

# Advanced Computer Graphics

## Lecture-08 Introduction to OpenGL-6

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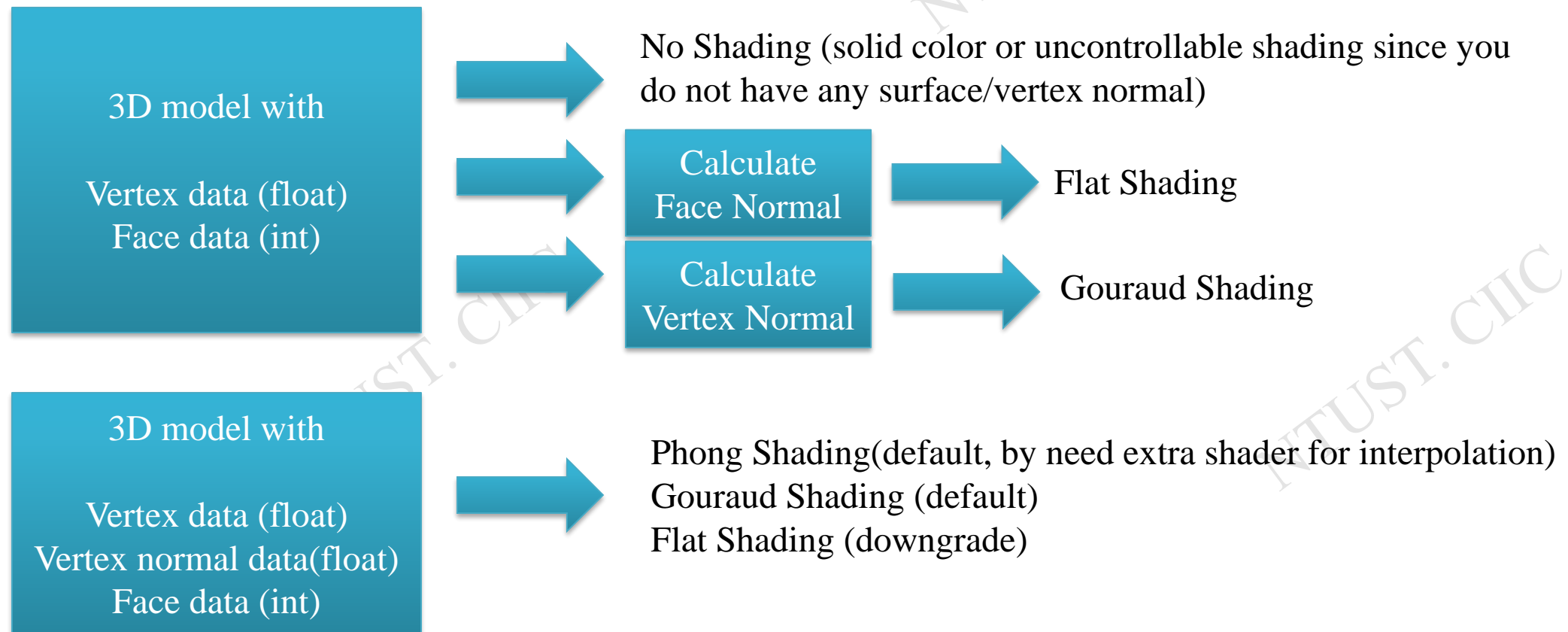
# Outline

- Gouraud Shading / Flat Shading
  - Backface Cull
  - Depth Test
  - Camera Control
- 
- The necessary data: vertex's normal



# Gouraud Shading vs Flat Shading

- For better visualization, you may need more data such vertex-normal.

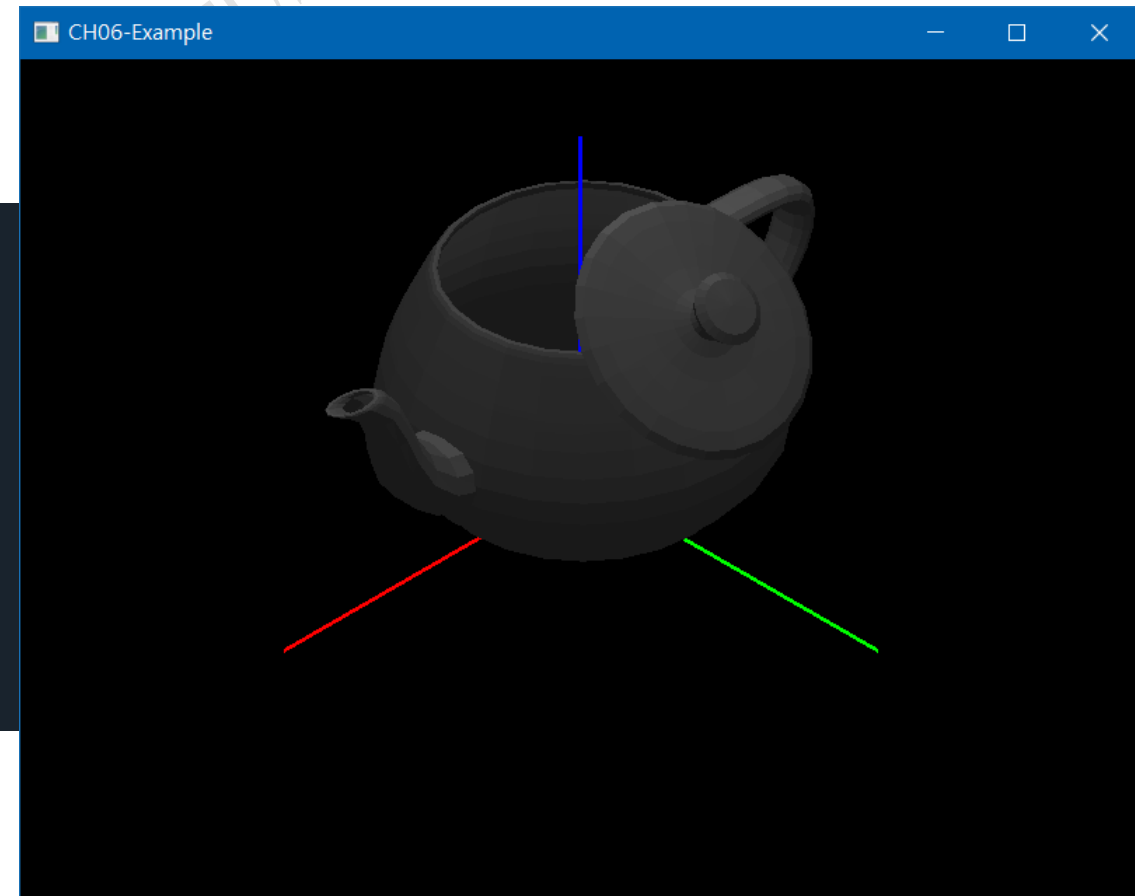




# Gouraud Shading vs Flat Shading

- Calculate Face Normal and assign it to each vertexes on a tringle (Flat shading)

```
4633 def drawTeapot():
4634     glBegin(GL_TRIANGLES)
4635     for fID in teapotFace:
4636         v1 = np.subtract(teapotVertex[fID[1]] ,teapotVertex[fID[0]])
4637         v2 = np.subtract(teapotVertex[fID[2]] ,teapotVertex[fID[0]])
4638         nv = np.cross(v1,v2)
4639         nlen = np.linalg.norm(nv, ord=1)
4640         nv = nv / nlen
4641         glNormal3f(nv[0],nv[1],nv[2])
4642         glVertex3fv(teapotVertex[fID[0]])
4643         glVertex3fv(teapotVertex[fID[1]])
4644         glVertex3fv(teapotVertex[fID[2]])
4645     glEnd()
```

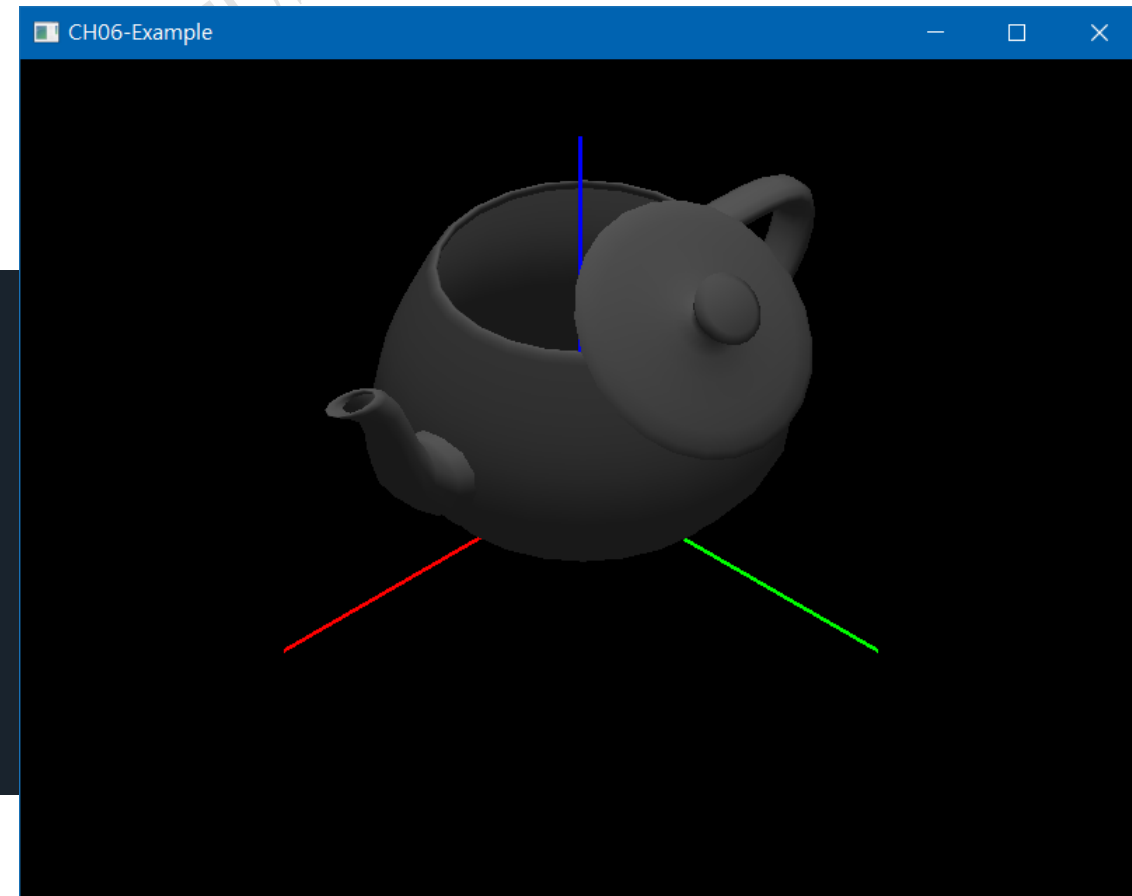




# Gouraud Shading vs Flat Shading

- Assign a normal vector to each vertex

```
4633 def drawTeapot():
4634     glBegin(GL_TRIANGLES)
4635     for fID in teapotFace:
4636         glNormal3fv(teapotVertexNormal[fID[0]])
4637         glVertex3fv(teapotVertex[fID[0]])
4638         glNormal3fv(teapotVertexNormal[fID[1]])
4639         glVertex3fv(teapotVertex[fID[1]])
4640         glNormal3fv(teapotVertexNormal[fID[2]])
4641         glVertex3fv(teapotVertex[fID[2]])
4642     glEnd()
4643
```

