

University of Tartu ICPC Team Notebook (2018-2019)

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Maxflow Complexity	
$\mathcal{O}(V^2 E)$ – Dinic	
$\Theta(VE \log U)$ – Capacity scaling	
$\Theta(\text{flow}E)$ – Small flow	
$\Theta(\min\{V^{\frac{2}{3}}, E^{\frac{1}{2}}\}E)$ – Unitary capacities	
$\Theta(\sqrt{V}E)$ – Each vertex other than S,T has only a single incoming unitary edge or outgoing one (bipartite matching)	
$\Theta(\text{flow}E \log V)$ – Min-cost-max flow	
Min Rotation of string	
<pre>int a=0, N=s.size(); s += s; ran(b,0,N){ ran(i,0,N) { if (a+i == b s[a+i] < s[b+i]) { b += max(0, i-1); break; } if (s[a+i] > s[b+i]) { a = b; break; } } }</pre>	

```

15     }
15 }
16 return a;
17 Series
18
19     
$$e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots, (-\infty < x < \infty)$$

20     
$$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots, (-1 < x \leq 1)$$

21     
$$\sqrt{1+x} = 1 + \frac{x}{2} - \frac{x^2}{8} + \frac{2x^3}{32} - \frac{5x^4}{128} + \dots, (-1 \leq x \leq 1)$$

22     
$$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots, (-\infty < x < \infty)$$

23     
$$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots, (-\infty < x < \infty)$$

24
25 Symmetric Submodular Functions; Queyranne's
26 algorithm
27 SSF: such function  $f : V \rightarrow R$  that satisfies  $f(A) = f(V/A)$  and for all  $x \in V, X \subseteq Y \subseteq V$  it holds that  $f(X+x) - f(X) \leq f(Y+x) - f(Y)$ .
28 Hereditary family: such set  $I \subseteq 2^V$  so that  $X \subset Y \wedge Y \in I \Rightarrow X \in I$ .
29 Loop: such  $v \in V$  so that  $v \notin I$ .
30
31 def minimize():
32     s = merge_all_loops()
33     while size >= 3:
34         t, u = find_pp()
35         {u} is a possible minimizer
36         tu = merge(t, u)
37         if tu not in I:
38             s = merge(tu, s)
39         for x in V:
40             {x} is a possible minimizer
41     def find_pp():
42         W = {s} # s as in minimizer()
43         todo = V/W
44         ord = []
45         while len(todo) > 0:
46             x = min(todo, key=lambda x: f(W+{x}) -
47                     f({x}))
48             W += {x}
49             todo -= {x}
50             ord.append(x)
51     return ord[-1], ord[-2]

```

```

def enum_all_minimal_minimizers(X):
    # X is a inclusionwise minimal minimizer
    s = merge(s, X)
    yield X
    for {v} in I:
        if f({v}) == f(X):
            yield X
            s = merge(v, s)
    while size(V) >= 3:
        t, u = find_pp()
        tu = merge(t, u)
        if tu not in I:
            s = merge(tu, s)
        elif f({tu}) == f(X):
            yield tu
            s = merge(tu, s)
Subset convolution  $\mathcal{O}(N \log N)$ 
c[z] =  $\sum_{z=x \oplus y} a[x] \cdot b[y]$ , where  $\oplus$  is one of AND, OR, XOR. The size of  $a$  must be a power of two.
void FST(vi& a, bool inv) { //size(a) == 2^x
    for (int n = (int)a.size(), step = 1; step <
        ~n; step *= 2) {
        for (int i = 0; i < n; i += 2 * step)
            ran(j, i, i + step) {
                int &u = a[j], &v = a[j + step];
                tie(u, v) =
                    inv ? pii(v - u, u) : pii(v, u + v);
                    // AND
                    inv ? pii(v, u - v) : pii(u + v, u);
                    // OR
                    pii(u + v, u - v);
                    // XOR
            }
        if (inv) trav(x, a) x /= a.size(); // XOR
        ~only
    }
    vi conv(vi a, vi b) {
        FST(a, 0);
        FST(b, 0);
        ran(i, 0, (int)a.size()) a[i] *= b[i];
        FST(a, 1);
        return a;
    }
}

```

Pythagorean Triples

The Pythagorean triples are uniquely generated by

$$a = k \cdot (m^2 - n^2), \quad b = k \cdot (2mn), \quad c = k \cdot (m^2 + n^2),$$

with $m > n > 0$, $k > 0$, $m \perp n$, and either m or n even.

Primes

$p = 962592769$ is such that $2^{21} \mid p - 1$, which may be useful. For hashing use 970592641 (31-bit number), 31443539979727 (45-bit), 3006703054056749 (52-bit). There are 78498 primes less than 1 000 000.

Primitive roots exist modulo any prime power p^a , except for $p = 2, a > 2$, and there are $\varphi(\varphi(p^a))$ many. For $p = 2, a > 2$, the group $\mathbb{Z}_{2^a}^\times$ is instead isomorphic to $\mathbb{Z}_2 \times \mathbb{Z}_{2^{a-2}}$.

Estimates

$$\sum_{d|n} d = O(n \log \log n).$$

The number of divisors of n is at most around 100 for $n < 5e4$, 500 for $n < 1e7$, 2000 for $n < 1e10$, 200 000 for $n < 1e19$.

Möbius inversion

$$\forall n : g(n) = \sum_{d|n} f(d) \iff \forall n : f(n) = \sum_{d|n} \mu(d)g\left(\frac{n}{d}\right)$$

Derangements

Permutations of a set such that none of the elements appear in their original position.

$$\begin{aligned} D(n) &= (n-1)(D(n-1) + D(n-2)) = \\ &nD(n-1) + (-1)^n = \left\lfloor \frac{n!}{e} \right\rfloor \end{aligned}$$

Burnside's lemma

Given a group G of symmetries and a set X , the number of elements of X up to symmetry equals

$$\frac{1}{|G|} \sum_{g \in G} |X^g|,$$

where X^g are the elements fixed by g ($g \cdot x = x$).

If $f(n)$ counts “configurations” (of some sort) of length n , we can ignore rotational symmetry using $G = \mathbb{Z}_n$ to get

$$g(n) = \frac{1}{n} \sum_{k=0}^{n-1} f(\gcd(n, k)) = \frac{1}{n} \sum_{k|n} f(k)\varphi(n/k).$$

Partition function

Number of ways of writing n as a sum of positive integers, disregarding the order of the summands.

$$p(0) = 1, p(n) = \sum_{k \in \mathbb{Z} \setminus \{0\}} (-1)^{k+1} p(n - k(3k-1)/2)$$

$$p(n) \sim 0.145/n \cdot \exp(2.56\sqrt{n})$$

n	0	1	2	3	4	5	6	7	8	9	20	50	100
$p(n)$	1	1	2	3	5	7	11	15	22	30	627	$\sim 2e5$	$\sim 2e8$

Stirling numbers of the first kind

Number of permutations on n items with k cycles.

$$c(n, k) = c(n-1, k-1) + (n-1)c(n-1, k), \quad c(0, 0) = 1$$

$$\sum_{k=0}^n c(n, k)x^k = x(x+1) \dots (x+n-1)$$

$$c(8, k) = 8, 0, 5040, 13068, 13132, 6769, 1960, 322, 28, 1$$

$$c(n, 2) = 0, 0, 1, 3, 11, 50, 274, 1764, 13068, 109584, \dots$$

Eulerian numbers

Number of permutations $\pi \in S_n$ in which exactly k elements are greater than the previous element. k j :s s.t. $\pi(j) > \pi(j+1)$, $k+1$ j :s s.t. $\pi(j) \geq j$, k j :s s.t. $\pi(j) > j$.

$$E(n, k) = (n-k)E(n-1, k-1) + (k+1)E(n-1, k)$$

$$E(n, 0) = E(n, n-1) = 1$$

$$E(n, k) = \sum_{j=0}^k (-1)^j \binom{n+1}{j} (k+1-j)^n$$

Stirling numbers of the second kind

Partitions of n distinct elements into exactly k groups.

$$S(n, k) = S(n-1, k-1) + kS(n-1, k)$$

$$S(n, 1) = S(n, n) = 1$$

$$S(n, k) = \frac{1}{k!} \sum_{j=0}^k (-1)^{k-j} \binom{k}{j} j^n$$

Bell numbers

Total number of partitions of n distinct elements. $B(n) = 1, 1, 2, 5, 15, 52, 203, 877, 4140, 21147, \dots$. For p prime,

$$B(p^m + n) \equiv mB(n) + B(n+1) \pmod{p}$$

Catalan numbers

$$C_n = \frac{1}{n+1} \binom{2n}{n} = \binom{2n}{n} - \binom{2n}{n+1} = \frac{(2n)!}{(n+1)!n!}$$

$$C_0 = 1, C_{n+1} = \frac{2(2n+1)}{n+2} C_n, C_{n+1} = \sum C_i C_{n-i}$$

$$C_n = 1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786, \dots$$

- sub-diagonal monotone paths in an $n \times n$ grid.
- strings with n pairs of parenthesis, correctly nested.
- binary trees with $n+1$ leaves (0 or 2 children).
- ordered trees with $n+1$ vertices.
- ways a convex polygon with $n+2$ sides can be cut into triangles by connecting vertices with straight lines.
- permutations of $[n]$ with no 3-term increasing subseq.

2D geometry

Define $\text{orient}(A, B, C) = \overline{AB} \times \overline{AC}$. CCW iff > 0 .
 Define $\text{perp}(a, b) = (-b, a)$. The vectors are orthogonal.
 For line $ax + by = c$ def $\bar{v} = (-b, a)$.
 Line through P and Q has $\bar{v} = \overline{PQ}$ and $c = \bar{v} \times P$.

$\text{side}_l(P) = \bar{v}_l \times P - c_l$ sign determines which side P is on from l .

$\text{dist}_l(P) = \text{side}_l(P)/\|\bar{v}_l\|$ squared is integer.

Sorting points along a line: comparator is $\bar{v} \cdot A < \bar{v} \cdot B$.
 Translating line by \bar{t} : new line has $c' = c + \bar{v} \times \bar{t}$.

Line intersection: is $(c_l \bar{v}_m - c_m \bar{v}_l) / (\bar{v}_l \times \bar{v}_m)$.

Project P onto l : is $P - \text{perp}(v) \text{side}_l(P)/\|v\|^2$.

Angle bisectors: $\bar{v} = \bar{v}_l/\|\bar{v}_l\| + \bar{v}_m/\|\bar{v}_m\|$

$c = c_l/\|\bar{v}_l\| + c_m/\|\bar{v}_m\|$.

P is on segment AB iff $\text{orient}(A, B, P) = 0$ and $\overline{PA} \cdot \overline{PB} \leq 0$.

Proper intersection of AB and CD exists iff $\text{orient}(C, D, A)$ and $\text{orient}(C, D, B)$ have opp. signs and $\text{orient}(A, B, C)$ and $\text{orient}(A, B, D)$ have opp. signs. Coordinates:

$$\frac{A \text{orient}(C, D, B) - B \text{orient}(C, D, A)}{\text{orient}(C, D, B) - \text{orient}(C, D, A)}.$$

Circumcircle center:

```
pt circumCenter(pt a, pt b, pt c) {
    b = b-a, c = c-a; // consider coordinates relative to A
    assert(cross(b,c) != 0); // no circumcircle if A,B,C aligned
    return a + perp(b*sq(c) - c*sq(b))/cross(b,c)/2;
```

Circle-line intersect:

```
int circleLine(pt o, double r, line l, pair<pt,pt> &out) {
    double h2 = r*r - l.sqDist(o);
    if (h2 >= 0) { // the line touches the circle
        pt p = l.proj(o); // point P
        pt h = l.v*sqrt(h2)/abs(l.v); // vector parallel to l, of len h
        out = {p-h, p+h};
    }
    return 1 + sgn(h2);
```

Circle-circle intersect:

```
int circleCircle(pt o1, double r1, pt o2, double r2, pair<pt,pt> &out) {
```

```
    pt d=o2-o1; double d2=sq(d);
    if (d2 == 0) {assert(r1 != r2); return 0;} // concentric circles
    double pd = (d2 + r1*r1 - r2*r2)/2; // = |O_1P| * d
    double h2 = r1*r1 - pd*pd/d2; // = h^2
    if (h2 >= 0) {
        pt p = o1 + d*pd/d2, h = perp(d)*sqrt(h2/d2);
        out = {p-h, p+h};}
    return 1 + sgn(h2);
```

Tangent lines:

```
int tangents(pt o1, double r1, pt o2, double r2,
             bool inner, vector<pair<pt,pt>> &out) {
    if (inner) r2 = -r2;
    pt d = o2-o1;
    double dr = r1-r2, d2 = sq(d), h2 = d2-dr*dr;
    if (d2 == 0 || h2 < 0) {assert(h2 != 0); return 0;}
    for (double sign : {-1,1}) {
        pt v = (d*dr + perp(d)*sqrt(h2)*sign)/d2;
        out.push_back({o1 + v*r1, o2 + v*r2});}
    return 1 + (h2 > 0);
```

3D geometry

$$\text{orient}(P, Q, R, S) = (\overline{PQ} \times \overline{PR}) \cdot \overline{PS}$$

S above $PQRS$ iff > 0 .

For plane $ax + by + cz = d$ def $\bar{n} = (a, b, c)$.

Line with normal \bar{n} through point P has $d = \bar{n} \cdot P$.

$\text{side}_\Pi(P) = \bar{n} \cdot P - d$ sign determines side from Π .

$\text{dist}_\Pi(P) = \text{side}_\Pi(P)/\|\bar{n}\|$.

Translating plane by \bar{t} makes $d' = d + \bar{n} \cdot \bar{t}$.

Plane-plane intersection of has direction $\bar{n}_1 \times \bar{n}_2$ and goes through $((d_1 \bar{n}_2 - d_2 \bar{n}_1) \times \bar{d})/\|\bar{d}\|^2$.

