Statistical comparison of various dayside magnetopause reconnection X-line prediction models

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Key Points:

10

11

- Compared four different reconnection line models.
- On average, the Maximum Bisection Field Model gives the best prediction of reconnection line location.
- The Maximum Exhaust Velocity model gives the worst prediction of the reconnection line location.

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Abstract

Reconnection at Earth's magnetopause drives magnetospheric convection and provides mass and energy input into the magnetosphere/ionosphere system thereby driving the coupling between solar wind and terrestrial magnetosphere. Despite its importance, the factors governing the location of dayside magnetopause reconnection are not well understood. Though a few models can predict X-line locations reasonably well, the underlying physics is still unresolved. In this study we present results from a comparative analysis of 274 magnetic reconnection events as observed by the Magnetospheric Multiscale (MMS) mission to determine what quantities affect the accuracy of such models and are most strongly associated with the occurrence of dayside magnetopause reconnection. We also attempt to determine under what upstream solar wind conditions each global X-line model becomes least reliable.

Plain Language Summary

Magnetic reconnection is an energy transferring process that happens at the Earth's magnetopause, the boundary between Earth's local plasma environment and the Sun's interplanetary environment. Reconnection helps move energy and particles into the region of space surrounding the earth called the magnetosphere. Dayside reconnection is important because it is a defining element to the amount of energy deposited into our magnetosphere, and state of safety to human life on Earth. Despite its importance, scientists still do not completely understand how it works and where it happens. This study looks at many observations of magnetic reconnection to try and understand its precise location and figure out under which conditions it is more likely to occur. This paper compares in-situ data with different models for predicting reconnection locations.

1 Introduction

The interplanetary magnetic field (IMF) emanating from the sun interacts with the terrestrial magnetic field giving rise to a complex and rich structures of scientifically interesting phenomena. The interaction between these two fields result in a reorientation of the topology of the magnetic field lines. This process is known as magnetic reconnection. The process is accompanied by the conversion of energy and is the primary process for exchange of particles between the solar wind and the magnetosphere (e.g., Paschmann, 2008). In three dimensional space, the location of reconnection is a line known as X-line. Magnetic reconnection at Earth's magnetopause deposits energy into the terrestrial magnetic field, the results of which have important consequences for the shape, size, and dynamics of the magnetosphere.

In the classical picture of magnetic reconnection, ignoring the Earth's dipole tilt, reconnection occurs at the sub-solar point when Earth's magnetic field lines encounter southward IMF, and in the polar cusp region for the northward IMF (Dungey, 1961). Southward IMF at the sub-solar point, the point of the magnetosphere closest to the sun, results in a process called anti-parallel reconnection since the Earth's magnetic field is in the Northward direction. On the other hand, for an arbitrary direction and magnitude of IMF, the location of reconnection is more complicated (Paschmann, 2008; Paschmann et al., 2013). Component reconnection occurs when the two reconnecting magnetic fields have some components of their directions perpendicular to the reconnection plane. Using in-situ spacecraft data as well as simulation data, both anti-parallel and component reconnection have been shown to occur at the magnetopause (Crooker, 1979; Gonzalez & Mozer, 1974; Paschmann et al., 2013, 2018, 1986; Fuselier et al., 2011; Trattner et al., 2007).

The location of reconnection sites, or X-lines, is crucial for understanding the dynamics of the magnetosphere and the effects of space weather at Earth. To predict the

Table 1. A list of reconnection models, the parameters which are maximized and the name given to those models in this study.

Model No.	Reference	Parameter	Name
1	Moore (2002)	Reconnecting component	Maximum Bisection Field Model
2	Trattner et al. (2007)	Magnetic shear	Maximum Shear Model
3	Cassak and Shay (2007)	Hybrid Alfvén velocity	Maximum Exhaust Velocity Model
4	Hesse et al. (2013)	Reconnection energy	Maximum Reconnection Energy Model

location of an X-line at the dayside magnetopause, multiple models have been developed over the last few decades. Some of these models encompass features of both anti-parallel and component reconnection. A sub-set of these models suggest that reconnection occurs along a line or in a region where some physical quantity or a parameter is maximized. Table 1 lists four models compared in this study and the parameter which is maximized in each of the models. The fourth column lists the name of the corresponding model as has been used in this study.

One assumption in each of these models is that reconnection occurs as a single spatially extended X-line across the dayside magnetopause. Inherent in each of these models is a prediction for what underlying physics controls the location of reconnection at the interface between the shocked solar wind and magnetosphere. None of them have been rigorously tested against other models using simulation or in-situ data. Komar et al. (2015) compared, among others, the models listed in Table 1 using global resistive magnetohydrodynamic (MHD) simulations and largely concluded that:

- 1. For the chosen [MHD] simulation parameters, we [Komar et. al. (2015)] find that all models are within a few Earth radii ($R_{\rm E}$) of the magnetic separators when the IMF has a southward orientation and no dipole tilt.
- 2. None of the models chosen for this study faithfully reproduce the entire magnetic separators when the IMF has a northward orientation and no dipole tilt. However, only the maximum magnetic shear model faithfully reproduces the portion of the separator nightward of the magnetic nulls where reconnection is expected to occur.

For all the tested models, results were within a few Earth radii of the magnetic separators when the IMF had a southward orientation, but only the maximum magnetic shear model faithfully reproduced the portion of the separator nightward of the magnetic nulls when the IMF had a northward orientation. Komar et al. (2015) did not directly compare the models' outputs, nor was a statistical study done. Souza et al. (2017) compared the output from three different analytical models (Maximum Shear Model, Maximum Current Density Model and Maximum Exhaust Velocity Model) with different spacecraft data. However, the study was done only for two reconnection events and thus lacked statistical significance. Nevertheless, several studies have validated the output of the Maximum Shear Model from different data sets (e.g., Petrinec et al., 2022; Trattner et al., 2021; Fuselier et al., 2017; Trattner, Burch, et al., 2017; Trattner, Thresher, et al., 2017). Another study was done recently by Liu et al. (2018) using a three dimensional particle-in-cell simulations in which they compared the results to different rate model predictions.

