11CSUR6

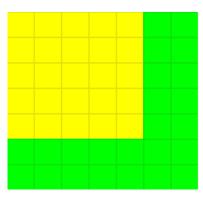
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§1 Solution

Solution. I claim the answer is (2n+1)(n+1).

Construction is simple enough: color the board with black stripes alternately. To prove this we will induct. Call the board Q(n). Color Q(n) as shown below, and call the **yellow** part Q(n-1) and the **green** part L(n-1).



Denote by |Q(n)|, |L(n)| the maximum amount of black cells possible with the given coloring.

We know that

$$|Q(n)| \le |Q(n-1)| + |L(n-1)|$$

Claim 1.1 — |L(n-1)| = 4n + 1

Proof. This is actually pretty easy just induct.

Now we will finish, assume |Q(n-1)| = (2(n-1)+1)((n-1)+1) note that

$$(2(n-1)+1)((n-1)+1)+(4n+1)=(2n+1)(n+1).$$

But that means $|Q(n)| \leq (2n+1)(n+1)$. So we are done.