Line-line distance:

```
double dist(line3d l1, line3d l2) {
    p3 n = l1.d*l2.d;
    if (n == zero) // parallel
        return l1.dist(l2.o);
    return abs((l2.o-l1.o)|n)/abs(n);
```

Spherical to Cartesian:

$$(r \cos \varphi \cos \lambda, r \cos \varphi \sin \lambda, r \sin \varphi).$$

Sphere-line intersection:

```
int sphereLine(p3 o, double r, line3d l, pair<p3,p3> &out) {
    double h2 = r*r - l.sqDist(o);
    if (h2 < 0) return 0; // the line doesn't touch the sphere
    p3 p = l.proj(o); // point P
    p3 h = l.d*sqrt(h2)/abs(l.d); // vector
```

```
parallel to l, of length h
out = {p-h, p+h};
return 1 + (h2 > 0);
```

Great-circle distance between points A and B is $r\angle AOB$.

Spherical segment intersection:

```
bool properInter(p3 a, p3 b, p3 c, p3 d, p3 &out)
{
    p3 ab = a*b, cd = c*d; // normals of planes OAB and OCD
    int oa = sgn(cd|a),
        ob = sgn(cd|b),
        oc = sgn(ab|c),
        od = sgn(ab|d);
    out = ab*cd*od; // four multiplications => careful with overflow !
    return (oa != ob && oc != od && oa != oc);
}
```

```
bool onSphSegment(p3 a, p3 b, p3 p) {
    p3 n = a*b;
    if (n == zero)
        return a*p == zero && (a|p) > 0;
    return (n|p) == 0 && (n|a*p) >= 0 && (n|b*p) <= 0;
}
```

```
struct directionSet : vector<p3> {
    using vector::vector; // import constructors
    void insert(p3 p) {
        for (p3 q : *this) if (p*q == zero) return;
        push_back(p);
    }
};
```

```
directionSet intersSph(p3 a, p3 b, p3 c, p3 d) {
    assert(validSegment(a, b) && validSegment(c, d));
    p3 out;
    if (properInter(a, b, c, d, out)) return {out};
    directionSet s;
    if (onSphSegment(c, d, a)) s.insert(a);
    if (onSphSegment(c, d, b)) s.insert(b);
    if (onSphSegment(a, b, c)) s.insert(c);
    if (onSphSegment(a, b, d)) s.insert(d);
    return s;
}
```

Angle between spherical segments AB and AC is angle between $A \times B$ and $A \times C$.

Oriented angle: subtract from 2π if mixed product is negative.

Area of a spherical polygon:

$$r^2[\text{sum of interior angles} - (n-2)\pi].$$

```

Triangle centers
const double min_delta = 1e-13;
const double coord_max = 1e6;
typedef complex<double> point;
point A, B, C; // vertexes of the triangle
bool collinear() {
    double min_diff =
        min(abs(A - B), min(abs(A - C), abs(B - C)));
    if (min_diff < coord_max * min_delta) return true;
    point sp = (B - A) / (C - A);
    double ang = M_PI / 2 - abs(abs(arg(sp)) - M_PI / 2);
    return ang < min_delta;
    // positive angle with the real line
}
point circum_center() {
    if (collinear()) return point(NAN, NAN);
    // squared lengths of sides
    double a2 = norm(B - C);
    double b2 = norm(A - C);
    double c2 = norm(A - B);
    // barycentric coordinates of the circumcenter
    // sin(2 * alpha) works also
    double c_A = a2 * (b2 + c2 - a2);
    double c_B = b2 * (a2 + c2 - b2);
    double c_C = c2 * (a2 + b2 - c2);
    double sum = c_A + c_B + c_C;
    c_A /= sum;
    c_B /= sum;
    c_C /= sum;
    return c_A * A + c_B * B + c_C * C; // cartesian
}
point centroid() { // center of mass
    return (A + B + C) / 3.0;
}
point ortho_center() { // euler line
    point O = circum_center();
    return O + 3.0 * (centroid() - O);
};
point nine_point_circle_center() { // euler line
    point O = circum_center();
    return O + 1.5 * (centroid() - O);
};
point in_center() {
    if (collinear()) return point(NAN, NAN);
    double a = abs(B - C); // side lenghts
    double b = abs(A - C);
    double c = abs(A - B);
    // trilinear coordinates are (1,1,1)
    double sum = a + b + c;
    a /= sum;
    b /= sum;
    c /= sum;
    return a * A + b * B + c * C; // cartesian
}

```

```

} %9596
Seg-Seg intersection, halfplane intersection area
struct Seg {
    Vec a, b;
    Vec d() { return b - a; }
}; %1709
Vec intersection(Seg l, Seg r) {
    Vec dl = l.d(), dr = r.d();
    if (cross(dl, dr) == 0) return {nanl(""), nanl("")};
    double h = cross(dr, l.a - r.a) / len(dr);
    double dh = cross(dr, dl) / len(dr);
    return l.a + dl * (h / -dh);
} // Returns the area bounded by halfplanes
double calc_area(const vector<Seg>& lines) {
    double lb = -HUGE_VAL, ub = HUGE_VAL;
    vector<Seg> slines[2];
    for (auto line : lines) {
        if (line.b.y == line.a.y) {
            if (line.a.x < line.b.x) {
                lb = max(lb, line.a.y);
            } else {
                ub = min(ub, line.a.y);
            }
        } else if (line.a.y < line.b.y) {
            slines[1].push_back(line);
        } else {
            slines[0].push_back({line.b, line.a});
        }
    }
    ran(i, 0, 2) {
        sort(slines[i].begin(), slines[i].end(),
            [&](Seg l, Seg r) {
                if (cross(l.d(), r.d()) == 0)
                    return normal(l.d()) * l.a -
                        normal(r.d()) * r.a;
                return (1 - 2 * i) * cross(l.d(), r.d()) < 0;
            });
    }
    // Now find the application area of the lines and clean
    // up redundant ones
    vector<double> ap_s[2];
    ran(side, 0, 2) {
        vector<double>& apply = ap_s[side];
        vector<Seg> clines;
        for (auto line : slines[side]) {
            while (clines.size() > 0) {
                Seg other = clines.back();
                if (cross(line.d(), other.d()) != 0) {
                    double start = intersection(line, other).y;
                    if (start > apply.back()) break;
                }
                clines.pop_back();
                apply.pop_back();
            }
            if (clines.size() == 0) {
                apply.push_back(-HUGE_VAL);
            }
        }
        else {
            apply.push_back(
                intersection(line, clines.back().y));
        }
        clines.push_back(line);
    }
    slines[side] = clines;
}
ap_s[0].push_back(HUGE_VALL);
ap_s[1].push_back(HUGE_VALL);
double result = 0;
{
    double lb = -HUGE_VALL, ub;
    for (int i = 0, j = 0; i < (int)slines[0].size() &&
        j < (int)slines[1].size(); 4531
        lb = ub) {
        ub = min(ap_s[0][i + 1], ap_s[1][j + 1]);
        double alb = lb, aub = ub;
        Seg l[2] = {slines[0][i], slines[1][j]};
        if (cross(l[1].d(), l[0].d()) > 0) {
            alb = max(alb, intersection(l[0], l[1]).y);
        } else if (cross(l[1].d(), l[0].d()) < 0) {
            aub = min(aub, intersection(l[0], l[1]).y);
        }
        alb = max(alb, lb);
        aub = min(aub, ub);
        aub = max(aub, alb);
        ran(k, 0, 2) {
            double x1 = l[0].a.x + (alb - l[0].a.y) /
                l[0].d().y * l[0].d().x;
            double x2 = l[0].a.x + (aub - l[0].a.y) /
                l[0].d().y * l[0].d().x;
            result += 8864
                (-1 + 2 * k) * (aub - alb) * (x1 + x2) / 2;
        }
        if (ap_s[0][i + 1] < ap_s[1][j + 1]) {
            i++;
        } else {
            j++;
        }
    }
}
return result;
} %3672
Convex polygon algorithms
typedef pair<int, int> Vec;
typedef pair<Vec, Vec> Seg;
typedef vector<Seg>::iterator SegIt;
#define F first
#define S second
#define MP(x, y) make_pair(x, y)
Vec sub(const Vec &v1, const Vec &v2) {
    return MP(v1.F - v2.F, v1.S - v2.S);
}
ll dot(const Vec &v1, const Vec &v2) {
    return (ll)v1.F * v2.F + (ll)v1.S * v2.S;
} 9034

```

```

11 cross(const Vec &v1, const Vec &v2) {
    return (ll)v1.F * v2.S - (ll)v2.F * v1.S;
}
11 dist_sq(const Vec &p1, const Vec &p2) {
    return (ll)(p2.F - p1.F) * (p2.F - p1.F) +
        (ll)(p2.S - p1.S) * (p2.S - p1.S);
}
} struct Point;
multiset<Point>::iterator end_node;
struct Point {
    Vec p;
    typename multiset<Point>::iterator get_it() const {
        // gcc rb_tree dependent
        tuple<void *> tmp = {(void *)this - 32};
        return *(multiset<Point>::iterator *)&tmp;
    }
    bool operator<(const Point &rhs) const {
        return (p.F < rhs.p.F); // sort by x
    }
    bool operator<(const Vec &q) const {
        auto nxt = next(get_it()); // convex hull trick
        if (nxt == end_node) return 0; // nxt == end()
        return q.S * dot(p, {q.F, 1}) <
            q.S * dot(nxt->p, {q.F, 1});
    }
}; template <int part> // 1 = upper, -1 = lower
struct HullDynamic : public multiset<Point, less<> {
    bool bad(iterator y) {
        if (y == begin()) return 0;
        auto x = prev(y);
        auto z = next(y);
        if (z == end())
            return y->p.F == x->p.F && y->p.S <= x->p.S;
        return part *
            cross(sub(y->p, x->p), sub(y->p, z->p)) <=
                0;
    }
    void insert_point(int m, int b) { // O(log(N))
        auto y = insert({{m, b}});
        if (bad(y)) {
            erase(y);
            return;
        }
        while (next(y) != end() && bad(next(y)))
            erase(next(y));
        while (y != begin() && bad(prev(y))) erase(prev(y));
    }
    ll eval(
        int x) { // O(log(N)) upper maximize dot({x, 1}, v)
        end_node =
            end(); // lower minimize dot({x, 1}, v)
        auto it = lower_bound((Vec){x, part});
        return (ll)it->p.F * x + it->p.S;
    }
}; struct Hull {
    vector<Seg> hull;
    SegIt up_beg;
    template <typename It>
    void extend(It beg, It end) { // O(n)
        vector<Vec> r;
        for (auto it = beg; it != end; ++it) {
            if (r.empty() || *it != r.back()) {
                while (r.size() >= 2) {
                    int n = r.size();
                    Vec v1 = {r[n - 1].F - r[n - 2].F,
                        r[n - 1].S - r[n - 2].S};
                    Vec v2 = {
                        it->F - r[n - 2].F, it->S - r[n - 2].S};
                    if (cross(v1, v2) > 0) break;
                    r.pop_back();
                }
                r.push_back(*it);
            }
        }
        ran(i, 0, (int)r.size() - 1)
            hull.emplace_back(r[i], r[i + 1]);
    }
    Hull(vector<Vec> &vert) { // atleast 2 distinct points
        sort(vert.begin(), vert.end()); // O(n log(n))
        extend(vert.begin(), vert.end());
        int diff = hull.size();
        extend(vert.rbegin(), vert.rend());
        up_beg = hull.begin() + diff;
    }
    bool contains(Vec p) { // O(log(n))
        if (p < hull.front().F || p > up_beg->F)
            return false;
    {
        auto it_low = lower_bound(hull.begin(), up_beg,
            MP(MP(p.F, (int)-2e9), MP(0, 0)));
        if (it_low != hull.begin()) --it_low;
        Vec a = {it_low->S.F - it_low->F.F,
            it_low->S.S - it_low->F.S};
        Vec b = {p.F - it_low->F.F, p.S - it_low->F.S};
        if (cross(a, b) <
            0) // < 0 is inclusive, <= 0 is exclusive
            return false;
    }
    {
        auto it_up = lower_bound(hull.rbegin(),
            hull.rbegin() + (hull.end() - up_beg),
            MP(MP(p.F, (int)2e9), MP(0, 0)));
        if (it_up - hull.rbegin() == hull.end() - up_beg)
            --it_up;
        Vec a = {it_up->F.F - it_up->S.F,
            it_up->F.S - it_up->S.S};
        Vec b = {p.F - it_up->S.F, p.S - it_up->S.S};
        if (cross(a, b) >
            0) // > 0 is inclusive, >= 0 is exclusive
            return false;
    }
    return true;
}
} // The function can have only one local min and max
// and may be constant only at min and max.
template <typename T>
SegIt max(function<T(Seg &)> f) { // O(log(n))
    auto l = hull.begin();
    auto r = hull.end();
    SegIt b = hull.end();
    T b_v;
    while (r - l > 2) {
        auto m = l + (r - l) / 2;
        T l_v = f(*l);
        T l_n_v = f(*(l + 1));
        T m_v = f(*m);
        T m_n_v = f(*(m + 1));
        if (b == hull.end() || l_v > b_v) {
            b = l; // If max is at l we may remove it from
                   // the range.
            b_v = l_v;
        }
        if (l_n_v > l_v) {
            if (m_v < l_v) {
                r = m;
            } else {
                if (m_n_v > m_v) {
                    l = m + 1;
                } else {
                    r = m + 1;
                }
            }
        } else {
            if (m_v < l_v) {
                l = m + 1;
            } else {
                if (m_n_v > m_v) {
                    l = m + 1;
                } else {
                    r = m + 1;
                }
            }
        }
    }
    T l_v = f(*l);
    if (b == hull.end() || l_v > b_v) {
        b = l;
        b_v = l_v;
    }
    if (r - l > 1) {
        T l_n_v = f(*(l + 1));
        if (b == hull.end() || l_n_v > b_v) {
            b = l + 1;
            b_v = l_n_v;
        }
    }
    return b;
}
} SegIt closest( %3267
2551
3586
8311
7715
9864
7606
%5939