Among the models that Liu et al. (2018) compared their predictions with, they found that for X-line orientation, the Maximum Reconnection Energy Model provided the closest predictions.

Given the use of some of these models for mission designing and answering science questions (Fuselier et al., 2014), it is thus important to conduct a comparative study of these models using in-situ spacecraft data for varying upstream solar wind conditions. In this study we thus present a statistical comparison between four different dayside magnetopause reconnection X-line prediction models. The next section (Section 2) introduces and gives a brief overview of the four different X-line prediction models (listed in Table 1) considered in this study. Section 3 discusses all the data, both observation and simulation, used in this study as well as describes the methodology in detail. In the following section (Section 4) we present the results from the study and discuss the performance of the models for varying upstream solar wind conditions. Finally, Section 5 summarizes and concludes the study.

2 Science Background

There are several models in the literature that predict the location of the dayside magnetopause reconnection X-line. In this study we consider four such models (see Table 1) all of which have a common feature, they maximize a parameter along the magnetopause to find the location of X-line. In this section, a brief overview of each model is presented to provide the necessary scientific background.

2.1 Maximum Shear Model

The Maximum Shear Model is an empirical model for the location of a reconnection X-line along the magnetopause surface based on the ion-flux distribution in the high-altitude cusps (Trattner et al., 2007). The model posits that reconnection "occurs along a ridge of maximum magnetic shear between the opposing magnetic fields on the two sides of the magnetopause" (Trattner et al., 2021). In order to find the location of the X-line, the maximum of the shear angle between the two opposing fields is found which is given as:

$$\cos(\theta) = (\mathbf{B}_{\mathrm{sh}} \cdot \mathbf{B}_{\mathrm{msp}}) / (|\mathbf{B}_{\mathrm{sh}}||\mathbf{B}_{\mathrm{msp}}|) \tag{1}$$

where, \mathbf{B}_* is the magnetic field and 'sh' and 'msp' refers to the magnetosheath and magnetosphere respectively. Sections 3.1 and 3.2 describe in detail how the relevant data for each side is obtained.

Though the original Maximum Shear Model study only considered southward IMF conditions (Trattner et al., 2007), a more recent study has shown the model to be valid for northward IMF conditions as well without losing statistical accuracy as long as B_y is the dominant component $(B_y/|\mathbf{B}| > 0.8)$ (Trattner, Thresher, et al., 2017). Since its inception, several studies in literature have quantified the performance of Maximum Shear Model (Trattner, Burch, et al., 2017; Fuselier et al., 2017; Komar et al., 2015).

2.2 Maximum Reconnection Energy

The Maximum Reconnection Energy Model is a theoretical model proposed by Hesse et al. (2013) to describe the collisionless magnetic reconnection of asymmetric systems. The model suggests that in an asymmetric system, the magnetic reconnection line is oriented in such a way that the product of available magnetic energy is maximized. For magnetosphere and solar wind magnetic interactions the following parameter is maximized:

$$E \propto \left(|\mathbf{B}_{\rm sh}|^2 \times |\mathbf{B}_{\rm msp}|^2 \right)$$
 (2)

where E is proportional to the available energy from two available fields. The model was originally proposed and supported by small scale reconnection simulations and has been tested using a MHD simulation. Komar et al. (2015) compared several dayside magnetic reconnection models in global magnetosphere simulations, one of which was Maximum Reconnection Energy Model and found that Maximum Reconnection Energy Model was within a few Earth radii ($R_{\rm E}$) of X-line for southward IMF and no dipole tilt. The model is strictly two dimensional and to enhance confidence in the model, a full three dimensional treatment of the theory is required.

2.3 Maximum Exhaust Velocity

The Maximum Exhaust Velocity Model is an application of a model proposed by Cassak and Shay (2007). The model conjectures that the X-line orientation is determined by maximizing the asymmetric reconnection outflow speed which is described as:

$$V_{\rm A} \sim \left[\frac{B_{\rm sh} B_{\rm msp} \left(B_{\rm sh} + B_{\rm msp} \right)}{\left(n_{\rm i,msp} B_{\rm sh} + n_{\rm i,sh} B_{\rm msp} \right)} \right]^{1/2}$$
 (3)

where $n_{i,msp}$ and $n_{i,sh}$ refers to the ion density in magnetosphere and magnetosheath respectively. The predictions of this model have been found to be consistent with space-craft observations of reconnection poleward of the cusp (Muzamil et al., 2014) as well as observations in simulation (Cassak & Fuselier, 2016; Komar et al., 2015). One of the limitations of the model is that it ignores the importance of plasma velocity parallel to the direction of reconnecting magnetic field (Komar et al., 2015).

2.4 Maximum Bisection Field

The Maximum Bisection Field Model was proposed by Moore (2002) to predict the location of the dayside X-line along the locus of points where the two opposite field lines, magnetospheric and magnetosheath, are bisected. This simplifies to finding the location where the following field is maximized:

$$B_{\rm rec} = |\mathbf{B}_{\rm msp} \cdot \mathbf{i}_{\rm xn}| \tag{4}$$

where, $B_{\rm rec}$ is the field component to be maximized and ${\bf i}$ is the the unit vector normal to the x-line. If the slope of the reconnection line were ${\bf m}$, then the slope of the unit vector ${\bf i}_{\rm xn}$ will be $-1/{\bf m}$. Once the location of maximum reconnecting field is found, the X-line is then found by integrating away from the point along the bisector of angle between the local fields. One of the assumption of Moore (2002) is that bisection only leads to equal and opposite reconnecting components if the magnitude of the magnetic field on both sides of the current sheet is the same, however this is not always the case for a full 3-D fields.

