

UNIVERSITY OF BUEA
FACULTY OF ENGINEERING AND TECHNOLOGY
ENTRANCE EXAMINATION

October 2020

MATHEMATICS

Time: 3 Hours

Answer all Questions

Each Question has four suggested answers A, B, C, D. Select only one answer.

<p>1. The parametric equations of a curve are $1 - x = \tan \theta$, $y = \sec \theta$. The Cartesian equation of this curve is</p> <p>A $x^2 - y^2 + 2x + 2 = 0$ B $x^2 - y^2 + 2x - 2 = 0$ <input checked="" type="radio"/> C $x^2 - y^2 - 2x + 2 = 0$ D $x + y^2 - 2x + 2 = 0$</p>	<p>5. If $y = \ln\left(\frac{x+1}{2x}\right)$, then $\frac{dy}{dx}$ is</p> <p>A $\frac{2x}{1+x}$ <input checked="" type="radio"/> B $\frac{1}{x+1} - \frac{1}{x}$ C $\frac{1}{x+1} + \frac{1}{2x}$ D $\frac{1}{x+1} - \frac{1}{2x}$</p>
<p>2. $n! + (n-1)! + (n-2)! =$</p> <p>A $n^2(n-1)!$ <input checked="" type="radio"/> B $n^2(n-2)!$ C $n(n-2)!$ D $n(n-1)!$</p>	<p>6. $\int_1^2 3e^{\ln x^2} dx =$</p> <p>A $6 \ln 2$ B $\frac{3}{\ln 4}$ C $\frac{8}{7}$ <input checked="" type="radio"/> D $\frac{7}{8}$</p>
<p>3. The center of the circle with equation $x^2 + y^2 - x + \frac{1}{2}y - \frac{1}{4} = 0$ is</p> <p>A $\left(\frac{1}{2}, \frac{1}{4}\right)$ B $(2, -1)$ C $\left(-\frac{1}{2}, -\frac{1}{4}\right)$ <input checked="" type="radio"/> D $\left(\frac{1}{2}, -\frac{1}{4}\right)$</p>	<p>7. The general solution of the differential equation $(x-3)\frac{dy}{dx} = y$ is</p> <p>A $y = \frac{x^2}{2} - 3x + K$ B $y = K e^{x-3}$ <input checked="" type="radio"/> C $y = K(x-3)$ D $y = (x-3) + K$</p>
<p>4. The general solution of the equation $\sin 2x = \frac{\sqrt{3}}{2}$ is</p> <p><input checked="" type="radio"/> A $\frac{\pi}{6}[3n + (-1)^n]$ B $\frac{\pi}{2}[6n + (-1)^n]$ C $\frac{\pi}{6}[2n + (-1)^n]$ D $\frac{\pi}{3}[3n + (-1)^n]$</p>	<p>8. The statement $x - 3 > \frac{x-4}{x}$, $x \in R$ is equivalent to</p> <p><input checked="" type="radio"/> A $\frac{x^2 - 4x + 4}{x} > 0$ B $x^2 - 4x + 4 > 0$ C $\frac{x^2 - 4x - 4}{x} > 0$ D $x^2 - 2x - 4 > 0$</p>

9. Given that -2, K, 5 are three consecutive terms of an arithmetic progression, then the common difference is

- A $\frac{3}{2}$ $5 - K = K + 2$
 B $\frac{7}{2}$ $3K = 3$
 C $\frac{7}{2}$ $K = 3$
 D 3

10. The set of values of x for which the geometric series $\sum_{r=0}^{\infty} (x-1)^r$ is convergent is

- A $0 < x < 2$
 B $-1 < x < 1$
 C $-2 < x < 1$
 D $0 \leq x \leq 2$

11. Given that x is a periodic function of period 4 and that

$$f(x) = \begin{cases} x^2, & 0 \leq x < 2 \\ x+2, & 2 \leq x < 4 \end{cases}$$

then $f(9) =$

- A 1 $f(0) = f(4) = f(8) = 1$
 B 81 $f(1) = 1$
 C 11
 D 7

12. The volume generated when the area of the finite region enclosed by the x-axis and the curve $y = x - x^2$ is rotated completely about the x-axis is

