

In the adjacent figure we have the following parameters:

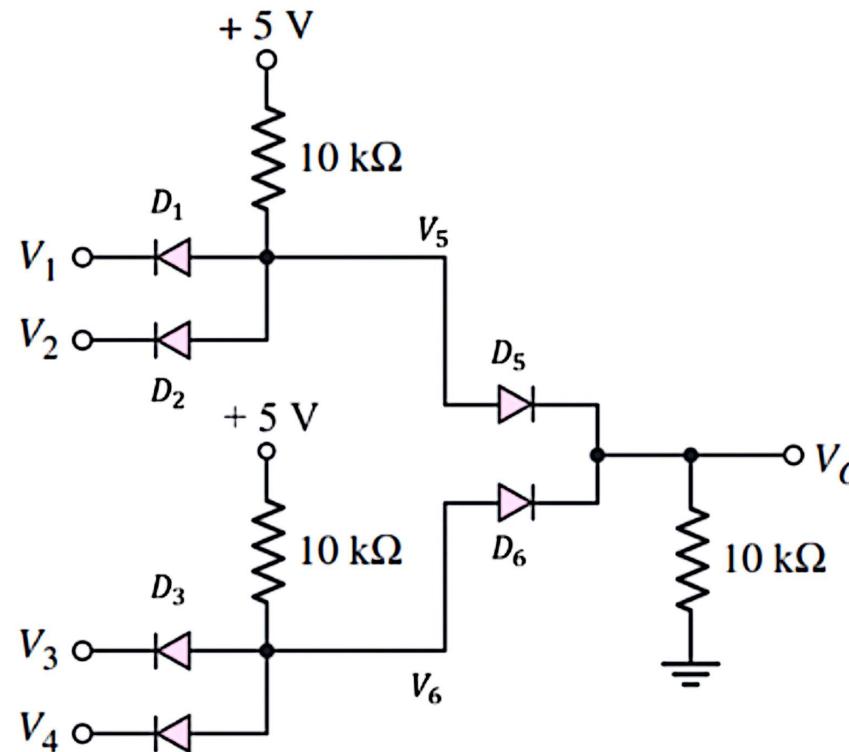
$$V_{D1} = 0.3 \text{ V}, \quad V_1 = 2 \text{ V}$$

$$V_{D2} = 0.5 \text{ V}, \quad V_2 = 1.7 \text{ V}$$

$$V_{D3} = 0.7 \text{ V}, \quad V_3 = 1.5 \text{ V}$$

$$V_{D4} = 0.9 \text{ V}, \quad V_4 = 1.1 \text{ V}$$

$$V_{D5} = V_{D6} = 1.1 \text{ V}$$



- a) Draw the IV characteristics of a diode as per the constant voltage drop + resistance model. Indicate the different operating modes in your graph. [3]
- b) Find V5 and V6. [3]
- c) Find VO. [2]
- d) Solve the circuit to get VO, when V1=7 V , V2 = 8 V and all other voltages remain the same. (Hint: Try to obtain V5 by solving the portion of the circuit with diodes D1 and D2, by method of assumed states.) [1 + 1]

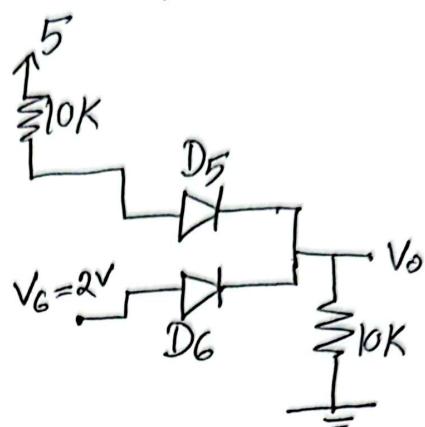
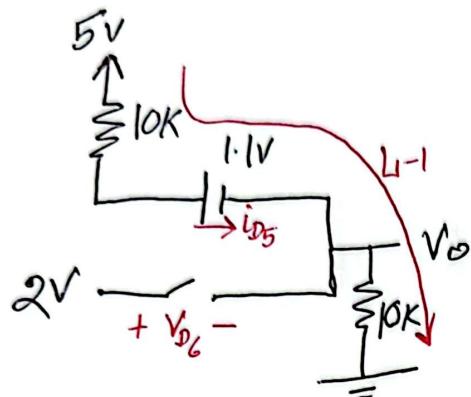
$$i) V_5 = \text{Min}(V_1 + V_{D_1}, V_2 + V_{D_2}) = \text{Min}(2.3, 2.2) = 2.2 \text{ V}$$

$$V_6 = \text{Min}(V_3 + V_{D_3}, V_4 + V_{D_4}) = \text{Min}(2.2, 2) = 2 \text{ V}$$

$$ii) V_o = \text{Max}(V_5 - V_{D_5}, V_6 - V_{D_6}) \\ = \text{Max}(1.1, 0.9) = 1.1 \text{ V}$$

iii) For $V_1 = 7V$ & $V_2 = 8V$, D_1 and D_2 are both in reverse bias as both V_1 & V_2 are greater than the 5V supply voltage.

