grammar G;
A: a;

Introduction to theory of languages

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Course plan

- Saturday, 25th of February 2017 lecture
 - Languages
 - Grammars
- 2 Saturday, 4th of March 2017 lecture
 - Parsing
 - ANTLR
- Saturday, 11th of March 2017 exercises
 - Grammars and languages
 - ANTLR
- Saturday, 25th of March 2017 exercises
 - ANTLR
- Exam

Additional informations

Any questions?

Ask by mail: kiepas@agh.edu.pl

Course web-page

 $\label{eq:http://home.agh.edu.pl/~kiepas} \rightarrow \textbf{Teaching} \rightarrow \textbf{Introduction to theory of languages (2017)}$

Plan of the lecture

- Introduction
- 2 Theory
 - Languages
 - Grammar
- Parsing
 - Methods
 - Tools
- 4 ANTLR

Introduction

Linguistics

Scientific study of languages. Involves analysis of language:

- form language evolution and task
- context environment of language usage
- semantics the meaning of the language

Some important aspects

- Phonetics
- Articulation
- Perception
- Acoustic features
- Morphology
- Syntax

Language types

- Natural languages
 - Ordinary evolves naturally in humans without planning
 - Controlled a restricted subset of natural language in order reduce or eliminate ambiguity and complexity
- Artificial languages
 - Constructed (planned a priori or a posteriori)
 - Engineered languages experiments in logic, philosophy, linguistics
 - Auxiliary languages international communication (e.g. Esperanto, Ido, Interlingua)
 - Artistic languages aesthetic pleasure or humorous effect (e.g. Klingon)
 - Formal
 - Computer programming languages (e.g. Java, Haskell, C, C++, Ruby)
 - Files and formats descriptions (e.g. YAML, JSON, XML)

Description of natural languages

A really small bit of history

- In the late 1950's Noam Chomsky tried to describe natural languages
- Important paper: "Three models for the description of language", Noam Chomsky (1956).
- In a result of his research two disciplines originated:
 - **1** Theory of formal grammars
 - @ Generative (transformational) grammars



Figure 1: Professor of Linguistics (Emeritus) at MIT, Cambridge

Description of natural languages

What we know now?

- Description of natural languages is hard
- Description of any natural languages might be impossible

Why this is important?

- Better understanding of language creation processes
- More insights into functioning of our brain
- Natural language processing (NLP)
 - Translations (e.g. Google Translator)
 - Synthesis (e.g. speech generation)
 - Perceiving (e.g. robots, voice-control)

Description of formal languages

Result

Description of natural languages help us describe an artificial (formal) ones

Programming languages

- Protocol for communication with the computer
- Performing operations and computations
- Interpretation and execution
- Compilation
- Static code analysis

Data formats

- Structured data
- Interchangeable model for communication and data transmission

Alphabet

Alphabet

A set Σ of available symbols, the simplest elements in the language

Examples

- binary alphabet {0,1}
- decimal numbers $\{0, 1, 2, 3, ..., 9\}$
- Latin alphabet $\{a, b, c, d, ..., z\}$
- Cyrillic

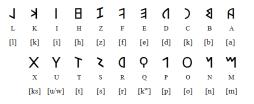


Figure 2: Ancient Latin alphabet

Word (I)

Word

Word w is a sequence of N symbols $w = x_1x_2...x_N$ where $x_i \in \Sigma$ (e.g. 010110, ABCDAAE)

Length

Length of word w is a number of symbols it contains |w| = N (e.g. |010110| = 6, |ABCDAAE| = 7)

Empty word

Special word ϵ with length $|\epsilon| = 0$

Word (II)

Words examples

- w = 010110 word over alphabet $\Sigma = \{0, 1\}$
- w = abc13dj3 word over alphabet $\Sigma = \{a, b, ...z, 0, 1, ...9\}$
- w = ACGTCCGGTA word over alphabet $\Sigma = \{A, C, G, T\}$

Closures

- Σ^* set of all words over Σ
- ullet Σ^+ set of all nonempty words $\Sigma^+ = \Sigma^* ackslash \{\epsilon\}$

Closures examples

- if $\Sigma = \{a\}$ then $\Sigma^* = \{\epsilon, a, aa, aaa, aaaa, aaaaa, aaaaaa, ...\}$
- if $\Sigma = \{a, b\}$ then $\Sigma^+ = \{a, b, aa, bb, ab, ba, aaa, bbb, ...\}$
- if $\Sigma = \{a, b, ..., z\}$ then $\Sigma^+ = \{cat, dog, a, aa, aaa, ...\}$

