

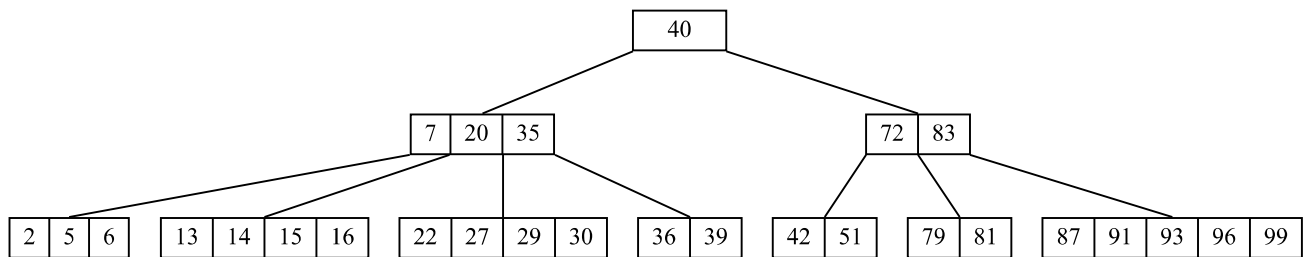
Deletions in B-Trees

Deletes a B-tree of degree (order) = 3

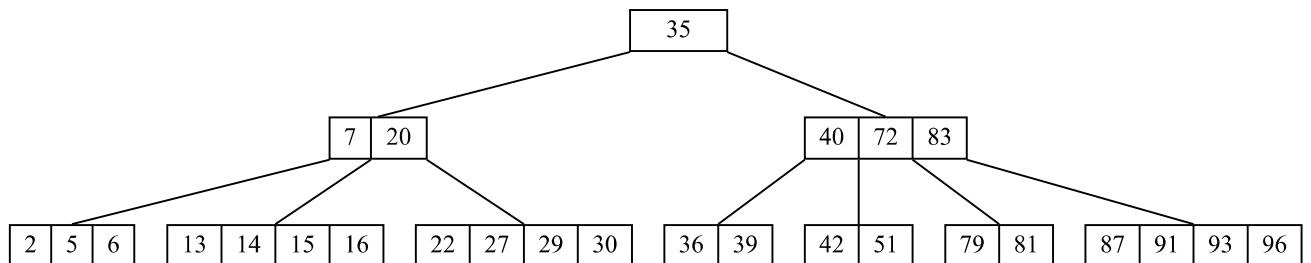
Method used: deletions with transformations in going down (precaution principle)

```
In [1]: from btrees_classics import delete
        from algopy.btree import BTree, display2, fromlist
        BTree.degree = 3
```

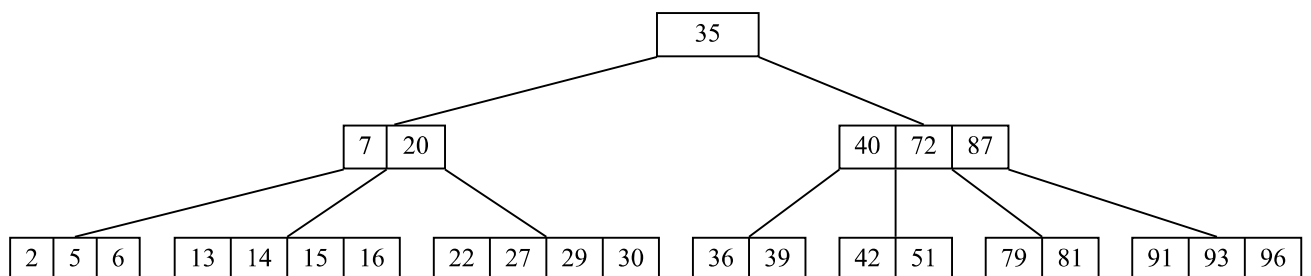
```
In [2]: B = fromlist('<40>(<7,20,35>(<2,5,6>)(<13,14,15,16>)(<22,27,29,30>)(<36,39>))(<72,83>(<42,51>)(<79,81>)(<87,91,93,96,99>)))', 3)
        display2(B)
```



