Chapter 8: Quadrilaterals

What is a Quadrilateral?

- A quadrilateral is a polygon with 4 sides and 4 angles. Examples: Square, Rectangle, Rhombus, Parallelogram, Trapezium, Kite
- Sum of all interior angles of any quadrilateral = 360°

Types of Quadrilaterals & Their Properties

Туре	Key Properties
Parallelogram	Opposite sides equal, opposite angles equal, diagonals bisect each other
Rectangle	All angles 90°, opposite sides equal, diagonals are equal & bisect each other
Rhombus	All sides equal, opposite angles equal, diagonals bisect at 90°
Square	All sides equal, all angles 90°, diagonals are equal & bisect at 90°
Trapezium	Only one pair of opposite sides is parallel
Kite	Two pairs of adjacent sides equal, one diagonal bisects the other at 90°

📏 Note:

- In any parallelogram, diagonal divides it into two congruent triangles
- Midpoint theorem: Line joining midpoints of two sides of a triangle is parallel to the third side and half of it

Important Theorems

A quadrilateral is a parallelogram if:

- Opposite sides are equal
- Opposite angles are equal
- Diagonals bisect each other
- One pair of opposite sides is equal and parallel
- ✓ The quadrilateral formed by joining midpoints of sides of any quadrilateral is a parallelogram
- 🗸 In rectangle: Diagonals are equal
- **✓ In rhombus:** Diagonals bisect at 90°
- ✓ In square: Diagonals are equal & perpendicular

? Multiple Choice Quick Practice

Example:

Q: If \angle BOC = 90° and \angle BDC = 50° in a parallelogram, then \angle OAB = ?

Answer: 40°

Q: A quadrilateral with angles in ratio 3:7:6:4 → Total = 360° Solve to find each angle and the type (e.g., trapezium)

Reasoning-Based Short Questions

- Can all angles of a quadrilateral be obtuse? X No! 4 obtuse angles > 360°
- © Can a quadrilateral have 3 equal angles? ✓ Possible but not necessarily a parallelogram
- 🧠 If diagonals of a quadrilateral bisect each other, is it a parallelogram? 🗹 Yes!
- If diagonals of a rectangle are perpendicular? X No, that's a rhombus or square

9 If a diagonal bisects one angle in a parallelogram \rightarrow it also bisects the opposite angle 4 (proven by congruence)

Application-Based Problems

- I Joining midpoints of sides of rhombus → forms a rectangle
- III Midpoints of square → again form a square
- In trapezium, line joining midpoints of non-parallel sides is parallel to parallel sides & half their sum

Geometry HOTS & Constructions

- **(©)** In parallelogram, if two opposite sides' midpoints are joined and extended, it forms another parallelogram
- ⊚ If diagonals of a quadrilateral are equal & perpendicular → joining midpoints → square

Long Answer Highlights

- Show that the figure formed by joining midpoints of a rhombus is a rectangle:
 - Use midpoints → prove opposite sides // and equal
 - Use diagonal properties → prove angle = 90°
- Prove: A diagonal of parallelogram bisecting one angle → also bisects opposite angle
 - Use alternate angle theorem + congruence
- Quadrilateral bisectors form a rectangle
 - Use angle bisector properties and symmetry

Summary Table

Property/Concept	Key Result
Sum of interior angles (quadrilateral)	360°
Parallelogram diagonals	Bisect each other
Rectangle diagonals	Equal and bisect each other
Rhombus diagonals	Bisect at 90°
Square diagonals	Equal, bisect at 90°
Midpoints joined (quadrilateral)	Forms a parallelogram
Diagonal bisecting one angle (parallelogram)	Also bisects opposite angle