

# University of Tartu ICPC Team Notebook

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- 9 Suffix automaton  $\mathcal{O}((n+q) \log(|\alpha|))$
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- 19 Templated multi dimensional BIT  $\mathcal{O}(\log(n)^{\text{dim}})$  per query
- 20 Treap  $\mathcal{O}(\log n)$  per query
- 21 FFT 5M length/sec

## 22 Rabbin Miller prime check

22

### 1 Setup

```
1 set smartindent cindent
2 set ts=4 sw=4 expandtab
3 syntax enable
4 set clipboard=unnamedplus
5 "colorscheme elflord
6 "setxkbmap -option caps:escape
7 "setxkbmap -option
8 "valgrind --vgdb-error=0 ./a <inp &
9 "gdb a
10 "target remote | vgdb
```

### 2 crc.sh

```
1 #!/bin/enubash
2 starts=$(sed '/~\s*/d' $1 | grep -n "//\!start" | cut -f1 -d:)
3 finishes=$(sed '/~\s*/d' $1 | grep -n "//\!finish" | cut -f1 -d:)
4 for ((i=0;i<${#starts[@]};i++)); do
5     for j in `seq 10 10 ${((finishes[i]-starts[i]+8))}`; do
6         sed '/~\s*/d' $1 | head -${((finishes[i]-1))} | tail
7         ↪ -${((finishes[i]-starts[i]-1))} | \
8         head -$j | tr -d '[:space:]' | cksum | cut -f1 -d ' ' | tail -c
9         ↪ 4
10     done #whistespaces don't matter
11     echo #there shouldn't be any comments in the checked range
12 done #check last number in each block
```

### 3 gcc ordered set

```
1 #include <bits/stdc++.h>
2 typedef long long ll;
3 using namespace std;
4 #include <ext/pb_ds/assoc_container.hpp>
5 #include <ext/pb_ds/tree_policy.hpp>
6 using namespace __gnu_pbds;
7 template <typename T>
8 using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
9     ↪ tree_order_statistics_node_update>;
10 int main(){
11     ordered_set<int> cur;
12     cur.insert(1);
13     cur.insert(3);
14     cout << cur.order_of_key(2) << endl; // the number of elements in the
15     ↪ set less than 2
16     cout << *cur.find_by_order(0) << endl; // the 0-th smallest number in
17     ↪ the set(0-based)
18     cout << *cur.find_by_order(1) << endl; // the 1-th smallest number in
19     ↪ the set(0-based)
20 }
21
```

#221

%574

#### 4 Numerical integration with Simpson's rule

```

1 //computing power = how many times function integrate gets called
2 template<typename T>
3 double simps(T f, double a, double b) {
4     return (f(a) + 4*f((a+b)/2) + f(b))*(b-a)/6;
5 }
6 template<typename T>
7 double integrate(T f, double a, double b, double computing_power){
8     double m = (a+b)/2;
9     double l = simps(f,a,m), r = simps(f,m,b), tot=simps(f,a,b);
10    if (computing_power < 1) return tot;
11    return integrate(f, a, m, computing_power/2) + integrate(f, m, b,
12        computing_power/2);

```

#430  
%360

#### 5 Triangle centers

```

1 const double min_delta = 1e-13;
2 const double coord_max = 1e6;
3 typedef complex < double > point;
4 point A, B, C; // vertices of the triangle
5 bool collinear(){
6     double min_diff = min(abs(A - B), min(abs(A - C), abs(B - C)));
7     if(min_diff < coord_max * min_delta)
8         return true;
9     point sp = (B - A) / (C - A);
10    double ang = M_PI/2-abs(abs(arg(sp))-M_PI/2); //positive angle with
11        the real line
12    return ang < min_delta;
13 }
14 point circum_center(){
15     if(collinear())
16         return point(NAN,NAN);
17     //squared lengths of sides
18     double a2, b2, c2;
19     a2 = norm(B - C);
20     b2 = norm(A - C);
21     c2 = norm(A - B);
22     //barycentric coordinates of the circumcenter
23     double c_A, c_B, c_C;
24     c_A = a2 * (b2 + c2 - a2); //sin(2 * alpha) may be used as well
25     c_B = b2 * (a2 + c2 - b2);
26     c_C = c2 * (a2 + b2 - c2);
27     double sum = c_A + c_B + c_C;
28     c_A /= sum;
29     c_B /= sum;
30     c_C /= sum;
31     // cartesian coordinates of the circumcenter
32     return c_A * A + c_B * B + c_C * C;
33 }
34 point centroid(){ //center of mass
35     return (A + B + C) / 3.0;
36 }
37 point ortho_center(){ //euler line
38     point O = circum_center();

```

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#385

%742

```

38 return O + 3.0 * (centroid() - O);
39 };
40 point nine_point_circle_center(){ //euler line
41     point O = circum_center();
42     return O + 1.5 * (centroid() - O);
43 };
44 point in_center(){
45     if(collinear())
46         return point(NAN,NAN);
47     double a, b, c; //side lengths
48     a = abs(B - C);
49     b = abs(A - C);
50     c = abs(A - B);
51     //trilinear coordinates are (1,1,1)
52     //barycentric coordinates
53     double c_A = a, c_B = b, c_C = c;
54     double sum = c_A + c_B + c_C;
55     c_A /= sum;
56     c_B /= sum;
57     c_C /= sum;
58     // cartesian coordinates of the incenter
59     return c_A * A + c_B * B + c_C * C;
60 }

```

#193  
%031

#157

%980

#### 6 2D line segment

```

1 const long double PI = acos(-1.0L);
2 struct Vec {
3     long double x, y;
4     Vec& operator-=(Vec r) {
5         x -= r.x, y -= r.y;
6         return *this;
7     }
8     Vec operator-(Vec r) {return Vec(*this) -= r;}
9     Vec& operator+=(Vec r) {
10         x += r.x, y += r.y;
11         return *this;
12     }
13     Vec operator+(Vec r) {return Vec(*this) += r;}
14     Vec operator-() {return {-x, -y};}
15     Vec& operator*=(long double r) {
16         x *= r, y *= r;
17         return *this;
18     }
19     Vec operator*(long double r) {return Vec(*this) *= r;}
20     Vec& operator/=(long double r) {
21         x /= r, y /= r;
22         return *this;
23     }
24     Vec operator/(long double r) {return Vec(*this) /= r;}
25     long double operator*(Vec r) {
26         return x * r.x + y * r.y;
27     }
28 };

```

#054

#673

```

29 ostream& operator<<(ostream& l, Vec r) {
30     return l << '(' << r.x << ", " << r.y << ')';
31 }
32 long double len(Vec a) {
33     return hypot(a.x, a.y);
34 }
35 long double cross(Vec l, Vec r) {
36     return l.x * r.y - l.y * r.x;
37 }
38 long double angle(Vec a) {
39     return fmod(atan2(a.y, a.x)+2*PI, 2*PI);
40 }
41 Vec normal(Vec a) {
42     return Vec(-a.y, a.x) / len(a);
43 }
44
45
46 struct Segment {
47     Vec a, b;
48     Vec d() {
49         return b-a;
50     }
51 };
52 ostream& operator<<(ostream& l, Segment r) {
53     return l << r.a << '-' << r.b;
54 }
55 Vec intersection(Segment l, Segment r) {
56     Vec dl = l.d(), dr = r.d();
57     if(cross(dl, dr) == 0)
58         return {nanl(""), nanl("")};
59     long double h = cross(dr, l.a-r.a) / len(dr);
60     long double dh = cross(dr, dl) / len(dr);
61     return l.a + dl * (h / -dh);
62 }
63 //Returns the area bounded by halfplanes
64 long double getArea(vector<Segment> lines) {
65     long double lowerbound = -HUGE_VALL, upperbound = HUGE_VALL;
66     vector<Segment> linesBySide[2];
67     for(auto line : lines) {
68         if(line.b.y == line.a.y) {
69             if(line.a.x < line.b.x) {
70                 lowerbound = max(lowerbound, line.a.y);
71             } else {
72                 upperbound = min(upperbound, line.a.y);
73             }
74         } else if(line.a.y < line.b.y) {
75             linesBySide[1].push_back(line);
76         } else {
77             linesBySide[0].push_back({line.b, line.a});
78         }
79     }
80     sort(linesBySide[0].begin(), linesBySide[0].end(), [](Segment l,
81         Segment r) {
82         if(cross(l.d(), r.d()) == 0) return normal(l.d())*l.a >
83             normal(r.d())*r.a;

```

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#049

```

37     return cross(l.d(), r.d()) < 0;
38 });
39 sort(linesBySide[1].begin(), linesBySide[1].end(), [](Segment l,
40     Segment r) {
41     if(cross(l.d(), r.d()) == 0) return normal(l.d())*l.a <
42         normal(r.d())*r.a;
43     return cross(l.d(), r.d()) > 0;
44 });
45 //Now find the application area of the lines and clean up redundant
46     ones
47 vector<long double> applyStart[2];
48 for(int side = 0; side < 2; side++) {
49     vector<long double> &apply = applyStart[side];
50     vector<Segment> curLines;
51     for(auto line : linesBySide[side]) {
52         while(curLines.size() > 0) {
53             Segment other = curLines.back();
54             if(cross(line.d(), other.d()) != 0) {
55                 long double start = intersection(line, other).y;
56                 if(start > apply.back()) break;
57             }
58             curLines.pop_back();
59             apply.pop_back();
60         }
61         if(curLines.size() == 0) {
62             apply.push_back(-HUGE_VALL);
63         } else {
64             apply.push_back(intersection(line, curLines.back()).y);
65         }
66         curLines.push_back(line);
67     }
68     linesBySide[side] = curLines;
69 }
70 applyStart[0].push_back(HUGE_VALL);
71 applyStart[1].push_back(HUGE_VALL);
72 long double result = 0;
73 {
74     long double lb = -HUGE_VALL, ub;
75     for(int i=0, j=0; i < (int)linesBySide[0].size() && j <
76         (int)linesBySide[1].size(); lb = ub) {
77         ub = min(applyStart[0][i+1], applyStart[1][j+1]);
78         long double alb = lb, aub = ub;
79         Segment l0 = linesBySide[0][i], l1 = linesBySide[1][j];
80         if(cross(l1.d(), l0.d()) > 0) {
81             alb = max(alb, intersection(l0, l1).y);
82         } else if(cross(l1.d(), l0.d()) < 0) {
83             aub = min(aub, intersection(l0, l1).y);
84         }
85         alb = max(alb, lowerbound);
86         aub = min(aub, upperbound);
87         aub = max(aub, alb);
88         {
89             long double x1 = l0.a.x + (alb - l0.a.y) / l0.d().y * l0.d().x;

```

#434

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#060

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```

86     long double x2 = 10.a.x + (aub - 10.a.y) / 10.d().y * 10.d().x;
87     result -= (aub - alb) * (x1 + x2) / 2;
88 }
89 {
90     long double x1 = 11.a.x + (alb - 11.a.y) / 11.d().y * 11.d().x;
91     long double x2 = 11.a.x + (aub - 11.a.y) / 11.d().y * 11.d().x;
92     result += (aub - alb) * (x1 + x2) / 2; #228
93 }
94 if(applyStart[0][i+1] < applyStart[1][j+1]) {
95     i++;
96 } else {
97     j++;
98 }
99 }
100 }
101 return result;
102 } %011

```

## 7 Convex polygon algorithms