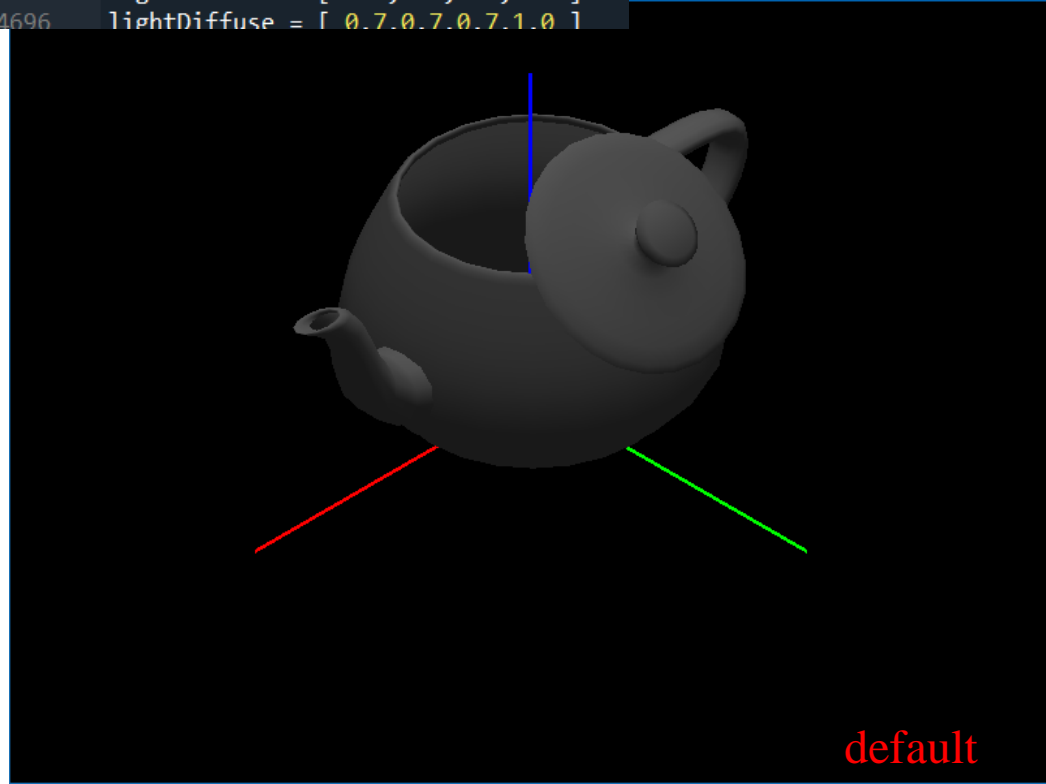




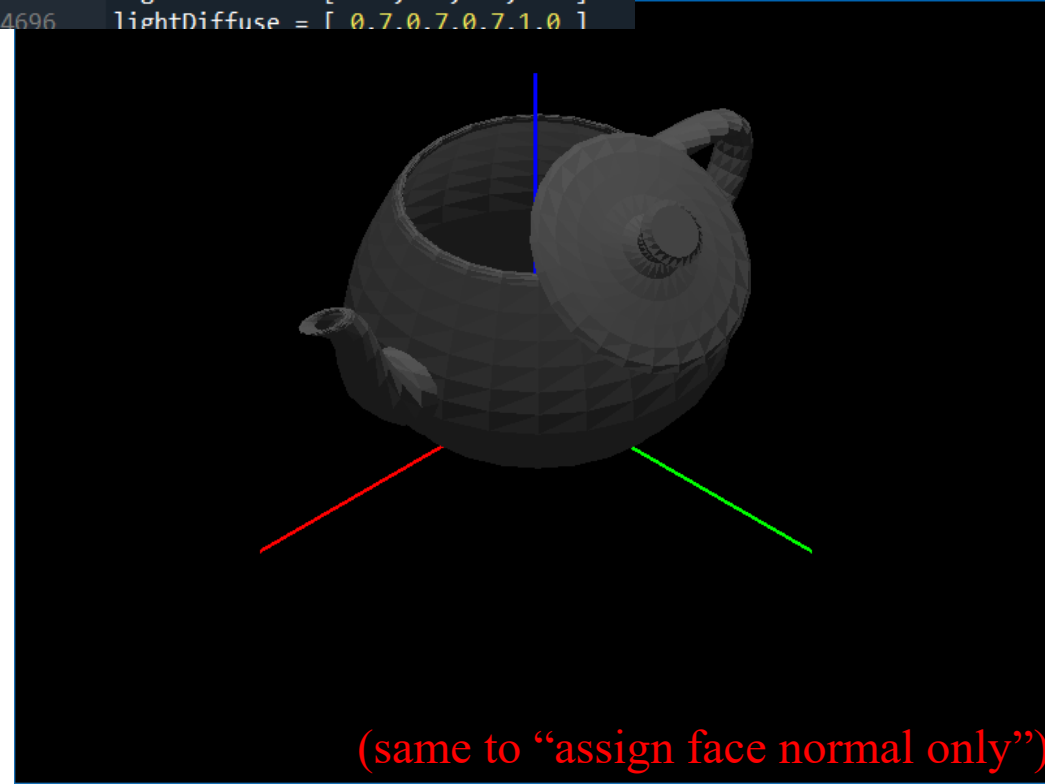
# Gouraud Shading vs Flat Shading

```
4632
4633 def drawTeapot(): (assign normal vectors to vertexes)
4634     glBegin(GL_TRIANGLES)
4635     for fID in teapotFace:
4636         glNormal3fv(teapotVertexNormal[fID[0]])
4637         glVertex3fv(teapotVertex[fID[0]])
4638         glNormal3fv(teapotVertexNormal[fID[1]])
4639         glVertex3fv(teapotVertex[fID[1]])
4640         glNormal3fv(teapotVertexNormal[fID[2]])
4641         glVertex3fv(teapotVertex[fID[2]])
4642     glEnd()
4643
```

```
4693 glEnable(GL_LIGHT0)
4694 glShadeModel(GL_SMOOTH)
4695 lightAmbient = [ 0.3,0.3,0.3,1.0 ]
4696 lightDiffuse = [ 0.7,0.7,0.7,1.0 ]
```



```
4693 glEnable(GL_LIGHT0)
4694 glShadeModel(GL_FLAT)
4695 lightAmbient = [ 0.3,0.3,0.3,1.0 ]
4696 lightDiffuse = [ 0.7,0.7,0.7,1.0 ]
```

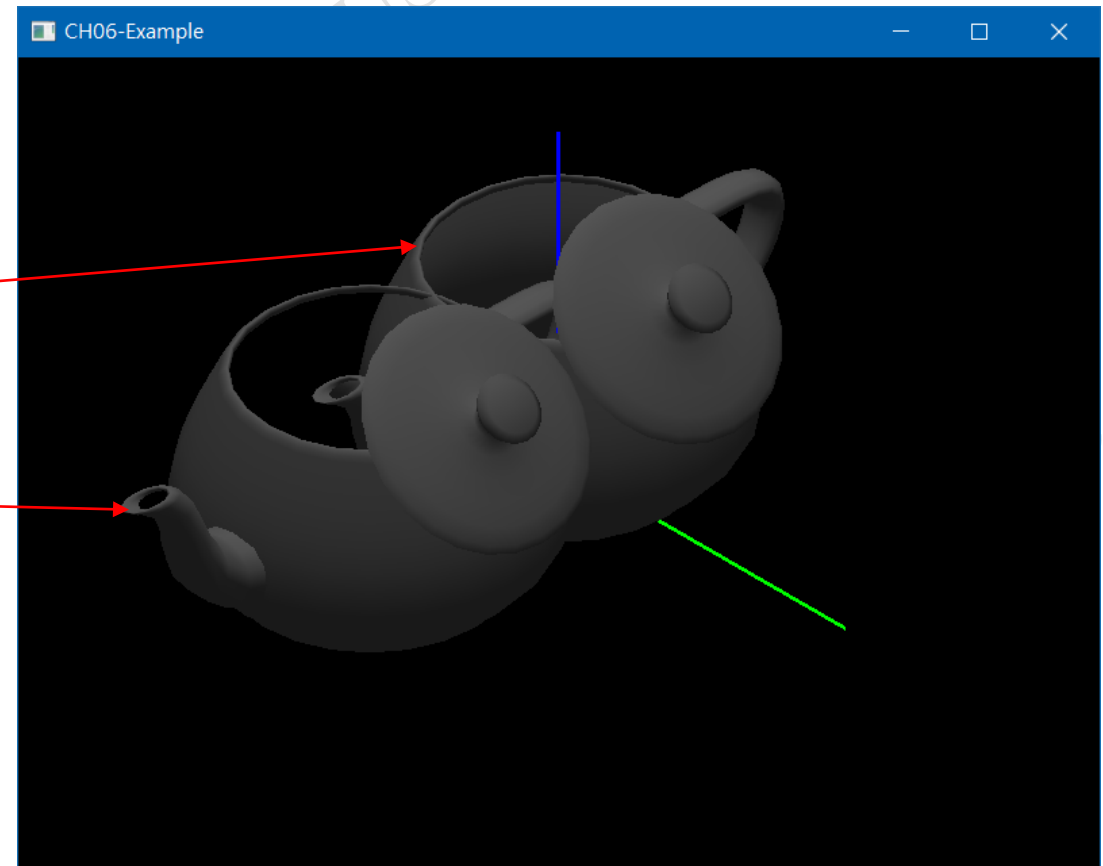




# Enable / Disable Cull Face

```

4667 glEnable(GL_LIGHTING)
4668 glPushMatrix()
4669 glDisable(GL_CULL_FACE)
4670 drawTeapot()
4671 glPopMatrix()
4672 glPushMatrix()
4673 glEnable(GL_CULL_FACE)
4674 glTranslatef(200,0,0)
4675 drawTeapot()
4676 glPopMatrix()
4677 glDisable(GL_LIGHTING)
4678 drawCoordinate()
4679 glutSwapBuffers()
    
```

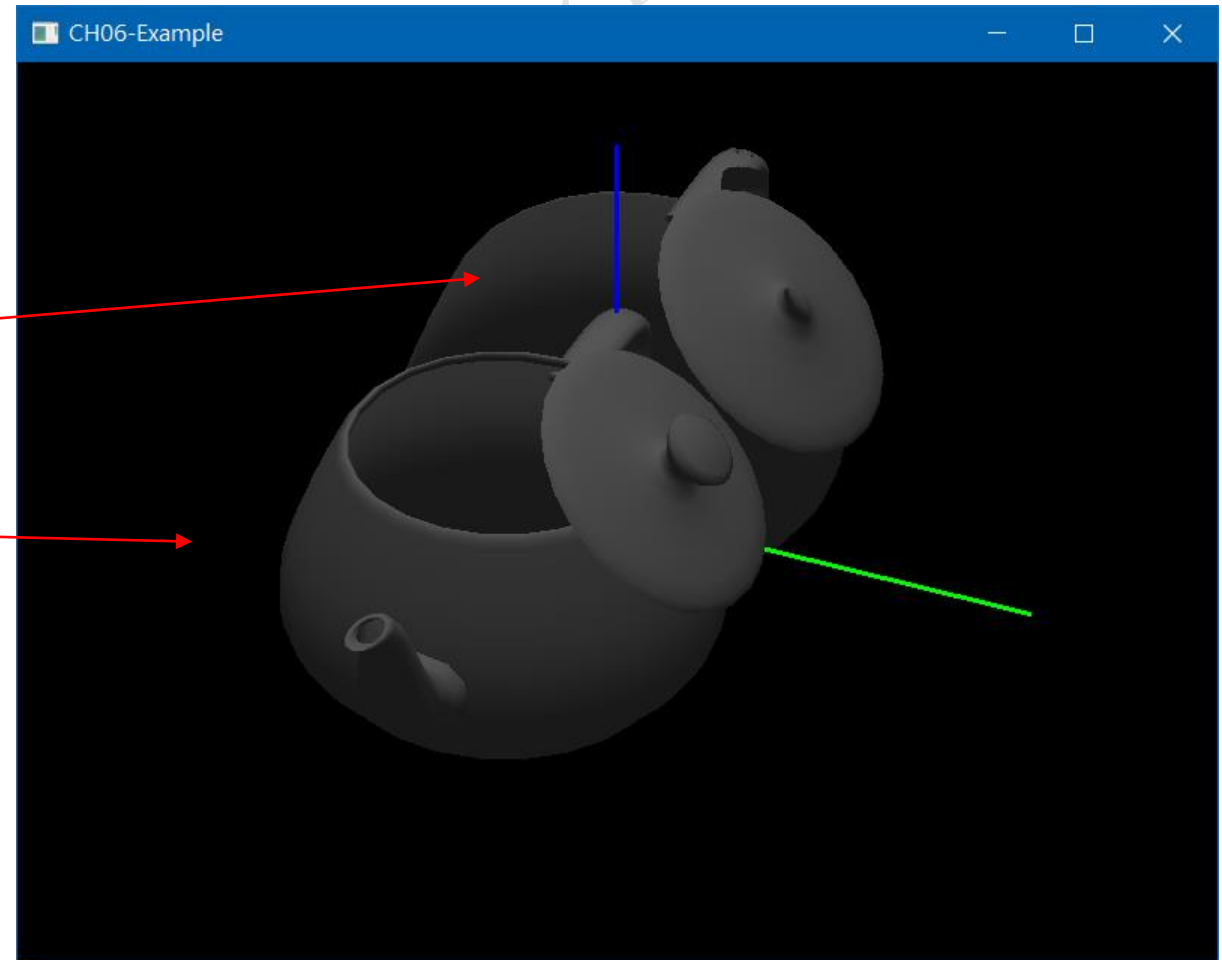




# Enable/Disable Depth\_Test

```

4668     glRotatef(angle,0,0,1)
4669     angle = angle+1
4670     glRotatef(angle,0,0,1)
4671     glPushMatrix()
4672     glDisable(GL_DEPTH_TEST)
4673     drawTeapot()
4674     glPopMatrix()
4675     glPushMatrix()
4676     glEnable(GL_DEPTH_TEST)
4677     glTranslatef(200,0,0)
4678     drawTeapot()
4679     glPopMatrix()
4680     glDisable(GL_LIGHTING)
4681     drawCoordinate()
4682     glutSwapBuffers()
    
```