- A $\pi \int_0^1 (x - x^2)^2 dx$ $\int \pi y^2 dx$
 B $\pi \int_0^2 (x - x^2)^2 dx$
 C $2\pi \int_{-1}^1 (x - x^2)^2 dx$
 D $2\pi \int_{-1}^0 (x - x^2)^2 dx$ $x=0, x=1$

13. Two consecutive integers between which a root of the equation $x^3 + x - 16 = 10$ lies are

- A 1 and 2 $2^3 + 2 - 16 = -16 < 0$
 B 2 and 3 $3^3 + 3 - 16 = 4 > 0$
 C 3 and 4
 D 4 and 5

14. The vectors a and b are such that $|a| = 3, |b| = 5$, and $ab = -14$

then $|a-b| =$

- A 62
 B $\sqrt{62}$
 C 44
 D $\sqrt{44}$

15. The sum of the first n terms of a series is given by $S_n = 5n^2 + 2n$. The n^{th} term of the series is

- A $10n + 7$
 B $10n - 3$
 C $10n + 3$
 D $10n - 7$

16. The expansion of $(2+3x)^{-1}$ is valid when

- A $-\frac{2}{3} < x < \frac{2}{3}$
 B $-\frac{1}{3} \leq x \leq \frac{1}{3}$
 C $-\frac{1}{3} < x < \frac{1}{3}$
 D $-\frac{3}{2} < x < \frac{3}{2}$