For the 2-D case, this direction is identical to the direction along which the proportional available magnetic energy is maximized as given by the Maximum Reconnection Energy Model (Hesse et al., 2013). This means that maximizing either Equation (2) or Equation (4) should give identical results. However, as seen in Section 4, for a full 3-D case, though the output from two models look very similar (see right panels in Figure 4), the location of the X-line as computed by maximizing each of the two parameters give slightly different results (see Tables 3 and 4).

Figure 1 shows the distribution of each of the four parameters discussed in this section, projected on the yz-plane. The parameters have been normalized against their respective maximum values. The three rows correspond to three different IMF conditions

(shown at the top right of each plot). Top row corresponds to a purely southward IMF whereas the bottom row corresponds to purely northward IMF. Middle row shows the distribution for Parker spiral like condition with zero field in z-direction. Clock angle for each IMF is shown in top left corner. For these sample plots, the ion density (n_p) is assumed to be $5 \, \mathrm{cm}^{-3}$ with plasma bulk velocity of $-500 \, \mathrm{km/s}$ in the x-direction and an average ion temperature of $1.5 \times 10^{-6} \, \mathrm{K}$. The DST index is $-5 \, \mathrm{nT}$ and the dynamic pressure is $2.4 \, \mathrm{nPa}$. For simplicity, Earth's dipole tilt was assumed to be zero for all three cases. The magnetic fields were computed using the Tsyganenko-96 model (Tsyganenko, 1996). See Section 3.2 for more details on how these images were generated. These figures are similar to those reported in literature (Moore, 2002; Trattner et al., 2007).

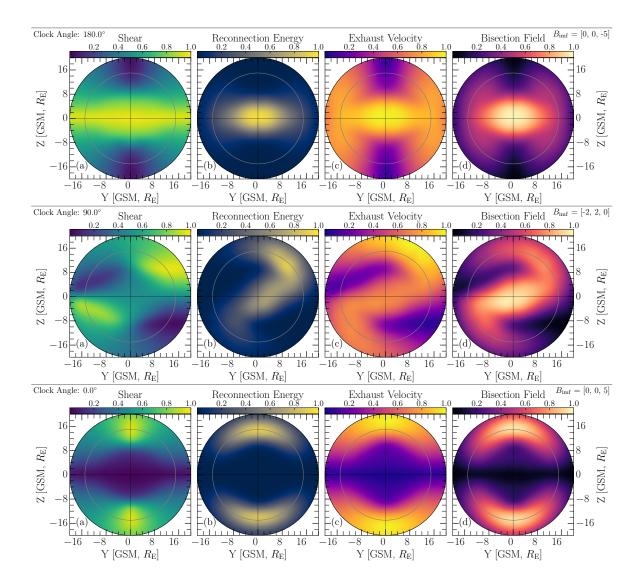


Figure 1. Sample figure of distribution of four parameters discussed in Section 2, projected on the yz-plane. Three rows correspond to three different IMF conditions (from top to bottom, purely southward IMF, Parker spiral and purely northward IMF) shown in the top right corner of each panel. For simplicity, Earth's dipole tilt is assumed to be zero.

3 Data Selection and Methodology

3.1 Data

This investigation uses high resolution OMNI data (1 minute resolution) propagated to the nose of Earth's bow shock (King & Papitashvili, 2005) along with data from the Fast Plasma Instrument (FPI) (Pollock et al., 2016) and the Fluxgate Magnetometer (FGM) (Russell et al., 2016; Torbert et al., 2016) aboard the MMS spacecraft. Since MMS is a constellation of 4 spacecraft, we looked into differences in the output of the model while using data from different spacecraft. We observed that using data from one versus other spacecraft made insignificant changes to the overall result of this study, and thus decided to use data from MMS 3 for this study. For easy identification of jet reversal (see Section 3.2 for more details), the study uses high resolution burst data from FPI which gives a full space density measurement every 150 ms (for ions). Section 3.2 describes how each of these data were used in this study and the methodology in greater detail.

3.2 Methodology

With the MMS spacecraft, between September 2015 and April 2018, 16,782 magnetopause current sheet crossings have been identified and documented (see Paschmann et al. (2018); Haaland et al. (2020) for details of methodology used for identification and classification). A spacecraft crossing the magnetopause current sheet can observe enhanced ion velocity tangential to the current sheet. This enhancement, known as a reconnection jet, is an indication that reconnection is occurring nearby. Enhanced ion-velocities with switching directions are called jet reversals, and are evidence of an X-line nearby the spacecraft position (e.g., Paschmann et al., 1979; Cowley, 1982; Gosling et al., 1982; Pu et al., 2007; Dunlop et al., 2011; Trattner, Burch, et al., 2017; Petrinec et al., 2022).

For each identified crossing, we record a 10-minute long time series centered at the crossing time ($t_{\rm cross}$). We transform the magnetic field and the ion-velocity from GSM-coordinate (Geocentric Solar Magnetic) to a local LMN-coordinate (boundary-normal) system using the empirical magnetopause model described in Shue et al. (1998). In the code, this was implement using coordinate transformation tools available in PySPEDAS (Grimes et al., 2019). Using the ion properties (density, temperature and energy spectra) we identify the magnetosheath and magnetopause locations. If there are multiple crossings within the 10-minute time period, then the values during the longest interval for both locations are averaged over to get a representative value of each parameter in that region. In the next step, we identify if a jet reversal was observed by MMS during the crossing by inspecting the ion velocity directions. In order to minimize the impact of varying condition of magnetosheath because of changes in the upstream solar wind condition, we subtract the representative ion-velocity, $\langle V_{\rm L} \rangle$ of magnetosheath from the velocity time series and call the resultant parameter $\Delta V_{\rm L}$, defined as:

