

Q2:

a)  $1 - \frac{1}{N} \sum_{i=1}^N I[\max\{r_1^{(i)}, r_2^{(i)}, r_3^{(i)}\} = 0]$ . We estimate the prob. of at least one day would rain by estimating the prob. of none of the day rains, this prob. can be estimated by counting the event that  $\max\{r_1^{(i)}, r_2^{(i)}, r_3^{(i)}\} = 0$ , which means none of the three days would rain.

b) Estimator 1: unbiased

Estimator 2: biased

Estimator 3: biased

c) Estimator 1. Since estimator 2 & 3 are just one bernoulli r.v., the variance is not reduced by sample number  $N$ , but the estimator 1's variance is reduced due to sampling  $N$  times.