

Department of Computer Science and Engineering (CSE)  
BRAC University

## Practice Problem Set 5

CSE251 - Electronic Devices and Circuits

### MOSFET CIRCUITS

S-Model, SR-Model, Real MOSFET Model, Logic Function Implementation, Method of Assumed States, and Multistage Circuits

[Course Description, COs,  
and Policies](#)



[Midterm and Final  
Questions](#)

# Problem 1

- Give a switch-MOSFET implementation of the following logic functions.  $A, B, C, D, E$ , and  $F$  are Boolean inputs.

$$I. \quad f = A \cdot B \cdot C + D \cdot E$$

$$II. \quad f = \overline{A \cdot B} \cdot (C + D)$$

$$III. \quad f = A \cdot B + \bar{A} \cdot \bar{B}$$

$$IV. \quad f = \overline{A \cdot C} + \overline{B + C}$$

$$V. \quad f = (A \cdot B + C) \cdot D$$

$$VI. \quad f = A \cdot B + C \cdot D$$

$$VII. \quad f = A \cdot B \cdot C + D$$

$$VIII. \quad f = (A + B) \cdot (C + D)$$

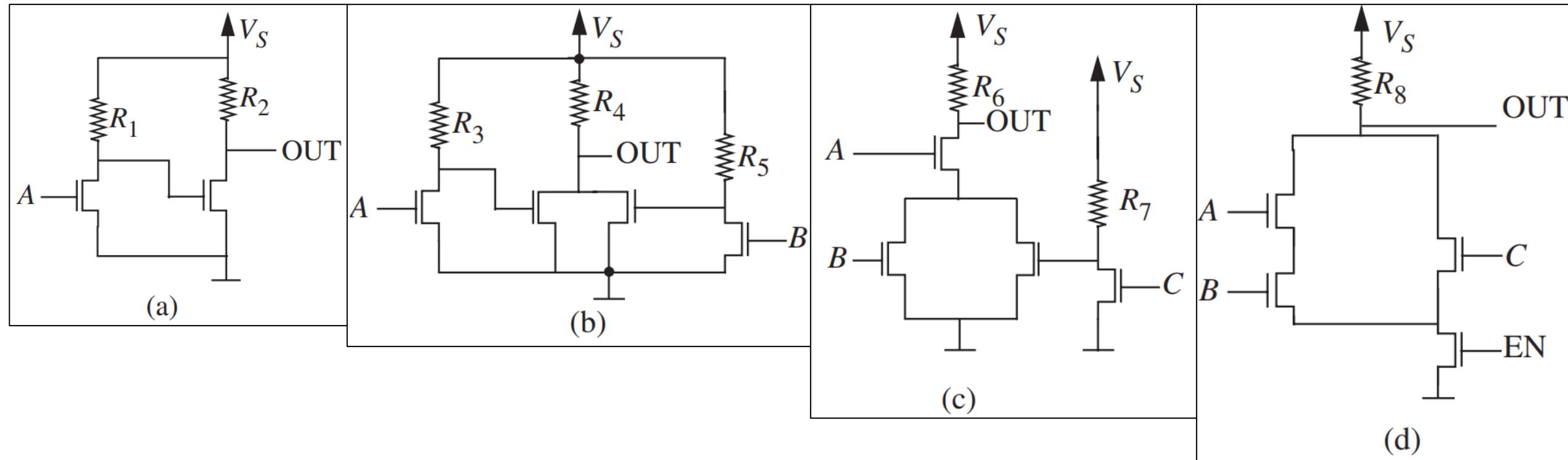
$$IX. \quad f = (A \cdot B + C) \cdot D \cdot (E + F)$$

$$X. \quad f = A \oplus B$$

$$XI. \quad f = \overline{C \cdot (A + B)} \cdot (A + \bar{B} + C)$$

# Problem 2

- Write a Boolean expression that describes the function of each of the circuits below.

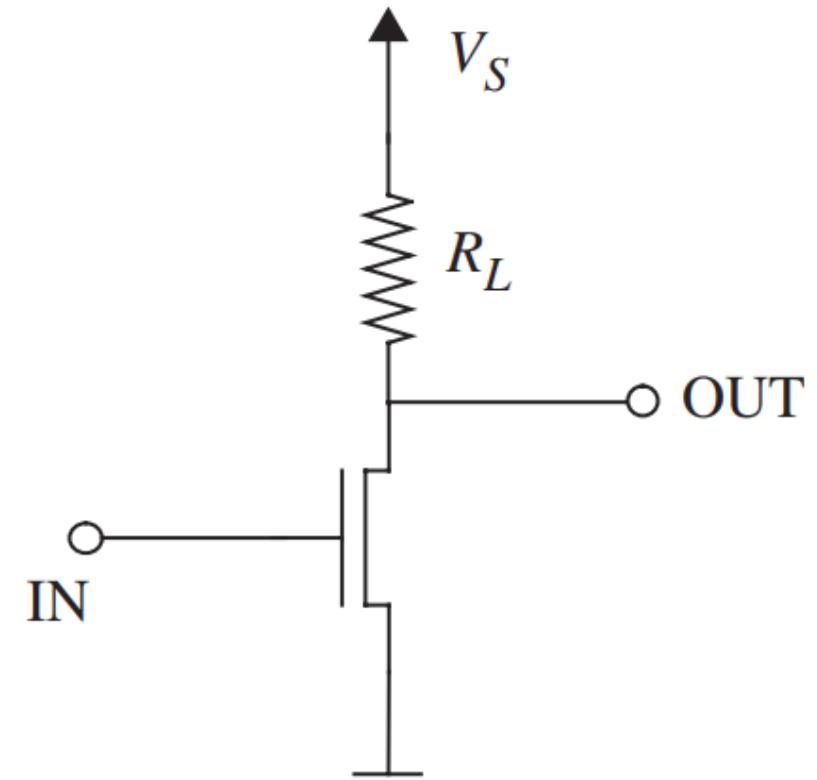


# Problem 3

- Draw voltage transfer characteristics (VTC) for the following logic gates implemented using MOSFETs. Use *S* – Model.
  - I. Inverter
  - II. 2-input NAND Gate
  - III. 2-input NOR Gate
  - IV. 3-input AND Gate or  $f = A \cdot B \cdot C$
  - V. 3-input OR Gate or  $f = A + B + C$

