



UNIVERSITA' POLITECNICA DELLE MARCHE

ENVIRONMENTAL ENGINEERING

Hydraulic engineering and renewable energy

WEC PROJECT

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Submitted to:

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1. Location selection

To figure out how much energy offshore wave energy converters (WECs) can generate each year, we picked two spots using the Copernicus platform. Copernicus is a website where you can get free info about Earth stuff like weather, oceans, and more. We're mainly interested in the marine part of Copernicus (CMEMS), which gives trustworthy info about the oceans worldwide.



Products 277

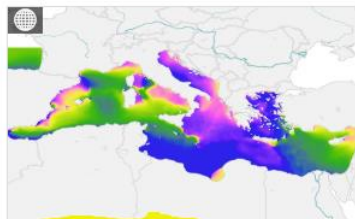
MOST POPULAR



Significant Satellite...

RT_014_001

Instantaneous



Mediterranean Sea Waves Reanalysis

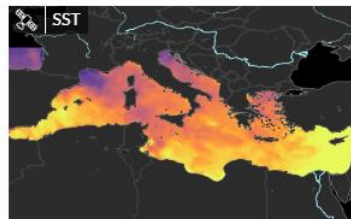
MEDSEA_MULTYEAR_WAV_006_012

Models

Med Sea, 0.042° × 0.042°

1 Jan 1993 to 1 Mar 2024, hourly, multi...

Velocity, wave



Mediterranean Sea High Resolution and Ultra High...

SST_MED_SST_L4_NRT_OBSERVA... 010_004

Satellite (L4)

Med Sea, 0.01° × 0.01°

1 Jan 2008 to 24 Mar 2024, daily

Temperature



Global Ocean Colour (Copernicus-GlobColour), Bio-...

OCEANCOLOUR_GLO_BGC_L3_M...009_

Satellite (L3)

Global, 4 × 4 km

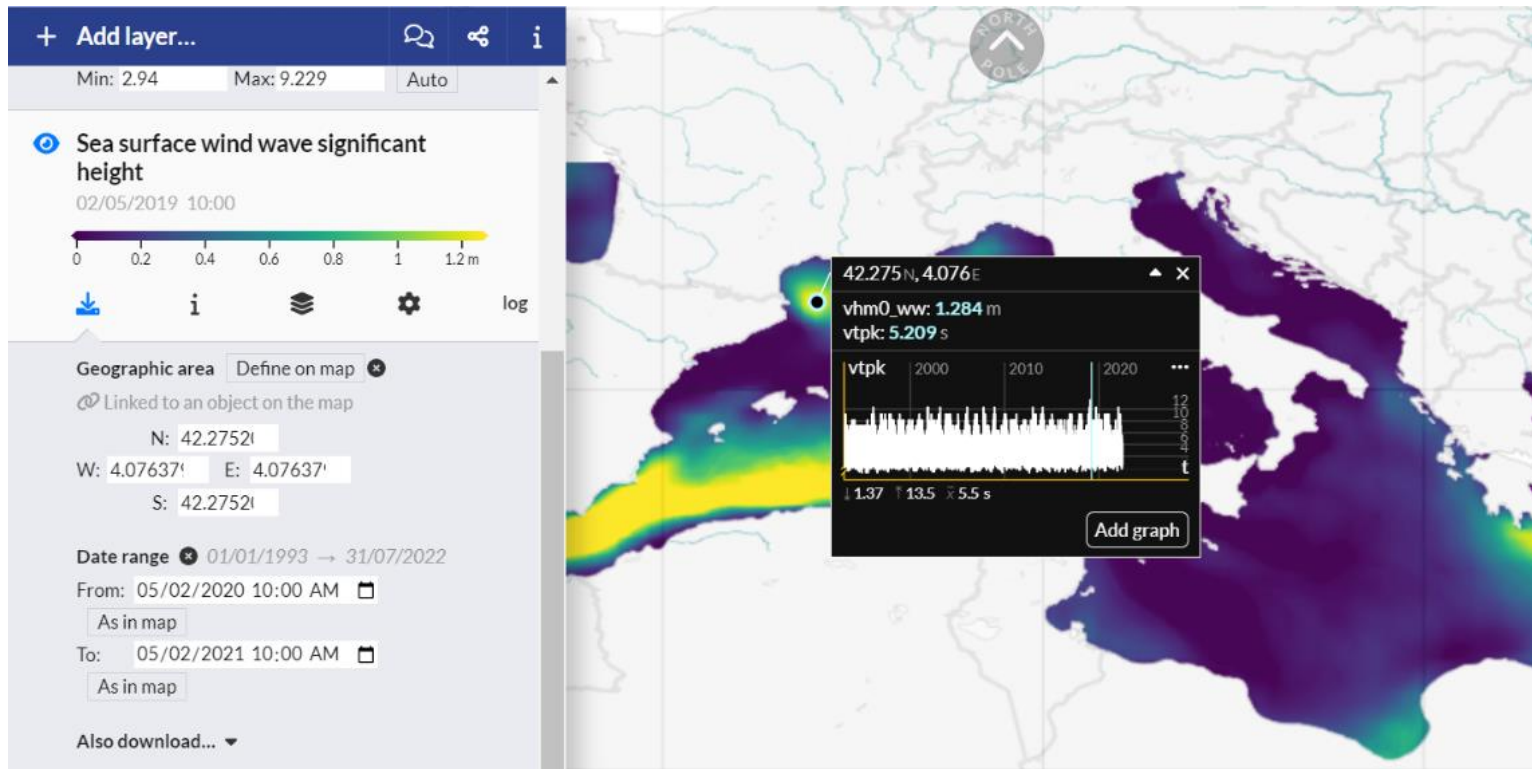
4 Sep 1997 to 15 Mar 2024, daily

Optics, plankton

In this project we selected 2 different location (1 for each student) were selected to compare the results and select which will result the best node. They are showed in the following pictures/figures:

