Report 2

Team information (B23-ISE-02):

- Team member 1 (leader): Kirill Efimovich (k.efimovich@innopolis.university), grade 5/5
- Team member 2: Arsen Galiev (a.galiev@innopolis.university), grade: 5/5
- Team member 3: Asqar Arslanov (a.arslanov@innopolis.university), grade: 5/5
- Team member 4: Ilya-Linh Nguen (i.nguen@innopolis.university), grade: 5/5

Link to the product:

• https://github.com/quintet-sdr/optimization-pt2

Programming language:

- Rust
- To launch the code: \$\\$ cargo run

Linear programming problem:

- Maximization
- Approximation accuracy $\epsilon = 2$
- $\alpha_1 = 0.5$
- $\alpha_2 = 0.9$

Tests:

You may find and edit the tests inside tests.json.

In all the default tests, the results for $\alpha = 0.5$ and $\alpha = 0.5$ are the same.

(1) **Input:**

- Name: Lab 6 / Problem 1
- Objective function: $F(x_1, x_2) = x_1 + x_2$
- Constraints: $\begin{cases} 2x_1 + 4x_2 \le 16 \\ x_1 + 3x_2 \ge 9 \\ x_1, x_2 \ge 0 \end{cases}$
- Initial point: $\begin{bmatrix} 0.5 & 3.5 & 1 & 2 \end{bmatrix}$.

Output:

- Decision variables: $\begin{bmatrix} 6 & 1 & 0 & 0 \end{bmatrix}$.
- Maximum values: 7.

(2) **Input:**

- Name: Lab 6 / Problem 2
- Objective function: $F(x_1, x_2, x_3) = 9x_1 + 10x_2 + 16x_3$
- Constraints: $\begin{cases} 18x_1 + 15x_2 + 12x_3 \le 360 \\ 6x_1 + 4x_2 + 8x_3 \le 192 \\ 5x_1 + 3x_2 + 3x_3 \le 180 \\ x_1, x_2, x_3 \ge 0 \end{cases}$
- Initial point: $\begin{bmatrix} 1 & 1 & 1 & 315 & 174 & 169 \end{bmatrix}$.

Output:

- Decision variables: $\begin{bmatrix} 0 & 8 & 20 & 0 & 0 & 96 \end{bmatrix}$.
- Maximum value: 400.

(3) **Input:**

- Name: Lec 6 / Problem 1
- Objective function: $F(x_1, x_2, x_3) = x_1 + 2x_2$
- Constraints: $\begin{cases} x_1 + x_2 + x_3 = 8 \\ x_1, x_2, x_3 \ge 0 \end{cases}$
- Initial point: [2 2 4].

Output:

- Decision variables: $\begin{bmatrix} 0 & 8 & 0 \end{bmatrix}$.
- Maximum value: 16.

(4) **Input:**

• Name: Tut 6 / Problem 1

• Objective function: $F(x_1, x_2) = 2x_1 + 5x_2 + 7x_3$

• Constraints: $\begin{cases} 1x_1 + 2x_2 + 3x_3 = 6 \\ x_1, x_2, x_3 \ge 0 \end{cases}$

• Initial point: [1 1 1].

Output:

• Decision variables: $\begin{bmatrix} 0 & 3 & 0 \end{bmatrix}$.

• Maximum value: 15.

(5) **Input:**

• Name: No Solution 1

• Objective function: $F(x_1, x_2) = 3x_1 + 2x_2$

• Constraints: $\begin{cases} x_1 - x_2 \le 2 \\ -2x_1 + x_2 \le -1 \\ x_1, x_2 \ge 0 \end{cases}$

• Initial point: [1 1].

Output:

• The problem doesn't have a solution.

(6) **Input:**

• Name: No Solution 2

• Objective function: $F(x_1, x_2) = 2x_1 + 1x_2$

• Constraints: $\begin{cases} x_1 - x_2 \le 10 \\ -2x_1 \le 40 \\ x_1, x_2 \ge 0 \end{cases}$

• Initial point: $\begin{bmatrix} 0 & 0 \end{bmatrix}$.