Assume $D_5 \rightarrow ON$, $D_6 \rightarrow OFF$



∇KVL at $L-1$

$$5 = 10i_{D5} + 1.1 + 10i_{D5}$$

$$i_{D5} = 0.195 > 0$$

$$V_0 = 0.195 \times 10 = 1.95V$$

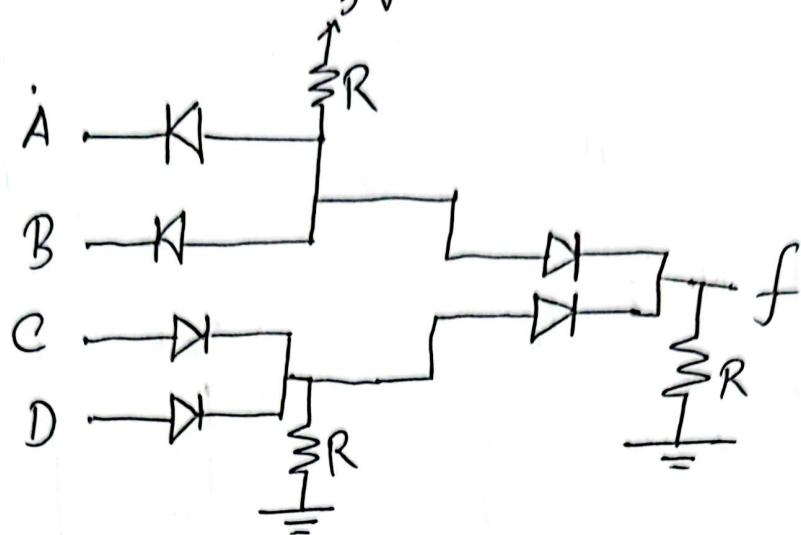
$$V_{D6} = 2 - 1.95 = 0.05 < 1.1V$$

Correct Assumption

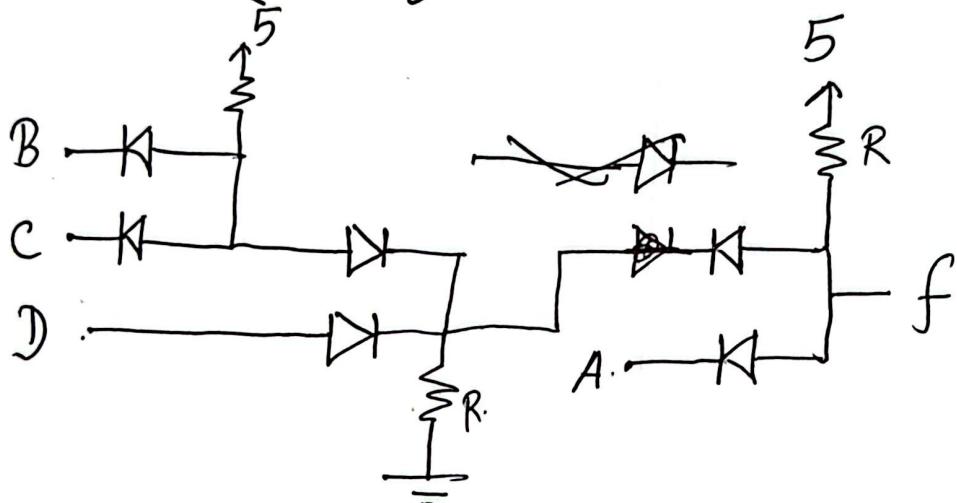
$$V_0 = 1.95V$$

Q-2 Implement the following expressions using Diodes

i) $f = (A \cdot B) + (C + D)$



ii) $f = (B \cdot C + D) \cdot A$



Q-3 Analyze the circuit to calculate

V_x , V_y , I_{D_1} , & I_{D_2} .

Use $V_{D0} = 0.7V$ for both diodes

Assuming D_1 ON & D_2 OFF

KCL at Node V_y

$$i_{D_1} = i_1$$

$$\Rightarrow \frac{15 - 0.7 - V_y}{1} = \frac{V_y - 0}{1}$$

$$\Rightarrow V_y = 7.15$$

$$I_{D_1} = \frac{15 - 0.7 - 7.15}{1}$$

$$= 7.15 \text{ mA} > 0$$

$$V_{D_2} = 0 - V_y = -7.15 < 0.7$$

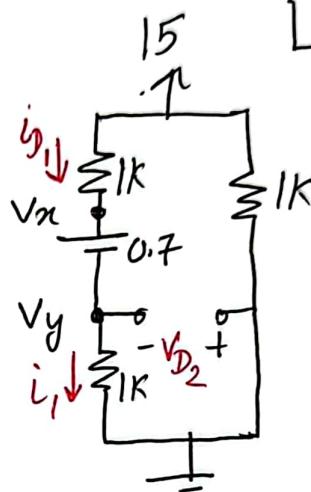
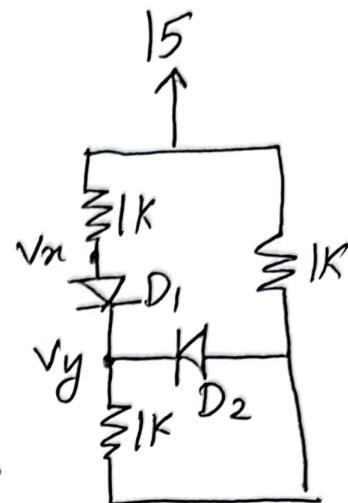
Assumption is correct

$$V_x - V_y = 0.7$$

$$\Rightarrow V_x = 7.85$$

$$I_{D_2} = 0 \text{ mA}$$

$V_x = 7.85 \text{ V}$ $V_y = 7.15 \text{ V}$ $I_{D_1} = 7.15 \text{ mA}$ $I_{D_2} = 0 \text{ mA}$