17. The Cartesian equation of the curve with parametric equation $x = 1 + t^2, y = 2t$,

where t is a parameter, is

- A $y^2 = 4(x-4)$
 B $y^2 = 4(x-1)$
 C $y^2 = 4(x+4)$
 D $y^2 = 4(1-x)$

18. $\lim_{x \rightarrow \pi} \frac{\sin 2x}{\sin x} =$

- A -1
 B 2
 C 0
 D -2

<p>19. $1 + \frac{1}{2} + \frac{1}{2^2} + \frac{1}{2^3} + \frac{1}{2^4} =$</p> <p>(A) $\frac{31}{16}$ ✓</p> <p>B $\frac{1}{2}$</p> <p>C $\frac{7}{8}$</p> <p>D $\frac{1}{2}$</p> <p>$1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} = \frac{16+8+4+2+1}{16} = \frac{31}{16}$</p>		<p>24 The equation $\cos x + \sqrt{3} \sin x = 1$ is equivalent to</p> <p>A $2 \sin(x + \frac{\pi}{6}) = 1$</p> <p>B $2 \sin(x + \frac{\pi}{3}) = 1$</p> <p>C $2 \cos(x - \frac{\pi}{6}) = 1$</p> <p>(D) $2 \cos(x - \frac{\pi}{3}) = 1$</p> <p>$2(\cos x \cos \frac{\pi}{3} + \sin x \sin \frac{\pi}{3}) = 1$</p>	
<p>20. The asymptotes of the curve $y = \frac{(x-5)^2}{(x+5)(x-3)}$ are</p> <p>A $x=3, x=-5, y=5$</p> <p>B $x=-3, x=-5, y=-5$</p> <p>(C) $x=3, x=-5, y=1$</p> <p>D $x=3, x=-5, y=-1$</p> <p>$x=3, x=-5$</p>		<p>25. Given that $\tan x = \frac{2}{3}$, $\tan 2x =$</p> <p>(A) $\frac{12}{5}$</p> <p>B $\frac{4}{3}$</p> <p>C $\frac{12}{13}$</p> <p>D $\frac{4}{9}$</p> <p>$\tan 2x = \frac{2 \tan x}{1 - \tan^2 x} = \frac{2 \cdot \frac{2}{3}}{1 - \frac{4}{9}} = \frac{\frac{4}{3}}{\frac{5}{9}} = \frac{4}{3} \cdot \frac{9}{5} = \frac{12}{5}$</p>	
<p>21. Given that $\begin{vmatrix} 1 & 2 & -2 \\ 2 & 1 & 3 \\ 3 & 2 & -4 \end{vmatrix} = d$, then</p> <p>$\begin{vmatrix} 1 & 6 & -8 \\ 2 & 3 & 12 \\ 3 & 6 & -16 \end{vmatrix} =$</p> <p>A $7d$</p> <p>B $72d$</p> <p>(C) $12d$ ✓</p> <p>D $12d^2$</p> <p>$3 \times 4 \times 2 = 12d$</p>		<p>26. The vector v, where $v = 28$, is in the direction of the vector $2i + 3j - 6k$.</p> <p>$v =$</p> <p>A $14i + 21j - 42k$</p> <p>(B) $8i + 12j - 24k$</p> <p>C $26i + 25j - 22k$</p> <p>D $14i + \frac{28}{3}j - \frac{14}{3}k$</p> <p>$\sin \theta = \frac{2}{\sqrt{13}}$ $\cos \theta = \frac{3}{\sqrt{13}}$</p>	
<p>22. When the polynomial function $x^3 + 2x^2 + \beta x - 3$ is divided by $x-2$ and $x+1$, the remainders are the same. The value of the constant β is</p> <p>(A) -5</p> <p>B 15</p> <p>C 18</p> <p>D -6</p> <p>$2 + 8 + 2\beta - 3 = -1 + 1 - \beta$ $2\beta = -15$ $\beta = -\frac{15}{2}$</p>		<p>27. The vector perpendicular to both $3i - 6j - 4k$ and $-3i + 2j + 2k$ is</p> <p>A $-4i + 6j + 12k$</p> <p>(B) $-4i + 6j - 12k$</p> <p>C $4i - 6j - 12k$</p> <p>D $-2i + 3j + 6k$</p>	
<p>23. α and β are the roots of a quadratic such that $\alpha + \beta = 2$ and $\alpha\beta = \frac{1}{2}$. The value of $\alpha^2 + \beta^2$ is</p> <p>A $\frac{7}{2}$</p> <p>(B) 3</p> <p>C 2</p> <p>D $\frac{9}{2}$</p> <p>$\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta = 2^2 - 2 \cdot \frac{1}{2} = 4 - 1 = 3$</p>		<p>28. Given that $f(x) = x^2 \ln(x-2)$</p> <p>$f'(3) =$</p> <p>(A) 9</p> <p>B 6</p> <p>C $6 \ln 5 - 9$</p> <p>D -9</p> <p>$f'(x) = 2x \ln(x-2) + \frac{x^2}{x-2}$ $f'(3) = 6 \ln 5 - 9$</p>	