Output:

• The problem doesn't have a solution.

Code:

```
crates/pt2-cli/src/main.rs
 use std::panic;
 use color_eyre::Result;
 mod cli;
 mod config;
 fn main() -> Result<()> {
     color_eyre::install()?;
     cli::enter_alternate_screen()?;
     panic::set_hook(Box::new(|_| {
         cli::enter_alternate_screen().unwrap();
         cli::leave_alternate_screen().unwrap();
     }));
     let result = cli::run();
     cli::leave_alternate_screen()?;
     result
 }
```

crates/pt2-cli/src/cli.rs

```
use std::io;
use color_eyre::{eyre::Context, Result};
use crossterm::terminal::{EnterAlternateScreen, LeaveAlternateScreen};
use crate::config::{self, Test};
pub fn run() -> Result<()> {
    let tests = config::read_tests().wrap_err("tests.json not found")?;
    while matches!(prompt(tests.clone())?, Next::Continue) {}
    Ok(())
enum Next {
   Continue,
    Break,
}
fn prompt(tests: Vec<Test>) -> Result<Next> {
   for _ in 0..crossterm::terminal::size()?.1 {
        println!();
   let Some(test) = inquire::Select::new("Select a test:", tests)
        .with_vim_mode(true)
        .prompt_skippable()?
    else {
        return Ok(Next::Break);
   };
   let Some(alpha) = inquire::Select::new("Select alpha:", vec![0.5, 0.9])
        .with_vim_mode(true)
        .prompt_skippable()?
    else {
        return Ok(Next::Break);
    };
   let Ok((lpp, iterations)) = pt2_core::interior_point(
        test.objective_function.clone(),
        &test.constraints,
        test.initial_point.clone(),
        test.eps,
        alpha,
    ) else {
        println!("The method is not applicable.");
        return Ok(Next::Continue);
   };
    println!("Epsilon: {} ({:.eps$})", test.eps, lpp.eps, eps = test.eps);
   println!(
        "Objective function: {:.eps$?}",
        lpp.c.iter().collect::<Box<[_]>>(),
        eps = test.eps,
    );
    println!(
        "Initial point: {:.eps$?}",
        lpp.x.iter().collect::<Box<[_]>>(),
        eps = test.eps,
    );
```

```
println!("Constraints:{:.eps$}", lpp.big_a, eps = test.eps);
    let last = iterations.last().unwrap();
    let Ok(result) = last else {
        println!("The problem doesn't have a solution.");
        return Ok(Next::Continue);
    };
    println!("Result:");
    println!("Maximum: {:.eps$}", result.max, eps = test.eps);
        "Decision variables: {:.eps$?}",
        result.decision_variables.iter().collect::<Box<[_]>>(),
        eps = test.eps
    );
    let Some(next) = inquire::Confirm::new("Next test?").prompt_skippable()? else {
        return Ok(Next::Break);
    };
    if !next {
        return Ok(Next::Break);
    };
    Ok(Next::Continue)
}
pub fn enter_alternate_screen() -> io::Result<()> {
    crossterm::execute!(io::stdout(), EnterAlternateScreen)
}
pub fn leave_alternate_screen() -> io::Result<()> {
    crossterm::execute!(io::stdout(), LeaveAlternateScreen)
```

crates/pt2-cli/src/config.rs

```
use std::fmt::{self, Display, Formatter};
use std::fs::File;
use std::io::BufReader;
use color_eyre::Result;
use serde::Deserialize;
use pt2_core::Constraints;
#[derive(Clone, Deserialize)]
#[serde(rename_all = "kebab-case")]
pub struct Test {
    #[serde(default = "name_default")]
    pub name: Box<str>,
    pub objective_function: Vec<f64>,
    pub constraints: Constraints,
    pub initial_point: Vec<f64>,
    #[serde(alias = "epsilon", default = "eps_default")]
    pub eps: usize,
}
impl Display for Test {
    fn fmt(&self, f: &mut Formatter<'_>) -> fmt::Result {
        write!(f, "{}", self.name)
    }
}
pub fn read_tests() -> Result<Vec<Test>>> {
    let tests_file = BufReader::new(File::open("tests.json")?);
    Ok(serde_json::from_reader(tests_file)?)
fn name_default() -> Box<str>> {
    Box::from("Unnamed")
const fn eps_default() -> usize {
}
```

