
62     }
63     fft_rec(arr.data(), root_pow.data(), 1 << (ord - 1));
64     if (invert)
65         for (int i = 0; i < (1 << ord); ++i) arr[i] /= (1 << ord); #380
66 }
67 void mult_poly_mod(
68     vector<int> &a, vector<int> &b, vector<int> &c) { // c += a*b
69     static vector<Complex>
70         arr[4]; // correct upto 0.5-2M elements(mod ~= 1e9)
71     if (c.size() < 400) {
72         for (int i = 0; i < a.size(); ++i)
73             for (int j = 0; j < b.size() && i + j < c.size(); ++j)
74                 c[i + j] = ((ll)a[i] * b[j] + c[i + j]) % mod;
75     } else {
76         int fft_ord = 32 - __builtin_clz(c.size()); #629
77         if (arr[0].size() != 1 << fft_ord)
78             for (int i = 0; i < 4; ++i) arr[i].resize(1 << fft_ord);
79         for (int i = 0; i < 4; ++i)
80             fill(arr[i].begin(), arr[i].end(), Complex{});
81         for (int &cur : a)
82             if (cur < 0) cur += mod;

```

```

83 for (int &cur : b)
84     if (cur < 0) cur += mod;
85 const int shift = 15;
86 const int mask = (1 << shift) - 1;
87 for (int i = 0; i < min(a.size(), c.size()); ++i) {
88     arr[0][i].a = a[i] & mask;
89     arr[1][i].a = a[i] >> shift;
90 }
91 for (int i = 0; i < min(b.size(), c.size()); ++i) {
92     arr[0][i].b = b[i] & mask;
93     arr[1][i].b = b[i] >> shift;
94 }
95 for (int i = 0; i < 2; ++i) fft(arr[i], fft_ord, false);
96 for (int i = 0; i < 2; ++i) {
97     for (int j = 0; j < 2; ++j) {
98         int tar = 2 + (i + j) / 2;
99         Complex mult = {0, -0.25};
100         if (i ^ j) mult = {0.25, 0};
101         for (int k = 0; k < (1 << fft_ord); ++k) {
102             int rev_k = ((1 << fft_ord) - k) % (1 << fft_ord);
103             Complex ca = arr[i][k] + conj(arr[i][rev_k]);
104             Complex cb = arr[j][k] - conj(arr[j][rev_k]);
105             arr[tar][k] = arr[tar][k] + mult * ca * cb;
106         }
107     }
108 }
109 for (int i = 2; i < 4; ++i) {
110     fft(arr[i], fft_ord, true);
111     for (int k = 0; k < (int)c.size(); ++k) {
112         c[k] = (c[k] + (((1l)(arr[i][k].a + 0.5) % mod)
113             << (shift * 2 * (i - 2)))) %
114             mod;
115         c[k] = (c[k] + (((1l)(arr[i][k].b + 0.5) % mod)
116             << (shift * (2 * (i - 2) + 1)))) %
117             mod;
118     }
119 }
120 }
121 }

```

#625

#644

#471

#108

%231

24 Fast mod mult, Rabbin Miller prime check, Pollard rho factorization $\mathcal{O}(\sqrt{p})$

```

1 struct ModArithm {
2     ull n;
3     ld rec;
4     ModArithm(ull _n) : n(_n) { // n in [2, 1<<63)
5         rec = 1.0L / n;
6     }
7     ull multf(ull a, ull b) { // a, b in [0, min(2*n, 1<<63))
8         ull mult = (ld)a * b * rec + 0.5L;
9         ll res = a * b - mult * n;
10        if (res < 0) res += n;
11        return res; // in [0, n-1)
12    }

```

#780