```

1 ll dot(const pair< int, int > &v1, const pair< int, int > &v2) {
2     return (ll)v1.first * v2.first + (ll)v1.second * v2.second;
3 }
4 ll cross(const pair< int, int > &v1, const pair< int, int > &v2) {
5     return (ll)v1.first * v2.second - (ll)v2.first * v1.second;
6 }
7 ll dist_sq(const pair< int, int > &p1, const pair< int, int > &p2) {
8     return (ll)(p2.first - p1.first) * (p2.first - p1.first) +
9         (ll)(p2.second - p1.second) * (p2.second - p1.second);
10 } %025
11 struct Hull {
12     vector< pair< pair< int, int >, pair< int, int > > > hull;
13     vector< pair< pair< int, int >, pair< int, int > > >::iterator
14     ↪ upper_begin;
15     template < typename Iterator >
16     void extend_hull(Iterator begin, Iterator end) { // O(n)
17         vector< pair< int, int > > res;
18         for (auto it = begin; it != end; ++it) {
19             if (res.empty() || *it != res.back()) {
20                 while (res.size() >= 2) {
21                     auto v1 = make_pair(res[res.size() - 1].first -
22                                         ↪ res[res.size() - 2].first, #048
23                                         res[res.size() - 1].second -
24                                         ↪ res[res.size() - 2].second);
25                     auto v2 = make_pair(it->first - res[res.size() - 2].first,
26                                         it->second - res[res.size() - 2].second);
27                     if (cross(v1, v2) > 0)
28                         break;
29                     res.pop_back();
30                 }
31                 res.push_back(*it);
32             }
33         }
34     }
35     for (int i = 0; i < res.size() - 1; ++i)
36         hull.emplace_back(res[i], res[i + 1]);

```

```

33 }
34 Hull(vector< pair< int, int > > &vert) { // at least 2 distinct
35     ↪ points
36     sort(vert.begin(), vert.end()); // O(n log(n))
37     extend_hull(vert.begin(), vert.end());
38     int diff = hull.size();
39     extend_hull(vert.rbegin(), vert.rend());
40     upper_begin = hull.begin() + diff; %873
41 }
42 bool contains(pair< int, int > p) { // O(log(n))
43     if (p < hull.front().first || p > upper_begin->first) return false;
44     {
45         auto it_low = lower_bound(hull.begin(), upper_begin,
46                                     make_pair(make_pair(p.first,
47                                     ↪ (int)-2e9), make_pair(0, 0)));
48         if (it_low != hull.begin())
49             --it_low;
50         auto v1 = make_pair(it_low->second.first - it_low->first.first,
51                             it_low->second.second -
52                             ↪ it_low->first.second);
53         auto v2 = make_pair(p.first - it_low->first.first, p.second -
54                             ↪ it_low->first.second); #094
55         if (cross(v1, v2) < 0) // < 0 is inclusive, <= 0 is exclusive
56             return false;
57     }
58     {
59         auto it_up = lower_bound(hull.rbegin(), hull.rbegin() +
60                                     ↪ (hull.end() - upper_begin),
61                                     make_pair(make_pair(p.first, (int)2e9),
62                                     ↪ make_pair(0, 0)));
63         if (it_up - hull.rbegin() == hull.end() - upper_begin)
64             --it_up;
65         auto v1 = make_pair(it_up->first.first - it_up->second.first,
66                             it_up->first.second - it_up->second.second);
67         ↪ #900
68         auto v2 = make_pair(p.first - it_up->second.first, p.second -
69                             ↪ it_up->second.second);
70         if (cross(v1, v2) > 0) // > 0 is inclusive, >= 0 is exclusive
71             return false;
72     }
73     return true;
74 } %092
75 template < typename T > // The function can have only one local min
76     ↪ and max and may be constant
77     // only at min and max.
78     vector< pair< pair< int, int >, pair< int, int > > >::iterator max(
79         function< T(const pair< pair< int, int >, pair< int, int > > &) >
80         ↪ f) { // O(log(n))
81         auto l = hull.begin();
82         auto r = hull.end();
83         vector< pair< pair< int, int >, pair< int, int > > >::iterator best
84         ↪ = hull.end();
85         T best_val;

```

```

75 while (r - l > 2) {
76     auto mid = l + (r - l) / 2;
77     T l_val = f(*l);
78     T l_nxt_val = f(*(l + 1));
79     T mid_val = f(*mid);
80     T mid_nxt_val = f(*(mid + 1));
81     if (best == hull.end() ||
82         l_val > best_val) { // If max is at l we may remove it from
83         ↪ the range.
84         best = l;
85         best_val = l_val;
86     }
87     if (l_nxt_val > l_val) {
88         if (mid_val < l_val) {
89             r = mid;
90         } else {
91             if (mid_nxt_val > mid_val) {
92                 l = mid + 1;
93             } else {
94                 r = mid + 1;
95             }
96         }
97     } else {
98         if (mid_val < l_val) {
99             l = mid + 1;
100         } else {
101             if (mid_nxt_val > mid_val) {
102                 l = mid + 1;
103             } else {
104                 r = mid + 1;
105             }
106         }
107     }
108     T l_val = f(*l);
109     if (best == hull.end() || l_val > best_val) {
110         best = l;
111         best_val = l_val;
112     }
113     if (r - l > 1) {
114         T l_nxt_val = f(*(l + 1));
115         if (best == hull.end() || l_nxt_val > best_val) {
116             best = l + 1;
117             best_val = l_nxt_val;
118         }
119     }
120     return best;
121 }
122 vector< pair< pair< int, int >, pair< int, int > >::iterator
123 ↪ closest(
124     pair< int, int >
125     p) { // p can't be internal(can be on border), hull must
126     ↪ have atleast 3 points

```

#242

#012

#373

#332

#930

%331

```

125 const pair< pair< int, int >, pair< int, int > > &ref_p =
126     ↪ hull.front(); // O(log(n))
127 return max(function< double(const pair< pair< int, int >, pair<
128     ↪ int, int > > &) >(&p, &ref_p)(const pair< pair< int, int >, pair< int, int > >
129     ↪ &seg) { // accuracy of used type should be
130     ↪ coord^2
131     if (p == seg.first) return 10 - M_PI;
132     auto v1 =
133         make_pair(seg.second.first - seg.first.first,
134         ↪ seg.second.second - seg.first.second);
135     auto v2 = make_pair(p.first - seg.first.first, p.second -
136     ↪ seg.first.second);
137     ll cross_prod = cross(v1, v2);
138     if (cross_prod > 0) { // order the backside by angle
139         auto v1 = make_pair(ref_p.first.first - p.first,
140         ↪ ref_p.first.second - p.second);
141         auto v2 = make_pair(seg.first.first - p.first,
142         ↪ seg.first.second - p.second);
143         ll dot_prod = dot(v1, v2);
144         ll cross_prod = cross(v2, v1);
145         return atan2(cross_prod, dot_prod) / 2;
146     }
147     ll dot_prod = dot(v1, v2);
148     double res = atan2(dot_prod, cross_prod);
149     if (dot_prod <= 0 && res > 0) res = -M_PI;
150     if (res > 0) {
151         res += 20;
152     } else {
153         res = 10 - res;
154     }
155     return res;
156 }));
157 }
158 pair< int, int > forw_tan(pair< int, int > p) { // can't be internal
159     ↪ or on border
160     const pair< pair< int, int >, pair< int, int > > &ref_p =
161     ↪ hull.front(); // O(log(n))
162     auto best_seg = max(function< double(const pair< pair< int, int >,
163     ↪ pair< int, int > > &) >(&p, &ref_p)(const pair< pair< int, int >, pair< int, int > >
164     ↪ &seg) { // accuracy of used type should be
165     ↪ coord^2
166     auto v1 = make_pair(ref_p.first.first - p.first,
167     ↪ ref_p.first.second - p.second);
168     auto v2 = make_pair(seg.first.first - p.first,
169     ↪ seg.first.second - p.second);
170     ll dot_prod = dot(v1, v2);
171     ll cross_prod = cross(v2, v1); // cross(v1, v2) for
172     ↪ back_tan!!!
173     return atan2(cross_prod, dot_prod); // order by signed
174     ↪ angle
175 }));

```

#685

#395

%483

#291



```

163     return best_seg->first;
164 } %850
165 vector< pair< pair< int, int >, pair< int, int > > >::iterator
166   ↪ max_in_dir(
167     pair< int, int > v) { // first is the ans. O(log(n))
168     return max(function< ll(const pair< pair< int, int >, pair< int,
169       ↪ int > > &) >(
170       [&v](const pair< pair< int, int >, pair< int, int > > &seg) {
171         ↪ return dot(v, seg.first); }));
172 }
173 pair< vector< pair< pair< int, int >, pair< int, int > > >::iterator,
174       vector< pair< pair< int, int >, pair< int, int > > >::iterator
175       ↪ > %013
176 intersections(pair< pair< int, int >, pair< int, int > > line) { //
177   ↪ O(log(n))
178   int x = line.second.first - line.first.first;
179   int y = line.second.second - line.first.second;
180   auto dir = make_pair(-y, x);
181   auto it_max = max_in_dir(dir);
182   auto it_min = max_in_dir(make_pair(y, -x));
183   ll opt_val = dot(dir, line.first);
184   if (dot(dir, it_max->first) < opt_val || dot(dir, it_min->first) >
185     ↪ opt_val)
186     return make_pair(hull.end(), hull.end());
187   vector< pair< pair< int, int >, pair< int, int > > >::iterator
188     ↪ it_r1, it_r2; #785
189   function< bool(const pair< pair< int, int >, pair< int, int > > &,
190     const pair< pair< int, int >, pair< int, int > > &)
191     ↪ >
192     inc_comp([&dir](const pair< pair< int, int >, pair< int, int >
193       ↪ > &lft,
194         const pair< pair< int, int >, pair< int, int >
195         ↪ > &rgt) {
196         return dot(dir, lft.first) < dot(dir, rgt.first);
197     });
198   function< bool(const pair< pair< int, int >, pair< int, int > > &,
199     const pair< pair< int, int >, pair< int, int > > &)
200     ↪ >
201     dec_comp([&dir](const pair< pair< int, int >, pair< int, int >
202       ↪ > &lft,
203         const pair< pair< int, int >, pair< int, int >
204         ↪ > &rgt) {
205         return dot(dir, lft.first) > dot(dir, rgt.first);
206     });
207   if (it_min <= it_max) {
208     it_r1 = upper_bound(it_min, it_max + 1, line, inc_comp) - 1;
209     if (dot(dir, hull.front().first) >= opt_val) {
210       it_r2 = upper_bound(hull.begin(), it_min + 1, line, dec_comp) -
211         ↪ 1;
212     } else {
213       it_r2 = upper_bound(it_min, hull.end(), line, inc_comp) - 1;
214     }
215     return make_pair(it_r1, it_r2);
216 } %000
217 pair< pair< int, int >, pair< int, int > > diameter() { // O(n)
218   pair< pair< int, int >, pair< int, int > > res;
219   ll dia_sq = 0;
220   auto it1 = hull.begin();
221   auto it2 = upper_begin;
222   auto v1 = make_pair(hull.back().second.first -
223     ↪ hull.back().first.first,
224     hull.back().second.second -
225     ↪ hull.back().first.second);
226   while (it2 != hull.begin()) {
227     auto v2 = make_pair((it2 - 1)->second.first - (it2 -
228       ↪ 1)->first.first,
229       (it2 - 1)->second.second - (it2 -
230         ↪ 1)->first.second); #671
231     ll decider = cross(v1, v2);
232     if (decider > 0) break;
233     --it2;
234 }
235 while (it2 != hull.end()) { // check all antipodal pairs
236   if (dist_sq(it1->first, it2->first) > dia_sq) {
237     res = make_pair(it1->first, it2->first);
238     dia_sq = dist_sq(res.first, res.second);
239   }
240   auto v1 =
241     make_pair(it1->second.first - it1->first.first,
242     ↪ it1->second.second - it1->first.second); #674
243   auto v2 =
244     make_pair(it2->second.first - it2->first.first,
245     ↪ it2->second.second - it2->first.second);
246   ll decider = cross(v1, v2);
247   if (decider == 0) { // report cross pairs at parallel lines.
248     if (dist_sq(it1->second, it2->first) > dia_sq) {
249       res = make_pair(it1->second, it2->first);
250       dia_sq = dist_sq(res.first, res.second);
251     }
252     if (dist_sq(it1->first, it2->second) > dia_sq) { #466
253       res = make_pair(it1->first, it2->second);
254       dia_sq = dist_sq(res.first, res.second);
255     }
256     ++it1;
257     ++it2;
258   } else if (decider < 0) {
259     ++it1;

```