crates/pt2-core/src/lib.rs

```
use lpp::Lpp;
pub use interfaces::{Constraints, Sign};
use interfaces::{InteriorPoint, NotApplicableError};
mod algorithm;
mod interfaces;
mod lpp;
pub fn interior_point(
    objective_function: Vec<f64>,
    constraints: &Constraints,
    initial_point: Vec<f64>,
    eps: usize,
    alpha: f64,
) -> Result<(Lpp, InteriorPoint), NotApplicableError> {
    let lpp = Lpp::try_new(objective_function, constraints, initial_point, eps)?;
    Ok((
        lpp.clone(),
        InteriorPoint {
            done: false,
            x: lpp.x,
            big_a: lpp.big_a,
            c: lpp.c,
            eps: lpp.eps,
            alpha,
       },
    ))
}
```

crates/pt2-core/src/algorithm.rs

```
use na::{DMatrix, DVector};
use crate::interfaces::{Auxiliary, InteriorPoint, Iteration, NoSolutionError};
impl Iterator for InteriorPoint {
    type Item = Result<Iteration, NoSolutionError>;
    fn next(&mut self) -> Option<Self::Item> {
        if self.done {
            return None;
        let size = self.x.len();
        let big_d = DMatrix::from_diagonal(&self.x);
        let big_a_tilde = &self.big_a * &big_d;
        let c_tilde = &big_d * &self.c;
        let big_p = {
            let big_i = DMatrix::identity(size, size);
            let big_a_tilde_tr = big_a_tilde.transpose();
            let Some(inverse) = (&big_a_tilde * &big_a_tilde_tr).try_inverse() else {
                self.done = true;
                return Some(Err(NoSolutionError));
            };
            big_i - big_a_tilde_tr * inverse * &big_a_tilde
        };
        let c_p = &big_p * &c_tilde;
        let Some(nu) = c_p
            .iter()
            .filter_map(|it| (it < &0.).then_some(it.abs()))</pre>
            .max_by(|a, b| a.partial_cmp(b).unwrap())
        else {
            self.done = true;
            return Some(Err(NoSolutionError));
        };
        let x_tilde = DVector::from_element(size, 1.) + (self.alpha / nu) * &c_p;
        let new_x = &big_d * &x_tilde;
        if (&new_x - &self.x).norm() < self.eps {</pre>
            self.done = true;
        self.x = new_x;
        Some(Ok(Iteration {
            auxiliary: Auxiliary {
                big_d,
                big_a_tilde,
                c_tilde,
                big_p,
                c_p,
                nu,
                x_tilde,
            },
            decision_variables: self.x.clone_owned(),
            max: self.x.dot(&self.c),
        }))
```