<p>29. $\int_0^{\frac{\pi}{4}} \tan x \, dx =$</p> <p>A $\frac{1}{2} \ln 2$</p> <p>B $-\frac{1}{2} \ln 2$</p> <p>C $\frac{1}{2} \ln 2 - 1$</p> <p>D $-\frac{1}{2} \ln 2 - 1$</p>	<p>34. The range of values of x for which $x-4 \leq 2$ is</p> <p>A $x \leq 6$</p> <p>B $x \leq 2$ or $x \geq 6$</p> <p>C $2 \leq x \leq 6$</p> <p>D $x \geq 2$</p>
<p>30. The curve $y = \frac{x^2}{x-1}$ cannot lie between $y=0$ and $y=4$. There is a local maximum of the curve at the point</p> <p>A (0, 0)</p> <p>B (0, 4)</p> <p>C (2, 4)</p> <p>D (2, 0)</p>	<p>35. Which of the following statements is TRUE?</p> <p>A If $x^2 = y^2$, then $x = y$</p> <p>B If $f(a)=0$ then $x+a$ is a factor of $f(x)$</p> <p>C If $f(x)$ has a maximum value at $x=a$ then $f''(a) > 0$</p> <p>D Let $m, n \in \mathbb{Z}$ be the set of integers. If m and n are both odd, then $m+n$ is even</p>
<p>31. The solution of the differential equation $y \frac{dy}{dx} = 2x$, given that $y=1$ and $x=1$ is</p> <p>A $x^2 = y^2 - 2$</p> <p>B $2x^2 = y^2 - 1$</p> <p>C $x = 2y^2 - 1$</p> <p>D $y^2 = 2x^2 - 1$</p>	<p>36. Given that $f(x) = \begin{vmatrix} x & x^2 & x^3 \\ 1 & 2x & 3x^2 \\ 0 & 2 & 6x \end{vmatrix}$, $f'(x) =$</p> <p>A 12</p> <p>B $6x^2$</p> <p>C $6x$</p> <p>D $42x^2$</p>
<p>32. The line segment PQ, where P is the point (7,7) and Q the point (-1,3), is the diameter of a circle. The equation of the circle is</p> <p>A $(x-7)(x+1) + (y-7)(y-3) = 0$</p> <p>B $(x-7)(x-1) + (y-7)(y-3) = 0$</p> <p>C $(x+7)(x-1) + (y+7)(y+3) = 0$</p> <p>D $(x+7)(x+1) + (y-7)(y+3) = 0$</p>	<p>37. Given that x is a periodic function of period 4 and that $f(x) = \begin{cases} x^2, & 0 \leq x < 2 \\ x+2, & 2 \leq x < 4 \end{cases}$</p> <p>then $f(9) =$</p> <p>A 1</p> <p>B 81</p> <p>C 11</p> <p>D 7</p>
<p>33. When $f(x) = 2x^3 + x^2 - 13x + 6$ is divided by $2x-1$, the remainder is</p> <p>A 13</p> <p>B 52</p> <p>C $\frac{1}{2}$</p> <p>D 0</p>	<p>38. Given that $\frac{x}{(3-x)(4-x)} \equiv \frac{p}{3-x} + \frac{q}{4-x}$</p> <p>A $p=3, q=4$</p> <p>B $p=4, q=-3$</p> <p>C $p=3, q=-4$</p> <p>D $p=-3, q=-4$</p>

39. Two consecutive integers between which a root of the equation $x^3 + x - 16 = 10$ lies are

- A 1 and 2
 (B) 2 and 3
 C 3 and 4
 D 4 and 5

44. The vector equation of a straight line is
 $r = 2i + j - 2k + t(3i + 2j + 6k)$
 The direction cosines of the line are

- A $[2, 1, -2]$
 B $[3, 2, 6]$
 C $\left[\frac{2}{7}, \frac{1}{7}, -\frac{2}{7}\right]$
 (D) $\left[\frac{3}{7}, \frac{2}{7}, \frac{6}{7}\right]$

40. The range of real values of x for which $\frac{x-3}{x+2} \leq 0$ is

- A $x \leq -2$ or $x \geq 3$
 (B) $-2 < x \leq 3$
 C $x \leq -3$ or $x \geq 2$
 D $-3 \leq x \leq 2$

45. Given the parametric equations
 $x = 2t + \sin 2t$ and $y = 2 - \cos 2t$
 Where t is the parameter,

$$\frac{dy}{dx} =$$

- A $-\tan t$
 B $\frac{\sin 2t}{2 + \cos 2t}$
 C $\cot t$
 D $\frac{\sin t \cos t}{2(1 + \cos 2t)}$

41. When $(3 - 2x)^{\frac{1}{2}}$ is expanded in ascending powers of x , the range of values of x for which the expansion is valid is

- A $-\frac{1}{2} < x < \frac{2}{3}$
 B $-\frac{2}{3} < x < \frac{3}{2}$
 C $-\frac{3}{2} < x < \frac{3}{2}$
 D $-\frac{2}{3} < x < \frac{2}{3}$

