

# Complementary Couple-Turns: An Effective Method for Reducing Common-Mode Noise in Full-Bridge *LLC* Resonant Converter With Split Primary Winding Transformer

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**Abstract**—In conventional full-bridge (FB) *LLC* resonant converters, the position of the resonant tank can affect the symmetry of the entire circuit, leading to different  $dv/dt$  values at the two winding terminals of the transformer. This results in noncancelable displacement currents generated in the parasitic interwinding capacitance of the transformer, leading to severe common-mode (CM) noise issues. In this article, a low CM noise FB *LLC* resonant converter with the split primary winding transformer (SPWT) configuration is proposed. The transformer primary winding is split into two windings and the resonant tank is connected between these two windings. With a symmetrical winding structure, the CM noise current generated in the transformer can be canceled completely. The concept of complementary couple-turns is proposed to ensure a symmetrical winding arrangement for the planar transformer in the printed circuit board (PCB) layout stage before it is fabricated physically. Practical considerations have been discussed when implementing the SPWT configuration, including leakage inductance, transformer winding loss, and voltage conversion ratio. A 360 W FB *LLC* converter with planar transformers is built to verify the proposed methods.

**Index Terms**—Common-mode (CM) noise, full-bridge (FB), *LLC* resonant converter, planar transformer, split primary winding transformer (SPWT).

## I. INTRODUCTION

COMMON-MODE (CM) noise primarily arises from the displacement currents flowing through parasitic capacitors with high  $dv/dt$  nodes, which can disrupt the proper functioning of electronic devices, equipment, and systems [1]. CM filters, which include Y-capacitors and bulky CM inductors, are usually employed to ensure that power converters meet the corresponding electromagnetic interference (EMI) standards. To improve the power density of the overall system, it is important to achieve low CM emissions of power converters so as to shrink the size of CM filters [2].

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The full-bridge (FB) *LLC* resonant converter has been widely used in medium-to-high power applications because of its simple structure, high cost-effectiveness, and soft-switching capability [3], [4], [5]. The FB *LLC* converter possesses a natural symmetrical structure, which yields a pair of switching nodes having complementary electric potentials with respect to the ground. When the associated parasitic capacitances of these nodes are equal, the generated CM noise displacement currents can be completely canceled by each other. However, the voltage across the resonant tank affects the electric potentials of the transformer's primary winding terminals, which generates a large CM noise displacement current in the interwinding capacitance of the transformer [6]. This issue is particularly severe in planar transformers, which have a larger parasitic interwinding capacitance than traditional wire-wound transformers due to the larger overlapping area between adjacent winding layers [7], [8], [9]. The combination of large parasitic interwinding capacitance and large  $dv/dt$  difference leads to severe CM noise problems.

Various methods have been proposed to suppress the CM noise current flowing through the transformer of isolated power converters [10], [11], [12], [13], [14], [15], [16], [17], [18], [19], [20], [21], [22], [23], [24], [25], [26]. The shielding technique is widely used to block the electric coupling between the transformer primary and secondary windings [10], [11], [12], [13], [14]. However, there is a large conduction loss in shielding layers because of the eddy current, which results in lower converter efficiency. In [15], [16], and [17], the overlapping primary and secondary winding layers of the transformer are made to have the same voltage distributions. There is no CM noise displacement current in the interwinding capacitance because of zero  $dv/dt$ . But this approach does not work for FB *LLC* converters since there are no static points in transformer primary winding terminals. The CM noise current cannot be completely canceled. In [18], a static-point connection is proposed to establish the static points at the primary winding, so as to build the paired winding layers with the same  $dv/dt$ . However, it is hard to implement this approach in medium-to-high power applications with planar transformers. Especially for the high turns ratio planar transformer with an interleaved winding structure, too many paired layers are needed to maintain zero  $dv/dt$  between primary and secondary winding layers, which results in high manufacture cost and large transformer size. Passive components and extra transformer

winding can be used to cancel the CM noise current in [19], [20], [21], [22], [23], [24], [25], and [26]. In [19], [20], [21], and [22], balanced resonant tanks are utilized for the CM noise reduction of FB *LLC* converters. Each resonant inductor and capacitor are separated into two components with the same value. The balance condition is sensitive to the components' tolerance. CM noise cancellation capacitor is added to the transformer in [23], [24], and [25]. The capacitor value is selected based on the calculation or experimental results of the transformer's equivalent interwinding capacitance. In [26], an antiphase winding is introduced to generate the out-of-phase CM noise current. Although the CM noise performance can be improved, extra components or transformer windings are needed which increases the cost and decreases the power density of the converter.

A method of balanced windings has been proposed in [27] for flyback converters. This method divides the primary winding of the flyback transformer into two branches, with the switch and control logic branch placed in the middle. However, the approach discussed in [27] is based on wire-wound transformers and does not provide a universally applicable winding method for transformers. In this article, the concept of balanced windings is extended to the FB *LLC* converter to reduce the CM noise. The *LLC* transformer primary winding is split into two windings and the resonant tank is connected between these two windings. The split primary windings of the transformer are wound on the same magnetic core. This FB *LLC* configuration is first mentioned in this article, which is named as split primary winding transformer (SPWT). The equivalent CM noise circuit of the FB *LLC* converter with SPWT configuration is developed and analyzed in detail. It has been found that, with a symmetrical winding structure, the CM noise current generated in the transformer can be canceled completely. The symmetrical conditions of the transformer from the CM noise perspective are discussed, and the concept of complementary couple-turns is proposed to ensure a symmetrical winding structure for the planar transformer. The proposed complementary couple-turns offers a simple and cost-effective solution for reducing CM noise in the SPWT configuration based FB *LLC* converter without using any additional components.

This article is organized as follows: Section II provides an analysis of CM noise in conventional FB *LLC* converters, which reveals that the different  $dv/dt$  characteristics of transformer primary winding terminals lead to noncancelable CM noise currents, resulting in degraded CM EMI performance. Section III presents the SPWT configuration for the FB *LLC* converter and develops a CM noise model, which demonstrates that the CM noise in the transformer with SPWT configuration can be canceled completely by ensuring a symmetrical winding arrangement. In Section IV, the concept of complementary couple-turns is proposed to ensure a symmetrical winding arrangement for the planar transformer. Section V discusses the influences of SPWT configuration on the FB *LLC* converter, including transformer leakage inductance, transformer winding loss, and voltage conversion ratio. Section VI presents experimental verification, and Section VII concludes the article.

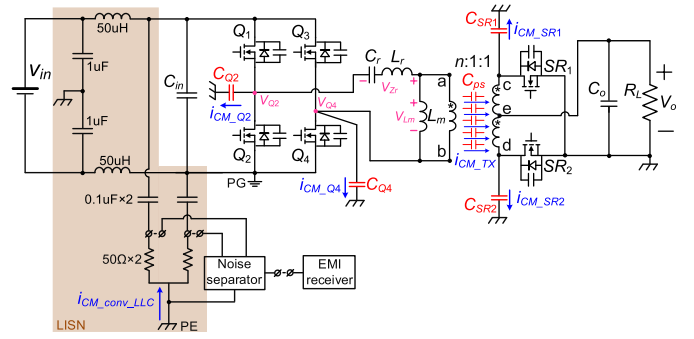


Fig. 1. CM noise propagation paths of conventional FB *LLC* resonant converter.

## II. CM NOISE ANALYSIS OF CONVENTIONAL FB *LLC* RESONANT CONVERTER

Fig. 1 depicts the CM noise propagation paths of the conventional FB *LLC* converter. During the conducted EMI measurement, the secondary ground (SG) is connected to the protective earth (PE). The CM noise currents generated by the switching nodes will couple into the PE via parasitic capacitances, which can be detected by the line impedance stabilization network (LISN). The LISN, as a passive network, serves the purpose of isolating the testing system with a reference impedance and providing measurement points to the EMI receiver. A noise separator is utilized to effectively separate the original conducted EMI noise into its CM noise component.

As shown in Fig. 1, on the secondary side,  $i_{CM\_SR1}$  and  $i_{CM\_SR2}$  denote the CM noise currents generated by the secondary-side voltage pulsation nodes on the circuit-to-PE parasitic capacitors ( $C_{SR1}$  and  $C_{SR2}$ ). Since SG is connected to PE, they circulate back through SG instead of LISN. Hence,  $i_{CM\_SR1}$  and  $i_{CM\_SR2}$  do not contribute to the total CM noise and can be ignored.

Typically, the magnitude of the current passing through the LISN is in the range of microamperes to milliamperes. In particular, a CM current of  $40 \mu A$  at 150 kHz (which translates to  $66 \text{ dB}\mu V$  when flowing into  $50 \Omega$ ) exceeds the limits specified by EN55032 Class B (quasi-peak value). Therefore, the  $dv/dt$  of the LISN can be considered negligible compared to that of the converter's voltage pulsation nodes, and the primary ground (PG) can be treated as equivalently connected to PE from the perspective of CM noise coupling. On the primary side,  $C_{Q2}$  ( $C_{Q4}$ ) is the parasitic capacitor between the drain of MOSFET  $Q_2$  ( $Q_4$ ) and PE. By using PE as the reference point, the electric potentials of primary phase-leg midpoints are denoted by  $v_{Q2}$  and  $v_{Q4}$ . The CM noise currents generated in  $C_{Q2}$  and  $C_{Q4}$  are denoted by  $i_{CM\_Q2}$  and  $i_{CM\_Q4}$ , respectively. Given the symmetrical layouts of the two primary phase legs and the consistent packaging of the MOSFETs,  $C_{Q2}$  can be considered as equal to  $C_{Q4}$ . Since  $Q_2$  and  $Q_4$  are switched at 50% duty and  $180^\circ$  out of phase with each other,  $v_{Q2}$  and  $v_{Q4}$  have complimentary  $dv/dt$  characteristics. When  $v_{Q2}$  has a positive  $dv/dt$ ,  $v_{Q4}$  will have a negative  $dv/dt$  with the same amplitude. Therefore,  $i_{CM\_Q2}$  and  $i_{CM\_Q4}$  will be canceled by each other.  $i_{CM\_Q2}$  and  $i_{CM\_Q4}$  are removed from the following CM noise analysis.

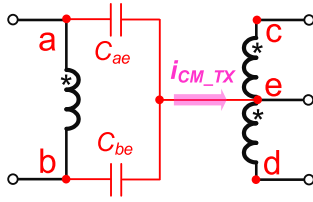


Fig. 2. Lumped interwinding capacitance mode of transformer in conventional FB LLC resonant converter.

According to the above analysis, the total CM noise current  $i_{CM\_conv\_LLC}$  is dominated by  $i_{CM\_TX}$ .  $i_{CM\_TX}$  represents the total CM noise displacement current flowing through the distributed interwinding capacitance  $C_{ps}$  of the transformer.  $i_{CM\_TX}$  is related to the electric potentials of the transformer winding terminals and parasitic interwinding capacitance of the transformer. In order to quantitatively analyze  $i_{CM\_TX}$ , the parasitic interwinding capacitance model of the transformer has been developed. By ignoring the effect of the transformer's leakage inductance, the two-capacitor model can be used to characterize the interwinding capacitance of a center-tapped three-winding transformer [24]. As shown in Fig. 2,  $C_{ae}$  and  $C_{be}$  are used to model the lumped interwinding capacitors of the transformer. Since the winding terminal  $e$  is connected to the dc output, the corresponding  $dv/dt$  can be treated as zero. Thus,  $i_{CM\_TX}$  can be calculated by (1), where  $v_a$  and  $v_b$  denote the electric potentials of transformer primary winding terminals  $a$  and  $b$  with respect to PE. When a transformer is constructed, the values of  $C_{ae}$  and  $C_{be}$  are then determined.  $v_a$  and  $v_b$  will vary with different operation conditions of the LLC converter, and then influence the CM EMI performance of the whole system

$$i_{CM\_TX} = C_{ae} \frac{dv_a}{dt} + C_{be} \frac{dv_b}{dt}. \quad (1)$$

In Fig. 1, since the winding terminal  $b$  is connected to the drain of MOSFET  $Q_4$ ,  $v_b$  is consistent with  $v_{Q4}$  which is a typical trapezoidal wave.  $v_a$  is equal to  $v_{Q2} + v_{Zr}$ , where  $v_{Zr}$  denotes the voltage across the resonant tank. So, (1) can be rewritten as shown in (2), where  $dv_{Q2}/dt$  is substituted by  $-dv_{Q4}/dt$  since  $v_{Q2}$  and  $v_{Q4}$  have complementary  $dv/dt$  characteristics. If the transformer is made symmetrically, the values of  $C_{ae}$  and  $C_{be}$  can be treated as equal; then, the influence of  $dv_{Q4}/dt$  on  $i_{CM\_TX}$  can be eliminated. However, the influence of  $v_{Zr}$  still exists

$$\begin{aligned} i_{CM\_TX} &= C_{ae} \frac{d(v_{Q2} + v_{Zr})}{dt} + C_{be} \frac{dv_{Q4}}{dt} \\ &= (C_{be} - C_{ae}) \frac{dv_{Q4}}{dt} + C_{ae} \frac{dv_{Zr}}{dt}. \end{aligned} \quad (2)$$

In conclusion, the placement of the resonant tank between the midpoint of the primary phase leg and transformer winding terminal  $a$  introduces an additional CM noise voltage variable,  $v_{Zr}$ .  $v_a$  and  $v_b$  will exhibit different  $dv/dt$  characteristics because of the influence of  $v_{Zr}$ . The CM noise displacement currents generated by  $v_a$  and  $v_b$  cannot be canceled with a symmetrical transformer winding arrangement. And CM noise is not minimized. In order to reduce the CM noise in

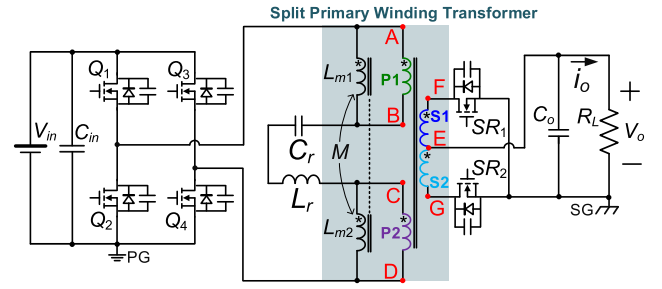


Fig. 3. FB LLC resonant converter with SPWT configuration.

the conventional FB LLC converter, the displacement currents generated by  $v_a$  and  $v_b$  via the corresponding parasitic interwinding capacitors should be eliminated.