```

```

Vec p) { // p can't be internal(can be on border),
    // hull must have atleast 3 points
Seg &ref_p = hull.front(); // O(log(n))
return max(function<double>(Seg &)>(
    [&p, &ref_p](Seg &seg) { // accuracy of used type
        // should be coord^-2
        if (p == seg.F) return 10 - M_PI;
        Vec v1 = {seg.S.F - seg.F.F, seg.S.S - seg.F.S}; 7855
        Vec v2 = {p.F - seg.F.F, p.S - seg.F.S};
        ll c_p = cross(v1, v2); 5939
        if (c_p > 0) { // order the backside by angle
            Vec v1 = {ref_p.F.F - p.F, ref_p.F.S - p.S};
            Vec v2 = {seg.F.F - p.F, seg.F.S - p.S};
            ll d_p = dot(v1, v2); 5063
            ll c_p = cross(v2, v1);
            return atan2(c_p, d_p) / 2;
        }
        ll d_p = dot(v1, v2);
        double res = atan2(d_p, c_p); 0469
        if (d_p <= 0 && res > 0) res = -M_PI;
        if (res > 0) {
            res += 20;
        } else {
            res = 10 - res;
        }
        return res;
    });
}); 3631
} %5632
template <int DIRECTION> // 1 or -1
Vec tan_point(
    Vec p) { // can't be internal or on border
    // -1 iff CCW rotation of ray from p to res takes it
    // away from
    // polygon?
    Seg &ref_p = hull.front(); // O(log(n))
    auto best_seg = max(function<double>(Seg &)>(
        [&p, &ref_p](Seg &seg) { // accuracy of used type
            // should be coord^-2
            Vec v1 = {ref_p.F.F - p.F, ref_p.F.S - p.S};
            Vec v2 = {seg.F.F - p.F, seg.F.S - p.S};
            ll d_p = dot(v1, v2); 0212
            ll c_p = DIRECTION * cross(v2, v1);
            return atan2(c_p, d_p); // order by signed angle
        }));
    return best_seg->F; 5890
} %5890
SegIt max_in_dir(
    Vec v) { // first is the ans. O(log(n))
return max(function<ll>(Seg &)>(
    [&v](Seg &seg) { return dot(v, seg.F); }));
} %5805
pair<SegIt, SegIt> intersections(Seg l) { // O(log(n))
    int x = l.S.F - l.F.F;
    int y = l.S.S - l.F.S; 0286
    Vec dir = {-y, x};
    auto it_max = max_in_dir(dir);
    auto it_min = max_in_dir(MP(y, -x)); 7759
}

ll opt_val = dot(dir, l.F);
if (dot(dir, it_max->F) < opt_val ||
    dot(dir, it_min->F) > opt_val)
    return MP(hull.end(), hull.end()); 8921
SegIt it_r1, it_r2;
function<bool>(const Seg &, const Seg &)> inc_c(
    [&dir](const Seg &lft, const Seg &rgt) {
        return dot(dir, lft.F) < dot(dir, rgt.F);
    });
function<bool>(const Seg &, const Seg &)> dec_c(
    [&dir](const Seg &lft, const Seg &rgt) {
        return dot(dir, lft.F) > dot(dir, rgt.F);
    });
if (it_min <= it_max) {
    it_r1 =
        upper_bound(it_min, it_max + 1, l, inc_c) - 1;
    if (dot(dir, hull.front().F) >= opt_val) {
        it_r2 = upper_bound( 8531
            hull.begin(), it_min + 1, l, dec_c) -
        1;
    } else {
        it_r2 =
            upper_bound(it_max, hull.end(), l, dec_c) - 1; 1848
    }
} else {
    it_r1 =
        upper_bound(it_max, it_min + 1, l, dec_c) - 1;
    if (dot(dir, hull.front().F) <= opt_val) {
        it_r2 = upper_bound( 1538
            hull.begin(), it_max + 1, l, inc_c) -
        1;
    } else {
        it_r2 =
            upper_bound(it_min, hull.end(), l, inc_c) - 7300
    }
}
return MP(it_r1, it_r2); 2168
} %2632
Seg diameter() { // O(n)
    Seg res;
    ll dia_sq = 0;
    auto it1 = hull.begin();
    auto it2 = up_beg;
    Vec v1 = {hull.back().S.F - hull.back().F.F,
              hull.back().S.S - hull.back().F.S};
    while (it2 != hull.begin()) {
        Vec v2 = {(it2 - 1)->S.F - (it2 - 1)->F.F,
                  (it2 - 1)->S.S - (it2 - 1)->F.S}; 5150
        if (cross(v1, v2) > 0) break;
        --it2;
    }
    while (
        it2 != hull.end()) { // check all antipodal pairs
        if (dist_sq(it1->F, it2->F) > dia_sq) {
            res = {it1->F, it2->F}; 1013
            dia_sq = dist_sq(res.F, res.S);
        }
    }
}

Vec v1 = {
    it1->S.F - it1->F.F, it1->S.S - it1->F.S};
Vec v2 = {
    it2->S.F - it2->F.F, it2->S.S - it2->F.S}; 2168
if (cross(v1, v2) == 0) {
    if (dist_sq(it1->S, it2->F) > dia_sq) {
        res = {it1->S, it2->F};
        dia_sq = dist_sq(res.F, res.S);
    }
    if (dist_sq(it1->F, it2->S) > dia_sq) {
        res = {it1->F, it2->S};
        dia_sq = dist_sq(res.F, res.S);
    }
} // report cross pairs at parallel lines.
++it1;
++it2;
} else if (cross(v1, v2) < 0) {
    ++it1;
} else {
    ++it2;
}
return res; 3883
} %1111
Delaunay triangulation O(nlogn)
const int max_co = (1 << 28) - 5;
struct Vec {
    int x, y;
    bool operator==(const Vec &oth) { 9015
        return x == oth.x && y == oth.y;
    }
    bool operator!=(const Vec &oth) { 5165
        return !operator==(oth);
    }
    Vec operator-(const Vec &oth) { 1233
        return {x - oth.x, y - oth.y};
    }
    ll cross(Vec a, Vec b) { 8495
        return (ll)a.x * b.y - (ll)a.y * b.x;
    }
    ll dot(Vec a, Vec b) { 2168
        return (ll)a.x * b.x + (ll)a.y * b.y;
    }
    struct Edge {
        Vec tar;
        Edge *nxxt;
        Edge *inv = NULL;
        Edge *rep = NULL;
        bool vis = false;
    };
    struct Seg {
        Vec a, b;
        bool operator==(const Seg &oth) { 3668
            return a == oth.a && b == oth.b;
        }
        bool operator!=(const Seg &oth) { 4994
    }
}

```

```

    return !operator==(oth);
}
};

ll orient(Vec a, Vec b, Vec c) {           6432
    return (ll)a.x * (b.y - c.y) + (ll)b.x * (c.y - a.y) +
        (ll)c.x * (a.y - b.y);
}                                               %3775
bool in_c_circle(Vec *arr, Vec d) {          0172}
    if (cross(arr[1] - arr[0], arr[2] - arr[0]) == 0)
        return true; // degenerate
    ll m[3][3];
    ran(i, 0, 3) {
        m[i][0] = arr[i].x - d.x;
        m[i][1] = arr[i].y - d.y;
        m[i][2] = m[i][0] * m[i][0];
        m[i][2] += m[i][1] * m[i][1];
    }
    __int128 res = 0; //double seems to work as well
    res +=
        (__int128)(m[0][0] * m[1][1] - m[0][1] * m[1][0]) *
        m[2][2];                                         4639
    res +=
        (__int128)(m[1][0] * m[2][1] - m[1][1] * m[2][0]) *
        m[0][2];
    res -=
        (__int128)(m[0][0] * m[2][1] - m[0][1] * m[2][0]) *
        m[1][2];                                         7716
    return res > 0;
}                                               %1845
Edge *add_triangle(Edge *a, Edge *b, Edge *c) {
    Edge *old[] = {a, b, c};
    Edge *tmp = new Edge[3];                         7117
    ran(i, 0, 3) {
        old[i]->rep = tmp + i;
        tmp[i] = {
            old[i]->tar, tmp + (i + 1) % 3, old[i]->inv};
        if (tmp[i].inv) tmp[i].inv->inv = tmp + i;
    }
    return tmp;
}
Edge *add_point(
    Vec p, Edge *cur) { // returns outgoing edge
    Edge *triangle[] = {cur, cur->nxt, cur->nxt->nxt}; 4184
    ran(i, 0, 3) {
        if (orient(triangle[i]->tar,
                    triangle[(i + 1) % 3]->tar, p) < 0)
            return NULL;
    }
    ran(i, 0, 3) {                                     4768
        if (triangle[i]->rep) {
            Edge *res = add_point(p, triangle[i]->rep);
            if (res)
                return res; // unless we are on last layer we
                               // must exit here
        }
    }
    Edge p_as_e{p};
}

Edge tmp{cur->tar};
tmp.inv = add_triangle(&p_as_e, &tmp, cur = cur->nxt);           0194
Edge *res = tmp.inv->nxt;
tmp.tar = cur->tar;
tmp.inv = add_triangle(&p_as_e, &tmp, cur = cur->nxt);           8359
tmp.tar = cur->tar;
res->inv = add_triangle(&p_as_e, &tmp, cur = cur->nxt);
res->inv->inv = res;                                              4263
return res;
}

Edge *delaunay(vector<Vec> &points) {
    random_shuffle(points.begin(), points.end());
    Vec arr[] = {{4 * max_co, 4 * max_co},
                 {-4 * max_co, max_co}, {max_co, -4 * max_co}};
    Edge *res = new Edge[3];
    ran(i, 0, 3) res[i] = {arr[i], res + (i + 1) % 3};
    for (Vec &cur : points) {
        Edge *loc = add_point(cur, res);
        Edge *out = loc;
        arr[0] = cur;
        while (true) {
            arr[1] = out->tar;
            arr[2] = out->nxt->tar;
            Edge *e = out->nxt->inv;
            if (e && in_c_circle(arr, e->nxt->tar)) {
                Edge tmp{cur};
                tmp.inv = add_triangle(&tmp, out, e->nxt);
                tmp.tar = e->nxt->tar;
                tmp.inv->inv =
                    add_triangle(&tmp, e->nxt->nxt, out->nxt->nxt);
                out = tmp.inv->nxt;
                continue;
            }
            out = out->nxt->nxt->inv;
            if (out->tar == loc->tar) break;
        }
        return res;
    }
}

void extract_triangles(
    Edge *cur, vector<vector<Seg>> &res) {
    if (!cur->vis) {
        bool inc = true;
        Edge *it = cur;
        do {
            it->vis = true;
            if (it->rep) {
                extract_triangles(it->rep, res);
                inc = false;
            }
            it = it->nxt;
        } while (it != cur);
        if (inc) {
            Edge *triangle[3] = {cur, cur->nxt, cur->nxt->nxt};
            res.resize(res.size() + 1);
            vector<Seg> &tar = res.back();
            ran(i, 0, 3) {
                if ((abs(triangle[i]->tar.x) < max_co &&
                     abs(triangle[(i + 1) % 3]->tar.x) <
                     max_co))
                    tar.push_back({triangle[i]->tar,
                                   triangle[(i + 1) % 3]->tar});
            }
            if (tar.empty()) res.pop_back();
        }
    }
}                                               %8602
}

Contest setup
alias g++='g++ -g -Wall -Wshadow -Wconversion \
-fsanitize=undefined,address -DCDEBUG'      #.bashrc
alias a='setxkbmap us -option'               #.bashrc
alias m='setxkbmap us -option caps:escape'   #.bashrc
alias ma='setxkbmap us -variant dvp \
-option caps:escape'                        #.bashrc
gsettings set org.compiz.core: \
    /org/compiz/profiles/Default/plugins/core/ hsize 4 #settings
gsettings set org.gnome.desktop.wm.preferences \
    focus-mode 'sloppy'                         #settings
gvim template.cpp
cd samps                                #copy everything
for d in *; do cd $d; for f in *; do \
    cp $f "../${d,,}${f,,}"; done; \
    cd ..; cp "../template.cpp" "../${d,,}.cpp"; done
cd ..
set si cin
set ts=4 sw=4 noet
set cb=unnamedplus
(global-set-key (kbd "C-x <next>") 'other-window) #.emacs
(global-set-key (kbd "C-x <prior>") \
    'previous-multiframe-window)                      #.emacs
(global-set-key (kbd "C-M-z") 'ansi-term)           #.emacs
(global-linum-mode 1)                          #.emacs
(column-number-mode 1)                         #.emacs
(show-paren-mode 1)                           #.emacs
(setq-default indent-tabs-mode nil)            #.emacs
valgrind --vgdb-error=0 ./a <inp &           #valgrind
gdb a                                         #valgrind
target remote | vgdb
crc.sh
#!/bin/env bash
for j in `seq $2 1 $3`; do #whitespace don't matter.
    sed '/^\$s*/d' $1 | head -$j | tr -d '[:space:]' \
    | cksum | cut -f1 -d ' ' | tail -c 5
done #there shouldn't be any COMMENTS.
#copy lines being checked to separate file.
# $ ./crc.sh tmp.cpp 999 999
# $ ./crc.sh tmp.cpp 1 333 | grep XXXX
gcc ordered set, hashtable
#define DEBUG(...) cerr << __VA_ARGS__ << endl;
#ifndef CDEBUG
#define DEBUG
#define DEBUG(...) ((void)0);
#define NDEBUG