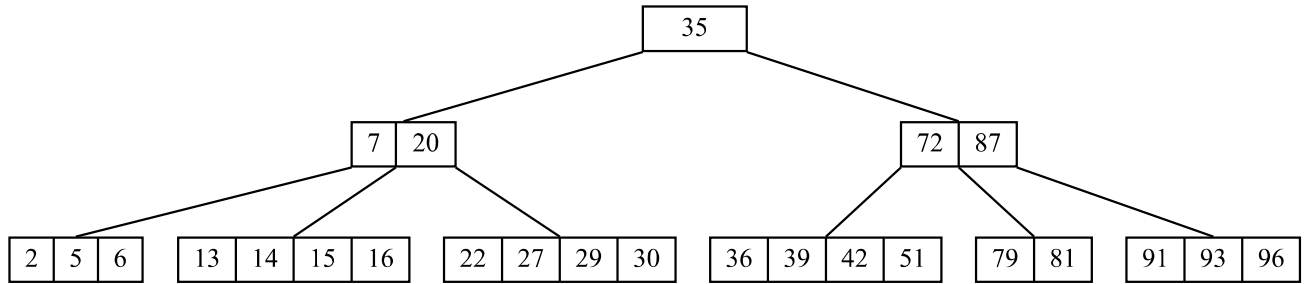
```
In [3]: B = delete(B, 99) # simple leaf deletion (precaution principle: right rotation child 0 -> 1)
        display2(B)
```



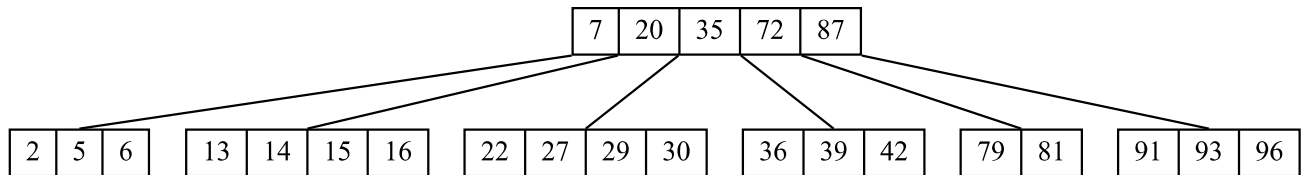
```
In [4]: B = delete(B, 83) # 83 replaced by 87 -> 87 in leaf deleted
        display2(B)
```



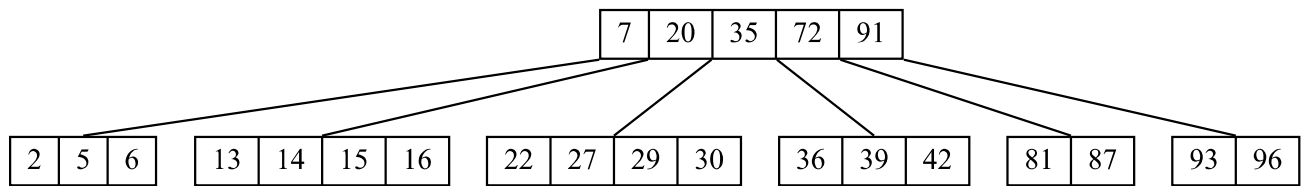
In [5]: `B = delete(B, 40) # 40 in internal node: its children 0 and 1 are merged, 40 deleted in the result`
`display2(B)`



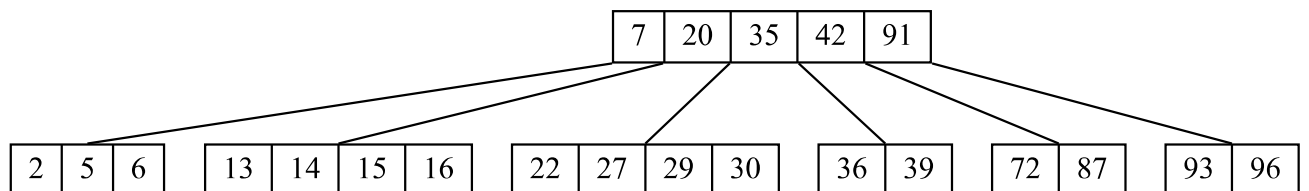
In [6]: `B = delete(B, 51) # children 0 and 1 merged, the root is now the result`
`display2(B)`



