Part 1: Analog Circuits

Principles

Ohm's Law:

$$V = IR \qquad P = VI = I^2R = \frac{V^2}{R}$$

Resistors and Capacitors: Parallel vs. Series:

$$R_{\text{series}} = R_1 + R_2$$
 $R_1 || R_2 = \left(\frac{1}{R_1} + \frac{1}{R_2}\right)^{-1}$

$$C_1||C_2 = C_1 + C_2$$
 $C_{\text{series}} = \left(\frac{1}{C_1} + \frac{1}{C_2}\right)^{-1}$

Capacitors and RC Charging/Discharging:

$$C = \frac{Q}{V} \qquad C = \frac{\epsilon_r \epsilon_0 A}{D}$$

Permittivity of Free Space: $\epsilon_0 = 8.854 \times 10^{-12} F/m$

Energy stored:
$$E_C = \frac{1}{2}CV^2$$

Charging:
$$V_C = V_{in} \left(1 - e^{-t/\tau} \right)$$

Discharging:
$$V_C = V_0 e^{-t/\tau}$$

Voltage and Current Dividers:

$$V_2 = V_1 \frac{Z_2}{Z_1 + Z_2} \qquad I_{R_1} = I_T \frac{R_2}{R_1 + R_2}$$

Methods & Tools

Thevenin Equivalence

 R_{th} : Remove load, short voltage sources, and open current sources. Find resistance which the load sees.

 V_{th} : Remove load and find open-circuit voltage.

Norton Equivalence

$$R_{nor} = R_{th}$$
 $V_{th} = I_{nor}R_{nor}$

Fourier Transforms

Continuous Domain:
$$V(\omega) = \int_{-\infty}^{\infty} v(t)e^{-j\omega t}dt$$

$$v(t) = a_0 + \sum_{i=1}^{\infty} \left[a_i \cos(\omega_i t) + b_i \sin(\omega_i t) \right]$$

$$a_i = \frac{2}{T} \int_0^T v(t) \cos(\omega_i t) dt$$
 $b_i = \frac{2}{T} \int_0^T v(t) \sin(\omega_i t) dt$

Common component Fourier-Domain Impedances:

$$Z_R(\omega) = R$$
 $Z_C(\omega) = \frac{1}{j\omega C}$ $Z_L = j\omega L$

• Capacitor: Voltage lags current by 90°

• Inductor: Voltage leads current by 90°

Power

Transformers

Faraday's Law: $V = -N \frac{\mathrm{d}}{\mathrm{d}t} [B \cdot A]$

$$\Rightarrow V_s = \frac{N_s}{N_p} V_p \qquad \qquad I_s = \frac{N_p}{N_s} I_p$$

Zener Diodes

Dynamic resistance: $\frac{\Delta V}{\Delta I} = R_{DYN}$

Linear Regulators (LM317)

$$V_{out} = 1.25 \left(1 + \frac{R_2}{R_1} \right)$$

AC/DC Converters: Linear

Main components:

- Transformer adjusts AC voltage
- Diode bridge rectifies the signal
- Capacitor smooths DC
- Linear regulator gives final cleaned output

AC/DC Converters: Switching

Main components:

- Diode bridge rectifies 60 Hz AC voltage
- Capacitor smooths DC
- Switch (controlled by feedback loop) adjusts voltage with PWM and switches at a much higher frequency
- Transformer acts on this new higher frequency AC
- Cleaned by another capcitor and linear regulator

Main advantages: higher switching frequency \rightarrow smaller transformer (Faraday's Law); more efficient.

DC/DC Converters

- Buck Converter: Step Down
- Boost Converter: Step Up
- Buck/Boost: Inverting, Step Up or Down

Main takeaways:

- Very efficient no intentionally dissipative components
- Switching devices \rightarrow the output will always have some noise

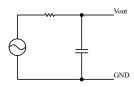
Filters

Cutoff frequency ω_0 is defined such that:

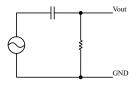
$$\omega_0 = \frac{1}{RC} \qquad \rightarrow \qquad |H(\omega_0)| = \frac{1}{\sqrt{2}}$$

Passive

Low-Pass Filter:

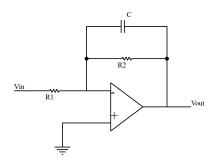


High-Pass Filter:

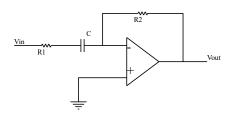


Active (Inverting Topologies)

Low-Pass Filter:



High-Pass Filter:



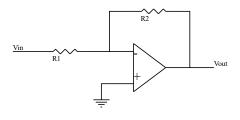
Amplifier Circuits

Golden Rules:

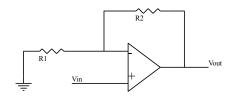
• Golden Rule 1: $I_{in} \rightarrow 0$

• Golden Rule 2: $V_A = V_B$

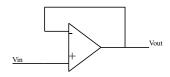
Inverting Amplifier:
$$H(\omega) = \frac{-R_2}{R_1}$$



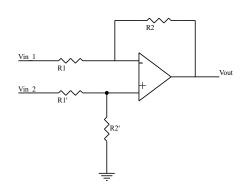
Non-inverting Amplifier: $H(\omega) = 1 + \frac{R_2}{R_1}$



Buffer (Voltage Follower): $V_{out} = V_{in}$



Difference Amplifier:
$$V_{out} = (V_2 - V_1) \frac{R_2}{R_1}$$



Part 2: Digital and Communications

Key topics:

- Binary. octal, and hexadecimal number systems
- ADCs quantize signal amplitude and sample in discrete time

Types of ADCs (increasing speed, decreasing precision):

- 1. Integrating
- 2. Sigma Delta
- 3. Successive Approximation
- 4. Subranging
- 5. Flash

Aliasing equation:

$$f_{\text{signal}} = |f_0 \pm N f_s|$$

where f_{signal} is the true signal frequency, f_0 is the apparent (measured) frequency, and f_s is the sampling frequency.

