

Chapter 10: Circles – Class 10 Maths

Key Concepts

1. A **circle** is the set of all points in a plane that are at a **fixed distance (radius)** from a fixed point (center).
2. **Chord** – a line segment joining any two points on the circle.
3. **Secant** – a line that intersects the circle in **two** points.
4. **Tangent** – a line that touches the circle at **only one** point.

Tangent to a Circle

- A **tangent** is a special case of a secant where both endpoints of the chord coincide.
- The **point of contact** is the only common point between the tangent and the circle.

Important Theorems

Theorem 10.1:

The tangent to a circle is perpendicular to the radius at the point of contact.

If O is the center, P is point of contact, and XY is the tangent, then
 $OP \perp XY$

Theorem 10.2:

The lengths of tangents drawn from an external point to a circle are equal.

If tangents PA and PB are drawn from a point P to a circle with centre O, then:
 $PA = PB$

How Many Tangents Can You Draw?

Position of the point	No. of tangents
Inside the circle	0
On the circle	1
Outside the circle	2

Some More Results

- The line through the radius and the point of contact is called the **normal**.
- Tangents drawn at the **ends of a diameter** are always **parallel**.
- A line **perpendicular** to a tangent at the point of contact **passes through the centre**.

Formula to Find Tangent Length

If a point lies outside the circle:

Length of tangent = $\sqrt{(\text{Distance}^2 \text{ from centre} - \text{Radius}^2)}$

Important Examples (Quick View)

- Two tangents drawn from a point are equal.
- Tangents at endpoints of a chord bisect it if they touch an inner circle.
- Angle between tangents from external point = $2 \times$ angle between radius and tangent.
- In a quadrilateral circumscribing a circle: $AB + CD = AD + BC$

Previous Year Exam Focus

Type of Question	Frequency
Prove tangent is \perp to radius	★★★★★
Equal length tangents from external point	★★★★★
Quadrilateral with circle ($AB + CD = AD + BC$)	★★★★★
Use Pythagoras to find tangent length	★★★★★
Tangents from diameter or parallel tangents	★★★

Summary

1. **Tangent** touches the circle at one point.
2. Tangent is always **perpendicular to the radius** at the point of contact.
3. **From a point outside a circle**, exactly **two equal tangents** can be drawn.