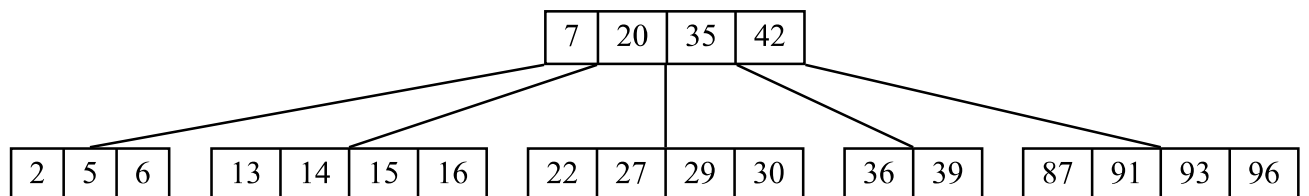
In [7]: `B = delete(B, 79) # left rotation`
`display2(B)`



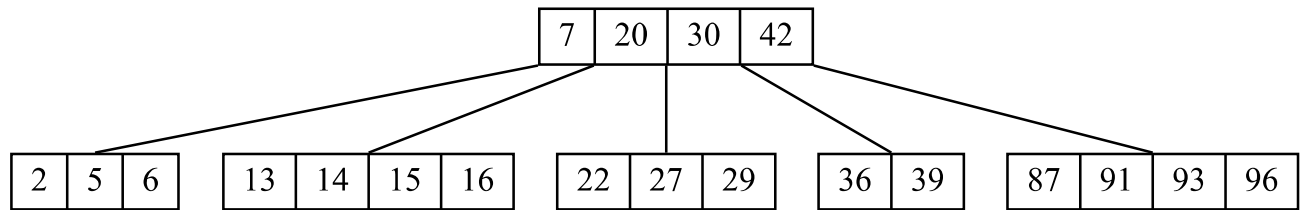
In [8]: `B = delete(B, 81) # right rotation`
`display2(B)`



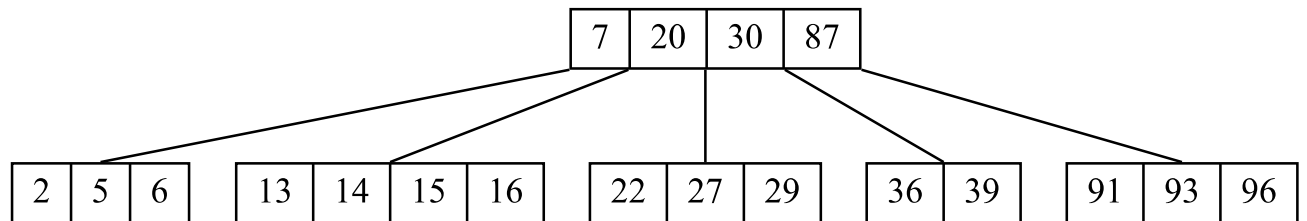
In [9]: `B = delete(B, 72) # merge`
`display2(B)`



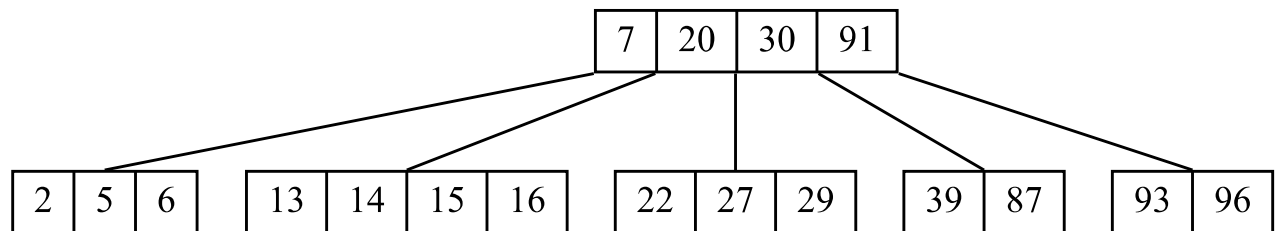
In [10]: `B = delete(B, 35) # 35 replaced by 30, 30 in leaf deleted`
`display2(B)`