### III. SPWT CONFIGURATION FOR FB LLC RESONANT CONVERTER

Fig. 3 shows the circuit diagram of the FB LLC converter with the SPWT configuration. Compared to conventional FB LLC converters, the transformer's primary winding is split into two separate windings  $P1$  and  $P2$ . The split two primary windings  $P1$  and  $P2$  have the same number of turns. The resonant inductor  $L_r$  and resonant capacitor  $C_r$  are placed between the primary windings  $P1$  and  $P2$ .  $L_{m1}$  ( $L_{m2}$ ) denotes the magnetizing inductance seen from the primary winding  $P1$  ( $P2$ ).  $M$  denotes the mutual inductance of  $L_{m1}$  and  $L_{m2}$ . The total primary side magnetizing inductance  $L_{m\_SPWT}$  is calculated as

$$L_{m\_SPWT} = L_{m1} + L_{m2} + 2M. \quad (3)$$

It should be noted that to ensure the same voltage gain characteristics as the conventional FB LLC converter,  $L_{m\_SPWT}$  should be equal to the transformer magnetizing inductance of the conventional FB LLC converter. The operation principle of the proposed converter is the same as that of the conventional FB LLC converter.

The CM noise model of the proposed FB LLC converter has been developed to better illustrate the cancellation mechanism of CM noise displacement currents. First, the input and output dc capacitors are treated as a short circuit within the conducted EMI frequency range and LISN is characterized as a 25-Ω resistor [29]. Based on the two-capacitor transformer winding capacitance model [24],  $C_{AE}$  and  $C_{BE}$  ( $C_{CE}$  and  $C_{DE}$ ) are used to model the lumped interwinding capacitors between the secondary windings and the primary winding  $P1$  ( $P2$ ), as shown in Fig. 4.

It should be pointed out that the interwinding capacitance between  $P1$  and  $P2$  does not introduce the CM noise current as the displacement current generated in that capacitance is confined within the transformer primary side. Then, the remaining circuit elements in Fig. 3 are replaced with CM noise sources by using substitution theory [30].  $Q_1$ ,  $Q_3$ ,  $SR_1$ ,  $SR_2$ , and resonant tank are substituted with current sources with their own current waveforms, which are denoted by  $i_{Q1}$ ,  $i_{Q3}$ ,  $i_{SR1}$ ,  $i_{SR2}$ , and  $i_{Zr}$ , respectively.  $Q_2$ ,  $Q_4$ , and primary winding  $P1$  are substituted with voltage sources with their

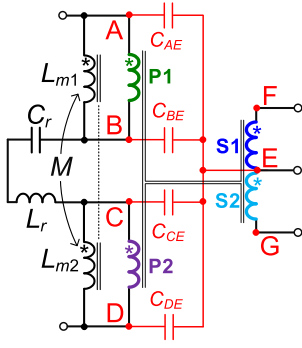


Fig. 4. Lumped interwinding capacitance model of transformer in proposed FB LLC resonant converter.

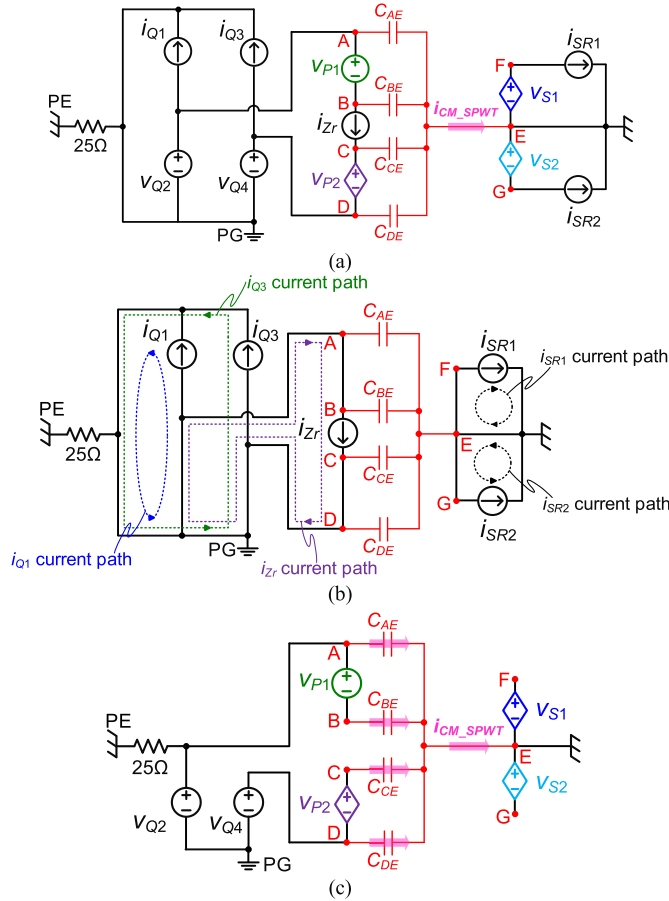


Fig. 5. CM noise equivalent circuits of proposed FB LLC resonant converter with SPWT configuration. (a) Equivalent CM noise coupling circuit by applying substitution theory. (b) Decoupled CM noise equivalent circuit with current noise sources. (c) Decoupled CM noise equivalent circuit with voltage noise sources.

own voltage waveforms, which are denoted by  $v_{Q2}$ ,  $v_{Q4}$ , and  $v_{P1}$  respectively. Based on the transformer turns ratio, all other transformer windings are substituted with voltage-controlled voltage sources  $v_{P2}$ ,  $v_{S1}$ , and  $v_{S2}$ . Since  $L_{m1}$  and  $L_{m2}$  are in parallel with voltage sources  $v_{P1}$  and  $v_{P2}$ , they are ignored in the CM noise analysis. Finally, the CM noise model of the proposed FB LLC converter is obtained, as shown in Fig. 5(a).

In Fig. 5(a),  $i_{CM\_SPWT}$  represents the total CM noise displacement current flowing through the interwinding capacitance of the transformer. To calculate  $i_{CM\_SPWT}$ , superposition

theory is used to simplify the circuit. When analyzing one noise source, the other voltage sources are considered as short circuits and current sources are considered as open circuits. Fig. 5(b) and (c) gives the decoupled CM noise equivalent circuits with current and voltage noise sources, respectively. According to Fig. 5(b), the current paths of  $i_{Q1}$ ,  $i_{Q3}$ , and  $i_{Zr}$  are confined within the primary side. The current paths of  $i_{SR1}$  and  $i_{SR2}$  are confined within the secondary side. Hence,  $i_{Q1}$ ,  $i_{Q3}$ ,  $i_{SR1}$ ,  $i_{SR2}$ , and  $i_{Zr}$  do not contribute to  $i_{CM\_SPWT}$ , which are ignored. In Fig. 5(c),  $v_{S1}$  and  $v_{S2}$  are open, which do not generate any CM noise currents. There are four remaining CM noise sources that are  $v_{Q2}$ ,  $v_{Q4}$ ,  $v_{P1}$ , and  $v_{P2}$ . Then,  $i_{CM\_SPWT}$  can be calculated by (4).  $v_A$ ,  $v_B$ ,  $v_C$ , and  $v_D$  denote the electric potentials of transformer primary winding terminals with respect to PE, which are given in (5). As  $v_{Q2}$  and  $v_{Q4}$  are complementary (i.e.,  $v_{Q2} = -v_{Q4}$ ), it follows that  $v_A$  and  $v_D$  are also complementary (i.e.,  $v_A = -v_D$ ). Furthermore, since the split two primary windings have the same number of turns, by ignoring the leakage inductance,  $v_{P1} = v_{P2}$ . Thus,  $v_B = v_{Q2} - v_{P1} = -v_{Q4} - v_{P2}$ , which implies  $v_B$  and  $v_C$  are also complementary (i.e.,  $v_B = -v_C$ ). Based on this, (4) can be rewritten by (6). It is observed that  $i_{CM\_SPWT}$  can be fully canceled if the transformer is made symmetrically, which means  $C_{AE} = C_{DE}$  and  $C_{BE} = C_{CE}$ . As a result, the CM noise current generated in  $C_{AE}$  can be canceled by that generated in  $C_{DE}$ , and the CM noise current generated in  $C_{BE}$  can be canceled by that generated in  $C_{CE}$ , thereby resulting in a net CM noise current of zero

$$i_{CM\_SPWT} = C_{AE} \frac{dv_A}{dt} + C_{DE} \frac{dv_D}{dt} + C_{BE} \frac{dv_B}{dt} + C_{CE} \frac{dv_C}{dt} \quad (4)$$

$$\begin{cases} v_A = v_{Q2} \\ v_B = v_{Q2} - v_{P1} \\ v_C = v_{Q4} + v_{P2} \\ v_D = v_{Q4} \end{cases} \quad (5)$$

$$i_{CM\_SPWT} = (C_{AE} - C_{DE}) \frac{dv_A}{dt} + (C_{BE} - C_{CE}) \frac{dv_B}{dt}. \quad (6)$$

In some applications with fixed voltage gain requirements, the LLC resonant inductance is typically realized by utilizing the leakage inductance of the transformer. This, however, does not compromise the effectiveness of the proposed SPWT configuration in reducing CM noise. As shown in Fig. 5(c), for winding P1 (P2), its leakage inductance is in series with the voltage source  $v_{P1}$  ( $v_{P2}$ ). When the transformer is symmetrically wound, the leakage inductances of P1 and P2 can be considered equal. Consequently, the voltage drop caused by the leakage inductances of P1 and P2 is the same, as they carry identical resonant currents. As a result,  $v_B$  and  $v_C$  remain complementary, allowing CM noise currents in  $C_{BE}$  and  $C_{CE}$  to mutually cancel each other.

As discussed above, achieving a symmetrical winding arrangement is crucial for effectively reducing the CM noise displacement current generated in the transformer interwinding capacitance when utilizing the SPWT configuration. Specifically, the symmetrical condition refers to the equality of  $C_{AE}$  and  $C_{DE}$  as well as  $C_{BE}$  and  $C_{CE}$ .



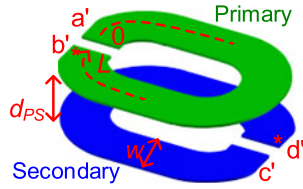


Fig. 6. Three-dimensional model of couple-turn when the layout is symmetrical.

The planar transformer structure is widely employed in LLC resonant converters due to its low height, low leakage inductance, high repeatability, and excellent thermal characteristics [31], [32]. Compared to the wire-wound transformer, the planar transformer typically features a large interwinding capacitance between overlapping primary and secondary winding turns. Therefore, it is crucial to take this large parasitic interwinding capacitance into consideration to ensure the symmetrical winding arrangement for the planar transformer. However, the parasitic interwinding capacitance model of the transformer in Fig. 4 does not reflect the effects of parasitic capacitances between each winding turn, and thus cannot guide the symmetrical winding arrangement of the planar transformer. In Section IV, the concept of couple-turn and its one-capacitor model will be reviewed, and an example analysis of symmetrical winding arrangement for the planar transformer will be presented. Finally, the concept of complementary couple-turns will be proposed to ensure the symmetrical winding arrangement for the planar transformer.

#### IV. DESIGN OF SYMMETRICAL PLANAR TRANSFORMER FOR CM NOISE MITIGATION WHEN USING SPWT CONFIGURATION

##### A. Review of Couple-Turn and Its One-Capacitor Model

Fig. 6 gives the 3-D model of a couple-turn in the planar transformer [25]. Couple-turn denotes a pair of overlapping winding turns that belong to the primary and secondary winding, respectively. It is assumed that the overlapping primary and secondary winding turns have a symmetrical layout. Hence, the parasitic structural interwinding capacitance  $C_{\text{struct}}$  of the couple-turn can be calculated by (7), where  $\epsilon_0$  denotes the permittivity of vacuum,  $\epsilon_{\text{Insul}}$  denotes the relative permittivity of the insulation material,  $d_{\text{PS}}$  denotes the distance between two winding turns, and  $L$  and  $w$  denote the length and width of the winding turns

$$C_{\text{struct}} = \epsilon_0 \epsilon_{\text{Insul}} \frac{w \cdot L}{d_{\text{PS}}}. \quad (7)$$

According to the one-capacitor couple-turn model derived in [25], from the CM noise perspective, the parasitic structural interwinding capacitance of the couple-turn can be equivalently placed between a pair of corresponding terminals. There are two types of one-capacitor couple-turn models as shown in Fig. 7. Four terminals of the couple-turn are denoted by  $a'$ ,  $b'$ ,  $c'$ , and  $d'$ , which correspond to the terminal sequence letters in Fig. 6. Terminals  $a'$  and  $c'$  ( $b'$  and  $d'$ ) on the couple-turn are a pair of corresponding terminals.  $i_{\text{CM\_couple-turn}}$  denotes the CM noise current generated in the couple-turn. Either of the two types of models in Fig. 7 can be used to analyze

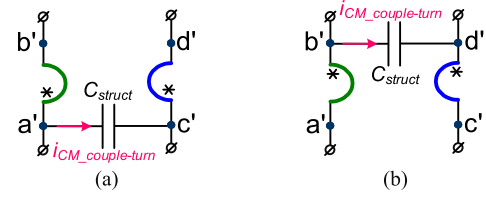


Fig. 7. Two types of one-capacitor models of couple-turn. (a)  $C_{\text{struct}}$  between corresponding terminals  $a'$  and  $c'$ . (b)  $C_{\text{struct}}$  between corresponding terminals  $b'$  and  $d'$ .

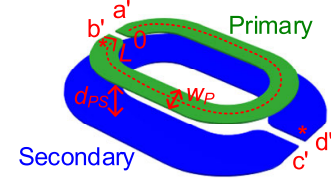


Fig. 8. Three-dimensional model of couple-turn when the layout is asymmetrical.

and characterize the CM noise current in the couple-turn. The selection criterion aims to acquire a CM noise model of the planar transformer that enables straightforward analysis.

Asymmetric layouts of couple-turns are also common in the design of planar transformers. For example, when the secondary winding of the transformer has one turn per layer while the primary winding has multiple turns per layer, the couple-turns formed by the turns of the primary and secondary winding will inevitably have an asymmetric layout. It should be noted that in this case, the one-capacitor couple-turn model is still valid. When calculating the structural capacitance of the couple-turn, the nonoverlapping area needs to be removed. Fig. 8 gives a typical example when the layout of the couple-turn is asymmetrical and  $C_{\text{struct}}$  can be recalculated as shown in (8), where  $w_P$  denotes the width of the primary winding turn. It is noted that the edge effect may introduce additional fringing capacitance [33]. The following equation maintains its accuracy when most of the electric field energies are confined within the overlapping areas of the two winding turns:

$$C_{\text{struct}} = \epsilon_0 \epsilon_{\text{Insul}} \frac{w_P \cdot L}{d_{\text{PS}}}. \quad (8)$$

##### B. Example Analysis of Symmetrical Winding Arrangement for Planar Transformer

A printed circuit board (PCB)-winding-based planar transformer with a turns ratio of 8:2:2 is used here as an example to demonstrate the effectiveness of the proposed SPWT configuration. Two examples are analyzed which are both using the sandwich winding structure but different implementations of primary winding turns.