46. Given that
 $y = x \ln(3x^2)$, the value of $\frac{dy}{dx}$ when $x = 1$ is

- A 3
 B $\ln 3$
 C $1 + \ln 3$
 (D) $2 + \ln 3$

42. The general solution of the equation $\sec(\theta + 30^\circ) = 2$ is

- A $\theta = 360^\circ n \pm 30^\circ - 60^\circ$
 B $\theta = 180^\circ n \pm 30^\circ - 60^\circ$
 C $\theta = 360^\circ n \pm 60^\circ - 30^\circ$
 D $\theta = 180^\circ n \pm 60^\circ - 30^\circ$

47. The values of y corresponding to the values of x are given in the table below.

x	5	9	12	15	18	21
y	0.3	0.8	1.4	2.1	3.0	4.3

Using the trapezoid rule, the approximate value

for $\int_5^{21} y dx$ is

- A 9.6
 B 35.7
 C 28.9
 D 23.8

43. The sine of the acute angle between the plane π and the line l , where

$$\pi: x - y + z = 2 \text{ and } l: \frac{x-2}{2} = \frac{y+1}{2} = \frac{z}{1} \text{ is}$$

- A $\frac{1}{\sqrt{3}}$
 B $\frac{1}{\sqrt{15}}$
 C $\frac{1}{3\sqrt{3}}$
 (D) $\frac{1}{\sqrt{3}}$

48. The gradient of the implicit function to the curve $x^3 + y^3 = 13$ at the point $(2, -2)$ is

- (A) $-\frac{2}{3}$
 B $\frac{3}{2}$
 C $\frac{2}{3}$
 D $-\frac{3}{2}$

<p>49. $\sin 50^\circ + \sin 40^\circ =$</p> <p>(A) $\sqrt{2} \cos 5^\circ$ B $2 \cos 10^\circ$ C $2 \cos 5^\circ$ D $\sqrt{2} \cos 10^\circ$</p>	<p>54. Given the complex number z, where $z = -\sqrt{3} - i$, the modulus-argument form for z is</p> <p>A $2(\cos \frac{\pi}{6} - i \sin \frac{\pi}{6})$ B $2(\cos \frac{5\pi}{6} - i \sin \frac{5\pi}{6})$ C $2(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6})$ D $2(\cos \frac{5\pi}{6} + i \sin \frac{5\pi}{6})$</p>
<p>50. The value of the constant λ, for which the plane $\lambda x - 3y + 4z = 5$ and the line $r = i - 2j - 3k + t(2i + 6j + 3k)$ are parallel is</p> <p>(A) 6 B 3 C 4 D 5</p>	<p>55. Given that $\sqrt{3} \cos x = \cos(\frac{\pi}{6} - x)$, $\tan x =$</p> <p>A $\sqrt{3}$ B $\frac{1}{\sqrt{3}}$ C 1 D $\frac{\sqrt{3}}{2}$</p>
<p>51. A point P divides the line segment joining the points M(4, 1) and N(7, 7) internally in the ratio 2:1. The coordinates of P are</p> <p>A (5, 6) B (5, 5) C (6, 3) D (6, 5)</p>	<p>56. $\int e^{3x} dx =$</p> <p>A $\frac{1}{3x+1} e^{3x+1} + k$ B $3e^{3x} + k$ C $e^{3x} + k$ D $\frac{1}{3} e^{3x} + k$</p>
<p>52. If $4 \log_{10} x - \log_{10} y = \log_{10} 13$ then</p> <p>A $x^4 y = 13$ B $4x = 13y$ (C) $x^4 = 13y$ D $4^x = 13y$</p>	<p>57. Given the parametric equations $x = 2t + \sin 2t$ and $y = 1 - \cos 2t$ where t is a parameter, $\frac{dy}{dx} =$</p> <p>A $-\tan t$ B $\cot t$ C $\frac{-\sin 2t}{1 + \cos 2t}$ (D) $\frac{\sin 2t}{1 + \cos 2t}$</p>
<p>53. A first approximation to the real root of the equation $x^3 + x^2 - 5x - 1 = 0$ is 2. A second approximation to the root of the equation, using the Newton-Raphson's method, is</p> <p>A $\frac{21}{11}$ B $\frac{23}{11}$ C $\frac{19}{11}$ D $\frac{18}{11}$</p>	<p>58. The curve $y = (x+2)^2$ has a minimum point at</p> <p>A (0, 4) B (4, 0) C (0, -2) (D) (-2, 0)</p>

