

UNIVERSITY OF SCIENCE  
FALCUTY OF INFORMATION TECHNOLOGY



**SUBJECT:** INTRODUCTION TO AI

**LAB 01 – THE KNIGHT’S TOUR  
CLASS 20CLC11**

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# Table of Contents

<b><i>I) Checklist.....</i></b>	<b><i>3</i></b>
<b><i>II) Statistical report .....</i></b>	<b><i>3</i></b>
1. Backtracking's Algorithm.....	3
2. Warnsdorff's Algorithm .....	4
<b><i>III) Reference .....</i></b>	<b><i>6</i></b>

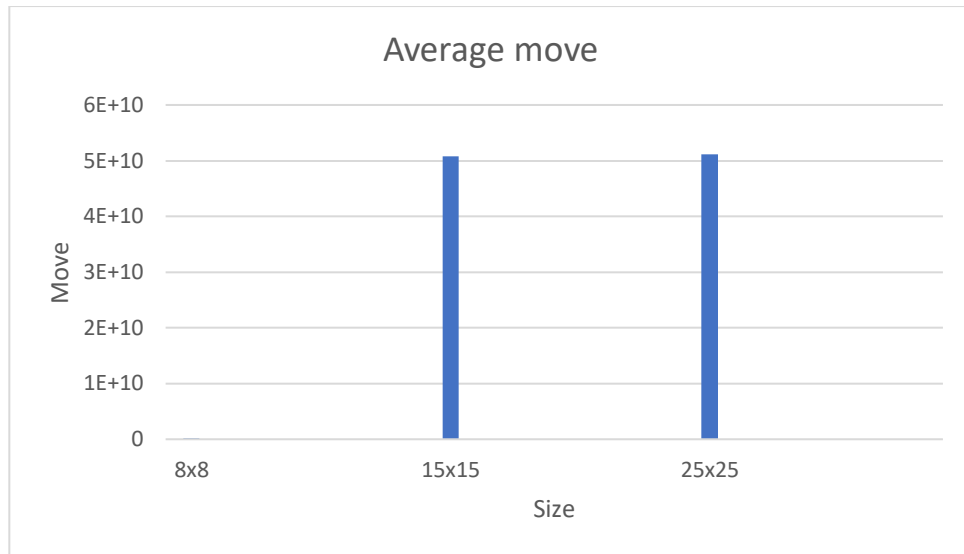
## I) Checklist

STT	Criteria	Done	Not done
1	Manipulate the input and output	X	
2	Implement the backtracking	X	
3	Implement the Warnsdorff's Heuristic	X	
4	Provide valid results for the backtracking strategy	X	
5	Provide valid results for the Warnsdorff's Heuristic	X	
6	Provide all evidential files in the OUTPUT folder	X	
7	Report sufficient information in the document	X	