1) *Example Planar Transformer #1*: The sandwich winding arrangement and schematic of example planar transformer #1 are shown in Fig. 9(a) and (b), respectively. The connections of winding terminals (A, B, C, D, E, F, and G) are shown in Fig. 3. This transformer includes two couple-turns:  $P1\_4-S1\_2$  and  $P2\_4-S2\_2$ . Each turn in both the primary and secondary windings is implemented using a single layer. It is assumed that all turns have the same length and width, and the structural interwinding capacitances of the couple-turns  $P1\_4-S1\_2$  and

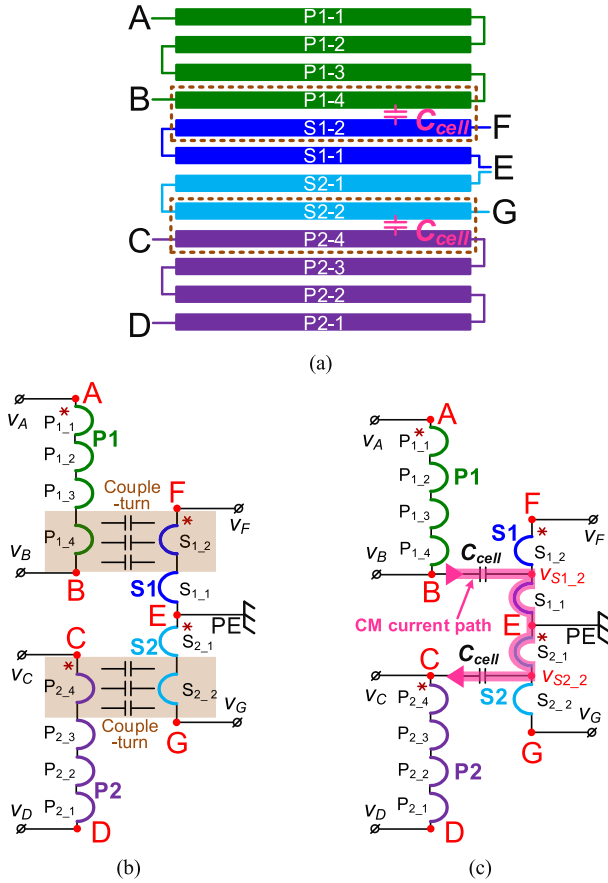


Fig. 9. Example planar transformer #1. (a) Transformer winding arrangement. (b) Transformer schematic. (c) CM noise current propagation path of transformer.

$P2_4-S2_2$  are considered equal by using the same insulation material with equal thickness, which are both denoted by  $C_{cell}$ .

Utilizing the one-capacitor couple-turn model, a lumped interwinding capacitance model of transformer #1 is shown in Fig. 9(c). Here,  $v_B$  and  $v_{S1_2}$  ( $v_C$  and  $v_{S2_2}$ ) denote the electric potentials of corresponding terminals for the couple-turn  $P1_4-S1_2$  ( $P2_4-S2_2$ ). The CM noise currents generated in couple-turns  $P1_4-S1_2$  and  $P2_4-S2_2$  are denoted by  $i_{CM\#1\_P1_4-S1_2}$  and  $i_{CM\#1\_P2_4-S2_2}$ , which can be calculated using (9) and (10), respectively,

$$i_{CM\#1\_P1_4-S1_2} = C_{cell} \frac{d(v_B - v_{S1_2})}{dt} \quad (9)$$

$$i_{CM\#1\_P2_4-S2_2} = C_{cell} \frac{d(v_C - v_{S2_2})}{dt}. \quad (10)$$

As the value of the winding turn resistance is significantly smaller than that of the inductance, the voltage difference between any two adjacent winding turns can be considered as constant. Consequently,  $v_{S1_2}$  and  $v_{S2_2}$  are calculated as  $v_F/2$  and  $v_G/2$  which are complementary (i.e.,  $v_{S1_2} = -v_{S2_2}$ ), and similarly,  $v_B$  and  $v_C$  are also complementary (i.e.,  $v_B = -v_C$ ). As a result,  $i_{CM\#1\_P1_4-S1_2} = -i_{CM\#1\_P2_4-S2_2}$ , indicating the CM noise current generated in couple-turn  $P1_4-S1_2$  can be completely canceled by the CM noise current generated in couple-turn  $P2_4-S2_2$ . The CM current path shown in Fig. 9(c) illustrates that there is no additional CM current

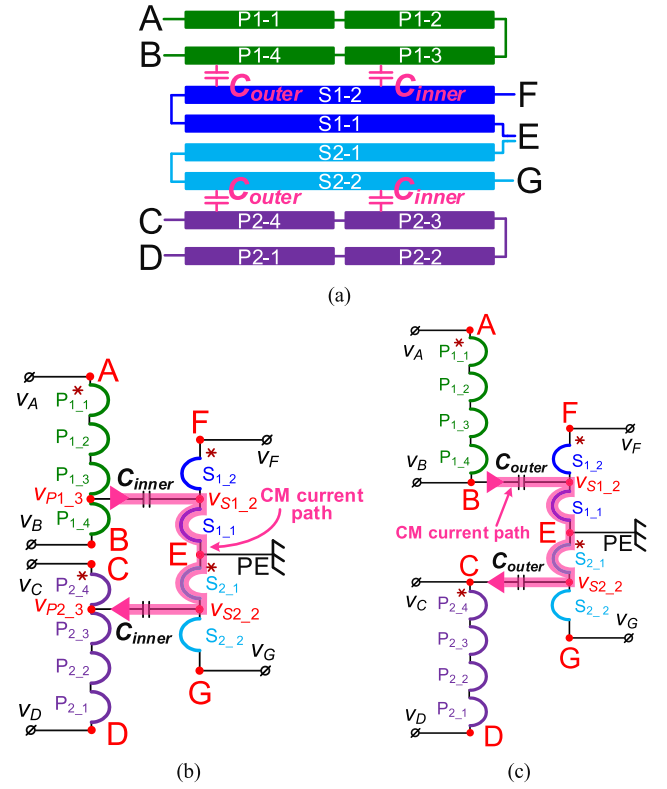


Fig. 10. Example planar transformer #2. (a) Transformer winding arrangement. (b) Propagation path of CM noise currents generated in couple-turns  $P1_3-S1_2$  and  $P2_3-S2_2$ . (c) Propagation path of CM noise currents generated in couple-turns  $P1_4-S1_2$  and  $P2_4-S2_2$ .

coupling into the secondary side, leading to a net CM noise current of zero. In conclusion, transformer #1 is symmetrical from the CM noise perspective.

2) *Example Planar Transformer #2*: Fig. 10(a) illustrate the winding arrangement of example planar transformer #2. Different from transformer #1, the primary winding turns are implemented with two turns per layer. There are four couple-turns which are  $P1_4-S1_2$ ,  $P1_3-S1_2$ ,  $P2_4-S2_2$ , and  $P2_3-S2_2$ . It is noted that couple-turns  $P1_4-S1_2$  and  $P2_4-S2_2$  have the same structural interwinding capacitance since they have the same overlapping area and the same isolation material with equal thickness. The conclusion is the same for the couple-turns  $P1_3-S1_2$  and  $P2_3-S2_2$ . The structural interwinding capacitances of couple-turns  $P1_4-S1_2$  and  $P2_4-S2_2$  ( $P1_3-S1_2$  and  $P2_3-S2_2$ ) are denoted by  $C_{outer}$  ( $C_{inner}$ ).

Fig. 10(b) gives the selected one-capacitor models of couple-turns  $P1_3-S1_2$  and  $P2_3-S2_2$ .  $v_{P1_3}$  and  $v_{S1_2}$  ( $v_{P2_3}$  and  $v_{S2_2}$ ) are the electric potentials of corresponding terminals for the couple-turn  $P1_3-S1_2$  ( $P2_3-S2_2$ ). The CM noise currents generated in these two couple-turns are denoted by  $i_{CM\#2\_P1_3-S1_2}$  and  $i_{CM\#2\_P2_3-S2_2}$ , which can be calculated as shown in (11) and (12), respectively

$$i_{CM\#2\_P1_3-S1_2} = C_{inner} \frac{d(v_{P1_3} - v_{S1_2})}{dt} \quad (11)$$

$$i_{CM\#2\_P2_3-S2_2} = C_{inner} \frac{d(v_{P2_3} - v_{S2_2})}{dt}. \quad (12)$$

Assuming a constant voltage difference between any two adjacent primary winding turns,  $v_{P1\_3}$  and  $v_{P2\_3}$  are calculated as shown in (13). As a result of the complementary electric potentials of  $v_A$  and  $v_D$ ,  $v_B$ , and  $v_C$ , the potentials of  $v_{P1\_3}$  and  $v_{P2\_3}$  are complementary (i.e.,  $v_{P1\_3} = -v_{P2\_3}$ ). Additionally, since  $v_{S1\_2}$  and  $v_{S2\_2}$  are complementary as well (i.e.,  $v_{S1\_2} = -v_{S2\_2}$ ),  $i_{CM\#2\_P1\_3-S1\_2}$  and  $i_{CM\#2\_P2\_3-S2\_2}$  can be completely canceled by each other

$$\begin{cases} v_{P1\_3} = v_A - 3 \frac{(v_A - v_B)}{4} = \frac{v_A}{4} + \frac{3v_B}{4} \\ v_{P2\_3} = v_D + 3 \frac{(v_C - v_D)}{4} = \frac{v_D}{4} + \frac{3v_C}{4} \end{cases} \quad (13)$$

Fig. 10(c) gives the selected one-capacitor models of couple-turns  $P1\_4-S1\_2$  and  $P2\_4-S2\_2$ .  $v_B$  and  $v_{S1\_2}$  ( $v_C$  and  $v_{S2\_2}$ ) are the electric potentials of corresponding terminals for the couple-turn  $P1\_4-S1\_2$  ( $P2\_4-S2\_2$ ). The CM noise currents generated in these two couple-turns are denoted by  $i_{CM\#2\_P1\_4-S1\_2}$  and  $i_{CM\#2\_P2\_4-S2\_2}$ , which can be calculated as shown in (14) and (15), respectively. Owing to the complementary electric potentials of  $v_B$  and  $v_C$ ,  $v_{S1\_2}$  and  $v_{S2\_2}$ ,  $i_{CM\#2\_P1\_4-S1\_2}$ , and  $i_{CM\#2\_P2\_4-S2\_2}$  can be completely canceled by each other. Therefore, the total CM noise displacement current generated in transformer #2 is zero, which indicates that transformer #2 is symmetrical from the CM noise perspective

$$i_{CM\#2\_P1\_4-S1\_2} = C_{outer} \frac{d(v_B - v_{S1\_2})}{dt} \quad (14)$$

$$i_{CM\#2\_P2\_4-S2\_2} = C_{outer} \frac{d(v_C - v_{S2\_2})}{dt} \quad (15)$$

### C. Concept of Complementary Couple-Turns

The concept of complementary couple-turns is proposed in this part. Complementary couple-turns refer to a pair of couple-turns that generate complementary CM noise currents, which can be completely canceled by each other. For instance, planar transformer #1,  $P1\_4-S1\_2$  and  $P2\_4-S2\_2$  are a pair of complementary couple-turns. Similarly, as shown in example planar transformer #2,  $P1\_4-S1\_2$  and  $P2\_4-S2\_2$  ( $P1\_3-S1\_2$  and  $P2\_3-S2\_2$ ) are also a pair of complementary couple-turns.

In SPWT configuration-based center-tapped planar transformer, there are two types of complementary couple-turns, as shown in Fig. 11(a) and (b). Fig. 11(a) shows the complementary couple-turns  $P1\_m-S1\_n$  and  $P2\_m-S2\_n$ . Fig. 11(b) shows the complementary couple-turns  $P1\_m-S2\_n$  and  $P2\_m-S1\_n$ .  $P1\_m$  ( $P2\_m$ ) is defined as the  $m$ th primary winding turn of  $P1$  ( $P2$ ) from terminal  $A$  ( $D$ ).  $S1\_n$  ( $S2\_n$ ) is defined as the  $n$ th secondary winding turn of  $S1$  ( $S2$ ) from terminal  $E$ .  $N_s$  denotes the turns number of secondary windings  $S1$  and  $S2$ .  $N_{P1}$  and  $N_{P2}$  denote the turns number of primary windings  $P1$  and  $P2$ , respectively.

In Fig. 11, the corresponding terminals of all complementary couple-turns are denoted by black dots. It should be noted that the difference between couple-turn  $P1\_m-S1\_n$  in Fig. 11(a) and couple-turn  $P1\_m-S2\_n$  in Fig. 11(b) lies in the distribution of their corresponding terminals. Specifically, in  $P1\_m-S1\_n$ , the corresponding terminals of the

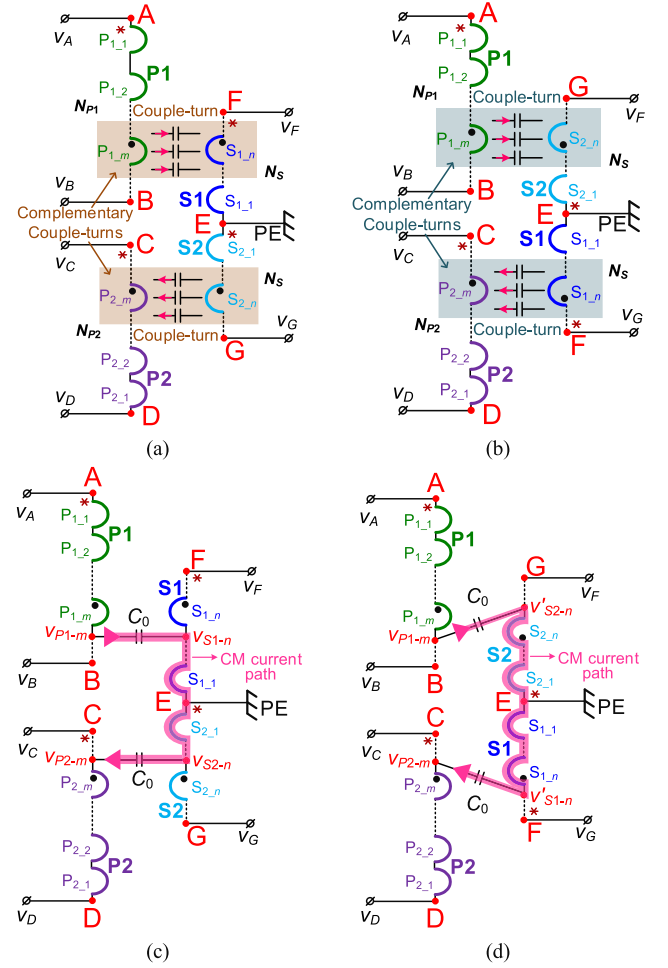


Fig. 11. Two types of complementary couple-turns. (a) Complementary couple-turns  $P1\_m-S1\_n$  and  $P2\_m-S2\_n$ . (b) Complementary couple-turns  $P1\_m-S2\_n$  and  $P2\_m-S1\_n$ . (c) Propagation path of CM noise currents generated in  $P1\_m-S1\_n$  and  $P2\_m-S2\_n$ . (d) Propagation path of CM noise currents generated in  $P1\_m-S2\_n$  and  $P2\_m-S1\_n$ .

primary and secondary winding turns are oriented in the same direction, while in  $P1\_m-S2\_n$ , they are oriented in opposite directions. In other words, the  $dv/dt$  phase of the primary and secondary winding turns are the same in  $P1\_m-S1\_n$ , but opposite in  $P1\_m-S2\_n$ . As a result, there will be different CM noise behaviors for the couple-turns  $P1\_m-S1\_n$  and  $P1\_m-S2\_n$ , which is the fundamental reason for the existence of two types of complementary couple-turns.