49. $\sin 50^\circ + \sin 40^\circ =$

- (A) $\sqrt{2} \cos 5^\circ$
 B $2 \cos 10^\circ$
 C $2 \cos 5^\circ$
 D $\sqrt{2} \cos 10^\circ$

50. The value of the constant λ , for which the plane $\lambda x - 3y + 4z = 5$ and the line

$r = i - 2j - 3k + t(2i + 6j + 3k)$ are parallel is

- (A) 6
 B 3
 C 4
 D 5

51. A point P divides the line segment joining the points M(4, 1) and N(7, 7) internally in the ratio 2:1. The coordinates of P are

- A (5, 6)
 B (5, 5)
 C (6, 3)
 D (6, 5)

52. If $4 \log_{10} x - \log_{10} y = \log_{10} 13$ then

- A $x^4 y = 13$
 B $4x = 13y$
 (C) $x^4 = 13y$
 D $4^x = 13y$

53. A first approximation to the real root of the equation $x^3 + x^2 - 5x - 1 = 0$ is 2. A second approximation to the root of the equation, using the Newton-Raphson's method, is

- A $\frac{21}{11}$
 B $\frac{23}{11}$
 C $\frac{19}{11}$
 D $\frac{18}{11}$

54. Given the complex number z , where $z = -\sqrt{3} - i$, the modulus-argument form for z is

- A $2(\cos \frac{\pi}{6} - i \sin \frac{\pi}{6})$
 B $2(\cos \frac{5\pi}{6} - i \sin \frac{5\pi}{6})$
 C $2(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6})$
 D $2(\cos \frac{5\pi}{6} + i \sin \frac{5\pi}{6})$

55. Given that $\sqrt{3} \cos x = \cos(\frac{\pi}{6} - x)$, $\tan x =$

- A $\sqrt{3}$
 B $\frac{1}{\sqrt{3}}$
 C 1
 D $\frac{\sqrt{3}}{2}$

56. $\int e^{3x} dx =$

- A $\frac{1}{3x+1} e^{3x+1} + k$
 B $3e^{3x} + k$
 C $e^{3x} + k$
 D $\frac{1}{3} e^{3x} + k$

57. Given the parametric equations $x = 2t + \sin 2t$ and $y = 1 - \cos 2t$ where t is a parameter, $\frac{dy}{dx} =$

- A $-\tan t$
 B $\cot t$
 C $\frac{-\sin 2t}{1 + \cos 2t}$
 (D) $\frac{\sin 2t}{1 + \cos 2t}$

58. The curve $y = (x + 2)^2$ has a minimum point at

- A (0, 4)
 B (4, 0)
 (C) (0, -2)
 D (-2, 0)

49. $\sin 50^\circ + \sin 40^\circ =$

- (A) $\sqrt{2} \cos 5^\circ$
 B $2 \cos 10^\circ$
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$r = i - 2j - 3k + t(2i + 6j + 3k)$ are parallel is

- (A) 6
 B 3
 C 4
 D 5

51. A point P divides the line segment joining the points M(4, 1) and N(7, 7) internally in the ratio 2:1. The coordinates of P are

- A (5, 6)
 B (5, 5)
 C (6, 3)
 D (6, 5)

