Report 1

Team information (B23-ISE-02):

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Link to the product:

- https://github.com/quintet-sdr/optimization-a1

Programming language:

- TypeScript (Bun)
- To launch the code: \$\\$ bun test

Linear programming problem:

- Maximization
- Approximation accuracy $\epsilon = 0.001$

Tests:

- (1) **Input:**
 - Objective function: $F(x_1, x_2) = 10x_1 + 20x_2$

- Constraints:
$$\begin{cases} -x_1 + 2x_2 \le 15 \\ x_1 + x_2 \le 12 \\ 5x_1 + 3x_2 \le 45 \\ x_1, x_2 \ge 0 \end{cases}$$

Output:

- Decision variables: {3,9}
- Maximum value: 210
- (2) **Input:**
 - Objective function: ...
 - Constraints: ...

Output:

- Unbounded solution

Code: src/util.ts export function arrayOf<T>(n: number, item: () => T): T[] { return new Array(n).fill(undefined).map(item); } export function prettyPrintWith(tableau: number[][], rowNames: string[], colNames: string[], precision: number,): void { prettyPrint([["Basic", ...colNames], \dots tableau.map((row, j) => [rowNames[j], ...row.map((num) => num.toFixed(precision)),]),]); } export function printHeading(text: string): void { const lines = new Array(24).fill("-").join(""); $console.log("\n" + `$\{lines\}[$\{text\}]$\{lines\}` + "\n");$ function prettyPrint(tableau: string[][]) { let colMaxes = []; for (let j = 0; j < tableau[0].length; <math>j += 1) { colMaxes.push(Math.max.apply(null, $tableau.map((row) \Rightarrow row[j]).map((n) \Rightarrow n.length),$),); } tableau.forEach((row) => console.log.apply(null,

row.map(

),),); } '\${new Array(colMaxes[j] - val.length + 1).join(" ")}\${val} ',

```
src/lib.ts
import { arrayOf, prettyPrintWith, printHeading } from "./util";
export type SimplexResult =
  | {
      ok: true;
      x: number[];
      max: number;
    }
  | {
      ok: false;
      error: "unbounded" | "no-pivot-row" | "no-pivot-col";
    };
/**
 * @param c - The coefficients of the objective function.
 \ast @param a - The coefficients of the constraint functions.
 \ast @param b - The right-hand side numbers.
 * Oparam eps - Precision in logging (digits after the decimal point).
 * @returns An object containing the computed decision variables and maximum value.
 */
export function maximize(
  c: number[],
  a: number[][],
  b: number[],
  eps: number,
): SimplexResult | never {
  assertLengths(c, a, b);
  const xStrings = c.map((_, i) \Rightarrow i + 1).map((i) \Rightarrow 'x[${i}]');
  const sStrings = a.map((_, i) \Rightarrow i + 1).map((i) \Rightarrow 's[${i}]');
  printHeading("* Simplex *");
  console.log(
    'Function: F(${xStrings.join(", ")}) = ${c.map((coeff, i) => '${coeff}}${xStrings[i]}').join(" + ")}',
  const rowNames = ["z", ...sStrings];
  const colNames = [...xStrings, ...sStrings, "Solution"];
  let tableau = buildTableau(c, a, b);
  const tableauCols = tableau[0].length;
  console.log("\n" + "Initial table:");
  prettyPrintWith(tableau, rowNames, colNames, eps);
  let iteration = 0;
  while (true) {
    if (checkUnbounded(tableau)) {
      printHeading("~Unbounded~");
      return { ok: false, error: "unbounded" };
    }
    iteration += 1;
    printHeading('Iteration ${iteration}');
    const pivotCol = findPivotCol(tableau[0]);
    if (pivotCol === undefined) {
      return { ok: false, error: "no-pivot-col" };
    }
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const ratios = tableau.map((row) => row[tableauCols - 1] / row[pivotCol]);
  const pivotRow = findPivotRow(ratios);
  if (pivotRow === undefined) {
    return { ok: false, error: "no-pivot-row" };
  }
  const pivotElement = tableau[pivotRow][pivotCol];
  console.log("Initially:");
  prettyPrintWith(
    tableau.map((row, i) => [...row, ratios[i]]),
    rowNames,
    [...colNames, "Ratio"],
    eps,
  );
  console.log();
  console.log('Pivot row: ${rowNames[pivotRow]}');
  console.log('Pivot column: ${colNames[pivotCol]}');
  console.log('Pivot element: ${pivotElement.toFixed(eps)}');
  tableau[pivotRow] = tableau[pivotRow].map((it) => it / pivotElement);
  console.log("\n" + "After dividing the pivot row:");
  prettyPrintWith(tableau, rowNames, colNames, eps);
  tableau = crissCrossed(tableau, pivotRow, pivotCol);
  if (rowNames[pivotRow] !== colNames[pivotCol]) {
    console.log(
      "\n" + '${rowNames[pivotRow]} leaves, ${colNames[pivotCol]} enters',
   rowNames[pivotRow] = colNames[pivotCol];
  }
  console.log("\n" + "After the iteration:");
  prettyPrintWith(tableau, rowNames, colNames, eps);
  if (tableau[0].every((it) => it >= 0)) {
    break;
  }
printHeading("Final Table");
prettyPrintWith(tableau, rowNames, colNames, eps);
const answer = tableau[0][tableauCols - 1];
const xIndexes = arrayOf(c.length, () => 0);
rowNames
  .map((rowName, i) => ({ rowName, i }))
  .slice(1)
  .forEach(({ rowName, i }) => {
    if (rowName.startsWith("x")) {
      const numPart = Number.parseInt(rowName.match(/\[(\d+)\]/)![1]);
      xIndexes[numPart - 1] = tableau[i][tableauCols - 1];
    }
 });
const result: SimplexResult = {
  ok: true,
  x: xIndexes,
```