$$\Delta V_{\rm L} = V_{\rm L} - \langle V_{\rm L,sheath} \rangle \tag{5}$$

where, $\langle V_{\rm L,sheath} \rangle$ is the average value of L-component of ion-velocity in the longest magnetosheath interval in the 10-minute period and $V_{\rm L}$ is the time series data of L-component of ion-velocity. We use this velocity, $\Delta V_{\rm L}$, to check for the presence of jet-reversal during crossings. In order to identify jet-reversal, we look for switches in $\Delta V_{\rm L}$ by more than $\pm 70\,\mathrm{km/s}$ within a 2-minute window of the 10-minute time series data. Previous studies (Trattner, Burch, et al., 2017; Petrinec et al., 2022) have used the same velocity change and time window values for a similar dataset. This study adds additional conditions to the crossings in order to constrain uncertain crossing measurements. To remove artificial peaks, the algorithm only identifies a velocity switch as a jet-reversal if $\Delta V_{\rm L}$ is larger (and smaller) than $+70\,\mathrm{km/s}$ ($-70\,\mathrm{km/s}$) continuously for at least a time interval of 3 seconds. Once we find such a time interval, we check if the maximum and minimum val-

ues of $\Delta V_{\rm L}$ occurred within a 2 minute time interval of each other. Once that condition has been satisfied, we assign time of the jet $(t_{\rm jet})$ as the time between the maximum and minimum value of $\Delta V_{\rm L}$. If there are multiple instances of $|\Delta V_{\rm L}| > 70\,{\rm km/s}$ within the 10 minute period, then the interval which has the highest peak of $\Delta V_{\rm L}$ is checked for presence of a jet. The methodology to identify jet reversals is based on methodology developed by Trattner, Burch, et al. (2017) and used in previous statistical studies Trattner, Burch, et al. (2017); Petrinec et al. (2022).

Figure 2 shows a typical MMS time series data of the parameters used in this study. The top panel (panel a) shows the ion energy spectra, and the next panel shows the magnetic field strength in the local LMN-coordinate system. Panel (c) and (d) show the ion-density and parallel and perpendicular temperatures respectively. The dip in ion-density and the corresponding enhancement of ion-temperature around 16:50:30 UTC, along with the change in ion-density spectra, is the indication of spacecraft moving from magnetosheath to magnetosphere. Next, panel (e) show the time series of ion-velocity components. Vertical red and blue lines mark the location of reference magnetosphere and magnetosheath, as identified by the automated code described earlier. The last panel (f) shows $\Delta V_{\rm L}$, which is the difference between $V_{\rm L}$ and the average value of $V_{\rm L}$ in the magnetosheath, described by Equation (5). The green vertical line shows the location of the center of the jet, which is at the center point between the maximum and minimum value of $\Delta V_{\rm L}$. The timestamp corresponding to this center point is referred as the time of the jet, $t_{\rm jet}$.

Once a jet has been identified, a 10-minute average value of solar wind observations from OMNI data centered at $t_{\rm jet}$ are used for the upstream condition. These solar wind upstream conditions are then used as input for the Shue-98 (Shue et al., 1998) model to compute the stand-off distance of the magnetopause sub-solar point and the general shape of the magnetopause. The upstream solar wind conditions are then used with the output of Shue-98 model as input for Tsyganenko-96 (Tsyganenko, 1996) model, which provides the magnetic field at the magnetopause.

For the magnetosheath fields, we use the Cooling-01 (Cooling et al., 2001) model to obtain the draped magnetosheath field just outside the magnetopause. For the Cooling-01 model, the magnetosheath density is derived from MMS data (using the average observed value, as previously described) and for the magnetopause ion density we assume a standard density of $0.1 {\rm cm}^{-3}$. The output from these models is used to compute the value of four parameters (magnetic shear, reconnection energy, exhaust velocity and bisection field) over the magnetopause spread over a circular region of radius $20\,{\rm R_E}$ as described by Equations (1) to (4).

Next, to trace the location of the predicted reconnection line from each model, maximization of each of the respective parameter (except for Maximum Bisection Model, see Section 2.4) is carried out over the projected circular region along the draped field lines. Thereafter, we compute the minimum 3-D distance of MMS spacecraft from each of the predicted line positions and store the value of distance to make statistical observations. Figure 3 shows the flowchart of the algorithm described above. Figure 4 shows a typical case where we have plotted each of the four parameters on the yz-plane along the magnetopause. The panels from a to d show shear, reconnection energy, exhaust velocity and bisection field. Each of these parameters are normalized against their maximum value in the plane so that they all range from 0 to 1. The grey circle at about 15 $R_{\rm E}$ corresponds to the terminator. MMS is represented by the white encircled plus. The red and blue arrow in each panel show the direction of the local magnetosheath field and ionvelocity at the position of MMS. $R_{\rm rc}$ is the measured minimum 3-D distance between the reconnection line and the spacecraft. For this study, cases where the point of minimum distance was outside the terminator were not used for the statistics.

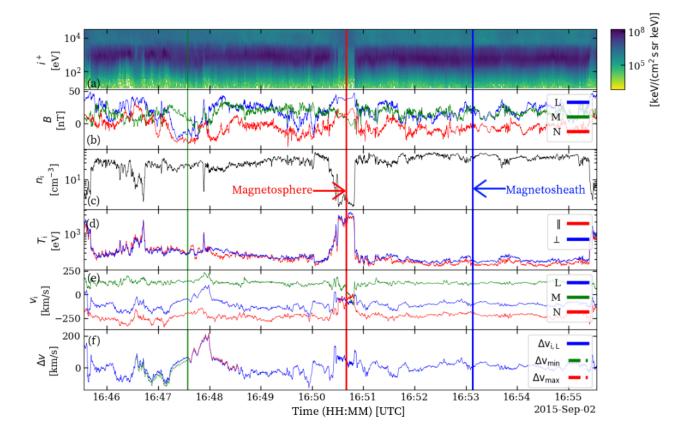


Figure 2. Time series of various data from MMS spacecraft. Top panel shows the ion energy spectra whereas the next panel (panel b) shows the time series of three magnetic field components in LMN-coordinate system. Panel c and d show the ion density and temperatures. Panel e shows the ion-velocity components. Vertical red and blue lines mark the location of magnetosphere and magnetosheath, as identified by the automated code. The last panel shows $\Delta V_{\rm L}$, which is the difference between $V_{\rm L}$ and the average value of $V_{\rm L}$ in the magnetosheath. The green vertical line shows the location of a jet, which is at the center point between the maximum and minimum value of $\Delta V_{\rm L}$.