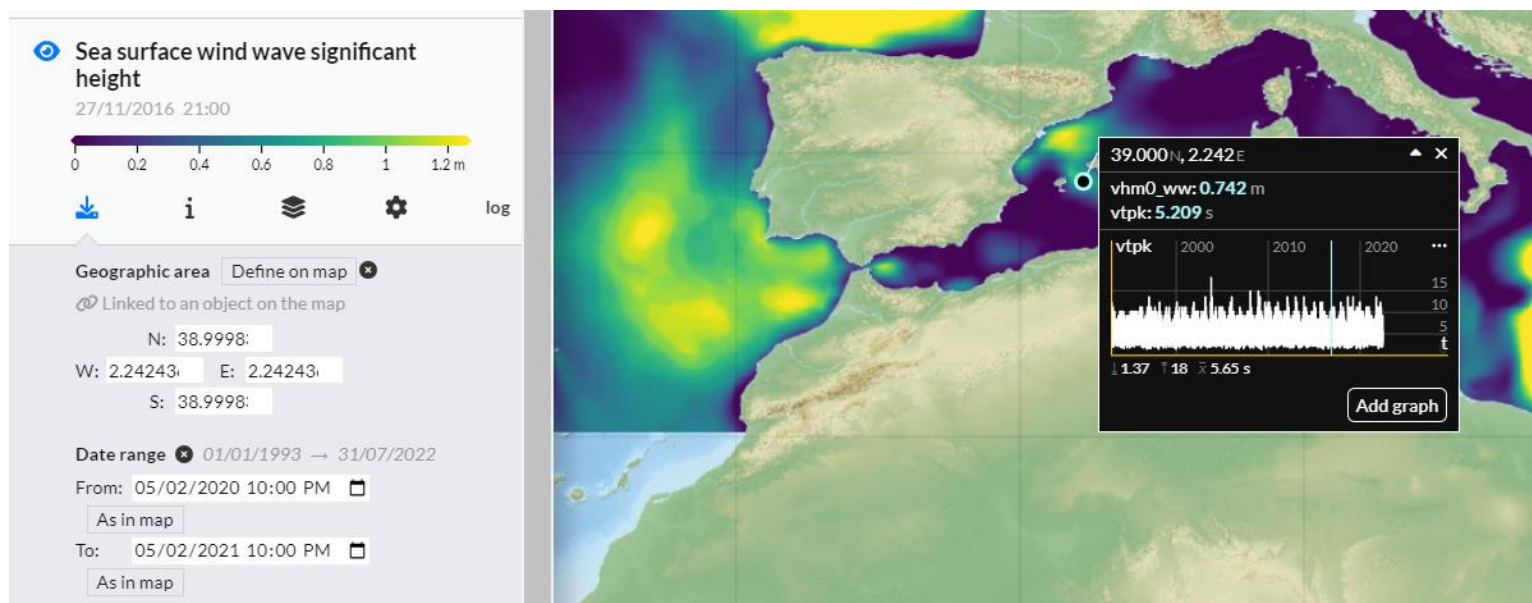
LOCATION 1:

Student: Passon Andar



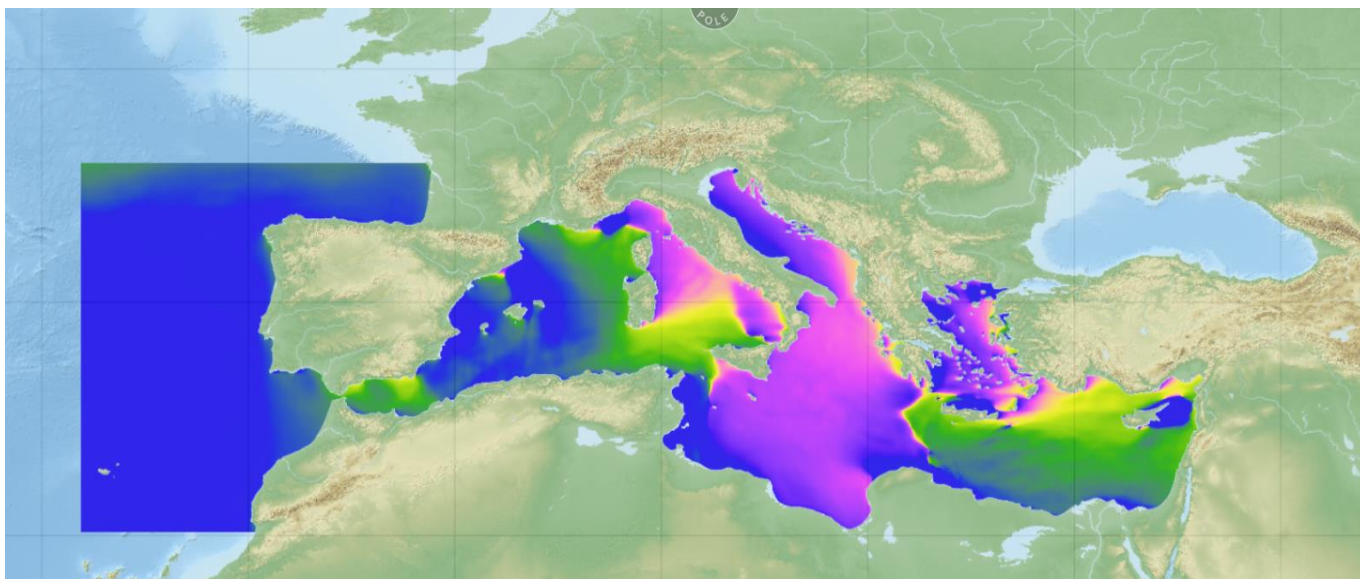
LOCATION 2:

Student: Qudratullah Ramzi



1. DOWNLOAD DATA OF THE SEA-STATE FROM THE COPERNICUS PLATFORM: SIGNIFICANT HEIGHT AND PEAK PERIOD

Available Data were downloaded on the Copernicus Marine Data Store, from the product “**Mediterranean Sea Waves Reanalysis**” considering “Sea surface wave significant height” and the “Sea surface wave period at variance spectral density maximum” of the sea-state in the 2 corresponding nodes in the reference period (1 year): **from Feb 5th 2020 to Feb 5th 2021.**



Dataset

Product identifier MEDSEA_MULTIYEAR_WAV_006_012
Product name Mediterranean Sea Waves Reanalysis
Dataset *Please choose one of the datasets in this product:*
med-hcmr-wav-rean-h