Based on the one-capacitor couple-turn model, Fig. 11(c) and (d) gives the lumped interwinding capacitance model of couple-turns shown in Fig. 11(a) and (b), respectively. In Fig. 11(c),  $v_{P1\_m}$  and  $v_{S1\_n}$  ( $v_{P2\_m}$  and  $v_{S2\_n}$ ) denote the electric potentials of corresponding terminals for the couple-turn  $P1\_m-S1\_n$  ( $P2\_m-S2\_n$ ). In Fig. 11(d),  $v_{P1\_m}$  and  $v'_{S2\_n}$  ( $v_{P2\_m}$  and  $v'_{S1\_n}$ ) denote the electric potentials of corresponding terminals for the couple-turn  $P1\_m-S2\_n$  ( $P2\_m-S1\_n$ ). By ignoring the impact of the leakage inductance and assuming a unit coupling coefficient, the voltage difference between any two adjacent winding turns is considered as a constant value, denoted as  $\Delta v$ , which can be calculated by (16).  $v_{P1\_m}$ ,  $v_{P2\_m}$ ,  $v_{S1\_n}$ ,  $v_{S2\_n}$ ,  $v'_{S1\_n}$ , and  $v'_{S2\_n}$  are calculated accordingly as shown in (17)–(22). The CM noise currents

generated in couple-turns  $P1\_m-S1\_n$  and  $P2\_m-S2\_n$  are denoted by  $i_{CM\_P1\_m-S1\_n}$  and  $i_{CM\_P2\_m-S2\_n}$ , which can be calculated as shown in (23) and (24), by assuming a constant parasitic structural interwinding capacitance  $C_0$  of each couple-turn. Based on (23) and (24), since  $v_A = -v_D$ , it can be concluded that  $i_{CM\_P1\_m-S1\_n} = -i_{CM\_P2\_m-S2\_n}$ , implying that couple-turns  $P1\_m-S1\_n$  and  $P2\_m-S2\_n$  have complementary CM noise displacement currents that can be canceled by each other. Hence,  $P1\_m-S1\_n$  and  $P2\_m-S2\_n$  are a pair of complementary couple-turns

$$\begin{aligned}\Delta v &= \frac{v_A - v_B}{N_{P1}} = \frac{v_C - v_D}{N_{P2}} \\ &= \frac{v_F - v_E}{N_S} = \frac{v_E - v_G}{N_S}\end{aligned}\quad (16)$$

$$v_{P1\_m} = v_A - m\Delta v \quad (17)$$

$$v_{P2\_m} = v_D + m\Delta v \quad (18)$$

$$v_{S1\_n} = (n-1)\Delta v \quad (19)$$

$$v_{S2\_n} = -(n-1)\Delta v \quad (20)$$

$$v'_{S1\_n} = n\Delta v \quad (21)$$

$$v'_{S2\_n} = -n\Delta v \quad (22)$$

$$\begin{aligned}i_{CM\_P1\_m-S1\_n} &= C_0 \frac{d(v_{P1\_m} - v_{S1\_n})}{dt} \\ &= C_0 \frac{d(v_A - (m+n-1)\Delta v)}{dt}\end{aligned}\quad (23)$$

$$\begin{aligned}i_{CM\_P2\_m-S2\_n} &= C_0 \frac{d(v_{P2\_m} - v_{S2\_n})}{dt} \\ &= C_0 \frac{d(v_D + (m+n-1)\Delta v)}{dt}.\end{aligned}\quad (24)$$

Likewise, based on Fig. 11(d), the CM noise displacement currents generated in couple-turns  $P1\_m-S2\_n$  and  $P2\_m-S1\_n$  are given in (25) and (26). Since  $v_A = -v_D$ , it can be concluded that  $i_{CM\_P1\_m-S2\_n} = -i_{CM\_P2\_m-S1\_n}$ , implying that  $P1\_m-S2\_n$  and  $P2\_m-S1\_n$  are also a pair of complementary couple-turns

$$\begin{aligned}i_{CM\_P1\_m-S2\_n} &= C_0 \frac{d(v_{P1\_m} - v'_{S2\_n})}{dt} \\ &= C_0 \frac{d(v_A - (m-n)\Delta v)}{dt}\end{aligned}\quad (25)$$

$$\begin{aligned}i_{CM\_P2\_m-S1\_n} &= C_0 \frac{d(v_{P2\_m} - v'_{S1\_n})}{dt} \\ &= C_0 \frac{d(v_D + (m-n)\Delta v)}{dt}.\end{aligned}\quad (26)$$

The use of complementary couple-turns enables the effective reduction of CM noise in planar transformers. The cancellation of CM noise is achieved by designing the winding arrangement and interwinding capacitance in such a way that the CM noise currents generated in the complementary couple-turns are equal in magnitude and opposite in phase.

#### D. Symmetrical Winding Arrangement Based on Complementary Couple-Turns

Based on the previous analysis, the planar transformer winding arrangement can be symmetrical from the CM noise perspective and the total CM noise displacement current

generated in the planar transformer can be fully canceled when the following two conditions are satisfied.

- 1) Overlapping layers should be selected based on the concept of complementary couple-turns. There are two types of complementary couple-turns:  $P1\_m-S1\_n$  and  $P2\_m-S2\_n$ , as well as  $P1\_m-S2\_n$  and  $P2\_m-S1\_n$ . Definitions for  $P1\_m-S1\_n$ ,  $P2\_m-S2\_n$ ,  $P1\_m-S2\_n$ , and  $P2\_m-S1\_n$  are provided in Fig. 11.

If the  $m$ th winding turn of  $P1$  is overlapped with the  $n$ th winding turn of  $S1$ , the  $m$ th winding turn of  $P2$  needs to be overlapped with the  $n$ th winding turn of  $S2$  so as to generate the complementary CM noise current. Likewise, if the  $m$ th winding turn of  $P1$  is overlapped with the  $n$ th winding turn of  $S2$ , the  $m$ th winding turn of  $P2$  needs to be overlapped with the  $n$ th winding turn of  $S1$ .

- 2) The complementary couple-turns should be designed to have the same parasitic structural interwinding capacitances. This is typically achieved through the symmetrical layout of complementary couple-turns. It should be noted that the thicknesses of insulation layers in most multilayer PCBs are not consistent. When constructing planar transformers using a single PCB board, attention should be given to the interlayer FR4 distance to ensure the same parasitic structural interwinding capacitances of complementary couple-turns.

Complementary couple-turns offer the advantage of utilizing the inherent coupling capacitance between the primary and secondary sides of a planar transformer to cancel out CM currents generated within the transformer. This eliminates the need for additional shielding layers or extra transformer windings. Furthermore, the utilization of complementary couple-turns is entirely compatible with the interleaved winding structure. This compatibility arises from the fact that the overlapping layers introduced by the interleaved winding structure can be harnessed to create complementary couple-turns. Consequently, the trade-off between the interleaved winding structure and the CM noise performance of the transformer is eliminated. Unlike the conventional winding methods for planar transformers mentioned in [15], [16], and [17], the overlapping primary and secondary winding layers of the transformer do not need to have identical voltage distributions. This significantly enhances the designer's flexibility when creating the structure of planar transformers. It should be pointed out that the concept of complementary couple-turns cannot be used to reduce the CM noise for the phase shift control-based FB LLC resonant converter. With the phase shift control, the electric potentials of two phase-leg midpoints change at different times, and the generated CM noise displacement currents flowing through the associated parasitic capacitance cannot be mutually canceled.

Even if the number of turns in the primary winding is odd, the proposed complementary couple-turns can still be utilized to ensure a symmetrical transformer winding arrangement when using the SPWT configuration. A planar transformer with a turns ratio of 3:1:1 is used as an example. Fig. 12 illustrates the winding arrangement of example planar transformer #3. The connections of winding terminals ( $A$ ,  $B$ ,  $C$ ,  $D$ ,  $E$ ,  $F$ ,



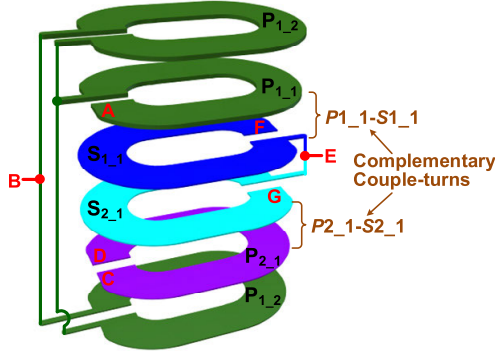


Fig. 12. Transformer winding arrangement of example planar transformer #3.

and  $G$ ) are shown in Fig. 3. In this figure,  $P1\_1-S1\_1$  and  $P2\_1-S2\_1$  represent a complementary pair of couple-turns. Based on (23) and (24), the CM noise currents generated in these two couple-turns can be calculated as shown in (27) and (28), respectively. The parasitic structural capacitances of  $P1\_1-S1\_1$  and  $P2\_1-S2\_1$  are denoted by  $C_{P1\_1-S1\_1}$  and  $C_{P2\_1-S2\_1}$ , which are considered equal by using the same insulation material with equal thickness. Since  $v_A$  and  $v_D$  are complementary (i.e.,  $v_A = -v_D$ ), it follows that  $i_{CM\#3\_P1\_1-S1\_1}$  and  $i_{CM\#3\_P2\_1-S2\_1}$  are also complementary. In conclusion, the CM noise currents generated in these two couple-turns can mutually cancel each other

$$i_{CM\#3\_P1\_1-S1\_1} = C_{P1\_1-S1\_1} \frac{d(v_A - \Delta v)}{dt} \quad (27)$$

$$i_{CM\#3\_P2\_1-S2\_1} = C_{P2\_1-S2\_1} \frac{d(v_D + \Delta v)}{dt}. \quad (28)$$

$P1\_2$  in transformer #3 is split into two parallel winding turns that are placed on the top and bottom layers, respectively.  $P1\_2$  does not overlap with the turns of the secondary winding. As a result,  $P1\_2$  does not generate any additional CM noise current, and transformer #3 remains symmetrical from the CM noise perspective.

In general, when the number of turns in the original primary winding of a planar transformer is odd, it is not possible to have an equal number of turns in both  $P1$  and  $P2$ . Specifically, if the number of turns in  $P1$  is one more than that of  $P2$  (i.e.,  $N_{P1} = N_{P2} + 1$ ), an additional CM noise displacement current will be induced by the primary winding turn  $P1_{N_{P1}}$  if it overlaps with the secondary winding turns. To avoid this issue, it is necessary to ensure that  $P1_{N_{P1}}$  does not overlap with the secondary winding turns.

## V. PRACTICAL CONSIDERATIONS

This section discusses the influences of SPWT configuration on the FB *LLC* converter, including transformer leakage inductance, transformer winding loss, and voltage conversion ratio.

In Fig. 13(a) and (c), two center-tapped planar transformers with a turns ratio of 16:1:1 are presented. Fig. 13(a) corresponds to the transformer designed for the proposed split primary winding FB *LLC* converter as shown in Fig. 3, while Fig. 13(c) corresponds to the transformer designed for the conventional FB *LLC* converter as shown in Fig. 1. For a fair comparison, apart from the different terminal connections of

TABLE I  
STACK-UP STRUCTURE OF PRIMARY WINDING PCBs

Layer	Stack up	Thickness (mm)
	Solder Mask	0.02
L1	3 OZ + Plating	0.14
	Prepreg (FR4)	0.28
L2	4 OZ	0.14
	Core (FR4)	0.47
L3	4 OZ	0.14
	Prepreg (FR4)	0.28
L4	3 OZ + Plating	0.14
	Solder Mask	0.02

the primary windings, the construction methods for these two transformers are identical. It should be pointed out that the proposed planar transformer can be rendered identical to the conventional planar transformer by short-circuiting terminals  $B$  and  $C$ , and subsequently connecting the resonant tank to terminal  $A$ . As shown in Fig. 13(c), for the conventional planar transformer, there is only one primary winding which is denoted by  $P1'$ .  $P1'_1$  is the first primary winding turn which is connected to the resonant tank.  $P1'_{16}$  is the last primary winding turn which is connected to  $Q_3$  (Source) in Fig. 1. As shown in Fig. 13(a), for the proposed planar transformer, there are two primary windings which are  $P1$  and  $P2$ .  $P1_1$  is the first primary winding turn of  $P1$ , which is connected to  $Q_1$  (Source) in Fig. 3.  $P2_1$  is the first primary winding turn of  $P2$ , which is connected to  $Q_3$  (Source) in Fig. 3. The resonant tank is connected between  $P1_8$  and  $P2_8$ , which are the last primary winding turns of  $P1$  and  $P2$ , respectively. The remaining specifications for these two transformers are identical and can be summarized as follows.

- 1) DMR96 ferrite core material from DMEGC is selected and the core size is ECW34C (customized from DMEGC). The specific structure and dimensions of ECW34C are provided in Fig. 14. There is an approximately 0.22 mm air gap in the middle of the center column and the two side columns of the magnetic core. Three air gaps are all filled with Kapton tapes.
- 2) The transformer windings are designed with a single turn per layer, each having the same width of 8 mm. Instead of the sandwich winding structure shown in Figs. 9(a) and 10(a), a partial interleaved winding structure is employed by stacking six PCBs. The choice of a partial interleaved winding structure in the final design aims to achieve lower ac losses for the transformer windings, which means higher system efficiency. Specifically, the primary windings are constructed by using four 4-layer 4 OZ PCBs with a PCB board thickness of 1.63 mm, while the secondary windings are constructed by using two 8-layer 4 OZ PCBs with a PCB board thickness of 2.41 mm. Detailed layer stack-up structures of the primary and secondary winding PCBs are provided in Tables I and II, respectively. The insulation layers between different PCBs are implemented by 0.25 mm electrical insulation papers with a relative permittivity of 2.6 [34].

