

Programming Assignment - 8

Quicksort and Priority Queue

1) Priority Queues

Suppose that the sequence `M Y P R I O * R * * I * T * Y * * * Q U E * * * U * E *` (where a letter means *insert* and an *asterisk* means remove the maximum) is applied to an initially empty priority queue. **Give the sequence of heaps** and the sequence letters returned by the *remove the maximum* operations.

2) Quicksort – Optimized version of 3-Way Quicksort

Implement an optimized version 3-Way quicksort algorithm with the following changes:

- a) Pivot: (i) First element (or any random element) and (ii) median of `a[left]`, `a[center]`, and `a[right]` of the subarray (or any three random elements in the subarray)
- b) Cutoff to insertion sort for subarrays with less than `M` elements from 0 to 30.

You need to add the following two methods:

- a) `getPivot(a, lo, hi)` method that returns the pivot element based on your chosen strategy in the subarray `a[lo..hi]`
- b) `insertionSort(a, lo, hi)` that sorts the subarray `a[lo..hi]`

Empirically determine the value `M` for which value of quicksort runs fastest in your environment to sort random arrays of `N` doubles, for $N = 10^3$, 10^4 , 10^5 , and 10^6 . Plot the average running times for `M` from 0 to 30.

3) Ternary heapsort

Implement a version of heapsort based on complete **ternary** heap as similar to the binary heap described in the text. Test your implementation using 100 randomly ordered distinct keys.