Variables + Add all Clear all

- | | |
|---|--|
| <input checked="" type="checkbox"/> Sea surface wave significant height <i>VHM0</i> [m] | <input type="checkbox"/> Sea surface wave stokes drift y velocity <i>VSDY</i> [m/s] |
| <input type="checkbox"/> Sea surface primary swell wave significant height <i>VHM0_SW1</i> [m] | <input type="checkbox"/> Sea surface primary swell wave mean period <i>VTM01_SW1</i> [s] |
| <input type="checkbox"/> Sea surface secondary swell wave significant height <i>VHM0_SW2</i> [m] | <input type="checkbox"/> Sea surface secondary swell wave mean period <i>VTM01_SW2</i> [s] |
| <input type="checkbox"/> Sea surface wind wave significant height <i>VHM0_WW</i> [m] | <input type="checkbox"/> Sea surface wind wave mean period <i>VTM01_WW</i> [s] |
| <input type="checkbox"/> Sea surface wave from direction <i>VMDR</i> [°] | <input type="checkbox"/> Sea surface wave mean period from variance spectral density second frequency moment <i>VTM02</i> [s] |
| <input type="checkbox"/> Sea surface primary swell wave from direction <i>VMDR_SW1</i> [°] | <input type="checkbox"/> Sea surface wave mean period from variance spectral density inverse frequency moment <i>VTM10</i> [s] |
| <input type="checkbox"/> Sea surface secondary swell wave from direction <i>VMDR_SW2</i> [°] | <input checked="" type="checkbox"/> Sea surface wave period at variance spectral density maximum <i>VTPK</i> [s] |
| <input type="checkbox"/> Sea surface wind wave from direction <i>VMDR_WW</i> [°] | |
| <input type="checkbox"/> Sea surface wave from direction at variance spectral density maximum <i>VPED</i> [°] | |
| <input type="checkbox"/> Sea surface wave stokes drift x velocity <i>VSDX</i> [m/s] | |

2. BUILD THE SCATTER MATRIX (OCCURRENCE PROBABILITY AS FUNCTION OF H_s AND T_p), USING H_s INTERVALS OF 0.2m AND T_p INTERVALS 0.5s

Inspect the content of the netCDF dataset

The downloaded data were opened in Matlab. The data are in a specific, standard format called **netCDF**, as shown by the extension (.nc) . We needed a bit of post-processing to extract the variables from the file. To investigate the structure of this dataset and check the variables contained in it, the function **ncdisp** was used.

```
subset:date      = "2024-03-24T13:26:25.624Z"
Dimensions:
  latitude = 1
  longitude = 1
  time = 8761
Variables:
  VHM0_WW
    Size: 1x1x8761
    Dimensions: longitude,latitude,time
    Datatype: single
    Attributes:
      units = "m"
      _FillValue = NaN
      standard_name = "sea_surface_wind_wave_significant_height"
      long_name = "Spectral significant wind wave height"
  VTPK
    Size: 1x1x8761
    Dimensions: longitude,latitude,time
    Datatype: single
    Attributes:
      units = "s"
      _FillValue = NaN
      standard_name = "sea_surface_wave_period_at_variance_spectral_density_maximum"
      long_name = "Wave period at spectral peak / peak period (Tp)"
  latitude
    Size: 1x1
    Dimensions: latitude
    Datatype: single
    Attributes:
```

As observed, downloading data for a single location from Copernicus platform, we have the dimensions: 1 point in longitude and 1 point in latitude, and 8761 points in time (representing the hours of data for a single node in a particular year)

Extract the variables of the netCDF dataset and plot graph of the significant wave height

We can extract the variables using the **ncread** function.

The variables in the file are as follows:

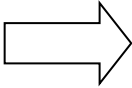
- **VTPK**: Peak wave period (**T_p**) with dimensions 1x1x8761
- **VHM0**: Significant wave height (**H_s**) with dimensions 1x1x8761.
- **Longitude** and **Latitude** variables containing the coordinates of the downloaded node (single values, as we downloaded a single node).
- **Time**: time vector indicating the hours each specific data corresponds to. Time is given in seconds, referred to as Posixtime in Matlab.

Since the time variable is expressed in seconds since January 1, 1970, it was converted into dates using the `datetime` function.

| Workspace | | |
|-----------|----------------|----------|
| Name | Value | Size |
| Hm0 | 1x1x8761 do... | 1x1x8761 |
| Tp | 1x1x8761 do... | 1x1x8761 |
| lat | 42.3125 | 1x1 |
| long | 4.0833 | 1x1 |
| time | 8761x1 double | 8761x1 |

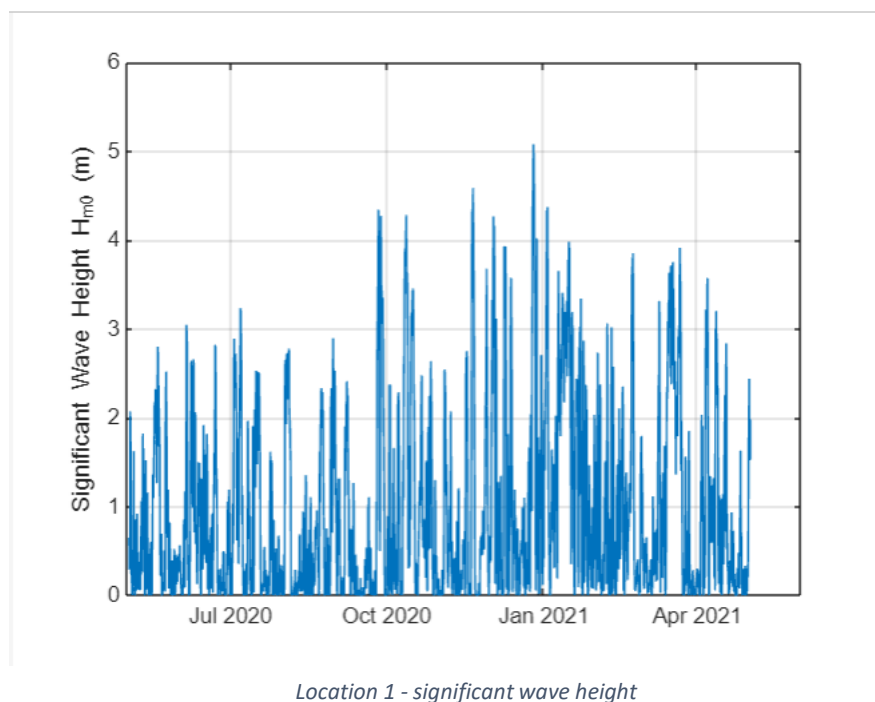
Now, it is possible to plot the variables using the `plot` function. However, before proceeding, it's important to note that the data extracted from the NetCDF file are arrays (3D data), while the plot function handles vectors or matrices. To address this, we converted Hm0 and Tp its structure from 1x1x8761 into a vector 8761x1 using the `squeeze` function.

