

University of Tartu ICPC Team Notebook (2017-2018) October 6, 2018

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- 21 FFT 5M length/sec

22 Rabin Miller prime check, Pollard rho factorization $\mathcal{O}(\sqrt{p})$

```
1      1 Setup
2      1 set smartindent cindent
3      1 set ts=4 sw=4 expandtab
4      1 syntax enable
5      1 set clipboard=unnamedplus
6      1 "colorscheme elflord
7      1 "setxkbmap -option caps:escape
8      1 "setxkbmap -option
9      1 "valgrind --vgdb-error=0 ./a <inp &
10     1 "gdb a
10     1 "target remote | vgdb
1
1      1 2 crc.sh
2      1 #!/bin/env bash
2      2 starts=$(($ sed '/^s*/d' $1 | grep -n "//\!start" | cut -f1 -d:))
3      2 finishes=$(($ sed '/^s*/d' $1 | grep -n "//\!finish" | cut -f1 -d:))
3      3 for ((i=0;i<${#starts[@]};i++)); do
4      4   for j in `seq 10 10 ${((finishes[$i]-starts[$i]+8))}`; do
5      5     sed '/^s*/d' $1 | head -$((finishes[$i]-starts[$i])) | tail
6      6     -$((finishes[$i]-starts[$i]-1)) | \
7      7       head -$j | tr -d '[:space:]' | cksum | cut -f1 -d ' ' | tail -c
7      8     4
8      8   done #whitespace don't matter
9      9   echo #there shouldn't be any comments in the checked range
10    10 done #check last number in each block
11
11     1 3 gcc ordered set
12    1 #include <bits/stdc++.h>
13    1 typedef long long ll;
13    2 using namespace std;
14    2 #include <ext/pb_ds/assoc_container.hpp>
14    3 #include <ext/pb_ds/tree_policy.hpp>
14    4 using namespace __gnu_pbds;
14    5 template <typename T>
14    6 using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
14    7   tree_order_statistics_node_update>;
16    8 int main(){
16    9   ordered_set<int> cur;                                     #221
17   10   cur.insert(1);
17   11   cur.insert(3);
18   12   cout << cur.order_of_key(2) << endl; // the number of elements in the
18   13   set less than 2
19   14   cout << *cur.find_by_order(0) << endl; // the 0-th smallest number in
19   15   the set(0-based)
20   16   cout << *cur.find_by_order(1) << endl; // the 1-th smallest number in
20   17   the set(0-based)                                         %574
21   18 }
```

4 Numerical integration with Simpson's rule

```

1 //computing power = how many times function integrate gets called
2 template<typename T>
3 double simps(T f, double a, double b) {
4     return (f(a) + 4*f((a+b)/2) + f(b))*(b-a)/6;
5 }
6 template<typename T>
7 double integrate(T f, double a, double b, double computing_power){
8     double m = (a+b)/2;
9     double l = simps(f,a,m), r = simps(f,m,b), tot=simps(f,a,b);
10    if (computing_power < 1) return tot;
11    return integrate(f, a, m, computing_power/2) + integrate(f, m, b,
12        computing_power/2);                                #430
12 }                                                 %360

```

5 Triangle centers

```

1 const double min_delta = 1e-13;
2 const double coord_max = 1e6;
3 typedef complex < double > point;
4 point A, B, C; // vertexes of the triangle
5 bool collinear(){
6     double min_diff = min(abs(A - B), min(abs(A - C), abs(B - C)));
7     if(min_diff < coord_max * min_delta)
8         return true;
9     point sp = (B - A) / (C - A);
10    double ang = M_PI/2-abs(abs(arg(sp))-M_PI/2); //positive angle with
11        the real line                                #623
11    return ang < min_delta;
12 }
13 point circum_center(){
14     if(collinear())
15         return point(NAN,NAN);
16     //squared lengths of sides
17     double a2, b2, c2;
18     a2 = norm(B - C);
19     b2 = norm(A - C);
20     c2 = norm(A - B);
21     //barycentric coordinates of the circumcenter
22     double c_A, c_B, c_C;
23     c_A = a2 * (b2 + c2 - a2); //sin(2 * alpha) may be used as well
24     c_B = b2 * (a2 + c2 - b2);
25     c_C = c2 * (a2 + b2 - c2);                                #385
26     double sum = c_A + c_B + c_C;
27     c_A /= sum;
28     c_B /= sum;
29     c_C /= sum;
30     // cartesian coordinates of the circumcenter
31     return c_A * A + c_B * B + c_C * C;                         %742
32 }
33 point centroid(){ //center of mass
34     return (A + B + C) / 3.0;
35 }
36 point ortho_center(){ //euler line
37     point O = circum_center();

```

```

38     return 0 + 3.0 * (centroid() - 0);
39 }
40 point nine_point_circle_center(){ //euler line
41     point O = circum_center();
42     return O + 1.5 * (centroid() - O);
43 };
44 point in_center(){
45     if(collinear())
46         return point(NAN,NAN);
47     double a, b, c; //side lengths
48     a = abs(B - C);
49     b = abs(A - C);
50     c = abs(A - B);
51     //trilinear coordinates are (1,1,1)
52     //barycentric coordinates
53     double c_A = a, c_B = b, c_C = c;
54     double sum = c_A + c_B + c_C;
55     c_A /= sum;                                         #157
56     c_B /= sum;
57     c_C /= sum;
58     // cartesian coordinates of the incenter
59     return c_A * A + c_B * B + c_C * C;
60 }                                                 %980

```

6 2D line segment

```

1 const long double PI = acos(-1.0L);
2 struct Vec {
3     long double x, y;
4     Vec& operator-=(Vec r) {
5         x -= r.x, y -= r.y;
6         return *this;
7     }
8     Vec operator-(Vec r) {return Vec(*this) -= r;}
9     Vec& operator+=(Vec r) {
10        x += r.x, y += r.y;                                #054
11        return *this;
12    }
13    Vec operator+(Vec r) {return Vec(*this) += r;}
14    Vec operator-() {return {-x, -y};}
15    Vec& operator*=(long double r) {
16        x *= r, y *= r;
17        return *this;
18    }
19    Vec operator*(long double r) {return Vec(*this) *= r;}
20    Vec& operator/=(long double r) {
21        x /= r, y /= r;                                         #673
22        return *this;
23    }
24    Vec operator/(long double r) {return Vec(*this) /= r;}
25    long double operator*(Vec r) {
26        return x * r.x + y * r.y;
27    }
28 };

```

```

29 ostream& operator<<(ostream& l, Vec r) {
30     return l << '(' << r.x << ", " << r.y << ')';
31 }
32 long double len(Vec a) {
33     return hypot(a.x, a.y);
34 }
35 long double cross(Vec l, Vec r) {
36     return l.x * r.y - l.y * r.x;
37 }
38 long double angle(Vec a) {
39     return fmod(atan2(a.y, a.x)+2*PI, 2*PI);
40 }
41 Vec normal(Vec a) {
42     return Vec({-a.y, a.x}) / len(a);
43 }



---


1 struct Segment {
2     Vec a, b;
3     Vec d() {
4         return b-a;
5     }
6 };
7 ostream& operator<<(ostream& l, Segment r) {
8     return l << r.a << '-' << r.b;
9 }
10 Vec intersection(Segment l, Segment r) {
11     Vec dl = l.d(), dr = r.d();
12     if(cross(dl, dr) == 0)
13         return {nanl(""), nanl("")};
14     long double h = cross(dr, l.a-r.a) / len(dr);
15     long double dh = cross(dr, dl) / len(dr);
16     return l.a + dl * (h / -dh);
17 }
18 //Returns the area bounded by halfplanes
19 long double getArea(vector<Segment> lines) {
20     long double lowerbound = -HUGE_VALL, upperbound = HUGE_VALL;
21     vector<Segment> linesBySide[2];
22     for(auto line : lines) {
23         if(line.b.y == line.a.y) {
24             if(line.a.x < line.b.x) {
25                 lowerbound = max(lowerbound, line.a.y);
26             } else {
27                 upperbound = min(upperbound, line.a.y);
28             }
29         } else if(line.a.y < line.b.y) {
30             linesBySide[1].push_back(line);
31         } else {
32             linesBySide[0].push_back({line.b, line.a});
33         }
34     }
35     sort(linesBySide[0].begin(), linesBySide[0].end(), [] (Segment l,
36         Segment r) {
37         if(cross(l.d(), r.d()) == 0) return normal(l.d())*l.a >
38         normal(r.d())*r.a;
39     });
40     sort(linesBySide[1].begin(), linesBySide[1].end(), [] (Segment l,
41         Segment r) {
42         if(cross(l.d(), r.d()) == 0) return normal(l.d())*l.a <
43         normal(r.d())*r.a;
44     });
45     //Now find the application area of the lines and clean up redundant
46     //ones
47     vector<long double> applyStart[2];
48     for(int side = 0; side < 2; side++) {
49         vector<long double> &apply = applyStart[side];
50         vector<Segment> curLines;
51         for(auto line : linesBySide[side]) {
52             while(curLines.size() > 0) {
53                 Segment other = curLines.back();
54                 if(cross(line.d(), other.d()) != 0) {
55                     long double start = intersection(line, other).y;
56                     if(start > apply.back()) break;
57                 }
58                 curLines.pop_back();
59                 apply.pop_back();
60             }
61             if(curLines.size() == 0) {
62                 apply.push_back(-HUGE_VALL);
63             } else {
64                 apply.push_back(intersection(line, curLines.back()).y);
65             }
66             curLines.push_back(line);
67         }
68         linesBySide[side] = curLines;
69     }
70     applyStart[0].push_back(HUGE_VALL);
71     applyStart[1].push_back(HUGE_VALL);
72     long double result = 0;
73     {
74         long double lb = -HUGE_VALL, ub;
75         for(int i=0, j=0; i < (int)linesBySide[0].size() && j <
76             (int)linesBySide[1].size(); lb = ub) {
77             ub = min(applyStart[0][i+1], applyStart[1][j+1]);
78             long double alb = lb, aub = ub;
79             Segment l0 = linesBySide[0][i], l1 = linesBySide[1][j];
80             if(cross(l1.d(), l0.d()) > 0) {
81                 alb = max(alb, intersection(l0, l1).y);
82             } else if(cross(l1.d(), l0.d()) < 0) {
83                 aub = min(aub, intersection(l0, l1).y);
84             }
85             alb = max(alb, lowerbound);
86             aub = min(aub, upperbound);
87             aub = max(aub, alb);
88             {
89                 long double x1 = l0.a.x + (alb - l0.a.y) / l0.d().y * l0.d().x;
90                 result += aub - x1;
91             }
92         }
93     }
94 }