# gluLookAt vs Coordinate Transformation

## ■ gluLookAt

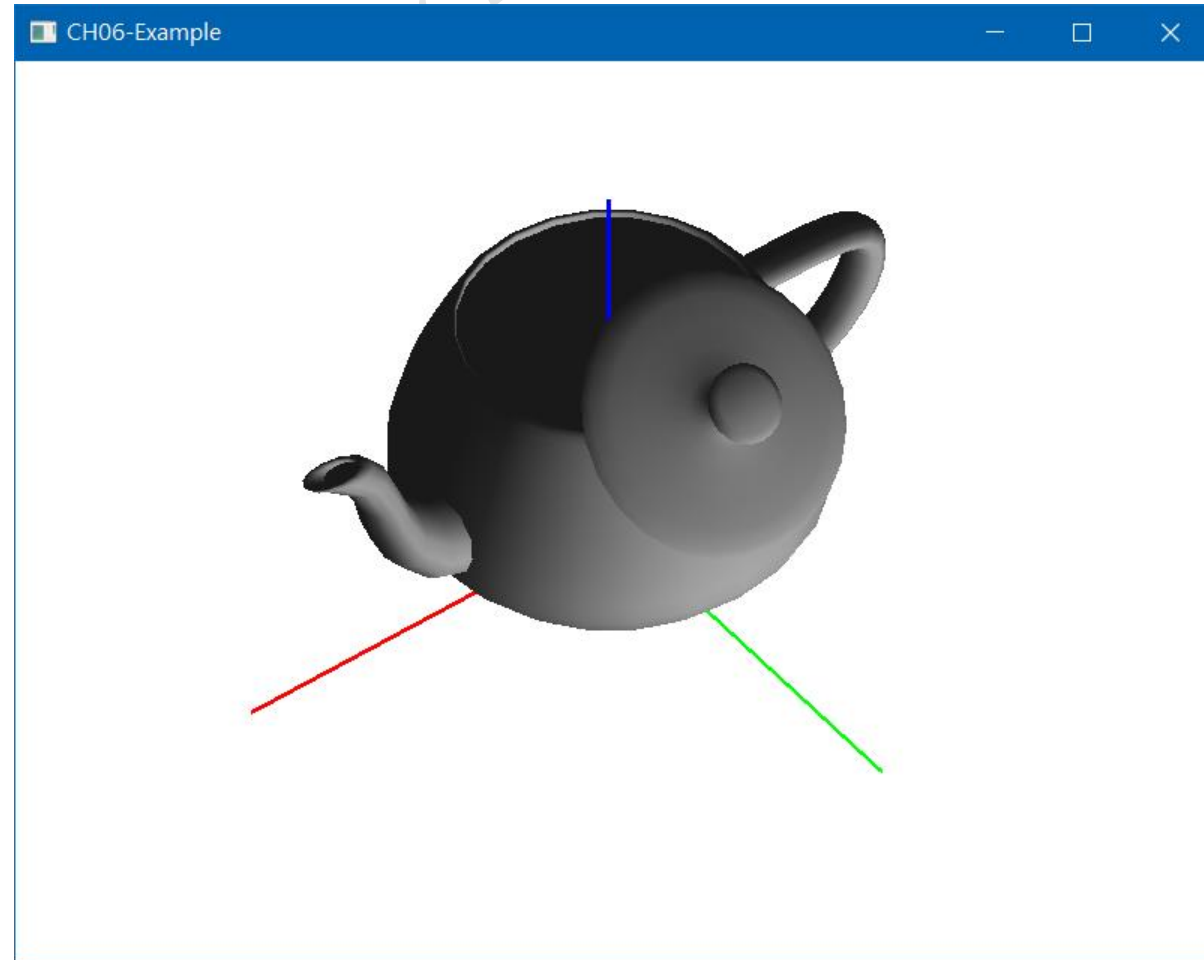
Look At

(300,400,500

10,20,30

0,0,1)

```
4660 def display():
4661     glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
4662     glMatrixMode(GL_PROJECTION)
4663     glLoadIdentity()
4664     glViewport(0, 0, windowWidth, windowHeight)
4665     glOrtho(-float(windowWidth)/2.0,float(windowWidth)/2.0,
4666             float(windowHeight)/2.0,-windowHeight*10.0,windowHeight*10.0)
4667     gluLookAt(300,400,500,10,20,30,0,0,1)
4668     glEnable(GL_LIGHTING)
4669     glPushMatrix()
4670     drawTeapot()
4671     glPopMatrix()
4672     glDisable(GL_LIGHTING)
4673     drawCoordinate()
4674     glutSwapBuffers()
```





# gluLookAt vs Coordinate Transformation

## ■ Coordinate Transformation

Here,

- E: eye (or camera) position
- A: reference point, where eye looks at
- U: direction of up vector

### gluLookAt

The **gluLookAt** function defines a viewing transformation.

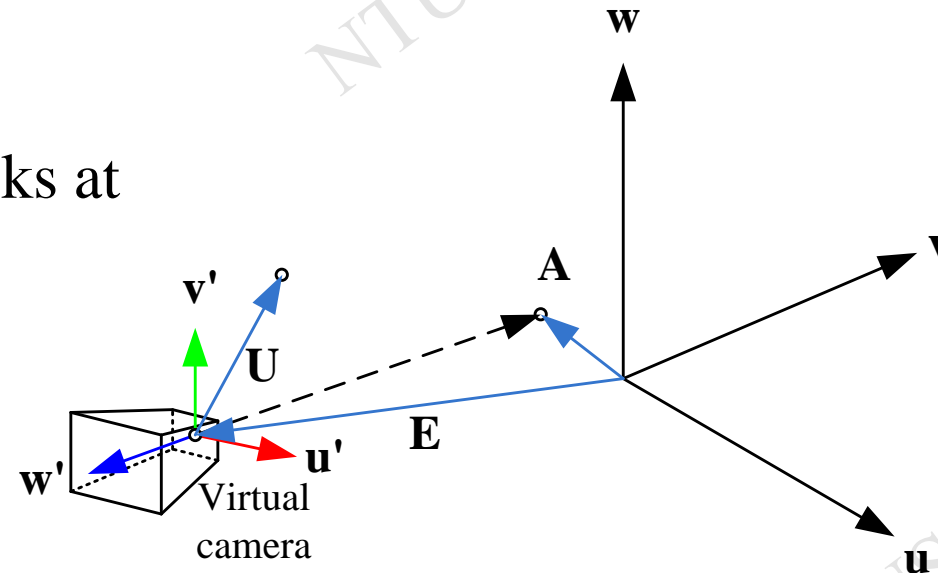
```
void gluLookAt(  
    GLdouble eyex,  
    GLdouble eyey,  
    GLdouble eyez,  
    GLdouble centerx,  
    GLdouble centery,  
    GLdouble centerz,  
    GLdouble upx,  
    GLdouble upy,  
    GLdouble upz  
);
```

#### Parameters

*eyex, eyey, eyez*  
The position of the eye point.

*centerx, centery, centerz*  
The position of the reference point.

*upx, upy, upz*  
The direction of the up vector.





# gluLookAt vs Coordinate Transformation

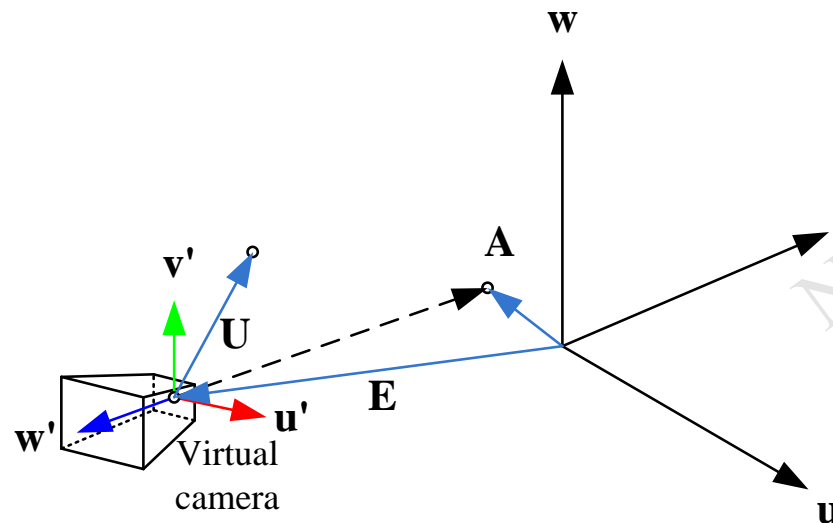
- To determine the camera transformation matrix
- Step-1: find  $\mathbf{w}'$  from  $(\mathbf{E}-\mathbf{A})$ .
- Step-2:  $\mathbf{u}'$  from cross product of  $\mathbf{U}$  and  $\mathbf{w}'$  (and convert into unit vector)
- Step-3:  $\mathbf{v}'$  from cross product of  $\mathbf{w}'$  and  $\mathbf{u}'$ .

$$\begin{bmatrix} u_x' & v_x' & w_x' & E_x \\ u_y' & v_y' & w_y' & E_y \\ u_z' & v_z' & w_z' & E_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{w}' = \text{Normalize}(\mathbf{E} - \mathbf{A})$$

$$\mathbf{u}' = \text{Normalize}(\mathbf{U} \times \mathbf{w}')$$

$$\mathbf{v}' = \mathbf{w}' \times \mathbf{u}'$$

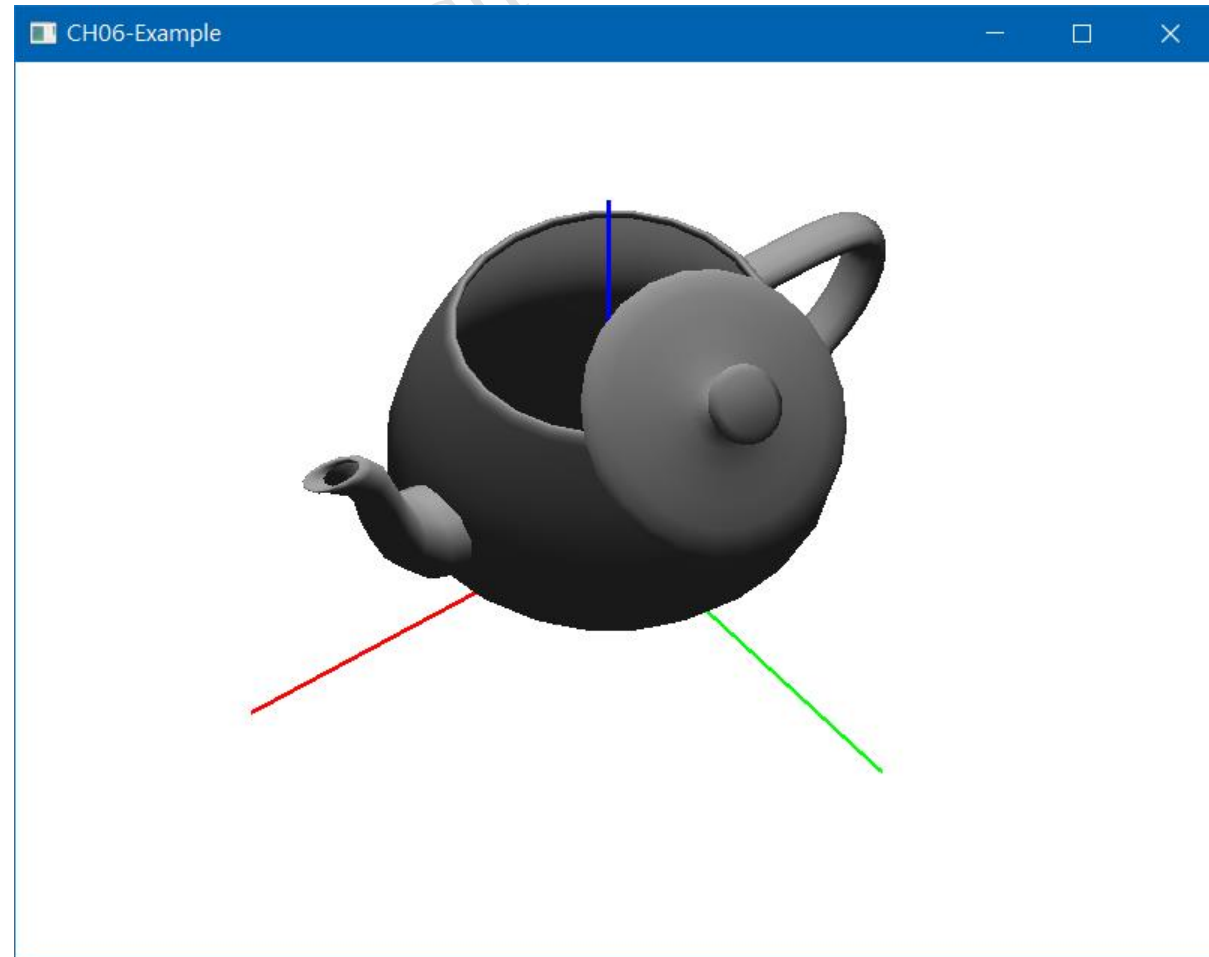




# gluLookAt vs Coordinate Transformation

```

4665     glOrtho(-float(windowWidth)/2.0,float(windowWidth)/2.0,-float(windowHeight)/2.0,float(windowHeight)/
windowHeight*10.0,windowHeight*10.0)
4666     glMatrixMode(GL_MODELVIEW)
4667     w = np.array([300,400,500])-np.array([10,20,30])
4668     w = w / np.linalg.norm(w)
4669     U = np.array([0,0,1])
4670     u = np.cross(U,w)
4671     u = u / np.linalg.norm(u)
4672     v = np.cross(w,u)
4673     M = [ [u[0], v[0], w[0], 300],[ u[1], v[1], w[1], 400], [u[2], v[2], w[2], 500], [0., 0., 0., 1.] ]
4674     Minv = np.linalg.inv(M)
4675     MinvT = np.transpose(Minv)
4676     matmatList = [MinvT[i][j] for i in range(4) for j in range(4)]
4677     glLoadMatrixf(matmatList)
4678     glEnable(GL_LIGHTING)
4679     glPushMatrix()
4680     drawTeapot()
4681     glPopMatrix()
4682     glDisable(GL_LIGHTING)
4683     drawCoordinate()
4684     glutSwapBuffers()
    
```