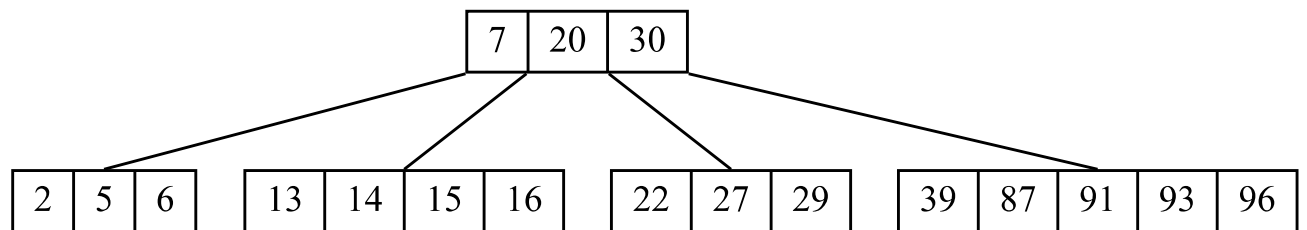
In [11]: `B = delete(B, 42) # 42 replaced by 87, 87 in leaf deleted`
`display2(B)`



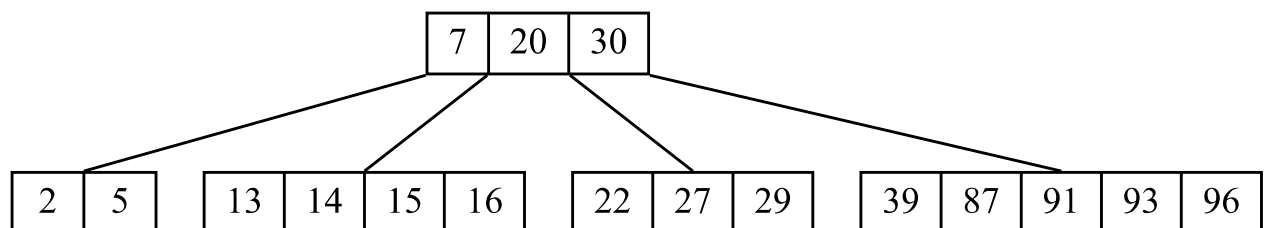
In [12]: `B = delete(B, 36) # left rotation`
`display2(B)`



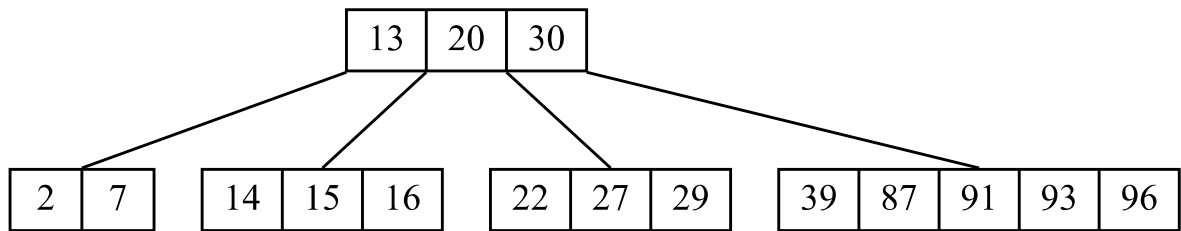
In [13]: `B = delete(B, 99) # non-existent key deletion, children 3 and 4 are merged`
`display2(B)`