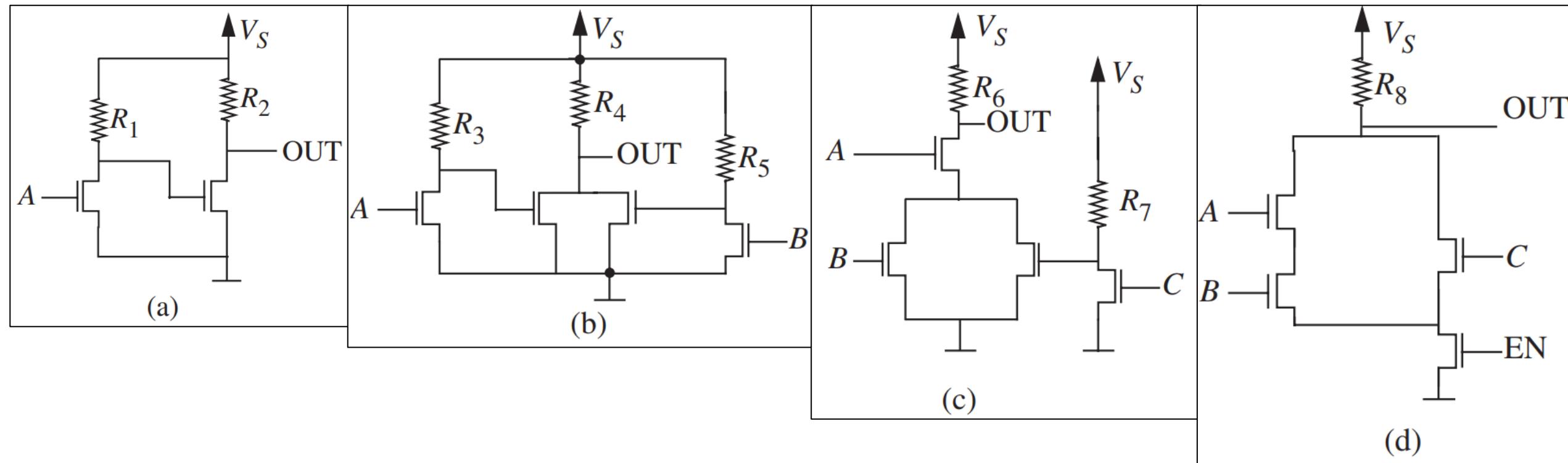
# Problem 4

- The MOSFET in the following inverter circuit has a threshold voltage  $V_{Tn} = 2 V$  and  $R_{ON} = 8 k\Omega$ . For the circuit,  $V_S = 5 V$ . Draw the  $OUT$  vs.  $IN$  (VTC) graph by modeling the MOSFETs using
  - $S$  –Model and
  - $SR$  –Model with  $R_L = 10 k\Omega$ .
  - $SR$  –Model with  $R_L = 40 k\Omega$ .



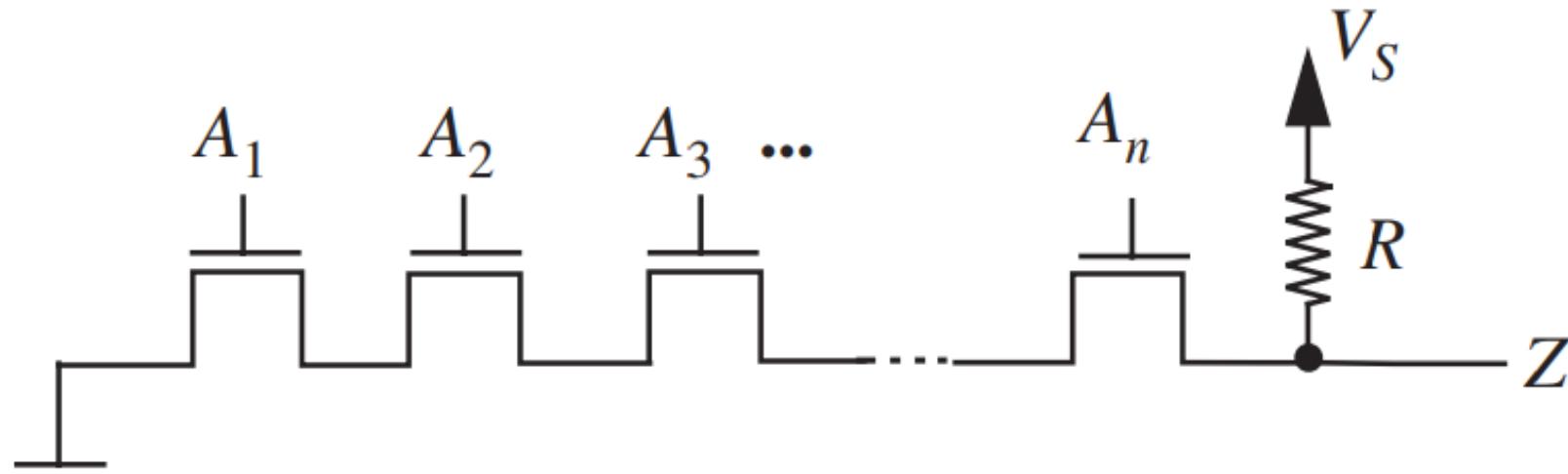
# Problem 5

- The static discipline of an electronic system is such that, an input or output will be considered "low" if it remains below 0.5 V. Determine minimum values for the resistors  $R_1$  through  $R_8$  in terms of  $R_{ON}$ , so that each circuit satisfies the static discipline of the system. Here,  $V_S = 5 \text{ V}$ .



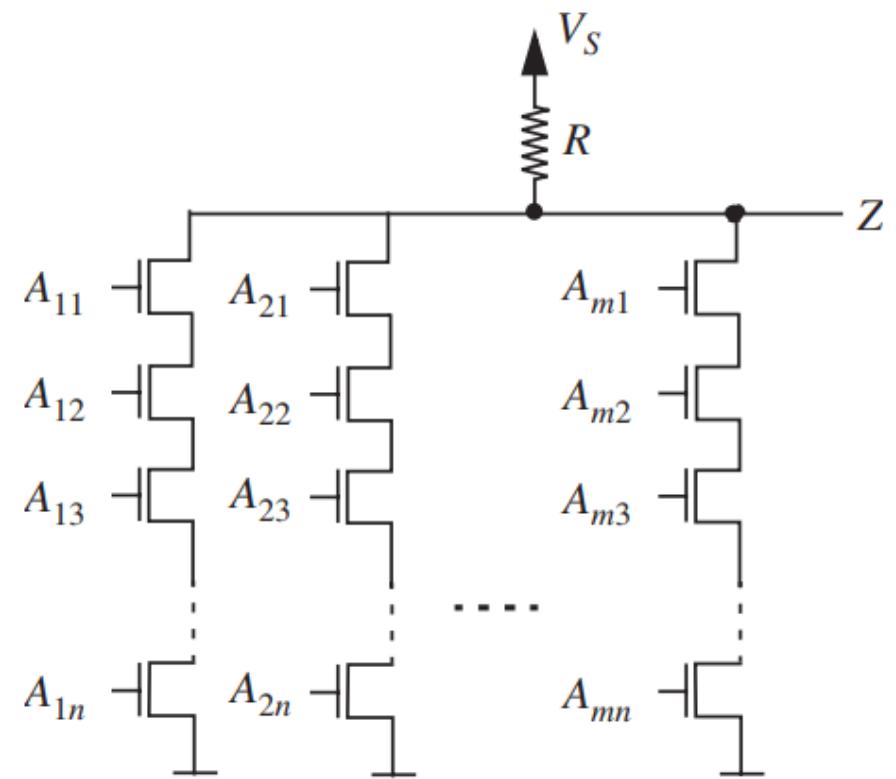
# Problem 6

- The static discipline of an electronic system is such that, an input or output will be considered "low" if it remains below 0.5 V. Consider the  $N$ -input NAND gate circuit shown below. In the design,  $V_S = 5$  V,  $R = 100 \text{ k}\Omega$ , and  $R_{ON} = 2 \text{ k}\Omega$ . Determine the maximum value of  $N$ , that is, the maximum number of MOSFETs that can be connected so that the circuit satisfies the static discipline.



