

# Report 1

**Team information (B23-ISE-02):**

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**Link to the product:**

- <https://github.com/quintet-sdr/optimization-a1>

**Programming language:**

- TypeScript (Bun)

**Linear programming problem:**

- Maximization
- ...

**Code:**`src/util.ts`

```

export function arrayOf<T>(n: number, item: () => T): T[] {
  return new Array(n).fill(undefined).map(item);
}

export function prettyPrintWith(
  tableau: number[][][],
  rowNames: string[],
  colNames: string[],
  precision: number,
): void {
  prettyPrint([
    ["Basic", ...colNames],
    ...tableau.map((row, j) => [
      rowNames[j],
      ...row.map((num) => num.toFixed(precision)),
    ]),
  ]);
}

export function printHeading(text: string): void {
  const lines = new Array(24).fill("-").join("");
  console.log("\n" + `${lines}[ ${text} ]${lines}` + "\n");
}

function prettyPrint(tableau: string[][][]) {
  let colMaxes = [];
  for (let j = 0; j < tableau[0].length; j += 1) {
    colMaxes.push(
      Math.max.apply(
        null,
        tableau.map((row) => row[j]).map((n) => n.length),
      ),
    );
  }

  tableau.forEach((row) =>
    console.log.apply(
      null,
      row.map(
        (val, j) =>
          `${new Array(colMaxes[j] - val.length + 1).join(" ")}${val} `,
      ),
    );
  );
}

```

```
src/lib.ts
```

```
import { arrayOf, prettyPrintWith, printHeading } from "./util";

export type SimplexResult =
  | {
    ok: true;
    x: number[];
    max: number;
  }
  | {
    ok: false;
    error: "unbounded" | "no-pivot-row" | "no-pivot-col";
  };

/**
 * @param c - The coefficients of the objective function.
 * @param a - The coefficients of the constraint functions.
 * @param b - The right-hand side numbers.
 * @param eps - Precision in logging (digits after the decimal point).
 * @returns An object containing the computed decision variables and maximum value.
 */
export function maximize(
  c: number[],
  a: number[][][],
  b: number[],
  eps: number,
): SimplexResult | never {
  assertLengths(c, a, b);

  const xStrings = c.map((_, i) => i + 1).map((i) => `x[${i}]`);
  const sStrings = a.map((_, i) => i + 1).map((i) => `s[${i}]`);

  printHeading("* Simplex *");

  console.log(
    `Function: F(${xStrings.join(", ")}) = ${c.map((coeff, i) => `${coeff}${xStrings[i]}`).join(" + ")}`,
  );

  const rowNames = ["z", ...sStrings];
  const colNames = [...xStrings, ...sStrings, "Solution"];

  let tableau = buildTableau(c, a, b);
  const tableauCols = tableau[0].length;

  console.log("\n" + "Initial table:");
  prettyPrintWith(tableau, rowNames, colNames, eps);

  let iteration = 0;
  while (true) {
    if (checkUnbounded(tableau)) {
      printHeading("~Unbounded~");
      return { ok: false, error: "unbounded" };
    }

    iteration += 1;
    printHeading(`Iteration ${iteration}`);

    const pivotCol = findPivotCol(tableau[0]);
    if (pivotCol === undefined) {
      return { ok: false, error: "no-pivot-col" };
    }
  }
}
```

```

const ratios = tableau.map((row) => row[tableauCols - 1] / row[pivotCol]);
const pivotRow = findPivotRow(ratios);
if (pivotRow === undefined) {
  return { ok: false, error: "no-pivot-row" };
}

const pivotElement = tableau[pivotRow][pivotCol];

console.log("Initially:");
prettyPrintWith(
  tableau.map((row, i) => [...row, ratios[i]]),
  rowNames,
  [...colNames, "Ratio"],
  eps,
);
console.log();
console.log(`Pivot row: ${rowNames[pivotRow]}`);
console.log(`Pivot column: ${colNames[pivotCol]}`);
console.log(`Pivot element: ${pivotElement.toFixed(eps)}`);

tableau[pivotRow] = tableau[pivotRow].map((it) => it / pivotElement);

console.log("\n" + "After dividing the pivot row:");
prettyPrintWith(tableau, rowNames, colNames, eps);

tableau = crissCrossed(tableau, pivotRow, pivotCol);

if (rowNames[pivotRow] !== colNames[pivotCol]) {
  console.log(
    "\n" + `${rowNames[pivotRow]} leaves, ${colNames[pivotCol]} enters`,
  );
  rowNames[pivotRow] = colNames[pivotCol];
}

console.log("\n" + "After the iteration:");
prettyPrintWith(tableau, rowNames, colNames, eps);

if (tableau[0].every((it) => it >= 0)) {
  break;
}
}

printHeading("Final Table");
prettyPrintWith(tableau, rowNames, colNames, eps);

const answer = tableau[0][tableauCols - 1];
const xIndexes = arrayOf(c.length, () => 0);

rowNames
  .map((rowName, i) => ({ rowName, i }))
  .slice(1)
  .forEach(({ rowName, i }) => {
    if (rowName.startsWith("x")) {
      const numPart = Number.parseInt(rowName.match(/\[(\d+)\]/)[1]);
      xIndexes[numPart - 1] = tableau[i][tableauCols - 1];
    }
  });

const result: SimplexResult = {
  ok: true,
  x: xIndexes,