For the proposed planar transformer, there are two pairs of complementary couple-turns which are  $P1_4-S1_1$  and  $P2_4-S2_1$ ,  $P1_5-S2_1$ , and  $P2_5-S1_1$ . Since six PCBs

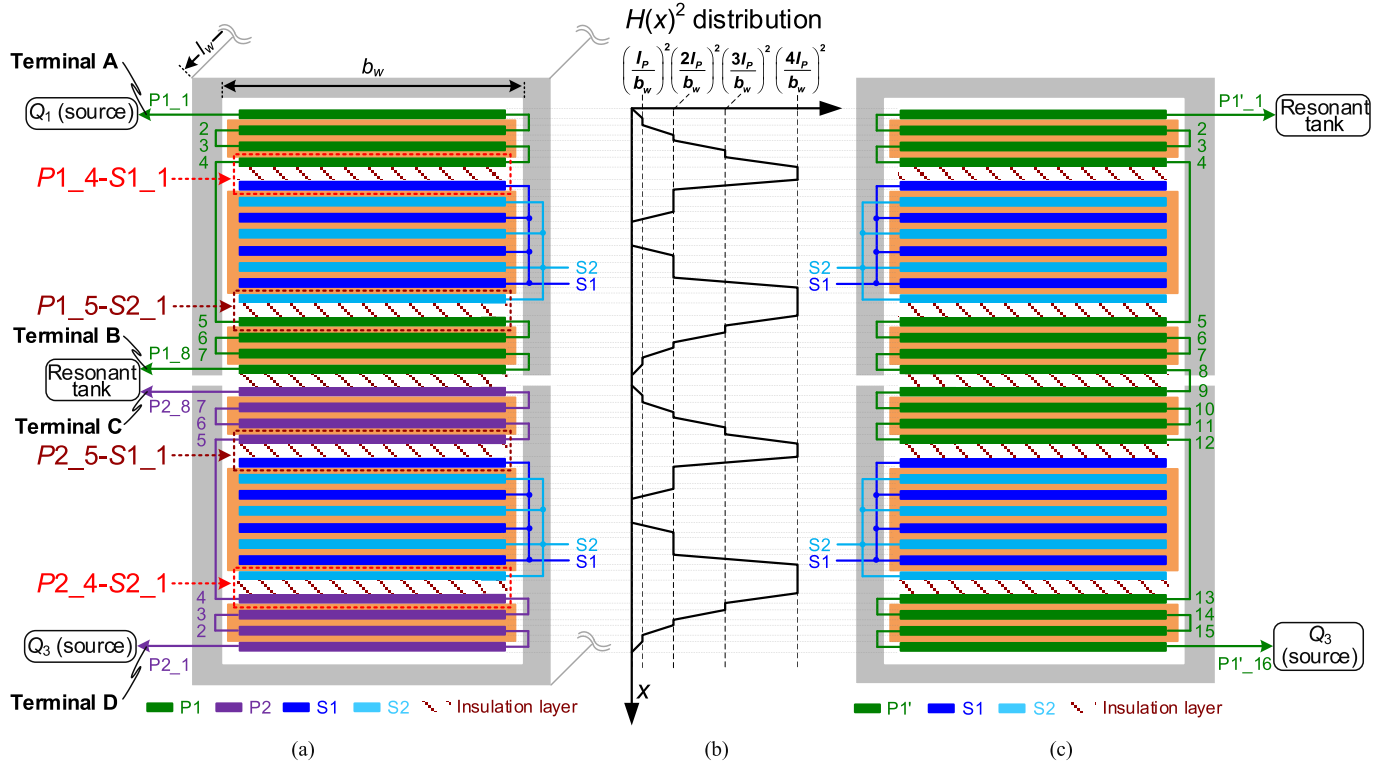


Fig. 13. (a) Transformer winding arrangement and terminal connections of proposed FB LLC resonant converter. Refer to Fig. 3 for locations of  $Q_1$  (source),  $Q_3$  (source), and resonant tank. (b) Distribution of  $H(x)^2$  for both proposed and conventional planar transformers. (c) Transformer winding arrangement and terminal connections of conventional FB LLC resonant converter. Refer to Fig. 1 for locations of  $Q_3$  (source) and resonant tank.

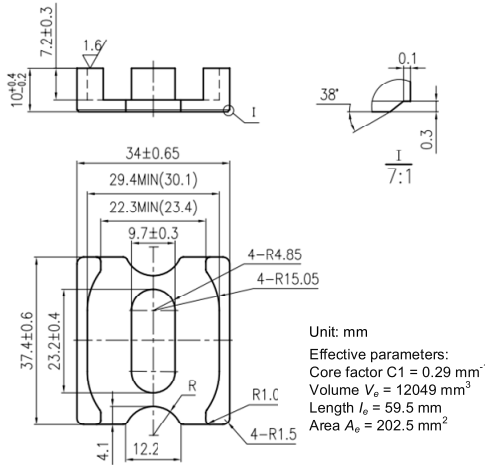


Fig. 14. Specific structure and dimensions of ECW34C magnetic core.

are stacked by using the same type of insulation material with the same thickness, the complementary couple-turns have the same parasitic structural interwinding capacitances. Thus, this planar transformer is symmetrical from the CM noise perspective and the total CM noise displacement current should be significantly reduced.

#### A. Transformer Leakage Inductance and Winding Loss

The leakage inductance referred to the primary side can be calculated by (29), demonstrating that the energy stored in the leakage inductance equals the leakage magnetic field energy. By calculating the total energy of the leakage magnetic

field, the theoretical value of the leakage inductance can be determined. Here, the total energy of the leakage magnetic field refers to the summation of energies stored in the primary winding layers, secondary winding layers, and insulation layers

$$E_{\text{energy}} = \frac{\mu_0}{2} \int_{\text{window area}} H^2 dV = \frac{1}{2} L_{\text{lk}} I_p^2 \quad (29)$$

where  $L_{\text{lk}}$  is the leakage inductance in the primary side,  $I_p$  is the current of the primary winding, and  $H$  is the magnetic field intensity in the window.

TABLE II  
STACK-UP STRUCTURE OF SECONDARY WINDING PCBs

Layer	Stack up	Thickness (mm)
	Solder Mask	0.025
L1	3 OZ + Plating	0.14
	Prepreg (FR4)	0.16
L2	4 OZ	0.14
	Prepreg (FR4)	0.12
L3	4 OZ	0.14
	Prepreg (FR4)	0.28
L4	4 OZ	0.14
	Core (FR4)	0.12
L5	4 OZ	0.14
	Prepreg (FR4)	0.28
L6	4 OZ	0.14
	Prepreg (FR4)	0.12
L7	4 OZ	0.14
	Prepreg (FR4)	0.16
L8	3 OZ + Plating	0.14
	Solder Mask	0.025

For the proposed planar transformer, because the primary windings  $P1$  and  $P2$  are connected in series, the currents in these windings are equal and denoted as  $I_p$ . Assuming the magnetic field intensity is constant in the horizontal direction, the leakage inductance can be calculated as

$$L_{lk} = \frac{\mu_0}{I_p^2} \int_V H(x)^2 dx = \frac{\mu_0 b_w l_w}{I_p^2} \int_0^x H(x)^2 dx \quad (30)$$

where  $V$  is the total volume of window area,  $b_w$  is the width of the magnetic core window,  $l_w$  is the depth of the magnetic core, and  $H(x)$  is the magnetic field intensity in the direction the geometric position  $x$  [see Fig. 13(b)]. Based on (30), the leakage inductance is proportional to the integral of the square of the magnetic field intensity. Hence, the distribution of  $H(x)^2$  provides an intuitive reflection of the magnitude of the leakage inductance. The graphical interpretation of the  $H(x)^2$  distribution is depicted in Fig. 13(b), in accordance with Ampere's circuital theorem. It is noted that secondary windings  $S1$  and  $S2$  conduct alternately for half of the switching period, and Fig. 13(b) is based on the operating scenario where  $S1$  conducts. Due to the identical winding arrangement in both the proposed and conventional planar transformers, they exhibit the same  $H(x)^2$  distribution. In other words, their leakage inductance performance is the same. The same conclusion can be drawn when analyzing the operating scenario where  $S2$  conducts.

It should be pointed out that the previous discussion does not take into account the effects of eddy current when the transformer operates under high-frequency (HF) conditions. In HF range, both the skin effect and proximity effect cause the winding current to concentrate near the conductor's surface. This phenomenon leads to an inhomogeneous distribution of  $H(x)^2$ , consequently changing the total leakage magnetic field energy.

On the other hand, the skin effect and proximity effect also contribute to increased ac resistance of the transformer windings, which can be explained by Ferreira's formula [35]

$$R_{tx\_ac} = R_{tx\_dc} \cdot (F_{skin} + F_{proximity}) \quad (31)$$

where  $F_{skin}$  and  $F_{proximity}$  represent the skin effect ratio and proximity effect ratio, respectively. Their expressions are given by

$$F_{skin} = \frac{\xi}{2} \cdot \frac{\sinh(\xi) + \sin(\xi)}{\cosh(\xi) - \cos(\xi)}, \quad \xi = \frac{h}{\delta} \quad (32)$$

$$F_{proximity} = \frac{\xi}{2} \cdot \left( \frac{2F(h)}{F(h) - F(0)} - 1 \right)^2 \cdot \left( \frac{\sinh(\xi) - \sin(\xi)}{\cosh(\xi) + \cos(\xi)} \right) \quad (33)$$

where  $h$  denotes the thickness of conductors, and  $\delta$  stands for the skin depth at the operating frequency.  $F(h)$  and  $F(0)$  correspond to the magnetomotive forces (MMFs) at the borders of the conductor, which depend on the transformer's winding arrangement. To mitigate the influence of the skin effect, the general design criterion is to ensure that the conductor thickness remains less than twice the skin depth. To mitigate the influence of the proximity effect, an interleaved structure is commonly employed in planar transformer applications. This

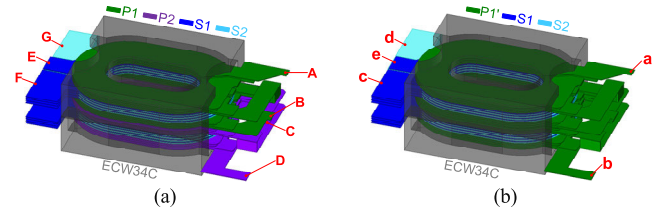


Fig. 15. Maxwell three-dimensional models of (a) proposed and (b) conventional transformers.

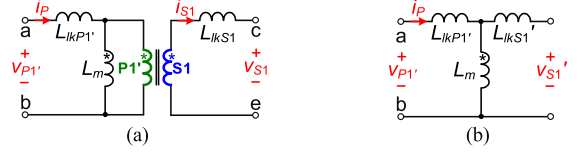


Fig. 16. (a)  $\pi$  model of conventional transformer. (b) Equivalent model used for calculating total leakage inductance.

structure reduces the MMF that drives lower  $F_{proximity}$ . Both the proposed and conventional planar transformers have equal conductor thickness for their primary and secondary windings, resulting in the same  $F_{skin}$  value under the same operating frequency. Furthermore, their winding arrangements are identical, theoretically yielding the same MMF distribution and the same  $F_{proximity}$  value under the same operating frequency. Consequently, these two transformers have equal additional losses introduced by the skin and proximity effects.

To quantitatively analyze the leakage inductance and winding loss, a 3-D finite element analysis (FEA) simulation is conducted using Maxwell software. Fig. 15 presents 3-D models of the proposed and conventional transformers. The interlayer distances of transformer winding turns are selected based on Tables I and II. To save simulation time, PCB vias are removed and the rounded corners of the magnetic core are replaced by right angles. The Maxwell solver is eddy current type and the excitation is 150 kHz current. As mentioned earlier, secondary windings  $S1$  and  $S2$  conduct alternately during half of the switching period. Therefore, each simulation model in Fig. 15 is executed twice to determine the transformer's leakage inductance and ac/dc resistance ratio.

1) *Simulation of Leakage Inductance:* Fig. 16(a) presents the  $\pi$  model of the conventional transformer, corresponding to the operating scenario where  $S1$  conducts.  $L'_{lkP1}$  and  $L'_{lkS1}$  denote the leakage inductances for the primary winding  $P1'$  and secondary winding  $S1$ , respectively. The total leakage inductance referred to the primary side is denoted by  $L'_{lkP\_S1\_conv}$ , which can be measured from the primary winding terminals when the secondary winding  $S1$  is short-circuited. Notably,  $L'_{lkP\_S1\_conv}$  includes both the primary leakage inductance  $L'_{lkP1}$  and secondary reflected leakage inductance. When  $S1$  is short-circuited, the secondary leakage inductance  $L'_{lkS1}$  is reflected to the primary side, resulting in  $L'_{lkS1}$ , as illustrated in Fig. 16(b). Consequently,  $L'_{lkP\_S1\_conv}$  is approximated as  $L'_{lkP1} + L'_{lkS1}$ .

Fig. 17(a) presents the  $\pi$  model of the proposed transformer, corresponding to the operating scenario where  $S1$  conducts.  $L'_{lkP1}$  and  $L'_{lkP2}$  denote the leakage inductances for the primary windings. The total leakage inductance referred to the primary side is denoted by  $L'_{lkP\_S1\_prop}$ , which can also be measured from the primary winding terminals when the

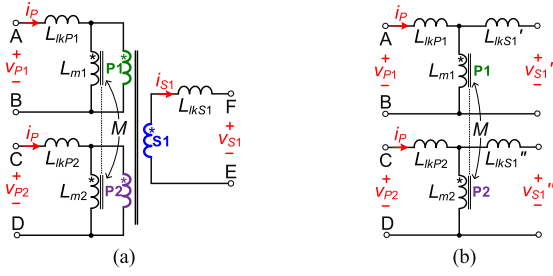


Fig. 17. (a)  $\pi$  model of proposed transformer. (b) Equivalent model used for calculating total leakage inductance.