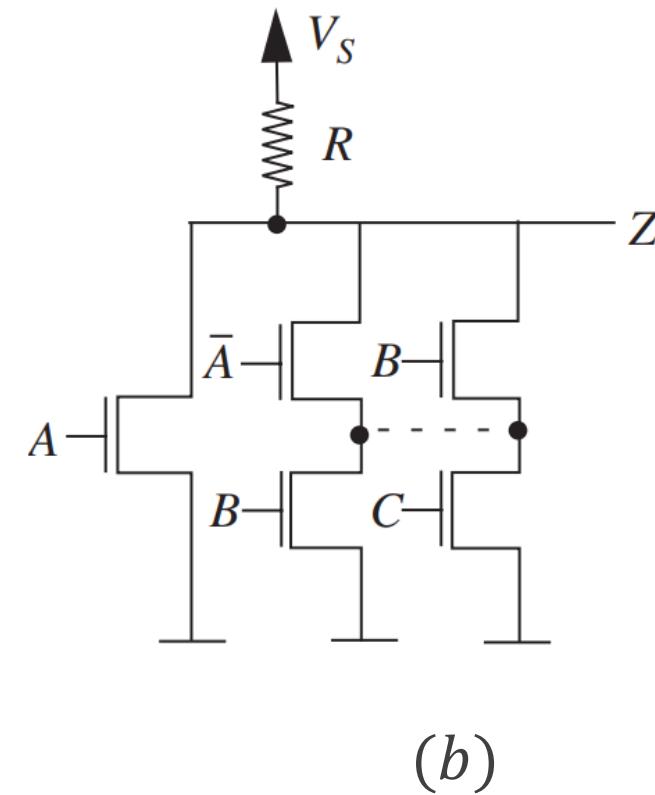
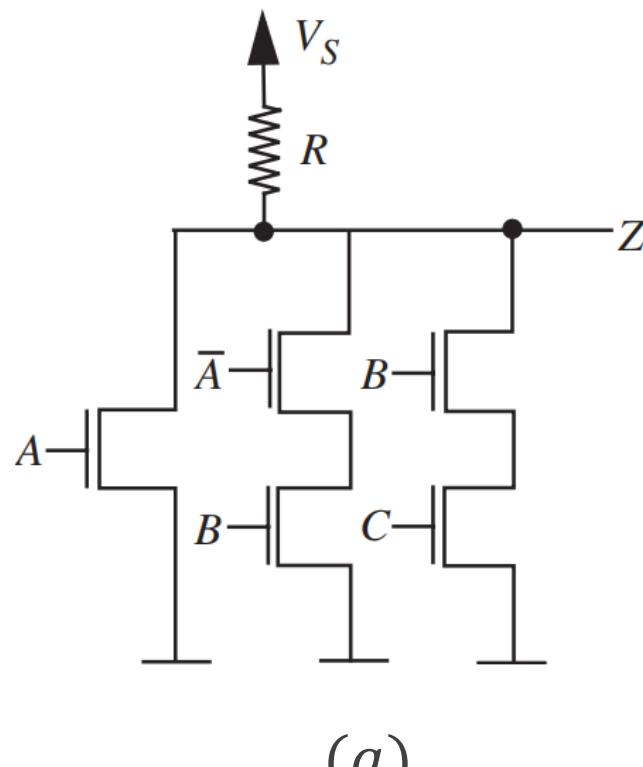
# Problem 7

- The static discipline of an electronic system is such that, an input or output will be considered "low" if it remains below 0.5 V. Consider the following logic circuit where,  $V_S = 5$  V and  $R_{ON} = 1 \text{ k}\Omega$ . Design the circuit so that the circuit satisfies the static discipline for  $m = 10$  and  $n = 25$ .



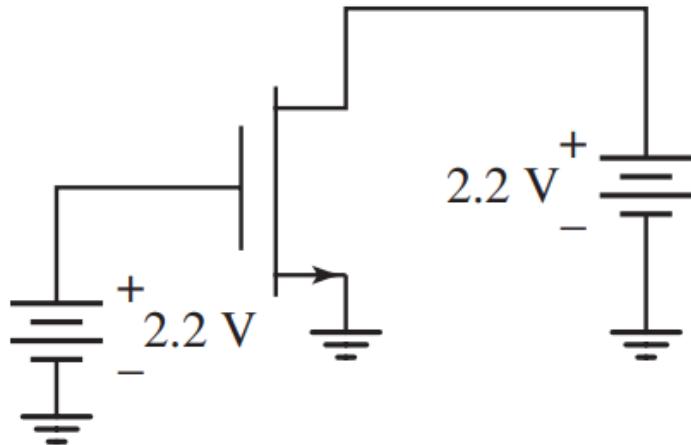
# Problem 8

- Write a Boolean expression that describes the function of the circuit in figure (a). What will be the expression if a manufacturing error results in a short circuit as indicated by the dashed line in (b).

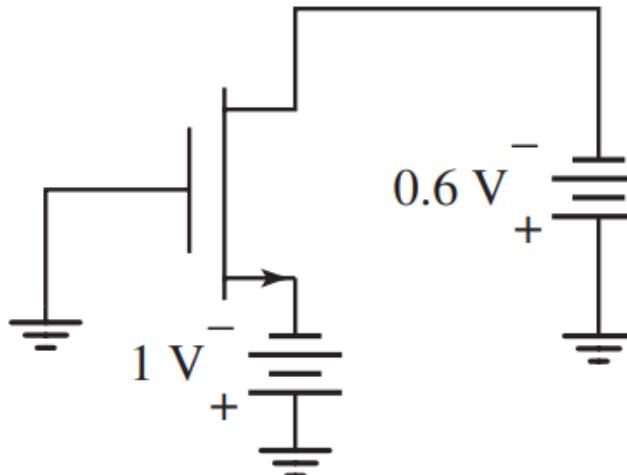


# Problem 9

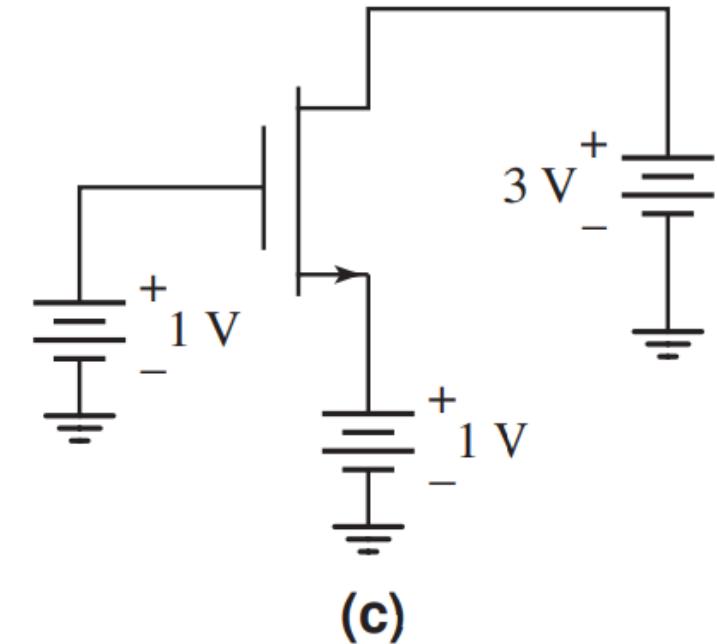
- The threshold voltage for each of the NMOS transistors in the following circuits is  $V_{Tn} = 0.4 V$ . Determine the operating region of the transistor in each circuit.