```

9617

7204

%8602

#.vimrc

#.vimrc

#.emacs

7485

```

#endif
#define ran(i, a, b) for (auto i = (a); i < (b); i++) 4696
#include <bits/stdc++.h>
typedef long long ll;
typedef long double ld;
using namespace std; %8529
#pragma GCC optimize("Ofast") // better vectorization
#pragma GCC target("avx,avx2")
// double vectorized performance
#include <bits/extc++.h> 7700
using namespace __gnu_pbds;
template <typename T, typename U> %8529
using hashmap = gp_hash_table<T, U>; %8529
// dumb, 3x faster than stl 2061
template <typename T>
using ordered_set = tree<T, null_type, less<T>, %8529
    rb_tree_tag, tree_order_statistics_node_update>;
int main() {
    ordered_set<int> cur;
    cur.insert(1);
    cur.insert(3);
    cout << cur.order_of_key(2) << endl;
    // the number of elements in the set less than 2
    cout << *cur.find_by_order(1) << endl;
    // the 1-st smallest number in the set(0-based)
    ordered_set<int> oth;
    oth.insert(5); // to join: cur < oth
    cur.join(oth); // cur = {1, 3, 5}, oth = {}
    cur.split(1, oth); // cur = {1}, oth = {3, 5}
    hashmap<int, int> h({}, {}, {}, {}, {1 << 16}); %8529
}

                PRNGs and Hash functions

mt19937 gen;
uint64_t rand64() { %5668
    return gen() ^ ((uint64_t)gen() << 32);
}
uint64_t rand64() { %6873
    static uint64_t x = 1; //x != 0
    x ^= x >> 12;
    x ^= x << 25;
    x ^= x >> 27;
    return x * 0x2545f4914f6cdd1d; // can remove mult
}
uint64_t mix(uint64_t x){ // deadbeef -> y allowed
variable uint64_t mem[2] = { x, 0xdeadbeeffeebdaedull }; %6873
    asm volatile ( %3187
        "pxor %%xmm0, %%xmm0;" %8147
        "movdq (%0), %%xmm1;" %8147
        "aesenc %%xmm0, %%xmm1;" %8147
        "movdq %%xmm1, (%0);" %8147
        :
        : "r" (&mem[0]) %8147
        : "memory" %8147
    );
    return mem[0]; // use both slots for 128 bit
}
uint64_t mix64(uint64_t x) f //x != 0 %7419P

```

```
4696     x = (x ^ (x >> 30)) * 0xbff58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        x = x ^ (x >> 31);
    return x;
}
%8529 uint64_t unmix64(uint64_t x) {
n     x = (x ^ (x >> 31) ^ (x >> 62)) * 0x319642b2d24f1;
     x = (x ^ (x >> 27) ^ (x >> 54)) * 0x96de1b173f1;
     x = x ^ (x >> 30) ^ (x >> 60);
    return x;
}
7700 uint64_t combine64(uint64_t x, uint64_t y) {
2061     if (y < x) swap(x, y); // remove for ord
     return mix64(mix64(x) + y);
}
Memmypool
const int BLOCK = 8;
const int MEM_SIZE = 1 << 26;
char glob_buf[MEM_SIZE];
int glob_idx;
vector<bool> glob_used;
void init_mem() {
    glob_used.resize(MEM_SIZE / BLOCK);
    glob_used[0] = true;
}
template <typename T>
struct Ptr {
    unsigned idx;
    explicit Ptr(T *tar) { idx = (char *)tar - glob_buf; }
    Ptr() { idx = 0; }
    template <typename... Args>
    void construct(Args... args) {
        new (glob_buf + idx) T(args...);
    }
    T *operator->() {
        assert(idx);
        return (T *)(glob_buf + idx);
    }
    T &operator*() { return *operator->(); }
    bool operator==(const Ptr &oth) const {
        return idx == oth.idx;
    }
%5668 operator unsigned() const { return idx; }
    Ptr &operator+=(int diff) {
        idx += diff * sizeof(T);
        return *this;
    }
    Ptr operator+(int diff) {
        Ptr res;
        res.idx = idx;
        return res += diff;
    }
    T &operator[](int diff) { return *operator+(diff); }
};
template <typename T, typename... Args>
Ptr<T> alloc(int n, Args... args) {
    unsigned len = 0; // TLE if running low on mem
```

```

const int nmax = 5e7;
ll arr[nmax], tmp[nmax];
int main() {
    for (int i = 0; i < nmax; ++i)
        arr[i] = ((ll)rand() << 32) | rand();
    rsort(arr, tmp, nmax);
    assert(is_sorted(arr, arr + nmax));
}

FFT 10-15M length/sec
// integer c = ab is accurate if c_i < 2^49
#pragma GCC optimize ("Ofast") //10% performance
#include <complex.h>
extern "C" __complex__ double __muldc3(
    double a, double b, double c, double d){ 1242
    return a*c-b*d+I*(a*d-b*c); // 40% performance
}
#include <bits/stdc++.h> 3540
typedef complex<double> Comp;
void fft_rec(Comp *arr, Comp *root_pow, int len) { 6092
    if (len != 1) {
        fft_rec(arr, root_pow, len >> 1);
        fft_rec(arr + len, root_pow, len >> 1);
    }
    root_pow += len; 1085
    ran(i, 0, len){ 5001
        tie(arr[i], arr[i + len]) = pair<Comp, Comp> {
            arr[i] + root_pow[i] * arr[i + len],
            arr[i] - root_pow[i] * arr[i + len] };
    }
}
void fft(vector<Comp> &arr, int ord, bool invert) { 7008
    assert(arr.size() == 1 << ord);
    static vector<Comp> root_pow(1);
    static int inc_pow = 1;
    static bool is_inv = false; 8060
    if (inc_pow <= ord) {
        int idx = root_pow.size();
        root_pow.resize(1 << ord);
        for (; inc_pow <= ord; ++inc_pow) { 8269
            for (int idx_p = 0; idx_p < 1 << (ord - 1);
                 idx_p += 1 << (ord - inc_pow), ++idx) { 0935
                root_pow[idx] = Comp {
                    cos(-idx_p * M_PI / (1 << (ord - 1))), 5222
                    sin(-idx_p * M_PI / (1 << (ord - 1))) };
                if (is_inv) root_pow[idx] = conj(root_pow[idx]);
            }
        }
    }
    if (invert != is_inv) { 8698
        is_inv = invert;
        for (Comp &cur : root_pow) cur = conj(cur);
    }
    int j = 0;
    ran(i, 1, (1<<ord)){ 8698
        int m = 1 << (ord - 1);
        bool cont = true;
        while (cont) {

```

```

ll v = arithm.sqp1(lv);
int idx = 1;
int tar = 1;
while (true) {
    ll cur = 1;
    ll v_cur = v;
    int j_stop = min(cum_cnt, tar - idx);
    for (int j = 0; j < j_stop; ++j) {
        cur = arithm.multf(cur, abs(v_cur - lv));
        v_cur = arithm.sqp1(v_cur);
        ++idx;
    }
    if (!cur) {
        for (int j = 0; j < cum_cnt; ++j) {
            ll g = __gcd(abs(v - lv), n);
            if (g == 1) {
                v = arithm.sqp1(v);
            } else if (g == n) {
                break;
            } else {
                return g;
            }
        }
        break;
    } else {
        ll g = __gcd(cur, n);
        if (g != 1) return g;
    }
    v = v_cur;
    idx += j_stop;
    if (idx == tar) {
        lv = v;
        tar *= 2;
        v = arithm.sqp1(v);
        ++idx;
    }
}
map<ll, int> prime_factor(
    ll n, map<ll, int> *res = NULL) {
// n <= 1<<62, ~1000/s (<500/s on CF)
if (!res) {
    map<ll, int> res_act;
    for (int p : small_primes) {
        while (!(n % p)) {
            ++res_act[p];
            n /= p;
        }
    }
    if (n != 1) prime_factor(n, &res_act);
    return res_act;
}
if (is_prime(n)) {
    ++(*res)[n];
} else {
    ll factor = pollard_rho(n);
}
```

```

    prime_factor(factor, res);
    prime_factor(n / factor, res);
}
return map<ll, int>();
} // Usage: fact = prime_factor(n);
        Berlekamp-Massey O(LN)
%1140
template <typename T, T P>
struct intmod {
    intmod() {}
constexpr intmod(T t) : x((t + P) % P) {}
T value() const { return x; }
bool operator!==(const intmod<T, P> i) { return x != i.x; }
bool operator==(const intmod<T, P> i) { return x == i.x; }
intmod<T, P> &operator+=(const intmod<T, P> i) {
    x = (x + i.x) % P;
    return *this;
}
intmod<T, P> &operator-=(const intmod<T, P> i) {
    x = (x - i.x) % P;
    return *this;
}
intmod<T, P> &operator*=(const intmod<T, P> i) {
    x = ((11)x * i.x) % P;
    return *this;
}
intmod<T, P> &operator/=(const intmod<T, P> i) {
    x = ((11)x * i.inverse().x) % P;
    return *this;
}
intmod<T, P> operator+(const intmod<T, P> i) const {
    auto j = *this;
    return j += i;
}
intmod<T, P> operator-(const intmod<T, P> i) const {
    auto j = *this;
    return j -= i;
}
intmod<T, P> operator*(const intmod<T, P> i) const {
    auto j = *this;
    return j *= i;
}
intmod<T, P> operator/(const intmod<T, P> i) const {
    auto j = *this;
    return j /= i;
}
intmod<T, P> operator-() const {
    intmod<T, P> n;
    n.x = (P - x) % P;
    return n;
}
intmod<T, P> inverse() const {
    if (x == 0) return 0;
    T a = x, b = P;
    T aa = 1, ab = 0;
    T ba = 0, bb = 1;
    while (a) {
        T q = b / a;
        return a;
}
9271
9567
1519
%4128
3023
8818

```

```

T r = b % a;
ba -= aa * q;
bb -= ab * q;
swap(ba, aa);
swap(bb, ab);
b = a;
a = r;
}
intmod<T, P> ix = intmod<T, P>(aa) + intmod<T, P>(ba);
assert(ix * x == unity); 1934
return ix;
}
static const intmod<T, P> zero;
static const intmod<T, P> unity;
private: 9068
T x;

template <typename T, T P>
constexpr intmod<T, P> intmod<T, P>::zero = 0; 8676
template <typename T, T P>
constexpr intmod<T, P> intmod<T, P>::unity = 1; 8052
using rem = intmod<char, 2>; %8052
template <typename K>
static vector<K> berlekamp_massey(vector<K> ss) { 8756
vector<K> ts(ss.size());
vector<K> cs(ss.size());
cs[0] = K::unity;
fill(cs.begin() + 1, cs.end(), K::zero); 7200
vector<K> bs = cs;
int l = 0, m = 1;
K b = K::unity;
for (int k = 0; k < (int)ss.size(); k++) { 8023
K d = ss[k];
assert(l <= k);
for (int i = 1; i <= l; i++) d += cs[i] * ss[k - i];
if (d == K::zero) {
m++;
} else if (2 * l <= k) { 5745
K w = d / b;
ts = cs;
for (int i = 0; i < (int)cs.size() - m; i++) 3157
cs[i + m] -= w * bs[i];
l = k + 1 - l;
swap(bs, ts);
b = d;
m = 1;
} else {
K w = d / b;
for (int i = 0; i < (int)cs.size() - m; i++) 2591
cs[i + m] -= w * bs[i];
m++;
}
}
cs.resize(l + 1);
while (cs.back() == K::zero) cs.pop_back();
return cs;
}
%8013