TABLE III

SIMULATED LEAKAGE INDUCTANCES (UNIT: $\mu\text{H}$ )		
Conventional	$L_{lkP\_S1\_conv}$	1.14
	$L_{lkP\_S2\_conv}$	1.13
Proposed	$L_{lkP\_S1\_prop}$	1.14
	$L_{lkP\_S2\_prop}$	1.13

TABLE IV

SIMULATED AC/DC RESISTANCE RATIOS AT 150 kHz		
	Conventional	Proposed
Primary winding(s)	1.78	1.78
Secondary winding S1	2.141	2.139
Secondary winding S2	2.096	2.1

secondary winding S1 is short-circuited. Notably,  $L_{lkP\_S1\_prop}$  includes both the primary leakage inductances and secondary reflected leakage inductances. When S1 is short-circuited, the secondary leakage inductance  $L_{lkS1}$  is reflected to the primary side, resulting in  $L'_{lkS}$  and  $L''_{lkS}$ , as illustrated in Fig. 17(b). Consequently,  $L_{lkP\_S1\_prop}$  is approximated as  $L_{lkP1} + L_{lkP2} + L'_{lkS} + L''_{lkS}$ .

The simulated total leakage inductances for the conventional and proposed transformers are provided in Table III. It can be observed that, whether S1 is conducting or S2 is conducting, the conventional and proposed planar transformers exhibit the same total leakage inductance.

2) *Simulation of AC/DC Resistance Ratio:* As shown in (31), the ac/dc resistance ratio refers to the summation of  $F_{skin}$  and  $F_{proximity}$ , which determines transformer winding losses. The benchmark for calculating the ac/dc resistance ratio is established through a 60-Hz simulation, during which the skin and proximity effects are negligible. A comparison of solid losses between simulation results at 150 kHz and 60 Hz enables a convenient determination of the ac/dc resistance ratio. The 3-D FEA simulation results are presented in Table IV. It is observed that the conventional and proposed planar transformers exhibit similar ac/dc resistance ratios for both primary and secondary windings.

In summary, the SPWT configuration-based planar transformer, when compared to the conventional planar transformer, demonstrates similar performance in terms of leakage inductance and winding loss. This similarity arises from the fact that the two primary windings in the proposed planar transformer are connected in series, ensuring identical conduction currents in both primary windings. By utilizing the same construction approach as the conventional planar transformer, the proposed transformer presents the equivalent leakage magnetic field energy and eddy current effects.

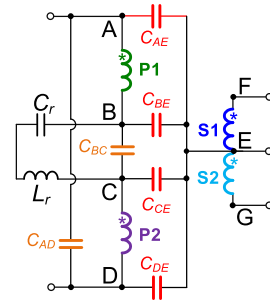


Fig. 18. Complete interwinding capacitance model of SPWT configuration based planar transformer.

## B. Voltage Conversion Ratio

The voltage regulation of *LLC* converters can be affected by interwinding capacitances when employing the SPWT configuration. As shown in Fig. 18, these capacitances include not only those between the primary and secondary windings but also capacitances between the primary windings P1 and P2. Here,  $C_{AD}$  and  $C_{BC}$  are used to model the interwinding capacitors between P1 and P2. It can be observed that  $C_{BC}$ ,  $C_{BE}$  and  $C_{CE}$  will participate in the resonance of  $L_r$  and  $C_r$ , potentially affecting the gain performance of the FB *LLC* converter under HF operation conditions.

The impedance of the resonant unit consisting of  $L_r$ ,  $C_r$ ,  $C_{BC}$ ,  $C_{BE}$ , and  $C_{CE}$  is calculated as

$$Z_{ru}(s) = \frac{C_r L_r s^2 + 1}{s(C_r C_e L_r s^2 + C_r + C_e)} \quad (34)$$

where

$$s = j\omega_s, \quad \omega_s = 2\pi f_s$$

$$C_e = C_{BC} + \frac{C_{BE} C_{CE}}{C_{BE} + C_{CE}} \quad (35)$$

where  $C_e$  represents the equivalent capacitance in parallel with the resonant tank. The impedance zero and pole of  $Z_{ru}$  are given by (36) and (37), respectively,

$$f_r = \frac{1}{2\pi\sqrt{L_r C_r}} \quad (36)$$

$$f_p = \frac{1}{2\pi\sqrt{L_r \frac{C_r C_e}{C_r + C_e}}}. \quad (37)$$

When  $f_s = f_r$ ,  $Z_{ru}$  is zero, equivalent to a short circuit, resulting in a voltage gain of 1 for the FB *LLC* converter. In contrast, when  $f_s = f_p$ ,  $Z_{ru}$  is infinite, equivalent to an open circuit, yielding a voltage gain of 0. By defining

$$k_e = \frac{C_e}{C_r}, \quad f_n = \frac{f_s}{f_r}$$

$$Z_r = j\omega_s L_r + \frac{1}{j\omega_s C_r}. \quad (38)$$

$Z_{ru}$  can be normalized and rewritten as

$$Z_{ru\_n} = \frac{Z_{ru}}{Z_r} = \frac{1}{1 + k_e - k_e f_n^2} \quad (39)$$

where  $Z_r$  represents the base impedance, corresponding to the series impedance of  $L_r$  and  $C_r$ .



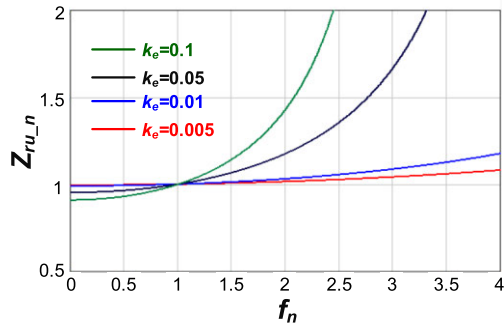


Fig. 19. Variation of  $Z_{ru_n}$  concerning frequency changes.

Fig. 19 illustrates the variation of  $Z_{ru_n}$  concerning frequency changes. Notably, as  $k_e$  increases, the deviation between  $Z_{ru}$  and  $Z_r$  becomes more pronounced, particularly at switching frequencies higher than  $f_r$ . In other words, for the same range of switching frequency variation,  $Z_{ru}$  can provide a larger range of impedance variation compared to  $Z_r$ . This implies that the FB *LLC* converter can achieve a wider voltage gain variation range, which is advantageous for wide-voltage-range applications and light-load voltage regulation. This phenomenon has been investigated in [36] and [37] and will not be further extended in this article due to the limited space. It is worth noting that the capacitors in parallel with the resonant tank in the referenced literature are additional components, whereas in this article,  $C_e$  represents the parasitic interwinding capacitance of the transformer introduced by the SPWT configuration.

In the proposed planar transformer,  $C_e$  is estimated to be around 93 pF. The derivation process is detailed in the Appendix. Combined with the designed  $C_r$  value of 17.6 nF,  $k_e$  is calculated as 0.005, corresponding to the red curve in Fig. 19. With this small  $k_e$ , the influence of  $C_e$  on the *LLC* voltage gain can be ignored. Consequently, the voltage gain of the proposed planar transformer-based FB *LLC* converter should be similar to the conventional one.

## VI. EXPERIMENTAL VERIFICATION

A 360 W FB *LLC* converter with 180–210 V input and 12 V/30 A output is studied as a typical example. This converter is originally designed for an open-frame two-stage ac–dc power supply with a 90–264 V<sub>ac</sub> input. When the input ac voltage is in low line range (90–136 V<sub>ac</sub>), the dc bus ranges from 180 to 210 V and the *LLC* converter operates in FB mode.

Fig. 20(a) shows the proposed FB *LLC* prototype. The main PCB in Fig. 20(a) is also compatible for building the conventional FB *LLC* prototype by replacing the SPWT daughter card with the conventional PCB transformer daughter card as shown in Fig. 20(b). The transformer winding arrangement and terminal connections for the proposed and conventional planar transformers are shown in Fig. 13(a) and (c), respectively. The electrical connections within the layers of the multilayer PCB board are established through PCB vias. Meanwhile, connections between different PCB boards are accomplished through soldering. Fig. 20(c)–(e) provides detailed views of the transformer windings. In Fig. 20(c) and (d), the solder joints are indicated by red rectangles, while the paths of

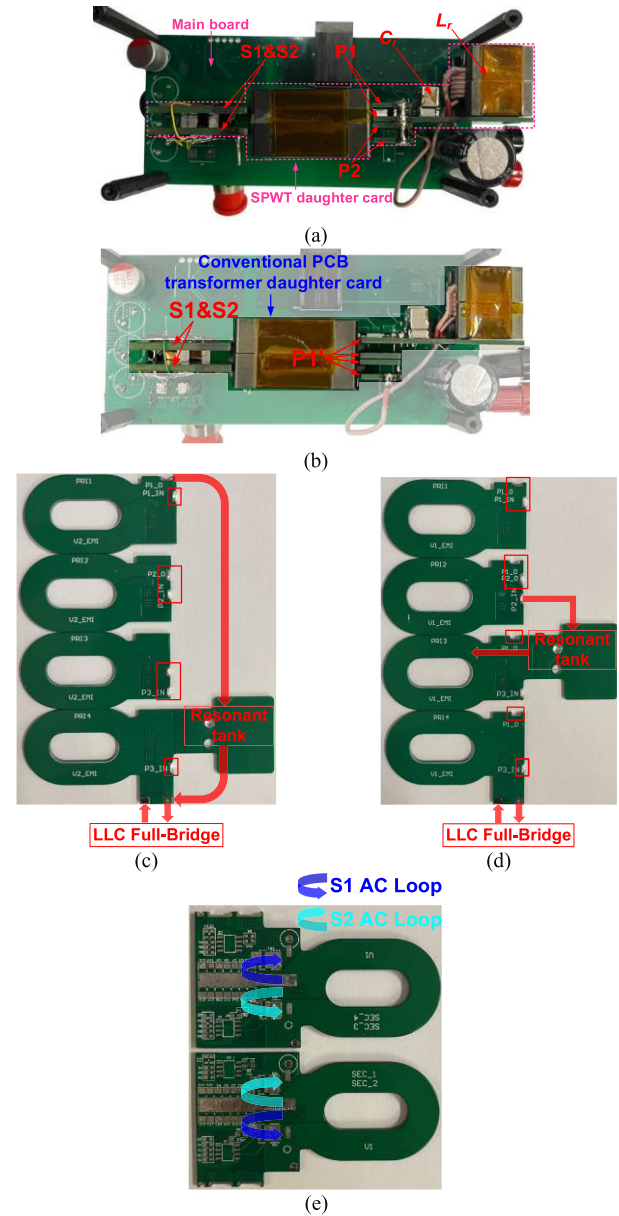


Fig. 20. Photographs of prototype. (a) Proposed SPWT daughter card. (b) Conventional PCB transformer daughter card. (c) Primary windings of proposed transformer. (d) Primary windings of conventional transformer. (e) Secondary daughter cards for both conventional and proposed transformers.

resonant currents are highlighted by red arrows. To minimize the secondary current loops, the secondary windings are constructed using two daughter cards, each having its own synchronous rectifier (SR) MOSFETs. The secondary daughter cards for the conventional and proposed transformers are identical, as shown in Fig. 20(e). Except for the planar transformer, other specifications of the conventional prototype are the same as the proposed FB *LLC* prototype, which can be found in Table V.

### A. Measured Leakage Inductance

An LCR meter (FLUKE PM6306) is used to measure the leakage inductances at 150 kHz. The total primary leakage inductances are measured by following the methods presented in the simulation section. For the conventional transformer,  $L_{lkP\_S1\_conv}$  is measured across the primary winding by

TABLE V  
SPECIFICATIONS OF FB *LLC* RESONANT CONVERTER

Parameter	Value
Resonant inductor ( $L_r$ )	62 $\mu$ H (3C97, PQ26/20, Ferroxcube) 24 turns (Litz 160x0.06 mm) Winding structure: 8-8-8
Resonant capacitor ( $C_r$ )	17.6 nF (C2225C222KZGACAU0, 8 in parallel)
Resonant frequency ( $f_r$ )	152 kHz
Primary switches ( $Q_1$ – $Q_4$ )	OSG65R125JF
Primary driver	EG3116D
Secondary SRs ( $SR_1$ , $SR_2$ )	NTMFS5C604NLT1G
SR driver	NCP4306AAZZZADR2G

TABLE VI  
MEASURED LEAKAGE INDUCTANCES (UNIT:  $\mu$ H)

		Measured	Simulated
Conventional	$L_{lkP\_S1\_conv}$	1.18	1.14
	$L_{lkP\_S2\_conv}$	1.19	1.13
Proposed	$L_{lkP\_S1\_prop}$	1.18	1.14
	$L_{lkP\_S2\_prop}$	1.19	1.13

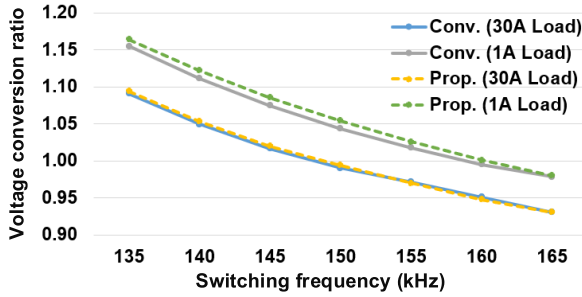


Fig. 21. Measured voltage conversion ratio.

short-circuiting secondary winding  $S1$  while leaving  $S2$  open. Similarly,  $L_{lkP\_S2\_conv}$  is measured across the primary winding by short-circuiting secondary winding  $S2$  while leaving  $S1$  open. The same method is employed to measure the leakage inductances of the proposed transformer, wherein two separate primary windings,  $P1$  and  $P2$ , were connected in series, and  $L_{lkP\_S1\_prop}$  and  $L_{lkP\_S2\_prop}$  are measured between winding terminals  $A$  and  $D$ .

Measured leakage inductances are provided in Table VI. It can be observed that, whether the secondary winding  $S1$  is conducting or the secondary winding  $S2$  is conducting, the conventional and proposed planar transformers exhibit the same total leakage inductance. Furthermore, the experimental results match well with the simulation results, with a discrepancy of only 0.04–0.06  $\mu$ H. This discrepancy mainly arises from the parasitic inductance of the short-circuit connecting wires between the secondary winding terminals. This parasitic inductance can be reflected to the transformer primary side and increase the measured value of the total leakage inductance.

### B. Measured Voltage Conversion Ratio and Efficiency

By sweeping the switching frequency from 135 to 165 kHz, the measured voltage gain curves of the proposed and conventional prototypes are shown in Fig. 21. It can be observed that they exhibit similar voltage gain performance under both 30 A full load and 1 A light load conditions. The maximum voltage

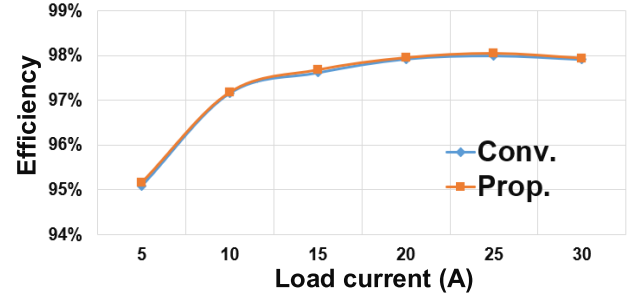


Fig. 22. Measured efficiency.  $V_{in} = 190$  V.  $V_o = 12$  V.

gain difference occurs at 135 kHz/1 A testing condition, where the voltage gain of the conventional prototype is only 1% lower than that of the proposed prototype. These experimental results validate the analysis presented in Section V-B that the proposed and conventional FB *LLC* prototypes should exhibit similar voltage gain performance.