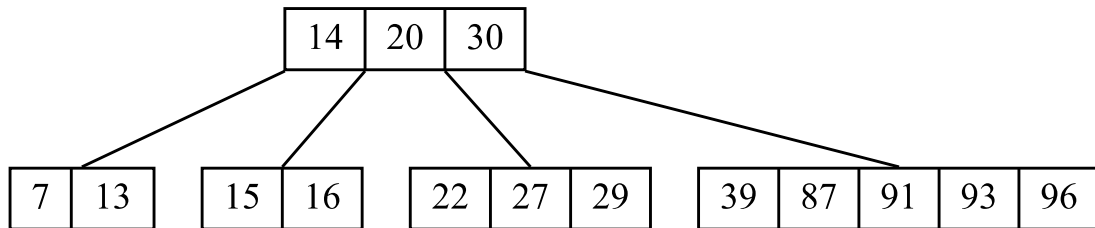
In [14]: `B = delete(B, 6)`
`display2(B)`



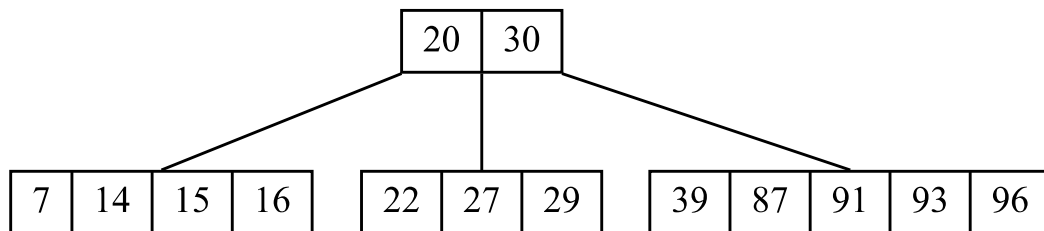
```
In [15]: B = delete(B, 5) # left rotation
display2(B)
```



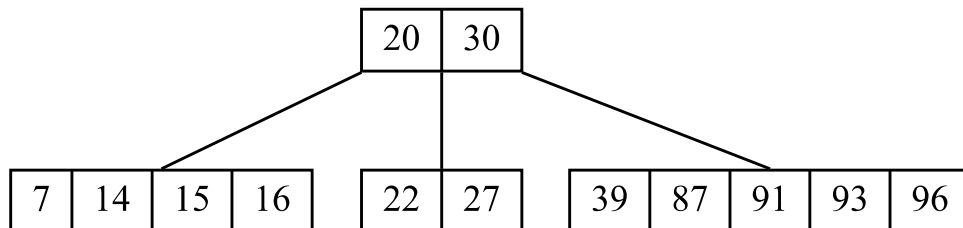
```
In [16]: B = delete(B, 2) # left rotation
display2(B)
```



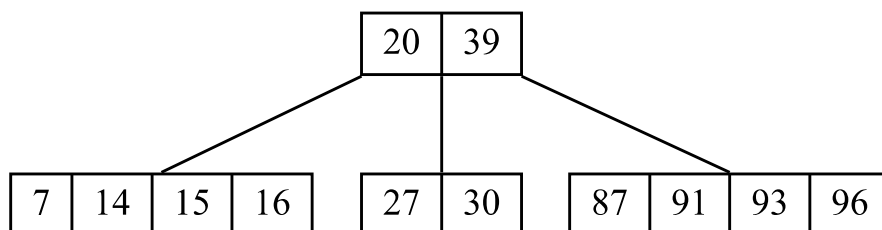
```
In [17]: B = delete(B, 13) # merge
display2(B)
```



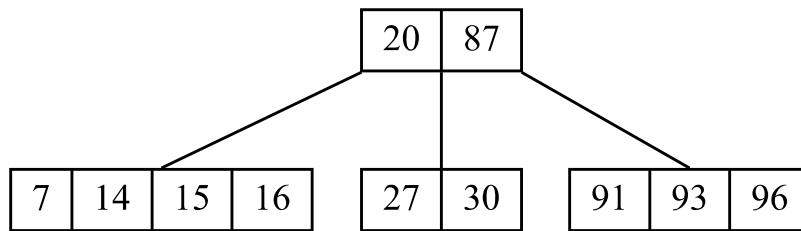
```
In [18]: B = delete(B, 29)
display2(B)
```