```

```

Linear algebra
bitset<10> add(bitset<10> p, bitset<10> q) {
    return p ^ q;
}
bitset<10> mult(bitset<10> v, bool k) {
    if (k) {
        return v;
    } else {
        return bitset<10>(0);
    }
}
bitset<10> normalize(bitset<10> v, int idx) { return v; }
bitset<10> neg(bitset<10> v) { return v; }
template <typename T>
vector<T> add(vector<T> p, vector<T> q) {
    ran(i, 0, (int)p.size()) p[i] += q[i];
    return p;
}
template <typename T>
vector<T> mult(vector<T> p, T k) {
    ran(i, 0, (int)p.size()) p[i] *= k;
    return p;
}
template <typename T>
vector<T> normalize(vector<T> v, int idx) {
    return mult(v, (T1 / v[idx]));
}
template <typename T>
vector<T> neg(vector<T> p) {
    return mult(p, (T-1));
}
/* V is the class implementing a vector, T is the type
 * within. examples: <bitset<10>, bool>; <vector<double>,
 * double> etc. V must have an "add" operation defined */
template <typename V, typename T>
pair<vector<V>, pair<vector<int>, vector<int>>>
diagonalize(vector<V> matrix, int width) { 9747
    /* width is the number of columns we consider for
     * diagonalizing. all columns after that can be used
     * for things after equal sign etc */
    int cur_row = 0;
    vector<int> crap_columns;
    vector<int> diag_columns;
    ran(i, 0, width) { 1006
        int row_id = -1;
        T best_val = 0; /* may want to replace with epsilon
                           if working over reals */
        ran(j, cur_row, (int)matrix.size()) {
            if (abs(matrix[j][i]) > abs(best_val)) {
                row_id = j;
                best_val = matrix[j][i];
            }
        }
        if (row_id == -1) {
            crap_columns.push_back(i);
        } else {
            diag_columns.push_back(i);
        }
    }
    swap(matrix[cur_row], matrix[row_id]);
    matrix[cur_row] = normalize(matrix[cur_row], i);
    ran(j, cur_row + 1, j < (int)matrix.size()) {
        if (matrix[j][i] != 0) { 6006
            matrix[j] = add(neg(normalize(matrix[j], i)),
                            matrix[cur_row]);
        }
    }
    cur_row++;
}
for (int i = (int)diag_columns.size() - 1; i >= 0; 5201
    --i) {
    for (int j = i - 1; j >= 0; --j) { 0074
        matrix[j] = add(matrix[j],
                        neg(
                            mult(matrix[i], matrix[j][diag_columns[i]])));
    }
}
return {matrix, {diag_columns, crap_columns}}; %9471
template <typename V, typename T>
int matrix_rank(vector<V> matrix, int width) {
    return diagonalize<V, T>(matrix, width)
        .second.first.size(); 5622
}
template <typename V, typename T>
vector<T> one_solution(
    vector<V> matrix, int width, vector<T> y) {
    /* finds one solution to the system Ax = y.
     * each row in matrix must have width at least width
     * + 1. aborts if there is no solution (you can check
     * whether solution exists using matrix_rank) */
    assert(matrix.size() == y.size()); 8765
    ran(i, 0, (int)matrix.size()) matrix[i][width] = y[i];
    pair<vector<V>, pair<vector<int>, vector<int>>> prr =
        diagonalize<V, T>(matrix, width); 5091
    vector<V> diag = prr.first;
    vector<int> diag_cols = prr.second.first;
    vector<T> ans(width, 0); 5278
    ran(i, 0, (int)matrix.size()) {
        if (i < (int)diag_cols.size()) {
            ans[diag_cols[i]] = diag[i][width]; 7136
        } else {
            assert(diag[i][width] == T(0));
            /* replace with epsilon if working over reals */
        }
    }
}
return ans; %4744
template <typename V, typename T>
vector<vector<T>> homog_basis(
    vector<V> matrix, int width) { 7924
    /* finds the basis of the nullspace of matrix */
    pair<vector<V>, pair<vector<int>, vector<int>>> prr =
        diagonalize<V, T>(matrix, width); 7752
    vector<V> diag = prr.first;
    vector<int> diag_cols = prr.second.first;
    vector<int> crap_cols = prr.second.second;
    vector<vector<T>> ans;
    for (int u : crap_cols) {
        vector<T> row(width, 0);
        row[u] = 1;
        ran(i, 0, (int)diag_cols.size())
            row[diag_cols[i]] = -diag[i][u];
        ans.push_back(row);
    }
}
return ans; %5812
Polynomial roots and O(n^2) interpolation
struct Poly {
    vector<double> a;
    double operator()(double x) const {
        double val = 0;
        for (int i = (int)a.size(); i--;) (val *= x) += a[i];
        return val;
    }
    void diff() {
        ran(i, 1, (int)a.size()) a[i - 1] = i * a[i];
        a.pop_back();
    }
    void divroot(double x0) {
        double b = a.back(), c;
        a.back() = 0;
        for (int i = (int)a.size() - 1; i--;) 4494
            c = a[i], a[i] = a[i + 1] * x0 + b, b = c;
        a.pop_back();
    }
}
void divroot(double x0) {
    double b = a.back(), c;
    a.back() = 0;
    for (int i = (int)a.size() - 1; i--;) 4494
        c = a[i], a[i] = a[i + 1] * x0 + b, b = c;
    a.pop_back();
}
/* Description: Finds the real roots to a polynomial.
 * Usage: poly_roots({{2,-3,1}},-1e9,1e9) // solve
 * x^2-3x+2 = 0 Time: O(n^2 \log(1/\epsilon)) */
vector<double> poly_roots(
    Poly p, double xmin, double xmax) {
    if (sz(p.a) == 2) return {-p.a[0] / p.a[1]};
    vector<double> ret;
    Poly der = p;
    der.diff();
    auto dr = poly_roots(der, xmin, xmax);
    dr.push_back(xmin - 1);
    dr.push_back(xmax + 1);
    sort(dr.begin(), dr.end());
    ran(i, 0, (int)dr.size() - 1) { 9906
        double l = dr[i], h = dr[i + 1];
        bool sign = p(l) > 0;
        if (sign ^ (p(h) > 0)) {
            ran(it, 0, 60) { // while (h - l > 1e-8)
                double m = (l + h) / 2, f = p(m);
                if ((f <= 0) ^ sign) {
                    l = m;
                } else {
                    h = m;
                }
            }
        }
    }
}

```

```

        ret.push_back((l + h) / 2);
    }
}
return ret;
} %2596
/* Description: Given $n$ points  $(x[i], y[i])$ , computes
 * an  $n-1$ -degree polynomial  $p$  that passes through them:
 *  $p(x) = a[0]*x^0 + \dots + a[n-1]*x^{n-1}$ . For
 * numerical precision, pick  $x[k] = c*\cos(k/(n-1)*\pi)$ ,
 *  $k=0 \dots n-1$ . Time:  $O(n^2)$  */
typedef vector<double> vd;
vd interpolate(vd x, vd y, int n) {
    vd res(n), temp(n);
    ran(k, 0, n - 1) ran(i, k + 1, n) y[i] =
        (y[i] - y[k]) / (x[i] - x[k]);
    double last = 0;
    temp[0] = 1;
    ran(k, 0, n) {
        ran(i, 0, n) {
            res[i] += y[k] * temp[i];
            swap(last, temp[i]);
            temp[i] -= last * x[k];
        }
    }
    return res;
} %2093
Simplex algorithm
/* Description: Solves a general linear maximization
 * problem: maximize  $c^T x$  subject to  $Ax \leq b$ ,  $x$ 
 *  $\geq 0$ . Returns  $-\infty$  if there is no solution,  $\infty$  if
 * there are arbitrarily good solutions, or the maximum
 * value of  $c^T x$  otherwise. The input vector is set to
 * an optimal  $x$  (or in the unbounded case, an arbitrary
 * solution fulfilling the constraints). Numerical
 * stability is not guaranteed. For better performance,
 * define variables such that  $x = 0$  is viable. Usage:
 * vvd A = {{1, -1}, {-1, 1}, {-1, -2}};
 * vd b = {1, 1, -4}, c = {-1, -1}, x;
 * T val = LPSolver(A, b, c).solve(x);
 * Time:  $O(NM * \#pivots)$ , where a pivot may be e.g. an
 * edge relaxation.  $O(2^n)$  in the general case. Status:
 * seems to work? */
typedef double
T; // long double, Rational, double + mod<P>...
typedef vector<T> vd;
typedef vector<vd> vvd;
const T eps = 1e-8, inf = 1 / .0;
#define MP make_pair
#define ltj(X) \
    if (s == -1 || MP(X[j], N[j]) < MP(X[s], N[s])) s = j
struct LPSolver { %6658
    int m, n;
    vi N, B;
    vvd D;
    LPSolver(const vvd& A, const vd& b, const vd& c) %0843
        : m(sz(b)), %1480
        n(sz(c)),

```

```

N(n + 1),
B(m),
D(m + 2, vd(n + 2)) {
ran(i, 0, m) ran(j, 0, n) D[i][j] = A[i][j];
ran(i, 0, m) {
    B[i] = n + i;
    D[i][n] = -1;
    D[i][n + 1] = b[i];
}
ran(j, 0, n) {
    N[j] = j;
    D[m][j] = -c[j];
}
N[n] = -1;
D[m + 1][n] = 1;
}
void pivot(int r, int s) {
T *a = D[r].data(), inv = 1 / a[s];
ran(i, 0, m + 2) if (i != r && abs(D[i][s]) > eps) {
    T *b = D[i].data(), inv2 = b[s] * inv;
    ran(j, 0, n + 2) b[j] -= a[j] * inv2;
    b[s] = a[s] * inv2;
}
ran(j, 0, n + 2) if (j != s) D[r][j] *= inv;
ran(i, 0, m + 2) if (i != r) D[i][s] *= -inv;
D[r][s] = inv;
swap(B[r], N[s]);
}
bool simplex(int phase) {
int x = m + phase - 1;
for (;;) {
    int s = -1;
    ran(j, 0, n + 1) if (N[j] != -phase) ltj(D[x]);
    if (D[x][s] >= -eps) return true;
    int r = -1;
    ran(i, 0, m) {
        if (D[i][s] <= eps) continue;
        if (r == -1 || MP(D[i][n + 1] / D[i][s], B[i]) <
            MP(D[r][n + 1] / D[r][s], B[r])) r = i;
    }
    if (r == -1) return false;
    pivot(r, s);
}
}
T solve(vd& x) {
int r = 0;
ran(i, 1, m) if (D[i][n + 1] < D[r][n + 1]) r = i;
if (D[r][n + 1] < -eps) {
    pivot(r, n);
    if (!simplex(2) || D[m + 1][n + 1] < -eps)
        return -inf;
    ran(i, 0, m) if (B[i] == -1) {
        int s = 0;
        ran(j, 1, n + 1) ltj(D[i]);
        pivot(i, s);
    }
}

```

```

    }
    bool ok = simplex(1);
    x = vd(n);
    ran(i, 0, m) if (B[i] < n) x[B[i]] = D[i][n + 1];
    return ok ? D[m][n + 1] : inf;
}
};  

Dinic  

struct MaxFlow {
    const static ll INF = 1e18;
    int source, sink;
    vector<int> start, now, lvl, adj, rcap, cap_loc, bfs;
    vector<int> cap, orig_cap;
    ll sink_pot = 0;
    vector<bool> visited;
    vector<ll> cost;
    priority_queue<pair<ll, intint>>, greater<pair<ll, int>> dist_que;
    void add_flow(int idx, ll flow, bool cont = true) {
        cap[idx] -= flow;
        if (cont) add_flow(rcap[idx], -flow, false);
    }
    MaxFlow(
        const vector<tuple<int, int, ll, ll, ll>> &edges) {
            for (auto &cur : edges) { //from, to, cap, rcap, cost
                start.resize(max(max(get<0>(cur), get<1>(cur)) + 2,
                    (int)start.size()));
                ++start[get<0>(cur) + 1];
                ++start[get<1>(cur) + 1];
            }
            ran(i, 1, (int)start.size()) start[i] += start[i-1];
            now = start;
            adj.resize(start.back());
            cap.resize(start.back());
            rcap.resize(start.back());
            cost.resize(start.back());
            for (auto &cur : edges) {
                int u, v;
                ll c, rc, c_cost;
                tie(u, v, c, rc, c_cost) = cur;
                assert(u != v);
                adj[now[u]] = v;
                adj[now[v]] = u;
                rcap[now[u]] = now[v];
                rcap[now[v]] = now[u];
                cap_loc.push_back(now[u]);
                cost[now[u]] = c_cost;
                cost[now[v]] = -c_cost;
                cap[now[u]++] = c;
                cap[now[v]++] = rc;
                orig_cap.push_back(c);
            }
        }
        bool dinic_bfs(int min_cap) {
            lvl.clear();
            lvl.resize(start.size());
            
```

```

bfs.clear();
bfs.resize(1, source);
now = start;
lvl[source] = 1;
ran(i, 0, (int)bfs.size()) {
    int u = bfs[i];
    while (now[u] < start[u + 1]) {
        int v = adj[now[u]];
        if (cost[now[u]] == 0 &&
            cap[now[u]] >= min_cap && lvl[v] == 0) {
            lvl[v] = lvl[u] + 1;
            if(v==sink) return true;
            bfs.push_back(v);
        }
        ++now[u];
    }
    return false;
}
11 dinic_dfs(int u, ll flow, int min_cap) {
    if (u == sink) return flow;
    if (lvl[u] == lvl[sink]) return 0;
    ll res = 0;
    while (now[u] < start[u + 1]) {
        int v = adj[now[u]];
        if (lvl[v] == lvl[u] + 1 && cost[now[u]] == 0 &&
            cap[now[u]] >= min_cap) {
            ll cur = dinic_dfs(v, min(flow, (ll)cap[now[u]]),
                min_cap);
            if (cur) {
                add_flow(now[u], cur);
                flow -= cur;
                res += cur;
                if(!flow) break;
            }
        }
        ++now[u];
    }
    return res;
}
bool recalc_dist(bool check_imp = false) {
    now = start;
    visited.clear();
    visited.resize(start.size());
    dist_que.emplace(0, source);
    bool imp = false;
    while (!dist_que.empty()) {
        int u;
        ll dist;
        tie(dist, u) = dist_que.top();
        dist_que.pop();
        if (!visited[u]) {
            visited[u] = true;
            if (check_imp && dist != 0) imp = true;
            if (u == sink) sink_pot += dist;
            while (now[u] < start[u + 1]) {
                int v = adj[now[u]];
                if (!visited[v] && cap[now[u]]) {
                    dist_que.emplace(dist + cost[now[u]], v);
                    cost[now[u]] += dist;
                    cost[rCap[now[u]+]] -= dist;
                }
            }
            if (check_imp) return imp;
            return visited[sink];
        }
        // return whether there is a negative cycle
        bool recalc_dist_bellman_ford() {
            int i = 0;
            for (; i < (int)start.size() - 1 &&
                recalc_dist(true); ++i) {}
            return i == (int)start.size() - 1;
        }
        pair<ll, ll> calc_flow(int _source, int _sink) {
            source = _source;
            sink = _sink;
            assert(max(source, sink) < start.size() - 1);
            ll tot_flow = 0;
            ll tot_cost = 0;
            if (recalc_dist_bellman_ford()) {
                assert(false);
            } else {
                while (recalc_dist()) {
                    ll flow = 0;
                    for(int min_cap = 1<<30; min_cap; min_cap >= 1) {
                        while (dinic_bfs(min_cap)) {
                            now = start;
                            ll cur;
                            while (cur = dinic_dfs(source, INF, min_cap))
                                flow += cur;
                        }
                        tot_flow += flow;
                        tot_cost += sink_pot * flow;
                    }
                }
                return {tot_flow, tot_cost};
            }
        }
        11 flow_on_edge(int idx) {
            assert(idx < cap.size());
            return orig_cap[idx] - cap[cap_loc[idx]];
        }
        const int nmax = 1055;
        int main() {
            int t;
            scanf("%d", &t);
            for (int i = 0; i < t; ++i) {
                vector<tuple<int, int, ll, ll, ll>> edges;
                int n;
                scanf("%d", &n);
                for (int j = 1; j <= n; ++j) {
                    edges.emplace_back(j, 2 * n + 1, 1, 0, 0);
                }
            }
            for (int j = 1; j <= n; ++j) {
                int card;
                scanf("%d", &card);
                edges.emplace_back(0, card, 1, 0, 0);
            }
            int ex_c;
            scanf("%d", &ex_c);
            for (int j = 0; j < ex_c; ++j) {
                int a, b;
                scanf("%d %d", &a, &b);
                if (b < a) swap(a, b);
                edges.emplace_back(a, b, nmax, 0, 1);
                edges.emplace_back(b, n + b, nmax, 0, 0);
                edges.emplace_back(n + b, a, nmax, 0, 1);
            }
            int v = 2 * n + 2;
            MaxFlow mf(edges);
            printf("%d\n", (int)mf.calc_flow(0, v - 1).second);
            //cout << mf.flow_on_edge(edge_index) << endl;
        }
    }
}

Min Cost Max Flow with Cycle Cancelling O(Cnm)
struct Network {
    struct Node;
    struct Edge {
        Node *u, *v;
        int f, c, cost;
        Node* from(Node* pos) {
            if (pos == u) return v;
            return u;
        }
        int getCap(Node* pos) {
            if (pos == u) return c - f;
            return f;
        }
        int addFlow(Node* pos, int toAdd) {
            if (pos == u) {
                f += toAdd;
                return toAdd * cost;
            } else {
                f -= toAdd;
                return -toAdd * cost;
            }
        }
    };
    struct Node {
        vector<Edge*> conn;
        int index;
    };
    deque<Node> nodes;
    deque<Edge> edges;
    Node* addNode() {
        nodes.push_back(Node());
        nodes.back().index = nodes.size() - 1;
        return &nodes.back();
    }
}