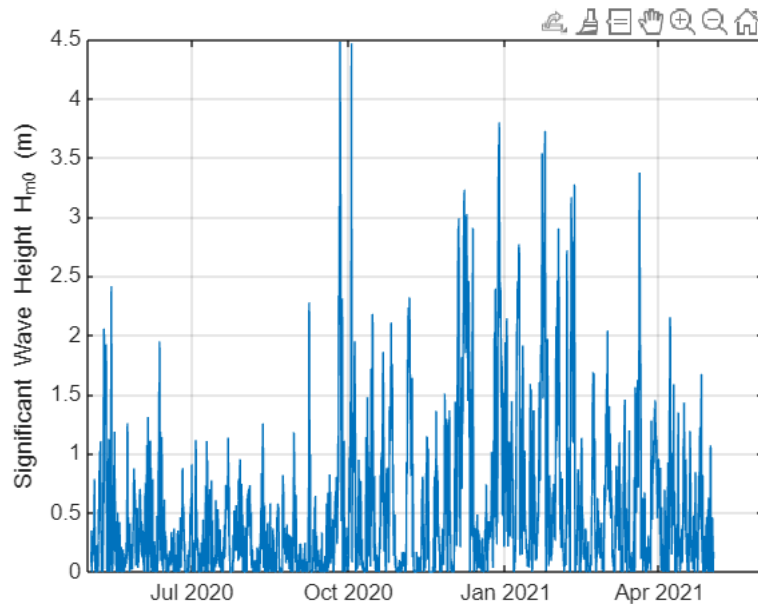
| Workspace | | |
|-----------|----------------|----------|
| Name | Value | Size |
| Hm0 | 1x1x8761 do... | 1x1x8761 |
| Tp | 1x1x8761 do... | 1x1x8761 |
| lat | 42.3125 | 1x1 |
| long | 4.0833 | 1x1 |
| time | 8761x1 double | 8761x1 |



| Workspace | | |
|-----------|---------------|--------|
| Name | Value | Size |
| Hm0 | 8761x1 double | 8761x1 |
| Tp | 8761x1 double | 8761x1 |

The plot illustrates a time series of the significant wave height Hm0 at the selected point over the reference time period from Feb 5th 2020 to Feb 5th 2021.





Location 2 - significant wave height

Scatter Matrix

- Input data:

Hm0 max

Tp max

- To build the scatter matrix we need to define a range for Hm0 and Tp considering their max values:

Hedges = 0:0.2:Hm0 max

Tedges = 1:0.5:Tp max

doing that we are creating a vector that goes:

- from 0 to Hm0 max with intervals of 0.2m of discretization for the height (Hs)
- from 1 to Tp max with interval of 0.5 s of discretization for the time (Tp)

```
[N,Hedges,Tedges] = histcounts2(Hm0,Tp,Hedges,Tedges);
```

The function histcounts2 divides a dataset into beans, in our case is defined by the vectors Hedges and Tedges.

N gives a description of how many sea states fall between the given intervals of Hm0 and Tp. In particular N is the matrix composed by the number of hours in which a given sea state occur in one year. To plot it, the command meshgrid and function pcolor was used, it returns 2D coordinates based on the coordinates contained in vectors Tedges and Hedges.

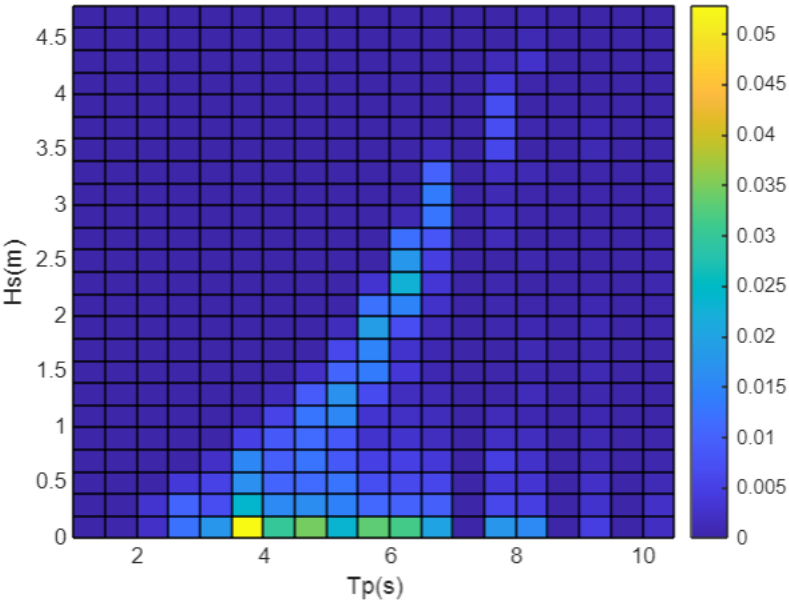
N ×

25x20 double

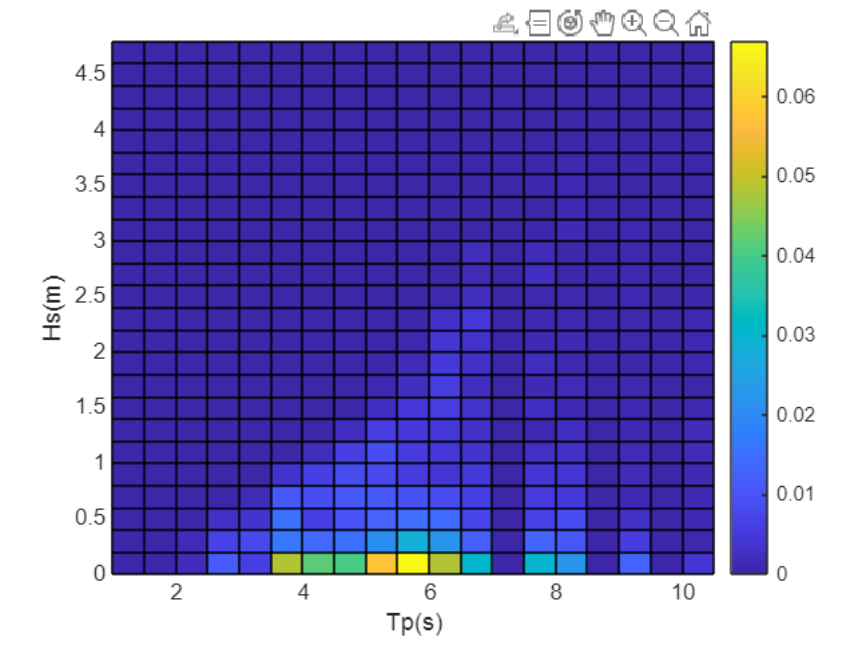
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | |
|----|---|---|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|--|
| 1 | 0 | 3 | 21 | 108 | 155 | 463 | 263 | 303 | 205 | 290 | 275 | 174 | |
| 2 | 0 | 0 | 26 | 92 | 60 | 208 | 136 | 142 | 125 | 95 | 87 | 85 | |
| 3 | 0 | 0 | 0 | 33 | 46 | 145 | 91 | 99 | 109 | 62 | 56 | 52 | |
| 4 | 0 | 0 | 0 | 0 | 20 | 135 | 83 | 109 | 76 | 43 | 43 | 34 | |
| 5 | 0 | 0 | 0 | 0 | 0 | 42 | 77 | 98 | 77 | 25 | 24 | 16 | |
| 6 | 0 | 0 | 0 | 0 | 0 | 7 | 48 | 111 | 134 | 27 | 19 | 13 | |
| 7 | 0 | 0 | 0 | 0 | 0 | 0 | 13 | 79 | 148 | 57 | 16 | 10 | |
| 8 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 21 | 91 | 119 | 31 | 6 | |
| 9 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 54 | 129 | 25 | 6 | |
| 10 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 13 | 165 | 61 | 12 | |
| 11 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 105 | 128 | 23 | |
| 12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 26 | 199 | 29 | |
| 13 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 156 | 40 | |
| 14 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 104 | 72 | |
| 15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 9 | 111 | |