```

```

    max: answer,
  };

  console.log();
  console.log('Decision variables: ${result.x}');
  console.log('Maximum value: ${result.max}');

  return result;
}

function buildTableau(c: number[], a: number[][], b: number[]): number[][] {
  const tableau = arrayOf(1 + a.length, () =>
    arrayOf(c.length + a.length + 1, () => 0),
  );

  for (let i = 0; 1 + i < tableau.length; i += 1) {
    for (let j = 0; j < c.length; j += 1) {
      // Z-row
      tableau[0][j] = -1 * c[j];

      // X-es
      tableau[1 + i][j] = a[i][j];
    }

    // S-es
    tableau[1 + i][c.length + i] = 1;

    // Solution row
    tableau[1 + i][tableau[0].length - 1] = b[i];
  }

  return tableau;
}

function crissCrossed(
  tableau: number[][],
  pivotRow: number,
  pivotCol: number,
): number[][] {
  const newTableau = tableau.map((row) => row.slice());

  for (let i = 0; i < tableau.length; i += 1) {
    for (let j = 0; j < tableau[0].length; j += 1) {
      if (i !== pivotRow) {
        newTableau[i][j] =
          tableau[i][j] - tableau[i][pivotCol] * tableau[pivotRow][j];
      }
    }
  }

  return newTableau;
}

function findPivotCol(zRow: number[]): number | undefined {
  return zRow
    .map((value, i) => ({ value, i }))
    .filter(({ value }) => value < 0)
    .reduce((acc: { value: number; i: number } | undefined, cur) => {
      if (acc === undefined || cur.value < acc.value) {
        return cur;
      } else {
        return acc;
      }
    });
}

```

```

    }
    }, undefined)?.i;
}

function findPivotRow(ratios: number[]): number | undefined {
    return ratios
        .map((ratio, i) => ({ ratio, i }))
        .filter(({ ratio }) => ratio > 0)
        .reduce((acc: { ratio: number; i: number } | undefined, cur) => {
            if (acc === undefined || cur.ratio < acc.ratio) {
                return cur;
            } else {
                return acc;
            }
        }, undefined)?.i;
}

function checkUnbounded(tableau: number[][]): boolean {
    return tableau[0]
        .slice(0, -1)
        .map((_, j) => j)
        .some((j) => tableau.every((row) => row[j] <= 0));
}

function assertLengths(c: number[], a: number[][], b: number[]): void | never {
    if (a.length !== b.length) {
        throw new Error(
            'numbers of constraints and right-hand sides don\'t match:\n' +
            ' constraints: ${a} (${a.length})\n' +
            ' right-hand sides: ${b} (${b.length})\n',
        );
    }

    a.forEach((row, i) => {
        if (row.length !== c.length) {
            throw new Error(
                'numbers of coefficients don\'t match:\n' +
                ' function: ${c} (${c.length})\n' +
                ' constraint ${i + 1}: ${row} (${row.length})',
            );
        }
    });
}

```

```
src/lib.test.ts
```

```
import { expect, test } from "bun:test";

import { maximize, type SimplexResult } from "../lib";

const PRECISION: number = 3;

test("tut-3", () => {
  const left = maximize(
    [10, 20],
    [
      [-1, 2],
      [1, 1],
      [5, 3],
    ],
    [15, 12, 45],
    PRECISION,
  );
  const right: SimplexResult = { ok: true, x: [3, 9], max: 210 };

  assertEq(left, right);
});

test("lab-3-problem-1", () => {
  const left = maximize(
    [9, 10, 16],
    [
      [18, 15, 12],
      [6, 4, 8],
      [5, 3, 3],
    ],
    [360, 192, 180],
    PRECISION,
  );
  const right: SimplexResult = { ok: true, x: [0, 8, 20], max: 400 };

  assertEq(left, right);
});

test("lab-3-problem-3", () => {
  const left = maximize(
    [2, -2, 6],
    [
      [2, 1, -2],
      [1, 2, 4],
      [1, -1, 2],
    ],
    [24, 23, 10],
    PRECISION,
  );
  const right: SimplexResult = {
    ok: true,
    x: [0, 3 / 4, 43 / 8],
    max: 123 / 4,
  };

  assertEq(left, right);
});

test("unbounded-1", () => {
  const left = maximize(
```

```

    [2, 1],
    [
      [1, -1],
      [2, 0],
    ],
    [10, 40],
    PRECISION,
  );
  const right: SimplexResult = { ok: false, error: "unbounded" };

  assertEq(left, right);
});

test("unbounded-2", () => {
  const left = maximize(
    [3, 2],
    [
      [1, -1],
      [-2, 1],
    ],
    [2, -1],
    PRECISION,
  );
  const right: SimplexResult = { ok: false, error: "unbounded" };

  assertEq(left, right);
});

function assertEq(left: SimplexResult, right: SimplexResult): void | never {
  expect(left.ok).toBe(right.ok);

  // HACK: this allows TypeScript to validate types.
  if (!left.ok || !right.ok) {
    if (!left.ok && !right.ok) {
      return expect(left.error).toBe(right.error);
    }
    return;
  }

  expect(left.max).toBeCloseTo(right.max, PRECISION);
  left.x.forEach((_, i) =>
    expect(left.x[i]).toBeCloseTo(right.x[i], PRECISION),
  );
}

```