(a)



(b)



(c)

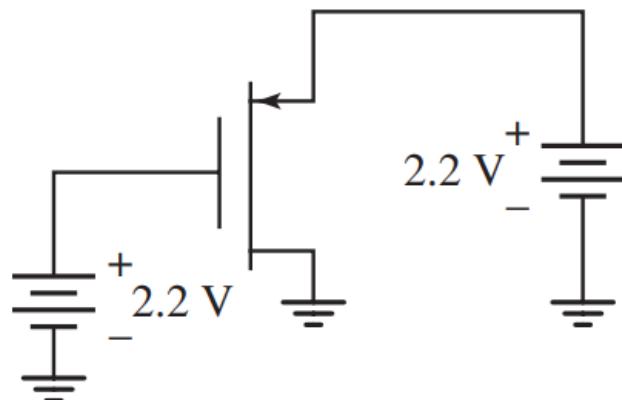
**Ans: Saturation**

**Ans: Triode**

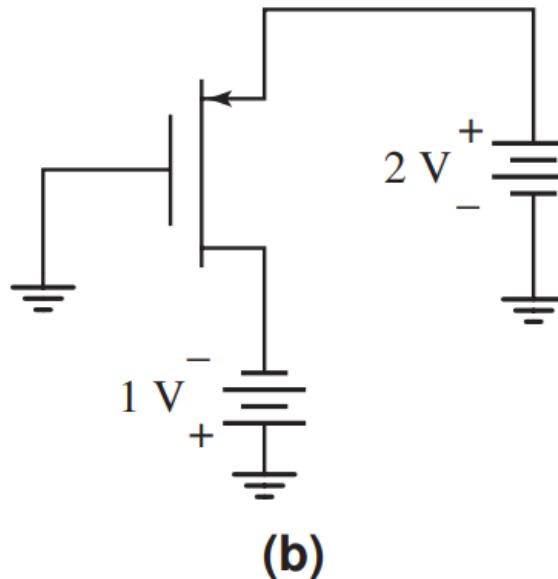
**Ans: Saturation**

# Problem 10

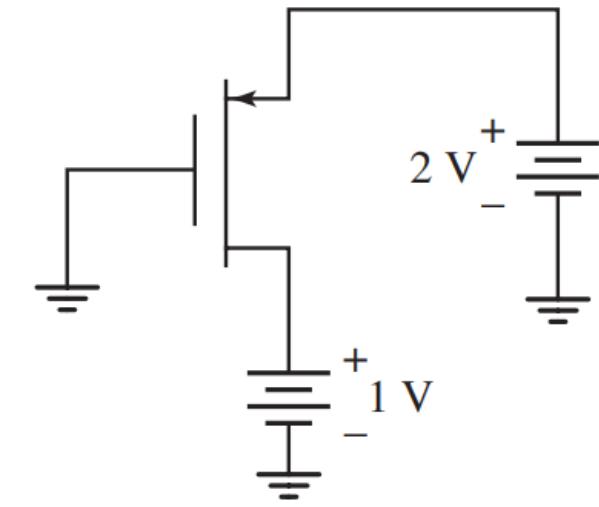
- The threshold voltage for each of the PMOS transistors in the following circuits is  $V_{Tp} = -0.4 \text{ V}$ . Determine the operating region of the transistor in each circuit.



(a)



(b)



(c)

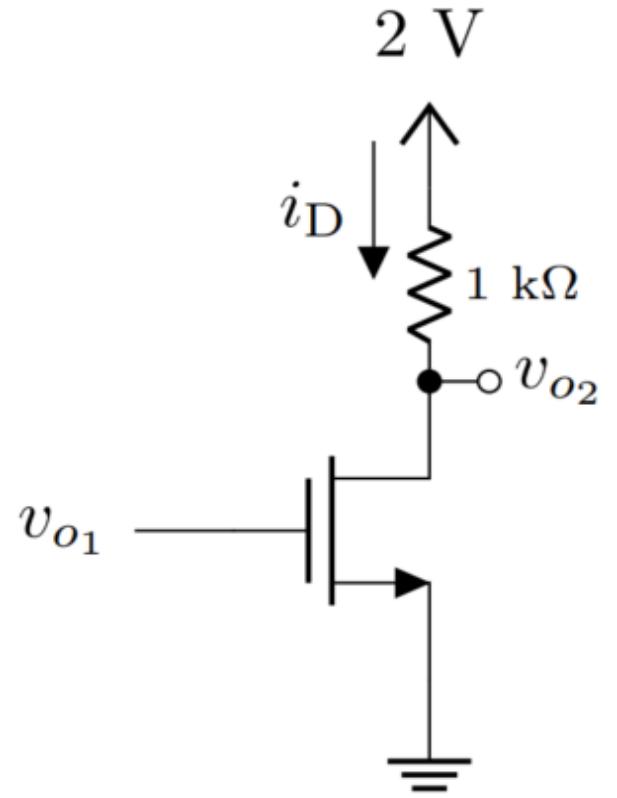
Ans: **Saturation**

Ans: **Saturation**

Ans: **Triode**

# Problem 11

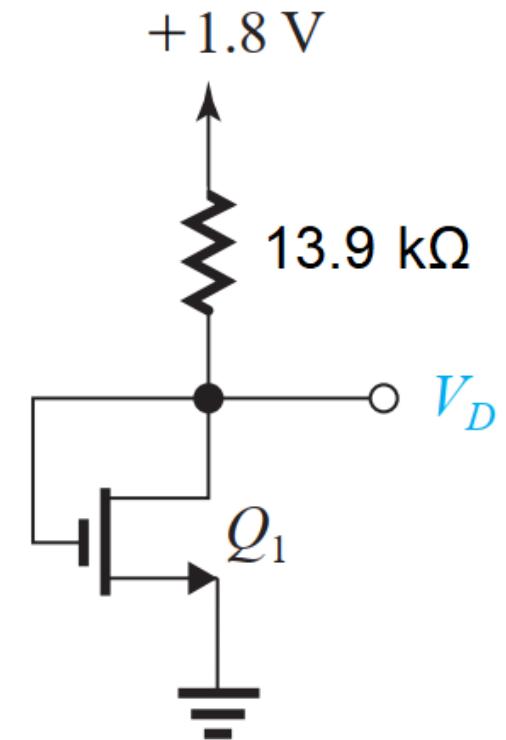
- The transistor in the following circuit has parameters  $V_{Tn} = 0.2 \text{ V}$  and  $k_n = k'_n \frac{W}{L} = 4 \text{ mA/V}^2$ . If  $v_{o_1} = 2 \text{ V}$ , determine  $i_D$  and  $v_{o_2}$ .



