

# Intermediate Value Theorem Project

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## 0.1 Definitions

**Definition 1** (Sequence). A sequence is a function  $s : \mathbb{N} \rightarrow$  for some set  $X$ .

**Definition 2** (Convergence). A sequence  $s : \mathbb{N} \rightarrow X$  converges to  $x \in X$  if for every neighbourhood  $U$  of  $x$  there exists  $N \in \mathbb{N}$  such that for all  $n \geq N$ ,  $s(n) \in U$ .

**Theorem 3** (Smale 1958). *There is a homotopy of immersions of  $\mathbb{S}^2$  into  $\mathbb{R}^3$  from the inclusion map to the antipodal map  $a : q \mapsto -q$ .*

*Proof.* This obviously follows from what we did so far. Testing changing my branch □