

## MCMS Problem Set

Name: Qusai Alotaqeen

Student no: 244849

### Question 2 Continued

- .) Finding the eigen values for the second equilibrium point Jacobian.

$$\begin{bmatrix} \beta(1 - 1/R_0) - \lambda & 0 \\ -\beta(1 - 1/R_0) & \lambda \end{bmatrix}$$

$$\rightarrow \lambda (\beta(1 - 1/R_0) - \lambda) = 0$$

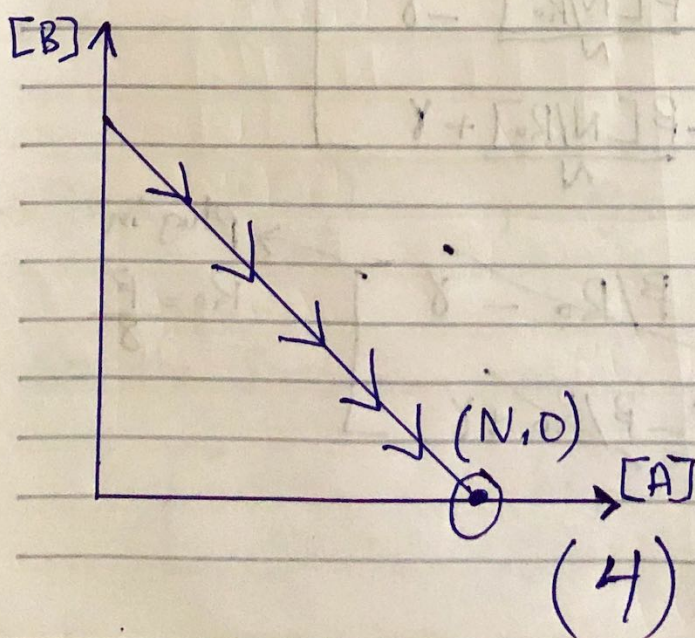
$$\boxed{\text{so } \lambda = 0} \quad \text{or} \quad \lambda = \beta(1 - 1/R_0)$$

$$\boxed{1 - 1/R_0 < 0} \quad \text{for stability to be achieved}$$

$$\boxed{\text{which means } \beta < \gamma} \quad \text{to be stable}$$

- .) Plotting the Phase Portrait

1) for  $(N, 0)$  and if  $\gamma < \beta$



2) for  $(N/R_0, N - N/R_0)$  and if  $\gamma > \beta$