}

```
max: answer,
 };
 console.log();
  console.log('Decision variables: ${result.x}');
 console.log('Maximum value: ${result.max}');
 return result;
}
function buildTableau(c: number[], a: number[][], b: number[][]: number[][] {
  const tableau = arrayOf(1 + a.length, () =>
    arrayOf(c.length + a.length + 1, () => 0),
 for (let i = 0; 1 + i < tableau.length; <math>i += 1) {
    for (let j = 0; j < c.length; j += 1) {
      // Z-row
      tableau[0][j] = -1 * c[j];
     // X-es
     tableau[1 + i][j] = a[i][j];
    }
    // S-es
    tableau[1 + i][c.length + i] = 1;
    // Solution row
    tableau[1 + i][tableau[0].length - 1] = b[i];
 }
 return tableau;
function crissCrossed(
 tableau: number[][],
 pivotRow: number,
 pivotCol: number,
): number[][] {
 const newTableau = tableau.map((row) => row.slice());
 for (let i = 0; i < tableau.length; i += 1) {</pre>
    for (let j = 0; j < tableau[0].length; <math>j += 1) {
      if (i != pivotRow) {
        newTableau[i][j] =
          tableau[i][j] - tableau[i][pivotCol] * tableau[pivotRow][j];
   }
 }
 return newTableau;
function findPivotCol(zRow: number[]): number | undefined {
 return zRow
    .map((value, i) => ({ value, i }))
    .filter(({ value }) => value < 0)</pre>
    .reduce((acc: { value: number; i: number } | undefined, cur) => {
      if (acc === undefined || cur.value < acc.value) {</pre>
        return cur;
     } else {
        return acc;
```

```
}, undefined)?.i;
}
function findPivotRow(ratios: number[]): number | undefined {
    .map((ratio, i) => ({ ratio, i }))
    .filter(({ ratio }) => ratio > 0)
    .reduce((acc: { ratio: number; i: number } | undefined, cur) => {
      if (acc === undefined || cur.ratio < acc.ratio) {</pre>
        return cur;
      } else {
        return acc;
    }, undefined)?.i;
}
function checkUnbounded(tableau: number[][]): boolean {
 return tableau[0]
    .slice(0, -1)
    .map((_, j) \Rightarrow j)
    .some((j) \Rightarrow tableau.every((row) \Rightarrow row[j] <= 0));
}
function assertLengths(c: number[], a: number[][], b: number[]): void | never {
  if (a.length !== b.length) {
    throw new Error(
      'numbers of constraints and right-hand sides don't match':\n' +
        ' constraints: {a} ({a.length})' +
        ' right-hand sides: {b} ({b.length})\n',
    );
 }
  a.forEach((row, i) => {
    if (row.length !== c.length) {
      throw new Error(
        'numbers of coefficients don't match:\n' +
          'function: {c} (s_{c.length})\n' +
          ' constraint ${i + 1}: ${row} (${row.length})',
      );
    }
 });
```

```
src/lib.test.ts
import { expect, test } from "bun:test";
import { maximize, type SimplexResult } from "./lib";
const PRECISION: number = 3;
test("tut-3", () => {
  const left = maximize(
    [10, 20],
    Ε
      [-1, 2],
      [1, 1],
      [5, 3],
    ],
    [15, 12, 45],
    PRECISION,
  );
  const right: SimplexResult = { ok: true, x: [3, 9], max: 210 };
  assertEq(left, right);
});
test("lab-3-problem-1", () => {
  const left = maximize(
    [9, 10, 16],
    Ε
      [18, 15, 12],
      [6, 4, 8],
      [5, 3, 3],
   ],
    [360, 192, 180],
    PRECISION,
  const right: SimplexResult = { ok: true, x: [0, 8, 20], max: 400 };
  assertEq(left, right);
test("lab-3-problem-3", () => {
  const left = maximize(
    [2, -2, 6],
    [
      [2, 1, -2],
      [1, 2, 4],
      [1, -1, 2],
   ],
    [24, 23, 10],
   PRECISION,
  );
  const right: SimplexResult = {
    ok: true,
    x: [0, 3 / 4, 43 / 8],
    max: 123 / 4,
  assertEq(left, right);
});
test("unbounded-1", () => {
  const left = maximize(
```

```
[2, 1],
    Γ
     [1, -1],
      [2, 0],
    [10, 40],
   PRECISION,
 const right: SimplexResult = { ok: false, error: "unbounded" };
 assertEq(left, right);
test("unbounded-2", () => {
  const left = maximize(
    [3, 2],
    [
      [1, -1],
      [-2, 1],
   ],
   [2, -1],
   PRECISION,
 );
 const right: SimplexResult = { ok: false, error: "unbounded" };
 assertEq(left, right);
});
function assertEq(left: SimplexResult, right: SimplexResult): void | never {
 expect(left.ok).toBe(right.ok);
 // HACK: this allows TypeScript to validate types.
 if (!left.ok || !right.ok) {
    if (!left.ok && !right.ok) {
     return expect(left.error).toBe(right.error);
   }
   return;
 }
 expect(left.max).toBeCloseTo(right.max, PRECISION);
 left.x.forEach((_, i) =>
    expect(left.x[i]).toBeCloseTo(right.x[i], PRECISION),
 );
}
```