```

```

Edge* addEdge(
    Node* u, Node* v, int f, int c, int cost) {
    edges.push_back({u, v, f, c, cost});
    u->conn.push_back(&edges.back());
    v->conn.push_back(&edges.back());
    return &edges.back();
}

// Assumes all needed flow has already been added
int minCostMaxFlow() {
    int n = nodes.size();
    int result = 0;
    struct State {
        int p;
        Edge* used;
    };
    while (1) {
        vector<vector<State>> state(
            1, vector<State>(n, {0, 0}));
        for (int lev = 0; lev < n; lev++) {
            state.push_back(state[lev]);
            for (int i = 0; i < n; i++) {
                if (lev == 0 ||
                    state[lev][i].p < state[lev - 1][i].p) {
                    for (Edge* edge : nodes[i].conn) {
                        if (edge->getCap(&nodes[i]) > 0) {
                            int np =
                                state[lev][i].p + (edge->u == &nodes[i]
                                    ? edge->cost
                                    : -edge->cost);
                            int ni = edge->from(&nodes[i])->index;
                            if (np < state[lev + 1][ni].p) {
                                state[lev + 1][ni].p = np;
                                state[lev + 1][ni].used = edge;
                            }
                        }
                    }
                }
            }
        }
        // Now look at the last level
        bool valid = false;
        for (int i = 0; i < n; i++) {
            if (state[n - 1][i].p > state[n][i].p) {
                valid = true;
                vector<Edge*> path;
                int cap = 1000000000;
                Node* cur = &nodes[i];
                int clev = n;
                vector<bool> exprl(n, false);
                while (!exprl[cur->index]) {
                    exprl[cur->index] = true;
                    State cstate = state[clev][cur->index];
                    cur = cstate.used->from(cur);
                    path.push_back(cstate.used);
                }
                reverse(path.begin(), path.end());
            }
        }
    }
}

int main() {
    int n = 5;
    vector<Node> nodes(n);
    for (int i = 0; i < n; i++) {
        nodes[i].p = i;
        nodes[i].conn.push_back(new Edge(i, 0, 1, 0));
        nodes[i].conn.push_back(new Edge(i, 1, 1, 0));
        nodes[i].conn.push_back(new Edge(i, 2, 1, 0));
        nodes[i].conn.push_back(new Edge(i, 3, 1, 0));
        nodes[i].conn.push_back(new Edge(i, 4, 1, 0));
    }
    cout << minCostMaxFlow();
}

```

```

vector<Node *> to_visit = {root};
ran(i, 0, to_visit.size()) {
    Node *cur = to_visit[i];
    ran(j, 0, alpha_size) {
        if (cur->nxt[j]) to_visit.push_back(cur->nxt[j]);
    }
}
for (int i = to_visit.size() - 1; i > 0; --i)
    to_visit[i]->suffix->cnt += to_visit[i]->cnt;
} %7950
int main() {
    int n, len;
    scanf("%d %d", &len, &n);
    vector<char> a(len + 1);
    scanf("%s", a.data());
    a.pop_back();
    for (char &c : a) c -= 'a';
    vector<vector<char>> dict(n);
    ran(i, 0, n) {
        scanf("%d", &len);
        dict[i].resize(len + 1);
        scanf("%s", dict[i].data());
        dict[i].pop_back();
        for (char &c : dict[i]) c -= 'a';
    }
    Node *root = aho_corasick(dict);
    cnt_matches(root, a);
    add_cnt(root);
    ran(i, 0, n) {
        Node *cur = root;
        for (char c : dict[i]) cur = walk(cur, c);
        printf("%d\n", cur->cnt);
    }
}

Suffix automaton and tree  $O((n+q)\log(|\alpha|)) - 10M$  length/s

struct Node;
typedef Ptr<Node> P;
struct Node {
    int act = 0;
    Ptr<P> out;
    int len; // Length of longest suffix in equivalence
    P suf; // class.
    char size = 0;
    char cap = 0;
    Node(int _len) : len(_len) {};
    Node(int &_act, Ptr<P> &_out, int &_len, P &_suf,
        int _size, int _cap) : act(_act), len(_len),
        suf(_suf), size(_size), cap(_cap) {
        out = alloc<P>(cap);
        ran(i, 0, size)
            out[i] = _out[i];
    }
    int has_nxt(char c) {
        return act & (1 << (c - 'a'));
    }
    P nxt(char c) {
        4180
    }
}

return
    out[__builtin_popcount(act & ((1 << (c - 'a')) - 1))];
}
void set_nxt(char c, P nxt) {
    2672
    int idx = __builtin_popcount(act & ((1 << (c - 'a')) - 1));
    if (has_nxt(c)){
        out[idx] = nxt;
    } else{
        if (size == cap){
            cap *= 2;
            if (!size)
                cap = 2;
            Ptr<P> nout = alloc<P>(cap);
            ran(i, 0, idx)
                nout[i] = out[i];
            ran(i, idx, size)
                nout[i+1] = out[i];
            deallocate(out, size);
            out = nout;
        } else {
            for(int i=size; i>idx; --i)
                out[i] = out[i-1];
        }
        act |= (1 << (c - 'a'));
        out[idx] = nxt;
        ++size;
    }
}
P split(int new_len) {
    return suf = alloc<Node>(1, act, out, new_len,
        suf, size, cap);
}
// Extra functions for matching and counting
P lower(int depth) {
    // move to longest suf of current with a maximum
    // length of depth.
    if (suf->len >= depth) return suf->lower(depth);
    return (P)this;
}
P walk(char c, int depth, int &match_len) {
    // move to longest suffix of walked path that is a
    // substring
    match_len = min(match_len, len);
    // includes depth limit(needed for finding matches)
    if (has_nxt(c)) { // as suffixes are in classes,
        // match_len must be tracked externally
        ++match_len;
        return nxt(c)->lower(depth);
    }
    if (suf) return suf->walk(c, depth, match_len);
    return (P)this;
}
bool vis = false;
bool vis_t = false;
int paths_to_end = 0;
void set_as_end() { // All suffixes of current node are
    paths_to_end += 1; // marked as ending nodes.
}
if (suf) suf->set_as_end();
}
void calc_paths() {
/* Call ONCE from ROOT. For each node calculates
 * number of ways to reach an end node. paths_to_end
 * is occurrence count for any strings in current
 * suffix equivalence class. */
if (!vis) {
    vis = true;
    ran(i, 0, size){
        out[i]->calc_paths();
        paths_to_end += out[i]->paths_to_end;
    }
}
// Transform into suffix tree of reverse string
P tree_links[26];
int end_d_v = 1 << 30;
int end_d() {
    if (end_d_v == 1 << 30) {
        ran(i, 0, size){
            end_d_v = min(end_d_v, 1 + out[i]->end_d());
        }
        if (end_d_v == 1 << 30)
            end_d_v = 0;
    }
    return end_d_v;
}
void build_suffix_tree(
    string &s) // Call ONCE from ROOT.
if (!vis_t) {
    vis_t = true;
    if (suf)
        suf->tree_links[s[(int)s.size() - end_d() -
            suf->len - 1] - 'a'] = (P)this;
    ran(i, 0, size){
        out[i]->build_suffix_tree(s);
    }
}
}
%7187%1877%5307
struct SufAuto {
    P last;
    P root;
    void extend(char new_c) {
        P nlast = alloc<Node>(1, last->len + 1);
        P swn = last;
        while (swn && !swn->has_nxt(new_c)) {
            swn->set_nxt(new_c, nlast);
            swn = swn->suf;
        }
        if (!swn) {
            nlast->suf = root;
        } else {
            P max_sbstr = swn->nxt(new_c);
            if (swn->len + 1 == max_sbstr->len) {
                nlast->suf = max_sbstr;
            }
        }
    }
}
0905
8388
9735
4227
5334 6170
6675
2630
2958 1581
1138

```

<pre> } else { // remove for minimal DFA that matches // suffixes and crap P eq_sbstr = max_sbstr->split(swn->len + 1); nlast->suf = eq_sbstr; P x = swn; // x = with_edge_to_eq_sbstr while (x != 0 && x->nxt(new_c) == max_sbstr) { x->set_nxt(new_c, eq_sbstr); x = x->suf; } last = nlast; } SufAuto(string &s) { last = root = alloc<Node>(1, 0); for (char c : s) extend(c); // To build suffix tree use reversed string root->build_suffix_tree(s); } </pre> <p style="text-align: right;">%5553%5020</p> <pre> Palindromic tree O(n) struct palindromic_tree { int len[MAXN], link[MAXN], cnt[MAXN]; char s[MAXN]; vector<pair<char, int>> to[MAXN]; int n, last, sz; void clear() { fill(to, to + MAXN, vector<pair<char, int>>()); memset(len, 0, sizeof(len)); memset(link, 0, sizeof(link)); memset(cnt, 0, sizeof(cnt)); memset(s, 0, sizeof(s)); n = last = 0; link[0] = 1; len[1] = -1; s[n++] = 27; sz = 2; } palindromic_tree() { clear(); } int get_link(int v) { while (s[n - len[v] - 2] != s[n - 1]) v = link[v]; return v; } int tr(int v, int c) { for (auto it : to[v]) if (it.first == c) return it.second; return 0; } int add_letter(int c) { s[n++] = c; int cur = get_link(last); if (!tr(cur, c)) { len[sz] = len[cur] + 2; link[sz] = tr(get_link(link[cur]), c); to[cur].push_back({c, sz++}); } last = tr(cur, c); } } </pre> <p style="text-align: right;">5222 5928 4761</p>	<pre> return cnt[last] = cnt[link[last]] + 1; } } DMST O(E log V) struct EdgeDesc { int from, to, w; } struct DMST { struct Node; struct Edge { Node *from; Node *tar; int w; bool inc; }; struct Circle { bool vis = false; vector<Edge *> cont; void clean(int idx); }; const static greater<pair<ll, Edge *>> comp; static vector<Circle> to_proc; static bool no_dmst; static Node *root; // Can use inline static since C++17 struct Node { Node *par = NULL; vector<pair<int, int>> out_cands; // Circ, edge idx vector<pair<ll, Edge *>> con; bool in_use = false; ll w = 0; // extra to add to edges in con Node *anc() { if (!par) return this; while (par->par) par = par->par; return par; } void clean() { if (!no_dmst) { in_use = false; for (auto &cur : out_cands) to_proc[cur.first].clean(cur.second); } } Node *con_to_root() { if (anc() == root) return root; in_use = true; Node *super = this; // Will become root or the first Node encountered // in a loop. while (super == this) { while (!con.empty() && con.front().second->tar->anc() == anc()) { pop_heap(con.begin(), con.end(), comp); con.pop_back(); } if (con.empty()) { no_dmst = true; return root; } } } }; } </pre> <p style="text-align: right;">3897 2157 1880</p>	<pre> } pop_heap(con.begin(), con.end(), comp); auto nxt = con.back(); con.pop_back(); w = -nxt.first; if (nxt.second->tar->in_use) { super = nxt.second->tar->anc(); to_proc.resize(to_proc.size() + 1); } else { super = nxt.second->tar->con_to_root(); } if (super != root) { to_proc.back().cont.push_back(nxt.second); out_cands.emplace_back(to_proc.size() - 1, to_proc.back().cont.size() - 1); } else { // Clean circles nxt.second->inc = true; nxt.second->from->clean(); } } if (super != root) { // we are some loops non first Node. if (con.size() > super->con.size()) { swap(con, super->con); // Largest con in loop should not be copied. swap(w, super->w); } for (auto cur : con) { super->con.emplace_back(cur.first - super->w + w, cur.second); push_heap(super->con.begin(), super->con.end(), comp); } } par = super; // root or anc() of first Node // encountered in a loop return super; } Node *croot; vector<Node> graph; vector<Edge> edges; DMST(int n, vector<EdgeDesc> &desc, int r) { // Self loops and multiple edges are okay. graph.resize(n); croot = &graph[r]; for (auto &cur : desc) // Edges are reversed internally edges.push_back(Edge{&graph[cur.to], &graph[cur.from], cur.w}); for (int i = 0; i < desc.size(); ++i) graph[desc[i].to].con.emplace_back(desc[i].w, &edges[i]); for (int i = 0; i < n; ++i) make_heap(graph[i].con.begin(), graph[i].con.end(), comp); } </pre> <p style="text-align: right;">9883 6612 4059 7094 0198 2509 0309 8100 4229 8811</p>
--	---	--

```

bool find() {
    root = croot;
    no_dmst = false;
    for (auto &cur : graph) {
        cur.con_to_root();
        to_proc.clear();
        if (no_dmst) return false;
    }
    return true;
}
ll weight() {
    ll res = 0;
    for (auto &cur : edges) {
        if (cur.inc) res += cur.w;
    }
    return res;
}
void DMST::Circle::clean(int idx) {
    if (!vis) {
        vis = true;
        for (int i = 0; i < cont.size(); ++i) {
            if (i != idx) {
                cont[i]->inc = true;
                cont[i]->from->clean();
            }
        }
    }
}
const greater<pair<ll, DMST::Edge *>> DMST::comp;
vector<DMST::Circle> DMST::to_proc;
bool DMST::no_dmst;
DMST::Node *DMST::root;
    Dominator tree O(NlogN)
struct Tree {
    /* insert structure here */
    void set_root(int u) {
        cout << "root is " << u << endl;
    }
    void add_edge(int u, int v) {
        cout << u << "-" << v << endl;
    }
};
struct Graph {
    vector<vector<int>> in_edges, out_edges;
    vector<int> ord, dfs_idx, parent;
    vector<int> sdom, idom;
    vector<vector<int>> rsdom; /* inverse of sdom */
    /* slightly modified version of dsu-s root[] */
    vector<int> dsu;
    vector<int> label;
    void dfs(int cur, int par, vector<int> &vis) {
        ord.push_back(cur);
        parent[cur] = par;
        dfs_idx[cur] = (int)ord.size() - 1;
        vis[cur] = 1;
        for (int nxt : out_edges[cur]) {
            2704 9919
            2594
            2342
            2166
            2000 1468
            2953
            3580
            8714
        }
    }
}