Note: light position is different

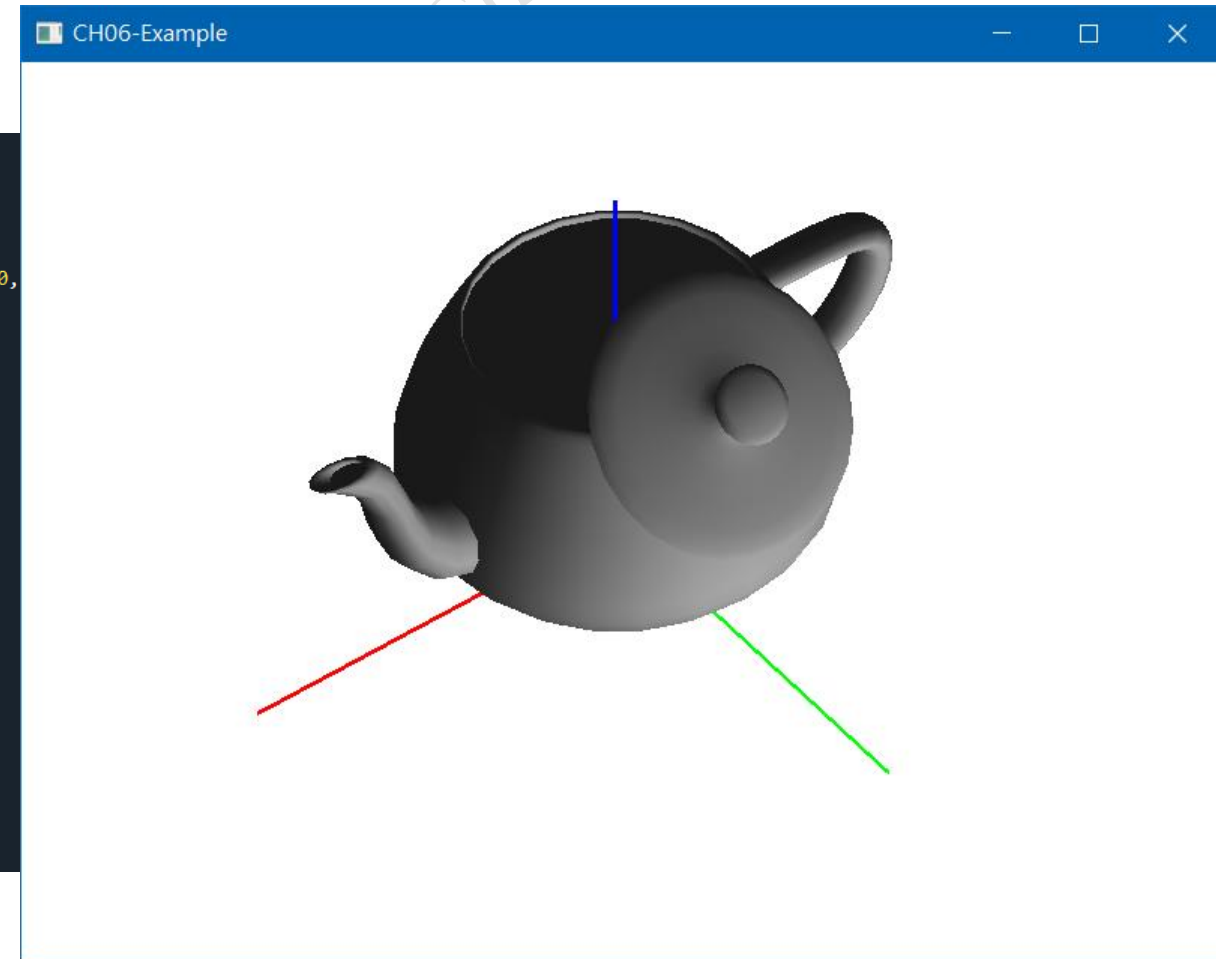


# gluLookAt vs Coordinate Transformation

```

4658 def display():
4659     glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
4660     glMatrixMode(GL_PROJECTION)
4661     glLoadIdentity()
4662     glViewport(0, 0, windowWidth, windowHeight)
4663     glOrtho(-float(windowWidth)/2.0,float(windowWidth)/2.0,-float(windowHeight)/2.0,float(windowHeight)/2.0,
windowHeight*10.0,windowHeight*10.0)
4664     glMatrixMode(GL_MODELVIEW)
4665     w = np.array([300,400,500])-np.array([10,20,30])
4666     w = w / np.linalg.norm(w)
4667     U = np.array([0,0,1])
4668     u = np.cross(U,w)
4669     u = u / np.linalg.norm(u)
4670     v = np.cross(w,u)
4671     M = [ [u[0], v[0], w[0], 300],[ u[1], v[1], w[1], 400], [u[2], v[2], w[2], 500], [0., 0., 0., 1.] ]
4672     Minv = np.linalg.inv(M)
4673     MinvT = np.transpose(Minv)
4674     matmatList = [MinvT[i][j] for i in range(4) for j in range(4)]
4675     glLoadMatrixf(matmatList)
4676     lightPosition = [ 0.0,1000.0,0.0,1.0 ]
4677     glLightfv(GL_LIGHT0, GL_POSITION, lightPosition)
4678     glEnable(GL_LIGHTING)
4679     glPushMatrix()
4680     drawTeapot()
4681     glPopMatrix()
4682     glDisable(GL_LIGHTING)
4683     drawCoordinate()
4684     glutSwapBuffers()
4685

```



Note: light position



LookAt

(300,400,500  
10,20,30  
0,0,1)

$$\mathbf{p}' = \begin{bmatrix} u_x' & v_x' & w_x' & E_x \\ u_y' & v_y' & w_y' & E_y \\ u_z' & v_z' & w_z' & E_z \\ 0 & 0 & 0 & 1 \end{bmatrix}^{-1} \mathbf{p}$$

$$\mathbf{w}' = \text{Normalize}(\mathbf{E} - \mathbf{A})$$

$$\mathbf{u}' = \text{Normalize}(\mathbf{U} \times \mathbf{w}')$$

$$\mathbf{v}' = \mathbf{w}' \times \mathbf{u}'$$

Statement for Matrix operation

$$\begin{aligned} \mathbf{w}' &= \text{normalize}(300-10, 400-20, 500-30) \\ &= (0.4325950, 0.5668486, 0.7011022) \end{aligned}$$

$$\begin{aligned} \mathbf{u}' &= (0,0,1) \times (0.4325950, 0.5668486, 0.7011022) \\ &= \dots = (-0.7949512, 0.6066733, 0) \rightarrow \text{normalized} \end{aligned}$$

$$\mathbf{v}' = (-0.42534, -0.5573420, 0.713061)$$

$$\begin{bmatrix} -0.7949512 & -0.4253400 & 0.4325950 & 300. \\ 0.6066733 & -0.5573420 & 0.5668486 & 400. \\ 0. & 0.7130608 & 0.7011022 & 500. \\ 0. & 0. & 0. & 1. \end{bmatrix}$$

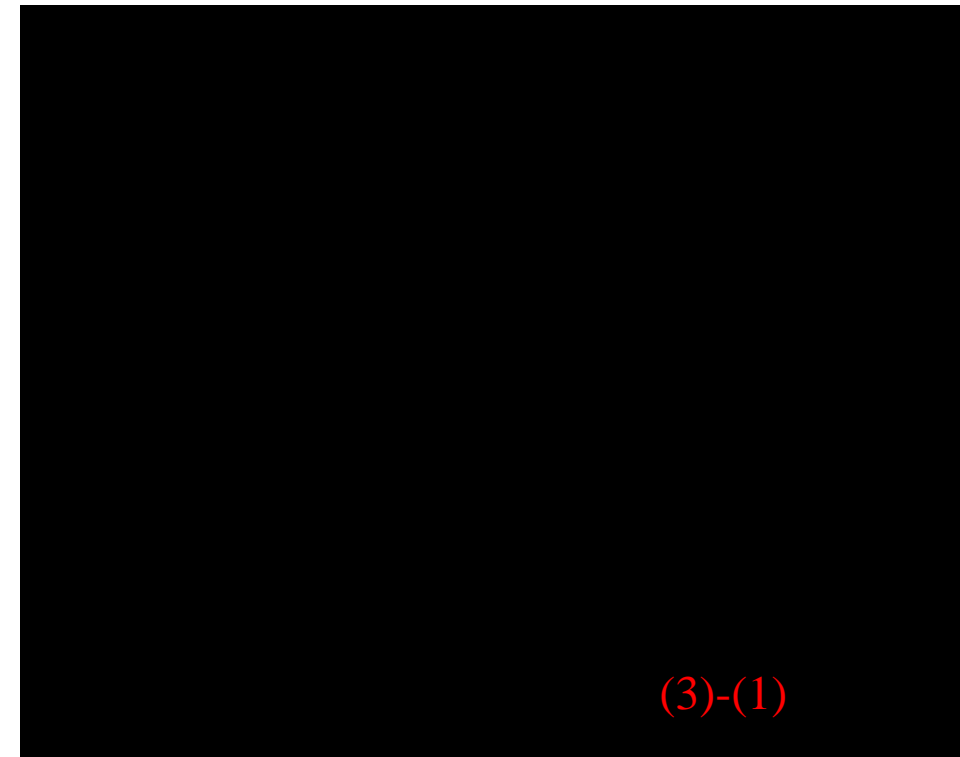
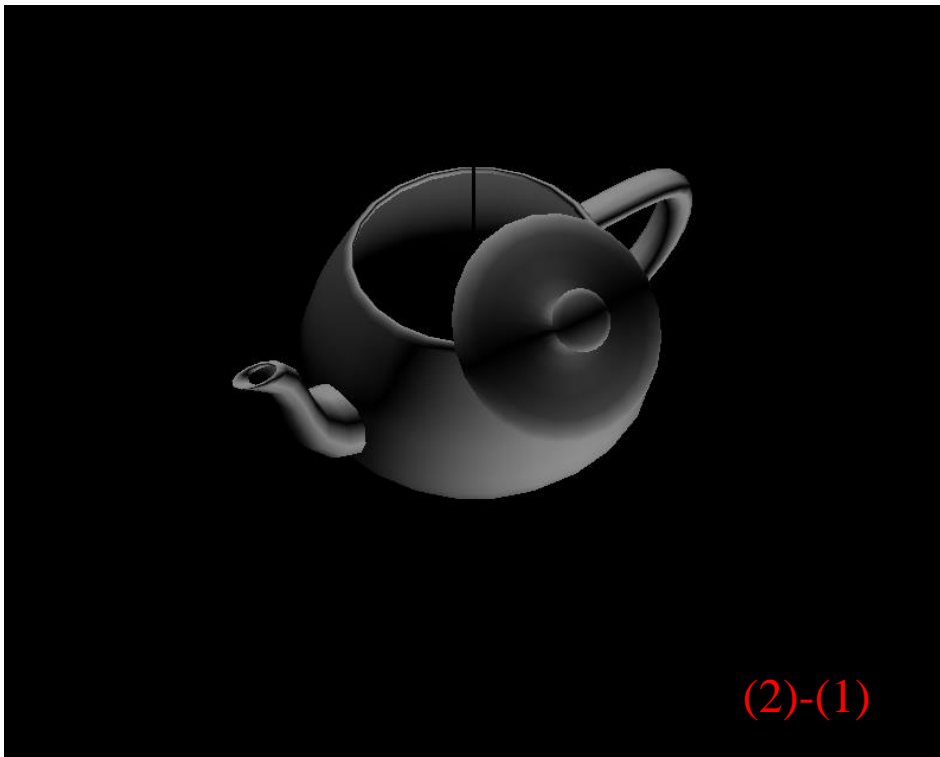
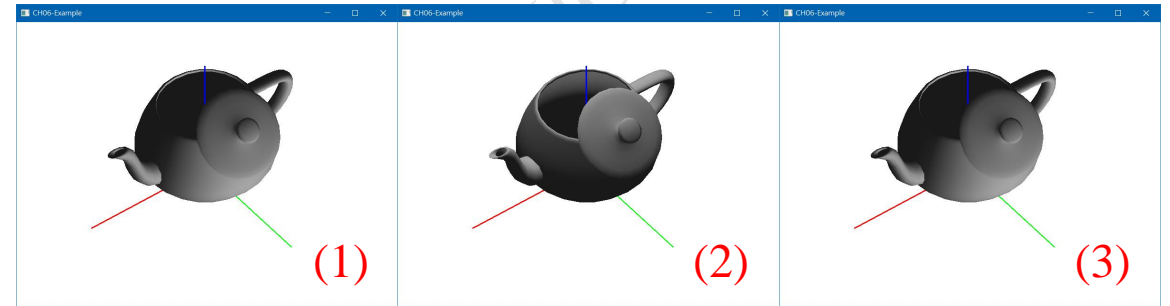
inverse

$$\begin{bmatrix} -0.7949513 & 0.6066734 & -6.275\text{D-}09 & -4.1839541 \\ -0.4253400 & -0.5573421 & 0.7130608 & -5.9915833 \\ 0.4325950 & 0.5668486 & 0.7011022 & -707.06902 \\ 0. & 0. & 0. & 1. \end{bmatrix}$$