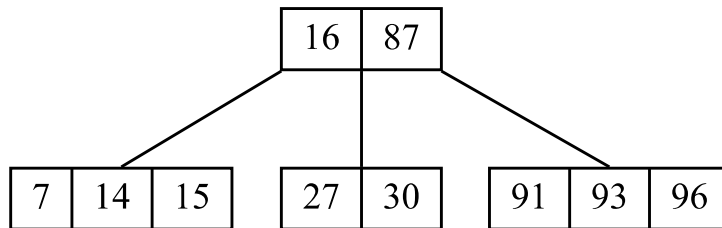
```
In [19]: B = delete(B, 22) # left rotation
display2(B)
```



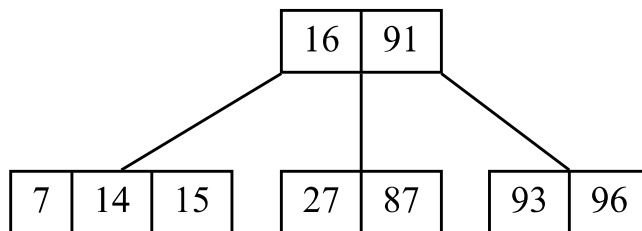
In [20]: `B = delete(B, 39) # 39 replaced by 87, 87 in, Leaf deleted`
`display2(B)`



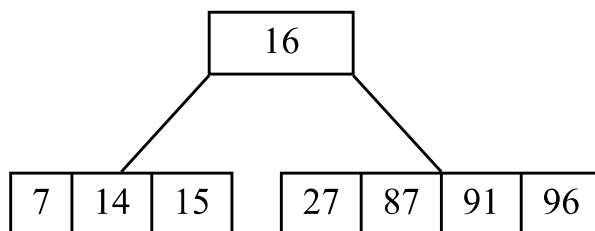
In [21]: `B = delete(B, 20) # 20 replaced by 16, 16 in Leaf deleted`
`display2(B)`



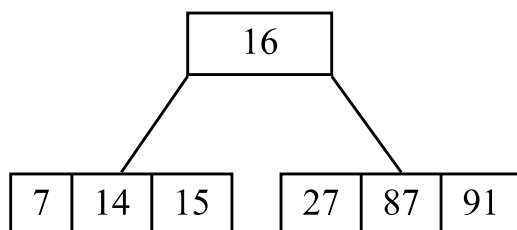
In [22]: `B = delete(B, 30) # left-rotation`
`display2(B)`



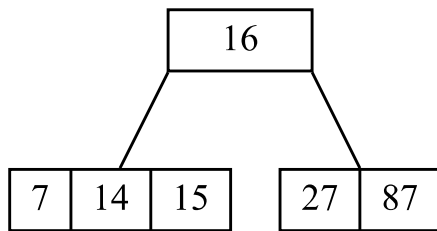
In [23]: `B = delete(B, 93) # merge`
`display2(B)`



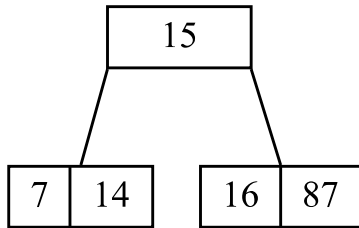
In [24]: `B = delete(B, 96)`
`display2(B)`



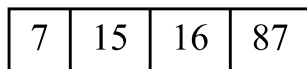
```
In [25]: B = delete(B, 91)
display2(B)
```



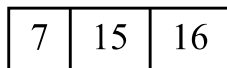
```
In [26]: B = delete(B, 27) # right rotation
display2(B)
```



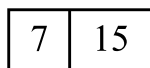
```
In [27]: B = delete(B, 14) # merge -> new root
display2(B)
```



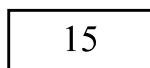
```
In [28]: B = delete(B, 87)
display2(B)
```



```
In [29]: B = delete(B, 16)
display2(B)
```



```
In [30]: B = delete(B, 7)
display2(B)
```



```
In [31]: B = delete(B, 15)
print(B)
```

None

```
In [ ]:
```