4 Results and Discussions

Using the methodology described in Section 3.2, between September 2015 and April 2018, a total of 274 jet reversals were identified. For each of these events we computed the distance between the predicted X-line location and the MMS spacecraft. Figure 5 shows the location of each of the jets in xy- and yz-plane with a nominal magnetopause location shown by the dashed-blue line. The two colors represent jet-reversal detection corresponding to the directions of B_z (southward for green and northward for orange). The average value of various solar wind parameters corresponding to the time of observation of each event are listed in Table 2. These values are very similar to nominal solar wind conditions observed at 1 AU by the WIND spacecraft (Wilson III et al., 2021). However, though the nominal value of B_z in the solar wind on average is very close to

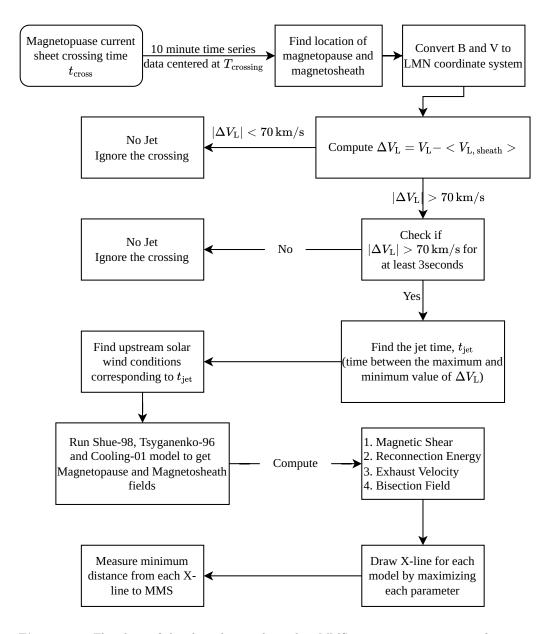


Figure 3. Flowchart of the algorithm used to select MMS magnetopause crossings for jet reversals and comparison to model X-line positions. See text for definition of each term and more details

zero, for the 274 jet reversals observed, the average value of B_z in the solar wind was close to -1, which shows a bias of jet reversal detection during southward IMF. This is to be expected because reconnection near the sub-solar region is more common during southward IMF. Statistically, we found that we were twice as likely to find a jet-reversal during southward IMF compared to northward IMF. Figure 6 shows a histogram of the distance of the modeled reconnection X-line ($R_{\rm rc}$) from the MMS spacecraft. The distance is plotted along the x-axis in the units of Earth radius ($R_{\rm E}$), with the frequency of events along y-axis. The dashed line in each panel corresponds to the mean value of the histogram.

The performance of the models across the various solar wind conditions are now compared. The average value of distance between spacecraft and the predicted X-line

Table 2. Average values of solar wind parameters during observed jet reversals

Parameter	Percentile			
	5^{th}	50^{th}	95^{th}	
B [nT]	2.69	4.76	9.67	
$n_{\rm i} \ [{\rm cm}^{-3}]$	2.22	4.97	12.02	
P_{dyn} [nPa]	1.23	2.23	4.88	
$V_{\rm i}~{ m [km/s]}$	337	507	693	
$T_{\rm i} \; { m [ev]}$	2.55	10.20	27.89	

for Maximum Bisection Field Model and Maximum Reconnection Energy Model are similar, though the Maximum Bisection Field Model with an average measured distance of $4.22\,R_{\rm E}$ gives the lowest value among the four tested models. The histogram for Maximum Bisection Field Model also has the least spread, implying the precision of the model, however it seems to lack the accuracy of the Maximum Bisection Field Model can be explained, in part, by the inherent observational bias in the data. Most of the jet-reversals were observed by MMS in the equatorial plane, very close to the sub-solar point (see Figure 5). In addition, for most upstream conditions (except for conditions with positive $B_{\rm x}$), the Maximum Bisection Field Model tends to predict the X-line location along or close to the equator; it therefore makes sense that the spread for this model will be least compared to other models.

Under the condition $B_{\rm z}<0$, the accuracy of each model improves compared to all IMF conditions. Figure 7 shows the histogram corresponding to this condition and Table 3 shows the difference in average values corresponding to two different conditions ($B_{\rm z}>0$ and $B_{\rm z}<0$) along with the average value of measured reconnection distance for each model for three different conditions. The improvement is most significant in the case of Maximum Reconnection Energy Model where the average value changes by 3.15 $R_{\rm E}$ followed by Maximum Exhaust Velocity Model (a change of 2.53 $R_{\rm E}$). The correlation between the model accuracy and the value of $B_{\rm z}$ can also be seen in Figure 8. Figure 8 shows the highest value of Pearson correlation coefficient for Maximum Reconnection Energy Model and Maximum Exhaust Velocity Model implying greater dependency of the accuracy of these two models on $B_{\rm z}$ followed by Maximum Shear Model and Maximum Bisection Field Model , which understandably shows the least correlation between the two parameters. For Figure 8, the histogram along each axis shows the distribution of the associated parameter.