N matrix

plotting the data we get the **scatter matrix** for the first location:



Location 1



Location 2

IDENTIFY THE MOST FREQUENT SEA STATE RANGE FOR THE REFERENCE PERIOD.

In the scatter matrix we have the X-axis corresponding to intervals of peak periods (T_p) and the Y-axis corresponding to intervals of the significant wave height (H_s), so the ranges that we have defined before using Tedges and Hedges. The intensity of the colours in each square is related to the probability (p_i) that a given sea state, so a couple of significant wave height and peak periods, falls between 2 given ranges of T_p and H_s . **The yellow square has the highest probability of occurrence.**

For our 2 locations we identify the most frequent sea-state in the reference period (1 year):

1. Location 1:

- $T_p = (3.5; 4)$ s
- $H_s = (0.0; 0.2)$ m

2. Location 2:

- $T_p = (4.5; 6)$ s
- $H_s = (0.0; 0.2)$ m

As supposed the 2 locations of Mediterranean Sea are characterized by the same most frequent sea-state with much shorter peak periods and significant wave height respect to the Ocean.

3. BUILT THE JONSWAP SPECTRUM WITH THE MID VALUES (H_s AND T_p) OF THE MOST FREQUENT ENERGETIC SEA STATE RANGE AND THE CORRESPONDING IRREGULAR WAVE

Jonswap Spectrum

The Jonswap spectrum (Joint North Sea Wave Project) is a mathematical model used to describe the properties of sea waves. **It describes how energy is distributed on waves of different frequencies.**

In order to build the Jonswap Spectrum, **it is necessary to find the mid values of H_s and T_p :**

1. Location 1:

- $T_p = 3.75$ s

- $H_s = 0.2$ m

2. Location 2:

- $T_p = 5.25$ s

- $H_s = 0.2$ m

The JONSWAP spectrum is described by the formula:

$$S(f) = \alpha \frac{5}{16} \frac{H_s^2}{T_p^4} \frac{1}{f^5} e^{-\frac{5}{4} \frac{1}{(T_p f)^4}} \gamma e^{\frac{(f T_p - 1)^2}{2\sigma^2}}$$

where α is the coefficient related to wind and fetch characteristics and γ is the frequency spreading coefficient:

In general, for Mediterranean Sea:

$$\alpha = 0.076 \left(\frac{U_{10}^2}{Fg} \right)^{0.22}$$

where U_{10} the wind speed at a height of 10 m and F the distance from a lee shore, called the fetch, or the distance over which the wind blows with constant velocity.

Used parameters provided by literature valid for Mediterranean Sea:

$\sigma = 0.07$ if $f < 1/T_p$ and $\sigma = 0.09$ if $f > 1/T_p$ and $\gamma = 3.3$

Irregular wave

The irregular wave corresponding to the spectrum can be obtained as the sum of the different frequencies contributions:

$$\eta(x, t) = \sum_i a_i \sin(k_i x - f_i t - \phi_i)$$

Where:

- $a_i = \sqrt{2 S(f_i) \Delta f}$;
- k_i is the wave number (obtained with the dispersion relation considering a time averaged water depth of 21 m)
- ϕ_i is a random difference in phase.

With the **dispersion relation**, you can get the value of L (wavelength), k (wave number), σ (wave angular frequency), using different solutions of the dispersion equation.

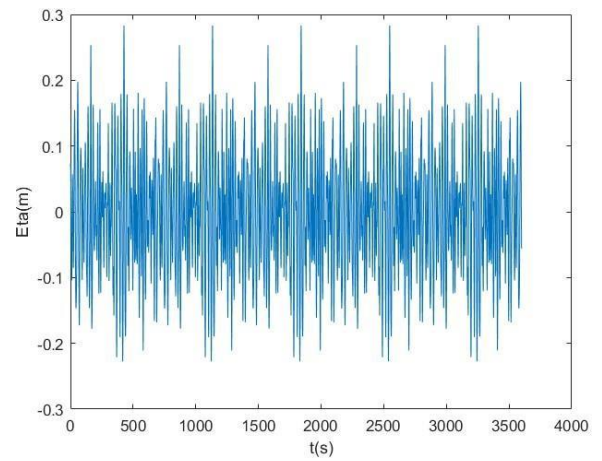
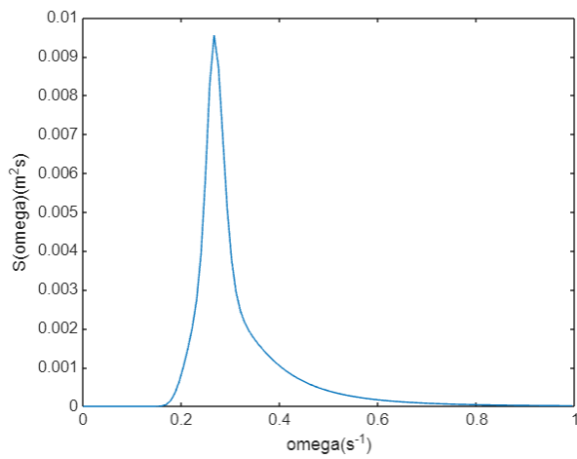
The solution process requires some kind of iterative approach (trial & error) since there are unknown on both sides of the equation. We solved it by using Eckhart's equations.