```

202   it_r1 = upper_bound(it_max, it_min + 1, line, dec_comp) - 1;
203   if (dot(dir, hull.front().first) <= opt_val) {
204     it_r2 = upper_bound(hull.begin(), it_max + 1, line, inc_comp) -
205       ↪ 1;
206   } else {
207     it_r2 = upper_bound(it_min, hull.end(), line, inc_comp) - 1;
208   }
209   return make_pair(it_r1, it_r2);
210 } %000
211 pair< pair< int, int >, pair< int, int > > diameter() { // O(n)
212   pair< pair< int, int >, pair< int, int > > res;
213   ll dia_sq = 0;
214   auto it1 = hull.begin();
215   auto it2 = upper_begin;
216   auto v1 = make_pair(hull.back().second.first -
217     ↪ hull.back().first.first,
218     hull.back().second.second -
219     ↪ hull.back().first.second);
220   while (it2 != hull.begin()) {
221     auto v2 = make_pair((it2 - 1)->second.first - (it2 -
222       ↪ 1)->first.first,
223       (it2 - 1)->second.second - (it2 -
224         ↪ 1)->first.second); #671
225     ll decider = cross(v1, v2);
226     if (decider > 0) break;
227     --it2;
228 }
229 while (it2 != hull.end()) { // check all antipodal pairs
230   if (dist_sq(it1->first, it2->first) > dia_sq) {
231     res = make_pair(it1->first, it2->first);
232     dia_sq = dist_sq(res.first, res.second);
233   }
234   auto v1 =
235     make_pair(it1->second.first - it1->first.first,
236     ↪ it1->second.second - it1->first.second); #674
237   auto v2 =
238     make_pair(it2->second.first - it2->first.first,
239     ↪ it2->second.second - it2->first.second);
240   ll decider = cross(v1, v2);
241   if (decider == 0) { // report cross pairs at parallel lines.
242     if (dist_sq(it1->second, it2->first) > dia_sq) {
243       res = make_pair(it1->second, it2->first);
244       dia_sq = dist_sq(res.first, res.second);
245     }
246     if (dist_sq(it1->first, it2->second) > dia_sq) { #466
247       res = make_pair(it1->first, it2->second);
248       dia_sq = dist_sq(res.first, res.second);
249     }
250     ++it1;
251     ++it2;
252   } else if (decider < 0) {
253     ++it1;

```

```

248     } else {
249         ++it2;
250     }
251 }
252 return res;
253 }
254 };

```

#502  
%215

### 8 Aho Corasick $\mathcal{O}(|\alpha| \sum \text{len})$

```

1 const int alpha_size=26;
2 struct node{
3     node *nxt[alpha_size]; //May use other structures to move in trie
4     node *suffix;
5     node(){
6         memset(nxt, 0, alpha_size*sizeof(node *));
7     }
8     int cnt=0;
9 };
10 node *aho_corasick(vector<vector<char> > &dict){
11     node *root= new node;
12     root->suffix = 0;
13     vector<pair<vector<char> *, node *> > cur_state;
14     for(vector<char> &s : dict)
15         cur_state.emplace_back(&s, root);
16     for(int i=0; !cur_state.empty(); ++i){
17         vector<pair<vector<char> *, node *> > nxt_state;
18         for(auto &cur : cur_state){
19             node *nxt=cur.second->nxt[(cur.first)[i]];
20             if(nxt){
21                 cur.second=nxt;
22             }else{
23                 nxt = new node;
24                 cur.second->nxt[(cur.first)[i]] = nxt;
25                 node *suf = cur.second->suffix;
26                 cur.second = nxt;
27                 nxt->suffix = root; //set correct suffix link
28                 while(suf){
29                     if(suf->nxt[(cur.first)[i]]){
30                         nxt->suffix = suf->nxt[(cur.first)[i]];
31                         break;
32                     }
33                     suf=suf->suffix;
34                 }
35             }
36             if(cur.first->size() > i+1)
37                 nxt_state.push_back(cur);
38         }
39         cur_state=nxt_state;
40     }
41     return root;
42 }
43 //auxiliary functions for searching and counting
44 node *walk(node *cur, char c){ //longest prefix in dict that is suffix
45     of walked string.

```

#480  
#888  
#786  
#940  
%064

```

45 while(true){
46     if(cur->nxt[c])
47         return cur->nxt[c];
48     if(!cur->suffix)
49         return cur;
50     cur = cur->suffix;
51 }
52 }
53 void cnt_matches(node *root, vector<char> &match_in){
54     node *cur = root;
55     for(char c : match_in){
56         cur = walk(cur, c);
57         ++cur->cnt;
58     }
59 }
60 void add_cnt(node *root){ //After counting matches propagete ONCE to
61     suffixes for final counts
62     vector<node *> to_visit = {root};
63     for(int i=0; i<to_visit.size(); ++i){
64         node *cur = to_visit[i];
65         for(int j=0; j<alpha_size; ++j){
66             if(cur->nxt[j])
67                 to_visit.push_back(cur->nxt[j]);
68         }
69     }
70     for(int i=to_visit.size()-1; i>0; --i)
71         to_visit[i]->suffix->cnt += to_visit[i]->cnt;
72 }
73 int main(){
74     //http://codeforces.com/group/s3etJR5zZK/contest/212916/problem/4
75     int n, len;
76     scanf("%d %d", &n, &len);
77     vector<char> a(len+1);
78     scanf("%s", a.data());
79     a.pop_back();
80     for(char &c : a)
81         c -= 'a';
82     vector<vector<char> > dict(n);
83     for(int i=0; i<n; ++i){
84         scanf("%d", &len);
85         dict[i].resize(len+1);
86         scanf("%s", dict[i].data());
87         dict[i].pop_back();
88         for(char &c : dict[i])
89             c -= 'a';
90     }
91     node *root = aho_corasick(dict);
92     cnt_matches(root, a);
93     add_cnt(root);
94     for(int i=0; i<n; ++i){
95         node *cur = root;
96         for(char c : dict[i])
97             cur = walk(cur, c);

```

%127  
%286  
#865  
%313

```

96     printf("%d\n", cur->cnt);
97 }
98 }

```

### 9 Suffix automaton $\mathcal{O}((n+q)\log(|\alpha|))$

```

1 class AutoNode {
2 private:
3     map< char, AutoNode * > nxt_char; // Map is faster than hashtable
4     ↪ and unsorted arrays
5 public:
6     int len; //Length of longest suffix in equivalence class.
7     AutoNode *suf;
8     bool has_nxt(char c) const {
9         return nxt_char.count(c);
10    }
11    AutoNode *nxt(char c) {
12        if (!has_nxt(c))
13            return NULL;
14        return nxt_char[c];
15    }
16    void set_nxt(char c, AutoNode *node) {
17        nxt_char[c] = node;
18    }
19    AutoNode *split(int new_len, char c) {
20        AutoNode *new_n = new AutoNode;
21        new_n->nxt_char = nxt_char;
22        new_n->len = new_len;
23        new_n->suf = suf;
24        suf = new_n;
25        return new_n;
26    }
27    // Extra functions for matching and counting
28    AutoNode *lower_depth(int depth) { //move to longest suffix of
29        ↪ current with a maximum length of depth.
30        if (suf->len >= depth)
31            return suf->lower_depth(depth);
32        return this;
33    }
34    AutoNode *walk(char c, int depth, int &match_len) { //move to longest
35        ↪ suffix of walked path that is a substring
36        match_len = min(match_len, len); //includes depth limit(needed for
37        ↪ finding matches)
38        if (has_nxt(c)) { //as suffixes are in classes match_len must be
39        ↪ tracked externally
40            ++match_len;
41            return nxt(c)->lower_depth(depth);
42        }
43        if (suf)
44            return suf->walk(c, depth, match_len);
45        return this;
46    }
47    int paths_to_end = 0;
48    void set_as_end() { //All suffixes of current node are marked as
49        ↪ ending nodes.

```

#486

#952

#795

#152

```

44     paths_to_end = 1;
45     if (suf) suf->set_as_end();
46 }
47 bool vis = false;
48 void calc_paths_to_end() { //Call ONCE from ROOT. For each node
49     ↪ calculates number of ways to reach an end node.
50     if (!vis) { //paths_to_end is ocurence count for any strings in
51     ↪ current suffix equivalence class.
52         vis = true;
53         for (auto cur : nxt_char) {
54             cur.second->calc_paths_to_end();
55             paths_to_end += cur.second->paths_to_end;
56         }
57     }
58 }
59 struct SufAutomaton {
60     AutoNode *last;
61     AutoNode *root;
62     void extend(char new_c) {
63         AutoNode *new_end = new AutoNode;
64         new_end->len = last->len + 1;
65         AutoNode *suf_w_nxt = last;
66         while (suf_w_nxt && !suf_w_nxt->has_nxt(new_c)) {
67             suf_w_nxt->set_nxt(new_c, new_end);
68             suf_w_nxt = suf_w_nxt->suf;
69         }
70         if (!suf_w_nxt) {
71             new_end->suf = root;
72         } else {
73             AutoNode *max_sbstr = suf_w_nxt->nxt(new_c);
74             if (suf_w_nxt->len + 1 == max_sbstr->len) {
75                 new_end->suf = max_sbstr;
76             } else {
77                 AutoNode *eq_sbstr = max_sbstr->split(suf_w_nxt->len + 1,
78                 ↪ new_c);
79                 new_end->suf = eq_sbstr
80                 AutoNode *w_edge_to_eq_sbstr = suf_w_nxt;
81                 while (w_edge_to_eq_sbstr != 0 &&
82                 ↪ w_edge_to_eq_sbstr->nxt(new_c) == max_sbstr) {
83                     w_edge_to_eq_sbstr->set_nxt(new_c, eq_sbstr);
84                     w_edge_to_eq_sbstr = w_edge_to_eq_sbstr->suf;
85                 }
86             }
87         }
88         last = new_end;
89     }
90     SufAutomaton(string to_suffix) {
91         root = new AutoNode;
92         root->len = 0;
93         root->suf = NULL;
94         last = root;
95         for (char c : to_suffix) extend(c);

```

#738

#885

#873

#881

#935



