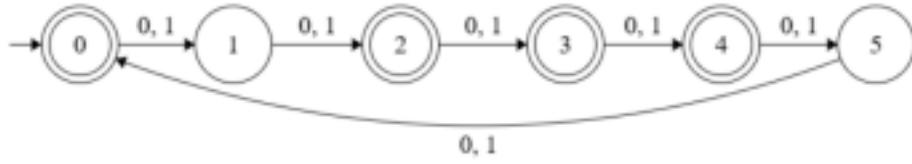


BRAC UNIVERSITY
CSE331 : Automata and Computability
Assignment 1

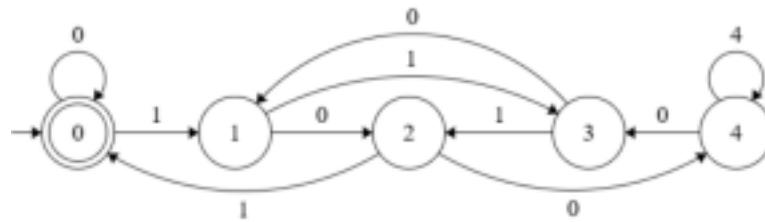
- 1. Draw the state diagram of a DFA for the following regular languages:** A. $L(M) \rightarrow \{w \in \Sigma^* \mid \text{the length of } w \text{ is a multiple of 2 or 3}\}$, where $\Sigma = \{0, 1\}$. (use 6 states)



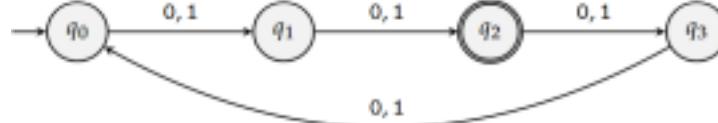
B.

$L(M) \rightarrow \{w \in \Sigma^* \mid \text{the sum of the symbols of } w \text{ is a multiple of 3}\}$, where $\Sigma = \{0, 1, 2\}$.
 See example 1.13 from the book.

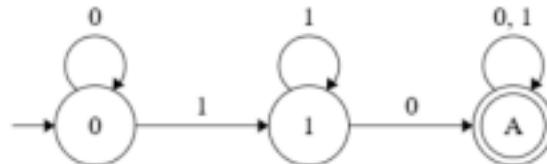
C. $L(M) \rightarrow \{w \in \Sigma^* \mid \text{the decimal equivalent of } w \text{ is a multiple of 5}\}$, where $\Sigma = \{0, 1\}$.



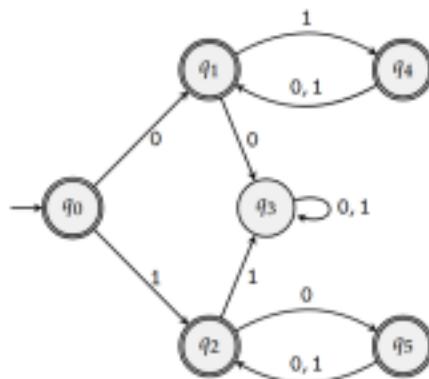
D. $L(M) \rightarrow \{w \in \Sigma^* \mid |w| \% 4 = 2\}$



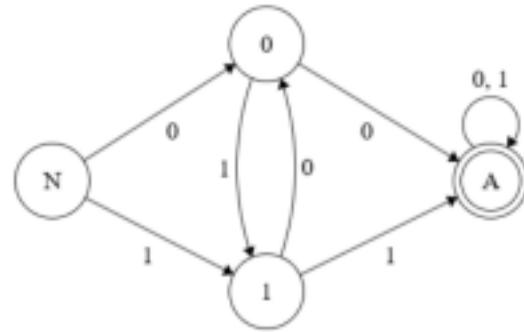
E. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ is any string not in } 0^*1^*\}$, where $\Sigma = \{0, 1\}$.



F. $L(M) \rightarrow \{w \in \Sigma^* \mid \text{Every even position letter in } w \text{ is different from the first letter of } w\}$



$$G. L(M) \rightarrow (L_1 \cap L_2)'$$



2. Write the RE for the following regular languages:

A. $L(M) \rightarrow \{w \in \Sigma^* \mid |w| \% 3 \neq 1\}$

$$(\Sigma\Sigma)^*(\epsilon \mid \Sigma\Sigma)$$

B. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ starts and ends with the same symbol}\}, \text{ where } \Sigma = \{0, 1\}.$

$$0\Sigma^*0 \mid 1\Sigma^*1 \mid 0 \mid 1$$

C. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ contains equal numbers of } 01 \text{ and } 10\}, \text{ where } \Sigma = \{0, 1\}.$

$$0\Sigma^*0 \mid 1\Sigma^*1 \mid 0 \mid 1 \mid \epsilon$$

D. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ contains at most two } 11\}$

$$(0 \mid 10)^*(11 \mid \epsilon)(0 \mid 10)^*(11 \mid \epsilon)(0 \mid 10)^*(1 \mid \epsilon)$$

E. $L(M) \rightarrow \{w \in \Sigma^* \mid w \text{ does not contain } 101\}, \text{ where } \Sigma = \{0, 1\}.$

$$(1|000^*)^* \mid \epsilon \mid \Sigma \mid \Sigma\Sigma$$

F. $L(M) \rightarrow L_1'$

$$(\Sigma\Sigma)^*\Sigma\Sigma0\Sigma^*$$

G. $L(M) \rightarrow L_1 \cap L_2$

$$(001)^*00 \mid \epsilon \mid 0 \mid 00$$