

1. Bisection Method: solve an equation.

$$x + 3 = 0 \Rightarrow x = -3$$

$$f(x) = x^2$$
$$f(a) = a^2$$

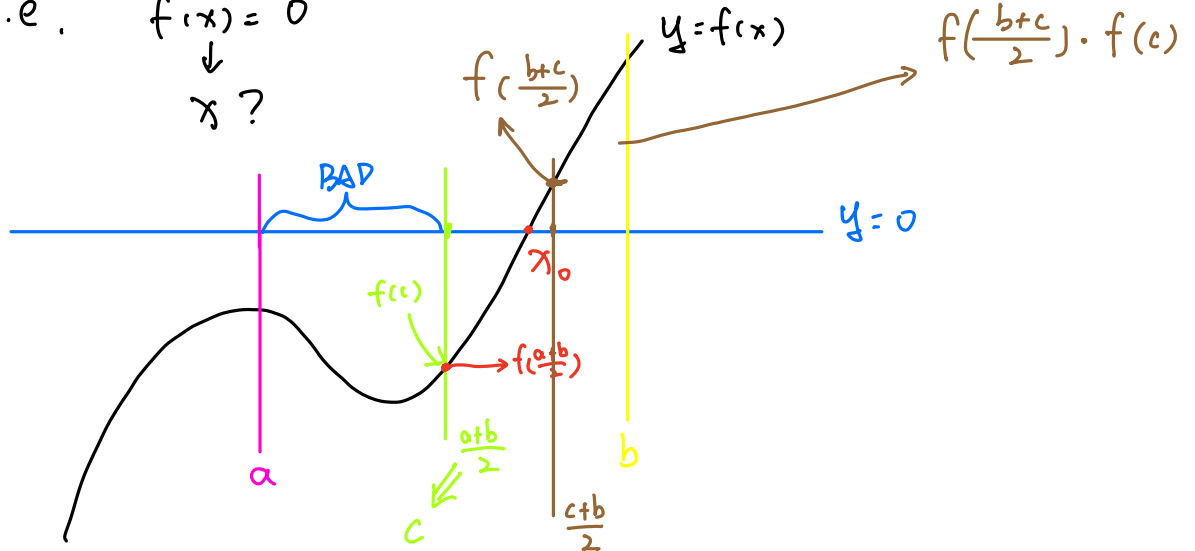
2. Set up:

Given a function  $f(\cdot)$ , calculate its zero point:

i.e.  $f(x) = 0$

$\downarrow$   
 $x?$

3.



Step 1: Initialize the boundary of the interval  
satisfying  $f(a) \cdot f(b) < 0$

Step 2: Calculate  $f\left(\frac{a+b}{2}\right)$   $\left\{ \begin{array}{l} x_0 \text{ is not between } a \text{ and } \frac{a+b}{2} \\ \text{if } f\left(\frac{a+b}{2}\right) \cdot f(a) > 0, \text{ that means} \\ \text{no zero point! So, } \frac{a+b}{2} < x_0 < b \end{array} \right.$

# Pseudo Code:

bisec\_method  $\leftarrow$  function()

Arguments:

①: Target function : a function

②: Boundary: numeric, vector of 2  
first element is left bound, second is right

③: Stopping criteria:

case 1:  $f(x) = 0$

case 2: Tolerance:  $10^{-6}$

case 3: maximum iteration steps.

bisec\_meth  $\leftarrow$  function()

①:  $tf$

②:  $bd \leftarrow$

③:  $tol$

④:  $max\_iter$  }

$a \leftarrow bd[1]$

$b \leftarrow bd[2]$

if ( $tf(a) \cdot tf(b) > 0$ ) { stop ("Bad INI") }

for (iter in  $1:max\_iter$ ) {

update  $c \leftarrow \frac{a+b}{2}$

update { if ( $f(c) = 0$ ) { return (c) }

$a, b$  { if ( $f(a) \cdot f(c) < 0$ ) {  $b \leftarrow c$  } else {  $a \leftarrow c$  }

$f(a) \cdot f(c) > 0$

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if (|a-b| < tol) { return a }  
if (iter == max_iter) { warning("Out of Iter.")  
    return(a) }
```

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}  
}
```