```

93 }
94 }; %543
1 #include <bits/stdc++.h>
2 using namespace std;
3 typedef long long ll; #section{Dinic}
4
5 struct MaxFlow{
6     typedef long long ll;
7     const ll INF = 1e18;
8     struct Edge{
9         int u,v;
10        ll c,rc;
11        shared_ptr<ll> flow;
12        Edge(int u, int v, ll c, ll rc = 0):u(u),v(v),c(c),rc(rc){
13        }
14    }; #787
15    struct FlowTracker{
16        shared_ptr<ll> flow;
17        ll cap, rcap;
18        bool dir;
19        FlowTracker(ll _cap, ll _rcap, shared_ptr<ll> _flow, int
        ↪ _dir):cap(_cap),rcap(_rcap),flow(_flow),dir(_dir){ }
20        ll rem() const {
21            if(dir == 0){
22                return cap-*flow;
23            }
24            else{ #844
25                return rcap-*flow;
26            }
27        }
28        void add_flow(ll f){
29            if(dir == 0)
30                *flow += f;
31            else
32                *flow -= f;
33            assert(*flow <= cap);
34            assert(-*flow <= rcap); #287
35        }
36        operator ll() const { return rem(); }
37        void operator--=(ll x){ add_flow(x); }
38        void operator+=(ll x){ add_flow(-x); }
39    };
40    int source,sink;
41    vector<vector<int>> > adj;
42    vector<vector<FlowTracker>> > cap;
43    vector<Edge> edges;
44    MaxFlow(int _source, int _sink):source(_source),sink(_sink){ #080
45        assert(source != sink);
46    }
47    int add_edge(int u, int v, ll c, ll rc = 0){
48        edges.push_back(Edge(u,v,c,rc));
49        return edges.size()-1;
50    }

```

```

51 vector<int> now,lv1;
52 void prep(){
53     int max_id = max(source, sink); #328
54     for(auto edge : edges)
55         max_id = max(max_id, max(edge.u, edge.v));
56     adj.resize(max_id+1);
57     cap.resize(max_id+1);
58     now.resize(max_id+1);
59     lv1.resize(max_id+1);
60     for(auto &edge : edges){
61         auto flow = make_shared<ll>(0);
62         adj[edge.u].push_back(edge.v);
63         cap[edge.u].push_back(FlowTracker(edge.c, edge.rc, flow, 0));
64         if(edge.u != edge.v){ #717
65             adj[edge.v].push_back(edge.u);
66             cap[edge.v].push_back(FlowTracker(edge.c, edge.rc, flow, 1));
67         }
68         assert(cap[edge.u].back() == edge.c);
69         edge.flow = flow;
70     }
71 }
72 bool dinic_bfs(){
73     fill(now.begin(),now.end(),0);
74     fill(lv1.begin(),lv1.end(),0); #038
75     lv1[source] = 1;
76     vector<int> bfs(1,source);
77     for(int i = 0; i < bfs.size(); ++i){
78         int u = bfs[i];
79         for(int j = 0; j < adj[u].size(); ++j){
80             int v = adj[u][j];
81             if(cap[u][j] > 0 && lv1[v] == 0){
82                 lv1[v] = lv1[u]+1;
83                 bfs.push_back(v);
84             }
85         }
86     }
87     return lv1[sink] > 0; #010
88 }
89 ll dinic_dfs(int u, ll flow){
90     if(u == sink)
91         return flow;
92     while(now[u] < adj[u].size()){
93         int v = adj[u][now[u]];
94         if(lv1[v] == lv1[u] + 1 && cap[u][now[u]] != 0){ #014
95             ll res = dinic_dfs(v,min(flow,(ll)cap[u][now[u]]));
96             if(res > 0){
97                 cap[u][now[u]] -= res;
98                 return res;
99             }
100         }
101         ++now[u];
102     }
103     return 0;

```

```

104 }
105 ll calc_max_flow(){
106     prep();
107     ll ans = 0;
108     while(dinic_bfs()){
109         ll cur = 0;
110         do{
111             cur = dinic_dfs(source,INF);
112             ans += cur;
113         }while(cur > 0);
114     }
115     return ans;
116 }
117 ll flow_on_edge(int edge_index){
118     assert(edge_index < edges.size());
119     return *edges[edge_index].flow;
120 }
121 };
122 int main(){
123     int n,m;
124     cin >> n >> m;
125     vector<pair<int, pair<int, int> > > graph(m);
126     for(int i=0; i<m; ++i){
127         cin>>graph[i].second.first>>graph[i].second.second>>graph[i].first;
128     }
129     ll res=0;
130     for(auto cur : graph){
131         auto mf = MaxFlow(cur.second.first,cur.second.second); // arguments
132         ↪ source and sink, memory usage O(largest node index + input
133         ↪ size), sink doesn't need to be last index
134         for(int i = 0; i < m; ++i){
135             if(graph[i].first > cur.first){
136                 mf.add_edge(graph[i].second.first,graph[i].second.second,1,1);
137                 ↪ // store edge index if care about flow value
138             }
139         }
140     }
141     res += mf.calc_max_flow();
142     cout<<res<<endl;
143 }

```

## 10 Min Cost Max Flow with successive dijkstra $\mathcal{O}(\text{flow} \cdot n^2)$

```

1 const int nmax=1055;
2 const ll inf=1e14;
3 int t, n, v; //0 is source, v-1 sink
4 ll rem_flow[nmax][nmax]; //set [x][y] for directed capacity from x to
5 ↪ y.
6 ll cost[nmax][nmax]; //set [x][y] for directed cost from x to y. SET TO
7 ↪ inf IF NOT USED
8 ll min_dist[nmax];
9 int prev_node[nmax];
10 ll node_flow[nmax];
11 bool visited[nmax];
12 ll tot_cost, tot_flow; //output

```

#197

#817

%583

%576

```

11 void min_cost_max_flow(){
12     tot_cost=0; //Does not work with negative cycles.
13     tot_flow=0;
14     ll sink_pot=0;
15     min_dist[0] = 0;
16     for(int i=1; i<=v; ++i){ //incase of no negative edges Bellman-Ford
17         ↪ can be removed.
18         min_dist[i]=inf;
19     }
20     for(int i=0; i<v-1; ++i){
21         for(int j=0; j<v; ++j){
22             for(int k=0; k<v; ++k){
23                 if(rem_flow[j][k] > 0 && min_dist[j]+cost[j][k] < min_dist[k])
24                     min_dist[k] = min_dist[j]+cost[j][k];
25             }
26         }
27     }
28     for(int i=0; i<v; ++i){ //Apply potentials to edge costs.
29         for(int j=0; j<v; ++j){
30             if(cost[i][j]!=inf){
31                 cost[i][j]+=min_dist[i];
32                 cost[i][j]-=min_dist[j];
33             }
34         }
35     }
36     sink_pot+=min_dist[v-1]; //Bellman-Ford end.
37     while(true){
38         for(int i=0; i<=v; ++i){ //node after sink is used as start value
39             ↪ for Dijkstra.
40             min_dist[i]=inf;
41             visited[i]=false;
42         }
43         min_dist[0]=0;
44         node_flow[0]=inf;
45         int min_node;
46         while(true){ //Use Dijkstra to calculate potentials
47             int min_node=v;
48             for(int i=0; i<v; ++i){
49                 if(!visited[i] && min_dist[i]<min_dist[min_node])
50                     min_node=i;
51             }
52             if(min_node==v) break
53             visited[min_node]=true;
54             for(int i=0; i<v; ++i){
55                 if(!visited[i] && min_dist[min_node]+cost[min_node][i] <
56                     ↪ min_dist[i]){
57                     min_dist[i]=min_dist[min_node]+cost[min_node][i];
58                     prev_node[i]=min_node;
59                     node_flow[i]=min(node_flow[min_node], rem_flow[min_node][i]);
60                 }
61             }
62         }
63     }
64     if(min_dist[v-1]==inf) break

```

%927

#599

%849

#782

#881

```

61 for(int i=0; i<v; ++i){ //Apply potentials to edge costs.
62     for(int j=0; j<v; ++j){ //Found path from source to sink becomes
        ↪ 0 cost.
63         if(cost[i][j] != inf){
64             cost[i][j] += min_dist[i];
65             cost[i][j] -= min_dist[j];
66         }
67     }
68 }
69 sink_pot += min_dist[v-1];
70 tot_flow += node_flow[v-1];
71 tot_cost += sink_pot * node_flow[v-1];
72 int cur = v-1;
73 while(cur != 0){ //Backtrack along found path that now has 0 cost.
74     rem_flow[prev_node[cur]][cur] -= node_flow[v-1];
75     rem_flow[cur][prev_node[cur]] += node_flow[v-1];
76     cost[cur][prev_node[cur]] = 0;
77     if(rem_flow[prev_node[cur]][cur] == 0)
78         cost[prev_node[cur]][cur] = inf;
79     cur = prev_node[cur];
80 }
81 }
82 }
83 int main(){ //http://www.spoj.com/problems/GREED/
84     cin >> t;
85     for(int i=0; i<t; ++i){
86         cin >> n;
87         for(int j=0; j<nmax; ++j){
88             for(int k=0; k<nmax; ++k){
89                 cost[j][k] = inf;
90                 rem_flow[j][k] = 0;
91             }
92         }
93         for(int j=1; j<=n; ++j){
94             cost[j][2*n+1] = 0;
95             rem_flow[j][2*n+1] = 1;
96         }
97         for(int j=1; j<=n; ++j){
98             int card;
99             cin >> card;
100             ++rem_flow[0][card];
101             cost[0][card] = 0;
102         }
103         int ex_c;
104         cin >> ex_c;
105         for(int j=0; j<ex_c; ++j){
106             int a, b;
107             cin >> a >> b;
108             if(b < a) swap(a, b);
109             cost[a][b] = 1;
110             rem_flow[a][b] = nmax;
111             cost[b][n+b] = 0;
112             rem_flow[b][n+b] = nmax;
113             cost[n+b][a] = 1;

```

#083

#582

%803

```

114     rem_flow[n+b][a] = nmax;
115 }
116 v = 2*n+2;
117 min_cost_max_flow();
118 cout << tot_cost << '\n';
119 }
120 }

```

## 11 Min Cost Max Flow with Cycle Cancelling $\mathcal{O}(\text{flow} \cdot nm)$