Serial Communications

Types of directional transmission:

- Simplex: data flows in one direction
- Half duplex: data can flow in either direction, but only in one direction at a time
- Full duplex: data flows in both directions simultaneously

RS-232 Data Frame:

- 1. Start bit (0)
- 2. Data bits, starting with LSB
- 3. Parity bit (optional)
- 4. Stop bit(s)

Serial Port Parameter Shorthand:

$$\underbrace{9600}_{\text{buad rate}} - \underbrace{8}_{\text{bits}} - \underbrace{E}_{\text{c}} - \underbrace{1}$$

Combinatorial Logic

DeMorgan's Law:

AND

$$\overline{AB} = \overline{A} + \overline{B}$$
 $\overline{A+B} = \overline{A} \ \overline{B}$ OR NAND NOR NOT XOR

Sequential Logic

Half-adder:

Full-adder:

SR Latch (NAND):

	\bar{S}	\bar{R}	Q	$ar{Q}$	Condition
ĺ	0	0	1	1	Race
	0	1	1	0	Set
	1	0	0	1	Reset
	1	1	Q	\bar{Q}	Hold

D Latch:

D	Q	$ar{Q}$	Mode
0	0	1	Reset
1	1	0	Set

 ${\it JK}$ Flip-Flop:

J	K	Q	\bar{Q}	Condition
0	0	Q	\bar{Q}	Hold
0	1	0	0	Reset
1	0	0	0	Set
1	1	\bar{Q}	Q	Toggle

Wireless Communications

Frequency mixing:

- Euler Identity: $\cos(\omega_0 t) = \frac{1}{2} \left(e^{j\omega_0 t} + e^{-j\omega_0 t} \right)$
- Multiply two sine waves $\rightarrow f = f_1 \pm f_2$ (half amplitude)
- Add two sine waves \rightarrow both frequencies are present
- Basic AM: $S(t) = B[1 + M \cdot x(t)] \cos(2\pi f_c t)$
- Diode mixers can do mediocre AM by rectifying the sum of the signals
- Basic FM: $S(t) = B \cos \left[2\pi f_c t + \frac{f_{\delta}}{f_m} \cos(2\pi f_m t) \right]$
- FM Bandwidth (Carson's Rule): $BW \approx 2(f_{\Delta} + f_m)$

Antennas

Transmission and Reception

Antenna gain:

$$G = 4\pi \eta \frac{A_{\text{phys}}}{\lambda^2} = 4\pi \frac{A_e}{\lambda^2} = \eta \left(\frac{\pi D}{\lambda}\right)^2$$
 $\lambda = \frac{G}{M}$

(Approximate) antenna beamwidth (half-power):

$$G\theta^2 \approx 4\pi\eta \left(\frac{180}{\pi}\right)^2 \approx \eta 41,253 \text{ deg}^2$$

Transmitter Irradiance:

$$I(R) = \frac{P_t L_t G_t}{4\pi R^2} = \frac{\text{EIRP}}{4\pi R^2} [\text{W/m}^2]$$

Received power (Friis equation):

$$P_r = I(R) \cdot A_e \qquad \rightarrow \qquad P_r = \frac{P_t G_t G_r \lambda^2}{(4\pi R)^2}$$

Alternate form — Space Loss:

$$L_s = \left(\frac{\lambda}{4\pi R}\right)^2 \qquad \rightarrow \qquad P_r = P_t G_t L_t G_r L_s$$

Noise

$$T_{ant} = \eta T_{ext} + (1 - \eta) T_{phys}$$

Noise Factor (F, linear) and Noise Figure (NF, dB):

$$F = 1 + \frac{T_{Rx}}{T_0}$$
 $NF = 10 \log_{10}(F)$

Total System Noise:

$$T_{sys} = T_{ant} + \frac{T_{cable}}{L} + \frac{T_{Rx}}{L}$$

Noise Power Density $(N_O, [W/Hz])$ and Noise Power (N, [W]):

$$N_O = kT_{sys}$$
 $N = KT_{sys}B$

$$P_{signal} = \frac{P_t L_t G_t G_r L_{atm} \lambda^2}{(4\pi R)^2} = \text{EIRP} \cdot G_r L_{atm} L_s$$
$$\text{SNR} = \frac{P_{signal}}{N_O B} = \frac{C}{N_O} \frac{1}{R}$$

Factor of Merit = FOM =
$$\frac{G_r}{T_{sus}}$$

$$SNR = \frac{1}{k} \cdot EIRP \cdot FOM \cdot (L_{atm}L_s) \cdot \frac{1}{R}$$

Digital \rightarrow SNR= $\frac{E_b}{N_O}$:

$$SNR_{min} = \frac{C}{N_O}[dB] - 10\log_{10}(R) + RDM$$

Link margin = actual SNR - minimum SNR