}

crates/pt2-core/src/interfaces.rs

```
use na::{DMatrix, DVector};
use serde::Deserialize;
use thiserror::Error;
#[derive(Error, Debug)]
#[error("method is not applicable")]
pub struct NotApplicableError;
#[derive(Error, Debug)]
#[error("problem has no solution")]
pub struct NoSolutionError;
pub struct Auxiliary {
   pub big_d: DMatrix<f64>,
   pub big_a_tilde: DMatrix<f64>,
   pub c_tilde: DVector<f64>,
   pub big_p: DMatrix<f64>,
   pub c_p: DVector<f64>,
   pub nu: f64,
   pub x_tilde: DVector<f64>,
pub struct Iteration {
    pub auxiliary: Auxiliary,
   pub decision_variables: DVector<f64>,
   pub max: f64,
pub struct InteriorPoint {
   pub(crate) done: bool,
   pub(crate) x: DVector<f64>,
   pub(crate) big_a: DMatrix<f64>,
   pub(crate) c: DVector<f64>,
   pub(crate) eps: f64,
   pub(crate) alpha: f64,
}
pub type Constraints = Box<[(Box<[f64]>, Sign, f64)]>;
#[derive(Clone, Deserialize)]
pub enum Sign {
    #[serde(rename = "<=")]</pre>
    #[serde(rename = "==", alias = "=")]
    #[serde(rename = ">=")]
    Ge,
}
impl Sign {
   pub fn compare<Lhs, Rhs>(&self, a: &Lhs, b: &Rhs) -> bool
    where
       Lhs: PartialOrd<Rhs>,
        let cmp_function = match self {
            Self::Le => PartialOrd::le,
            Self::Eq => PartialEq::eq,
            Self::Ge => PartialOrd::ge,
        };
```

```
cmp_function(a, b)
}
```

```
use na::{DMatrix, DVector};
use crate::{interfaces::NotApplicableError, Constraints, Sign};
#[derive(Clone)]
pub struct Lpp {
    pub x: DVector<f64>,
    pub big_a: DMatrix<f64>,
   pub c: DVector<f64>,
   pub eps: f64,
impl Lpp {
   pub fn try_new(
        objective_function: Vec<f64>,
        constraints: &Constraints,
        initial_point: Vec<f64>,
        eps: usize,
    ) -> Result<Self, NotApplicableError> {
        let (n, m) = get_n_and_m(constraints).ok_or(NotApplicableError)?;
        if constraints
            .iter()
            .any(|row| row.0.len() != objective_function.len())
        {
            return Err(NotApplicableError);
        }
        let initial_point_is_feasible = constraints.iter().all(|(coefficients, sign, rhs)| {
            let constraint_sum: f64 = coefficients
                .iter()
                .zip(&initial_point)
                .map(|(coeff, x)| coeff * x)
                .sum();
            sign.compare(&constraint_sum, rhs)
        });
        if !initial_point_is_feasible {
            return Err(NotApplicableError);
        let no_slack_rows = constraints
            .iter()
            .enumerate()
            .filter_map(|(i, (_, sign, _))| matches!(sign, Sign::Eq).then_some(i));
        let no_slack_cols = no_slack_rows.map(|j| m + j).collect::<Box<[_]>>();
        let slack_cols_count = n - no_slack_cols.len();
        if initial_point.len() != m + slack_cols_count {
            return Err(NotApplicableError);
        }
        let x = DVector::from_vec(initial_point);
        let big_a = {
            let left_part_row_elements = constraints
                .flat_map(|(coefficients, _, _)| coefficients)
                .copied();
```

crates/pt2-core/src/lpp.rs

```
let right_part_diagonal_elements = &DVector::from_vec(
                constraints
                    .iter()
                    .map(|(_, sign, _)| match sign {
                        Sign::Le => 1.,
                        Sign::Eq => 0.,
                        Sign::Ge => -1.,
                    })
                    .collect(),
            );
            let mut big_a = DMatrix::from_row_iterator(n, m, left_part_row_elements)
                .resize_horizontally(m + n, 0.);
            big_a
                .view_mut((0, m), (n, n))
                .set_diagonal(right_part_diagonal_elements);
            big_a.remove_columns_at(&no_slack_cols)
        };
        let c = DVector::from_vec(objective_function).resize_vertically(m + slack_cols_count, 0.);
        let eps = up_to_n_dec_places(i32::try_from(eps).map_err(|_| NotApplicableError)?);
        Ok(Self { x, big_a, c, eps })
    }
}
fn get_n_and_m(constraints: &Constraints) -> Option<(usize, usize)> {
    Some((constraints.len(), constraints.first()?.0.len()))
fn up_to_n_dec_places(n: i32) \rightarrow f64 {
    0.1_f64.powi(n) / 2.
```