The measured efficiency curves of the proposed and conventional prototypes are illustrated in Fig. 22. It can be observed that, under testing conditions ranging from 5 A light load to 30 A full load, they exhibit similar efficiency performance. The maximum efficiency difference occurs at 5 A load condition, where the efficiency of the proposed prototype is 0.07% higher than that of the conventional prototype. These experimental results validate the analysis presented in Section V-A that the use of the SPWT configuration does not introduce extra winding loss, and proposed and conventional FB *LLC* prototypes should exhibit similar efficiency performance.

### C. Symmetry Verification of Proposed Planar Transformer

To validate the symmetry of the proposed planar transformer, it is necessary to extract the capacitances of the four parasitic interwinding capacitors ( $C_{AE}$ ,  $C_{BE}$ ,  $C_{CE}$ , and  $C_{DE}$ ) associated with this transformer. The precise locations of these capacitors are shown in Fig. 4. The extraction process involves two steps.

- 1) Measure the capacitances of  $C_{P1\_S}$  and  $C_{P2\_S}$ .  $C_{P1\_S}$  denotes the structural capacitance between  $P1$  and the secondary windings ( $S1$  and  $S2$ ), which corresponds to the summation of  $C_{AE}$  and  $C_{BE}$ .  $C_{P2\_S}$  denotes the structural capacitance between  $P2$  and the secondary windings, which corresponds to the summation of  $C_{CE}$  and  $C_{DE}$ .
- 2) Determine the capacitance ratio  $K_1$  ( $K_2$ ) between  $C_{AE}$  and  $C_{P1\_S}$  ( $C_{CE}$  and  $C_{P2\_S}$ ) by using a signal generator. Then,  $C_{AE}$  and  $C_{BE}$ , as well as  $C_{CE}$  and  $C_{DE}$ , can be obtained by solving the following equations:

$$\begin{cases} C_{P1\_S} = C_{AE} + C_{BE} \\ K_1 = \frac{C_{AE}}{C_{P1\_S}} \end{cases} \quad (40)$$

$$\begin{cases} C_{P2\_S} = C_{CE} + C_{DE} \\ K_2 = \frac{C_{CE}}{C_{P2\_S}} \end{cases} \quad (41)$$

Fig. 23(a) illustrates the circuit connections during the measurement of  $C_{P1\_S}$  and  $C_{P2\_S}$ . The transformer winding terminals are short-circuited to ensure uniform electric

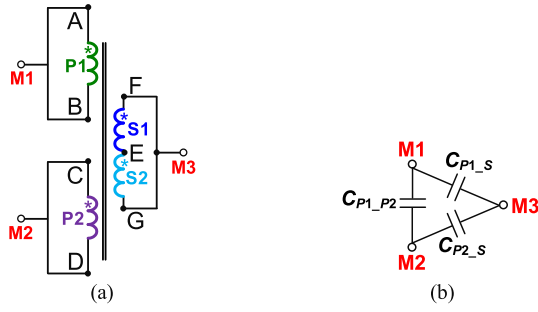


Fig. 23. Measuring  $C_{P1\_S}$  and  $C_{P2\_S}$ . (a) Circuit connections. (b) Equivalent capacitance network.

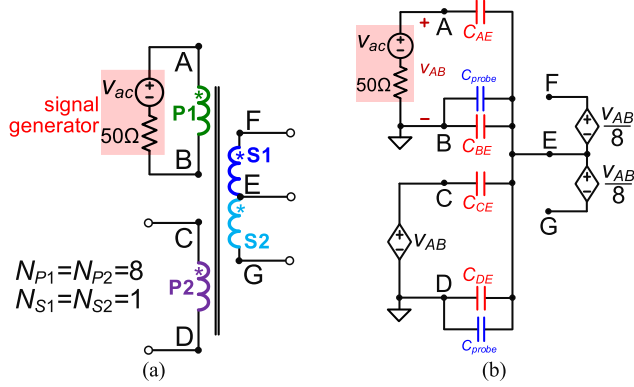


Fig. 24. Measuring  $K_1$  and  $K_2$ . (a) Circuit connections. (b) Equivalent circuit.

potential within each winding. Fig. 23(b) gives the equivalent capacitance network. Notably,  $C_{P1\_S}$  and  $C_{P2\_S}$  cannot be directly measured because of the existence of  $C_{P1\_P2}$  (interwinding capacitor between  $P1$  and  $P2$ ). In Fig. 23(a), the measured capacitances between  $M1$  and  $M2$ ,  $M1$  and  $M3$ , and  $M2$  and  $M3$  are denoted by  $C_{M1\_M2}$ ,  $C_{M1\_M3}$ , and  $C_{M2\_M3}$ , respectively. Then, the capacitances of  $C_{P1\_S}$  and  $C_{P2\_S}$  can be obtained by solving the following equations, which are both around 113 pF:

$$C_{M1\_M2} = C_{P1\_P2} + \frac{C_{P1\_S}C_{P2\_S}}{C_{P1\_S} + C_{P2\_S}} \quad (42)$$

$$C_{M1\_M3} = C_{P1\_S} + \frac{C_{P1\_P2}C_{P2\_S}}{C_{P1\_P2} + C_{P2\_S}} \quad (43)$$

$$C_{M2\_M3} = C_{P2\_S} + \frac{C_{P1\_S}C_{P1\_P2}}{C_{P1\_S} + C_{P1\_P2}} \quad (44)$$

Fig. 24(a) illustrates the method for extracting the capacitance ratios  $K_1$  and  $K_2$ . A signal generator is applied to  $P1$  winding terminals  $A$  and  $B$ , while the other winding terminals are left open. This method simulates the generation of the CM noise displacement currents via the interwinding capacitors. The equivalent circuit is given by Fig. 24(b). By adding the sinusoidal excitation signal  $v_{ac}$  at 150 kHz, the voltage distribution along transformer windings is established. Then, in Fig. 24(b), the voltage from  $E$  to  $B$  ( $v_{EB}$ ), and the voltage from  $A$  to  $B$  ( $v_{AB}$ ) are measured to calculate  $K_1$ , as shown in (45). In (45),  $C_{probe}$  represents the parallel capacitance introduced by the voltage probe, which is 3.9 pF for Tektronix TPP0250.  $V_{EB\_peak}$  ( $V_{AB\_peak}$ ) is the peak value of  $v_{EB}$  ( $v_{AB}$ ). Similarly, the voltage from  $E$  to  $D$  ( $v_{ED}$ ), and the voltage from  $C$  to  $D$  ( $v_{CD}$ ) are measured to calculate  $K_2$ , as shown

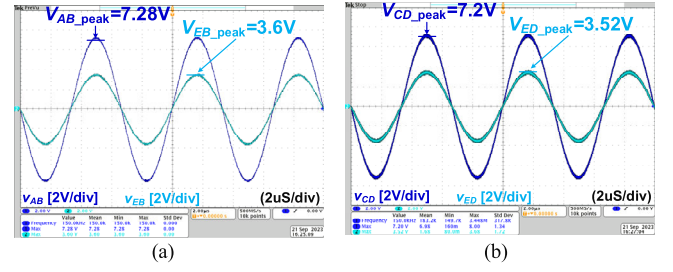


Fig. 25. Measured waveforms. (a)  $v_{AB}$  and  $v_{EB}$ . (b)  $v_{CD}$  and  $v_{ED}$ .

TABLE VII

MEASURED CAPACITANCES OF  $C_{AE}$ ,  $C_{BE}$ ,  $C_{CE}$ , AND  $C_{DE}$

	$C_{AE}$	$C_{BE}$	$C_{CE}$	$C_{DE}$
Experimental results	58 pF	55 pF	57 pF	56 pF

in (46).  $V_{ED\_peak}$  ( $V_{CD\_peak}$ ) is the peak value of  $v_{ED}$  ( $v_{CD}$ )

$$\frac{V_{EB\_peak}}{V_{AB\_peak}} = \frac{C_{AE}}{C_{P1\_S} + C_{probe}} = \frac{K_1}{1 + C_{probe}/C_{P1\_S}} \quad (45)$$

$$\frac{V_{ED\_peak}}{V_{CD\_peak}} = \frac{C_{CE}}{C_{P2\_S} + C_{probe}} = \frac{K_2}{1 + C_{probe}/C_{P2\_S}} \quad (46)$$

Fig. 25 gives the measured waveforms of  $v_{AB}$ ,  $v_{EB}$ ,  $v_{CD}$ , and  $v_{ED}$ . In Fig. 25(a),  $V_{EB\_peak}$  and  $V_{AB\_peak}$  are measured as 3.6 and 7.28 V, respectively. Then, the value of  $K_1$  can be determined by solving (45), which is around 0.512. In Fig. 25(b),  $V_{ED\_peak}$  and  $V_{CD\_peak}$  are measured as 3.52 and 7.2 V, respectively. Then, the value of  $K_2$  can be determined by solving (46), which is around 0.506.

Substituting the values of  $K_1$ ,  $K_2$ ,  $C_{P1\_S}$ , and  $C_{P2\_S}$  into (40) and (41) allows for determining the capacitances of  $C_{AE}$ ,  $C_{BE}$ ,  $C_{CE}$ , and  $C_{DE}$ , which are provided in Table VII. It can be observed that the capacitances of  $C_{AE}$  and  $C_{BE}$ , as well as  $C_{CE}$  and  $C_{DE}$ , are very close. This observation verifies the symmetry of the proposed planar transformer from the CM noise perspective. In addition, Table VIII in the Appendix provides the calculated values for these four capacitances, all of which are 65 pF. These calculation results match well with the experimental results in Table VII, showing a minimal discrepancy of 8–10 pF. This discrepancy mainly arises from the imperfect stacking of different PCBs and insulation papers, resulting in distributed air gaps between them. Consequently,  $C_{P1\_S}$  and  $C_{P2\_S}$  are slightly overestimated during the calculation process, leading to the subsequent overestimations of  $C_{AE}$ ,  $C_{BE}$ ,  $C_{CE}$ , and  $C_{DE}$ .

#### D. Measured Voltage Waveforms of Transformer Winding Terminals

Fig. 26 provides the resonant tank current waveform ( $i_{res}$ ), as well as the electric potential waveforms of the transformer terminals ( $v_a$  and  $v_b$ ), for the conventional FB LLC prototype operating under full load conditions. The reference ground for  $v_a$  and  $v_b$  is PG. It is worth noting that  $v_a$  and  $v_b$  exhibit different  $dv/dt$  characteristics in both boost ( $f_s = 135 \text{ kHz} < f_r$ ) and buck ( $f_s = 165 \text{ kHz} > f_r$ ) mode operation range, which is consistent with the analysis in



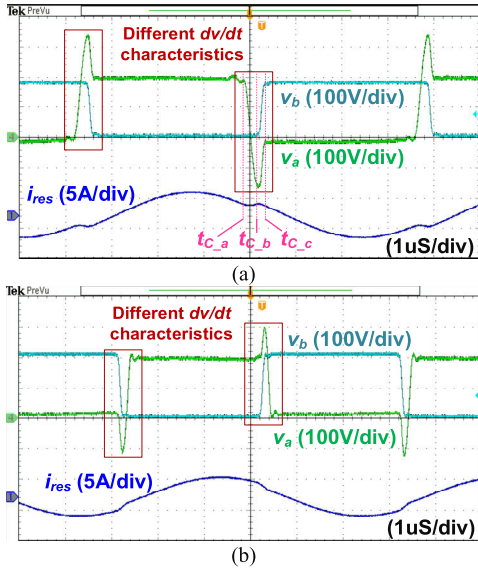


Fig. 26. Waveforms of transformer terminals in conventional FB LLC resonant converter under full load conditions. (a) Boost mode ( $f_s < f_r$ ),  $V_{in} = 180$  V,  $f_s = 135$  kHz. (b) Buck mode ( $f_s > f_r$ ),  $V_{in} = 210$  V,  $f_s = 165$  kHz.

Section II. Specifically, as depicted in Fig. 26(a), negative  $dv/dt$  on  $v_a$  is observed during the interval  $[t_{C_a}, t_{C_b}]$ , which induces CM noise current from the secondary side to the primary side through the corresponding parasitic interwinding capacitance. During the interval  $[t_{C_b}, t_{C_c}]$ , positive  $dv/dt$  on both  $v_a$  and  $v_b$  is observed, inducing CM noise currents from the primary side to the secondary side through the corresponding parasitic interwinding capacitance. As a result, the different  $dv/dt$  characteristics of  $v_a$  and  $v_b$  generate CM noise displacement currents with different magnitudes and phases that cannot cancel each other, thereby deteriorating the CM EMI performance of the conventional LLC prototype. The conclusion is the same when the conventional LLC prototype operates above  $f_r$ .

Fig. 27 provides the voltage waveforms of the transformer terminals with respect to PG in the proposed FB LLC prototype under full load conditions. It is observed that  $v_B$  and  $v_C$  ( $v_A$  and  $v_D$ ) have complimentary  $dv/dt$  characteristics in both boost and buck mode operation range, which is consistent with the analysis in Section III.

When  $f_s = f_r$ , the impedance of the resonant tank is zero. For the conventional FB LLC converter,  $v_{Q2}$  (see Fig. 1) and  $v_a$  are in phase. However, due to the influence of  $v_{Lm}$  (voltage across the magnetizing inductor), the  $dv/dt$  of  $v_a$  and  $v_b$  exhibit different slew rates during the dead time. As illustrated in Fig. 28(a), the  $dv/dt$  of  $v_a$  is slower than  $v_{Q2}$ . Consequently, the complementary nature of  $v_a$  and  $v_b$  is significantly weakened. In contrast to the conventional FB LLC converter, the proposed FB LLC converter demonstrates enhanced complementary characteristics in transformer winding terminals when  $f_s = f_r$ , as illustrated in Fig. 28(b).

The complimentary  $dv/dt$  characteristics introduced by the proposed SPWT configuration enable the CM noise cancellation in the transformer with a symmetrical winding structure, resulting in low CM EMI noise.

