# IE 5561: Final Project

Quyen Huynh

2024-05-03

## Objective

Heart disease is the leading cause of death in the United States, affecting people of most ethnic backgrounds and genders. Even though heart disease is not curable (yet), predicting and detecting it earlier will help the doctor and patient reduce the severity of the problem and manage the symptoms. The goal of this project is to use machine learning models to predict whether a person has heart disease based on a number of variables.

## **Dataset**

The dataset used in this project is from Kaggle and can be accessed through the following link: https://www.kaggle.com/datasets/mexwell/heart-disease-dataset. There are 1190 observations and 12 variables, with the last variable target indicating whether the person has heart disease or not. The dataset attribute description in the link lists the values of the categorical variables, along with other important information about the columns.

## Approaches

First, we need to set working directory and set seed for the entire notebook. We also suppress any warnings and messages in the code output.

```
set.seed(1)
knitr::opts_chunk$set(message=FALSE, warning=FALSE)
```

Next, we will do some data exploration.

```
Heart = read.csv("./heart-disease-dataset/heart-disease.csv")
str(Heart)
```

```
'data.frame':
                    1190 obs. of 12 variables:
##
   $ age
                                40 49 37 48 54 39 45 54 37 48 ...
                                1 0 1 0 1 1 0 1 1 0 ...
##
   $ sex
   $ chest.pain.type
                                2 3 2 4 3 3 2 2 4 2 ...
                                140 160 130 138 150 120 130 110 140 120 ...
  $ resting.bp.s
                         : int
   $ cholesterol
                                289 180 283 214 195 339 237 208 207 284 ...
                         : int
   $ fasting.blood.sugar: int
                                0 0 0 0 0 0 0 0 0 0 ...
   $ resting.ecg
                                0 0 1 0 0 0 0 0 0 0 ...
                         : int
                                172 156 98 108 122 170 170 142 130 120 ...
   $ max.heart.rate
                         : int
```

```
## $ oldpeak : num 0 1 0 1.5 0 0 0 0 1.5 0 ...

## $ ST.slope : int 1 2 1 2 1 1 1 1 2 1 ...

## $ target : int 0 1 0 1 0 0 0 0 1 0 ...
```

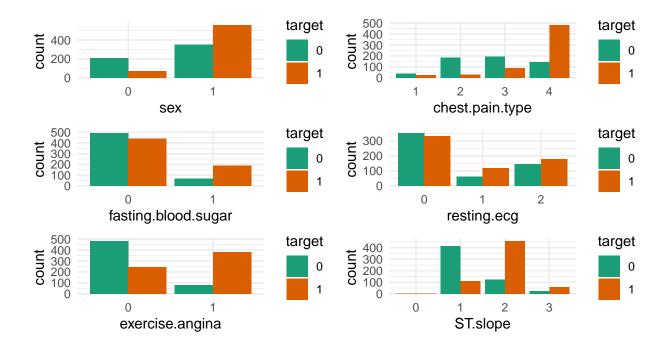
: int 000100010...