Inputs:

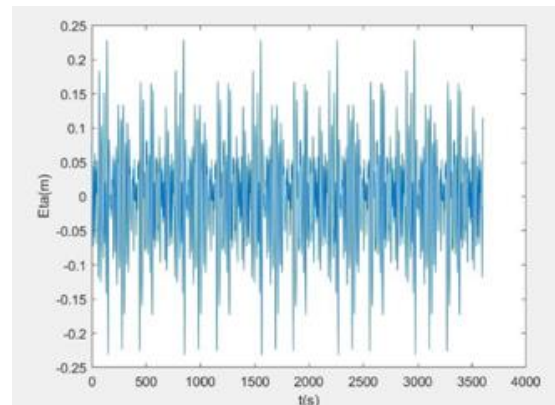
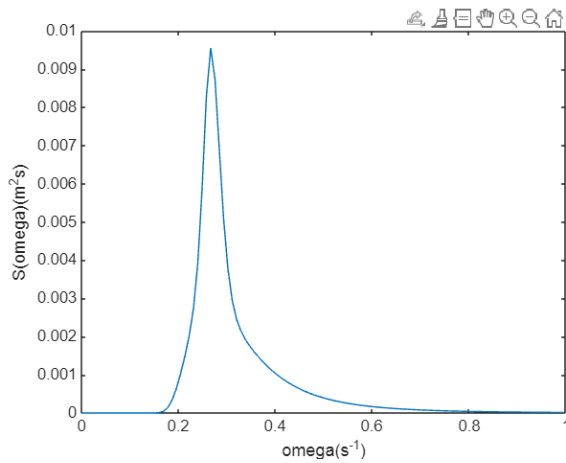
- h = deep water (m)

- T_p = wave peak period (s)

Jonswap spectrum and the corresponding irregular wave for the 3 different locations are reported in the figures below:



Location 1 - Jonswap spectrum and corresponding irregular wave



Location 2- Jonswap spectrum and corresponding irregular wave

5. COMPARE THE DIFFERENT JONSWAP SPECTRA OBTAINED BY THE DIFFERENT MEMBERS OF THE TEAM

$S(f)$ is a measure of the amount of energy contained in the wave per unit frequency interval. It describes how the energy of the wave is distributed over different frequencies.

The spectrum for the first 2 locations, having the same T_p in the most frequent energetic sea-state and therefore the same wave frequency ($1/T_p$), has the same value of the Spectral Peak. It means that they have the same energy at a given frequency; indeed, being both locations situated in relatively calm seas (Ligurian and Tyrrhenian), confined and more naturally constrained respect to the ocean are characterized by smaller wave height and few energy.

In fact, if we check the spectrum for the third location is characterized by higher T_p (i.e. lower frequency at which we have Spectrum peak) and higher value of $S(f)$ for this frequency.

The ocean is characterized by higher wave heights and different winds that can affect the energy production of the WEC.

An important factor to take into account is the difference in the wave generation provided by the wind and in particular the size and the development of the "fetch", that is a region of the sea on which the wind blows without obstacles, on whose length depends the size of the wave generated.

In the ocean we have different winds generating important fetch, so a lot of distance useful to increase the height of the wave; instead in Italian seas it can be affected by the natural restraint that influence the blowing of the winds and affect the wave propagation and development towards the shore.

This can be an important element to consider in the design phase choosing the proper location to optimize the total energy produced by the waves.

6. EVALUATE THE ANNUAL ENERGY PRODUCTION

In order to calculate the annual energy production (AEP) for the reference Wave Energy Converter we have to apply the formula:

$$AEP = \sum_i p_i P_{WEC,i} T_{year}$$

Where

- p_i : occurrence probability, as annual time fraction of the occurrence of each sea state
- $P_{WEC,i}$: available power for the i -th sea state, with occurrence probability p_i , estimated as:

$$P_{wave-i} \simeq 0.4 H_{s-i}^2 T_{p-i} \text{ or } P_{wave-i} \simeq \frac{1}{2} H_{s-i}^2 T_{e-i}$$

- T_{year} : reference time (one year in hours)

The annual variation in sea states is represented by the scatter matrix, represented in matlab by the matrix N ; this matrix that we already created in chapter 3 has values that represents how many hours a specific sea state occurred in one year. From the N matrix, it is possible to create the **probability matrix (p_i)**, by dividing each value of N by the hours in one year (in our case 8761hours).

| N × | | | | | | | | | | | | |
|--------------|---|---|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 25x20 double | | | | | | | | | | | | |
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 0 | 3 | 21 | 108 | 155 | 463 | 263 | 303 | 205 | 290 | 275 | 174 |
| 2 | 0 | 0 | 26 | 92 | 60 | 208 | 136 | 142 | 125 | 95 | 87 | 85 |
| 3 | 0 | 0 | 0 | 33 | 46 | 145 | 91 | 99 | 109 | 62 | 56 | 52 |
| 4 | 0 | 0 | 0 | 0 | 20 | 135 | 83 | 109 | 76 | 43 | 43 | 34 |
| 5 | 0 | 0 | 0 | 0 | 0 | 42 | 77 | 98 | 77 | 25 | 24 | 16 |
| 6 | 0 | 0 | 0 | 0 | 0 | 7 | 48 | 111 | 134 | 27 | 19 | 13 |
| 7 | 0 | 0 | 0 | 0 | 0 | 0 | 13 | 79 | 148 | 57 | 16 | 10 |
| 8 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 21 | 91 | 119 | 31 | 6 |
| 9 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 54 | 129 | 25 | 6 |
| 10 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 13 | 165 | 61 | 12 |
| 11 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 105 | 128 | 23 |
| 12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 26 | 199 | 29 |
| 13 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 156 | 40 |
| 14 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 104 | 72 |
| 15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 9 | 111 |

N matrix

| probability_matrix × | | | | | | | | | | | | |
|----------------------|---|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 22x20 double | | | | | | | | | | | | |
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 1 | 0 | 0.0003 | 0.0024 | 0.0123 | 0.0177 | 0.0528 | 0.0300 | 0.0346 | 0.0234 | 0.0331 | 0.0314 | 0.0199 |
| 2 | 0 | 0 | 0.0030 | 0.0105 | 0.0068 | 0.0237 | 0.0155 | 0.0162 | 0.0143 | 0.0108 | 0.0099 | 0.0097 |
| 3 | 0 | 0 | 0 | 0.0038 | 0.0053 | 0.0166 | 0.0104 | 0.0113 | 0.0124 | 0.0071 | 0.0064 | 0.0059 |
| 4 | 0 | 0 | 0 | 0 | 0.0023 | 0.0154 | 0.0095 | 0.0124 | 0.0087 | 0.0049 | 0.0049 | 0.0039 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0.0048 | 0.0088 | 0.0112 | 0.0088 | 0.0029 | 0.0027 | 0.0018 |
| 6 | 0 | 0 | 0 | 0 | 0 | 0.0008 | 0.0055 | 0.0127 | 0.0153 | 0.0031 | 0.0022 | 0.0015 |
| 7 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0015 | 0.0090 | 0.0169 | 0.0065 | 0.0018 | 0.0011 |
| 8 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0024 | 0.0104 | 0.0136 | 0.0035 | 0.0007 |
| 9 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0062 | 0.0147 | 0.0029 | 0.0007 |
| 10 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0015 | 0.0188 | 0.0070 | 0.0014 |
| 11 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0120 | 0.0146 | 0.0026 |
| 12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0030 | 0.0227 | 0.0033 |
| 13 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0178 | 0.0046 |
| 14 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0119 | 0.0082 |
| 15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0010 | 0.0127 |

