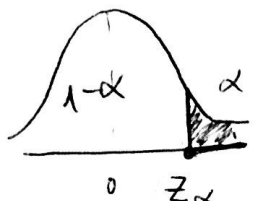
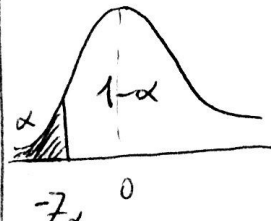
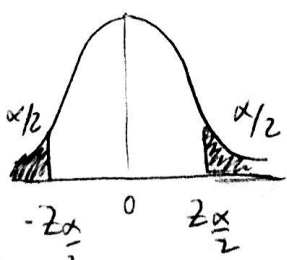
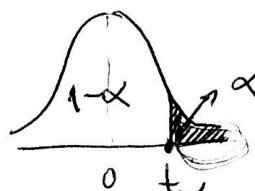
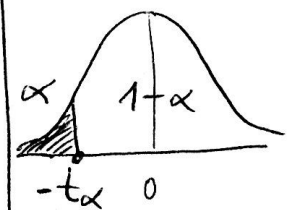
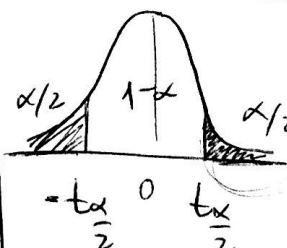


Summary: hypothesis testing for a proportion: p .

follow 8 steps.

| steps 1-3 | step 4 | step 5 | step 6 | step 7 | step 8 |
|-------------------------------------|---------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------|
| $H_0: p = p_0$ $H_1: p > p_0$ | choose α (0.01 0.05 0.1) | $Z^{stat} = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$ Under the assumption that the H_0 is true it follows the standard normal distribution. |  $p\text{-value} = P(Z > Z^{stat})$ | reject H_0 $Z^{stat} > Z_\alpha$ or $p\text{-value} < \alpha$ | non technical interpretation of step 7. |
| $H_0: p = p_0$ $H_1: p < p_0$ | | |  $p\text{-value} = P(Z < Z^{stat})$ | reject H_0 $Z^{stat} < -Z_\alpha$ or $p\text{-value} < \alpha$ | |
| $H_0: p = p_0$ $H_1: p \neq p_0$ | | |  $p\text{-value} = 2 P(Z > Z^{stat})$ if $Z^{stat} > 0$ $p\text{-value} = P(Z < Z^{stat})$ if $Z^{stat} < 0$ | reject H_0 $Z^{stat} > Z_{\frac{\alpha}{2}}$ or $Z^{stat} < -Z_{\frac{\alpha}{2}}$ or $p\text{-value} < \alpha$ | |

Test of hypothesis for the mean μ .
follow 8 steps.

| steps 1-3 | step 4 | step 5 | step 6 | step 7 | step 8 |
|---------------------------------------------|---------------------------------------|----------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------|
| $H_0: \mu = \mu_0$ $H_1: \mu > \mu_0$ | $\in H_0$ t_{stat} α . | $t^{stat} = \frac{\bar{X} - \mu_0}{S/\sqrt{n}}$ <p>under the assumption that H_0 is true it follows</p> |  <p> $P\text{-value} = P(t > t^{stat})$ </p> | <p>reject H_0 $t^{stat} > t_\alpha$ or $P\text{-value} < \alpha$.</p> | <p>make non technical interpretation of step 7</p> |
| $H_0: \mu = \mu_0$ $H_1: \mu < \mu_0$ | | <p>the student t distribution with $(n-1)$ degrees of freedom.</p> |  <p> $P\text{-value} = P(t < t^{stat})$ </p> | <p>reject H_0 $t^{stat} < -t_\alpha$ or $P\text{-value} < \alpha$.</p> | |
| $H_0: \mu = \mu_0$ $H_1: \mu \neq \mu_0$ | | |  <p> $P\text{-value} = 2P(t > t^{stat})$ if $t^{stat} > 0$ $P\text{-value} = 2P(t < t^{stat})$ if $t^{stat} < 0$. </p> | <p>reject H_0 $t^{stat} > t_{\alpha/2}$ or $t^{stat} < -t_{\alpha/2}$ or $P\text{-value} < \alpha$</p> | |

Slide 7.

step 1: "the mean amount of sleep for adults is less than 7 hours".
 $\mu < 7$

step 2: $\mu \geq 7$.

step 3: $H_0: \mu = 7$ $H_1: \mu < 7$

step 4: level of significance is 0.05. $\alpha = 0.05$
 $\alpha = P(\text{reject } H_0 \text{ when the } H_0 \text{ is true})$

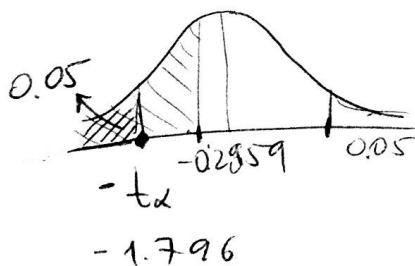
2.201.

step 5: $t^{\text{stat}} = \frac{\bar{X} - \mu_0}{S/\sqrt{n}} = \frac{6.83 - 7}{1.99/\sqrt{12}} = -0.2959$.

t^{stat} has a student t distribution with $(n-1) = 11$ degrees of freedom.

step 6: critical ~~value~~ value is

11 degrees of freedom.



$$-t_{\alpha} = -1.796$$

software

$$p\text{-value} = P(t < -0.2959) = 0.3864$$

step 7: based on critical value we fail to reject the H_0 . (because $t^{\text{stat}} = -0.2959 > -1.796 = -t_{\alpha}$).

step 8: There is not enough evidence to support the claim that the mean amount of sleep for adults is less than 7 hours.