Figure 9 shows the distribution between the cone angle ($\theta_{\rm cone} = \cos^{-1}(B_{\rm x}/|{\bf B}|)$) and the z-component of IMF. Low $\theta_{\rm cone}$ means the IMF is dominated by the radial magnetic field component and likely has a foreshock upstream of the dayside magnetopause. Each bubble represents an observation point and its radius is proportional to the measured distance between X-line and MMS for the corresponding model. The larger bubble implies lesser accuracy in predicting the location of X-line by the model. For both the Maximum Bisection Field Model and Maximum Reconnection Energy Model at $B_{\rm z} > 0$ there is a visible increment in $R_{\rm rc}$ values (see Table 3). At all $\theta_{\rm cone}$, as long as $B_{\rm z}$ is negative, the two models remain fairly accurate. For mid range values of $\theta_{\rm cone}$ (values between [50, 120] degrees), even when $B_{\rm z}$ is positive, the model (Maximum Bisection Field Model and Maximum Reconnection Energy Model) predictions remain accurate. The

Maximum Shear Model behaves in a very similar way with two interesting differences. For mid range values of cone angle, for all values of $B_{\rm z}$ and especially for positive values, the Maximum Shear Model does the best job of predicting the correct location of X-line. And at low values of cone angle, Maximum Shear Model performs as well as the Maximum Reconnection Energy and Maximum Bisection Field Model. At very high values of $\theta_{\rm cone}$ (> 150 degrees) irrespective of the sign of $B_{\rm z}$, Maximum Shear Model performs relatively poorly ($\langle R_{\rm c,shear} \rangle = 9.50\,R_{\rm E}$ vs $\langle R_{\rm c,bisec} \rangle = 3.65\,R_{\rm E}$).

In Figure 9 there is also an asymmetry in the computed values of $R_{\rm rc}$ for very low ($\theta_{\rm cone} < 30$ degrees) and very high ($\theta_{\rm cone} > 150$ degrees) cone angles for all models. This can in part be explained the fact that the effect on the draping filed, as computed using Cooling-01 model, is not symmetric for positive and negative $B_{\rm x}$. Also, while computing the fields using T-96 model, dipole tilt of the Earth is considered whereas it is ignored during computation of draping field using Cooling-01 model. This also leads to some asymmetry to the result of computed distance. Though this asymmetry is present in all cases, it is most pronounced for Maximum Shear Model. Previous work has reported the Maximum Shear Model struggled during time periods with large $B_{\rm x}$ or small $\theta_{\rm cone}$ possibly due to the draping model being used (Trattner, Thresher, et al., 2017).

In order to look at the affect of $B_{\rm y}$ on the accuracy of the models, we plot $B_{\rm y}/|{\bf B}|$ against the z-component of IMF in Figure 10. Figure 10 is made in a similar style to that of figure Figure 9, except $B_{\rm y}/|{\bf B}|$ is along the y-axis. We plot this ratio instead of the value of $B_{\rm y}$ in order to look at the variation in different X-line predictions based on how dominant the y-component is. It has been noted in literature (Trattner, Thresher, et al., 2017) that for dominant $B_{\rm y}$ the Maximum Shear Model still works even for a northward IMF. We see that to be the case here as well in the top left panel of Figure 10 corresponding to the Maximum Shear Model. For other models shown in Figure 10 the effects of $B_{\rm y}$ are much less prominent. This is clear from Table 4 where we have shown the average values of R_c corresponding to cases $B_{\rm y}/|{\bf B}| > 0.7$ and $B_{\rm y}/|{\bf B}| < 0.3$ as well as percentage change in the average values for all four models. Maximum Shear Model has the highest change percentage whereas Maximum Bisection Field Model is least affected by the change in $B_{\rm y}/|{\bf B}|$. The effect of $B_{\rm y}$ is even more dominant when we only consider the cases where the IMF was northward. In such conditions, the accuracy of Maximum Shear Model increases by $\sim 45\%$.

The Maximum Exhaust Velocity Model performs worst compared to all the other models in this study. Although there is significant improvement in prediction accuracy when we consider cases of only negative $B_{\rm z}$ (see Table 3), the average $R_{\rm rc}$ values are more than all other models. Part of the reason for this poor performance might be the fact that the Maximum Exhaust Velocity Model uses both the magnetic field and density of ions in its computation of the hybrid Alfvén speed. We explicitly assume the value of ion density in the magnetosphere as $0.1\,cm^{-3}$ which would have the impact on the accuracy of the computed velocity.

5 Summary and Conclusion

Magnetic reconnection occurring at the magnetopause of Earth is known to exert a significant influence on magnetospheric convection and facilitates the influx of mass and energy into the magnetosphere/ionosphere system. Despite its importance, the factors governing the location of a dayside magnetic reconnecting X-line are not well understood. Several models have been proposed to predict the location of the X-line. For this study, we chose to compare the statistical performance of four such models. These models share a common assumption that the X-line location can be determined by the maximization of a physical quantity along the magnetopause boundary. The models considered maximizes the magnetic shear, magnetic reconnection energy, hybrid exhaust velocity and the bisection field. We referred to them as Maximum Shear Model, Maximum

Table 3. Table of average distance between MMS observation and model predicted X-line locations for different conditions of z-component of IMF B_z . $\langle R_{c,B_z<0} \rangle$ refers to average distance from reconnection line for cases where $B_Z < 0$.

Model	${\bf Average\ Distance}\ (R_{\rm rc})$			Difference, $\Delta R_{ m rc}$
Wiodei	All IMF conditions	$\langle R_{\rm rc,B_z<0} \rangle$	$\langle R_{\rm rc,B_z>0} \rangle$	$\left (\langle R_{\rm rc,B_z>0} \rangle - \langle R_{\rm rc,B_z<0} \rangle) \right $
Maximum Shear Model	5.16	4.53	6.34	1.81
Maximum Reconnection Energy Model	4.65	3.74	6.88	3.14
Maximum Exhaust Velocity Model	5.93	5.16	7.69	2.53
Maximum Bisection Field Model	4.22	3.65	5.27	1.62

Table 4. Table of average distance between MMS observation and model predicted X-line locations for different values of IMF $B_y/|\mathbf{B}|$

Model	Average Dis	Difference, $\Delta R_{ m rc}$	
Wiodei	$B_{\mathrm{y}}/ \mathbf{B} < 0.3$	$B_{\rm y}/ {f B} >0.8$	(Percentage)
Maximum Shear Model	7.57	5.48	27.61
Maximum Reconnection Energy Model	6.79	5.45	19.73
Maximum Exhaust Velocity Model	8.98	7.95	11.47
Maximum Bisection Field Model	4.82	4.69	2.70

Reconnection Energy Model, Maximum Exhaust Velocity Model, and Maximum Bisection Field Model.