```

```

86     long double x2 = 10.a.x + (aub - 10.a.y) / 10.d().y * 10.d().x;
87     result -= (aub - alb) * (x1 + x2) / 2;
88 }
89 {
90     long double x1 = 11.a.x + (alb - 11.a.y) / 11.d().y * 11.d().x;
91     long double x2 = 11.a.x + (aub - 11.a.y) / 11.d().y * 11.d().x;
92     result += (aub - alb) * (x1 + x2) / 2;                                #228
93 }
94 if(applyStart[0][i+1] < applyStart[1][j+1]) {
95     i++;
96 } else {
97     j++;
98 }
99 }
100 }                                              %011
101 return result;
102 }



---



## 7 Convex polygon algorithms



---


11 dot(const pair< int, int > &v1, const pair< int, int > &v2) {
12     return (ll)v1.first * v2.first + (ll)v1.second * v2.second;
13 }
14 ll cross(const pair< int, int > &v1, const pair< int, int > &v2) {
15     return (ll)v1.first * v2.second - (ll)v2.first * v1.second;
16 }
17 ll dist_sq(const pair< int, int > &p1, const pair< int, int > &p2) {
18     return (ll)(p2.first - p1.first) * (p2.first - p1.first) +
19             (ll)(p2.second - p1.second) * (p2.second - p1.second);          %025
20 }
21 struct Hull {
22     vector< pair< pair< int, int >, pair< int, int > > > hull;
23     vector< pair< pair< int, int >, pair< int, int > > >::iterator
24         → upper_begin;
25     template < typename Iterator >
26     void extend_hull(Iterator begin, Iterator end) { // O(n)
27         vector< pair< int, int > > res;
28         for (auto it = begin; it != end; ++it) {
29             if (res.empty() || *it != res.back()) {
30                 while (res.size() >= 2) {
31                     auto v1 = make_pair(res[res.size() - 1].first -
32                         → res[res.size() - 2].first,                      #048
33                         res[res.size() - 1].second -
34                         → res[res.size() - 2].second);
35                     auto v2 = make_pair(it->first - res[res.size() - 2].first,
36                         it->second - res[res.size() - 2].second);
37                     if (cross(v1, v2) > 0)
38                         break;
39                     res.pop_back();
40                 }
41                 res.push_back(*it);
42             }
43         }                                              #901
44         for (int i = 0; i < res.size() - 1; ++i)
45             hull.emplace_back(res[i], res[i + 1]);
46     }
47 }



---


33     }
34     Hull(vector< pair< int, int > > &vert) { // atleast 2 distinct
35         → points
36         sort(vert.begin(), vert.end());           // O(n log(n))
37         extend_hull(vert.begin(), vert.end());
38         int diff = hull.size();
39         extend_hull(vert.rbegin(), vert.rend());
40         upper_begin = hull.begin() + diff;        %873
41     }
42     bool contains(pair< int, int > p) { // O(log(n))
43         if (p < hull.front().first || p > upper_begin->first) return false;
44         {
45             auto it_low = lower_bound(hull.begin(), upper_begin,
46                         make_pair(make_pair(p.first,
47                             → (int)-2e9), make_pair(0, 0)));
48             if (it_low != hull.begin())
49                 --it_low;
50             auto v1 = make_pair(it_low->second.first - it_low->first.first,
51                         it_low->second.second - → it_low->first.second);
52             auto v2 = make_pair(p.first - it_low->first.first, p.second - →
53                         it_low->first.second);                           #094
54             if (cross(v1, v2) < 0) // < 0 is inclusive, <=0 is exclusive
55                 return false;
56         }
57         auto it_up = lower_bound(hull.rbegin(), hull.rbegin() +
58             → (hull.end() - upper_begin),
59             make_pair(make_pair(p.first, (int)2e9),
60                         → make_pair(0, 0)));
61         if (it_up - hull.rbegin() == hull.end() - upper_begin)
62             --it_up;
63         auto v1 = make_pair(it_up->first.first - it_up->second.first,
64                         it_up->first.second - it_up->second.second);    #900
65         auto v2 = make_pair(p.first - it_up->second.first, p.second - →
66                         it_up->second.second);
67         if (cross(v1, v2) > 0) // > 0 is inclusive, >=0 is exclusive
68             return false;
69     }
70     template < typename T > // The function can have only one local min
71         → and max and may be constant
72         // only at min and max.
73     vector< pair< pair< int, int >, pair< int, int > > >::iterator max(
74         function< T(const pair< pair< int, int >, pair< int, int > > &) >
75             → f) { // O(log(n))
76         auto l = hull.begin();
77         auto r = hull.end();
78         vector< pair< pair< int, int >, pair< int, int > > >::iterator best
79             → = hull.end();
80         T best_val;
81     }
82 }

```

```

75 while (r - l > 2) {
76     auto mid = l + (r - l) / 2;
77     T l_val = f(*l);
78     T l_nxt_val = f(*(l + 1));
79     T mid_val = f(*mid);
80     T mid_nxt_val = f(*(mid + 1));
81     if (best == hull.end() ||
82         l_val > best_val) { // If max is at l we may remove it from
83         // the range.
84     best = l;
85     best_val = l_val;
86 } if (l_nxt_val > l_val) {
87     if (mid_val < l_val) {
88         r = mid;
89     } else {
90         if (mid_nxt_val > mid_val) {
91             l = mid + 1;
92         } else {
93             r = mid + 1;
94         }
95     }
96 } else {
97     if (mid_val < l_val) {
98         l = mid + 1;
99     } else {
100        if (mid_nxt_val > mid_val) {
101            l = mid + 1;
102        } else {
103            r = mid + 1;
104        }
105    }
106 }
107 T l_val = f(*l);
108 if (best == hull.end() || l_val > best_val) {
109     best = l;
110     best_val = l_val;
111 }
112 if (r - l > 1) {
113     T l_nxt_val = f(*(l + 1));
114     if (best == hull.end() || l_nxt_val > best_val) {
115         best = l + 1;
116         best_val = l_nxt_val;
117     }
118 }
119 return best;
120 }
121 vector< pair< pair< int, int >, pair< int, int > >::iterator
122     closest(
123     pair< int, int >
124     p) { // p can't be internal(can be on border), hull must
125         const pair< pair< int, int >, pair< int, int > > &ref_p =
126             hull.front(); // O(log(n))
127         return max(function< double(const pair< pair< int, int >, pair<
128             int, int > > >(&p, &ref_p)(const pair< pair< int, int >, pair< int, int > >,
129             &seg) { // accuracy of used type should be
130                 coord-2
131                 if (p == seg.first) return 10 - M_PI;
132                 auto v1 =
133                     make_pair(seg.second.first - seg.first.first,
134                         seg.second.second - seg.first.second); #685
135                 auto v2 = make_pair(p.first - seg.first.first, p.second -
136                     seg.first.second);
137                 ll cross_prod = cross(v1, v2);
138                 if (cross_prod > 0) { // order the backside by angle
139                     auto v1 = make_pair(ref_p.first.first - p.first,
140                         ref_p.first.second - p.second);
141                     auto v2 = make_pair(seg.first.first - p.first,
142                         seg.first.second - p.second);
143                     ll dot_prod = dot(v1, v2);
144                     ll cross_prod = cross(v2, v1);
145                     return atan2(cross_prod, dot_prod) / 2;
146                 }
147                 ll dot_prod = dot(v1, v2); #395
148                 double res = atan2(dot_prod, cross_prod);
149                 if (dot_prod <= 0 && res > 0) res = -M_PI;
150                 if (res > 0) {
151                     res += 20;
152                 } else {
153                     res = 10 - res;
154                 }
155                 return res;
156             }));
157         pair< int, int > forw_tan(pair< int, int > p) { // can't be internal
158             or on border
159             const pair< pair< int, int >, pair< int, int > > &ref_p =
160                 hull.front(); // O(log(n))
161             auto best_seg = max(function< double(const pair< pair< int, int >,
162                 pair< int, int > > >(&p, &ref_p)(const pair< pair< int, int >, pair< int, int > >,
163                 &seg) { // accuracy of used type should be
164                     coord-2
165                     auto v1 = make_pair(ref_p.first.first - p.first,
166                         ref_p.first.second - p.second);
167                     auto v2 = make_pair(seg.first.first - p.first,
168                         seg.first.second - p.second);
169                     ll dot_prod = dot(v1, v2);
170                     ll cross_prod = cross(v2, v1); // cross(v1, v2) for
171                         backtan!!!
172                     return atan2(cross_prod, dot_prod); // order by signed
173                         angle
174             }));
175     }