Language

Definition

Formal language $L\subseteq \Sigma^*$ is a subset of all words built over an alphabet Σ

Examples

- Language L_1 of palindromes in English $L_1 = \{mum, hannah, madam, ...\}$
- Morse code with alphabet $\Sigma = \{\cdot, -\}, L_2 = \{\cdot -, \cdot \cdot ..., - \cdot \cdot\}$
- Empty language
- English language
- Language L_3 with the set of words with fixed-size of N

Grammar

Grammar

- Description of a language
- A recipe for composing elements into sentence
- Describes syntax of a language

Definition

Grammar is a system $G = (V_T, V_N, P, S)$ where:

- V_T terminals (alphabet Σ)
- V_N nonterminals
- P production rules
- S start symbol, $S \in V_N$

Grammar and languages

Definition

Grammar is a system $G = (V_T, V_N, P, S)$ where:

- V_N, V_T, P are finite, nonempty sets
- $V_N \cap V_T = \emptyset$ are disjoint
- $V = V_N \cup V_T$ vocabulary (terminals and nonterminals)
- $P \subseteq V^+ \times V^*$

Grammar and languages

- Sentence generated by some G is every $w \in \Sigma^*$ for each exists derivation from S
- Language L(G) is generated by G and consists of sentences derivate using grammar G
- Two grammars G_1 and G_2 are (weakly) equivalent if $L(G_1) = L(G_2)$

Derivations

$$\bullet$$
 $s \implies s' \implies s'' \implies ... \implies w$

• $s \stackrel{*}{\Longrightarrow} w$

Grammar example

Examples

Digits separated by plus or minus signs

$$list \rightarrow list + list$$

$$list \rightarrow list - list$$

$$\textit{list} \rightarrow \hspace{0.1cm} 0 \hspace{0.1cm}|\hspace{0.1cm} 1 \hspace{0.1cm}|\hspace{0.1cm} 2 \hspace{0.1cm}|\hspace{0.1cm} 3 \hspace{0.1cm}|\hspace{0.1cm} 4 \hspace{0.1cm}|\hspace{0.1cm} 5 \hspace{0.1cm}|\hspace{0.1cm} 6 \hspace{0.1cm}|\hspace{0.1cm} 7 \hspace{0.1cm}|\hspace{0.1cm} 8 \hspace{0.1cm}|\hspace{0.1cm} 9$$

Chomsky's hierarchy

Hierarchy

- Describe the grammar expressiveness
- Describe the grammar hardness
- Tells us what "mechanical procedure" we need to use in order to:
 - Accept language
 - Generate language
- ullet $lpha,eta\in V^*$ any sequence of terminals and nonterminals
- ullet $\gamma \in V^+$ any nonempty sequence of terminals and nonterminals
- $A, B \in NT$ nonterminals
- $a, b \in \Sigma$ terminals

Grammar	Language	Automaton	Production rules
Type-0	Recursively enumerable	Turing machine	$\alpha \to \beta$
Type-1	Context-sensitive	Linear bounded ND TM	$\alpha A \beta \to \alpha \gamma \beta$
Type-2	Context-free	ND pushdown	$\alpha \rightarrow \gamma$
Type-3	Regular	Finite state	A ightarrow a and $A ightarrow aB$

Limiting condition

For all production rules $\forall (\alpha \rightarrow \beta) \in P$ it is true:

First condition

• $|\alpha| \le |\beta|$ - they don't decrease length of a word

Second condition

- $\alpha \in V_N$ is a nonterminal
- $\beta \in V^+$ is not empty

Third condition

- $\alpha \in V_N$ is a nonterminal
- β has a form $\beta = a$ or $\beta = aB$ where $a \in V_T, B \in V_N$

Grammar examples

Grammar

Let $G = (V_N, V_T, P, S)$, where

- $V_N = \{S\}$
- $V_T = \{a, b\}$
- $\bullet \ P = \{S \to aS \lor S \to Sa, S \to b\}$

Derivations

$$S \implies aS \implies aaS \implies aaaaS \implies aaaaaS \implies ...$$

$$S \Longrightarrow Sa \Longrightarrow S$$
aa $\Longrightarrow S$ aaa $\Longrightarrow S$ aaaa $\Longrightarrow S$ aaaaa $\Longrightarrow ...$

Language

$$L(G) = \{a^n b\}, \text{ where } n \geq 0$$

Example sentences

b, ab, aab, aaab, aaaab, aaaaab, aaaaaab, aaaaaaab, aaaaaaab, ...