**Ans:**  $v_{o_2} = 0.26 \text{ V}$ ;  $i_D = 1.74 \text{ mA}$

# Problem 12

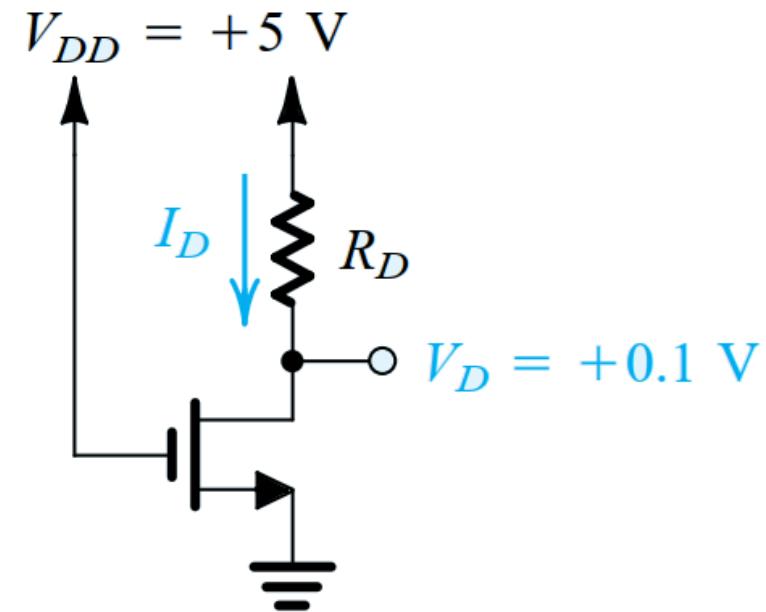
- The transistor in the following circuit has parameters  $V_{Tn} = 0.5 \text{ V}$  and  $k_n = k'_n \frac{W}{L} = 1.6 \text{ mA/V}^2$ . Determine  $V_D$ .



Ans:  $V_D = 0.79 \text{ V}$

# Problem 13

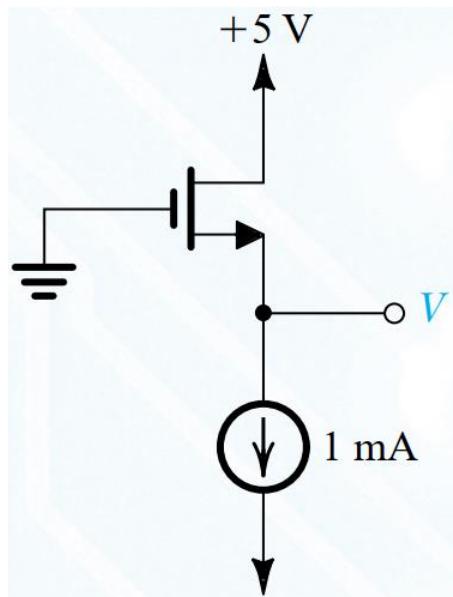
- Design the circuit, that is, determine the values of  $R_D$ , so that the transistor operates at  $V_D = 0.1 V$ . The NMOS transistor has  $V_{Tn} = 1 V$  and  $k_n = k'_n \frac{W}{L} = 1 \text{ mA/V}^2$ .



Ans:  $I_D = 0.395 \text{ mA}$ ;  $R_D = 12.4 \text{ k}\Omega$

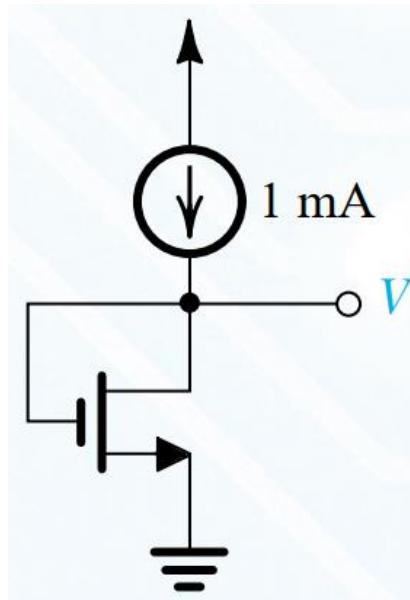
# Problem 14

- The transistors in the following circuits has  $V_{Tn} = 0.8 V$  and  $k_n = k'_n \frac{W}{L} = 0.5 \text{ mA/V}^2$ . Determine  $V$  in each circuit.



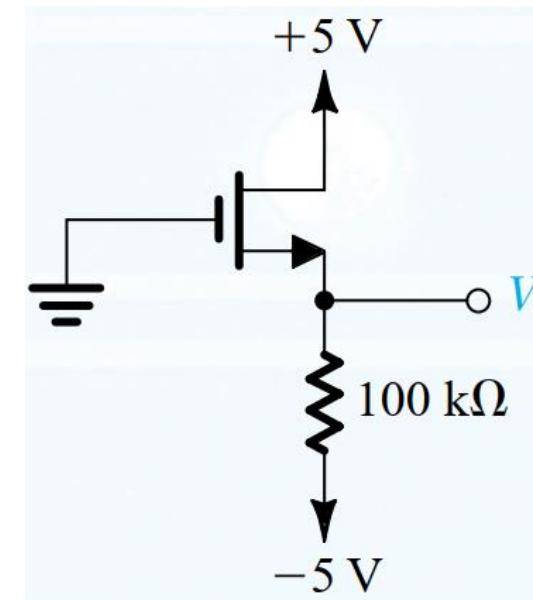
Ans:  $V = 2.8 V$

(a)



Ans:  $V = 2.8 V$

(b)

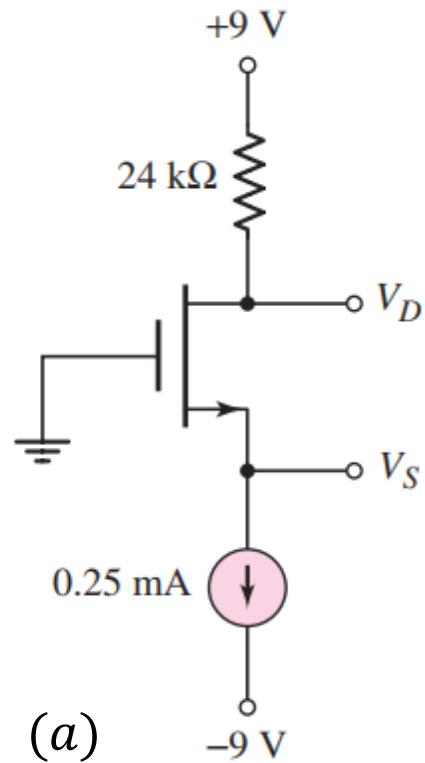


Ans:  $V = 1.19 V$

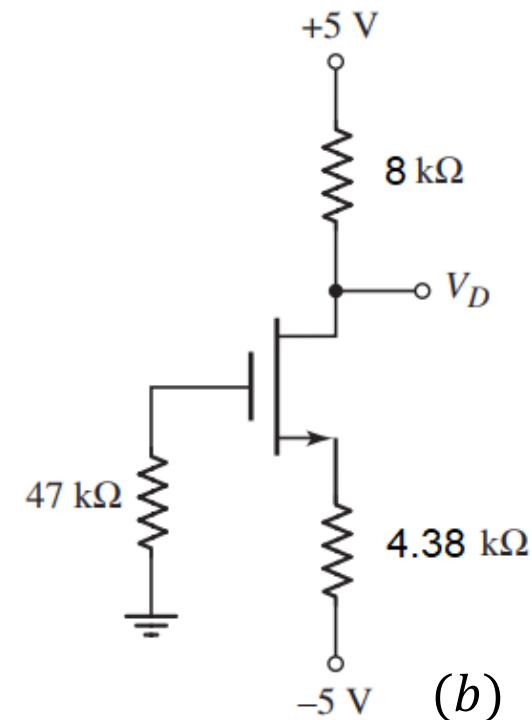
(c)

# Problem 15

- The transistors in the following circuits has parameters  $V_{Tn} = 0.6 V$  and  $k_n = k'_n \frac{W}{L} = 200 \mu A/V^2$ . Determine  $V_D$  and  $V_S$ .