```

```

163     return best_seg->first;
164 }
165 vector< pair< pair< int, int >, pair< int, int > >::iterator
166     ↪ max_in_dir(
167         pair< int, int > v) { // first is the ans. O(log(n))
168     return max(function< ll(const pair< pair< int, int >, pair< int,
169         int > > &) >(
170             [&v](const pair< pair< int, int >, pair< int, int > > &seg) {
171                 ↪ return dot(v, seg.first); }));
172 }
173 pair< vector< pair< pair< int, int >, pair< int, int > >::iterator,
174     vector< pair< pair< int, int >, pair< int, int > >::iterator
175     ↪ >
176 intersections(pair< pair< int, int >, pair< int, int > > line) { // %
177     ↪ O(log(n))
178     int x = line.second.first - line.first.first;
179     int y = line.second.second - line.first.second;
180     auto dir = make_pair(-y, x);
181     auto it_max = max_in_dir(dir);
182     auto it_min = max_in_dir(make_pair(y, -x));
183     ll opt_val = dot(dir, line.first);
184     if (dot(dir, it_max->first) < opt_val || dot(dir, it_min->first) >
185         ↪ opt_val)
186         return make_pair(hull.end(), hull.end());
187     vector< pair< pair< int, int >, pair< int, int > >::iterator
188         ↪ it_r1, it_r2; #785
189     function< bool(const pair< pair< int, int >, pair< int, int > > &,
190                 const pair< pair< int, int >, pair< int, int > > &)
191                 ↪ >
192         inc_comp([&dir](const pair< pair< int, int >, pair< int, int > >
193             ↪ > &lft,
194                 const pair< pair< int, int >, pair< int, int > >
195                     ↪ > &rgt) {
196                     ↪
197                     return dot(dir, lft.first) < dot(dir, rgt.first);
198                 });
199     function< bool(const pair< pair< int, int >, pair< int, int > > &,
200                 const pair< pair< int, int >, pair< int, int > > &)
201                 ↪ >
202         dec_comp([&dir](const pair< pair< int, int >, pair< int, int > >
203             ↪ > &lft,
204                 const pair< pair< int, int >, pair< int, int > >
205                     ↪ > &rgt) {
206                     ↪
207                     return dot(dir, lft.first) > dot(dir, rgt.first);
208                 });
209     if (it_min <= it_max) {
210         it_r1 = upper_bound(it_min, it_max + 1, line, inc_comp) - 1;
211         if (dot(dir, hull.front().first) >= opt_val) {
212             it_r2 = upper_bound(hull.begin(), it_min + 1, line, dec_comp) -
213                     ↪ 1;
214         } else {
215             it_r2 = upper_bound(it_max, hull.end(), line, dec_comp) - 1;
216         }
217     } else {
218         it_r1 = upper_bound(it_max, it_min + 1, line, dec_comp) - 1;
219         if (dot(dir, hull.front().first) <= opt_val) {
220             it_r2 = upper_bound(hull.begin(), it_max + 1, line, inc_comp) -
221                     ↪ 1;
222         } else {
223             it_r2 = upper_bound(it_min, hull.end(), line, inc_comp) - 1;
224         }
225     }
226     return make_pair(it_r1, it_r2); %000
227 }
228 pair< pair< int, int >, pair< int, int > > diameter() { // O(n)
229     pair< pair< int, int >, pair< int, int > > res;
230     ll dia_sq = 0;
231     auto it1 = hull.begin();
232     auto it2 = upper_begin;
233     auto v1 = make_pair(hull.back().second.first -
234         ↪ hull.back().first.first,
235             hull.back().second.second -
236                 ↪ hull.back().first.second);
237     while (it2 != hull.begin()) {
238         auto v2 = make_pair((it2 - 1)->second.first - (it2 -
239             ↪ 1)->first.first,
240                 (it2 - 1)->second.second - (it2 -
241                     ↪ 1)->first.second); #671
242         ll decider = cross(v1, v2);
243         if (decider > 0) break;
244         --it2;
245     }
246     while (it2 != hull.end()) { // check all antipodal pairs
247         if (dist_sq(it1->first, it2->first) > dia_sq) {
248             res = make_pair(it1->first, it2->first);
249             dia_sq = dist_sq(res.first, res.second);
250         }
251         auto v1 =
252             make_pair(it1->second.first - it1->first.first,
253                 ↪ it1->second.second - it1->first.second); #674
254         auto v2 =
255             make_pair(it2->second.first - it2->first.first,
256                 ↪ it2->second.second - it2->first.second);
257         ll decider = cross(v1, v2);
258         if (decider == 0) { // report cross pairs at parallel lines.
259             if (dist_sq(it1->second, it2->first) > dia_sq) {
260                 res = make_pair(it1->second, it2->first);
261                 dia_sq = dist_sq(res.first, res.second);
262             }
263             if (dist_sq(it1->first, it2->second) > dia_sq) #466
264                 res = make_pair(it1->first, it2->second);
265                 dia_sq = dist_sq(res.first, res.second);
266             }
267             ++it1;
268             ++it2;
269         } else if (decider < 0) {
270             ++it1;
271         }
272     }
273 }
```

```

248     } else {
249         ++it2;
250     }
251 }
252 return res;
253 }
254 #502 %215


---


8 Aho Corasick  $\mathcal{O}(|\alpha| \sum \text{len})$ 
1 const int alpha_size=26;
2 struct node{
3     node *nxt[alpha_size]; //May use other structures to move in trie
4     node *suffix;
5     node(){
6         memset(nxt, 0, alpha_size*sizeof(node *));
7     }
8     int cnt=0;
9 };
10 node *aho_corasick(vector<vector<char> > &dict){ #480
11     node *root= new node;
12     root->suffix = 0;
13     vector<pair<vector<char> *, node *> > cur_state;
14     for(vector<char> &s : dict)
15         cur_state.emplace_back(&s, root);
16     for(int i=0; !cur_state.empty(); ++i){
17         vector<pair<vector<char> *, node *> > nxt_state;
18         for(auto &cur : cur_state){
19             node *nxt=cur.second->nxt[(*cur.first)[i]];
20             if(nxt){
21                 cur.second=nxt;
22             }else{
23                 nxt = new node;
24                 cur.second->nxt[(*cur.first)[i]] = nxt;
25                 node *suf = cur.second->suffix;
26                 cur.second = nxt;
27                 nxt->suffix = root; //set correct suffix link
28                 while(suf){
29                     if(suf->nxt[(*cur.first)[i]]){
30                         nxt->suffix = suf->nxt[(*cur.first)[i]];
31                         break;
32                     }
33                     suf=suf->suffix;
34                 }
35                 if(cur.first->size() > i+1)
36                     nxt_state.push_back(cur);
37             }
38             cur_state=nxt_state;
39         }
40     }
41     return root;
42 }
43 //auxiliary functions for searching and counting
44 node *walk(node *cur, char c){ //longest prefix in dict that is suffix
    → of walked string.
#888 #786 #940 %064
45     while(true){
46         if(cur->nxt[c])
47             return cur->nxt[c];
48         if(!cur->suffix)
49             return cur;
50         cur = cur->suffix;
51     }
52 }
53 void cnt_matches(node *root, vector<char> &match_in){ #127
54     node *cur = root;
55     for(char c : match_in){
56         cur = walk(cur, c);
57         ++cur->cnt;
58     }
59 }
60 void add_cnt(node *root){ //After counting matches propagate ONCE to
    → suffixes for final counts
61     vector<node *> to_visit = {root};
62     for(int i=0; i<to_visit.size(); ++i){
63         node *cur = to_visit[i];
64         for(int j=0; j<alpha_size; ++j){
65             if(cur->nxt[j])
66                 to_visit.push_back(cur->nxt[j]);
67         }
68     }
69     for(int i=to_visit.size()-1; i>0; --i) #865
70         to_visit[i]->suffix->cnt += to_visit[i]->cnt;
71 }
72 int main(){ #313
    → //http://codeforces.com/group/s3etJR5zZK/contest/212916/problem/4
73     int n, len;
74     scanf("%d %d", &len, &n);
75     vector<char> a(len+1);
76     scanf("%s", a.data());
77     a.pop_back();
78     for(char &c : a)
79         c -= 'a';
80     vector<vector<char> > dict(n);
81     for(int i=0; i<n; ++i){
82         scanf("%d", &len);
83         dict[i].resize(len+1);
84         scanf("%s", dict[i].data());
85         dict[i].pop_back();
86         for(char &c : dict[i])
87             c -= 'a';
88     }
89     node *root = aho_corasick(dict);
90     cnt_matches(root, a);
91     add_cnt(root);
92     for(int i=0; i<n; ++i){
93         node *cur = root;
94         for(char c : dict[i])
95             cur = walk(cur, c);

```

```

96     printf("%d\n", cur->cnt);
97 }
98 }



---



### 9 Suffix automaton $\mathcal{O}((n+q) \log(|\text{alpha}|))$



---


1 class AutoNode {
2 private:
3     map< char, AutoNode * > nxt_char; // Map is faster than hashtable
4         ↪ and unsorted arrays
5 public:
6     int len; //Length of longest suffix in equivalence class.
7     AutoNode *suf;
8     bool has_nxt(char c) const {
9         return nxt_char.count(c);
10    }
11    AutoNode *nxt(char c) { #486
12        if (!has_nxt(c))
13            return NULL;
14        return nxt_char[c];
15    }
16    void set_nxt(char c, AutoNode *node) {
17        nxt_char[c] = node;
18    }
19    AutoNode *split(int new_len, char c) { #952
20        AutoNode *new_n = new AutoNode;
21        new_n->nxt_char = nxt_char;
22        new_n->len = new_len;
23        new_n->suf = suf;
24        suf = new_n;
25        return new_n;
26    }
27    // Extra functions for matching and counting
28    AutoNode *lower_depth(int depth) { //move to longest suffix of
29        ↪ current with a maximum length of depth.
30        if (suf->len >= depth)
31            return suf->lower_depth(depth);
32        return this; #795
33    }
34    AutoNode *walk(char c, int depth, int &match_len) { //move to longest
35        ↪ suffix of walked path that is a substring
36        match_len = min(match_len, len); //includes depth limit(needed for
37        ↪ finding matches)
38        if (has_nxt(c)) { //as suffixes are in classes match_len must be
39            ↪ tracked externally
40            ++match_len;
41            return nxt(c)->lower_depth(depth);
42        }
43        if (suf)
44            return suf->walk(c, depth, match_len);
45        return this; #152
46    }
47    int paths_to_end = 0;
48    void set_as_end() { //All suffixes of current node are marked as
49        ↪ ending nodes.

```

```

44    paths_to_end = 1;
45    if (suf) suf->set_as_end();
46 }
47 bool vis = false;
48 void calc_paths_to_end() { //Call ONCE from ROOT. For each node
49     ↪ calculates number of ways to reach an end node.
50     if (!vis) { //paths_to_end is occurrence count for any strings in
51         ↪ current suffix equivalence class.
52         vis = true;
53         for (auto cur : nxt_char) { #738
54             cur.second->calc_paths_to_end();
55             paths_to_end += cur.second->paths_to_end;
56         }
57     }
58 struct SufAutomaton {
59     AutoNode *last;
60     AutoNode *root;
61     void extend(char new_c) { #885
62         AutoNode *new_end = new AutoNode;
63         new_end->len = last->len + 1;
64         AutoNode *suf_w_nxt = last;
65         while (suf_w_nxt && !suf_w_nxt->has_nxt(new_c)) {
66             suf_w_nxt->set_nxt(new_c, new_end);
67             suf_w_nxt = suf_w_nxt->suf;
68         }
69         if (!suf_w_nxt) {
70             new_end->suf = root;
71         } else { #873
72             AutoNode *max_sbstr = suf_w_nxt->nxt(new_c);
73             if (suf_w_nxt->len + 1 == max_sbstr->len) {
74                 new_end->suf = max_sbstr;
75             } else {
76                 AutoNode *eq_sbstr = max_sbstr->split(suf_w_nxt->len + 1,
77                     ↪ new_c);
78                 new_end->suf = eq_sbstr
79                 AutoNode *w_edge_to_eq_sbstr = suf_w_nxt;
80                 while (w_edge_to_eq_sbstr != 0 &&
81                     ↪ w_edge_to_eq_sbstr->nxt(new_c) == max_sbstr) {
82                     w_edge_to_eq_sbstr->set_nxt(new_c, eq_sbstr);
83                     w_edge_to_eq_sbstr = w_edge_to_eq_sbstr->suf; #881
84                 }
85             }
86         }
87         last = new_end;
88     }
89     SufAutomaton(string to_suffix) {
90         root = new AutoNode;
91         root->len = 0;
92         root->suf = NULL;
93         last = root;
94         for (char c : to_suffix) extend(c); #935
95     }
96 }