# gluLookAt vs Coordinate Transformation

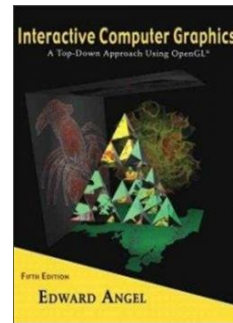
## ■ Difference between images





# glOrtho vs Projection Matrix

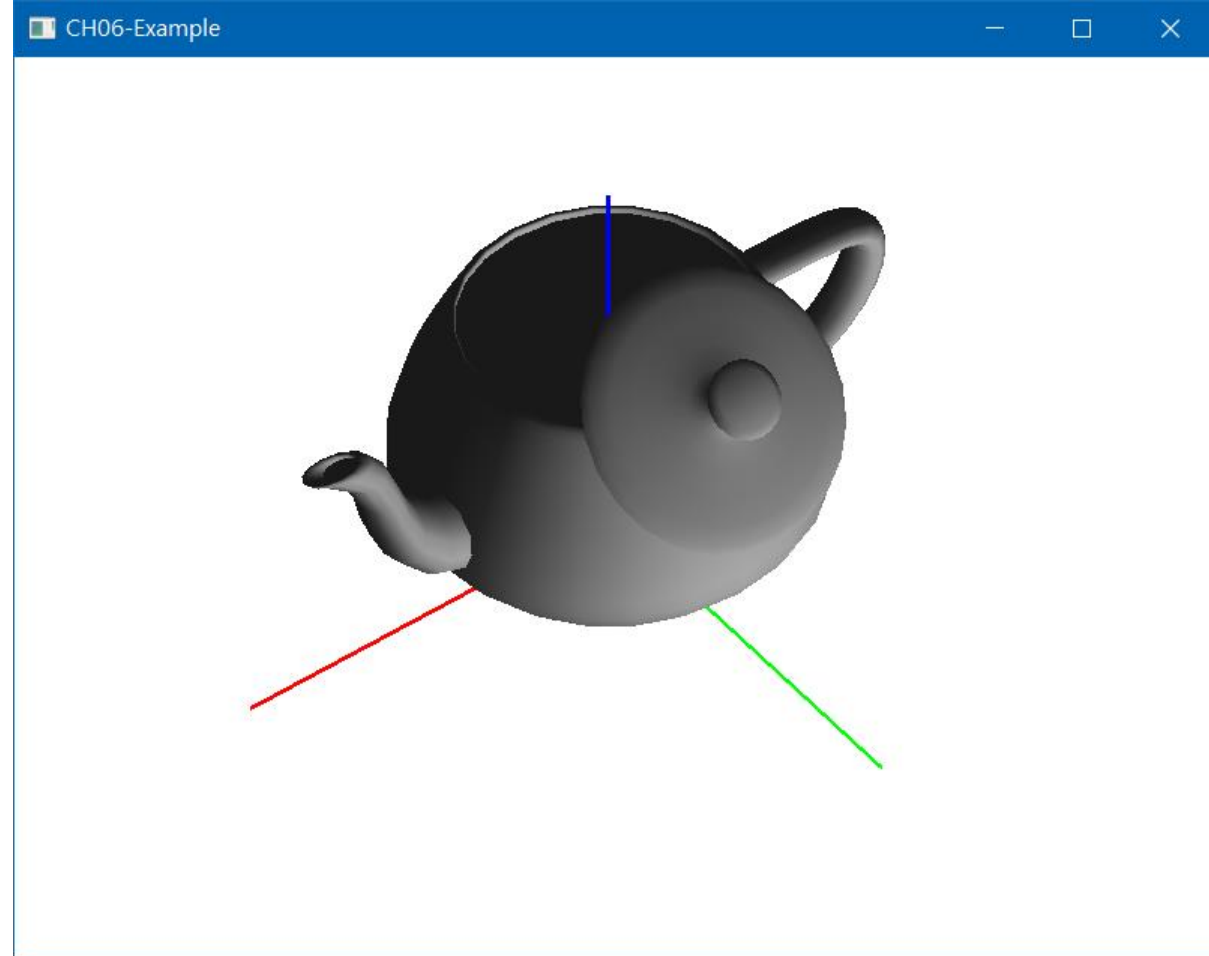
$$P = ST = \begin{bmatrix} \frac{2}{right-left} & 0 & 0 & -\frac{left+right}{right-left} \\ 0 & \frac{2}{top-bottom} & 0 & -\frac{top+bottom}{top-bottom} \\ 0 & 0 & -\frac{2}{far-near} & -\frac{far+near}{far-near} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



```

4659 def display():
4660     glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
4661     glMatrixMode(GL_PROJECTION)
4662     glLoadIdentity()
4663     glViewport(0, 0, windowWidth, windowHeight)
4664     #glOrtho(-float(windowWidth)/2.0,float(windowWidth)/2.0,-float(windowHeight)/2.0,float(windowHeight)/2.0,-
windowHeight*10.0,windowHeight*10.0)
4665
4666     Mortho = [ [ 2./windowWidth, 0.0, 0.0, -0.0/windowWidth],[ 0.0, 2./windowHeight, 0.0, -0.0/windowHeight],
[ 0.0, 0.0, -2.0/(20*windowHeight), -0.0/(20*windowHeight)], [0., 0., 0., 1.] ]
4667     MorthoT = np.transpose(Mortho)
4668     matmatList = [Mortho[i][j] for i in range(4) for j in range(4)]
4669     glLoadMatrixf(matmatList)
4670
4671     gluLookAt(300,400,500,10,20,30,0,0,1)
4672     glEnable(GL_LIGHTING)
4673     glPushMatrix()
4674     drawTeapot()
4675     glPopMatrix()
4676     glDisable(GL_LIGHTING)
4677     drawCoordinate()
4678     glutSwapBuffers()
4679

```



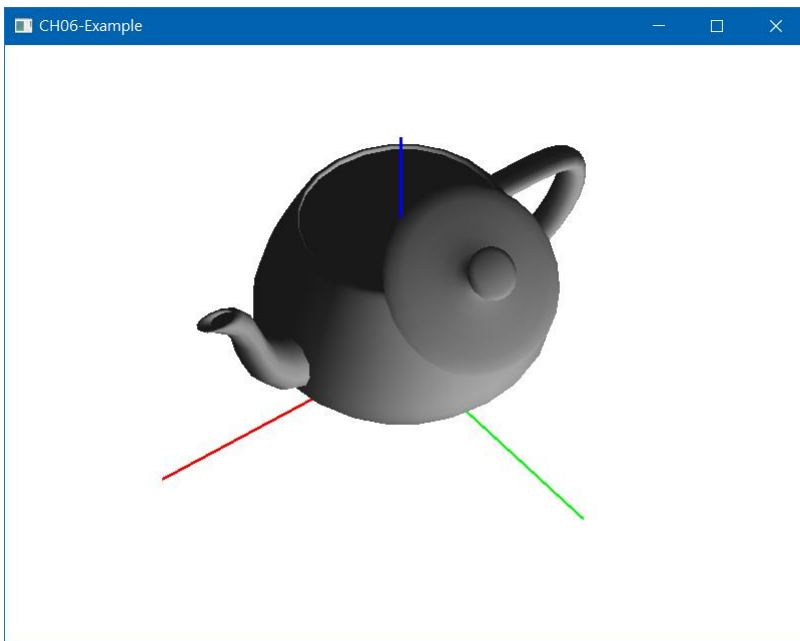




# glOrtho vs Projection Matrix

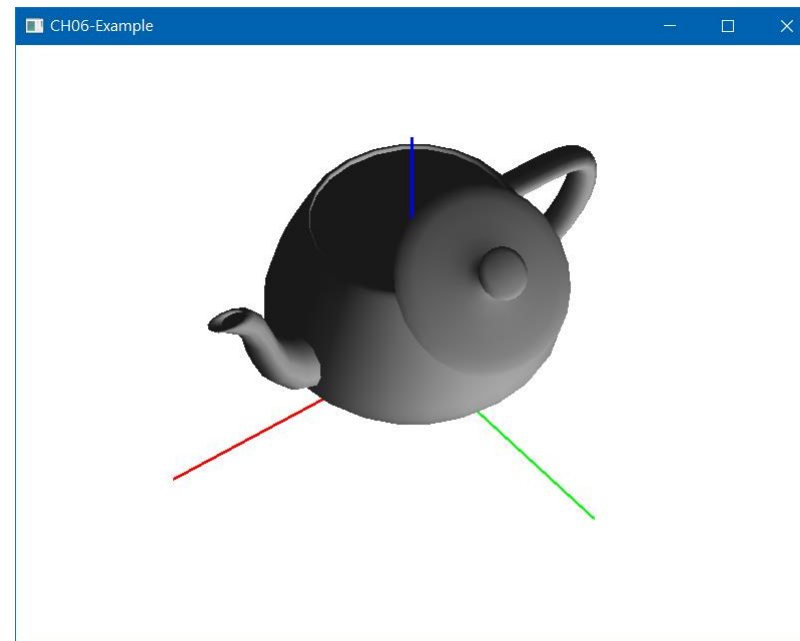
```

4659 def display():
4660     glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
4661     glMatrixMode(GL_PROJECTION)
4662     glLoadIdentity()
4663     glViewport(0, 0, windowWidth, windowHeight)
4664     glOrtho(-float(windowWidth)/2.0, float(windowWidth)/2.0, -float(windowHeight)/2.0, float(windowHeight)/2.0, -
        windowHeight*10.0, windowHeight*10.0)
4665     ...
4666     Mortho = [ [ 2./windowWidth, 0.0, 0.0, -0.0/windowWidth], [ 0.0, 2./windowHeight, 0.0, -0.0/windowHeight],
        [ 0.0, 0.0, -2.0/(20*windowHeight), -0.0/(20*windowHeight)], [ 0., 0., 0., 1. ] ]
4667     MorthoT = np.transpose(Mortho)
4668     matmatList = [Mortho[i][j] for i in range(4) for j in range(4)]
4669     glLoadMatrixf(matmatList)
4670     ...
4671
4672     gluLookAt(300,400,500,10,20,30,0,0,1)
4673     glEnable(GL_LIGHTING)
4674     glPushMatrix()
4675     drawTeapot()
4676     glPopMatrix()
4677     glDisable(GL_LIGHTING)
4678     drawCoordinate()
4679     glutSwapBuffers()
    
```



```

4659 def display():
4660     glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
4661     glMatrixMode(GL_PROJECTION)
4662     glLoadIdentity()
4663     glViewport(0, 0, windowWidth, windowHeight)
4664     #glOrtho(-float(windowWidth)/2.0, float(windowWidth)/2.0, -float(windowHeight)/2.0, float(windowHeight)/2.0, -
        windowHeight*10.0, windowHeight*10.0)
4665     ...
4666     Mortho = [ [ 2./windowWidth, 0.0, 0.0, -0.0/windowWidth], [ 0.0, 2./windowHeight, 0.0, -0.0/windowHeight],
        [ 0.0, 0.0, -2.0/(20*windowHeight), -0.0/(20*windowHeight)], [ 0., 0., 0., 1. ] ]
4667     MorthoT = np.transpose(Mortho)
4668     matmatList = [Mortho[i][j] for i in range(4) for j in range(4)]
4669     glLoadMatrixf(matmatList)
4670     ...
4671
4672     gluLookAt(300,400,500,10,20,30,0,0,1)
4673     glEnable(GL_LIGHTING)
4674     glPushMatrix()
4675     drawTeapot()
4676     glPopMatrix()
4677     glDisable(GL_LIGHTING)
4678     drawCoordinate()
4679     glutSwapBuffers()
    
```