Probability matrix (pi) = N/8761

$P_{WEC,i}$ in our case is represented by the given **Power Matrix**, it collects the power production of the WEC for each sea-state range

| power_matrix × | | | | | | | | | | | | | |
|----------------|---|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--|
| 22x20 double | | | | | | | | | | | | | |
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.1000 | 0.0800 | 0.1200 | |
| 4 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0600 | 0.1100 | 0.1600 | 0.2100 | 0.3200 | |
| 5 | 0 | 0 | 0 | 0 | 0 | 0.0600 | 0.0800 | 0.1200 | 0.1500 | 0.2200 | 0.3500 | 0.4000 | |
| 6 | 0 | 0 | 0 | 0.0700 | 0.0500 | 0.0600 | 0.1300 | 0.1800 | 0.2100 | 0.3100 | 0.4700 | 1.0100 | |
| 7 | 0 | 0 | 0.0100 | 0.1100 | 0.1600 | 0.2100 | 0.2300 | 0.2700 | 0.2900 | 0.4100 | 0.6300 | 0.9000 | |
| 8 | 0 | 0.1200 | 0.0900 | 0.1700 | 0.3100 | 0.2700 | 0.3100 | 0.3300 | 0.3700 | 0.6300 | 0.8100 | 1.4200 | |
| 9 | 0 | 0.1700 | 0.2100 | 0.2300 | 0.3100 | 0.3200 | 0.3300 | 0.3500 | 0.4300 | 0.7200 | 1.3700 | 1.3900 | |
| 10 | 0 | 0.2300 | 0.2500 | 0.2900 | 0.3100 | 0.3400 | 0.3300 | 0.4100 | 0.5700 | 1.0000 | 1.4100 | 1.4600 | |
| 11 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1.5200 | 1.5700 | |
| 12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1.7800 | 1.8200 | |
| 13 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 2.2500 | 2.4500 | |
| 14 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 2.8100 | 3.0100 | |
| 15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 3.2700 | 3.4400 | |

Power Matrix

In order to multiply scalarly each value between the **probability matrix (pi)** and the **Power matrix (Pwec)** is fundamental to have the same resolution, so we arranged the size of the 2 to allow this product.

To do this we extended the P_{WEC} dimensions adding zeros in the ranges needed, considering as a precaution that in these conditions the device does not produce energy.

| ppm × | | | | | | | | | | | | | |
|--------------|---|---|---|---|---|--------|--------|--------|--------|--------|--------|--------|---|
| 22x20 double | | | | | | | | | | | | | |
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 1 |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0007 | 0.0005 | 0.0007 | |
| 4 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0007 | 0.0010 | 0.0008 | 0.0010 | 0.0012 | |
| 5 | 0 | 0 | 0 | 0 | 0 | 0.0003 | 0.0007 | 0.0013 | 0.0013 | 0.0006 | 0.0010 | 0.0007 | |
| 6 | 0 | 0 | 0 | 0 | 0 | 0.0000 | 0.0007 | 0.0023 | 0.0032 | 0.0010 | 0.0010 | 0.0015 | |
| 7 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0003 | 0.0024 | 0.0049 | 0.0027 | 0.0012 | 0.0010 | |
| 8 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0008 | 0.0038 | 0.0086 | 0.0029 | 0.0010 | |
| 9 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0027 | 0.0106 | 0.0039 | 0.0010 | |
| 10 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0008 | 0.0188 | 0.0098 | 0.0020 | |
| 11 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0222 | 0.0041 | |
| 12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0404 | 0.0060 | |
| 13 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0401 | 0.0112 | |
| 14 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0334 | 0.0247 | |
| 15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0.0034 | 0.0436 | |

Produced power matrix

7. COMPARE THE ANNUAL ENERGY PRODUCTION IN DIFFERENT LOCATION

To obtain the final value of energy produced by each WEC we have to multiply the power produced by the hour in the year (**Tyear**):

1. Location 1: Passon Andar

AEP = 3400 kWh

2. Location 2: Qudratullah Ramzi

AEP = 2012 KWh

As previously hypothesized the WEC located in the ocean (Location 1) higher amount of energy than the second location in the considered reference period.