```

```

93     }
94 };
%543

1 #include <bits/stdc++.h>
2 using namespace std;
3 typedef long long ll; \section{Dinic}
4
5 struct MaxFlow{
6     typedef long long ll;
7     const ll INF = 1e18;
8     struct Edge{
9         int u,v;
10        ll c,rc;
11        shared_ptr<ll> flow;
12        Edge(int _u, int _v, ll _c, ll _rc = 0):u(_u),v(_v),c(_c),rc(_rc){
13    } #787
14    };
15    struct FlowTracker{
16        shared_ptr<ll> flow;
17        ll cap, rcap;
18        bool dir;
19        FlowTracker(ll _cap, ll _rcap, shared_ptr<ll> _flow, int
20        _dir):cap(_cap),rcap(_rcap),flow(_flow),dir(_dir){ }
21        ll rem() const {
22            if(dir == 0){
23                return cap-*flow;
24            }
25            else{ #844
26                return rcap+*flow;
27            }
28        void add_flow(ll f){
29            if(dir == 0)
30                *flow += f;
31            else
32                *flow -= f;
33            assert(*flow <= cap);
34            assert(-*flow <= rcap);
35        }
36        operator ll() const { return rem(); }
37        void operator-=(ll x){ add_flow(x); }
38        void operator+=(ll x){ add_flow(-x); }
39    };
40    int source,sink;
41    vector<vector<int>> adj;
42    vector<vector<FlowTracker>> cap;
43    vector<Edge> edges;
44    MaxFlow(int _source, int _sink):source(_source),sink(_sink){ #080
45        assert(source != sink);
46    }
47    int add_edge(int u, int v, ll c, ll rc = 0){
48        edges.push_back(Edge(u,v,c,rc));
49        return edges.size()-1;
50    }

```

```

51    vector<int> now,lvl;
52    void prep(){
53        int max_id = max(source, sink);
54        for(auto edge : edges)
55            max_id = max(max_id, max(edge.u, edge.v));
56        adj.resize(max_id+1);
57        cap.resize(max_id+1);
58        now.resize(max_id+1);
59        lvl.resize(max_id+1);
60        for(auto &edge : edges){
61            auto flow = make_shared<ll>(0);
62            adj[edge.u].push_back(edge.v);
63            cap[edge.u].push_back(FlowTracker(edge.c, edge.rc, flow, 0));
64            if(edge.u != edge.v){ #717
65                adj[edge.v].push_back(edge.u);
66                cap[edge.v].push_back(FlowTracker(edge.c, edge.rc, flow, 1));
67            }
68            assert(cap[edge.u].back() == edge.c);
69            edge.flow = flow;
70        }
71    }
72    bool dinic_bfs(){ #038
73        fill(now.begin(),now.end(),0);
74        fill(lvl.begin(),lvl.end(),0);
75        lvl[source] = 1;
76        vector<int> bfs(1,source);
77        for(int i = 0; i < bfs.size(); ++i){
78            int u = bfs[i];
79            for(int j = 0; j < adj[u].size(); ++j){
80                int v = adj[u][j];
81                if(cap[u][j] > 0 && lvl[v] == 0){
82                    lvl[v] = lvl[u]+1;
83                    bfs.push_back(v);
84                }
85            }
86        }
87        return lvl[sink] > 0;
88    }
89    ll dinic_dfs(int u, ll flow){ #010
90        if(u == sink)
91            return flow;
92        while(now[u] < adj[u].size()){
93            int v = adj[u][now[u]];
94            if(lvl[v] == lvl[u] + 1 && cap[u][now[u]] != 0){ #014
95                ll res = dinic_dfs(v,min(flow,(ll)cap[u][now[u]]));
96                if(res > 0){
97                    cap[u][now[u]] -= res;
98                    return res;
99                }
100            }
101            ++now[u];
102        }
103        return 0;

```

```

104 }
105 ll calc_max_flow(){
106     prep();
107     ll ans = 0;
108     while(dinic_bfs()){
109         ll cur = 0;
110         do{
111             cur = dinic_dfs(source, INF);
112             ans += cur;
113         }while(cur > 0);
114     }
115     return ans;
116 }
117 ll flow_on_edge(int edge_index){
118     assert(edge_index < edges.size());
119     return *edges[edge_index].flow;
120 }
121 };
122 int main(){
123     int n,m;
124     cin >> n >> m;
125     vector<pair<int, pair<int, int>>> graph(m);
126     for(int i=0; i<m; ++i){
127         cin >> graph[i].second.first >> graph[i].second.second >> graph[i].first;
128     }
129     ll res=0;
130     for(auto cur : graph){
131         auto mf = MaxFlow(cur.second.first, cur.second.second); // arguments
132         ← source and sink, memory usage O(largest node index + input
133         ← size), sink doesn't need to be last index
134         for(int i = 0; i < m; ++i){
135             if(graph[i].first > cur.first){
136                 mf.add_edge(graph[i].second.first, graph[i].second.second, 1, 1);
137                 ← store edge index if care about flow value
138             }
139             res += mf.calc_max_flow();
140         }
141         cout << res << endl;
142     }

```

10 Min Cost Max Flow with successive dijkstra $\mathcal{O}(\text{flow} \cdot n^2)$

```

1 const int nmax=1055;
2 const ll inf=1e14;
3 int t, n, v; //0 is source, v-1 sink
4 ll rem_flow[nmax][nmax]; //set [x][y] for directed capacity from x to
← y.
5 ll cost[nmax][nmax]; //set [x][y] for directed cost from x to y. SET TO
← inf IF NOT USED
6 ll min_dist[nmax];
7 int prev_node[nmax];
8 ll node_flow[nmax];
9 bool visited[nmax];
10 ll tot_cost, tot_flow; //output

```

```

#197
11 void min_cost_max_flow(){ //Does not work with negative cycles.
12     tot_cost=0;
13     tot_flow=0;
14     ll sink_pot=0;
15     min_dist[0] = 0; %927
16     for(int i=1; i<=v; ++i){ //in case of no negative edges Bellman-Ford
17         ← can be removed.
18         min_dist[i]=inf;
19     }
20     for(int i=0; i<v-1; ++i){
21         for(int j=0; j<v; ++j){
22             for(int k=0; k<v; ++k){
23                 if(rem_flow[j][k] > 0 && min_dist[j]+cost[j][k] < min_dist[k])
24                     min_dist[k] = min_dist[j]+cost[j][k];
25             }
26         }
27     }
28     for(int i=0; i<v; ++i){ //Apply potentials to edge costs.
29         for(int j=0; j<v; ++j){
30             if(cost[i][j]!=inf){
31                 cost[i][j]+=min_dist[i];
32                 cost[i][j]-=min_dist[j];
33             }
34         }
35     }
36     sink_pot+=min_dist[v-1]; //Bellman-Ford end. %849
37     while(true){
38         for(int i=0; i<=v; ++i){ //node after sink is used as start value
39             ← for Dijkstra.
40             min_dist[i]=inf;
41             visited[i]=false;
42         }
43         min_dist[0]=0;
44         node_flow[0]=inf;
45         int min_node;
46         while(true){ //Use Dijkstra to calculate potentials
47             int min_node=v;
48             for(int i=0; i<v; ++i){
49                 if(!visited[i]) && min_dist[i]<min_dist[min_node]
50                     min_node=i;
51             }
52             if(min_node==v) break;
53             visited[min_node]=true;
54             for(int i=0; i<v; ++i){
55                 if((!visited[i]) && min_dist[min_node]+cost[min_node][i] <
56                     min_dist[i]){
57                     min_dist[i]=min_dist[min_node]+cost[min_node][i];
58                     prev_node[i]=min_node;
59                     node_flow[i]=min(node_flow[min_node], rem_flow[min_node][i]); #881
60                 }
61             }
62         }
63         if(min_dist[v-1]==inf) break

```

```

61   for(int i=0; i<v; ++i){ //Apply potentials to edge costs.
62     for(int j=0; j<v; ++j){ //Found path from source to sink becomes
63       ← 0 cost.
64       if(cost[i][j] != inf){
65         cost[i][j]+=min_dist[i];
66         cost[i][j]-=min_dist[j];
67       }
68     }
69     sink_pot+=min_dist[v-1];
70     tot_flow+=node_flow[v-1];
71     tot_cost+=sink_pot*node_flow[v-1];
72     int cur=v-1;
73     while(cur!=0){ //Backtrack along found path that now has 0 cost.
74       rem_flow[prev_node[cur]][cur]-=node_flow[v-1];
75       rem_flow[cur][prev_node[cur]]+=node_flow[v-1]; #582
76       cost[cur][prev_node[cur]]=0;
77       if(rem_flow[prev_node[cur]][cur]==0)
78         cost[prev_node[cur]][cur]=inf;
79       cur=prev_node[cur];
80     }
81   }
82 }
83 int main(){//http://www.spoj.com/problems/GREED/
84   cin>>t;
85   for(int i=0; i<t; ++i){
86     cin>>n;
87     for(int j=0; j<nmax; ++j){
88       for(int k=0; k<nmax; ++k){
89         cost[j][k]=inf;
90         rem_flow[j][k]=0;
91       }
92     }
93     for(int j=1; j<=n; ++j){
94       cost[j][2*n+1]=0;
95       rem_flow[j][2*n+1]=1;
96     }
97     for(int j=1; j<=n; ++j){
98       int card;
99       cin>>card;
100      ++rem_flow[0][card];
101      cost[0][card]=0;
102    }
103    int ex_c;
104    cin>>ex_c;
105    for(int j=0; j<ex_c; ++j){
106      int a, b;
107      cin>>a>>b;
108      if(b<a) swap(a,b);
109      cost[a][b]=1;
110      rem_flow[a][b]=nmax;
111      cost[b][n+b]=0;
112      rem_flow[b][n+b]=nmax;
113      cost[n+b][a]=1;

```

#083

```

114   rem_flow[n+b][a]=nmax;
115 }
116 v=2*n+2;
117 min_cost_max_flow();
118 cout<<tot_cost<<'\n';
119 }
120 }