```

1 struct Network {
2     struct Node;
3     struct Edge {
4         Node *u, *v;
5         int f, c, cost;
6         Node* from(Node* pos) {
7             if(pos == u)
8                 return v;
9             return u;
10        }
11        int getCap(Node* pos) {
12            if(pos == u)
13                return c-f;
14            return f;
15        }
16        int addFlow(Node* pos, int toAdd) {
17            if(pos == u) {
18                f += toAdd;
19                return toAdd * cost;
20            } else {
21                f -= toAdd;
22                return -toAdd * cost;
23            }
24        }
25    };
26    struct Node {
27        vector<Edge*> conn;
28        int index;
29    };
30    deque<Node> nodes;
31    deque<Edge> edges;
32    Node* addNode() {
33        nodes.push_back(Node());
34        nodes.back().index = nodes.size()-1;
35        return &nodes.back();
36    }
37    Edge* addEdge(Node* u, Node* v, int f, int c, int cost) {
38        edges.push_back({u, v, f, c, cost});
39        u->conn.push_back(&edges.back());
40        v->conn.push_back(&edges.back());
41        return &edges.back();
42    }
43    //Assumes all needed flow has already been added
44    int minCostMaxFlow() {

```

#042

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```

45 int n = nodes.size();
46 int result = 0;
47 struct State {
48     int p;
49     Edge* used;
50 };
51 while(1) {
52     vector<vector<State> > state(1, vector<State>(n, {0, 0}));
53     for(int lev = 0; lev < n; lev++) {
54         state.push_back(state[lev]);
55         for(int i=0;i<n;i++){
56             if(lev == 0 || state[lev][i].p < state[lev-1][i].p) {
57                 for(Edge* edge : nodes[i].conn){
58                     if(edge->getCap(&nodes[i]) > 0) {
59                         int np = state[lev][i].p + (edge->u == &nodes[i] ?
60                             ↪ edge->cost : -edge->cost);
61                         int ni = edge->from(&nodes[i])->index;
62                         if(np < state[lev+1][ni].p) {
63                             state[lev+1][ni].p = np;
64                             state[lev+1][ni].used = edge;
65                         }
66                     }
67                 }
68             }
69         }
70         //Now look at the last level
71         bool valid = false;
72         for(int i=0;i<n;i++)
73             if(state[n-1][i].p > state[n][i].p) {
74                 valid = true;
75                 vector<Edge*> path;
76                 int cap = 1000000000;
77                 Node* cur = &nodes[i];
78                 int clev = n;
79                 vector<bool> explr(n, false);
80                 while(!explr[cur->index]) {
81                     explr[cur->index] = true;
82                     State cstate = state[clev][cur->index];
83                     cur = cstate.used->from(cur);
84                     path.push_back(cstate.used);
85                 }
86                 reverse(path.begin(), path.end() );
87                 {
88                     int i=0;
89                     Node* cur2 = cur;
90                     do {
91                         cur2 = path[i]->from(cur2);
92                         i++;
93                     } while(cur2 != cur);
94                     path.resize(i);
95                 }
96                 for(auto edge : path) {
97                     cap = min(cap, edge->getCap(cur));

```

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```

98         cur = edge->from(cur);
99     }
100     for(auto edge : path) {
101         result += edge->addFlow(cur, cap);
102         cur = edge->from(cur);
103     }
104     if(!valid) break;
105 }
106 return result;
107 }
108 }
109 };

```

#599

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## 12 DMST $\mathcal{O}(E \log V)$

```

1 struct EdgeDesc{
2     int from, to, w;
3 };
4 struct DMST{
5     struct Node;
6     struct Edge{
7         Node *from;
8         Node *tar;
9         int w;
10        bool inc;
11    };
12    struct Circle{
13        bool vis = false;
14        vector<Edge*> contents;
15        void clean(int idx);
16    };
17    const static greater<pair<ll, Edge*> > comp; //Can use inline static
18    ↪ since C++17
19    static vector<Circle> to_process;
20    static bool no_dmst;
21    static Node *root;
22    struct Node{
23        Node *par = NULL;
24        vector<pair<int, int> > out_cands; //Circ, edge idx
25        vector<pair<ll, Edge*> > con;
26        bool in_use = false;
27        ll w = 0; //extra to add to edges in con
28        Node *anc(){
29            if(!par)
30                return this;
31            while(par->par)
32                par = par->par;
33            return par;
34        }
35        void clean(){
36            if(!no_dmst){
37                in_use = false;
38                for(auto &cur : out_cands)
39                    to_process[cur.first].clean(cur.second);

```

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```

39     }
40 }
41 Node *con_to_root(){
42     if(anc() == root)
43         return root;
44     in_use = true;
45     Node *super = this; //Will become root or the first Node
46     ↪ encountered in a loop.
47     while(super == this){
48         while(!con.empty() && con.front().second->tar->anc() == anc()){
49             pop_heap(con.begin(), con.end(), comp);
50             con.pop_back();
51         }
52         if(con.empty()){
53             no_dmst = true;
54             return root;
55         }
56         pop_heap(con.begin(), con.end(), comp);
57         auto nxt = con.back();
58         con.pop_back();
59         w = -nxt.first;
60         if(nxt.second->tar->in_use){ //anc() wouldn't change anything
61             super = nxt.second->tar->anc();
62             to_process.resize(to_process.size()+1);
63         } else {
64             super = nxt.second->tar->con_to_root();
65         }
66         if(super != root){
67             to_process.back().contents.push_back(nxt.second);
68             out_cands.emplace_back(to_process.size()-1,
69                 ↪ to_process.back().contents.size()-1);
70         } else { //Clean circles
71             nxt.second->inc = true;
72             nxt.second->from->clean();
73         }
74     }
75     if(super != root){ //we are some loops non first Node.
76         if(con.size() > super->con.size()){
77             swap(con, super->con); //Largest con in loop should not be
78             ↪ copied.
79             swap(w, super->w);
80         }
81         for(auto cur : con){
82             super->con.emplace_back(cur.first - super->w + w,
83                 ↪ cur.second);
84             push_heap(super->con.begin(), super->con.end(), comp);
85         }
86     }
87     par = super; //root or anc() of first Node encountered in a loop
88     return super;
89 }
90 Node *cur_root;
91 vector<Node> graph;

```

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#375

```

89 vector<Edge> edges;
90 DMST(int n, vector<EdgeDesc> &desc, int r){ //Self loops and multiple
91     ↪ edges are okay.
92     graph.resize(n);
93     cur_root = &graph[r];
94     for(auto &cur : desc) //Edges are reversed internally
95         edges.push_back(Edge{&graph[cur.to], &graph[cur.from], cur.w});
96     for(int i=0; i<desc.size(); ++i)
97         graph[desc[i].to].con.emplace_back(desc[i].w, &edges[i]);
98     for(int i=0; i<n; ++i)
99         make_heap(graph[i].con.begin(), graph[i].con.end(), comp);
100 }
101 bool find(){
102     root = cur_root;
103     no_dmst = false;
104     for(auto &cur : graph){
105         cur.con_to_root();
106         to_process.clear();
107         if(no_dmst) return false;
108     }
109     return true;
110 }
111 ll weight(){
112     ll res = 0;
113     for(auto &cur : edges){
114         if(cur.inc)
115             res += cur.w;
116     }
117     return res;
118 }
119 void DMST::Circle::clean(int idx){
120     if(!vis){
121         vis = true;
122         for(int i=0; i<contents.size(); ++i){
123             if(i != idx){
124                 contents[i]->inc = true;
125                 contents[i]->from->clean();
126             }
127         }
128     }
129 }
130 const greater<pair<ll, DMST::Edge *> > DMST::comp;
131 vector<DMST::Circle> DMST::to_process;
132 bool DMST::no_dmst;
133 DMST::Node *DMST::root;

```

#469

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### 13 Bridges $\mathcal{O}(n)$

```

1 struct vert;
2 struct edge{
3     bool exists = true;
4     vert *dest;
5     edge *rev;

```



```

6  edge(vert *_dest) : dest(_dest){
7      rev = NULL;
8  }
9  vert &operator*(){
10     return *dest;
11 }
12 vert *operator->(){
13     return dest;
14 }
15 bool is_bridge();
16 };
17 struct vert{
18     deque<edge> con;
19     int val = 0;
20     int seen;
21     int dfs(int upd, edge *ban){ //handles multiple edges
22         if(!val){
23             val = upd;
24             seen = val;
25             for(edge &nxt : con){
26                 if(nxt.exists && (&nxt) != ban)
27                     seen = min(seen, nxt->dfs(upd+1, nxt.rev));
28             }
29         }
30         return seen;
31     }
32     void remove_adj_bridges(){
33         for(edge &nxt : con){
34             if(nxt.is_bridge())
35                 nxt.exists = false;
36         }
37     }
38     int cnt_adj_bridges(){
39         int res = 0;
40         for(edge &nxt : con)
41             res += nxt.is_bridge();
42         return res;
43     }
44 };
45 bool edge::is_bridge(){
46     return exists && (dest->seen > rev->dest->val || dest->val <
47         ↪ rev->dest->seen);
48 }
49 vert graph[nmax];
50 int main(){ //Mechanics Practice BRIDGES
51     int n, m;
52     cin>>n>>m;
53     for(int i=0; i<m; ++i){
54         int u, v;
55         scanf("%d %d", &u, &v);
56         graph[u].con.emplace_back(graph+v);
57         graph[v].con.emplace_back(graph+u);
58         graph[u].con.back().rev = &graph[v].con.back();

```

#955

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#673  
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%056

%223

```

58     graph[v].con.back().rev = &graph[u].con.back();
59 }
60 graph[1].dfs(1, NULL);
61 int res = 0;
62 for(int i=1; i<=n; ++i)
63     res += graph[i].cnt_adj_bridges();
64 cout<<res/2<<endl;
65 }

```

#### 14 2-Sat $\mathcal{O}(n)$ and SCC $\mathcal{O}(n)$

```

1 struct Graph {
2     int n;
3     vector<vector<int>> > conn;
4     Graph(int nsize) {
5         n = nsize;
6         conn.resize(n);
7     }
8     void add_edge(int u, int v) {
9         conn[u].push_back(v);
10    }
11    void _topsort_dfs(int pos, vector<int> &result, vector<bool>
12        ↪ &explr, vector<vector<int>> > &revconn) {
13        if(explr[pos])
14            return;
15        explr[pos] = true;
16        for(auto next : revconn[pos])
17            _topsort_dfs(next, result, explr, revconn);
18        result.push_back(pos);
19    }
20    vector<int> topsort() {
21        vector<vector<int>> > revconn(n);
22        for(int u = 0; u < n; u++) {
23            for(auto v : conn[u])
24                revconn[v].push_back(u);
25        }
26        vector<int> result;
27        vector<bool> explr(n, false);
28        for(int i=0; i < n; i++)
29            _topsort_dfs(i, result, explr, revconn);
30        reverse(result.begin(), result.end());
31        return result;
32    }
33    void dfs(int pos, vector<int> &result, vector<bool> &explr) {
34        if(explr[pos])
35            return;
36        explr[pos] = true;
37        for(auto next : conn[pos])
38            dfs(next, result, explr);
39        result.push_back(pos);
40    }
41    vector<vector<int>> > scc(){ // tested on
42        ↪ https://www.hackerearth.com/practice/algorithms/graphs/strongly-connect
43        vector<int> order = topsort();
44        reverse(order.begin(), order.end());

```

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```

43     vector<bool> explr(n, false);
44     vector<vector<int>> results;
45     for(auto it = order.rbegin(); it != order.rend(); ++it){
46         vector<int> component;
47         _topsort_dfs(*it, component, explr, conn);
48         sort(component.begin(), component.end());
49         results.push_back(component);
50     }
51     sort(results.begin(), results.end());
52     return results;
53 }
54 };
55 //Solution for:
56   ↪ http://codeforces.com/group/PjzGiggT71/contest/221700/problem/C
57 int main() {
58     int n, m;
59     cin >> n >> m;
60     Graph g(2*m);
61     for(int i=0; i<n; i++) {
62         int a, sa, b, sb;
63         cin >> a >> sa >> b >> sb;
64         a--, b--;
65         g.add_edge(2*a + 1 - sa, 2*b + sb);
66         g.add_edge(2*b + 1 - sb, 2*a + sa);
67     }
68     vector<int> state(2*m, 0);
69     {
70         vector<int> order = g.topsort();
71         vector<bool> explr(2*m, false);
72         for(auto u : order) {
73             vector<int> traversed;
74             g.dfs(u, traversed, explr);
75             if(traversed.size() > 0 && !state[traversed[0]^1]) {
76                 for(auto c : traversed)
77                     state[c] = 1;
78             }
79         }
80         for(int i=0; i < m; i++) {
81             if(state[2*i] == state[2*i+1]) {
82                 cout << "IMPOSSIBLE\n";
83                 return 0;
84             }
85         }
86         for(int i=0; i < m; i++) {
87             cout << state[2*i+1] << '\n';
88         }
89         return 0;
90 }

```

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### 15 Lazy Segment Tree $\mathcal{O}(\log n)$ per query