We report the performance of these models under various upstream solar wind conditions. We used high cadence MMS data in conjunction with data from OMNI. Output from models (Tsyganenko-96, Shue-98 and Cooling-01) were used to get the magnetospheric and magnetosheath magnetic fields. In order to locate the actual locations of the X-line, we found the time intervals where MMS observed jet reversals with sustained high positive and negative values of ion velocities for at least 3 seconds in each direction, within a 2 minute window. The location of MMS at these intervals were then compared with the prediction for an X-line from the aforementioned four different models. We computed the shortest distance between the predicted X-line and the MMS location. For the 274 jet reversals observed between September 2015 and April 2018, under no constraints on the upstream IMF conditions, the Maximum Bisection Field Model gives the shortest average distance from the estimated X-line compared to the other models with an average value of $R_{\rm rc} = 4.22\,R_{\rm E}$. The Maximum Reconnection Energy Model does a comparable job with an average value of $R_{\rm rc} = 4.65 R_{\rm E}$. For the cases where $B_{\rm z}$ <0, we observe maximum improvement for the Maximum Reconnection Energy ($R_{\rm rc}=$ $3.74\,R_{\rm E}$) thereby implying strongest dependence on $B_{\rm z}$. Though for Maximum Bisection Field Model, the improvement is not as significant $(R_{\rm rc} = 3.65 R_{\rm E})$, it still is the best model. Under all circumstances, we found that the Maximum Bisection Model performed best.

Considering the effect of B_y , we reconfirmed the results of (Trattner, Thresher, et al., 2017), that for a dominant B_y , $(B_y/|\mathbf{B}| > 0.8)$, the Maximum Shear Model performs well, at par with the Maximum Reconnection Energy Model and slightly worse than the Maximum Bisection Field Model. The difference in the improvement of the Maximum Shear Model was highest ($\sim 28\%$) for the four tested models. If we consider dominant B_y along with $B_z > 0$, the improvement in the model increases to $\sim 45\%$.

Overall, the Maximum Bisection Field Model seems to perform best for different upstream conditions and also appears to be most precise. However, part of the reason can be attributed to the inherent observational bias in the MMS data. The Maximum Bisection Field Model tends to predict the location of X-line along or close to the equator, which is also where MMS observed most of the jet reversals (see Figure 5).

Among the four models we compared and various solar wind conditions that we observed, the Maximum Exhaust Velocity Model seems to perform poorest. This can party be because in this study we assumed the magnetospheric ion density to be constant ($n_i = 0.1\,\mathrm{cm}^{-3}$) which is not necessarily true. An accurate measurement of the density would alter the hybrid Alfvén velocity and thus affect the average values of measured distance.

Though, as expected, the accuracy of all the models improves with the strength of southwards IMF, the effect is most pronounced for Maximum Exhaust Velocity Model and and least for the Maximum Bisection Field Model as seen in Figure 8. The Maximum Exhaust Velocity Model is also most affected by the extreme values of the cone angle ($<30^{\circ}$ and $>150^{\circ}$). Though for small cone angles, and for southward oriented IMF, Maximum Shear Model is fairly accurate, at high values of cone angle, for all B_z , the model tends to perform poorly, as seen in Figure 9. For this condition, however, the Maximum Reconnection Energy and the Maximum Bisection Field Model remain largely unaffected.

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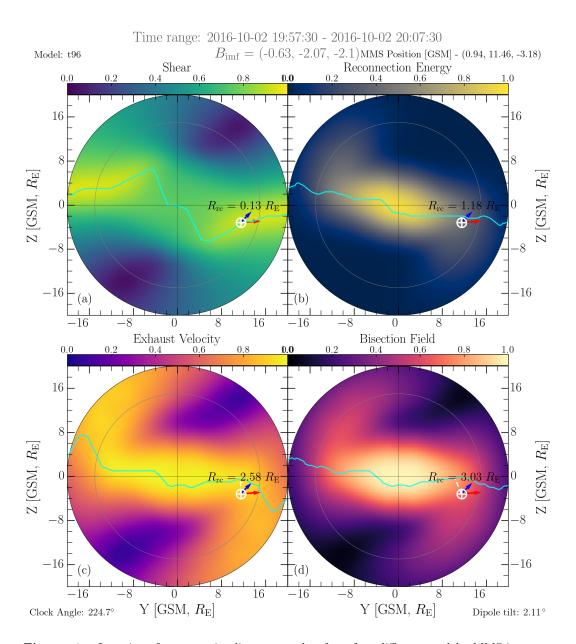


Figure 4. Location of reconnection line, cyan color, from four different models. MMS is represented by the white encircled plus. Red arrow shows the direction of local magnetosheath field whereas blue arrow shows the direction of local ion-velocity. $R_{\rm rc}$ is the measured minimum distance between the reconnection line and the spacecraft.

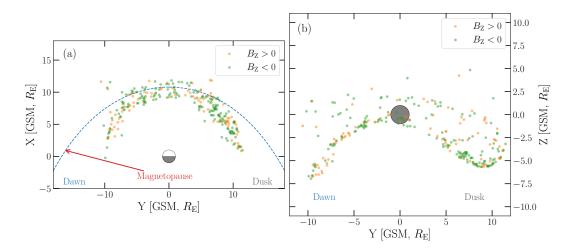


Figure 5. Location of all the reconnection events used in this study, as observed by MMS, with nominal magnetopause shown as a dashed-blue line.