```

%803

11 Min Cost Max Flow with Cycle Cancelling $\mathcal{O}(\text{flow} \cdot nm)$

```

1 struct Network {
2   struct Node;
3   struct Edge {
4     Node *u, *v;
5     int f, c, cost;
6     Node* from(Node* pos) {
7       if(pos == u)
8         return v;
9       return u;
10    }
11   int getCap(Node* pos) {
12     if(pos == u)
13       return c-f;
14     return f;
15   }
16   int addFlow(Node* pos, int toAdd) {
17     if(pos == u) {
18       f += toAdd;
19       return toAdd * cost;
20     } else {
21       f -= toAdd;
22       return -toAdd * cost;
23     }
24   }
25 };
26 struct Node {
27   vector<Edge*> conn;
28   int index;
29 };
30 deque<Node> nodes; #965
31 deque<Edge> edges;
32 Node* addNode() {
33   nodes.push_back(Node());
34   nodes.back().index = nodes.size()-1;
35   return &nodes.back();
36 }
37 Edge* addEdge(Node* u, Node* v, int f, int c, int cost) { #534
38   edges.push_back({u, v, f, c, cost});
39   u->conn.push_back(&edges.back());
40   v->conn.push_back(&edges.back());
41   return &edges.back();
42 }
43 //Assumes all needed flow has already been added
44 int minCostMaxFlow() {

```

#042

#507

#534

#507

```

45 int n = nodes.size();
46 int result = 0;
47 struct State {
48     int p;
49     Edge* used;
50 };
51 while(1) {                                     #877
52     vector<vector<State>> state(1, vector<State>(n, {0, 0}));
53     for(int lev = 0; lev < n; lev++) {
54         state.push_back(state[lev]);
55         for(int i=0;i<n;i++){
56             if(lev == 0 || state[lev][i].p < state[lev-1][i].p) {
57                 for(Edge* edge : nodes[i].conn){
58                     if(edge->getCap(&nodes[i]) > 0) {
59                         int np = state[lev][i].p + (edge->u == &nodes[i] ?
60                             -edge->cost : edge->cost);
61                         int ni = edge->from(&nodes[i])->index;
62                         if(np < state[lev+1][ni].p) {           #281
63                             state[lev+1][ni].p = np;
64                             state[lev+1][ni].used = edge;
65                         }
66                     }
67                 }
68             }
69         }
70     }
71     //Now look at the last level
72     bool valid = false;
73     for(int i=0;i<n;i++) {                      #283
74         if(state[n-1][i].p > state[n][i].p) {
75             valid = true;
76             vector<Edge*> path;
77             int cap = 1000000000;
78             Node* cur = &nodes[i];
79             int clev = n;
80             vector<bool> exprl(n, false);
81             while(!exprl[cur->index]) {
82                 exprl[cur->index] = true;
83                 State cstate = state[clev][cur->index];      #954
84                 cur = cstate.used->from(cur);
85                 path.push_back(cstate.used);
86             }
87             reverse(path.begin(), path.end());
88             {
89                 int i=0;
90                 Node* cur2 = cur;
91                 do {
92                     cur2 = path[i]->from(cur2);
93                     i++;
94                 } while(cur2 != cur);
95                 path.resize(i);
96             }
97             for(auto edge : path) {
98                 cap = min(cap, edge->getCap(cur));
99             }
100         }
101     }
102 }
```

```

103     cur = edge->from(cur);
104 }
105     for(auto edge : path) {
106         result += edge->addFlow(cur, cap);
107         cur = edge->from(cur);                                #599
108     }
109 }
```

12 DMST $\mathcal{O}(E \log V)$

```

1 struct EdgeDesc{
2     int from, to, w;
3 };
4 struct DMST{
5     struct Node;
6     struct Edge{
7         Node *from;
8         Node *tar;
9         int w;
10        bool inc;
11    };
12     struct Circle{
13         bool vis = false;
14         vector<Edge *> contents;
15         void clean(int idx);
16     };
17     const static greater<pair<ll, Edge *>> comp; //Can use inline static
18     since C++17
19     static vector<Circle> to_process;
20     static bool no_dmst;
21     static Node *root;                                #536
22     struct Node{
23         Node *par = NULL;
24         vector<pair<int, int>> out_cands; //Circ, edge idx
25         vector<pair<ll, Edge *>> con;
26         bool in_use = false;
27         ll w = 0; //extra to add to edges in con
28         Node *anc(){                                #425
29             if(!par)
30                 return this;
31             while(par->par)
32                 par = par->par;
33             return par;
34         }
35         void clean(){                                #425
36             if(!no_dmst){
37                 in_use = false;
38                 for(auto &cur : out_cands)
39                     to_process[cur.first].clean(cur.second);
40             }
41         }
42     };
43 }
```

```

39     }
40 }
41 Node *con_to_root(){ #561
42     if(anc() == root)
43         return root;
44     in_use = true;
45     Node *super = this; //Will become root or the first Node
46     → encountered in a loop.
47     while(super == this){
48         while(!con.empty() && con.front().second->tar->anc() == anc()){
49             pop_heap(con.begin(), con.end(), comp);
50             con.pop_back();
51         } #522
52         if(con.empty()){
53             no_dmst = true;
54             return root;
55         }
56         pop_heap(con.begin(), con.end(), comp);
57         auto nxt = con.back();
58         con.pop_back();
59         w = -nxt.first;
60         if(nxt.second->tar->in_use){ //anc() wouldn't change anything
61             super = nxt.second->tar->anc(); #174
62             to_process.resize(to_process.size()+1);
63         } else {
64             super = nxt.second->tar->con_to_root();
65         }
66         if(super != root){
67             to_process.back().contents.push_back(nxt.second);
68             out_cands.emplace_back(to_process.size()-1,
69             → to_process.back().contents.size()-1);
70         } else { //Clean circles
71             nxt.second->inc = true;
72             nxt.second->from->clean(); #629
73         }
74     if(super != root){ //we are some loops non first Node.
75         if(con.size() > super->con.size()){
76             swap(con, super->con); //Largest con in loop should not be
77             → copied.
78             swap(w, super->w);
79         }
80         for(auto cur : con){
81             super->con.emplace_back(cur.first - super->w + w,
82             → cur.second);
83             push_heap(super->con.begin(), super->con.end(), comp); #375
84         }
85     }
86     par = super; //root or anc() of first Node encountered in a loop
87     return super;
88 }
89 vector<Edge> edges;
90 DMST(int n, vector<EdgeDesc> &desc, int r){ //Self loops and multiple
91     → edges are okay.
92     graph.resize(n);
93     cur_root = &graph[r];
94     for(auto &cur : desc) //Edges are reversed internally
95         edges.push_back(Edge{&graph[cur.to], &graph[cur.from], cur.w});
96     for(int i=0; i<desc.size(); ++i)
97         graph[desc[i].to].con.emplace_back(desc[i].w, &edges[i]);
98     for(int i=0; i<n; ++i)
99         make_heap(graph[i].con.begin(), graph[i].con.end(), comp);
100 }
101 bool find(){ #469
102     root = cur_root;
103     no_dmst = false;
104     for(auto &cur : graph){
105         cur.con_to_root();
106         to_process.clear();
107         if(no_dmst) return false;
108     }
109     return true;
110 }
111 ll weight(){ #732
112     ll res = 0;
113     for(auto &cur : edges){
114         if(cur.inc)
115             res += cur.w;
116     }
117     return res;
118 }
119 void DMST::Circle::clean(int idx){ #477
120     if(!vis){
121         vis = true;
122         for(int i=0; i<contents.size(); ++i){
123             if(i != idx){
124                 contents[i]->inc = true;
125                 contents[i]->from->clean();
126             }
127         }
128     }
129 }
130 const greater<pair<ll, DMST::Edge *>> DMST::comp;
131 vector<DMST::Circle> DMST::to_process;
132 bool DMST::no_dmst;
133 DMST::Node *DMST::root; #771

```

13 Bridges $\mathcal{O}(n)$

```

1 struct vert;
2 struct edge{
3     bool exists = true;
4     vert *dest;
5     edge *rev;

```

```

6  edge(vert *_dest) : dest(_dest){
7      rev = NULL;
8  }
9  vert &operator*(){
10     return *dest;
11 }
12 vert *operator->(){
13     return dest;
14 }
15 bool is_bridge();
16 };
17 struct vert{
18     deque<edge> con;
19     int val = 0;
20     int seen;
21     int dfs(int upd, edge *ban){ //handles multiple edges
22         if(!val){
23             val = upd;
24             seen = val;
25             for(edge &nxt : con){
26                 if(nxt.exists && (&nxt) != ban)
27                     seen = min(seen, nxt->dfs(upd+1, nxt.rev));
28             }
29         }
30         return seen;
31     }
32     void remove_adj_bridges(){
33         for(edge &nxt : con){
34             if(nxt.is_bridge())
35                 nxt.exists = false;
36         }
37     }
38     int cnt_adj_bridges(){
39         int res = 0;
40         for(edge &nxt : con)
41             res += nxt.is_bridge();
42         return res;
43     }
44 };
45 bool edge::is_bridge(){
46     return exists && (dest->seen > rev->dest->val || dest->val <
47     ↵ rev->dest->seen);
48 }
49 int main(){ //Mechanics Practice BRIDGES
50     int n, m;
51     cin>>n>>m;
52     for(int i=0; i<m; ++i){
53         int u, v;
54         scanf("%d %d", &u, &v);
55         graph[u].con.emplace_back(graph+v);
56         graph[v].con.emplace_back(graph+u);
57         graph[u].con.back().rev = &graph[v].con.back();
58     }
59 }
60 graph[1].dfs(1, NULL);
61 int res = 0;
62 for(int i=1; i<=n; ++i)
63     res += graph[i].cnt_adj_bridges();
64 cout<<res/2<<endl;
65 }

#955
#336
#673
%624
%106
%056
%0223

```

```

58     graph[v].con.back().rev = &graph[u].con.back();
59 }
60 graph[1].dfs(1, NULL);
61 int res = 0;
62 for(int i=1; i<=n; ++i)
63     res += graph[i].cnt_adj_bridges();
64 cout<<res/2<<endl;
65 }



---



### 14 2-Sat $\mathcal{O}(n)$ and SCC $\mathcal{O}(n)$


1 struct Graph {
2     int n;
3     vector<vector<int> > conn;
4     Graph(int nsiz) {
5         n = nsiz;
6         conn.resize(n);
7     }
8     void add_edge(int u, int v) {
9         conn[u].push_back(v);
10    }
11    void _topsort_dfs(int pos, vector<int> &result, vector<bool>
12        ↵ &explr, vector<vector<int> > &revconn) {
13        if(explr[pos])
14            return;
15        explr[pos] = true;
16        for(auto next : revconn[pos])
17            _topsort_dfs(next, result, explr, revconn);
18        result.push_back(pos);
19    }
20    vector<int> topsort() {
21        vector<vector<int> > revconn(n);
22        for(int u = 0; u < n; u++) {
23            for(auto v : conn[u])
24                revconn[v].push_back(u);
25        }
26        vector<int> result;
27        vector<bool> explr(n, false);
28        for(int i=0; i < n; i++)
29            _topsort_dfs(i, result, explr, revconn);
30        reverse(result.begin(), result.end());
31        return result;
32    }
33    void dfs(int pos, vector<int> &result, vector<bool> &explr) {
34        if(explr[pos])
35            return;
36        explr[pos] = true;
37        for(auto next : conn[pos])
38            dfs(next, result, explr);
39        result.push_back(pos);
40    }
41    vector<vector<int> > scc(){ // tested on
42        ↵ https://www.hackerearth.com/practice/algorithms/graphs/strongly-connect
43        vector<int> order = topsort();
44        reverse(order.begin(), order.end());
45    }
46 }

#078
#346
#991
#603

