

# 13SLA4

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## §1 Solution

*Solution.* Couldnt solve it myself. Loved the solution by @randomusername.

Represent  $a_i$  by a bardiagram  $P$  with  $P = \{y = a_i; x \in [i - 1, i]\}$ . Reflect  $P$  over line  $y = x$  call this  $P'$ , now translate this such that its base sits on the line  $x = -n$ . Call the square  $\{0 \leq y \leq n; n \leq x \leq n\} = S$  To finish notice that,

$$n^2 \geq [P \cup S] + [P' \cup S] = \sum_{i=1}^n \min(a_i, n) + \sum_{i=1}^n \max(a_i - n, 0) = \sum_{i=1}^n a_i$$

□