Matlab Codes:

```
ncdisp("med-hcmr-wav-rean-h_Passon1711286785622.nc")
Source:
    /MATLAB Drive/med-hcmr-wav-rean-h_Passon1711286785622.nc
Format:
    netcdf4
Global Attributes:
    Conventions      = "CF-1.11"
    title            = "Wave fields (2D) - Hourly Instantaneous"
    institution      = "Hellenic Centre for Marine Research (HCMR)- Athens,Greece"
    producer         = "CMEMS-MED Monitoring and Forecasting Centre"
    source           = "MEDWAM3"
    credit           = "Copernicus Marine Environment Monitoring Service (CMEMS)"
    contact          = "servicedesk.cmems@mercator-ocean.eu"
    references       = "Please check in CMEMS catalogue the INFO section for product
MEDSEA_MULTIYEAR_WAV_006_012 - http://marine.copernicus.eu"
    comment          = "Please check in CMEMS catalogue the INFO section for product
MEDSEA_MULTIYEAR_WAV_006_012 - http://marine.copernicus.eu"
    subset:source    = "ARCO data downloaded from the Marine Data Store using the MyOcean Data
Portal"
    subset:productId = "MEDSEA_MULTIYEAR_WAV_006_012"
    subset:datasetId = "med-hcmr-wav-rean-h_202105"
    subset:date      = "2024-03-24T13:26:25.624Z"
Dimensions:
    latitude = 1
    longitude = 1
    time      = 8761
Variables:
    VHM0_WW
        Size:      1x1x8761
        Dimensions: longitude,latitude,time
        Datatype:  single
        Attributes:
            units      = "m"
            _FillValue = NaN
            standard_name = "sea_surface_wind_wave_significant_height"
            long_name  = "Spectral significant wind wave height"
    VTPK
        Size:      1x1x8761
        Dimensions: longitude,latitude,time
        Datatype:  single
        Attributes:
            units      = "s"
            _FillValue = NaN
            standard_name = "sea_surface_wave_period_at_variance_spectral_density_maximum"
            long_name  = "Wave period at spectral peak / peak period (Tp)"
    latitude
        Size:      1x1
        Dimensions: latitude
        Datatype:  single
        Attributes:
            standard_name = "latitude"
            long_name    = "Latitude"
            units        = "degrees_north"
            unit_long    = "Degrees North"
            axis         = "Y"
            valid_min    = 30.1875
            valid_max    = 45.9792
    longitude
        Size:      1x1
        Dimensions: longitude
        Datatype:  single
        Attributes:
            standard_name = "longitude"
```

```

                                long_name      = "Longitude"
                                units           = "degrees_east"
                                unit_long      = "Degrees East"
                                axis           = "X"

time
    Size:          8761x1
    Dimensions:    time
    Datatype:      double
    Attributes:
        standard_name = "time"
        long_name     = "Time"
        units         = "seconds since 1970-01-01 00:00:00"
        calendar      = "gregorian"
        axis          = "T"

lat = ncread('med-hcmr-wav-rean-h_Passon1711286785622.nc','latitude');
long = ncread('med-hcmr-wav-rean-h_Passon1711286785622.nc','longitude');
time = ncread('med-hcmr-wav-rean-h_Passon1711286785622.nc','time');
Hm0 = ncread('med-hcmr-wav-rean-h_Passon1711286785622.nc','VHM0_WW');
Tp = ncread('med-hcmr-wav-rean-h_Passon1711286785622.nc','VTPK');

date = datetime(time,'ConvertFrom','posixtime');
Hm0 = squeeze(Hm0);
Tp = squeeze(Tp);
plot(date,Hm0); grid on
ylabel('Significant Wave Height H_{m0} (m)');


maxHm0= max(Hm0);
maxTp = max(Tp);
Hedges = 0:.2:5.077;
Tedges = 1:.5:11.167;
[N,Hedges,Tedges] = histcounts2(Hm0,Tp,Hedges,Tedges);
[T,H] = meshgrid(Tedges(1:end-1),Hedges(1:end-1));
p = pcolor(T,H,N/numel(Hm0));
colorbar;
xlabel('Tp(s)')
ylabel('Hs(m)')


%sea_state_plots - jonswap spectrum
Hs=0.1;%m
Tp=3.75;%s
alpha=0.862; % ParunovEtAl_OE2011
omega_p = 1/Tp;
omega_max=1; %(qualitative threshold of gravity wave);
d_omega=(1/Tp)/30;
omega_vett=[0:d_omega:omega_max];
sigma = (omega_vett<=omega_p)*0.07+(omega_vett>omega_p)*0.09;
gamma = 3.3; % ParunovEtAl_OE2011
fac1=alpha*(5/16)*(Hs^2)/(Tp^4);
fac2=omega_vett.^-5;
fac3=exp(-(5/4)*(omega_vett*Tp).^-4);
Aa = exp(-((omega_vett*Tp-1)./(sigma*sqrt(2))).^2);
fac4 = gamma.^Aa;
S_vett = fac1.*fac2.*fac3.*fac4;
S_vett(1)=0;
plot(omega_vett,S_vett);
xlabel('omega(s^-1)')
ylabel('S(omega)(m^2s)')


h=21;%m
T=3.75;

```



```

x0 =0.0001;
Lr=0;
if sign(h) == -1
h = -h;
end
X=0;
t_vett=0:dt:60*60;

dt=0.1;
h=21;%m
T=3.75;
x0 =0.0001;
Lr=0;
if sign(h) == -1
h = -h;
end
X=0;
t_vett=0:dt:60*60;
Lr=0;
ke = sigma/(9.81*sqrt(tanh(h*(sigma/9.81))));
Le = (2*pi)/ke;
Ce = Le/T;
ne =0.5*(1+((2*ke*h)/sinh(2*ke*h)));
Cge = ne * Ce;
ee = (abs(Lr-Le)/abs(Lr))*100;
phi=2*pi*rand(1,numel(omega_vett));
for index=1:numel(omega_vett)
a(index)=sqrt(2*S_vett(index)*d_omega);
[L(index),k(index),sigma(index)]=disper(h,1/omega_vett(index));
eta(index,:)=a(index)*sin(k(index)*X-omega_vett(index)*t_vett - phi(index));
end

Lr=0;
ke = sigma/(9.81*sqrt(tanh(h*(sigma/9.81))));
Le = (2*pi)/ke;
Ce = Le/T;
ne =0.5*(1+((2*ke*h)/sinh(2*ke*h)));
Cge = ne * Ce;
ee = (abs(Lr-Le)/abs(Lr))*100;
phi=2*pi*rand(1,numel(omega_vett));
for index=1:numel(omega_vett)
a(index)=sqrt(2*S_vett(index)*d_omega);
eta(index,:)=a(index)*sin(k(index)*X-omega_vett(index)*t_vett - phi(index));
end
eta_seastate=sum(eta,1);
plot(t_vett,eta_seastate);
xlabel('t(s)')
ylabel('Eta(m)')

dt=0.1;
h=21;%m
T=3.75;
x0 =0.0001;
Lr=0;
if sign(h) == -1
h = -h;
end
X=0;
t_vett=0:dt:60*60;
[Lr,kr,sigma]=disper(h,T)
% ***** Solving dispersion equation, using Eckhart *****
Lr=0;

```

```

ke = sigma/(9.81*sqrt(tanh(h*(sigma/9.81))));
Le = (2*pi)/ke;
Ce = Le/T;
ne =0.5*(1+((2*ke*h)/sinh(2*ke*h)));
Cge = ne * Ce;
ee = (abs(Lr-Le)/abs(Lr))*100;
phi=2*pi*rand(1,numel(omega_vett));
for index=1:numel(omega_vett)
a(index)=sqrt(2*S_vett(index)*d_omega);
eta(index,:)=a(index)*sin(k(index)*X-omega_vett(index)*t_vett - phi(index));
end
eta_seastate=sum(eta,1);
plot(t_vett,eta_seastate);
xlabel('t(s)')
ylabel('Eta(m)')

```

```

power_matrix=readtable("power_matrix.xlsx")
power_matrix = removevars(power_matrix, ["Var1","Var2","Var3"]);
power_matrix(1:3,:) = [];
power_matrix=table2array(power_matrix)
power_matrix(isnan(power_matrix)) = 0
probability_matrix= N/8761
probability_matrix(end-2, :) = []; as needed
ppm = probability_matrix.*power_matrix
average_power=sum(ppm(:))
AEP = average_power*8761

```