## \$ exercise.angina

```
##
                                   chest.pain.type resting.bp.s
        age
                        sex
                          :0.0000
  Min.
          :28.00
                   Min.
                                          :1.000
                                                   Min.
                                                        : 0.0
   1st Qu.:47.00
                   1st Qu.:1.0000
                                   1st Qu.:3.000
##
                                                   1st Qu.:120.0
## Median :54.00
                   Median :1.0000
                                   Median :4.000
                                                   Median :130.0
## Mean
         :53.72
                   Mean
                        :0.7639
                                   Mean
                                          :3.233
                                                   Mean
                                                         :132.2
## 3rd Qu.:60.00
                   3rd Qu.:1.0000
                                   3rd Qu.:4.000
                                                   3rd Qu.:140.0
## Max.
                                                          :200.0
          :77.00
                   Max.
                         :1.0000
                                   Max.
                                          :4.000
                                                   Max.
##
    cholesterol
                   fasting.blood.sugar resting.ecg
                                                       max.heart.rate
## Min. : 0.0
                 Min.
                         :0.0000
                                      Min.
                                            :0.0000
                                                       Min. : 60.0
                                      1st Qu.:0.0000
## 1st Qu.:188.0
                   1st Qu.:0.0000
                                                      1st Qu.:121.0
## Median :229.0
                  Median :0.0000
                                      Median :0.0000 Median :140.5
## Mean
         :210.4
                 Mean
                         :0.2134
                                      Mean :0.6983 Mean
                                                              :139.7
## 3rd Qu.:269.8
                   3rd Qu.:0.0000
                                      3rd Qu.:2.0000
                                                       3rd Qu.:160.0
                                                              :202.0
## Max.
          :603.0
                   Max.
                         :1.0000
                                      {\tt Max.}
                                             :2.0000
                                                      Max.
## exercise.angina
                       oldpeak
                                        ST.slope
                                                         target
## Min.
          :0.0000
                           :-2.6000
                                     Min.
                                            :0.000
                                                            :0.0000
                    Min.
                                                     Min.
## 1st Qu.:0.0000
                    1st Qu.: 0.0000
                                     1st Qu.:1.000
                                                     1st Qu.:0.0000
## Median :0.0000
                    Median : 0.6000
                                     Median :2.000
                                                     Median :1.0000
## Mean
         :0.3874
                    Mean
                          : 0.9228
                                     Mean
                                           :1.624
                                                     Mean
                                                            :0.5286
## 3rd Qu.:1.0000
                    3rd Qu.: 1.6000
                                     3rd Qu.:2.000
                                                     3rd Qu.:1.0000
## Max.
          :1.0000
                    Max.
                          : 6.2000
                                     Max.
                                            :3.000
                                                     Max.
                                                            :1.0000
```

There are categorical variables in the dataset, so we will convert those to factors and visualize them.

```
library(tidyverse)
library(gridExtra)
# Convert categorical columns to factors
categorical_vars = c("sex", "chest.pain.type", "fasting.blood.sugar", "resting.ecg",
                     "exercise.angina", "ST.slope", "target")
Heart[categorical_vars] = lapply(Heart[categorical_vars], as.factor)
# List of plots
plots = vector("list", length(categorical_vars))
i = 1
for (c in categorical_vars[!categorical_vars=="target"]) {
  plots[[i]] =
    ggplot(Heart) +
      geom_bar(aes(x=.data[[c]], fill=target), position=position_dodge()) +
      theme_minimal() +
      scale_fill_brewer(palette="Dark2")
  i = i + 1
}
# Arrange plots into 3x2 grid
do.call("grid.arrange", c(plots, ncol=2))
```



The top left plot shows that there are more males (1) than females (0) in the dataset and more males having heart disease than their female counterparts. The middle left graph reveals that those having fasting blood sugar higher than 120 mg/dl (1) are more likely to have heart disease than those do not (0), and the latter group makes up a larger portion of the data. Similarly, people who have exercise-induced angina (1) are more likely to have heart disease. An interesting finding is that, in the top right plot, there are much more heart disease cases in the chest pain type 4 group (asymptomatic) than other groups. As to electrocardiogram results, the majority of the observations are normal (0), and there seems to be relatively more heart disease cases in the other groups. Finally, instances with flat slope of the peak exercise ST segment (2), compared to upsloping and downsloping, are more likely to have heart disease.

The bottom right plot shows that there are some observations with ST.slope = 0, which is not defined in the attribute description. Checking the value counts of the column, we see that there is only one row with value 0, so we will drop this row.

```
##
## 0 1 2 3
## 1 526 582 81

# Drop row with ST.slope = 0
Heart = Heart[Heart$ST.slope != 0,]
```