52. If $4 \log_{10} x - \log_{10} y = \log_{10} 13$ then

- A $x^4 y = 13$
 B $4x = 13y$
 (C) $x^4 = 13y$
 D $4^x = 13y$

53. A first approximation to the real root of the equation $x^4 + x^3 - 5x - 1 = 0$ is 2. A second approximation to the root of the equation, using the Newton-Raphson's method, is

- A $\frac{21}{11}$
 B $\frac{23}{11}$
 C $\frac{19}{11}$
 D $\frac{18}{11}$

54. Given the complex number z , where $z = -\sqrt{3} - i$, the modulus-argument form for z is

- A $2(\cos \frac{\pi}{6} - i \sin \frac{\pi}{6})$
 B $2(\cos \frac{5\pi}{6} - i \sin \frac{5\pi}{6})$
 C $2(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6})$
 D $2(\cos \frac{5\pi}{6} + i \sin \frac{5\pi}{6})$

55. Given that $\sqrt{3} \cos x = \cos(\frac{\pi}{6} - x)$, $\tan x =$

- A $\sqrt{3}$
 B $\frac{1}{\sqrt{3}}$
 C 1
 D $\frac{\sqrt{3}}{2}$

56. $\int e^{3x} dx =$

- A $\frac{1}{3x+1} e^{3x+1} + k$
 B $3e^{3x} + k$
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57. Given the parametric equations $x = 2t + \sin 2t$ and $y = 1 - \cos 2t$ where t is a parameter, $\frac{dy}{dx} =$

- A $-\tan t$
 B $\cot t$
 C $\frac{-\sin 2t}{1 + \cos 2t}$
 (D) $\frac{\sin 2t}{1 + \cos 2t}$

58. The curve $y = (x + 2)^2$ has a minimum point at

- A (0, 4)
 B (4, 0)
 C (0, -2)
 (D) (-2, 0)

<p>59. The number of selections of 3 students from a class of 7 students for a party in which the class prefect must attend is</p> <p>A $1 \times {}^6C_3$ B $1 + {}^6C_3$ C $1 \times {}^6C_2$ D $1 + {}^6C_2$</p>	<p>64. Given that $\frac{d}{dx}(3x^3e^{2x}) = 3x^2(a+bx)e^{2x}$</p> <p>A $a=9, b=6$ B $a=6, b=9$ C $a=2, b=3$ D $a=3, b=2$</p>
<p>60. Given that $x-c$ is a factor of $f(x)$, where $f(x) = 2x^3 - cx^2 + c(1-c)x - (6+c)$, the value of the constant c is</p> <p>A 2 or -3 B -2 or 3 C -2 or -3 D 2 or 3</p>	<p>65. The number of arrangements of the letters of the word MINIMUM is</p> <p>A $\frac{7!}{2!3!}$ B $7! \times 3! \times 2!$ C $7!$ D $\frac{5!}{2!3!}$</p>
<p>61. Given the differential equation $\cos x \frac{dy}{dx} = y \sin x$, then</p> <p>A $y = \ln(\sec x) + K$ B $\ln y = \ln(\sec x) + K$ C $y = \sec x + K$ D $\ln y = \sec x + K$</p>	<p>66. If $\frac{2}{x-2} + \frac{3}{x+1} = \frac{ax+b}{(x-2)(x+1)}$ then the values of the real constants a and b are respectively</p> <p>A 5, 4 B 5, -4 C -5, 4 D -5, -4</p>
<p>62. $\sum_{r=1}^{2n} (r-1) =$</p> <p>A $\frac{1}{2}n(n+1) - (n+1)$ B $\frac{1}{2}n(n+1)(n+2) - n$ C $\frac{1}{2}n(n+1)$ D $\frac{1}{2}n(n+2) - (n+1)$</p>	<p>67. The roots of the quadratic equation $cx^2 - 3x - c = 0$ are</p> <p>A $\frac{3 \pm \sqrt{9-4c^2}}{2c}$ B $\frac{3 \pm \sqrt{9+4c}}{2c}$ C $\frac{3 \pm \sqrt{9+4c^2}}{2c}$ D $\frac{3 \pm \sqrt{9-4c}}{2c}$</p>
<p>63. $\lim_{x \rightarrow 0} \left(\frac{\sin 2x - \sin x}{\sin x} \right) =$</p> <p>A 0 B -3 C 2 D 1</p>	<p>68. Given that $x \in R$ and that $x > 0$, the root of the equation $\log 2 + \log(2x^2 + 2x - 1) = 0$ is</p> <p>A $\frac{3}{2}$ B $\frac{2}{3}$ C $\frac{1}{4}$ D $\frac{1}{2}$</p>