```

```

43     vector<bool> exprl(n, false);
44     vector<vector<int>> results;
45     for(auto it = order.rbegin(); it != order.rend(); ++it){
46         vector<int> component;
47         _topsort_dfs(*it, component, exprl, conn);
48         sort(component.begin(), component.end());
49         results.push_back(component); #741
50     }
51     sort(results.begin(), results.end());
52     return results;
53 }
54 }; %983
55 //Solution for:
56 → http://codeforces.com/group/PjzGiggT71/contest/221700/problem/C
57 int main() {
58     int n, m;
59     cin >> n >> m;
60     Graph g(2*m);
61     for(int i=0; i<n; i++) {
62         int a, sa, b, sb;
63         cin >> a >> sa >> b >> sb;
64         a--; b--;
65         g.add_edge(2*a + 1 - sa, 2*b + sb);
66         g.add_edge(2*b + 1 - sb, 2*a + sa);
67     }
68     vector<int> state(2*m, 0);
69     {
70         vector<int> order = g.toposort();
71         vector<bool> exprl(2*m, false);
72         for(auto u : order) {
73             vector<int> traversed;
74             g.dfs(u, traversed, exprl);
75             if(traversed.size() > 0 && !state[traversed[0]^1]) {
76                 for(auto c : traversed)
77                     state[c] = 1;
78             }
79         }
80         for(int i=0; i < m; i++) {
81             if(state[2*i] == state[2*i+1]) {
82                 cout << "IMPOSSIBLE\n";
83                 return 0;
84             }
85         }
86         for(int i=0; i < m; i++) {
87             cout << state[2*i+1] << '\n';
88         }
89     }
90 }

```

15 Lazy Segment Tree $\mathcal{O}(\log n)$ per query

```

1 struct SegmentTree {
2     struct Node {
3         long long value = 0;

```

```

4         int size = 1;
5         int lazy_add = 0;
6         bool lazy_set = false;
7         int lazy_to_set = 0;
8         void set(int to_set) {
9             lazy_set = true;
10            lazy_to_set = to_set;
11            lazy_add = 0;
12        }
13    };
14    int n;
15    vector<Node> nodes;
16    void propagate(int pos) {
17        Node& cur = nodes[pos];
18        if(cur.lazy_set) {
19            if(pos < n) {
20                nodes[pos*2].set(cur.lazy_to_set); #388
21                nodes[pos*2+1].set(cur.lazy_to_set);
22            }
23            cur.value = 1LL * cur.size * cur.lazy_to_set;
24            cur.lazy_set = false;
25        }
26        if(cur.lazy_add != 0) {
27            if(pos < n) {
28                nodes[pos*2].lazy_add += cur.lazy_add;
29                nodes[pos*2+1].lazy_add += cur.lazy_add; #114
30            }
31            cur.value += 1LL * cur.size * cur.lazy_add;
32            cur.lazy_add = 0;
33        }
34    }
35    long long get_value(int pos) {
36        propagate(pos);
37        return nodes[pos].value;
38    }
39    SegmentTree(int nsize) { #759
40        n = 1;
41        while(n < nsize) n*=2;
42        nodes.resize(2*n);
43        for(int i=n-1; i>0; i--)
44            nodes[i].size = nodes[2*i].size * 2;
45    }
46    void set(int l, int r, int to_set, int pos = 1, int lb = 0, int rb
47 ← = -1) {
48        propagate(pos);
49        if(rb == -1) rb = n;
50        if(l <= lb && rb <= r) {
51            nodes[pos].set(to_set); #567
52            return;
53        }
54        int mid = (lb + rb) / 2;
55        if(l < mid)
            set(l, r, to_set, pos*2, lb, mid);

```

```

56     if(mid < r)
57         set(l, r, to_set, pos*2+1, mid, rb);
58     nodes[pos].value = get_value(pos*2) + get_value(pos*2+1);
59 }
60 void add(int l, int r, int to_add, int pos = 1, int lb = 0, int rb
61     = -1) {                                     #168
62     propagate(pos);
63     if(rb == -1) rb = n;
64     if(l <= lb && rb <= r) {
65         nodes[pos].lazy_add += to_add;
66         return;
67     }
68     int mid = (lb + rb) / 2;
69     if(l < mid)
70         add(l, r, to_add, pos*2, lb, mid);           #620
71     if(mid < r)
72         add(l, r, to_add, pos*2+1, mid, rb);
73     nodes[pos].value = get_value(pos*2) + get_value(pos*2+1);
74 }
75 long long get(int l, int r, int pos = 1, int lb = 0, int rb = -1) {
76     propagate(pos);
77     if(rb == -1) rb = n;
78     if(l <= lb && rb <= r) return get_value(pos);
79     int mid = (lb + rb) / 2;
80     long long result = 0;                         #133
81     if(l < mid)
82         result += get(l, r, pos*2, lb, mid);
83     if(mid < r)
84         result += get(l, r, pos*2+1, mid, rb);
85     return result;
86 };                                              %280
87 //Solution for:
88     → http://codeforces.com/group/U01GDa2Gwb/contest/219104/problem/LAZY
89 int main() {
90     int n, m;
91     cin >> n >> m;
92     SegmentTree stree(n);
93     for(int i=0;i<n;i++) {
94         int a;
95         cin >> a;
96         stree.set(i, i+1, a);
97     }
98     for(int i=0;i<m;i++) {
99         int type;
100        cin >> type;
101        if(type == 1) {
102            int l, r, d;
103            cin >> l >> r >> d;
104            stree.add(l-1, r, d);
105        } else if(type == 2) {
106            int l, r, x;
107            cin >> l >> r >> x;
108            stree.set(l-1, r, x);
109        }
110    }
111 }
```

```

108     } else {
109         int l, r;
110         cin >> l >> r;
111         cout << stree.get(l-1, r) << '\n';
112     }
113 }
114 }
```

16 Generic segment tree(lazy, noncommutative)

```

1 struct Segment{
2     ll sum_val=0;
3     ll min_val=0;
4     void find_sum(int seg_len, ll &cur_sum){
5         cur_sum = cur_sum + sum_val;
6     }
7     void find_min(int seg_len, ll &cur_min){
8         cur_min = min(cur_min, min_val);
9     }
10    void recalc(int seg_len, const Segment &lhs_seg, const Segment
11        &rhs_seg){                                #599
12        sum_val = lhs_seg.sum_val + rhs_seg.sum_val;
13        min_val = min(lhs_seg.min_val, rhs_seg.min_val);
14    }
15    struct Lazy{
16        ll add_val;
17        ll assign_val; //LLONG_MIN if no assign;
18        void init(){
19            add_val = 0;
20            assign_val = LLONG_MIN;                #577
21        }
22        Lazy(){ init(); }
23        void apply_to_lazy(int seg_len, Lazy &child) const{
24            if(assign_val != LLONG_MIN){
25                child.add_val = 0;
26                child.assign_val = assign_val;
27            }
28            child.add_val += add_val;
29        }
30        void apply_to_seg(int seg_len, Segment &cur) const{          #523
31            if(assign_val != LLONG_MIN){
32                cur.min_val = assign_val;
33                cur.sum_val = seg_len * assign_val;
34            }
35            cur.min_val += add_val;
36            cur.sum_val += seg_len * add_val;
37        } //Following code should not need to be modified             %992
38        void split(int seg_len, Lazy &lhs_lazy, Lazy &rhs_lazy){
39            apply_to_lazy(seg_len, lhs_lazy); //Empty current and pass on to
40            ← children
41            apply_to_lazy(seg_len, rhs_lazy);
42            init();
43        }
44    }
45 }
```

```

43 };
44 // Highly optimized generic segment tree with lazy propagation
45 class SegTree{ //indexes start from 0, ranges are [beg, end)
46 private:
47     int offset;
48     int height;
49     Segment *segs;
50     Lazy *lazys;
51     vector<bool> is_lazy;
52     void split(int len, int idx){ #678
53         is_lazy[idx] = false;
54         lazys[idx].apply_to_seg(len/2, segs[2*idx]);
55         lazys[idx].apply_to_seg(len/2, segs[2*idx+1]);
56         lazys[idx].split(len/2, lazys[2*idx], lazys[2*idx+1]);
57         is_lazy[2*idx] = true;
58         is_lazy[2*idx+1] = true; #984
59     }
60     void push(int bot_idx){
61         for(int s = height-1; s>0; --s){
62             int idx = bot_idx>>s;
63             if(is_lazy[idx]){ //Lazys can be below other lazys
64                 split(1<<s, idx);
65             }
66         }
67     }
68     void build(int len, int idx){ #201
69         for(; idx; len<=>1, idx>>=1){
70             segs[idx].recalc(len, segs[2*idx], segs[2*idx+1]);
71         }
72     }
73 public:
74     SegTree(int tree_size){
75         offset = tree_size;
76         height = 32 - __builtin_clz(tree_size);
77         segs = new Segment[2*tree_size];
78         lazys = new Lazy[2*tree_size];
79         is_lazy.resize(2*tree_size, false); #920
80     }
81     ~SegTree(){
82         delete[] segs;
83         delete[] lazys;
84     }
85     void modify(int l, int r, const Lazy &upd){ #744
86         l+=offset;
87         r+=offset;
88         push(l);
89         push(r-1);
90         int len = 1;
91         for(int l_tmp = l, r_tmp = r; l_tmp<=r_tmp; l_tmp >>= 1, r_tmp >>= 1, len <=> 1){ #744
92             if(l_tmp & 1){
93                 upd.apply_to_lazy(len, lazys[l_tmp]);
94                 upd.apply_to_seg(len, segs[l_tmp]);
95                 is_lazy[l_tmp] = true;
96             }
97             ++l_tmp;
98         }
99         if(r_tmp & 1){ #347
100             --r_tmp;
101             upd.apply_to_lazy(len, lazys[r_tmp]);
102             upd.apply_to_seg(len, segs[r_tmp]);
103             is_lazy[r_tmp] = true;
104         }
105         len = 1<<(__builtin_ctz(l)+1);
106         l >>= __builtin_ctz(l) + 1;
107         build(len, l);
108         len = 1<<(__builtin_ctz(r)+1);
109         r >>= __builtin_ctz(r) + 1;
110         build(len, r); #339
111     }
112     template< typename ...QueryArgs >
113     void query(int l, int r, void (Segment::*query_func)(int, #008
114             QueryArgs...), QueryArgs &&...query_args){
115         l+=offset;
116         r+=offset;
117         push(l);
118         push(r-1);
119         int len = 1; #008
120         int r_orig = r;
121         for(; l< r; l>>=1, r>>=1, len <<= 1){ //Segments applied in order
122             to querrey
123             if(l & 1){
124                 (segs[l++].*query_func)(len, query_args...);
125             }
126             for(; r < r_orig;){ #766
127                 r<=>1;
128                 len>>=1;
129                 if(r_orig & len){ #766
130                     (segs[r++].*query_func)(len, query_args...); #766
131                 }
132             }
133         }; #509
134         int main(){ #509
135             int n, m; //solves Mechanics Practice LAZY
136             cin>>n>>m;
137             SegTree seg_tree(n);
138             for(int i=0; i<n; ++i){
139                 Lazy tmp;
140                 scanf("%lld", &tmp.assign_val);
141                 seg_tree.modify(i, i+1, tmp);
142             }
143             for(int i=0; i<m; ++i){
144                 int o;
145                 int l, r;
146                 scanf("%d %d %d", &o, &l, &r);
147             }
148         }
149     }