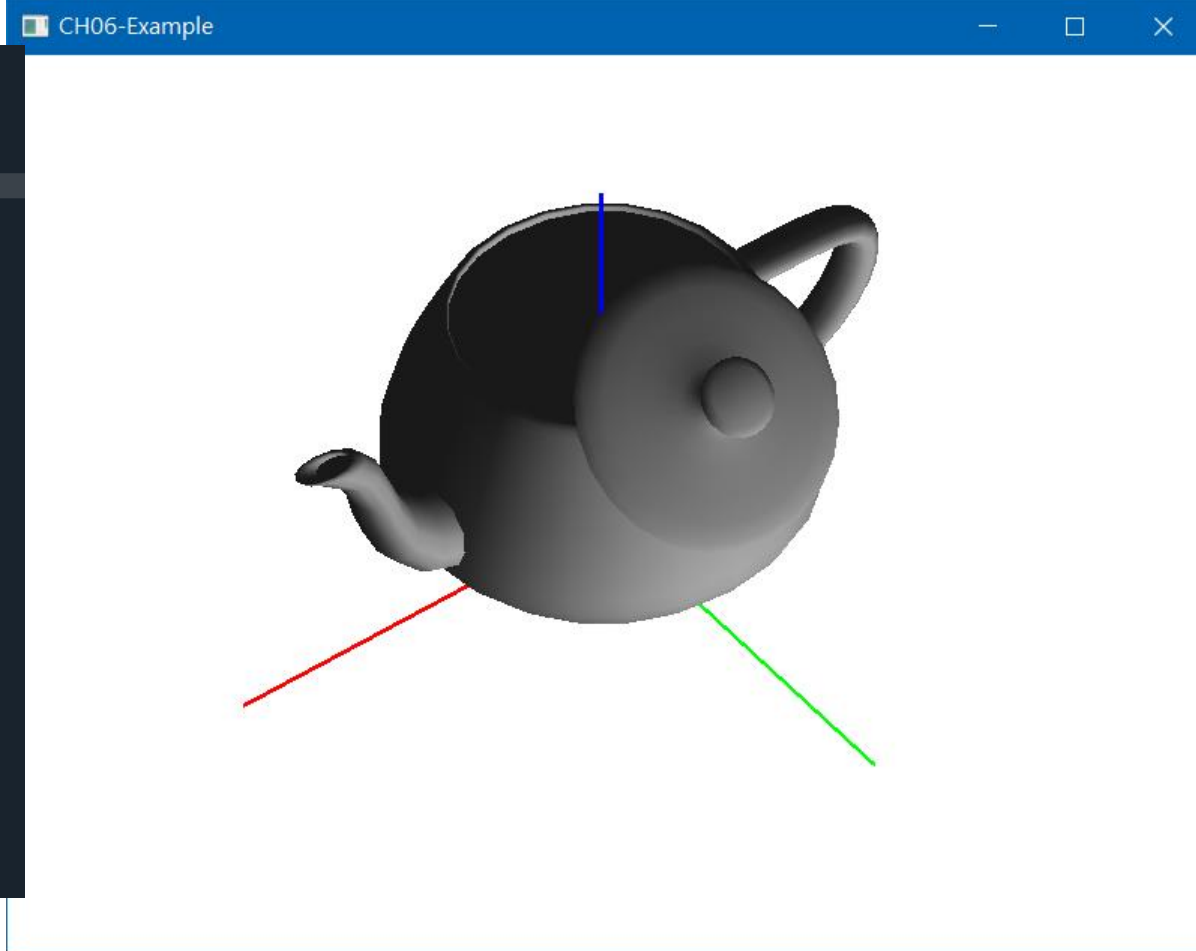
# glOrtho vs Projection Matrix (more complex form)

- All using glLoadMatrixf instead of glOrtho and glLookAt

```

4659 def display():
4660     glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
4661     glMatrixMode(GL_PROJECTION)
4662     glLoadIdentity()
4663     glViewport(0, 0, windowWidth, windowHeight)
4664
4665     Mortho = [ [ 2./windowWidth, 0.0, 0.0, -0.0/windowWidth],[ 0.0, 2./windowHeight, 0.0, -0.0/windowHeight],
4666 [ 0.0, 0.0, -2.0/(20*windowHeight), -0.0/(20*windowHeight)], [0., 0., 0., 1.] ]
4667     MorthoT = np.transpose(Mortho)
4668     matmatList = [Mortho[i][j] for i in range(4) for j in range(4)]
4669     glLoadMatrixf(matmatList)
4670
4671     glMatrixMode(GL_MODELVIEW)
4672     w = np.array([300,400,500])-np.array([10,20,30])
4673     w = w / np.linalg.norm(w)
4674     U = np.array([0,0,1])
4675     u = np.cross(U,w)
4676     u = u / np.linalg.norm(u)
4677     v = np.cross(w,u)
4678     M = [ [u[0], v[0], w[0], 300],[ u[1], v[1], w[1], 400], [u[2], v[2], w[2], 500], [0., 0., 0., 1.] ]
4679     Minv = np.linalg.inv(M)
4680     MinvT = np.transpose(Minv)
4681     matmatList = [MinvT[i][j] for i in range(4) for j in range(4)]
4682     glLoadMatrixf(matmatList)
4683     lightPosition = [ 0.0,1000.0,0.0,1.0 ]
4684     glLightfv(GL_LIGHT0, GL_POSITION, lightPosition)
4685     glEnable(GL_LIGHTING)
4686     glPushMatrix()
4687     drawTeapot()
4688     glPopMatrix()
4689     glDisable(GL_LIGHTING)
4690     drawCoordinate()
4691     glutSwapBuffers()

```



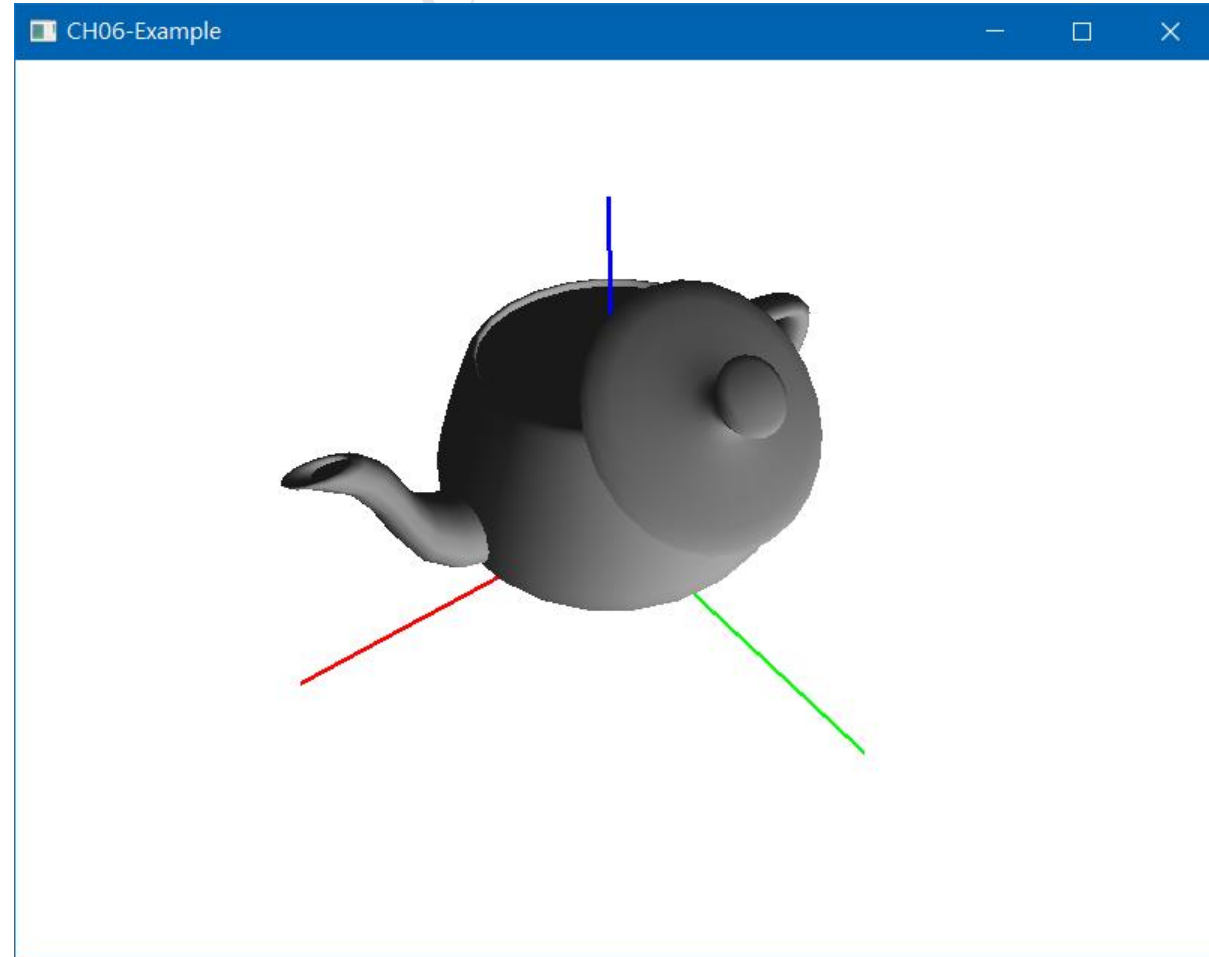


# glFrustum vs Projection Matrix

## ■ by glFrustum

`glFrustum(-800/1000.0, 800/1000.0,  
- 600/1000.0, 600/1000.0, 1.0, 5000)`

```
4659 def display():
4660     glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
4661     glMatrixMode(GL_PROJECTION)
4662     glLoadIdentity()
4663     glViewport(0, 0, windowWidth, windowHeight)
4664     glFrustum(-800/1000.0, 800/1000.0, - 600/1000.0, 600/1000.0, 1.0, 5000);
4665
4666     gluLookAt(300,400,500,10,20,30,0,0,1)
4667     glEnable(GL_LIGHTING)
4668     glPushMatrix()
4669     drawTeapot()
4670     glPopMatrix()
4671     glDisable(GL_LIGHTING)
4672     drawCoordinate()
4673     glutSwapBuffers()
4674
```