```

1 struct SegmentTree {
2     struct Node {
3         long long value = 0;

```

```

4         int size = 1;
5         int lazy_add = 0;
6         bool lazy_set = false;
7         int lazy_to_set = 0;
8         void set(int to_set) {
9             lazy_set = true;
10            lazy_to_set = to_set;
11            lazy_add = 0;
12        }
13    };
14    int n;
15    vector<Node> nodes;
16    void propagate(int pos) {
17        Node& cur = nodes[pos];
18        if(cur.lazy_set) {
19            if(pos < n) {
20                nodes[pos*2].set(cur.lazy_to_set);
21                nodes[pos*2+1].set(cur.lazy_to_set);
22            }
23            cur.value = 1LL * cur.size * cur.lazy_to_set;
24            cur.lazy_set = false;
25        }
26        if(cur.lazy_add != 0) {
27            if(pos < n) {
28                nodes[pos*2].lazy_add += cur.lazy_add;
29                nodes[pos*2+1].lazy_add += cur.lazy_add;
30            }
31            cur.value += 1LL * cur.size * cur.lazy_add;
32            cur.lazy_add = 0;
33        }
34    }
35    long long get_value(int pos) {
36        propagate(pos);
37        return nodes[pos].value;
38    }
39    SegmentTree(int nsize) {
40        n = 1;
41        while(n < nsize) n*=2;
42        nodes.resize(2*n);
43        for(int i=n-1; i>0; i--)
44            nodes[i].size = nodes[2*i].size * 2;
45    }
46    void set(int l, int r, int to_set, int pos = 1, int lb = 0, int rb
47    ↪ = -1) {
48        propagate(pos);
49        if(rb == -1) rb = n;
50        if(l <= lb && rb <= r) {
51            nodes[pos].set(to_set);
52            return;
53        }
54        int mid = (lb + rb) / 2;
55        if(l < mid)
56            set(l, r, to_set, pos*2, lb, mid);

```

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#567

```

56     if(mid < r)
57         set(l, r, to_set, pos*2+1, mid, rb);
58     nodes[pos].value = get_value(pos*2) + get_value(pos*2+1);
59 }
60 void add(int l, int r, int to_add, int pos = 1, int lb = 0, int rb
    ↪ = -1) { #168
61     propagate(pos);
62     if(rb == -1) rb = n;
63     if(l <= lb && rb <= r) {
64         nodes[pos].lazy_add += to_add;
65         return;
66     }
67     int mid = (lb + rb) / 2;
68     if(l < mid)
69         add(l, r, to_add, pos*2, lb, mid);
70     if(mid < r) #620
71         add(l, r, to_add, pos*2+1, mid, rb);
72     nodes[pos].value = get_value(pos*2) + get_value(pos*2+1);
73 }
74 long long get(int l, int r, int pos = 1, int lb = 0, int rb = -1) {
75     propagate(pos);
76     if(rb == -1) rb = n;
77     if(l <= lb && rb <= r) return get_value(pos);
78     int mid = (lb + rb) / 2;
79     long long result = 0;
80     if(l < mid) #133
81         result += get(l, r, pos*2, lb, mid);
82     if(mid < r)
83         result += get(l, r, pos*2+1, mid, rb);
84     return result;
85 }
86 }; #280
87 //Solution for:
88 ↪ http://codeforces.com/group/U01GDa2Gwb/contest/219104/problem/LAZY
89 int main() {
90     int n, m;
91     cin >> n >> m;
92     SegmentTree stree(n);
93     for(int i=0;i<n;i++) {
94         int a;
95         cin >> a;
96         stree.set(i, i+1, a);
97     }
98     for(int i=0;i<m;i++) {
99         int type;
100         cin >> type;
101         if(type == 1) {
102             int l, r, d;
103             cin >> l >> r >> d;
104             stree.add(l-1, r, d);
105         } else if(type == 2) {
106             int l, r, x;
107             cin >> l >> r >> x;
108             stree.set(l-1, r, x);

```

```

108     } else {
109         int l, r;
110         cin >> l >> r;
111         cout << stree.get(l-1, r) << '\n';
112     }
113 }
114 }

```

## 16 Generic segment tree(lazy, noncommutative)

```

1 struct Segment{
2     ll sum_val=0;
3     ll min_val=0;
4     void find_sum(int seg_len, ll &cur_sum){
5         cur_sum = cur_sum + sum_val;
6     }
7     void find_min(int seg_len, ll &cur_min){
8         cur_min = min(cur_min, min_val);
9     }
10    void recalc(int seg_len, const Segment &lhs_seg, const Segment
    ↪ &rhs_seg){ #599
11        sum_val = lhs_seg.sum_val + rhs_seg.sum_val;
12        min_val = min(lhs_seg.min_val, rhs_seg.min_val);
13    }
14 };
15 struct Lazy{
16     ll add_val;
17     ll assign_val; //LLONG_MIN if no assign;
18     void init(){
19         add_val = 0;
20         assign_val = LLONG_MIN; #577
21     }
22     Lazy(){ init(); }
23     void apply_to_lazy(int seg_len, Lazy &child) const{
24         if(assign_val != LLONG_MIN){
25             child.add_val = 0;
26             child.assign_val = assign_val;
27         }
28         child.add_val += add_val;
29     }
30     void apply_to_seg(int seg_len, Segment &cur) const{ #523
31         if(assign_val != LLONG_MIN){
32             cur.min_val = assign_val;
33             cur.sum_val = seg_len * assign_val;
34         }
35         cur.min_val += add_val;
36         cur.sum_val += seg_len * add_val;
37     } //Following code should not need to be modified %992
38     void split(int seg_len, Lazy &lhs_lazy, Lazy &rhs_lazy){
39         apply_to_lazy(seg_len, lhs_lazy); //Empty current and pass on to
    ↪ children
40         apply_to_lazy(seg_len, rhs_lazy);
41         init();
42     }

```

```

43 };
44 // Highly optimized generic segment tree with lazy propagation
45 class SegTree{ //indexes start from 0, ranges are [beg, end)
46 private:
47     int offset;
48     int height;
49     Segment *segs;
50     Lazy *lazys;
51     vector<bool> is_lazy;
52     void split(int len, int idx){
53         is_lazy[idx] = false;
54         lazys[idx].apply_to_seg(len/2, segs[2*idx]);
55         lazys[idx].apply_to_seg(len/2, segs[2*idx+1]);
56         lazys[idx].split(len/2, lazys[2*idx], lazys[2*idx+1]);
57         is_lazy[2*idx] = true;
58         is_lazy[2*idx+1] = true;
59     }
60     void push(int bot_idx){
61         for(int s = height-1; s>0; --s){
62             int idx = bot_idx>>s;
63             if(is_lazy[idx]){ //Lazys can be below other lazys
64                 split(1<<s, idx);
65             }
66         }
67     }
68     void build(int len, int idx){
69         for(; idx; len<=1, idx>>=1){
70             segs[idx].recalc(len, segs[2*idx], segs[2*idx+1]);
71         }
72     }
73 public:
74     SegTree(int tree_size){
75         offset = tree_size;
76         height = 32 - __builtin_clz(tree_size);
77         segs = new Segment[2*tree_size];
78         lazys = new Lazy[2*tree_size];
79         is_lazy.resize(2*tree_size, false);
80     }
81     ~SegTree(){
82         delete[] segs;
83         delete[] lazys;
84     }
85     void modify(int l, int r, const Lazy &upd){
86         l+=offset;
87         r+=offset;
88         push(l);
89         push(r-1);
90         int len = 1;
91         for(int l_tmp = l, r_tmp = r; l_tmp<r_tmp; l_tmp >>= 1, r_tmp >>=
92             ↳ 1, len <= 1){
93             if(l_tmp & 1){
94                 upd.apply_to_lazy(len, lazys[l_tmp]);
95                 upd.apply_to_seg(len, segs[l_tmp]);
96                 is_lazy[l_tmp] = true;

```

#678

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#201

#920

#744

```

96         ++l_tmp;
97     }
98     if(r_tmp & 1){
99         --r_tmp;
100         upd.apply_to_lazy(len, lazys[r_tmp]);
101         upd.apply_to_seg(len, segs[r_tmp]);
102         is_lazy[r_tmp] = true;
103     }
104 }
105 len = 1<<(__builtin_ctz(l)+1);
106 l >>= __builtin_ctz(l) + 1;
107 build(len, l);
108 len = 1<<(__builtin_ctz(r)+1);
109 r >>= __builtin_ctz(r) + 1;
110 build(len, r);
111 }
112 template< typename ...QueryArgs >
113 void query(int l, int r, void (Segment::*query_func)(int,
114     ↳ QueryArgs...), QueryArgs &&...query_args){
115     l+=offset;
116     r+=offset;
117     push(l);
118     push(r-1);
119     int len = 1;
120     int r_orig = r;
121     for(; l<r; l>>=1, r>>=1, len <= 1){ //Segments applied in order
122         ↳ to query
123         if(l & 1){
124             (segs[l++].*query_func)(len, query_args...);
125         }
126     }
127     for(;r < r_orig;){
128         r<<=1;
129         len>>=1;
130         if(r_orig & len){
131             (segs[r++].*query_func)(len, query_args...);
132         }
133     }
134 };
135 int main(){
136     int n, m; //solves Mechanics Practice LAZY
137     cin>>n>>m;
138     SegTree seg_tree(n);
139     for(int i=0; i<n; ++i){
140         Lazy tmp;
141         scanf("%lld", &tmp.assign_val);
142         seg_tree.modify(i, i+1, tmp);
143     }
144     for(int i=0; i<m; ++i){
145         int o;
146         int l, r;
147         scanf("%d %d %d", &o, &l, &r);

```

#347

#339

#008

#766

%509

```

147 --l;
148 if(o==1){
149     Lazy tmp;
150     scanf("%lld", &tmp.add_val);
151     seg_tree.modify(l, r, tmp);
152 } else if(o==2){
153     Lazy tmp;
154     scanf("%lld", &tmp.assign_val);
155     seg_tree.modify(l, r, tmp);
156 } else {
157     ll res=0;
158     seg_tree.query(l, r, &Segment::find_sum, res);
159     printf("%lld\n",res);
160 }
161 }
162 }

```

### 17 Templated Persitent Segment Tree $\mathcal{O}(\log n)$ per query

```

1 template<typename T, typename comp>
2 class PersistentST {
3     struct Node {
4         Node *left, *right;
5         int lend, rend;
6         T value;
7         Node (int position, T _value) {
8             left = NULL;
9             right = NULL;
10            lend = position;
11            rend = position;
12            value = _value;
13        }
14        Node (Node *_left, Node *_right) {
15            left = _left;
16            right = _right;
17            lend = left->lend;
18            rend = right->rend;
19            value = comp()(left->value, right->value);
20        }
21        T query (int qlleft, int qright) {
22            qlleft = max(qlleft, lend);
23            qright = min(qright, rend);
24            if (qlleft == lend && qright == rend) {
25                return value;
26            } else if (qlleft > qright) {
27                return comp().identity;
28            } else {
29                return comp()(left->query(qlleft, qright), right->query(qlleft,
30                    ↪ qright));
31            }
32        };
33        int size;
34        Node **tree;
35        vector<Node*> roots;

```

#479

#373

#766