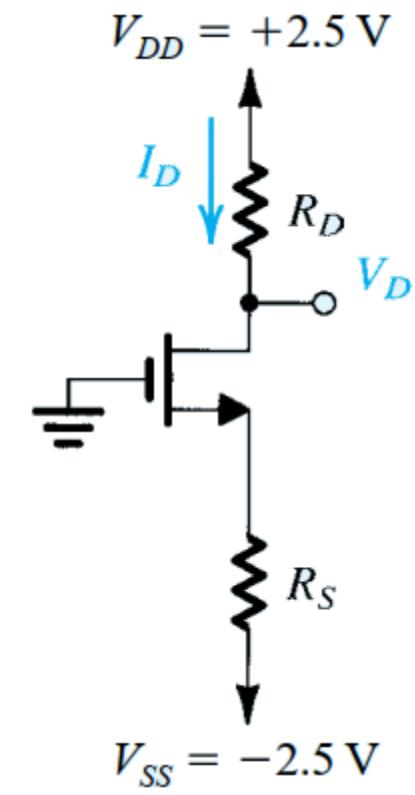
Ans:  $V_D = 3 V, V_S = 2.18 V$



Ans:  $V_D = 1.03 V, V_S = 2.83 V$

# Problem 16

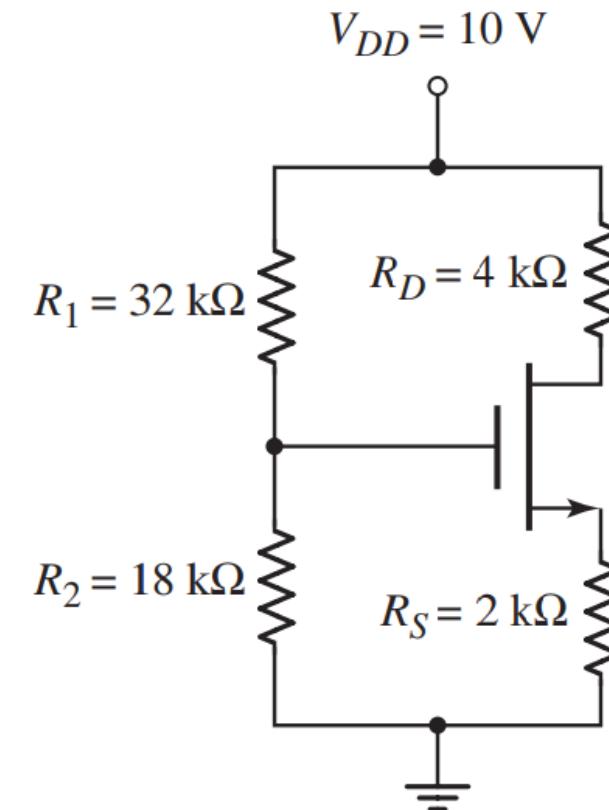
- Design the circuit, that is, determine the values of  $R_D$  and  $R_S$ , so that the transistor operates at  $I_D = 0.4 \text{ mA}$  and  $V_D = 0.5 \text{ V}$ . The transistor has  $V_{Tn} = 0.7 \text{ V}$  and  $k_n' \frac{W}{L} = 3.2 \text{ mA/V}^2$ .



**Ans:**  $R_D = 5 \text{ k}\Omega$ ,  $R_S = 3.25 \text{ k}\Omega$

# Problem 17

- The transistor in the following circuit has parameters  $V_{Tn} = 0.8 \text{ V}$  and  $k_n = k'_n \frac{W}{L} = 0.5 \text{ mA/V}^2$ . Determine the voltages across the transistor.