### Logistic Regression

The first method we will try is logistic regression, which is a classic approach to classification problems. The dataset is split into training and test sets before fitting the model. The model tries to predict target using all other variables.

```
# Split 80/20 train/test sets
train = sample(nrow(Heart), size=0.8*nrow(Heart))
test = -train
# Logistic Regression
glm.fit = glm(target ~ ., data=Heart, family="binomial", subset=train)
summary(glm.fit)
##
## Call:
## glm(formula = target ~ ., family = "binomial", data = Heart,
##
       subset = train)
##
## Deviance Residuals:
      Min
                 10
                      Median
                                   30
                                           Max
## -2.6111 -0.4595
                      0.1727
                               0.4885
                                        2.6646
##
## Coefficients:
##
                         Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                    1.368411 -3.339 0.000839 ***
                        -4.569801
                         0.014223
                                    0.012287
                                               1.158 0.247043
## age
## sex1
                         1.636733
                                    0.257126
                                               6.365 1.95e-10 ***
## chest.pain.type2
                         0.084496
                                    0.455859
                                               0.185 0.852951
## chest.pain.type3
                         0.315102
                                    0.398564
                                               0.791 0.429182
## chest.pain.type4
                         1.883974
                                    0.389634
                                               4.835 1.33e-06 ***
## resting.bp.s
                         0.009268
                                    0.005620
                                               1.649 0.099114 .
## cholesterol
                        -0.003696
                                    0.001084 -3.409 0.000653 ***
## fasting.blood.sugar1 0.847826
                                    0.254375
                                               3.333 0.000859 ***
## resting.ecg1
                        -0.015969
                                              -0.052 0.958632
                                    0.307875
## resting.ecg2
                         0.136478
                                    0.231383
                                               0.590 0.555302
## max.heart.rate
                        -0.006094
                                    0.004708
                                             -1.294 0.195545
## exercise.angina1
                         0.797517
                                    0.227868
                                               3.500 0.000465 ***
## oldpeak
                         0.478135
                                    0.109410
                                               4.370 1.24e-05 ***
## ST.slope2
                         1.948747
                                    0.227118
                                               8.580 < 2e-16 ***
## ST.slope3
                         0.668438
                                    0.422090
                                               1.584 0.113276
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 1316.93
                               on 950
                                       degrees of freedom
## Residual deviance: 683.84
                               on 935 degrees of freedom
## AIC: 715.84
##
## Number of Fisher Scoring iterations: 5
```

```
library(caret)
# Function to print metrics using confusion matrix
printMetrics = function(confuse) {
 accuracy = round(mean(glm.pred==Heart$target[-train]), 4)
 sensitivity = round(sensitivity(confuse), 4)
 specificity = round(specificity(confuse), 4)
 print(paste("Accuracy:", accuracy))
 print(paste("Sensitivity:", sensitivity))
 print(paste("Specificity:", specificity))
 return (c(accuracy, sensitivity, specificity))
}
glm.probs = predict(glm.fit, type="response", newdata=Heart[-train,])
glm.pred = ifelse(glm.probs > 0.5, 1, 0)
confusion = table(glm.pred, Heart$target[-train])
confusion
##
## glm.pred 0 1
         0 93 19
##
         1 11 115
glm.metrics = printMetrics(confusion)
## [1] "Accuracy: 0.8739"
## [1] "Sensitivity: 0.8942"
## [1] "Specificity: 0.8582"
Since the p-values for max.heart.rate, resting.ecg, and resting.bp.s are relatively high, we will refit
the model excluding those variables.
# Drop variables and refit model
glm.fit = glm(target ~ . -resting.ecg -resting.bp.s -max.heart.rate,
             data=Heart, family="binomial", subset=train)
summary(glm.fit)
##
## Call:
## glm(formula = target ~ . - resting.ecg - resting.bp.s - max.heart.rate,
      family = "binomial", data = Heart, subset = train)
##
##
## Deviance Residuals:
                    Median
##
      Min
                1Q
                                 3Q
                                         Max
## -2.6242 -0.4650
                   0.1857 0.4972
                                      2.6897
##
## Coefficients:
                       Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                       ## age
                       1.634599  0.254445  6.424  1.33e-10 ***
## sex1
                      0.077110 0.455479 0.169 0.865566
## chest.pain.type2
```

```
## chest.pain.type3
                        0.279011
                                   0.399341
                                              0.699 0.484752
## chest.pain.type4
                                   0.386032 4.899 9.63e-07 ***
                        1.891221
## cholesterol
                       -0.003518
                                   0.001007 -3.493 0.000477 ***
## fasting.blood.sugar1 0.853199
                                   0.252122
                                              3.384 0.000714 ***
## exercise.angina1
                        0.897095
                                   0.218728
                                              4.101 4.11e-05 ***
## oldpeak
                                             4.456 8.36e-06 ***
                        0.477175
                                   0.107095
## ST.slope2
                                              9.072 < 2e-16 ***
                        1.992424
                                   0.219613
## ST.slope3
                        0.713769
                                   0.415231
                                              1.719 0.085621 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 1316.93 on 950
##
                                      degrees of freedom
## Residual deviance: 688.38 on 939 degrees of freedom
## AIC: 712.38
##
## Number of Fisher Scoring iterations: 5
glm.probs = predict(glm.fit, type="response", newdata=Heart[-train,])
glm.pred = ifelse(glm.probs > 0.5, 1, 0)
confusion = table(glm.pred, Heart$target[-train])
confusion
##
## glm.pred
             0
                 1
##
           93 19
##
          1 11 115
glm.metrics = printMetrics(confusion)
## [1] "Accuracy: 0.8739"
## [1] "Sensitivity: 0.8942"
## [1] "Specificity: 0.8582"
```