```

```

    in_edges[nxt].push_back(cur);
    if (!vis[nxt])
        dfs(nxt, cur, vis);
}
void add_edge(int u, int v) {
    out_edges[u].push_back(v);
}
Graph(int n) {
    in_edges.resize(n, vector<int>(0));
    out_edges.resize(n, vector<int>(0));
    rsdom.resize(n, vector<int>(0));
    dfs_idx.resize(n, -1);
    parent.resize(n, -1);
    ran(i, 0, n) {
        sdom.push_back(i);
        idom.push_back(i);
        dsu.push_back(i);
        label.push_back(i);
    }
}
int find(int u, int x = 0) {
    if (u == dsu[u]) {
        if (x) {
            return -1;
        } else {
            return u;
        }
    }
    int v = find(dsu[u], x + 1);
    if (v < 0) {
        return u;
    }
    if (dfs_idx[sdom[label[dsu[u]]]] <
        dfs_idx[sdom[label[u]]]) {
        label[u] = label[dsu[u]];
    }
    dsu[u] = v;
    return x ? v : label[u];
}
void merge(int u, int v) { dsu[v] = u; }
Tree dom_tree(int src) {
    vector<int> vis(idom.size(), 0);
    dfs(src, -1, vis);
    for (int i = (int)ord.size() - 1; i >= 0; --i) {
        int u = ord[i];
        for (int v : in_edges[u]) {
            int w = find(v);
            if (dfs_idx[sdom[u]] > dfs_idx[sdom[w]]) {
                sdom[u] = sdom[w];
            }
        }
        if (i > 0) {
            rsdom[sdom[u]].push_back(u);
        }
        for (int w : rsdom[u]) {
            int v = find(w);
            9381 9803
            3371 2760
            9724 5825
            5015 3306
            3975
            7954
            4543
            6393
            7801
            4694
            8791
            9412
            8032
            6574
            7922
            5074
            4393
            5034
            5205
            2528
            6069
            9799
            0088
            5037
            4393
            1297 5319
            5838
            9341
        }
    }
}

```

```

if (sdom[v] == sdom[w]) {
    idom[w] = sdom[w];
} else {
    idom[w] = v;
}
if (i > 0) {
    merge(parent[u], u);
}
Tree ans; /* if your constructor needs # of vertices,
           * use (int)idom.size() + 5 for example */
ran(i, 1, (int)ord.size()) {
    int u = ord[i];
    if (idom[u] != sdom[u]) {
        idom[u] = idom[idom[u]];
    }
    ans.add_edge(idom[u], u);
}
ans.set_root(src);
return ans;
}
    Bridges O(n)
%7388%1935%7257
struct vert;
struct edge {
    bool exists = true;
    vert *dest;
    edge *rev;
    edge(vert *_dest) : dest(_dest) { rev = NULL; }
    vert &operator*() { return *dest; }
    vert *operator->() { return dest; }
    bool is_bridge();
};
struct vert {
    deque<edge> con;
    int val = 0;
    int seen;
    int dfs(int upd, edge *ban) { // handles multiple edges
        if (!val) {
            val = upd;
            seen = val;
            for (edge &nxt : con) {
                if (nxt.exists && (&nxt) != ban)
                    seen = min(seen, nxt->dfs(upd + 1, nxt.rev));
            }
        }
        return seen;
    }
    void remove_adj_bridges() {
        for (edge &nxt : con) {
            if (nxt.is_bridge()) nxt.exists = false;
        }
    }
    int cnt_adj_bridges() {
        int res = 0;
        for (edge &nxt : con) res += nxt.is_bridge();
    }
}

```

```

    return res;
}
bool edge::is_bridge() {
    return exists && (dest->seen > rev->dest->val ||
                      dest->val < rev->dest->seen);
} %3548%8614%4558
vert graph[nmax];
int main() { // Mechanics Practice BRIDGES
    int n, m;
    cin >> n >> m;
    for (int i = 0; i < m; ++i) {
        int u, v;
        scanf("%d %d", &u, &v);
        graph[u].con.emplace_back(graph + v);
        graph[v].con.emplace_back(graph + u);
        graph[u].con.back().rev = &graph[v].con.back();
        graph[v].con.back().rev = &graph[u].con.back();
    }
    graph[1].dfs(1, NULL);
    int res = 0;
    for (int i = 1; i <= n; ++i)
        res += graph[i].cnt_adj_bridges();
    cout << res / 2 << endl;
}

2-Sat O(n) and SCC O(n)
struct Graph {
    int n;
    vector<vector<int> > con;
    Graph(int nsize) {
        n = nsize;
        con.resize(n);
    }
    void add_edge(int u, int v) { con[u].push_back(v); }
    void top_dfs(int pos, vector<int> &result,
                 vector<bool> &explr, vector<vector<int> > &revcon) {
        if (explr[pos]) return;
        explr[pos] = true;
        for (auto next : revcon[pos])
            top_dfs(next, result, explr, revcon);
        result.push_back(pos);
    }
    vector<int> topsort() {
        vector<vector<int> > revcon(n);
        ran(i, 0, n) {
            for (auto v : con[u]) revcon[v].push_back(u);
        }
        vector<int> result;
        vector<bool> explr(n, false);
        ran(i, 0, n) top_dfs(i, result, explr, revcon);
        reverse(result.begin(), result.end());
        return result;
    }
    void dfs(
        int pos, vector<int> &result, vector<bool> &explr) {
        if (explr[pos]) return;
        explr[pos] = true;
        for (auto next : con[pos]) dfs(next, result, explr);
        result.push_back(pos);
    }
}

0800 for (auto next : con[pos]) dfs(next, result, explr);
0239 result.push_back(pos);
}
vector<vector<int> > scc() {
9591     vector<int> order = topsort();
8807     reverse(order.begin(), order.end());
8640     vector<bool> explr(n, false);
9591     vector<vector<int> > res;
8807     for (auto it = order.rbegin(); it != order.rend();
9591         ++it) {
8807         vector<int> comp;
8807         top_dfs(*it, comp, explr, con);
8807         sort(comp.begin(), comp.end());
8807         res.push_back(comp);
9591     }
8807     sort(res.begin(), res.end());
9591     return res;
}
0503%6965%4511
int main() {
    int n, m;
    cin >> n >> m;
    Graph g(2 * m);
    ran(i, 0, n) {
        int a, sa, b, sb;
        cin >> a >> sa >> b >> sb;
        a--, b--;
        g.add_edge(2 * a + 1 - sa, 2 * b + sb);
        g.add_edge(2 * b + 1 - sb, 2 * a + sa);
    }
    vector<int> state(2 * m, 0);
    {
        vector<int> order = g.topsort();
        vector<bool> explr(2 * m, false);
        for (auto u : order) {
            vector<int> traversed;
            g.dfs(u, traversed, explr);
            if (traversed.size() > 0 &&
                !state[traversed[0] ^ 1]) {
                for (auto c : traversed) state[c] = 1;
            }
        }
    }
    ran(i, 0, m) {
        if (state[2 * i] == state[2 * i + 1]) {
            cout << "IMPOSSIBLE\n";
            return 0;
        }
    }
    ran(i, 0, m) cout << state[2 * i + 1] << '\n';
    return 0;
}

Templated multi dimensional BIT O(log(n)^d) per query
2438 // Fully overloaded any dimensional BIT, use any type for
// coordinates, elements, return_value. Includes
// coordinate compression.
template <class E_T, class C_T, C_T n_inf, class R_T>
6191 struct BIT {
6191     vector<C_T> pos;
6191     vector<E_T> elems;
6191     bool act = false;
6191     BIT() { pos.push_back(n_inf); }
8228     void init() {
8228         if (act) {
8228             for (E_T &c_elem : elems) c_elem.init();
8228         } else {
8228             act = true;
8228             sort(pos.begin(), pos.end());
6080             pos.resize(
6080                 unique(pos.begin(), pos.end()) - pos.begin());
6080             elems.resize(pos.size());
6080         }
6080     }
6080     template <typename... loc_form>
6080     void update(C_T cx, loc_form... args) {
6080         if (act) {
6080             int x = lower_bound(pos.begin(), pos.end(), cx) -
6080                 pos.begin();
6080             for (; x < (int)pos.size(); x += x & -x)
6080                 elems[x].update(args...);
5773         } else {
5773             pos.push_back(cx);
5773         }
5773     }
5773     template <typename... loc_form>
5773     R_T query(
5773         C_T cx, loc_form... args) { // sum in (-inf, cx)
5773         R_T res = 0;
5773         int x = lower_bound(pos.begin(), pos.end(), cx) -
5773             pos.begin() - 1;
5773         for (; x > 0; x -= x & -x)
5773             res += elems[x].query(args...);
5773         return res;
5773     }
5773 }
6893 template <typename I_T>
6893 struct wrapped {
6893     I_T a = 0;
6893     void update(I_T b) { a += b; }
6893     I_T query() { return a; }
6893     // Should never be called, needed for compilation
6893     void init() { DEBUG('i') }
6893     void update() { DEBUG('u') }
6893 }
6893 int main() {
6893     // return type should be same as type inside wrapped
6893     BIT<BIT<wrapped<ll>, int, INT_MIN, ll>, int, INT_MIN,
6893         ll> fenwick;
6893     int dim = 2;
6893     vector<tuple<int, int, ll> > to_insert;
6893     to_insert.emplace_back(1, 1, 1);
6893     // set up all pos that are to be used for update

```

```

for (int i = 0; i < dim; ++i) {
    for (auto &cur : to_insert)
        fenwick.update(get<0>(cur), get<1>(cur));
    // May include value which won't be used
    fenwick.init();
}
// actual use
for (auto &cur : to_insert)
    fenwick.update(
        get<0>(cur), get<1>(cur), get<2>(cur));
cout << fenwick.query(2, 2) << '\n';
}

Treap O(log (n)) per query
mt19937 randgen;
struct Treap {
    struct Node {
        int key;
        int value;
        unsigned int priority;
        ll total;
        Node* lch;
        Node* rch;
        Node(int new_key, int new_value) {
            key = new_key;
            value = new_value;
            priority = randgen();
            total = new_value;
            lch = 0;
            rch = 0;
        }
        void update() {
            total = value;
            if (lch) total += lch->total;
            if (rch) total += rch->total;
        }
    };
    deque<Node> nodes;
    Node* root = 0;
    pair<Node*, Node*> split(int key, Node* cur) {
        if (cur == 0) return {0, 0};
        pair<Node*, Node*> result;
        if (key <= cur->key) {
            auto ret = split(key, cur->lch);
            cur->lch = ret.second;
            result = {ret.first, cur};
        } else {
            auto ret = split(key, cur->rch);
            cur->rch = ret.first;
            result = {cur, ret.second};
        }
        cur->update();
        return result;
    }
    Node* merge(Node* left, Node* right) {
        if (left == 0) return right;
        if (right == 0) return left;
        Node* top:

```

```

if (left->priority < right->priority) {
    left->rch = merge(left->rch, right);
    top = left;
} else {
    right->lch = merge(left, right->lch);
    top = right;
}
top->update();
return top;
}
void insert(int key, int value) {
    nodes.push_back(Node(key, value));
    Node* cur = &nodes.back();
    pair<Node*, Node*> ret = split(key, root);
    cur = merge(ret.first, cur);
    cur = merge(cur, ret.second);
    root = cur;
}
void erase(int key) {
    Node *left, *mid, *right;
    tie(left, mid) = split(key, root);
    tie(mid, right) = split(key + 1, mid);
    root = merge(left, right);
}
int sum_upto(int key, Node* cur) {
    if (cur == 0) return 0;
    if (key <= cur->key) {
        return sum_upto(key, cur->lch);
    } else {
        int result = cur->value + sum_upto(key, cur->rch);
        if (cur->lch) result += cur->lch->total;
        return result;
    }
}
int get(int l, int r) {
    return sum_upto(r + 1, root) - sum_upto(l, root);
}
int main() {
ios_base::sync_with_stdio(false);
cin.tie(0);
int m;
Treap treap;
cin >> m;
for (int i = 0; i < m; i++) {
    int type;
    cin >> type;
    if (type == 1) {
        int x, y;
        cin >> x >> y;
        treap.insert(x, y);
    } else if (type == 2) {
        int x;
        cin >> x;
        treap.erase(x);
    } else {
        int l, r;
        cin >> l >> r;
        cout << sum_upto(r + 1, root) - sum_upto(l, root) << endl;
    }
}
}