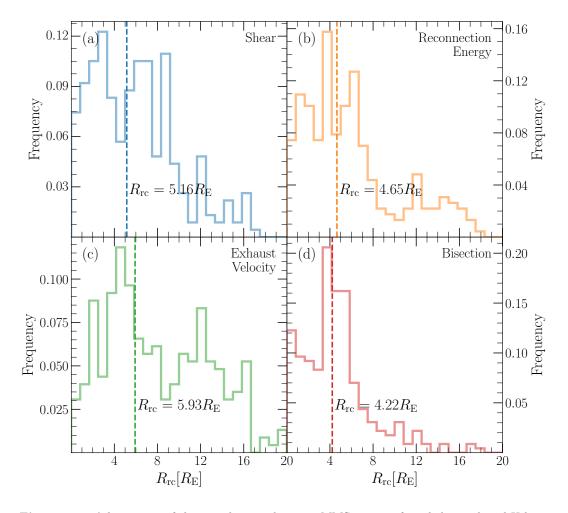


Figure 6. A histogram of shortest distance between MMS spacecraft and the predicted X-line location by different models. The distance is plotted along x-axis in units of Earth radius, with counts along y-axis. Vertical dashed line in each Panel corresponds to the mean distance of 274 individual measurements.

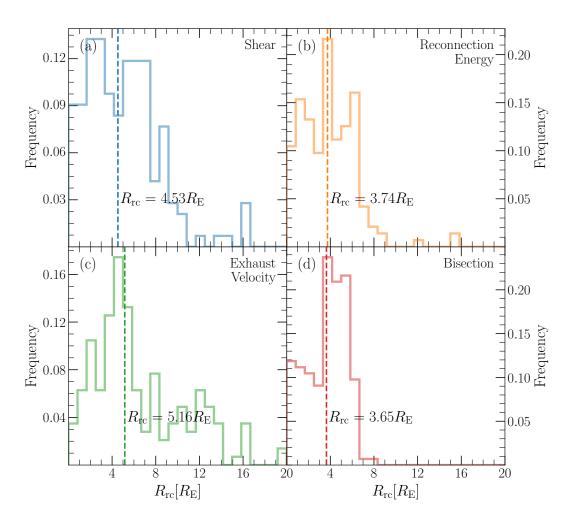


Figure 7. A histogram of shortest distance between MMS spacecraft and the predicted X-line location by different models when $B_{\rm z} < 0$. The distance is plotted along x-axis in units of Earth radius, with counts along y-axis. Vertical dashed line in each panel corresponds to the mean distance.

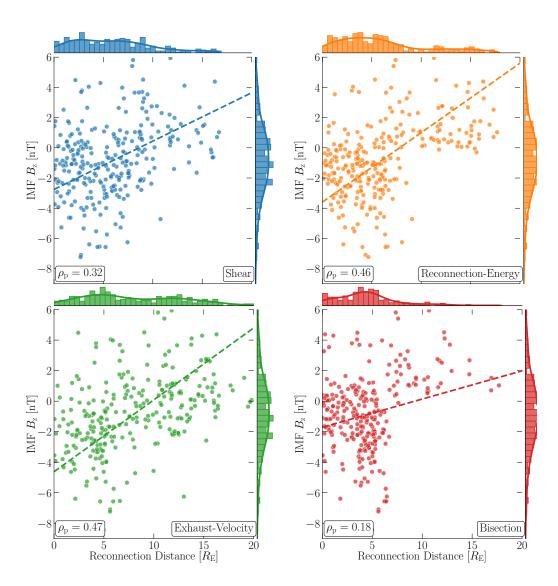


Figure 8. Correlation between the z-component of IMF and the distance between the predicted X-line and MMS for different models. $\rho_{\rm p}$ is the Pearson correlation coefficient. The dashed lined is the trend line with $\rho_{\rm p}$ as slope. The histogram along the edges shows the distribution of parameters

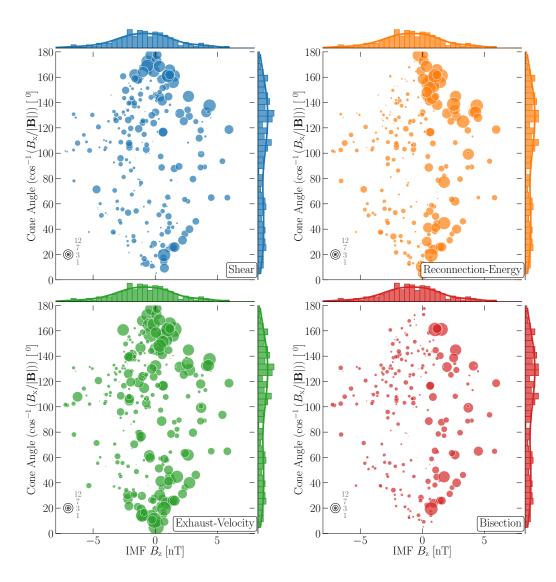


Figure 9. Plot between the IMF cone angle and the corresponding z-component for different models. The size of each circular marker is a representative of measured reconnection distance from the predicted X-line location. Histograms on each of the axis represents the distribution of the parameter along those axes.

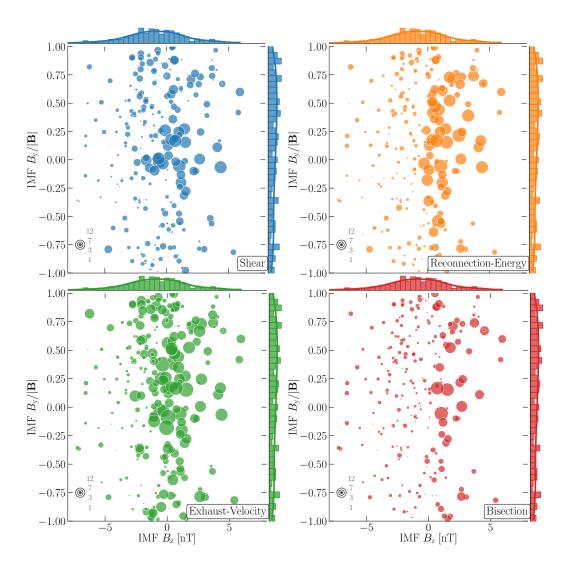


Figure 10. Plot between the ratio of IMF y-component to its magnitude and corresponding z-component for different models. The size of each circular marker is a representative of measured reconnection distance from the predicted X-line location. Histograms on each of the axis represents the distribution of the parameter along those axes