Grammar example: mirror language

Grammar

Let $G = (V_N, V_T, P, S)$, where

- $V_N = \{S\}$
- $V_T = \{a, b\}$
- $\bullet \ \ P = \{S \rightarrow aSa, S \rightarrow bSb, S \rightarrow aa, S \rightarrow bb\}$

Derivations

$${\color{red}S} \implies {\color{blue}aS}{\color{blue}a} \implies {\color{blue}abS}{\color{blue}b}{\color{blue}b} \implies {\color{blue}abbaS}{\color{blue}abba} \implies {\color{blue}abbaS}{\color{blue}abba} \implies {\color{blue}...}$$

Language

 $L(G) = \{ww^R\}$, where w^R represents reflection of w, and $|w| \ge 1$. This language L(G) is called a *mirror language*.

Example sentences

aa, bb, aaaa, abba, baab, bbbb, abaaba, baaaab, abbbba, babbab, aaaaaa...

Grammar example

Grammar

Let $G = (V_N, V_T, P, S)$, where

- $V_N = \{S, E, F\}$
- $V_T = \{a, b, c, d\}$
- $P = \{S \rightarrow ESF, S \rightarrow EF, E \rightarrow ab, F \rightarrow cd\}$

Derivations

$$S \Rightarrow ESF \Rightarrow EESFF \Rightarrow EEESFFF \Rightarrow E^{n-1}SF^{n-1} \Rightarrow E^nF^n$$

Language

$$L(G) = \{(ab)^n (cd)^n\}, \text{ where } n \ge 1.$$

Example sentences

abcd, ababcdcd, abababcdcdcd, ababababcdcdcdcd, ...

Grammar example

Grammar

Let $G = (V_N, V_T, P, S)$, where

- $V_N = \{S, E, F\}$
- $V_T = \{a, b, c, d\}$
- $\bullet \ \ P = \{S \rightarrow \textit{ESF}, S \rightarrow \textit{abcd}, \textit{Ea} \rightarrow \textit{aE}, \textit{dF} \rightarrow \textit{Fd}, \textit{Eb} \rightarrow \textit{abb}, \textit{cF} \rightarrow \textit{ccd}\}$

Derivations

$$S \implies ESF \implies EabcdF \implies aEbcdF \implies aEbcFd \implies aabbcFd \implies aabbccdd$$

Language

$$L(G) = \{a^n b^n c^n d^n\}, \text{ where } n \geq 2.$$

Sentences

 $aabbccdd, aaabbbcccddd, aaaabbbbccccdddd, aaaaabbbbbcccccddddd, \dots$

Grammar example - regular

Grammar

Let $G = (V_N, V_T, P, S)$, where

- $V_N = \{S, B\}$
- $V_T = \{a, b\}$
- $P = \{S \rightarrow aB, B \rightarrow bS, B \rightarrow b\}$

Derivation

$${\color{red} S} \implies {\color{blue} ab} {\color{blue} S} \implies {\color{blue} aba} {\color{blue} B} \implies {\color{blue} abab} {\color{blue} S} \implies {\color{blue} ababa} {\color{blue} B} \implies ...$$

Language

$$L(G) = \{(ab)^n\}, \text{ where } n \ge 1.$$

Derivation trees

Also : tree diagrams, phrase markers. For regular and context-free grammars.

Chomsky's Normal Form

Language and grammar

Two common tasks:

- Check if language is legal (accepted by the grammar) trace all the applicable rules (derive it language from the start symbol) or... use corresponding automaton!
- Generate language from grammar start from start symbol, go through all applicable rules

Backus-Naur form (BNF)

Backus-Naur form (BNF)

Notation technique for *context-free grammars*. Frequently used to describe syntax of *programming languages*, *document formats* etc.

Syntax

```
<term> ::= __expression__
```

- <term> is a nonterminal
- __expression__ is a sequence of one or more terminal and/or nonterminal symbols separated by vertical line |
- Terminal symbols: a, b, c, A, 0, 1, 2 etc.
- Nonterminal symbols: <digit>, <postal-code> etc.

Backus-Naur form (BNF)

Meta-symbols

- ::= production rule definition
- | rule alternative
- <> nonterminals
- "" literal
- < EOL > End Of Line

Examples

```
<digit> ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
<postal-code> ::= <digit> <digit> <digit> <digit> <digit> <digit>
```

BNF example: Palindrome

Palindrome grammar

Results

a bb

bb bab

pop

hannah

BNF example: Postal address

Postal address grammar

```
<postal-address> ::= <name-part> <street-address> <zip-part>
<name-part> ::= <first-name> <last-name> <EOL>
<street-address> ::= <number> <street-name> <apt-num> <EOL>
<zip-part> ::= <postal-code> <town-name> <EOL>
<apt-num> ::= <number> | ""
```

ANTLR v4

Parser generator

content...