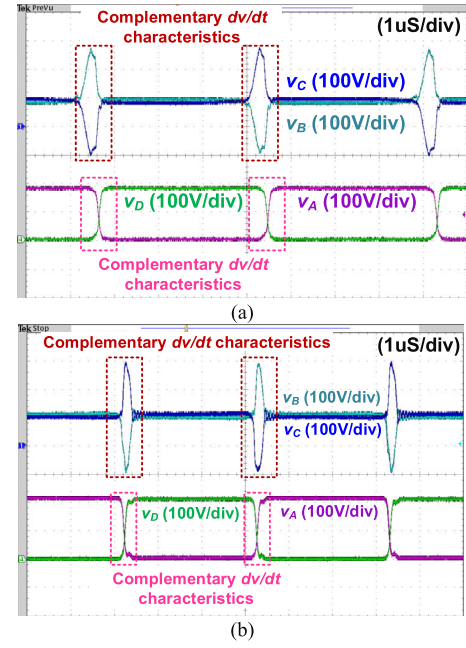


Fig. 27. Waveforms of transformer terminals in proposed FB LLC resonant converter under full load conditions. (a) Boost mode ( $f_s < f_r$ ),  $V_{in} = 180$  V,  $f_s = 135$  kHz. (b) Buck mode ( $f_s > f_r$ ),  $V_{in} = 210$  V,  $f_s = 165$  kHz.

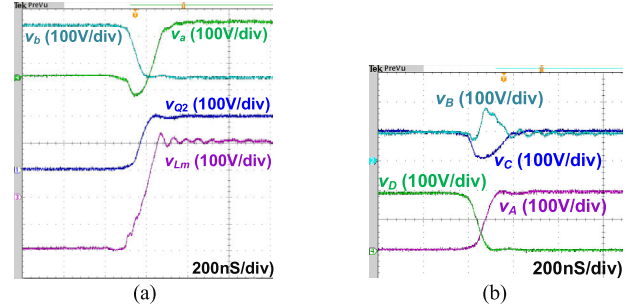


Fig. 28. Key waveforms during dead-time period when  $f_s = f_r$ . (a) Conventional FB LLC resonant converter under full load conditions. (b) Proposed FB LLC resonant converter under full load conditions.

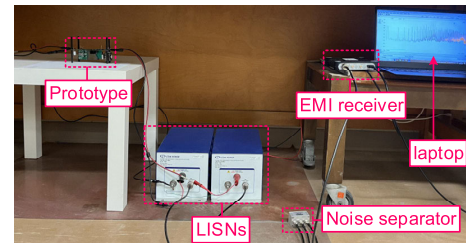


Fig. 29. Hardware setup.

### E. Measured CM Noise Spectra

The hardware setup of the conducted CM EMI measurement is shown in Fig. 29. The conducted CM noise is initially measured using a LISN named LI-125C, and then separated into its CM component using a noise separator named ZSC-2-2+. The conducted CM EMI spectrum is scanned by an EMI receiver named RSA306B in accordance with the EN55032 class B standard. Fig. 30 illustrates the measured CM noise spectra (quasi-peak value) of the conventional and proposed FB LLC prototypes under full load conditions. The enveloping curves of the CM noise for the conventional



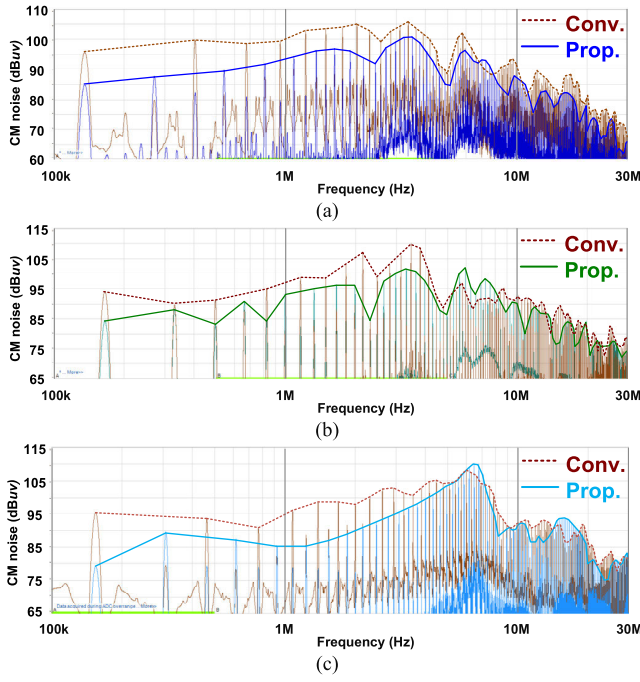


Fig. 30. Measured CM noise spectra. (a) Boost mode ( $f_s < f_r$ ),  $V_{in} = 180$  V,  $f_s = 135$  kHz. (b) Buck mode ( $f_s > f_r$ ),  $V_{in} = 210$  V,  $f_s = 165$  kHz. (c)  $f_s = f_r = 152$  kHz,  $V_{in} = 195$  V.

and proposed *LLC* prototypes are depicted by dashed and solid lines, respectively. Some peaks are not connected to the enveloping curves to ensure the clear readability of the amplitude trend of the CM noise. In Fig. 30, some noise peaks occur at frequencies that are not integer multiples of the switching frequency, which is attributed to background noise caused by the layout of the PCB [38]. These peaks do not affect CM noise reduction and can be resolved by appropriate PCB layout design.

The results presented in Fig. 30 show that the proposed SPWT configuration and symmetrical winding arrangement can achieve an approximately 11 dB $\mu$ V reduction in CM noise for the fundamental frequencies in both boost and buck mode operation ranges of the FB *LLC* prototype. At the resonant frequency, a reduction of approximately 16 dB $\mu$ V in CM noise for the fundamental frequency can be achieved. It should be noted that this CM noise attenuation is achieved without increasing the bill of materials (BOM) cost. However, for frequencies above 5 MHz, the reduction in CM noise is reduced due to the dominant impedance of the transformer leakage inductance. In this range, the transformer should be modeled using a complex parasitic inductance and capacitance network for CM noise analysis. Nevertheless, the CM noise remains relatively low across most of the frequency spectrum. Therefore, the proposed SPWT configuration is very effective for reducing the size of the CM EMI filter since the corner frequency of the EMI filter is determined by the noise magnitude at the fundamental frequency.

## VII. CONCLUSION

In this article, a low CM noise FB *LLC* converter with SPWT configuration is proposed. By placing the resonant tank between two split primary windings, the voltage across

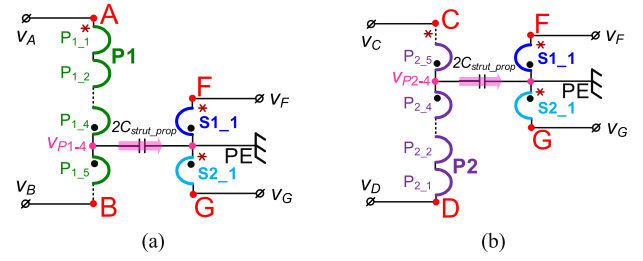


Fig. 31. (a) Lumped interwinding capacitance models of  $P1_4-S1_1$  and  $P1_5-S2_1$ . (b) Lumped interwinding capacitance models of  $P2_4-S2_1$  and  $P2_5-S1_1$ .

the original primary winding is redistributed and two created separate primary winding branches have complementary  $dv/dt$  characteristics; thus, the CM noise current generated in the transformer can be canceled completely with the symmetrical winding structure. The concept of complementary couple-turns is proposed for planar transformer applications. By choosing the overlapping primary and secondary winding turns based on the concept of complementary couple-turns, the planar transformer can be ensured to have a symmetrical winding arrangement and minimized CM noise currents before it is physically fabricated. The experimental results of a 360 W FB *LLC* converter show that the CM noise can be reduced significantly by around 16 dB $\mu$ V (a reduction of around 6.3 times) at the fundamental frequency when  $f_s = f_r$ . The decreased CM noise allows for a reduction in the size of the CM EMI filter, which helps to improve the power density of the whole system. Importantly, it should be noted that achieving this CM noise reduction incurs no additional cost.

## APPENDIX

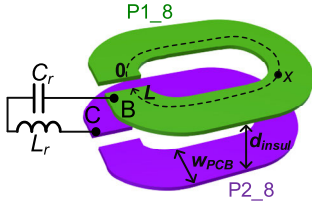
The principle of displacement current conservation is used to derive the interwinding capacitances of the proposed planar transformer shown in Fig. 13(a), including  $C_{AE}$ ,  $C_{BE}$ ,  $C_{CE}$ ,  $C_{DE}$ ,  $C_{BC}$ , and  $C_{AD}$ . The precise locations of these capacitors are shown in Fig. 18. In Fig. 13(a), there are distributed interwinding capacitors within five pairs of overlapping layers, which are  $P1_4-S1_1$ ,  $P1_5-S2_1$ ,  $P2_4-S2_1$ ,  $P2_5-S1_1$ , and  $P1_8-P2_8$ . The structural capacitance within each pair of overlapping layers remains the same. This structural capacitance is denoted as  $C_{strut\_prop}$  in the following analysis.

### A. Derivation of $C_{AE}$ , $C_{BE}$ , $C_{CE}$ , and $C_{DE}$

Based on the one-capacitor couple-turn model, the lumped interwinding capacitance models of  $P1_4-S1_1$ ,  $P1_5-S2_1$ ,  $P2_4-S2_1$ , and  $P2_5-S1_1$  are illustrated in Fig. 31. In Fig. 31(a), black dots denotes the corresponding terminals that are used to place  $C_{strut\_prop}$ . It is noted that  $C_{strut\_prop}$  in  $P1_4-S1_1$  and  $P1_5-S2_1$  are placed at the same position and the total capacitance is  $2C_{strut\_prop}$ . The same applies to Fig. 31(b).

In Fig. 31(a), the displacement current from primary winding  $P1$  to secondary windings is calculated as

$$i_{P1_S} = 2C_{strut\_prop} \frac{dv_{P1_4}}{dt} \quad (A1)$$

Fig. 32. Three-dimensional models of  $P1\_8$  and  $P2\_8$ .

where  $v_{P1\_4}$  can be derived as

$$v_{P1\_4} = v_A - 4\Delta v = v_A - \frac{v_A - v_B}{2} = \frac{v_A + v_B}{2}. \quad (A2)$$

In (A2),  $\Delta v$  is the voltage gradient on each turn. Substituting (A2) into (A1),  $i_{P1\_S}$  can be rewritten as

$$i_{P1\_S} = C_{strut\_prop} \frac{d(v_A + v_B)}{dt}. \quad (A3)$$

According to the principle of displacement current conservation, the displacement current generated in  $C_{AE}$  and  $C_{BE}$  should be equal to  $i_{P1\_S}$ , which can be expressed as

$$i_{P1\_S} = C_{AE} \frac{dv_A}{dt} + C_{BE} \frac{dv_B}{dt}. \quad (A4)$$

By comparing (A3) and (A4),  $C_{AE}$  and  $C_{BE}$  can be derived as

$$C_{AE} = C_{BE} = C_{strut\_prop}. \quad (A5)$$

The method used to derive  $C_{AE}$  and  $C_{BE}$  can similarly be applied to derive  $C_{CE}$  and  $C_{DE}$ . The specific calculation process is omitted, and  $C_{CE}$  and  $C_{DE}$  are directly provided as

$$C_{CE} = C_{DE} = C_{strut\_prop}. \quad (A6)$$

### B. Derivation of $C_{AD}$ and $C_{BC}$

$C_{AD}$  and  $C_{BC}$  primarily arise from the structural capacitance between primary winding turns  $P1\_8$  and  $P2\_8$ . The winding-to-core capacitances are ignored due to their relatively small values. Fig. 32 provides 3-D models of  $P1\_8$  and  $P2\_8$ .  $x$  denotes the winding length direction and the overall winding length is denoted by  $L$ . The voltage distributions of  $P1\_8$  and  $P2\_8$  are denoted by  $v_{P1\_8}(x)$  and  $v_{P2\_8}(x)$ , respectively. By assuming that the voltage of the winding turn is evenly distributed,  $v_{P1\_8}(x)$  and  $v_{P2\_8}(x)$  can be calculated by

$$\begin{cases} v_{P1\_8}(x) = v_B + \Delta v - \frac{\Delta v \cdot x}{L}, & x \in (0, L) \\ v_{P2\_8}(x) = v_C - \frac{\Delta v \cdot x}{L} = -v_B - \frac{\Delta v \cdot x}{L}, & x \in (0, L). \end{cases} \quad (A7)$$

The displacement current flowing from  $P1\_8$  to  $P2\_8$  can be calculated as

$$\begin{aligned} i_{P1\_8-P2\_8} &= \int_0^L \frac{\epsilon_0 \epsilon_{insul} w_{PCB}}{d_{insul}} \frac{d}{dt} (v_{P1\_8}(x) - v_{P2\_8}(x)) dx \\ &= C_{strut\_prop} \frac{d(2v_B + \Delta v)}{dt}. \end{aligned} \quad (A8)$$

TABLE VIII

INTERWINDING CAPACITANCES OF PROPOSED PLANAR TRANSFORMER

	$C_{AE}, C_{BE}, C_{CE}, C_{DE}$	$C_{AD}$	$C_{BC}$	$C_e$
Calculation results	65 pF	4 pF	61 pF	93 pF

Since  $\Delta v$  is equal to  $(v_A - v_B)/8$ , (A8) can be rewritten as

$$i_{P1\_8-P2\_8} = C_{strut\_prop} \frac{d}{dt} \left( \frac{v_A + 15v_B}{8} \right). \quad (A9)$$

Based on the principle of displacement current conservation, the displacement current generated in  $C_{BC}$  and  $C_{AD}$  should be equal to  $i_{P1\_8-P2\_8}$ , which is expressed as

$$\begin{aligned} i_{P1\_8-P2\_8} &= C_{AD} \frac{d(v_A - v_D)}{dt} + C_{BC} \frac{d(v_B - v_C)}{dt} \\ &= 2C_{AD} \frac{dv_A}{dt} + 2C_{BC} \frac{dv_B}{dt}. \end{aligned} \quad (A10)$$

By comparing (A9) and (A10),  $C_{AD}$  and  $C_{BC}$  can be derived as

$$\begin{cases} C_{AD} = C_{strut\_prop}/16 \\ C_{BC} = 15C_{strut\_prop}/16. \end{cases} \quad (A11)$$

The capacitance  $C_e$  can be calculated by

$$C_e = C_{BC} + \frac{C_{BE}C_{CE}}{C_{BE} + C_{CE}} = 23C_{strut\_prop}/16. \quad (A12)$$

The calculation results are summarized in Table VIII.

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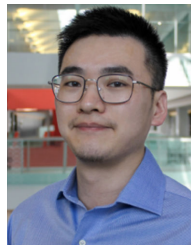
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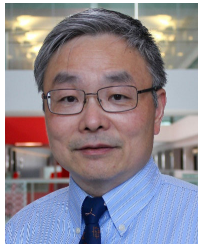




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