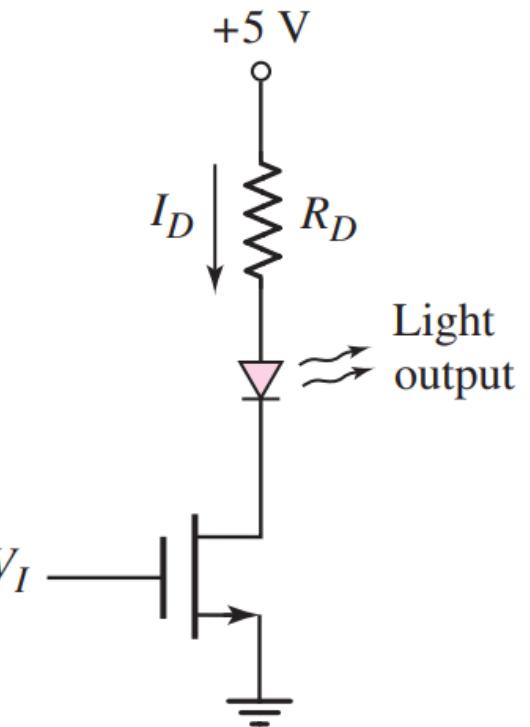


Ans:  $V_G = 3.6 \text{ V}$ ,  $V_D = 7.54 \text{ V}$ ,  $V_S = 1.23 \text{ V}$

# Problem 18

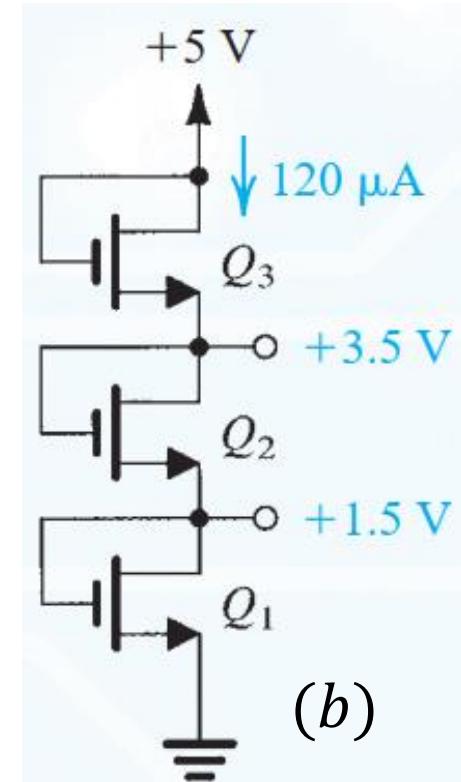
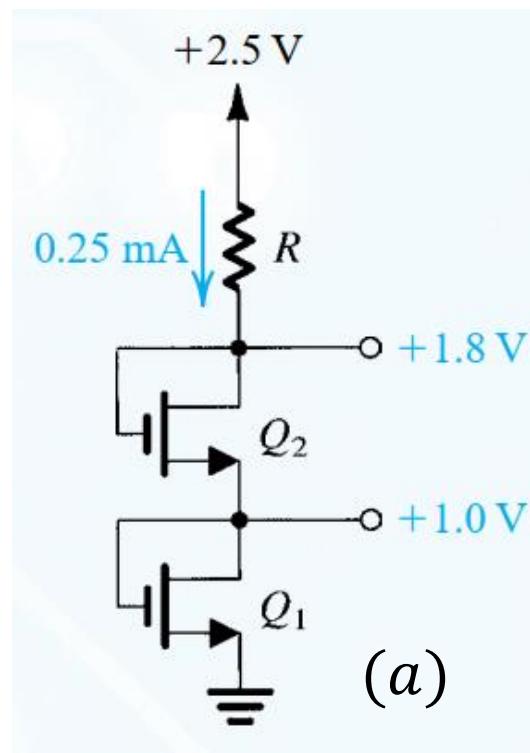
- The transistor in the following circuit is used to turn the LED on and off. The transistor parameters are  $V_{Tn} = 0.6 \text{ V}$  and  $k'_n = 80 \mu\text{A}/\text{V}^2$ . The diode cut-in voltage is  $V_{D_o} = 1.6 \text{ V}$ . Design  $R_D$  and transistor width-to-length  $(\frac{W}{L})$  ratio such that  $I_D = 12 \text{ mA}$  for  $V_I = 5 \text{ V}$  and  $V_{DS} = 0.15 \text{ V}$ .

**Ans:**  $R_D = 0.27 \text{ k}\Omega$ ,  $(\frac{W}{L}) = 15.5$



# Problem 19

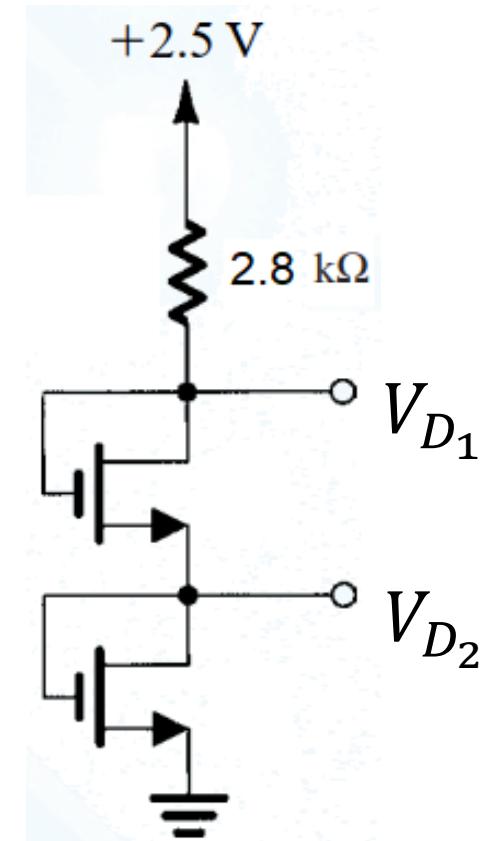
- The transistors in the following circuits have parameters  $V_{Tn} = 0.5 \text{ V}$ ,  $k'_n = \mu_n C_{oc} = 250 \frac{\mu\text{A}}{\text{V}^2}$ , and  $L = 0.25 \mu\text{m}$ . Determine the required values of gate width for each of the transistors.



Ans: (a)  $W_{Q_2} = 2.77 \mu\text{m}$ ,  $W_{Q_1} = 1 \mu\text{m}$ ; (b)  $W_{Q_3} = 0.12 \mu\text{m}$ ,  $W_{Q_2} = 0.053 \mu\text{m}$ ,  $W_{Q_1} = 0.12 \mu\text{m}$

# Problem 20

- For the transistors in the following circuit,  $V_{Tn} = 1 \text{ V}$  and  $k_n = k'_n \frac{W}{L} = 5 \text{ mA/V}^2$ . Determine  $V_{D_1}$  and  $V_{D_2}$ .

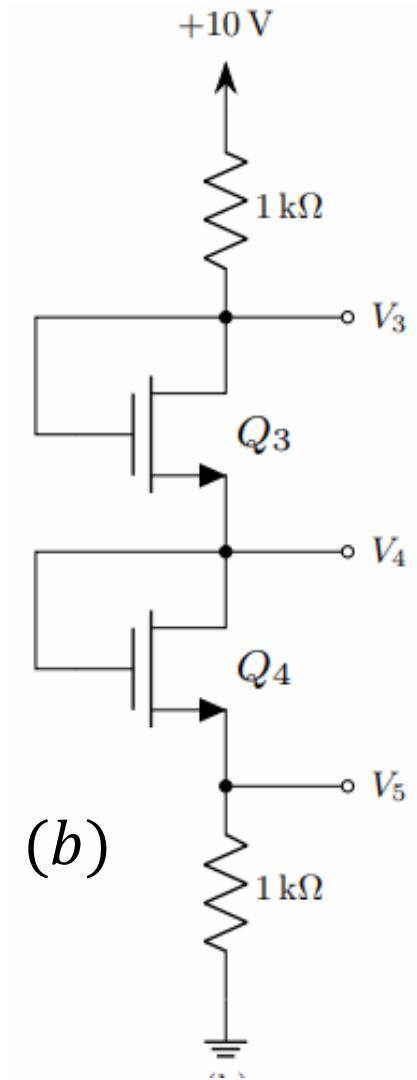
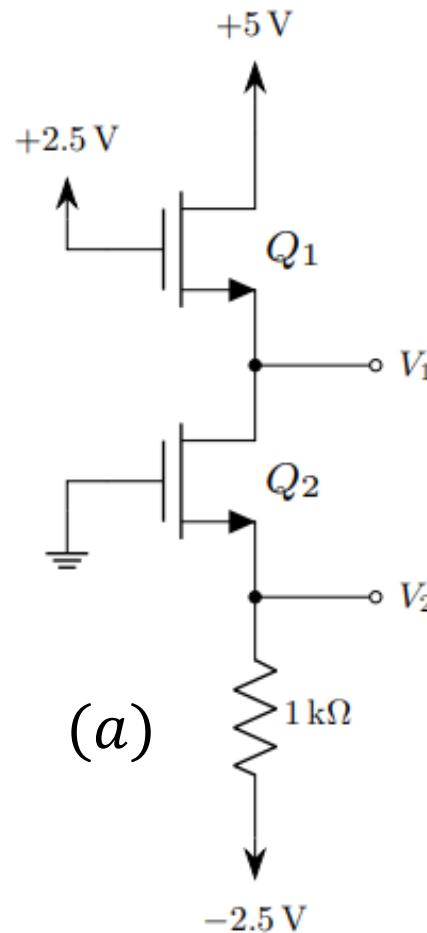


**Ans:**  $V_{D_1} = 2.32 \text{ V}, V_{D_2} = 1.16 \text{ V}$

# Problem 21

- For the transistors in the following circuits,  $V_{Tn} = 1\text{ V}$  and  $k_n = k'_n \frac{W}{L} = 2\text{ mA/V}^2$ . Determine  $V_1$  through  $V_5$ .