Q-4

Find the current passing through $100\text{ k}\Omega$ resistor.

$$V_{D_0} = 0.7\text{ V}$$

Assuming D_1 ON, D_2 ON

$$\frac{V_1 - 5}{1.2} + \frac{V_1 - 0}{100} + \frac{V_2 - 5}{1} + \frac{V_2 - 0}{4.7} = 0$$

Format Approach

$$V_1 \left(\frac{1}{1.2} + \frac{1}{100} \right) + V_2 \left(1 + \frac{1}{4.7} \right) - \frac{5}{1.2} - \frac{5}{1} = 0 \quad \dots \textcircled{i}$$

$$V_1 - V_2 = 1.4 \quad \dots \textcircled{ii}$$

$$V_1 = 5.28$$

$$V_2 = 3.88$$

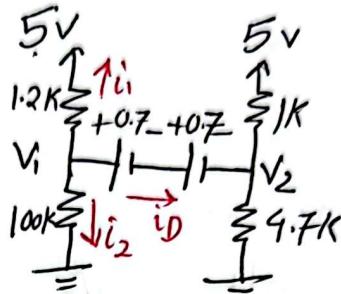
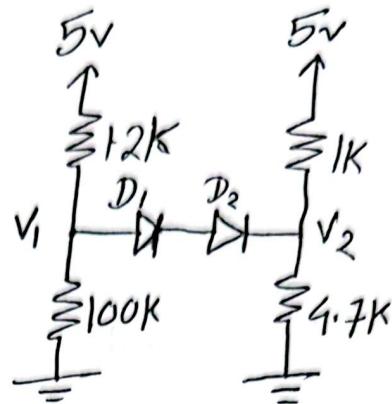
KCL at V_1

$$i_1 + i_2 + i_D = 0$$

$$i_D = -i_1 - i_2 = \frac{V_1 - 5}{1.2}$$

$$= -0.233 - 0.052$$

$$= -0.285 < 0$$



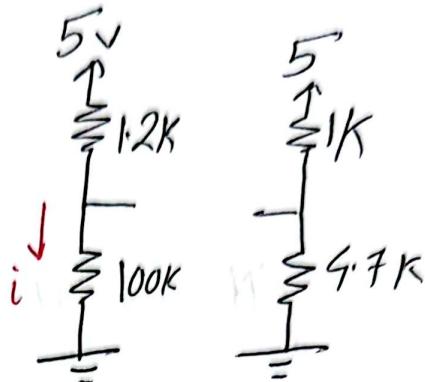
$$i_1 = \frac{5.28 - 5}{1.2} = 0.233\text{ mA}$$

$$i_2 = \frac{5.28}{100} = 0.052\text{ mA}$$

Assumption is wrong

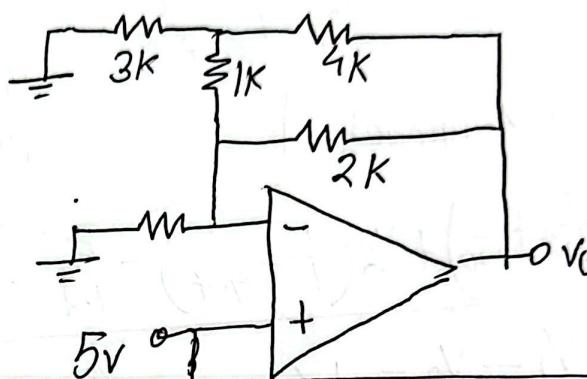
Assuming D_1 & $D_2 \rightarrow \text{Off}$

$$I = \frac{5}{1.2 + 100} \\ = 0.049 \text{ mA}$$



(Q5)

Determine the Output voltage V_o .



KCL at V_L

$$\frac{5-0}{2} + \frac{5-V_o}{2} + \frac{5-V_1}{1} = 0 \\ \Rightarrow 5 + 5 - V_o + 10 - 2V_1 = 0$$

$$\Rightarrow V_o + 2V_1 = 20 \dots \text{(i)}$$

KCL at V_1

$$\frac{V_1}{3} + \frac{V_1 - V_o}{4} + \frac{V_1 - 5}{1} = 0$$

$$\Rightarrow 4V_1 + 3V_1 - 3V_o + 12V_1 - 60 = 0$$

$$\Rightarrow -3V_o + 19V_1 = 60 \dots \text{(ii)}$$

Solving eqn (i) & (ii)

$V_o = 10.4 \text{ V}$