```

```

147 --l;
148 if(o==1){
149     Lazy tmp;
150     scanf("%lld", &tmp.add_val);
151     seg_tree.modify(l, r, tmp);
152 } else if(o==2){
153     Lazy tmp;
154     scanf("%lld", &tmp.assign_val);
155     seg_tree.modify(l, r, tmp);
156 } else {
157     ll res=0;
158     seg_tree.query(l, r, &Segment::find_sum, res);
159     printf("%lld\n",res);
160 }
161 }
162 }
```

17 Templatized Persistent Segment Tree $\mathcal{O}(\log n)$ per query

```

1 template<typename T, typename comp>
2 class PersistentST {
3     struct Node {
4         Node *left, *right;
5         int lend, rend;
6         T value;
7         Node (int position, T _value) {
8             left = NULL;
9             right = NULL;
10            lend = position;
11            rend = position;
12            value = _value;
13        }
14        Node (Node *_left, Node *_right) {
15            left = _left;
16            right = _right;
17            lend = left->lend;
18            rend = right->rend;
19            value = comp()(left->value, right->value);
20        }
21        T query (int qleft, int qright) {
22            qleft = max(qleft, lend);
23            qright = min(qright, rend);
24            if (qleft == lend && qright == rend) {
25                return value;
26            } else if (qleft > qright) {
27                return comp().identity();
28            } else {
29                return comp()(left->query(qleft, qright), right->query(qleft,
30                                         qright));
31            }
32        }
33        int size;
34        Node **tree;
35        vector<Node*> roots;
#479
#373
#766
```

```

36 public:
37     PersistentST () {}
38     PersistentST (int _size, T initial) {
39         for (int i = 0; i < 32; i++) {
40             if ((1 << i) > _size) {
41                 size = 1 << i;
42                 break;
43             }
44         }
45         tree = new Node* [2 * size + 5];
46         for (int i = size; i < 2 * size; i++)
47             tree[i] = new Node (i - size, initial);
48         for (int i = size - 1; i > 0; i--)
49             tree[i] = new Node (tree[2 * i], tree[2 * i + 1]);
50         roots = vector<Node*> (1, tree[1]);
#128
51     }
52     void set (int position, T _value) {
53         tree[size + position] = new Node (position, _value);
54         for (int i = (size + position) / 2; i >= 1; i /= 2)
55             tree[i] = new Node (tree[2 * i], tree[2 * i + 1]);
56         roots.push_back(tree[1]);
57     }
58     int last_revision () {
59         return (int) roots.size() - 1;
60     }
#890
61     T query (int qleft, int qright, int revision) {
62         return roots[revision]->query(qleft, qright);
63     }
64     T query (int qleft, int qright) {
65         return roots[last_revision()]->query(qleft, qright);
66     }
#280
```

18 Templatized HLD $\mathcal{O}(M(n) \log n)$ per query

```

1 class dummy {
2 public:
3     dummy () {}
4     dummy (int, int) {}
5     void set (int, int) {}
6     int query (int left, int right) {
7         cout << this << ' ' << left << ' ' << right << endl;
8     }
9 };
%932
10 /* T should be the type of the data stored in each vertex;
11 * DS should be the underlying data structure that is used to perform
12 * the
13 * group operation. It should have the following methods:
14 * * DS () - empty constructor
15 * * DS (int size, T initial) - constructs the structure with the given
16 * size,
17 * * initially filled with initial.
18 * * void set (int index, T value) - set the value at index `index` to
19 * `value`
```

```

17 * * T query (int left, int right) - return the "sum" of elements
18   ↪ between left and right, inclusive.
19 */
20 template<typename T, class DS>
21 class HLD {
22     int vertexc;
23     vector<int> *adj;
24     vector<int> subtree_size;
25     DS structure;
26     DS aux;
27     void build_sizes (int vertex, int parent) {
28         subtree_size[vertex] = 1;
29         for (int child : adj[vertex]) {
30             if (child != parent) {
31                 build_sizes(child, vertex);
32                 subtree_size[vertex] += subtree_size[child];
33             }
34         }
35     int cur;
36     vector<int> ord;
37     vector<int> chain_root;
38     vector<int> par;
39     void build_hld (int vertex, int parent, int chain_source) {           #593
40         cur++;
41         ord[vertex] = cur;
42         chain_root[vertex] = chain_source;
43         par[vertex] = parent;
44         if (adj[vertex].size() > 1) {
45             int big_child, big_size = -1;
46             for (int child : adj[vertex]) {
47                 if ((child != parent) && (subtree_size[child] > big_size)) {    #646
48                     big_child = child;
49                     big_size = subtree_size[child];
50                 }
51             }
52             build_hld(big_child, vertex, chain_source);
53             for (int child : adj[vertex]) {
54                 if ((child != parent) && (child != big_child))
55                     build_hld(child, vertex, child);
56             }
57         }
58     }
59 public:
60     HLD (int _vertexc) {
61         vertexc = _vertexc;
62         adj = new vector<int> [vertexc + 5];
63     }
64     void add_edge (int u, int v) {
65         adj[u].push_back(v);
66         adj[v].push_back(u);
67     }
68     void build (T initial) {                                              #841
69         subtree_size = vector<int> (vertexc + 5);
70         ord = vector<int> (vertexc + 5);
71         chain_root = vector<int> (vertexc + 5);
72         par = vector<int> (vertexc + 5);
73         cur = 0;
74         build_sizes(1, -1);
75         build_hld(1, -1, 1);
76         structure = DS (vertexc + 5, initial);
77         aux = DS (50, initial);
78     }                                                               #793
79     void set (int vertex, int value) {
80         structure.set(ord[vertex], value);
81     }
82     T query_path (int u, int v) { /* returns the "sum" of the path u->v
83       ↪ */                                #517
84         int cur_id = 0;
85         while (chain_root[u] != chain_root[v]) {
86             if (ord[u] > ord[v]) {
87                 cur_id++;
88                 aux.set(cur_id, structure.query(ord[chain_root[u]], ord[u]));
89             } else {
90                 cur_id++;
91                 aux.set(cur_id, structure.query(ord[chain_root[v]], ord[v]));
92                 v = par[chain_root[v]];
93             }
94         }
95         cur_id++;
96         aux.set(cur_id, structure.query(min(ord[u], ord[v]), max(ord[u],
97             ↪ ord[v])));                                %257
98         return aux.query(1, cur_id);
99     }
100    void print () {
101        for (int i = 1; i <= vertexc; i++) {
102            cout << i << ' ' << ord[i] << ' ' << chain_root[i] << ' ' <<
103             ↪ par[i] << endl;
104    }
105    int main () {
106        int vertexc;
107        cin >> vertexc;
108        HLD<int, dummy> hld (vertexc);
109        for (int i = 0; i < vertexc - 1; i++) {
110            int u, v;
111            cin >> u >> v;
112            hld.add_edge(u, v);
113        }
114        hld.build();
115        hld.print();
116        int queryc;
117        cin >> queryc;
118        for (int i = 0; i < queryc; i++) {
119            int u, v;
            cin >> u >> v;

```

```

120     hld.query_path(u, v);
121     cout << endl;
122 }
123 }



---



### 19 Tempered multi dimensional BIT $\mathcal{O}(\log(n)^{\dim})$ per query



---


1 // Fully overloaded any dimensional BIT, use any type for coordinates,
2 // elements, return_value.
3 // Includes coordinate compression.
4 template < typename elem_t, typename coord_t, coord_t n_inf, typename
5   ↪ ret_t >
6 class BIT {
7   vector< coord_t > positions;
8   vector< elem_t > elems;
9   bool initiated = false;
10 public:
11   BIT() {
12     positions.push_back(n_inf);
13   }
14   void initiate() { #448
15     if (initiated) {
16       for (elem_t &c_elem : elems)
17         c_elem.initiate();
18     } else {
19       initiated = true;
20       sort(positions.begin(), positions.end());
21       positions.resize(unique(positions.begin(), positions.end()) -
22                         ↪ positions.begin());
23       elems.resize(positions.size());
24     }
25   }
26   template < typename... loc_form > #036
27   void update(coord_t cord, loc_form... args) {
28     if (initiated) {
29       int pos = lower_bound(positions.begin(), positions.end(), cord) -
30             ↪ positions.begin();
31       for (; pos < positions.size(); pos += pos & -pos)
32         elems[pos].update(args...);
33     } else {
34       positions.push_back(cord);
35     }
36   }
37   template < typename... loc_form > #154
38   ret_t query(coord_t cord, loc_form... args) { //sum in open interval
39     ↪ (-inf, cord)
40     ret_t res = 0;
41     int pos = (lower_bound(positions.begin(), positions.end(), cord) -
42               ↪ positions.begin())-1;
43     for (; pos > 0; pos -= pos & -pos)
44       res += elems[pos].query(args...);
45     return res;
46   }
47 };



---


42 template < typename internal_type > #895