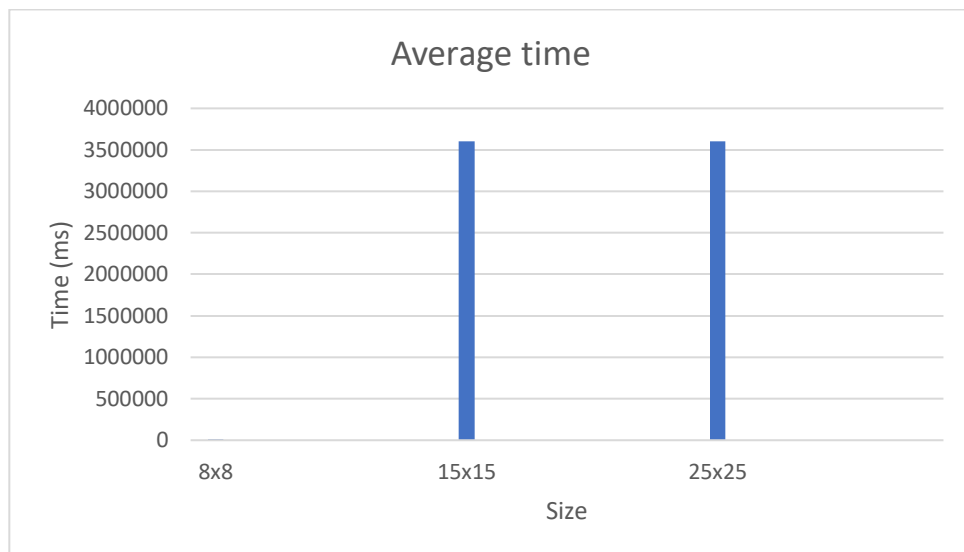
## II) Statistical report

### 1. Backtracking's Algorithm

SIZE	POSITION	MOVES	RUNNING TIME (ms)	AVERAGE MOVES	AVERAGE TIME (ms)
<b>8x8</b>	(1, 1)	8250733	526.819	~ 150121277.8	~ 9749.9316
	(5, 1)	9152986	613.815		
	(8, 1)	3242065	288.334		
	(5, 3)	108524012	6938.09		
	(8, 2)	621436593	40382.6		
<b>15x15</b>	(1, 1)	> 460000000000	3600000	~ 508000000000	~ 3600000
	(5, 1)	> 490000000000	3600000		
	(4, 6)	> 520000000000	3600000		
	(5, 3)	> 610000000000	3600000		
	(4, 3)	> 460000000000	3600000		
<b>25x25</b>	(1, 1)	> 620000000000	3600000	~ 512000000000	~ 3600000
	(8, 1)	> 500000000000	3600000		
	(5, 3)	> 470000000000	3600000		
	(4, 6)	> 510000000000	3600000		
	(4, 2)	> 460000000000	3600000		



*(The graph shows the average moves using backtracking algorithm)*



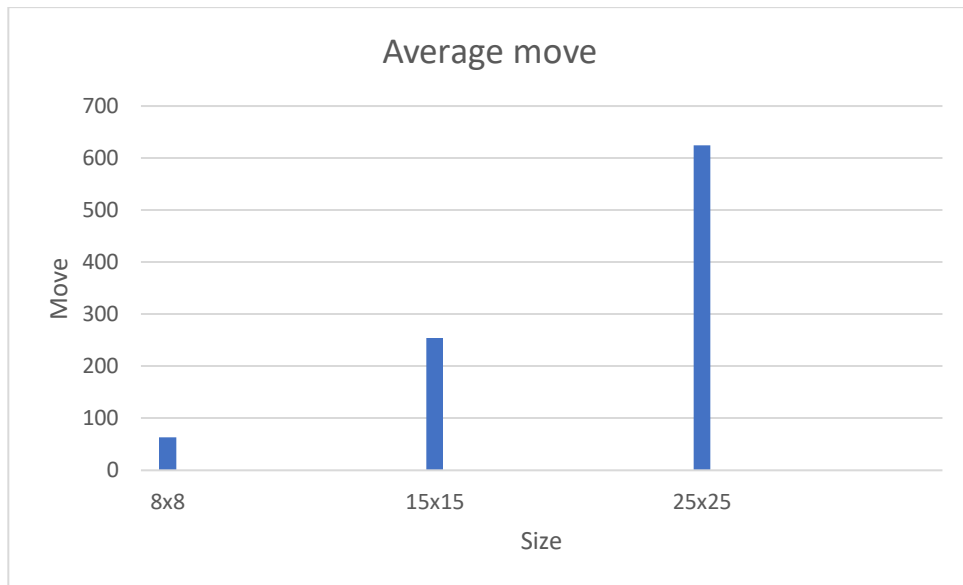
*(The graph shows the average time using backtracking algorithm)*