[Hint: Form simultaneous equations consisting of voltage variables for circuit in (b).]

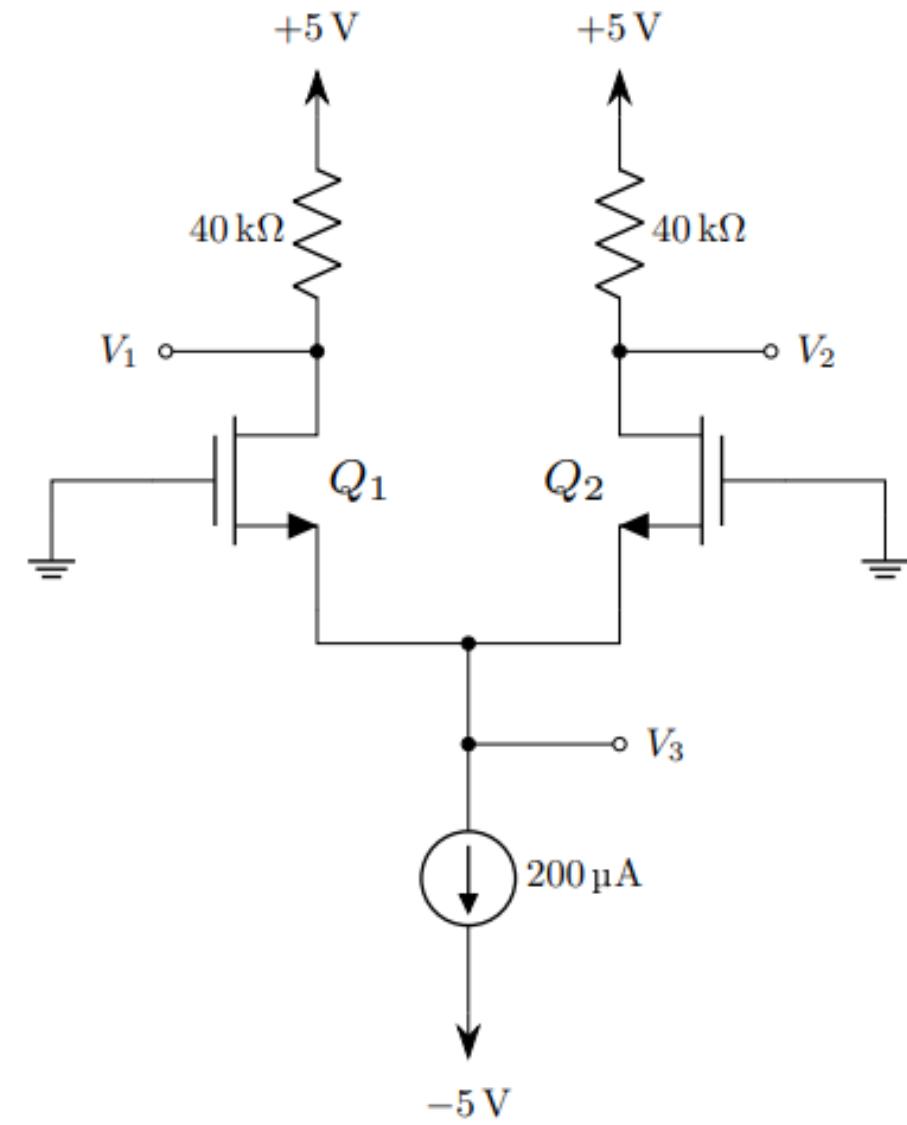


Ans: (a) **Both in sat**,  $V_1 = 4.5625\text{ V}$ ,  $V_2 = 0.75\text{ V}$

Ans: (b) **All in sat**,  $V_3 = 7.55\text{ V}$ ,  $V_4 = 5\text{ V}$ ,  $V_5 = 2.45\text{ V}$

# Problem 22

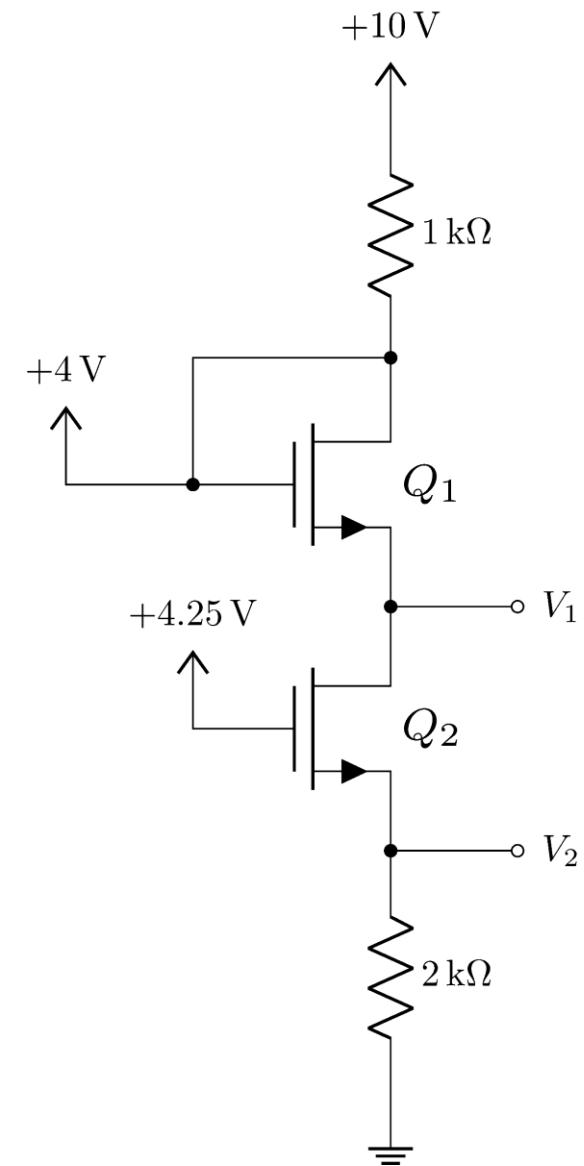
- For the transistors in the following circuits,  $V_{Tn} = 1\text{ V}$ ,  $k'_n = 10 \mu\text{A}/\text{V}^2$ , and  $\left(\frac{W}{L}\right)_1 = \left(\frac{W}{L}\right)_2 = 20$ . Determine  $V_1$  through  $V_3$ .



Ans:  $V_1 = V_2 = 1\text{ V}$ ,  $V_3 = 0\text{ V}$

# Problem 23

- For the transistors in the following circuits,  $V_{Tn} = 1\text{ V}$  and  $k_n = k'_n \frac{W}{L} = 100 \mu\text{A}/\text{V}^2$ . Determine  $V_1$  and  $V_2$ .



**Ans:** Both in sat,  $V_1 = 5.95\text{ V}$ ,  $V_2 = 0.295\text{ V}$