The metrics do not change after removing the variables from the model, so it is likely that the removed variables do not affect the chance of having heart disease.

#### **Decision Trees**

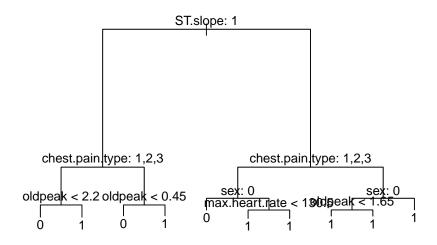
The next approach is decision trees, which are also popular for classification problems. We will first build a decision tree using all predictors, then prune the tree using cross-validation, and use the pruned tree to predict the test data.

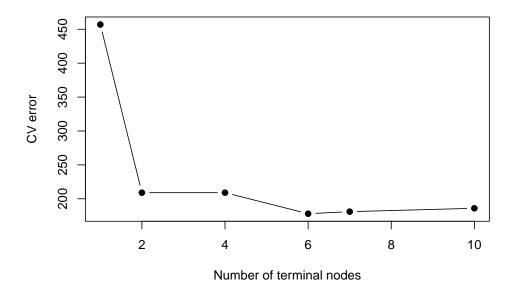
```
library(tree)

# Build initial tree
Heart.tree = tree(target ~ ., data=Heart, subset=train)
summary(Heart.tree)
```

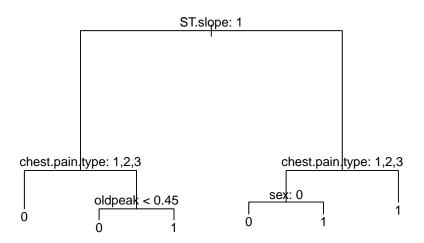
```
##
## Classification tree:
## tree(formula = target ~ ., data = Heart, subset = train)
## Variables actually used in tree construction:
## [1] "ST.slope" "chest.pain.type" "oldpeak" "sex"
## [5] "max.heart.rate"
## Number of terminal nodes: 10
## Residual mean deviance: 0.7464 = 702.3 / 941
## Misclassification error rate: 0.163 = 155 / 951

plot(Heart.tree)
text(Heart.tree, pretty=0)
```





```
# Prune tree
prune.tree = prune.misclass(Heart.tree, k=6)
plot(prune.tree)
text(prune.tree, pretty=0)
```



```
# Tree predictions
tree.pred = predict(prune.tree, newdata=Heart[-train,], type="class")
```

```
confusion = table(tree.pred, Heart$target[-train])
confusion

##

## tree.pred 0 1

## 0 88 19

## 1 16 115

tree.metrics = printMetrics(confusion)

## [1] "Accuracy: 0.8739"

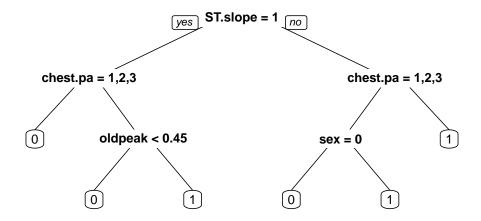
## [1] "Sensitivity: 0.8462"

## [1] "Specificity: 0.8582"
```