```

36 public:
37     PersistentST () {}
38     PersistentST (int _size, T initial) {
39         for (int i = 0; i < 32; i++) {
40             if ((1 << i) > _size) {
41                 size = 1 << i;
42                 break;
43             }
44         }
45         tree = new Node* [2 * size + 5];
46         for (int i = size; i < 2 * size; i++)
47             tree[i] = new Node (i - size, initial);
48         for (int i = size - 1; i > 0; i--)
49             tree[i] = new Node (tree[2 * i], tree[2 * i + 1]);
50         roots = vector<Node*> (1, tree[1]);
51     }
52     void set (int position, T _value) {
53         tree[size + position] = new Node (position, _value);
54         for (int i = (size + position) / 2; i >= 1; i /= 2)
55             tree[i] = new Node (tree[2 * i], tree[2 * i + 1]);
56         roots.push_back(tree[1]);
57     }
58     int last_revision () {
59         return (int) roots.size() - 1;
60     }
61     T query (int qlleft, int qright, int revision) {
62         return roots[revision]->query(qlleft, qright);
63     }
64     T query (int qlleft, int qright) {
65         return roots[last_revision()]->query(qlleft, qright);
66     }
67 };

```

#250

#128

#890

%280

### 18 Templated HLD $\mathcal{O}(M(n) \log n)$ per query

```

1 class dummy {
2 public:
3     dummy () {}
4     dummy (int, int) {}
5     void set (int, int) {}
6     int query (int left, int right) {
7         cout << this << ' ' << left << ' ' << right << endl;
8     }
9 };
10 /* T should be the type of the data stored in each vertex;
11  * DS should be the underlying data structure that is used to perform
12  * ↪ the
13  * group operation. It should have the following methods:
14  * * DS () - empty constructor
15  * * DS (int size, T initial) - constructs the structure with the given
16  * ↪ size,
17  * initially filled with initial.
18  * * void set (int index, T value) - set the value at index `index` to
19  * ↪ `value`

```

%932



```

17   * T query (int left, int right) - return the "sum" of elements
18   ↪ between left and right, inclusive.
19   */
20  template<typename T, class DS>
21  class HLD {
22      int vertexc;
23      vector<int> *adj;
24      vector<int> subtree_size;
25      DS structure;
26      DS aux;
27      void build_sizes (int vertex, int parent) {
28          subtree_size[vertex] = 1;
29          for (int child : adj[vertex]) {
30              if (child != parent) {
31                  build_sizes(child, vertex);
32                  subtree_size[vertex] += subtree_size[child];
33              }
34          }
35          int cur;
36          vector<int> ord;
37          vector<int> chain_root;
38          vector<int> par;
39          void build_hld (int vertex, int parent, int chain_source) {
40              cur++;
41              ord[vertex] = cur;
42              chain_root[vertex] = chain_source;
43              par[vertex] = parent;
44              if (adj[vertex].size() > 1) {
45                  int big_child, big_size = -1;
46                  for (int child : adj[vertex]) {
47                      if ((child != parent) && (subtree_size[child] > big_size)) {
48                          big_child = child;
49                          big_size = subtree_size[child];
50                      }
51                  }
52                  build_hld(big_child, vertex, chain_source);
53                  for (int child : adj[vertex]) {
54                      if ((child != parent) && (child != big_child))
55                          build_hld(child, vertex, child);
56                  }
57              }
58          }
59      public:
60          HLD (int _vertexc) {
61              vertexc = _vertexc;
62              adj = new vector<int> [vertexc + 5];
63          }
64          void add_edge (int u, int v) {
65              adj[u].push_back(v);
66              adj[v].push_back(u);
67          }
68          void build (T initial) {
69              subtree_size = vector<int> (vertexc + 5);

```

#037

#593

#646

#738

#841

```

70      ord = vector<int> (vertexc + 5);
71      chain_root = vector<int> (vertexc + 5);
72      par = vector<int> (vertexc + 5);
73      cur = 0;
74      build_sizes(1, -1);
75      build_hld(1, -1, 1);
76      structure = DS (vertexc + 5, initial);
77      aux = DS (50, initial);
78  }
79  void set (int vertex, int value) {
80      structure.set(ord[vertex], value);
81  }
82  T query_path (int u, int v) { /* returns the "sum" of the path u->v
83      ↪ */
84      int cur_id = 0;
85      while (chain_root[u] != chain_root[v]) {
86          if (ord[u] > ord[v]) {
87              cur_id++;
88              aux.set(cur_id, structure.query(ord[chain_root[u]], ord[u]));
89              u = par[chain_root[u]];
90          } else {
91              cur_id++;
92              aux.set(cur_id, structure.query(ord[chain_root[v]], ord[v]));
93              v = par[chain_root[v]];
94          }
95      }
96      cur_id++;
97      aux.set(cur_id, structure.query(min(ord[u], ord[v]), max(ord[u],
98      ↪ ord[v])));
99      return aux.query(1, cur_id);
100  }
101  void print () {
102      for (int i = 1; i <= vertexc; i++)
103          cout << i << ' ' << ord[i] << ' ' << chain_root[i] << ' ' <<
104          ↪ par[i] << endl;
105  }
106  int main () {
107      int vertexc;
108      cin >> vertexc;
109      HLD<int, dummy> hld (vertexc);
110      for (int i = 0; i < vertexc - 1; i++) {
111          int u, v;
112          cin >> u >> v;
113          hld.add_edge(u, v);
114      }
115      hld.build(0);
116      hld.print();
117      int queryc;
118      cin >> queryc;
119      for (int i = 0; i < queryc; i++) {
120          int u, v;
121          cin >> u >> v;

```

#793

#517

%257

```

120     hld.query_path(u, v);
121     cout << endl;
122 }
123 }

```

### 19 Templated multi dimensional BIT $\mathcal{O}(\log(n)^{\dim})$ per query

```

1 // Fully overloaded any dimensional BIT, use any type for coordinates,
  // elements, return value.
2 // Includes coordinate compression.
3 template < typename elem_t, typename coord_t, coord_t n_inf, typename
  ↪ ret_t >
4 class BIT {
5     vector< coord_t > positions;
6     vector< elem_t > elems;
7     bool initiated = false;
8 public:
9     BIT() {
10         positions.push_back(n_inf);
11     }
12     void initiate() {
13         if (initiated) {
14             for (elem_t &c_elem : elems)
15                 c_elem.initiate();
16         } else {
17             initiated = true;
18             sort(positions.begin(), positions.end());
19             positions.resize(unique(positions.begin(), positions.end()) -
20                               ↪ positions.begin());
21             elems.resize(positions.size());
22         }
23     }
24     template < typename... loc_form >
25     void update(coord_t cord, loc_form... args) {
26         if (initiated) {
27             int pos = lower_bound(positions.begin(), positions.end(), cord) -
28                 ↪ positions.begin();
29             for (; pos < positions.size(); pos += pos & -pos)
30                 elems[pos].update(args...);
31         } else {
32             positions.push_back(cord);
33         }
34     }
35     template < typename... loc_form >
36     ret_t query(coord_t cord, loc_form... args) { //sum in open interval
37         ↪ (-inf, cord)
38         ret_t res = 0;
39         int pos = (lower_bound(positions.begin(), positions.end(), cord) -
40             ↪ positions.begin())-1;
41         for (; pos > 0; pos -= pos & -pos)
42             res += elems[pos].query(args...);
43         return res;
44     }
45 };
46 template < typename internal_type >

```

#448

#036

#154

#895

```

43 struct wrapped {
44     internal_type a = 0;
45     void update(internal_type b) {
46         a += b;
47     }
48     internal_type query() {
49         return a;
50     }
51     // Should never be called, needed for compilation
52     void initiate() {
53         cerr << 'i' << endl;
54     }
55     void update() {
56         cerr << 'u' << endl;
57     }
58 };
59 int main() {
60     // return type should be same as type inside wrapped
61     BIT< BIT< wrapped< ll >, int, INT_MIN, ll >, int, INT_MIN, ll >
62     ↪ fenwick;
63     int dim = 2;
64     vector< tuple< int, int, ll > > to_insert;
65     to_insert.emplace_back(1, 1, 1);
66     // set up all positions that are to be used for update
67     for (int i = 0; i < dim; ++i) {
68         for (auto &cur : to_insert)
69             fenwick.update(get< 0 >(cur), get< 1 >(cur)); // May include
70             ↪ value which won't be used
71         fenwick.initiate();
72     }
73     // actual use
74     for (auto &cur : to_insert)
75         fenwick.update(get< 0 >(cur), get< 1 >(cur), get< 2 >(cur));
76     cout << fenwick.query(2, 2)<<'\n';
77 }

```

#560

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### 20 Treap $\mathcal{O}(\log n)$ per query

```

1 mt19937 randgen;
2 struct Treap {
3     struct Node {
4         int key;
5         int value;
6         unsigned int priority;
7         long long total;
8         Node* lch;
9         Node* rch;
10        Node(int new_key, int new_value) {
11            key = new_key;
12            value = new_value;
13            priority = randgen();
14            total = new_value;
15            lch = 0;
16            rch = 0;
17        }

```

#698

```

18     void update() {
19         total = value;
20         if(lch) total += lch->total;
21         if(rch) total += rch->total;
22     }
23 };
24 deque<Node> nodes;
25 Node* root = 0;
26 pair<Node*, Node*> split(int key, Node* cur) {
27     if(cur == 0) return {0, 0};
28     pair<Node*, Node*> result;
29     if(key <= cur->key) {
30         auto ret = split(key, cur->lch);
31         cur->lch = ret.second;
32         result = {ret.first, cur};
33     } else {
34         auto ret = split(key, cur->rch);
35         cur->rch = ret.first;
36         result = {cur, ret.second};
37     }
38     cur->update();
39     return result;
40 }
41 Node* merge(Node* left, Node* right) {
42     if(left == 0) return right;
43     if(right == 0) return left;
44     Node* top;
45     if(left->priority < right->priority) {
46         left->rch = merge(left->rch, right);
47         top = left;
48     } else {
49         right->lch = merge(left, right->lch);
50         top = right;
51     }
52     top->update();
53     return top;
54 }
55 void insert(int key, int value) {
56     nodes.push_back(Node(key, value));
57     Node* cur = &nodes.back();
58     pair<Node*, Node*> ret = split(key, root);
59     cur = merge(ret.first, cur);
60     cur = merge(cur, ret.second);
61     root = cur;
62 }
63 void erase(int key) {
64     Node *left, *mid, *right;
65     tie(left, mid) = split(key, root);
66     tie(mid, right) = split(key+1, mid);
67     root = merge(left, right);
68 }
69 long long sum_upto(int key, Node* cur) {
70     if(cur == 0) return 0;
71     if(key <= cur->key) {

```

#295

#233

#230

#510

#760

#634