### Discussion:

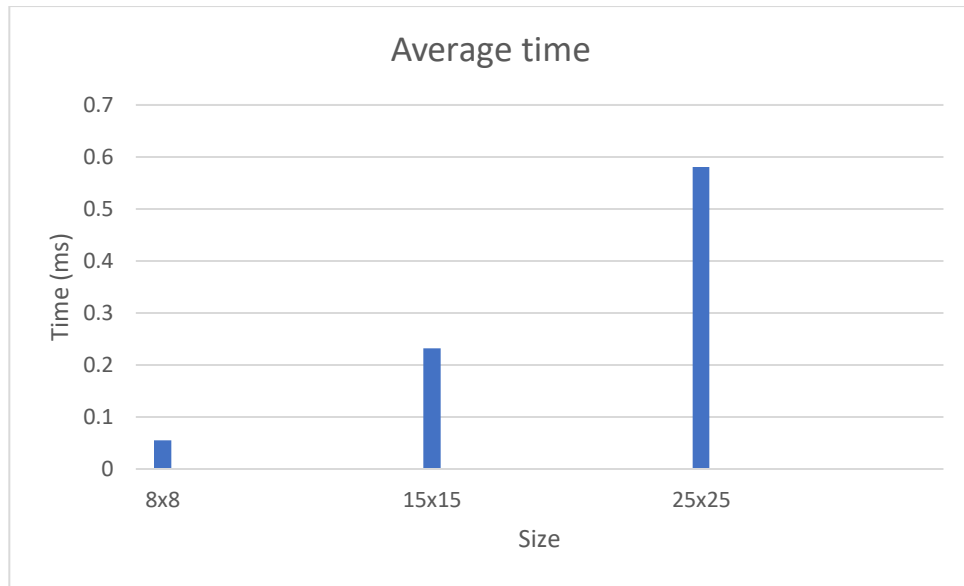
- Most of the coordinates on the board like -px 1 -py 5 with size 8x8, backtracking algorithm solves in a very long time that normal computers can't process.
- With board size 8x8, only some specific coordinates such as (1, 1), (5,1), (5,3), the program can give faster outputs. Either with board size 15x15 and 25x25.

## 2. Warnsdorff's Algorithm

SIZE	POSITION	MOVES	RUNNING TIME (ms)	AVERAGE MOVES	AVERAGE TIME (ms)
<b>8x8</b>	(1, 1)	64	0.056	~ 64	0.0552
	(5, 1)	64	0.056		
	(8, 1)	64	0.054		
	(8, 2)	64	0.057		
	(4, 3)	64	0.053		
<b>15x15</b>	(2, 6)	225	0.215	~ 254	0.2324
	(5, 1)	225	0.193		
	(5, 3)	225	0.279		
	(1, 8)	222	0.272		
	(4, 1)	224	0.203		
<b>25x25</b>	(1, 1)	625	0.529	~ 625	0.5802
	(5, 1)	625	0.614		
	(8, 8)	625	0.666		
	(4, 6)	625	0.546		
	(2, 7)	624	0.546		



*(The graph shows the average moves using Warnsdorff's heuristic algorithm)*



*(The graph shows the average time using Warnsdorff's heuristic algorithm)*

### Discussion:

- Heuristic algorithm in some cases does not provide the correct solution to solve the board. Since it uses heuristic functions to declare the next move with smallest moveable steps.
- Therefore, with cases that cannot reach all cells in the board, steps will be counted respectively and the statistics will output the probability of success knight tours.

### III) Reference

1. Wikipedia The Knight's Tour: [https://en.wikipedia.org/wiki/Knight%27s\\_tour](https://en.wikipedia.org/wiki/Knight%27s_tour)
2. GeeksForGeeks Backtracking's Algorithm: <https://www.geeksforgeeks.org/the-knights-tour-problem-backtracking-1/>
3. GeeksForGeeks Warnsdorff's Algorithm: <https://www.geeksforgeeks.org/warnsdorffs-algorithm-knights-tour-problem/>