Below is another way to build the same tree using different libraries, with a more nicely-formatted output tree.

```
library(rpart)
library(rpart.plot)

tree = rpart(target ~ ., data=Heart)
best = tree$cptable[which.min(tree$cptable[, "xerror"]), "CP"]
pruned_tree = prune(tree, cp=best)
prp(pruned_tree)
```



```
tree.pred = predict(pruned_tree, newdata=Heart[-train,], type="class")
confusion = table(tree.pred, Heart$target[-train])
confusion
```

```
##
## tree.pred
               0
                   1
##
           0
              88
                 19
##
           1
             16 115
tree.metrics = printMetrics(confusion)
## [1] "Accuracy: 0.8739"
## [1] "Sensitivity: 0.8462"
## [1] "Specificity: 0.8582"
```

The most important variable in predicting heart disease seems to be whether the person has ST.slope = 1, which corresponds to an upsloping peak exercise ST segment. The second most important feature is chest.pa = 1,2,3. Looking at the bar plots earlier, we can see that people with ST.slope = 1 are less likely to have heart disease, and people in the chest pain type 4 group are more likely to be classified as heart disease patient. Therefore, the decision tree makes sense in classifying people who have ST.slope = 1 and chest.pa = 1,2,3 (far left branch) as normal, and those not having ST.slope = 1 and chest.pa = 1,2,3 (far right branch) as heart disease patients. If the observation has a mixed answer yes/no to those criteria, oldpeak and sex will be considered.

#### **Bagging**

0

1

5 125

##

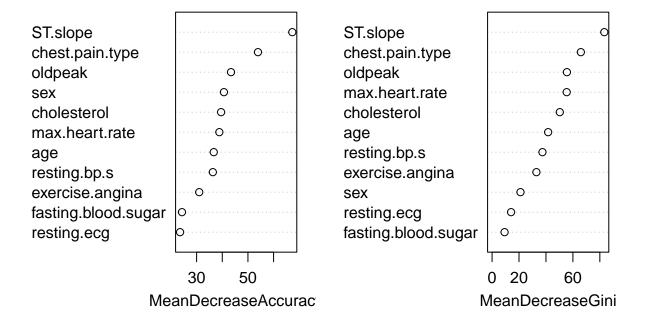
Decision trees usually suffer from high variance, so we will use bagging and random forest to build more powerful trees with lower variance. Random forests are improved bagged trees and consider only a subset of variables at each split of a tree.

```
library(randomForest)
# Bagging
Heart.bag = randomForest(target ~ ., data=Heart, subset=train, mtry=11, importance=TRUE)
Heart.bag
##
## Call:
   randomForest(formula = target ~ ., data = Heart, mtry = 11, importance = TRUE,
                                                                                         subset = train)
##
                  Type of random forest: classification
##
                        Number of trees: 500
## No. of variables tried at each split: 11
##
##
           OOB estimate of error rate: 8.2%
## Confusion matrix:
           1 class.error
## 0 408 49 0.10722101
## 1 29 465 0.05870445
bag.pred = predict(Heart.bag, newdata=Heart[-train,])
confusion = table(bag.pred, Heart$target[-train])
confusion
##
## bag.pred
              0
                  1
            99
                  9
```

```
bag.metrics = printMetrics(confusion)
## [1] "Accuracy: 0.8739"
## [1] "Sensitivity: 0.9519"
## [1] "Specificity: 0.9328"
Random Forest
We will use \sqrt{11} = 3 variables to grow a random forest as this is a classification problem.
# Random forest
Heart.rf = randomForest(target ~ ., data=Heart, subset=train, mtry=3, importance=TRUE)
Heart.rf
##
## Call:
   randomForest(formula = target ~ ., data = Heart, mtry = 3, importance = TRUE,
                                                                                    subset = train)
                 Type of random forest: classification
##
                       Number of trees: 500
## No. of variables tried at each split: 3
##
##
          OOB estimate of error rate: 7.26%
## Confusion matrix:
   0 1 class.error
##
## 0 414 43 0.09409190
## 1 26 468 0.05263158
rf.pred = predict(Heart.rf, newdata=Heart[-train,])
confusion = table(rf.pred, Heart$target[-train])
confusion
##
## rf.pred
           0 1
##
        0 99
        1
           5 128
##
rf.metrics = printMetrics(confusion)
## [1] "Accuracy: 0.8739"
## [1] "Sensitivity: 0.9519"
## [1] "Specificity: 0.9552"
# Variable importance
importance(Heart.rf)
##
                                      1 MeanDecreaseAccuracy MeanDecreaseGini
                             0
## age
                      31.63741 23.51490
                                                    36.68211
                                                              41.621907
## sex
                      32.29490 32.06782
                                                    40.64608
                                                                   21.084490
## chest.pain.type 45.16994 39.37718
                                                  53.91323
                                                                   65.910061
                    26.81636 25.11076
## resting.bp.s
                                                   36.32411
                                                                   37.412195
```

```
## cholesterol
                       32.81126 26.03458
                                                       39.54687
                                                                       50.285112
## fasting.blood.sugar 20.02320 18.02029
                                                       24.29908
                                                                        9.283397
## resting.ecg
                        19.02089 18.18698
                                                       23.55285
                                                                       14.109942
## max.heart.rate
                                                       38.86051
                                                                       55.416151
                        26.46509 30.77178
## exercise.angina
                        22.50810 27.22961
                                                       31.01566
                                                                       32.911112
## oldpeak
                        39.85787 26.27165
                                                       43.41520
                                                                       55.556218
## ST.slope
                       60.66862 43.91797
                                                       67.29896
                                                                       83.323201
varImpPlot(Heart.rf)
```