```

72         return sum_upto(key, cur->lch);
73     } else {
74         long long result = cur->value + sum_upto(key, cur->rch);
75         if(cur->lch) result += cur->lch->total;
76         return result;
77     }
78 }
79 long long get(int l, int r) {
80     return sum_upto(r+1, root) - sum_upto(l, root);
81 }
82 };
83 //Solution for:
84 ↪ http://codeforces.com/group/U01GDa2Gwb/contest/219104/problem/TREAP
85 int main() {
86     ios_base::sync_with_stdio(false);
87     cin.tie(0);
88     Treap treap;
89     cin >> m;
90     for(int i=0; i<m; i++) {
91         int type;
92         cin >> type;
93         if(type == 1) {
94             int x, y;
95             cin >> x >> y;
96             treap.insert(x, y);
97         } else if(type == 2) {
98             int x;
99             cin >> x;
100             treap.erase(x);
101         } else {
102             int l, r;
103             cin >> l >> r;
104             cout << treap.get(l, r) << endl;
105         }
106     }
107     return 0;
108 }

```

#509

%959

## 21 FFT 5M length/sec

```

1 struct Complex{
2     double a=0, b=0;
3     Complex &operator/=(const int &oth){
4         a /= oth;
5         b /= oth;
6         return *this;
7     }
8 };
9 Complex operator+(const Complex &lft, const Complex &rgt){
10     return Complex {lft.a+rgt.a, lft.b+rgt.b};
11 }
12 Complex operator-(const Complex &lft, const Complex &rgt){
13     return Complex {lft.a-rgt.a, lft.b-rgt.b};

```

#384

```

14 }
15 Complex operator*(const Complex &lft, const Complex &rgt){
16     return Complex {lft.a*rgt.a-lft.b*rgt.b, lft.a*rgt.b+lft.b*rgt.a};
17 }
18 void fft_rec(Complex *arr, Complex *root_pow, int len){
19     if(len != 1){
20         fft_rec(arr, root_pow, len>>1);
21         fft_rec(arr+len, root_pow, len>>1);
22     }
23     root_pow += len;
24     for(int i=0; i < len; ++i){
25         Complex tmp = arr[i]+root_pow[i]*arr[i+len];
26         arr[i+len] = arr[i]-root_pow[i]*arr[i+len];
27         arr[i] = tmp;
28     }
29 }
30 void fft(vector<Complex> &arr, int ord, bool invert){
31     assert(arr.size() == 1<<ord);
32     static vector<Complex> root_pow(1);
33     static int inc_pow = 1;
34     static bool is_inv = false;
35     if(inc_pow <= ord){
36         int idx = root_pow.size();
37         root_pow.resize(1<<ord);
38         for(; inc_pow<=ord; ++inc_pow){
39             for(int idx_p = 0; idx_p < 1<<(ord-1); idx_p += 1<<(ord-inc_pow),
40                 ↪ ++idx){
41                 root_pow[idx] = Complex {cos(-idx_p*M_PI/(1<<(ord-1))),
42                     ↪ sin(-idx_p*M_PI/(1<<(ord-1)))};
43                 if(is_inv)
44                     root_pow[idx].b = -root_pow[idx].b;
45             }
46         }
47         if(invert != is_inv){
48             is_inv = invert;
49             for(Complex &cur : root_pow)
50                 cur.b = -cur.b;
51         }
52         int rev = 0;
53         for(int i=0; i < (1<<ord)-1; ++i){
54             if(i < rev)
55                 swap(arr[i], arr[rev]);
56             int j=0;
57             do{
58                 rev ^= 1<<(ord-1-j);
59             } while(i & 1<<(j++));
60         }
61         fft_rec(arr.data(), root_pow.data(), 1<<(ord-1));
62         if(invert)
63             for(int i=0; i < (1<<ord); ++i)
64                 arr[i] /= (1<<ord);
65     }

```

#767

#689

#830

#717

#351

%402

```

65 void mult_poly_mod(vector<int> &a, vector<int> &b, vector<int> &c){ //
66     ↪ c += a*b
67     static vector<Complex> arr[7]; //correct upto 0.5-2M elements(mod ~=
68     ↪ 1e9)
69     if(c.size() < 400){
70         for(int i=0; i < (int)a.size(); ++i)
71             for(int j=0; j < (int)b.size() && i+j < (int)c.size(); ++j)
72                 c[i+j] = ((ll)a[i]*b[j]+c[i+j])%mod;
73     } else {
74         int fft_ord = 32-__builtin_clz(c.size());
75         if((int)arr[0].size() < 1<<fft_ord)
76             for(int i=0; i<7; ++i)
77                 arr[i].resize(1<<fft_ord);
78         for(int i=0; i<7; ++i)
79             fill(arr[i].begin(), arr[i].end(), Complex{});
80         for(int &cur : a)
81             if(cur < 0)
82                 cur += mod;
83         for(int &cur : b)
84             if(cur < 0)
85                 cur += mod;
86         const int shift = 15;
87         const int mask = (1<<shift)-1;
88         for(int i=0; i < (int)min(a.size(), c.size()); ++i){
89             arr[0][i].a = a[i]&mask;
90             arr[1][i].a = a[i]>>shift;
91         }
92         for(int i=0; i < (int)min(b.size(), c.size()); ++i){
93             arr[2][i].a = b[i]&mask;
94             arr[3][i].a = b[i]>>shift;
95         }
96         for(int i=0; i<4; ++i)
97             fft(arr[i], fft_ord, false);
98         for(int i=0; i<2; ++i){
99             for(int j=0; j<2; ++j){
100                 int tar = 4+i+j;
101                 for(int k=0; k<(1<<fft_ord); ++k)
102                     arr[tar][k] = arr[tar][k] + arr[i][k] * arr[2+j][k];
103             }
104         }
105         for(int i=4; i<7; ++i){
106             fft(arr[i], fft_ord, true);
107             for(int k=0; k<(int)c.size(); ++k)
108                 c[k] = (c[k]+(((ll)(arr[i][k].a+0.5)%mod)<<(shift*(i-4))))%mod;
109         }
110     }
111 }

```

#082

#019

#432

#272

%089

## 22 Rabbin Miller prime check

```

1 __int128 pow_mod(__int128 a, ll n, __int128 mod) {
2     __int128 res = 1;
3     for (ll i = 0; i < 64; ++i) {
4         if (n & (1LL << i))
5             res = (res * a) % mod;

```

```
6     a = (a * a) % mod;
7 }
8 return res;
9 }
10 bool is_prime(ll n) { //guaranteed for 64 bit numbers           #280
11     if (n == 2 || n == 3) return true;
12     if (!(n & 1) || n == 1) return false;
13     static vector< char > witnesses = {2, 3, 5, 7, 11, 13, 17, 19, 23,
14         ↪ 29, 31, 37};
15     ll s = __builtin_ctz(n - 1);
16     ll d = (n - 1) >> s;
17     __int128 mod = n;
18     for (__int128 a : witnesses) {
19         if (a >= mod) break;
20         a = pow_mod(a, d, mod);
21         if (a == 1 || a == mod - 1) continue;           #667
22         for (ll r = 1; r < s; ++r) {
23             a = a * a % mod;
24             if (a == 1) return false;
25             if (a == mod - 1) break;
26         }
27         if (a != mod - 1) return false;
28     }
29     return true;                                         %083
}
```

---





## Combinatorics Cheat Sheet

## Useful formulas

$\binom{n}{k} = \frac{n!}{k!(n-k)!}$  — number of ways to choose  $k$  objects out of  $n$

$\binom{n+k-1}{k-1}$  — number of ways to choose  $k$  objects out of  $n$  with repetitions

$[n]$  — Stirling numbers of the first kind; number of permutations of  $n$  elements with  $k$  cycles

$$[n+1] = n[n] + [n-1]$$

$$(x)_n = x(x-1)\dots x-n+1 = \sum_{k=0}^n (-1)^{n-k} [n]_k x^k$$

$\left\{ \begin{smallmatrix} n \\ m \end{smallmatrix} \right\}$  — Stirling numbers of the second kind; number of partitions of set  $1, \dots, n$  into  $k$  disjoint subsets.

$$\left\{ \begin{smallmatrix} n+1 \\ m \end{smallmatrix} \right\} = k \left\{ \begin{smallmatrix} n \\ k \end{smallmatrix} \right\} + \left\{ \begin{smallmatrix} n \\ k-1 \end{smallmatrix} \right\}$$

$$\sum_{k=0}^n \left\{ \begin{smallmatrix} n \\ k \end{smallmatrix} \right\} (x)_k = x^n$$

$$C_n = \frac{1}{n+1} \binom{2n}{n} — \text{Catalan numbers}$$

$$C(x) = \frac{1-\sqrt{1-4x}}{2x}$$

## Binomial transform

If  $a_n = \sum_{k=0}^n \binom{n}{k} b_k$ , then  $b_n = \sum_{k=0}^n (-1)^{n-k} \binom{n}{k} a_k$

$$\bullet a = (1, x, x^2, \dots), b = (1, (x+1), (x+1)^2, \dots)$$

$$\bullet a_i = i^k, b_i = \left\{ \begin{smallmatrix} n \\ i \end{smallmatrix} \right\} i!$$

## Burnside's lemma

Let  $G$  be a group of *action* on set  $X$  (Ex.: cyclic shifts of array, rotations and symmetries of  $n \times n$  matrix, ...)

Call two objects  $x$  and  $y$  *equivalent* if there is an action  $f$  that transforms  $x$  to  $y$ :  $f(x) = y$ .

The number of equivalence classes then can be calculated as follows:  $C = \frac{1}{|G|} \sum_{f \in G} |X^f|$ , where  $X^f$  is the set of *fixed points* of  $f$ :  $X^f = \{x | f(x) = x\}$

## Generating functions

Ordinary generating function (o.g.f.) for sequence  $a_0, a_1, \dots, a_n, \dots$  is  $A(x) = \sum_{n=0}^{\infty} a_n x^n$

Exponential generating function (e.g.f.) for sequence  $a_0, a_1, \dots, a_n, \dots$  is  $A(x) = \sum_{n=0}^{\infty} a_n \frac{x^n}{n!}$

$$B(x) = A'(x), b_{n-1} = n \cdot a_n$$

$$c_n = \sum_{k=0}^n a_k b_{n-k} \text{ (o.g.f. convolution)}$$

$$c_n = \sum_{k=0}^n \binom{n}{k} a_k b_{n-k} \text{ (e.g.f. convolution, compute with FFT using } \widetilde{a}_n = \frac{a_n}{n!} \text{)}$$

## General linear recurrences

If  $a_n = \sum_{k=1}^n b_k a_{n-k}$ , then  $A(x) = \frac{a_0}{1-B(x)}$ . We also can compute all  $a_n$  with Divide-and-Conquer algorithm in  $O(n \log^2 n)$ .

Inverse polynomial modulo  $x^l$ 

Given  $A(x)$ , find  $B(x)$  such that  $A(x)B(x) = 1 + x^l \cdot Q(x)$  for some  $Q(x)$

$$1. \text{ Start with } B_0(x) = \frac{1}{a_0}$$

$$2. \text{ Double the length of } B(x): B_{k+1}(x) = (-B_k(x)^2 A(x) + 2B_k(x)) \bmod x^{2^{k+1}}$$

## Fast subset convolution

Given array  $a_i$  of size  $2^k$ , calculate  $b_i = \sum_{j \& i = i} b_j$

```
for b = 0..k-1
  for i = 0..2^k-1
    if (i & (1 << b)) != 0:
      a[i + (1 << b)] += a[i]
```

## Hadamard transform

Treat array  $a$  of size  $2^k$  as  $k$ -dimensional array of size  $2 \times 2 \times \dots \times 2$ , calculate FFT of that array:

```
for b = 0..k-1
  for i = 0..2^k-1
    if (i & (1 << b)) != 0:
      u = a[i], v = a[i + (1 << b)]
      a[i] = u + v
      a[i + (1 << b)] = u - v
```