```

13 ull sqp1(ull a) { return multf(a, a) + 1; }
14 };
15 ull pow_mod(ull a, ull n, ModArithm &arithm) {
16     ull res = 1;
17     for (ull i = 1; i <= n; i <= 1) {
18         if (n & i) res = arithm.multf(res, a);
19         a = arithm.multf(a, a);
20     }
21     return res;
22 }
23 vector<char> small_primes = {
24     2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
25 bool is_prime(ull n) { // n <= 1<<63, 1M rand/s
26     ModArithm arithm(n);
27     if (n == 2 || n == 3) return true;
28     if (!(n & 1) || n == 1) return false;
29     ull s = __builtin_ctz(n - 1);
30     ull d = (n - 1) >> s;
31     for (ull a : small_primes) {
32         if (a >= n) break;
33         a = pow_mod(a, d, arithm);
34         if (a == 1 || a == n - 1) continue;
35         for (ull r = 1; r < s; ++r) {
36             a = arithm.multf(a, a);
37             if (a == 1) return false;
38             if (a == n - 1) break;
39         }
40         if (a != n - 1) return false;
41     }
42     return true;
43 }
44 ll pollard_rho(ll n) {
45     ModArithm arithm(n);
46     int cum_cnt = 64 - __builtin_clz(n);
47     cum_cnt *= cum_cnt / 5 + 1;
48     while (true) {
49         ll lv = rand() % n;
50         ll v = arithm.sqp1(lv);
51         int idx = 1;
52         int tar = 1;
53         while (true) {
54             ll cur = 1;
55             ll v_cur = v;
56             int j_stop = min(cum_cnt, tar - idx);
57             for (int j = 0; j < j_stop; ++j) {
58                 cur = arithm.multf(cur, abs(v_cur - lv));
59                 v_cur = arithm.sqp1(v_cur);
60                 ++idx;
61             }
62             if (!cur) {
63                 for (int j = 0; j < cum_cnt; ++j) {
64                     ll g = __gcd(abs(v - lv), n);
65                     if (g == 1) {

```

%493

%144

#402

#806

%975

#290

#912

```

66     v = arithm.sqp1(v);
67     } else if (g == n) {
68         break;
69     } else {
70         return g;
71     }
72 }
73 break;
74 } else {
75     ll g = __gcd(cur, n);
76     if (g != 1) return g;
77 }
78 v = v_cur;
79 idx += j_stop;
80 if (idx == tar) {
81     lv = v;
82     tar *= 2;
83     v = arithm.sqp1(v);
84     ++idx;
85 }
86 }
87 }
88 }
89 map<ll, int> prime_factor(ll n,
90 map<ll, int> *res = NULL) { // n <= 1<<61, ~1000/s (<500/s on CF)
91     if (!res) {
92         map<ll, int> res_act;
93         for (int p : small_primes) {
94             while (!(n % p)) {
95                 ++res_act[p];
96                 n /= p;
97             }
98         }
99         if (n != 1) prime_factor(n, &res_act);
100         return res_act;
101     }
102     if (is_prime(n)) {
103         ++(*res)[n];
104     } else {
105         ll factor = pollard_rho(n);
106         prime_factor(factor, res);
107         prime_factor(n / factor, res);
108     }
109     return map<ll, int>();
110 } // Usage: fact = prime_factor(n);

```

#208
#174
%542
#612
#350
%477

25 Symmetric Submodular Functions; Queyrannes's algorithm

SSF: such function $f : V \rightarrow R$ that satisfies $f(A) = f(V/A)$ and for all $x \in V, X \subseteq Y \subseteq V$ it holds that $f(X+x) - f(X) \leq f(Y+x) - f(Y)$. **Hereditary family:** such set $I \subseteq 2^V$ so that $X \subset Y \wedge Y \in I \Rightarrow X \in I$. **Loop:** such $v \in V$ so that $v \notin I$.

```

def minimize():
    s = merge_all_loops()
    while size >= 3:
        t, u = find_pp()

```

```

    {u} is a possible minimizer
    tu = merge(t, u)
    if tu not in I:
        s = merge(tu, s)
    for x in V:
        {x} is a possible minimizer
def find_pp():
    W = {s} # s as in minimizer()
    todo = V/W
    ord = []
    while len(todo) > 0:
        x = min(todo, key=lambda x: f(W+{x}) - f({x}))
        W += {x}
        todo -= {x}
        ord.append(x)
    return ord[-1], ord[-2]
def enum_all_minimal_minimizers(X):
    # X is a inclusionwise minimal minimizer
    s = merge(s, X)
    yield X
    for {v} in I:
        if f({v}) == f(X):
            yield X
            s = merge(v, s)
    while size(V) >= 3:
        t, u = find_pp()
        tu = merge(t, u)
        if tu not in I:
            s = merge(tu, s)
        elif f({tu}) = f(X):
            yield tu
            s = merge(tu, s)

```