### Heart.rf



The results indicate that across all of the trees considered in the random forest, the slope of the peak exercise ST segment (ST.slope) and the chest pain type (chest.pain.type) are by far the two most important variables.

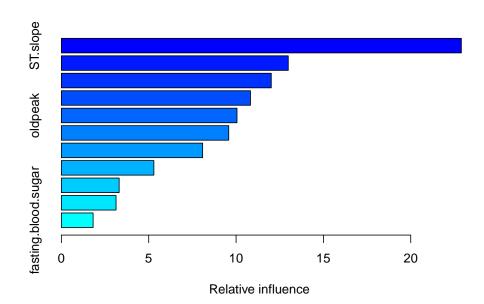
#### **Boosting**

Rather than fitting a single decision tree to the data, the boosting approach learns slowly and fits a tree to the residuals from the current model rather than the outcome Y.

```
library(gbm)

# Convert `target` to numeric

temp = Heart$target
Heart$target = as.numeric(Heart$target) - 1
```



```
##
                                       var
                                             rel.inf
## ST.slope
                                  ST.slope 22.896599
## chest.pain.type
                           chest.pain.type 12.989469
## cholesterol
                               cholesterol 12.015801
## max.heart.rate
                            max.heart.rate 10.825593
## oldpeak
                                   oldpeak 10.054108
                              resting.bp.s 9.581129
## resting.bp.s
## age
                                       age 8.087023
## sex
                                       sex 5.295483
                           exercise.angina 3.307666
## exercise.angina
## resting.ecg
                               resting.ecg 3.129860
## fasting.blood.sugar fasting.blood.sugar
                                           1.817269
# Convert `target` back to factor
Heart$target = as.factor(Heart$target)
gbm.prob = predict(Heart.gbm, newdata=Heart[-train,], type="response", n.trees=5000)
gbm.pred = ifelse(gbm.prob > 0.5, 1, 0)
confusion = table(gbm.pred, Heart$target[-train])
confusion
```

##

##

## gbm.pred

ed 0 0 97

7 125

1

#### boost.metrics = printMetrics(confusion)

```
## [1] "Accuracy: 0.8739"
## [1] "Sensitivity: 0.9327"
## [1] "Specificity: 0.9328"
```