69. The diameters of two concentric circles are 10m and 6m. The area of the region between the two circles is

- A 16π
 B 64π
 C 4π
 D 9π

70. The parametric equations of a curve are $1 - x = \tan \theta$, $y = \sec \theta$.

The Cartesian equation of this curve is

- A $x^2 - y^2 + 2x + 2 = 0$
 B $x^2 - y^2 + 2x - 2 = 0$
 C $x^2 - y^2 - 2x + 2 = 0$
 D $x + y^2 - 2x + 2 = 0$

71. $n! + (n-1)! + (n-2)! =$

- A $n^2(n-1)!$
 B $n^2(n-2)!$
 C $n(n-2)!$
 D $n(n-1)!$

72. The period of the function $f(x) = 3 \cos 5x$ is

- A $\frac{2\pi}{5}$
 B $\frac{5\pi}{2}$
 C $\frac{2\pi}{3}$
 D $\frac{3\pi}{5}$

73. The general solution of the equation $\sin 2x = \frac{\sqrt{3}}{2}$ is

- A $\frac{\pi}{6}[3n + (-1)^n]$
 B $\frac{\pi}{2}[6n + (-1)^n]$
 C $\frac{\pi}{6}[2n + (-1)^n]$
 D $\frac{\pi}{3}[3n + (-1)^n]$

74. If $y = \ln\left(\frac{x+1}{2x}\right)$, then $\frac{dy}{dx}$ is

- A $\frac{2x}{1+x}$
 B $\frac{1}{x+1} - \frac{1}{x}$
 C $\frac{1}{x+1} + \frac{1}{2x}$
 D $\frac{1}{x+1} - \frac{1}{2x}$

75. $\int_1^2 3e^{\ln x^2} dx =$

- A $6 \ln 2$
 B $\frac{3}{\ln 4}$
 C 8
 D 7

76. An Arithmetic Progression has first term $\ln 2$ and common difference $\ln 4$. The sum of the first 4 terms of the progression is

- A $16 \ln 4$
 B $16 \ln 2$
 C $10 \ln 4$
 D $8 \ln 2$

77. The statement $x - 3 > \frac{x-4}{x}$, $x \in \mathbb{R}$ is equivalent to

- A $\frac{x^2 - 4x + 4}{x} > 0$
 B $x^2 - 4x + 4 > 0$
 C $\frac{x^2 - 4x - 4}{x} > 0$
 D $x^2 - 2x - 4 > 0$

78. The argument of the complex number z , where $z = \frac{1+i}{1-i}$ is

- A $\frac{\pi}{4}$
 B $\frac{\pi}{3}$
 C $\frac{\pi}{2}$
 D $\frac{\pi}{6}$

79. The set of values of x for which the geometric series $\sum_{r=0}^{\infty} (x-1)^r$ is convergent is

- A $0 < x < 2$
- B $-1 < x < 1$
- C $-2 < x < 1$
- D $0 \leq x \leq 2$

80. The partial fractions corresponding to $\frac{2x+7}{x^2+5x+6}$ are

- A $\frac{3}{x+2} - \frac{1}{x+3}$
- B $-\frac{3}{x+2} + \frac{1}{x+3}$
- C $-\frac{3}{x+2} - \frac{1}{x+3}$
- D $\frac{3}{x+2} + \frac{1}{x+3}$