```

```

43 struct wrapped {
44   internal_type a = 0;
45   void update(internal_type b) {
46     a += b;
47   }
48   internal_type query() {
49     return a;
50   }
51   // Should never be called, needed for compilation
52   void initiate() { #560
53     cerr << 'i' << endl;
54   }
55   void update() { #714
56     cerr << 'u' << endl;
57   }
58 };
59 int main() {
60   // return type should be same as type inside wrapped
61   BIT< BIT< wrapped< ll >, int, INT_MIN, ll >, int, INT_MIN, ll > #714
62   ↪ fenwick;
63   int dim = 2;
64   vector< tuple< int, int, ll > > to_insert;
65   to_insert.emplace_back(1, 1, 1);
66   // set up all positions that are to be used for update
67   for (int i = 0; i < dim; ++i) {
68     for (auto &cur : to_insert)
69       fenwick.update(get< 0 >(cur), get< 1 >(cur)); // May include
70       ↪ value which won't be used
71     fenwick.initiate();
72   }
73   // actual use
74   for (auto &cur : to_insert)
75     fenwick.update(get< 0 >(cur), get< 1 >(cur), get< 2 >(cur));
76   cout << fenwick.query(2, 2) << '\n';
77 }



---



```

20 Treap $\mathcal{O}(\log n)$ per query

```

1 mt19937 randgen;
2 struct Treap {
3   struct Node {
4     int key;
5     int value;
6     unsigned int priority;
7     long long total;
8     Node* lch;
9     Node* rch;
10    Node(int new_key, int new_value) { #698
11      key = new_key;
12      value = new_value;
13      priority = randgen();
14      total = new_value;
15      lch = 0;
16      rch = 0;
17    }

```

```

18     void update() {
19         total = value;
20         if(lch) total += lch->total;
21         if(rch) total += rch->total;
22     }
23 }
24 deque<Node> nodes;
25 Node* root = 0;
26 pair<Node*, Node*> split(int key, Node* cur) {
27     if(cur == 0) return {0, 0};
28     pair<Node*, Node*> result;
29     if(key <= cur->key) {
30         auto ret = split(key, cur->lch);
31         cur->lch = ret.second;
32         result = {ret.first, cur};
33     } else {
34         auto ret = split(key, cur->rch);
35         cur->rch = ret.first;
36         result = {cur, ret.second};
37     }
38     cur->update();
39     return result;
40 }
41 Node* merge(Node* left, Node* right) {
42     if(left == 0) return right;
43     if(right == 0) return left;
44     Node* top;
45     if(left->priority < right->priority) {
46         left->rch = merge(left->rch, right);
47         top = left;
48     } else {
49         right->lch = merge(left, right->lch);
50         top = right;
51     }
52     top->update();
53     return top;
54 }
55 void insert(int key, int value) {
56     nodes.push_back(Node(key, value));
57     Node* cur = &nodes.back();
58     pair<Node*, Node*> ret = split(key, root);
59     cur = merge(ret.first, cur);
60     cur = merge(cur, ret.second);
61     root = cur;
62 }
63 void erase(int key) {
64     Node *left, *mid, *right;
65     tie(left, mid) = split(key, root);
66     tie(mid, right) = split(key+1, mid);
67     root = merge(left, right);
68 }
69 long long sum_upto(int key, Node* cur) {
70     if(cur == 0) return 0;
71     if(key <= cur->key) {
#295
#233
#230
#510
#760
#634
#72
#73
#74
#75
#76
#77
#78
#79
#80
#81
#82
#83
#84
#85
#86
#87
#88
#89
#90
#91
#92
#93
#94
#95
#96
#97
#98
#99
#100
#101
#102
#103
#104
#105
#106
#107
#108
#509
%959
//Solution for:
→ http://codeforces.com/group/U01GDa2Gwb/contest/219104/problem/TREAP
int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(0);
    int m;
    Treap treap;
    cin >> m;
    for(int i=0;i<m;i++) {
        int type;
        cin >> type;
        if(type == 1) {
            int x, y;
            cin >> x >> y;
            treap.insert(x, y);
        } else if(type == 2) {
            int x;
            cin >> x;
            treap.erase(x);
        } else {
            int l, r;
            cin >> l >> r;
            cout << treap.get(l, r) << endl;
        }
    }
    return 0;
}

```

21 FFT 5M length/sec

integer $c = a * b$ is accurate if $c_i < 2^{49}$

```

1 struct Complex {
2     double a = 0, b = 0;
3     Complex &operator/=(const int &oth) {
4         a /= oth;
5         b /= oth;
6         return *this;
7     }
8 };
9 Complex operator+(const Complex &lft, const Complex &rgt) {
10    return Complex{lft.a + rgt.a, lft.b + rgt.b};
11 }
#384

```

22 Rabin Miller prime check, Pollard rho factorization $\mathcal{O}(\sqrt{p})$

```
static vector< char > small_primes = {2, 3, 5, 7, 11, 13, 17, 19, 23,
→ 29, 31, 37};
__int128 pow_mod(__int128 a, ll n, __int128 mod) {
    __int128 res = 1;
    for (ll i = 1; i <= n; i<<=1) {
        if (n & i)
```

```

6     res = (res * a) % mod;
7     a = (a * a) % mod;
8 }
9 return res;
10}
11bool is_prime(ll n) { //guaranteed for 64 bit numbers
12 if (n == 2 || n == 3) return true;
13 if (!(n & 1) || n == 1) return false;
14 ll s = __builtin_ctz(n - 1);
15 ll d = (n - 1) >> s;
16 __int128 mod = n;
17 for (__int128 a : small_primes) {
18     if (a >= mod) break;
19     a = pow_mod(a, d, mod);
20     if (a == 1 || a == mod - 1) continue;
21     for (ll r = 1; r < s; ++r) {
22         a = a * a % mod;
23         if (a == 1) return false;
24         if (a == mod - 1) break;
25     }
26     if (a != mod - 1) return false;
27 }
28 return true;
29}
30ll sqp1(ll x, ll n){
31    return ((__int128)x*x+1)%n;
32};
33ll pollard_rho(ll n){
34    while(true){
35        ll lv = rand()%n;
36        ll v = sqp1(lv, n);
37        int tar = 1;
38        for(int i=1; ; ++i){
39            ll g = __gcd(abs(v-lv), n);
40            if(g == n){
41                break;
42            } else if(g != 1){
43                return g;
44            }
45            if(i == tar){
46                lv = v;
47                tar <= 1;
48            }
49            v = sqp1(v, n);
50        }
51    }
52}
53void prime_factor(ll n, map<ll, int> &res){
54    while(!(n&1)){
55        ++res[2];
56        n >>=1;
57    }
58    for(int i=3; n>1 && i<=1000; i += 2){
59        while(!(n%i)){
#180
#754
#457
#695
#852
#475
#475
#850
#047

```

Combinatorics Cheat Sheet

Useful formulas

$\binom{n}{k} = \frac{n!}{k!(n-k)!}$ — number of ways to choose k objects out of n
 $\binom{n+k-1}{k-1}$ — number of ways to choose k objects out of n with repetitions

$[n]_m$ — Stirling numbers of the first kind; number of permutations of n elements with k cycles

$$[n+1]_m = n[n]_m + [n]_{m-1}$$

$$(x)_n = x(x-1)\dots x - n + 1 = \sum_{k=0}^n (-1)^{n-k} [n]_k x^k$$

$\{\cdot\}_m$ — Stirling numbers of the second kind; number of partitions of set $1, \dots, n$ into k disjoint subsets.

$$\{\cdot\}_m^{n+1} = k \{\cdot\}_k^n + \{\cdot\}_{k-1}^n$$

$$\sum_{k=0}^n \{\cdot\}_k(x)_k = x^n$$

$C_n = \frac{1}{n+1} \binom{2n}{n}$ — Catalan numbers

$$C(x) = \frac{1-\sqrt{1-4x}}{2x}$$

Binomial transform

If $a_n = \sum_{k=0}^n \binom{n}{k} b_k$, then $b_n = \sum_{k=0}^n (-1)^{n-k} \binom{n}{k} a_k$

- $a = (1, x, x^2, \dots)$, $b = (1, (x+1), (x+1)^2, \dots)$
- $a_i = i^k, b_i = \{\cdot\}_i^k i!$

Burnside's lemma

Let G be a group of *action* on set X (Ex.: cyclic shifts of array, rotations and symmetries of $n \times n$ matrix, ...)

Call two objects x and y *equivalent* if there is an action f that transforms x to y : $f(x) = y$.

The number of equivalence classes then can be calculated as follows: $C = \frac{1}{|G|} \sum_{f \in G} |X^f|$, where X^f

is the set of *fixed points* of f : $X^f = \{x | f(x) = x\}$

Generating functions

Ordinary generating function (o.g.f.) for sequence $a_0, a_1, \dots, a_n, \dots$ is $A(x) = \sum_{n=0}^{\infty} a_n x^n$

Exponential generating function (e.g.f.) for sequence $a_0, a_1, \dots, a_n, \dots$ is $A(x) = \sum_{n=0}^{\infty} a_n \frac{x^n}{n!}$

$$B(x) = A'(x), b_{n-1} = n \cdot a_n$$

$$c_n = \sum_{k=0}^n a_k b_{n-k} \text{ (o.g.f. convolution)}$$

$$c_n = \sum_{k=0}^n \binom{n}{k} a_k b_{n-k} \text{ (e.g.f. convolution, compute with FFT using } \widetilde{a_n} = \frac{a_n}{n!})$$

General linear recurrences

If $a_n = \sum_{k=1}^n b_k a_{n-k}$, then $A(x) = \frac{a_0}{1-B(x)}$. We also can compute all a_n with Divide-and-Conquer algorithm in $O(n \log^2 n)$.

Inverse polynomial modulo x^l

Given $A(x)$, find $B(x)$ such that $A(x)B(x) = 1 + x^l \cdot Q(x)$ for some $Q(x)$

1. Start with $B_0(x) = \frac{1}{a_0}$
2. Double the length of $B(x)$:

$$B_{k+1}(x) = (-B_k(x)^2 A(x) + 2B_k(x)) \bmod x^{2^{k+1}}$$

Fast subset convolution

Given array a_i of size 2^k , calculate $b_i = \sum_{j \& i = i} b_j$

```
for b = 0..k-1
  for i = 0..2^k-1
    if (i & (1 << b)) != 0:
      a[i + (1 << b)] += a[i]
```

Hadamard transform

Treat array a of size 2^k as k -dimensional array of size $2 \times 2 \times \dots \times 2$, calculate FFT of that array:

```
for b = 0..k-1
  for i = 0..2^k-1
    if (i & (1 << b)) != 0:
      u = a[i], v = a[i + (1 << b)]
      a[i] = u + v
      a[i + (1 << b)] = u - v
```