## Support Vector Machine (SVM)

The last approach we will try is support vector machines, with two different kernels: radial and polynomial. We will perform cross-validation to find the best  $\gamma$  for the model with radial kernel and best degree d for the model with polynomial kernel.

```
##
## Parameter tuning of 'svm':
##
## - sampling method: 10-fold cross validation
##
## - best parameters:
##
   cost gamma
##
     10
          0.5
##
## - best performance: 0.1041228
##
## - Detailed performance results:
                     error dispersion
##
      cost gamma
## 1
     1e-01 0.1 0.1534978 0.02841417
## 2 1e+00 0.1 0.1303838 0.03023536
             0.1 0.1293531 0.01661015
## 3 1e+01
## 4
             0.1 0.1398246 0.02461773
     1e+02
## 5 1e+03
             0.1 0.1230482 0.03851090
## 6 1e-01
             0.5 0.2039803 0.04118035
## 7 1e+00
             0.5 0.1156689 0.01985228
## 8 1e+01
              0.5 0.1041228 0.02461721
## 9 1e+02
              0.5 0.1041228 0.02461721
## 10 1e+03
              0.5 0.1041228 0.02461721
## 11 1e-01
              1.0 0.4416009 0.04659846
## 12 1e+00
              1.0 0.1272259 0.02237726
## 13 1e+01
              1.0 0.1125439 0.02775176
## 14 1e+02
             1.0 0.1125439 0.02775176
## 15 1e+03
              1.0 0.1125439 0.02775176
## 16 1e-01
              2.0 0.4805154 0.04339625
## 17 1e+00
              2.0 0.1808114 0.04980074
## 18 1e+01
              2.0 0.1734649 0.04535428
## 19 1e+02
              2.0 0.1734649 0.04535428
```

```
## 20 1e+03
              2.0 0.1734649 0.04535428
## 21 1e-01
              3.0 0.4805154 0.04339625
## 22 1e+00
              3.0 0.2029057 0.04790197
## 23 1e+01
              3.0 0.1987061 0.05384867
## 24 1e+02
              3.0 0.1987061 0.05384867
## 25 1e+03
             3.0 0.1987061 0.05384867
## 26 1e-01
              4.0 0.4805154 0.04339625
## 27 1e+00
              4.0 0.2186732 0.05407079
## 28 1e+01
              4.0 0.2102741 0.05140251
## 29 1e+02
              4.0 0.2102741 0.05140251
## 30 1e+03
              4.0 0.2102741 0.05140251
svm.pred = predict(svm.tune$best.model, newdata=Heart[-train,])
confusion = table(svm.pred, Heart$target[-train])
svm.radial.metrics = printMetrics(confusion)
## [1] "Accuracy: 0.8739"
## [1] "Sensitivity: 0.9423"
## [1] "Specificity: 0.9254"
# SVM with polynomial kernel
svm.tune = tune(svm, target ~ ., data=Heart[train,], kernel="polynomial",
                ranges=list(cost=c(0.1,1,10,100,1000),
                            d=c(1,2,3,4,5))
summary(svm.tune)
##
## Parameter tuning of 'svm':
  - sampling method: 10-fold cross validation
##
##
## - best parameters:
   cost d
   1000 4
##
##
## - best performance: 0.1325439
## - Detailed performance results:
##
       cost d
                  error dispersion
## 1 1e-01 1 0.1682346 0.03707928
## 2 1e+00 1 0.1556250 0.03570673
## 3 1e+01 1 0.1566557 0.04124628
     1e+02 1 0.1534978 0.04024826
    1e+03 1 0.1534978 0.04024826
## 6 1e-01 2 0.1577851 0.03763580
     1e+00 2 0.1493750 0.04390635
## 8 1e+01 2 0.1535855 0.04485988
## 9 1e+02 2 0.1620175 0.04116488
## 10 1e+03 2 0.1693750 0.04684429
## 11 1e-01 3 0.2020066 0.04261684
## 12 1e+00 3 0.1577741 0.04224079
## 13 1e+01 3 0.1398904 0.05021312
## 14 1e+02 3 0.1462061 0.03741777
```

```
## 15 1e+03 3 0.1514583 0.03423364
## 16 1e-01 4 0.3994189 0.11497383
## 17 1e+00 4 0.2314364 0.04007595
## 18 1e+01 4 0.1525329 0.04568674
## 19 1e+02 4 0.1367544 0.03694048
## 20 1e+03 4 0.1325439 0.03765567
## 21 1e-01 5 0.4773136 0.04814601
## 22 1e+00 5 0.3039803 0.05748385
## 23 1e+01 5 0.1946162 0.03547689
## 24 1e+02 5 0.1356908 0.04056225
## 25 1e+03 5 0.1367325 0.03265888
svm.pred = predict(svm.tune$best.model, newdata=Heart[-train,])
confusion = table(svm.pred, Heart$target[-train])
svm.poly.metrics = printMetrics(confusion)
## [1] "Accuracy: 0.8739"
## [1] "Sensitivity: 0.9712"
## [1] "Specificity: 0.8433"
```