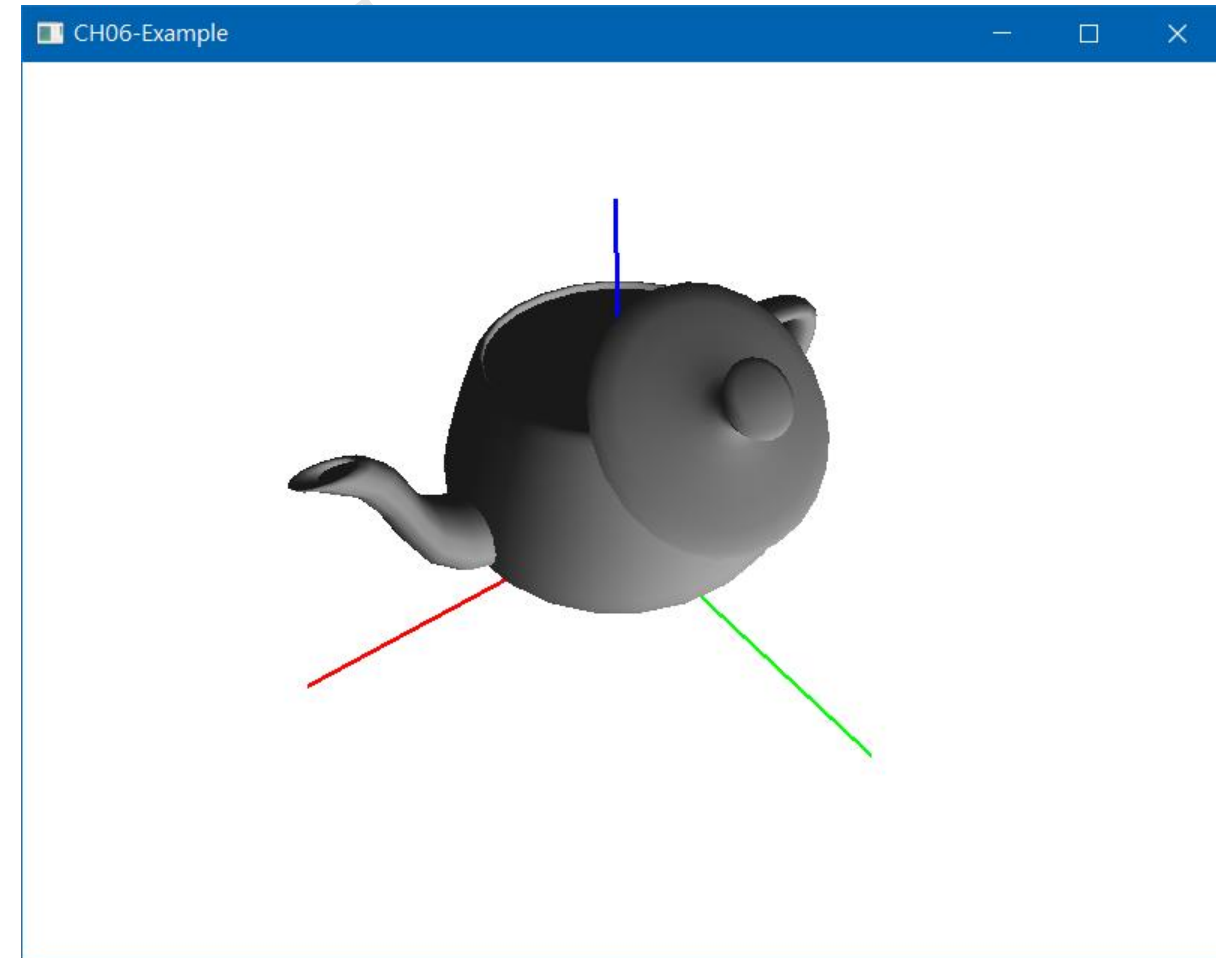
# glFrustum vs Projection Matrix

## ■ by Projection matrix

```

4659 def display():
4660     glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
4661     glMatrixMode(GL_PROJECTION)
4662     glLoadIdentity()
4663     glViewport(0, 0, windowWidth, windowHeight)
4664
4665     Mfrustum = [ [ 2./(0.8+0.8), 0.0, 0.0, 0.0],[ 0.0, 2./(0.6+0.6), 0.0, 0.0],
4666     [ 0.0, 0.0, -(5000+1.0)/(5000-1.0), -2.0*1.0*5000./(5000-1.0)], [0., 0., -1.0,
4667     0.0] ]
4668     MfrustumT = np.transpose(Mfrustum)
4669     matmatList = [MfrustumT[i][j] for i in range(4) for j in range(4)]
4670     glLoadMatrixf(matmatList)
4671
4672     gluLookAt(300,400,500,10,20,30,0,0,1)
4673     glEnable(GL_LIGHTING)
4674     glPushMatrix()
4675     drawTeapot()
4676     glPopMatrix()
4677     glDisable(GL_LIGHTING)
4678     drawCoordinate()
4679     glutSwapBuffers()
4680

```





## glFrustum

The **glFrustum** function multiplies the current matrix by a perspective matrix.

```
void glFrustum(
    GLdouble left,
    GLdouble right,
    GLdouble bottom,
    GLdouble top,
    GLdouble znear,
    GLdouble zfar
);
```

### Parameters

*left, right*  
The coordinates for the left and right vertical clipping planes.

*bottom, top*  
The coordinates for the bottom and top horizontal clipping planes.

*znear, zfar*  
The distances to the near and far depth clipping planes. Both distances must be positive.

### Remarks

The **glFrustum** function describes a perspective matrix that produces a perspective projection. The (*left, bottom, znear*) and (*right, top, znear*) parameters specify the points on the near clipping plane that are mapped to the lower-left and upper-right corners of the window, respectively, assuming that the eye is located at (0, 0, 0). The *zfar* parameter specifies the location of the far clipping plane. Both *znear* and *zfar* must be positive. The corresponding matrix is:

$$\begin{pmatrix} \frac{2 \text{ near}}{\text{right-left}} & 0 & A & 0 \\ 0 & \frac{2 \text{ near}}{\text{top-bottom}} & B & 0 \\ 0 & 0 & C & D \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

$$A = \frac{\text{right} + \text{left}}{\text{right} - \text{left}}$$

$$B = \frac{\text{top} + \text{bottom}}{\text{top} - \text{bottom}}$$

$$C = -\frac{\text{far} + \text{near}}{\text{far} - \text{near}}$$

$$D = -\frac{2 \text{ far near}}{\text{far} - \text{near}}$$

The **glFrustum** function multiplies the current matrix by this matrix, with the result replacing the current matrix. That is, if M is the current matrix and F is the frustum perspective matrix, then **glFrustum** replaces M with  $M \cdot F$ .

**glFrustum**(-800/1000.0, 800/1000.0, -600/1000.0,  
600/1000.0, 1.0, 5000)

near : 1

Far : 5000

left: -0.8

right: 0.8

top: 0.6

bottom: -0.6

Projection Matrix :

$$F = \begin{bmatrix} 2 \cdot 1 / (0.8 + 0.8) & 0 & (0.8 - 0.8) / (0.8 + 0.8) & 0 \\ 2 \cdot 1 / (0.6 + 0.6) & (0.6 - 0.6) / (0.6 + 0.6) & 0 & 0 \\ (5000 + 1) / (5000 - 1) & -2 \cdot 1 \cdot 5000 / (5000 - 1) & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$$

$$F = \begin{bmatrix} 1.25 & 0. & 0. & 0. \\ 0. & 1.67 & 0. & 0. \\ 0. & 0. & -1.0004 & -2.0004 \\ 0. & 0. & -1. & 0. \end{bmatrix}$$

$$F = \begin{bmatrix} 1.25 & 0. & 0. & 0. \\ 0. & 1.67 & 0. & 0. \\ 0. & 0. & -1.0004 & -2.0004 \\ 0. & 0. & -1. & 0. \end{bmatrix}$$

F =

$$\begin{bmatrix} 1.25 & 0. & 0. & 0. \\ 0. & 1.67 & 0. & 0. \\ 0. & 0. & -1.0004 & -2.0004 \\ 0. & 0. & -1. & 0. \end{bmatrix}$$

$$\begin{bmatrix} 0. & 1.67 & 0. & 0. \\ 0. & 0. & -1.0004 & -2.0004 \\ 0. & 0. & -1. & 0. \end{bmatrix}$$

$$\begin{bmatrix} 0. & 0. & -1.0004 & -2.0004 \\ 0. & 0. & -1. & 0. \end{bmatrix}$$

$$\begin{bmatrix} 0. & 0. & -1. & 0. \end{bmatrix}$$

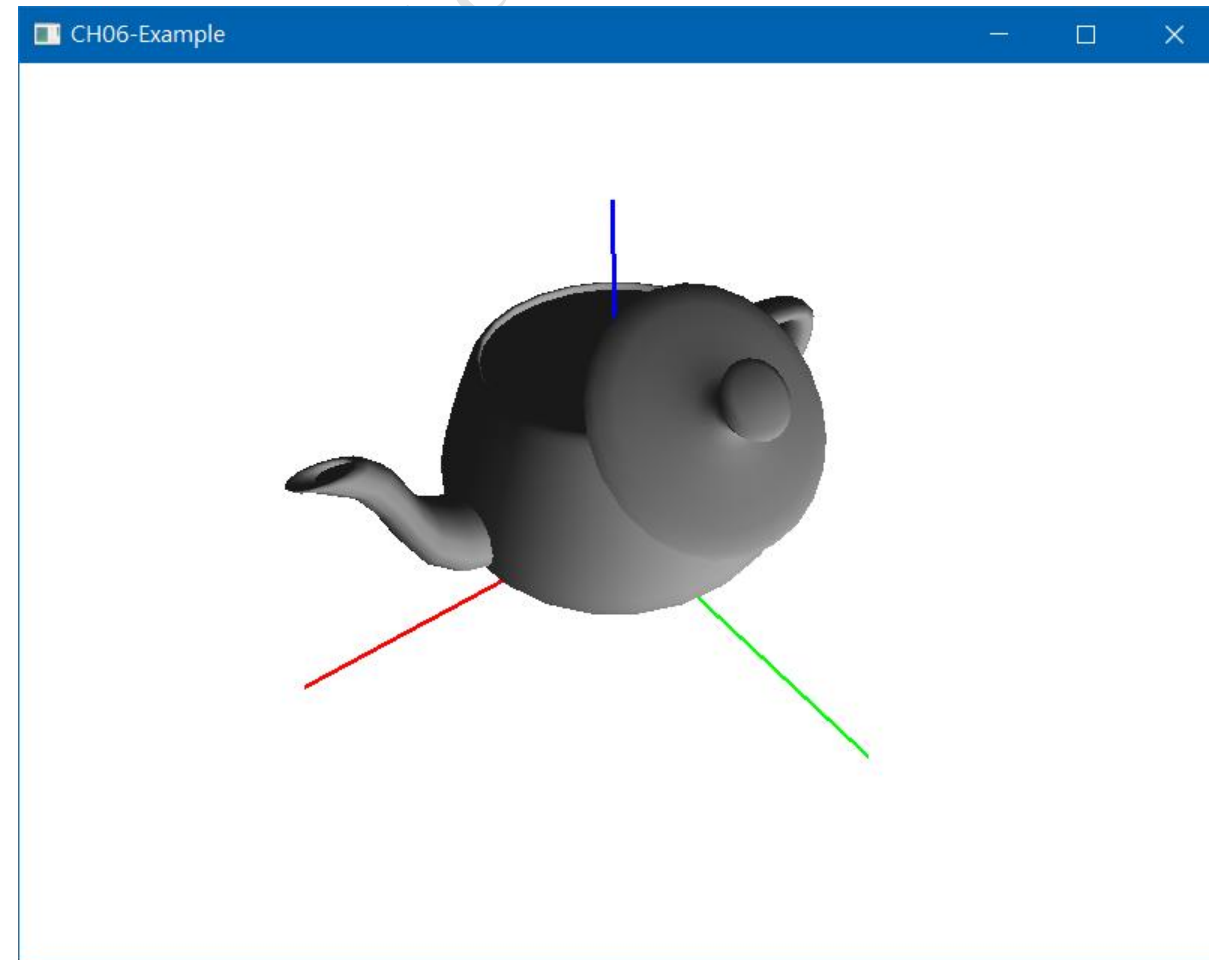


# glFrustum vs Projection Matrix

```

4659 def display():
4660     glClear(GL_COLOR_BUFFER_BIT|GL_DEPTH_BUFFER_BIT)
4661     glMatrixMode(GL_PROJECTION)
4662     glLoadIdentity()
4663     glViewport(0, 0, windowWidth, windowHeight)
4664
4665     Mfrustum = [ [ 2./(0.8+0.8), 0.0, 0.0, 0.0],[ 0.0, 2./(0.6+0.6), 0.0, 0.0],
4666     [ 0.0, 0.0, -(5000+1.0)/(5000-1.0), -2.0*1.0*5000./(5000-1.0)], [0., 0., -1.0,
4667     0.0] ]
4668     MfrustumT = np.transpose(Mfrustum)
4669     matmatList = [MfrustumT[i][j] for i in range(4) for j in range(4)]
4670     glLoadMatrixf(matmatList)
4671
4672     glMatrixMode(GL_MODELVIEW)
4673     w = np.array([300,400,500])-np.array([10,20,30])
4674     w = w / np.linalg.norm(w)
4675     U = np.array([0,0,1])
4676     u = np.cross(U,w)
4677     u = u / np.linalg.norm(u)
4678     v = np.cross(w,u)
4679     M = [ [u[0], v[0], w[0], 300],[ u[1], v[1], w[1], 400], [u[2], v[2], w[2],
4680     500], [0., 0., 0., 1.] ]
4681     Minv = np.linalg.inv(M)
4682     MinvT = np.transpose(Minv)
4683     matmatList = [MinvT[i][j] for i in range(4) for j in range(4)]
4684     glLoadMatrixf(matmatList)
4685     lightPosition = [ 0.0,1000.0,0.0,1.0 ]
4686     glLightfv(GL_LIGHT0, GL_POSITION, lightPosition)
4687
4688     glEnable(GL_LIGHTING)
4689     glPushMatrix()
4690     drawTeapot()
4691     glPopMatrix()
4692     glDisable(GL_LIGHTING)
4693     drawCoordinate()
4694     glutSwapBuffers()
4695

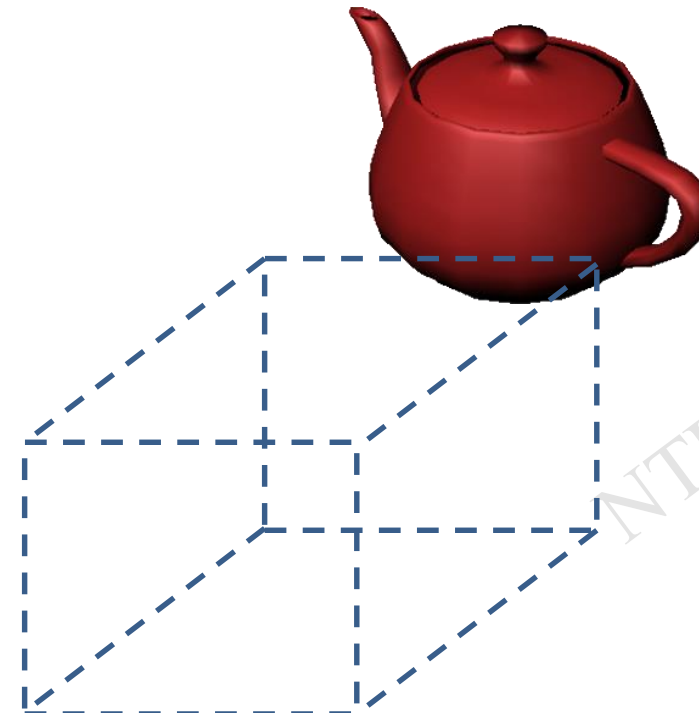
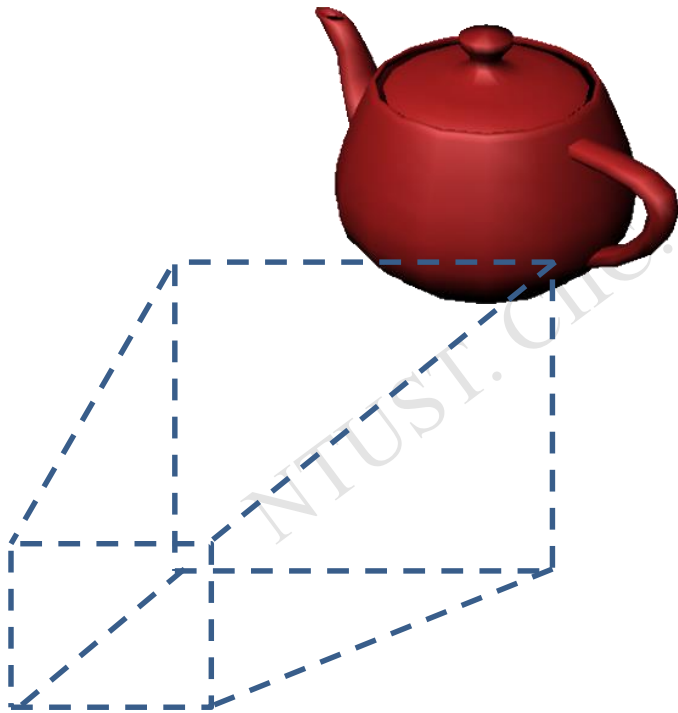
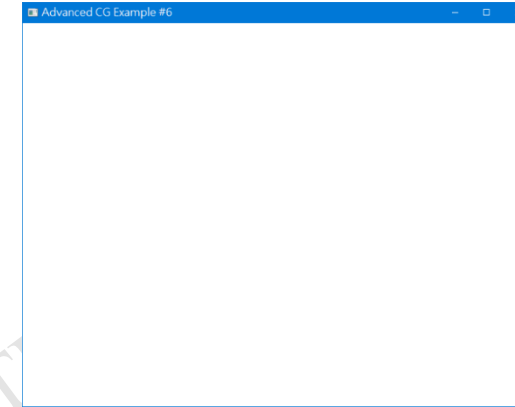
```





