

ANOVA Tables

N : total # of obs.

• One-way ANOVA

<u>Source</u>	<u>DF</u>	<u>SS</u>
Factor A	$a-1$	$N \bar{y}_{..}^2$ (SSA)
Error	$N-a$	$\sum_{i=1}^a \sum_{j=1}^{n_i} (y_{ij} - \bar{y}_{i.})^2$ (SSE)

• Two-way ANOVA (Balanced case)

$$y_{ijk} = \mu + \alpha_i + \beta_j + \gamma_{ij} + \varepsilon_{ijk} \leftarrow$$

<u>Source</u>	<u>DF</u>	<u>SS</u>	<u>MS</u>
Factor A	$a-1$	SSA	$SSA / (a-1)$
Factor B	$b-1$	SSB	$SSB / (b-1)$
Interaction	$(a-1)(b-1)$	SSI	$SSI / [(a-1)(b-1)]$
Error	$ab(n-1)$	SSE	$SSE / [ab(n-1)]$

$$SSA = bn \sum_i (\bar{y}_{i..} - \bar{y}_{...})^2$$

$$SSB = an \sum_j (\bar{y}_{.j.} - \bar{y}_{...})^2$$

$$SSI = n \sum_i \sum_j (\bar{y}_{ij.} - \bar{y}_{i..} - \bar{y}_{.j.} + \bar{y}_{...})^2$$

$$SSE = \sum_i \sum_j \sum_k (y_{ijk} - \bar{y}_{ij.})^2$$