#### Discussion

#### Model Performance

	Logistic Regression	Decision Tree	Bagging	Random Forest	Boosting	SVM Radial	SVM Polynomial
Accuracy	0.8739	0.8739	0.8739	0.8739	0.8739	0.8739	0.8739
Sensitivity	0.8942	0.8462	0.9519	0.9519	0.9327	0.9423	0.9712
Specificity	0.8582	0.8582	0.9328	0.9552	0.9328	0.9254	0.8433

Accuracy rate stays the same across all models. The SVM model with polynomial kernel has the highest sensitivity, and random forest has the highest specificity. A high sensitivity means that there are few false negative results, and a high specificity means that there are few false positive results. Even though the SVM with polynomial kernel has the highest sensitivity, its specificity is the lowest among all models. Using a model with low specificity in the healthcare setting would lead to many false positive cases and patients receiving unnecessary medical treatments. Meanwhile, Bagging and Random Forest have the second highest sensitivity, and their specificity values are also in the top 2.

It is clear that, for our problem, Random Forest is the best model, closely followed by Bagging. Boosting and SVM with radial kernel have only slightly lower sensitivity and specificity than the top 2 models. As mentioned above, SVM with polynomial kernel has the highest sensitivity but lowest specificity. Since heart disease is a serious health condition and the leading cause of death in the US, a model with high sensitivity is desirable. It is more important to correctly diagnose all the positive cases than trying to lower the false positive rate. However, while Random Forest has a sensitivity rate that is around 2% lower than that of SVM with polynomial kernel, the former has a specificity rate that is a little more than 10% higher than that of the latter. Therefore, it is better to prefer the Random Forest model in this case. Finally, the Logistic Regression and Simple Decision Tree have the worst performance, likely due to their simple model assumptions of the data.

Aside from the models presented above, LDA and QDA were also considered, but they cannot be applied to this data because the variables are not continuous and do not meet the normal distribution requirement.

## Variable Importance

It is consistent across all models that ST.slope and chest.pain.type are the two most important variables in deciding whether a person has heart disease. The variable importance plot from the Random Forest model and the relative influence plot from Boosting show those two variables at the top; the decision trees also have those two factors at the first two splits. This makes sense because chest pain is indeed the most common symptom of heart disease. Other important variables are oldpeak, sex, cholesterol, and max.heart.rate.

The Logistic Regression model does not have a small p-value for max.heart.rate, and this is likely due to the simple model formula, as maximum heart rate can be an important factor in the health of the heart. Decision Trees outperform other models in interpretability and visuals as they are easy to use, even by people who are less familiar with machine learning models. Logistic Regression is also not too difficult to interpret, given that the formula is provided. However, as we can see from the model performance summary, despite their high interpretability, Logistic Regression and Decision Trees have the lowest performance in terms of sensitivity and specificity. This is an important trade-off that we should keep in mind.

## Conclusion

As heart disease is a serious health condition and affects many people, not just in the US but also around the world, it has always been of great interest to develop machine learning models to predict heart disease. This project explored a number of classification models, such as Logistic Regression, Decision Trees, Random Forests, SVM, etc., all of which can be used to predict whether a person has heart disease using a number of variables. The results show that Random Forest performs the best on this dataset, followed by the Bagging approach. The models reveal the most important factors in predicting heart disease to be the slope of the peak exercise ST segment and the type of chest pain, followed by other variables such as sex, cholesterol, max heart rate, etc.

To improve model performance and further the development of heart disease predicting models, there are a few suggestions. First, we can explore other formulas, such as polynomial and interactions, in the Logistic Regression model. Subset selection can be used to narrow down the most important features, and regularization can be added to improve model fitting. Second, the parameters in the more complex models, such as number of trees and interaction depth in Boosting, can be further tuned by cross-validation. Finally, it is possible that other classification models that were not discussed in this project perform even better, such as KNN, neural networks, etc. No matter which model we choose, it is crucial to consider the sensitivity of the approach, as detecting heart disease early is better than incorrect classification and further complications for the patient.