```

```

0054     cin >> l >> r;
0055     cout << treap.get(l, r) << endl;
0056 }
0057 return 0;
0058 }

0634 Generic persistent compressed lazy segment tree
0635 struct Seg {
0636     ll sum = 0;
0637     void recalc(const Seg &lhs_seg, int lhs_len,
0638         const Seg &rhs_seg, int rhs_len) {
0639         sum = lhs_seg.sum + rhs_seg.sum;
0640     }
0641 } _attribute_((packed));
0642 struct Lazy {
0643     ll add;
0644     ll assign_val; // LLONG_MIN if no assign;
0645     void init() {
0646         add = 0;
0647         assign_val = LLONG_MIN;
0648     }
0649     Lazy() { init(); }
0650     void split(Lazy &lhs_lazy, Lazy &rhs_lazy, int len) {
0651         lhs_lazy = *this;
0652         rhs_lazy = *this;
0653         init();
0654     }
0655     void merge(Lazy &oth, int len) {
0656         if (oth.assign_val != LLONG_MIN) {
0657             add = 0;
0658             assign_val = oth.assign_val;
0659         }
0660         add += oth.add;
0661     }
0662     void apply_to_seg(Seg &cur, int len) const {
0663         if (assign_val != LLONG_MIN) {
0664             cur.sum = len * assign_val;
0665         }
0666         cur.sum += len * add;
0667     }
0668 } _attribute_((packed));
0669 struct Node { // Following code should not need to be
0670     // modified
0671     int ver;
0672     bool is_lazy = false;
0673     Seg seg;
0674     Lazy lazy;
0675     Node *lc = NULL, *rc = NULL;
0676     void init() {
0677         if (!lc) {
0678             lc = new Node{ver};
0679             rc = new Node{ver};
0680         }
0681     }
0682     Node *upd(
0683         int L, int R, int l, int r, Lazy &val, int tar_ver) {
0684         if (ver != tar_ver) {
0685             if (L <= l && R >= r) {
0686                 val = Lazy{assign_val + add * (r - l)};
0687             } else if (l <= L && R <= r) {
0688                 val = lazy;
0689             } else if (L < l && R > r) {
0690                 val = Seg{sum: 0, add: 0};
0691             } else {
0692                 val = Seg{sum: 0, add: 0};
0693                 val.lc = upd(lc, L, R, l, r, val, tar_ver);
0694                 val.rc = upd(rc, l, R, r, val, tar_ver);
0695             }
0696         }
0697     }
0698 }
```

```

Node *rep = new Node(*this);
rep->ver = tar_ver;
return rep->upd(L, R, l, r, val, tar_ver);
}
if (L >= l && R <= r) {
    val.apply_to_seg(seg, R - L);
    lazy.merge(val, R - L);
    is_lazy = true;
} else {
    init();
    int M = (L + R) / 2;
    if (is_lazy) {
        Lazy l_val, r_val;
        lazy.split(l_val, r_val, R - L);
        lc = lc->upd(L, M, l, M, l_val, ver);
        rc = rc->upd(M, R, M, R, r_val, ver);
        is_lazy = false;
    }
    Lazy l_val, r_val;
    val.split(l_val, r_val, R - L);
    if (l < M) lc = lc->upd(L, M, l, r, l_val, ver);
    if (M < r) rc = rc->upd(M, R, l, r, r_val, ver);
    seg.recalc(lc->seg, M - L, rc->seg, R - M);
}
return this;
}
void get(int L, int R, int l, int r, Seg *&lft_res,
Seg *&tmp, bool last_ver) {
if (L >= l && R <= r) {
    tmp->recalc(*lft_res, L - l, seg, R - L);
    swap(lft_res, tmp);
} else {
    init();
    int M = (L + R) / 2;
    if (is_lazy) {
        Lazy l_val, r_val;
        lazy.split(l_val, r_val, R - L);
        lc = lc->upd(L, M, l, M, l_val, ver + last_ver);
        lc->ver = ver;
        rc = rc->upd(M, R, M, R, r_val, ver + last_ver);
        rc->ver = ver;
        is_lazy = false;
    }
    if (l < M)
        lc->get(L, M, l, r, lft_res, tmp, last_ver);
    if (M < r)
        rc->get(M, R, l, r, lft_res, tmp, last_ver);
}
}
__attribute__((packed));
struct SegTree { // indexes start from 0, ranges are
                 // [beg, end)
vector<Node *> roots; // versions start from 0
int len;
SegTree(int _len) : len(_len) {
    roots.push_back(new Node{0});
}

```

```

int upd(
    int l, int r, Lazy &val, bool new_ver = false) {
    Node *cur_root = roots.back()->upd(
        0, len, l, r, val, roots.size() - !new_ver);
    if (cur_root != roots.back())
        roots.push_back(cur_root);
    return roots.size() - 1;
}
Seg get(int l, int r, int ver = -1) {
    if (ver == -1) ver = roots.size() - 1;
    Seg seg1, seg2;
    Seg *pres = &seg1, *ptmp = &seg2;
    roots[ver]->get(
        0, len, l, r, pres, ptmp, roots.size() - 1);
    return *pres;
}
int main() {
    int n, m; // solves Mechanics Practice LAZY
    cin >> n >> m;
    SegTree seg_tree(1 << 17);
    for (int i = 0; i < n; ++i) {
        Lazy tmp;
        scanf("%lld", &tmp.assign_val);
        seg_tree.upd(i, i + 1, tmp);
    }
    for (int i = 0; i < m; ++i) {
        int o;
        int l, r;
        scanf("%d %d %d", &o, &l, &r);
        -1;
        if (o == 1) {
            Lazy tmp;
            scanf("%lld", &tmp.add);
            seg_tree.upd(l, r, tmp);
        } else if (o == 2) {
            Lazy tmp;
            scanf("%lld", &tmp.assign_val);
            seg_tree.upd(l, r, tmp);
        } else {
            Seg res = seg_tree.get(l, r);
            printf("%lld\n", res.sum);
        }
    }
}
Templated HLD O(M(n) log n) per query
class dummy {
public:
    dummy() {}
    dummy(int, int) {}
    void set(int, int) {}
    int query(int left, int right) {
        cout << this << ' ' << left << ' ' << right << endl;
    }
}
/* T should be the type of the data stored in each
 * vertex; DS should be the underlying data structure

```

```

* that is used to perform the group operation. It should
* have the following methods:
* * DS () - empty constructor
* * DS (int size, T initial) - constructs the structure
* with the given size, initially filled with initial.
* * void set (int index, T value) - set the value at
* index 'index' to 'value'
* * T query (int left, int right) - return the "sum" of
* elements between left and right, inclusive.
*/
template <typename T, class DS>
class HLD {
    int vertexc;
    vector<int> *adj;
    vector<int> subtree_size;
    DS structure;
    DS aux;
    void build_sizes(int vertex, int parent) {
        subtree_size[vertex] = 1;
        for (int child : adj[vertex]) {
            if (child != parent) {
                build_sizes(child, vertex);
                subtree_size[vertex] += subtree_size[child];
            }
        }
    }
    int cur;
    vector<int> ord;
    vector<int> chain_root;
    vector<int> par;
    void build_hld(
        int vertex, int parent, int chain_source) {
        cur++;
        ord[vertex] = cur;
        chain_root[vertex] = chain_source;
        par[vertex] = parent;
        if (adj[vertex].size() > 1 ||
            (vertex == 1 && adj[vertex].size() == 1)) {
            int big_child, big_size = -1;
            for (int child : adj[vertex]) {
                if ((child != parent) &&
                    (subtree_size[child] > big_size)) {
                    big_child = child;
                    big_size = subtree_size[child];
                }
            }
            build_hld(big_child, vertex, chain_source);
            for (int child : adj[vertex]) {
                if ((child != parent) && (child != big_child))
                    build_hld(child, vertex, child);
            }
        }
    }
    public:
        HLD(int _vertexc) {
            vertexc = _vertexc;
            adj = new vector<int>[vertexc + 5];
        }
}

```

```

} void add_edge(int u, int v) {
    adj[u].push_back(v);
    adj[v].push_back(u);
}
void build(T initial) { 456
    subtree_size = vector<int>(vertexc + 5);
    ord = vector<int>(vertexc + 5);
    chain_root = vector<int>(vertexc + 5);
    par = vector<int>(vertexc + 5);
    cur = 0;
    build_sizes(1, -1);
    build_hld(1, -1, 1);
    structure = DS(vertexc + 5, initial); 854.
    aux = DS(50, initial);
}
void set(int vertex, int value) { 918
    structure.set(ord[vertex], value);
}
T query_path(int u, 817
    int v) { /* returns the "sum" of the path u->v */
    int cur_id = 0;
    while (chain_root[u] != chain_root[v]) {
        if (ord[u] > ord[v]) { 632
            cur_id++;
            aux.set(cur_id,
                structure.query(ord[chain_root[u]], ord[u]));
            u = par[chain_root[u]]; 453
        } else {
            cur_id++;
            aux.set(cur_id,
                structure.query(ord[chain_root[v]], ord[v]));
            v = par[chain_root[v]]; 384
        }
    }
    cur_id++;
    aux.set(cur_id, structure.query(min(ord[u], ord[v]),
                                    max(ord[u], ord[v])));
    return aux.query(1, cur_id); 715
}
void print() { 715
    for (int i = 1; i <= vertexc; i++)
        cout << i << ' ' << ord[i] << ' ' << chain_root[i]
            << ' ' << par[i] << endl;
}
int main() {
    int vertexc;
    cin >> vertexc;
    HLD<int, dummy> hld(vertexc);
    for (int i = 0; i < vertexc - 1; i++) {
        int u, v;
        cin >> u >> v;
        hld.add_edge(u, v);
    }
    hld.build();
    hld.print();
}

```

```

int queryc;
cin >> queryc;
for (int i = 0; i < queryc; i++) {
    int u, v;
    cin >> u >> v;
    hld.query_path(u, v);
    cout << endl;
}
} 666
} 542
Splay Tree + Link-Cut O(NlogN)
struct Tree *treev;
struct Tree {
    struct T {
        int i;
        constexpr T() : i(-1) {}
        T(int _i) : i(_i) {}
        operator int() const { return i; }
        explicit operator bool() const { return i != -1; }
        Tree *operator->() { return treev + i; }
    };
    T c[2], p;
    /* insert monoid here */
    T link;
    Tree() {
        /* init monoid here */
        link = -1;
    }
} 538
using T = Tree::T;
constexpr T NIL;
void update(T t) { /* recalculate the monoid here */ } 3006
void propagate(T t) { 4076
    assert(t);
    for (T c : t->c)
        if (c) c->link = t->link;
    /* lazily propagate updates here */
}
void lazy_reverse(T t) { /* lazily reverse t here */ } 8098
T splay(T n) { 6086
    for (;;) {
        propagate(n);
        T p = n->p;
        if (p == NIL) break;
        propagate(p);
        if (p->c[1] == n) 8109
            assert(p->c[px] == n);
        T g = p->p;
        if (g == NIL) { /* zig */ 8587
            p->c[px] = n->c[px ^ 1];
            p->c[px ^ 1]->p = p;
            n->c[px ^ 1] = p;
            n->c[px ^ 1]->p = n;
            n->p = NIL;
            update(p);
            update(n);
        } 6563 0914
    } 8717 2795
} 50

```

```

        break;
    }
propagate(g);
11 gx = g->c[1] == p;
assert(g->c[gx] == p);
T gg = g->p;
11 ggx = gg && gg->c[1] == g;
if (gg) assert(gg->c[ggx] == g);
if (gx == px) { /* zig zig */
    g->c[gx] = p->c[gx ^ 1];
    g->c[gx]->p = g;
    p->c[gx ^ 1] = g;
    p->c[gx ^ 1]->p = p;
    p->c[gx] = n->c[gx ^ 1];
    p->c[gx]->p = p;
    n->c[gx ^ 1] = p;
    n->c[gx ^ 1]->p = n;
} else { /* zig zag */
    g->c[gx] = n->c[gx ^ 1];
    g->c[gx]->p = g;
    n->c[gx ^ 1] = g;
    n->c[gx ^ 1]->p = n;
    p->c[gx ^ 1] = n->c[gx];
    p->c[gx ^ 1]->p = p;
    n->c[gx] = p;
    n->c[gx]->p = n;
}
}
if (gg) gg->c[ggx] = n;
n->p = gg;
update(g);
update(p);
update(n);
if (gg) update(gg);
}
return n;

extreme(T t, int x) {
while (t->c[x]) t = t->c[x];
return t;
}

set_child(T t, int x, T a) {
T o = t->c[x];
t->c[x] = a;
update(t);
o->p = NIL;
a->p = t;
return o;
}

***** Link-Cut Tree: *****
expose(T t) {
set_child(splay(t), 1, NIL);
T leader = splay(extreme(t, 0));
if (leader->link == NIL) return t;
set_child(splay(leader), 0, expose(leader->link));
return splay(t);
}

oid link(T t, T p) {

```

```
assert(t->link == NIL);
t->link = p;
}
T cut(T t) {
T p = t->link;
if (p) expose(p);

    t->link = NIL;
    return p;
}

void make_root(T t) {
    expose(t);
    lazy_reverse(extreme(splay(t), 0));
}

%7295%6269
```