ANTLR

A parser generator which allows to:

•

Usages

- Twitter search queries are parsed using ANTLR
- Lex Machina extracts informations from legal texts using ANTLR

^alexmachina com

ANTLR syntax (I)

Grammar structure

```
grammar ANY_NAME;
options {...}
import ...;
tokens {...}
channels {...}
@actionName {...}
// lexer rules
LEXER_RULE1
LEXER_RULE2
// parser rules
parser_rule1
parser_rule2
```

Grammar properties

- Each section can be specified in any order
- Only one definition for sections: *options*, *imports*, *tokens*
- The header and at least one rule are mandatory

Reserved keywords

import, fragment, lexer, parser, grammar, returns, locals, throws, catch, finally, mode, options, tokens

Grammar file

The file name with grammar ANY_NAME must be called ANY_NAME.g4

Lexer vs parser

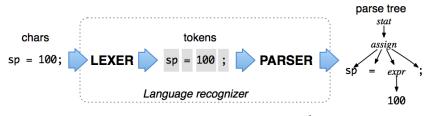


Figure 3: Caption goes here¹

Lexer

Tokens (terminal symbols with semantics) are symbols for the parser. Parser understands context-free grammar (Chomsky's level 2).

¹From ANTLR4 on-line documentation

ANTLR syntax (II)

Syntax	Description
X	Match token, rule or subrule x
<i>xyz</i>	Match a sequence of elements
()	Sub-rule with multiple alternatives
<i>x</i> ?	Match x or skip it
X*	Match x zero or more times
x+	Match x one or more times
r:	Define rule <i>r</i>
r:()	Define rule r with multiple alternatives

ANTLR patterns

Pattern name	Examples
Sequence	'[' INT+ ']'
Sequence with terminator	(statement ';')*
Sequence with separator	(expr (',' expr)*)?
Choice	type : 'int' 'float'
Token dependency	ID '[' expr ']'
Nested phrase	expr : '(' expr ')' ID

Action and semantic predicate

First grammar

Simple grammar (Hello.g4)

```
// define a grammar called Hello
grammar Hello;
// match lower-case identifiers
ID : [a-z]+;
// skip spaces, tabs, newlines, \r (Windows)
WS : [ \t\r\n]+ -> skip;
// match keyword hello followed by an identifier
r : 'hello' ID;
```

Nested arrays

Nested arrays grammar (ArrayInit.g4)

```
grammar ArrayInit;
// matches at least one comma-separated value between {...}
init : '{' value (',' value)* '}';
// A value can be either a nested array or an integer (INT)
value : init | INT;
// define token INT as one or more digits
INT : [0-9]+;
WS : [ \t\r\n]+ -> skip;
```

// parser rules start with lowercase letters, lexer rules with uppercase

Parser tester

```
import org.antlr.v4.runtime.*;
import org.antlr.v4.runtime.tree.*;
public class Test {
    public static void main(String[] args) throws Exception {
        // create a CharStream that reads from standard input
        ANTLRInputStream input = new ANTLRInputStream(System.in);
        // create a lexer that feeds off of input
        CharStream ArrayInitLexer lexer = new ArrayInitLexer(input);
        // create a buffer of tokens pulled from the lexer
        CommonTokenStream tokens = new CommonTokenStream(lexer);
        // create a parser that feeds off the tokens buffer
        ArrayInitParser parser = new ArrayInitParser(tokens);
        ParseTree tree = parser.init();
        System.out.println(tree.toStringTree(parser));
```

Calculator

```
grammar Expr;
prog: stat+;
stat: expr NEWLINE
    | ID '=' expr NEWLINE
     NEWLINE:
expr: expr ('*'|'/') expr
    | expr ('+'|'-') expr
    | INT
| ID
| '(' expr ')';
ID : [a-zA-Z]+;
INT : [0-9]+:
// return newlines to parser (is end-statement signal)
NEWLINE: ' \ r'? ' \ n';
WS : [ \ \ \ ]+ \rightarrow skip;
```

Generated parser

Generated lexer

Generated tree visitor

Generated tree listener

Importing grammars

show two files : lexer & grammar

ANTLR caveats

• Lexer/Parser rules order matter

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