## Other issue: See nothing

- Object is not inside the viewing volume



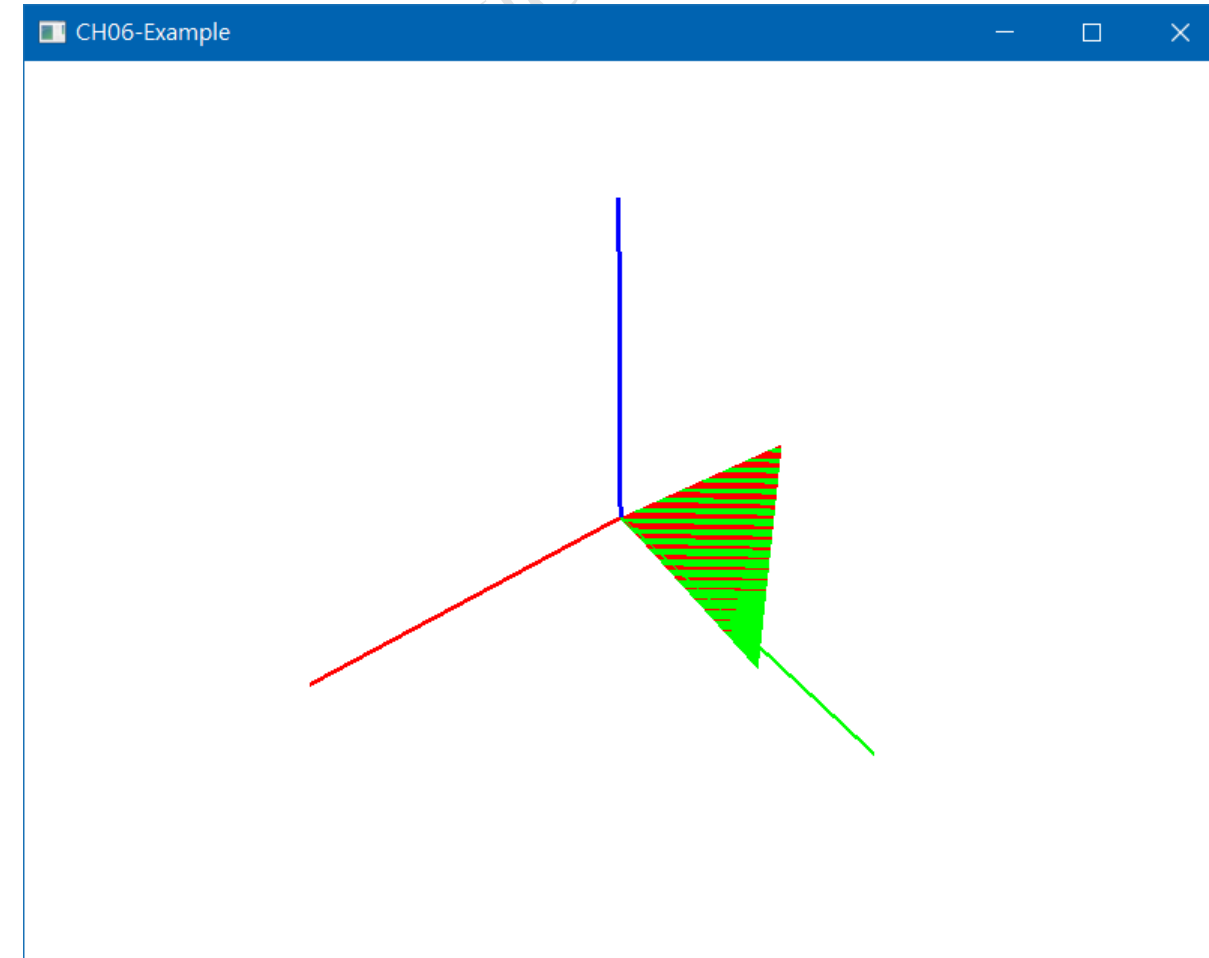




# Other issue: Poor depth resolution

```
14 def drawTriangles():
15     glBegin(GL_TRIANGLES)
16     glColor3f(1,0,0)
17     glNormal3f(0.,0.,1.)
18     glVertex3f(0.,0.,0.)
19     glVertex3f(200.,0.,0.)
20     glVertex3f(0.,200.,0.)
21     glColor3f(0,1,0)
22     glNormal3f(0.,0.,1.)
23     glVertex3f(0.,0.,0.01)
24     glVertex3f(200.,0.,0.01)
25     glVertex3f(0.,200.,0.01)
26     glEnd()
27
```

```
43 def display():
44     glClear(GL_COLOR_BUFFER_BIT |
45     GL_DEPTH_BUFFER_BIT)
46     glMatrixMode(GL_PROJECTION)
47     glLoadIdentity()
48     glViewport(0, 0, windowWidth, windowHeight)
49     vscale = 1
50     glFrustum(-800/1000.0*vscale,
51     800/1000.0*vscale, - 600/1000.0*vscale,
52     600/1000.0*vscale, 1.0*vscale, 5000)
53
54     gluLookAt(300,400,500,10,20,30,0,0,1)
55     global angle
56     angle = angle+0.01
57     glPushMatrix()
58     glRotatef(angle,0,0,1)
59     drawTriangles()
60     glPopMatrix()
61     drawCoordinate()
62     glutSwapBuffers()
63     glutPostRedisplay()
64
```



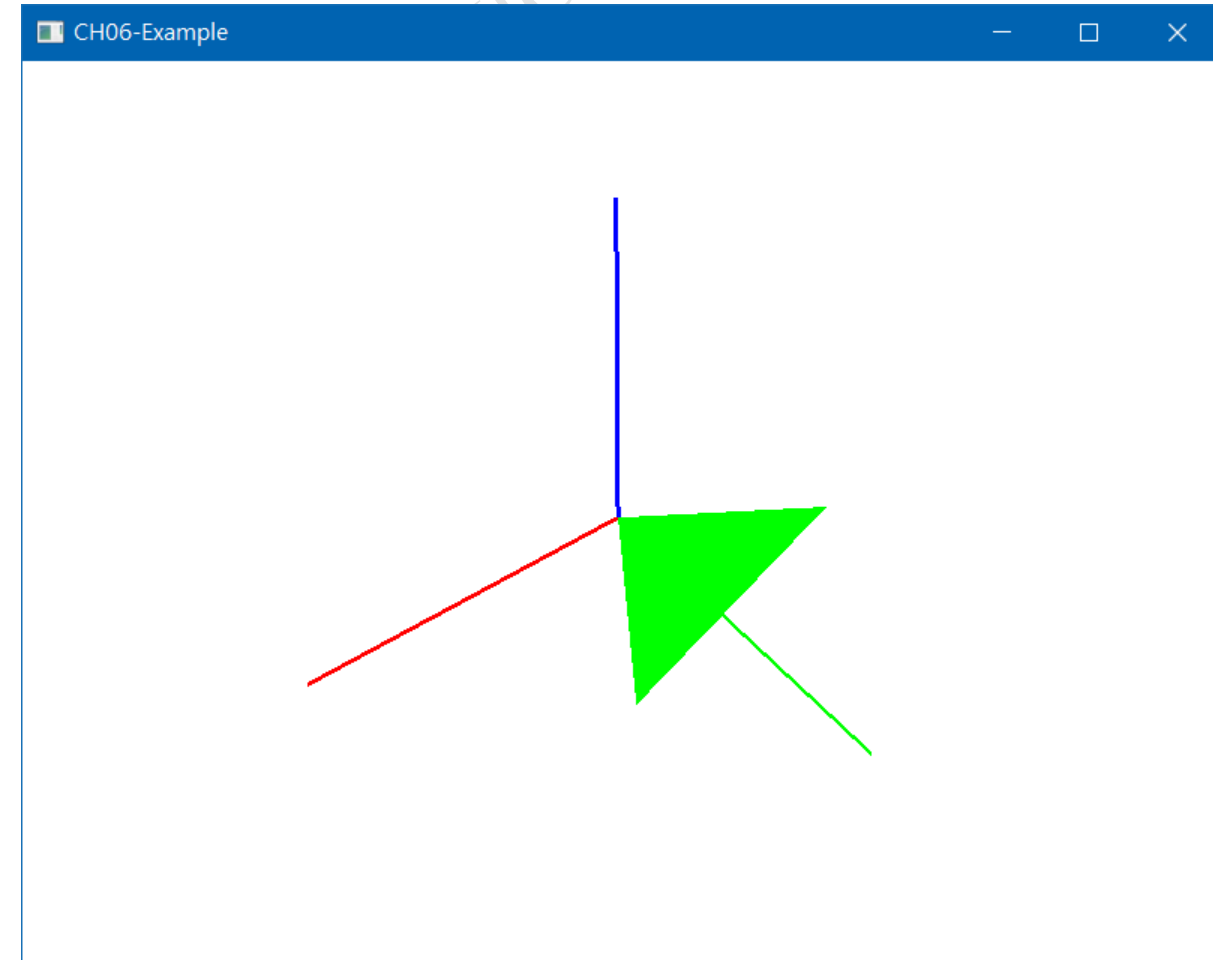




# Other issue: Poor depth resolution

```
14 def drawTriangles():
15     glBegin(GL_TRIANGLES)
16     glColor3f(1,0,0)
17     glNormal3f(0.,0.,1.)
18     glVertex3f(0.,0.,0.)
19     glVertex3f(200.,0.,0.)
20     glVertex3f(0.,200.,0.)
21     glColor3f(0,1,0)
22     glNormal3f(0.,0.,1.)
23     glVertex3f(0.,0.,0.01)
24     glVertex3f(200.,0.,0.01)
25     glVertex3f(0.,200.,0.01)
26     glEnd()
```

```
43 def display():
44     glClear(GL_COLOR_BUFFER_BIT |
45     GL_DEPTH_BUFFER_BIT)
46     glMatrixMode(GL_PROJECTION)
47     glLoadIdentity()
48     glViewport(0, 0, windowWidth, windowHeight)
49     vscale = 10
50     glFrustum(-800/1000.0*vscale,
51     800/1000.0*vscale, - 600/1000.0*vscale,
52     600/1000.0*vscale, 1.0*vscale, 5000)
53
54     gluLookAt(300,400,500,10,20,30,0,0,1)
55     global angle
56     angle = angle+0.01
57     glPushMatrix()
58     glRotatef(angle,0,0,1)
59     drawTriangles()
60     glPopMatrix()
61     drawCoordinate()
62     glutSwapBuffers()
63     glutPostRedisplay()
```





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