# Advanced Digital Signal Processing 高等數位訊號處理

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課程網頁:http://djj.ee.ntu.edu.tw/ADSP.htm

歡迎大家來修課,也歡迎有問題時隨時聯絡!

### • 評分方式:

#### **Basic: 15 scores**

原則上每位同學都可以拿到 12 分以上,另外,上課回答問題,每回答一次加0.8分

Homework: 60 scores (5 times, 每 3 週一次)

請自己寫,和同學內容極高度相同,將扣70%的分數就算寫錯但好好寫也會給40~95%的分數,遲交分數打8折,不交不給分。不知道如何寫,可用E-mail和我聯絡,或於上課時發問禁止Ctrl-C Ctrl-V 的情形。

### Term paper 25 scores

### Term paper 25 scores

方式有四種

### (1) 書面報告

10頁以上(不含封面),中英文皆可,11或12的字體,題目可選擇和課程有關的任何一個主題。

格式和一般寫期刊論文或碩博士論文相同,包括 abstract, conclusion, 及 references,並且要分 sections,必要時有subsections。 References 的寫法, 可參照一般 IEEE 的論文的寫法 鼓勵多做實驗及模擬,

有做模擬的同學請將程式附上來,會有額外加分。 嚴禁 Ctrl-C Ctrl-V 的情形,否則扣 70% 的分數

### (2) Tutorial (對既有領域做淺顯易懂的整理)

限十七個名額,和書面報告格式相同,但頁數限制為18頁以上(若為加強前人的 tutorial,則頁數為 (2/3)N+13 以上,N 為前人 tutorial 之頁數),題目由老師指定,以**清楚且有系統**的介紹一個主題的基本概念和應用為要求,為上課內容的進一步探討和補充, $\overline{\mathbf{交}}$  Word 檔。

選擇這個項目的同學,學期成績加4分

or Latex resource

### (3) 口頭報告

限四個名額,每個人 40分鐘,題目可選擇和課程有關的任何一個主題。 口頭報告將於 4月30日(第 9 週)進行。有意願的同學,請儘早告知,以 先登記的同學為優先。

口頭報告時,鼓勵大家提問(包括口頭報告的同學,也可針對其他同學的報告內容提問)。曾經提問的同學,加分同上課回答問題。 選擇這個項目的同學,學期成績加2分

### (4) 編輯 Wikipedia

中文或英文網頁皆可,至少 2 個條目,但不可同一個條目翻成中文和英文。總計 80行以上。限和課程相關者,自由發揮,越有條理、有系統的越好

選擇編輯 Wikipedia 的同學,請於 6月25日前,向我登記並告知我要編緝的條目(2 個以上),若有和其他同學選擇相同條目的情形,則較晚向我登記的同學將更換要編緝的條目

書面報告和編輯 Wikipedia,期限是7月2日

以上若有做實驗模擬,請附上程式碼,會有額外的加分 (鼓勵不強制)

### Tutorial 可供選擇的題目(共 17 個,可以略做修改)

- (1) Quantum Fourier Transform
- (2) Graph Fourier Transform
- (3) Bioacoustics
- (4) Gaussian Mixture Model
- (5) Facial Landmark Extraction
- (6) Metrics for Visual Quality Assessment
- (7) Target Localization Technique
- (8) Vehicle Sensing and Tracking
- (9) Anomaly Detection Using Neural Networks
- (10) Dictionary Learning
- (11) Chromatic Derivative
- (12) Bargmann Transform

### Tutorial 可供選擇的題目(可以略做修改)

- (13) Learning Based Video Compression Techniques
- (14) AV1 Video Coding
- (15) Recent Advance in FinTech
- (16) Remote Sensing Techniques
- (17) Machine Learning for Wireless Communication

上課時間:16週

4/2 放假

2/26, 4/30, Oral Presentation, 5/7, 出 HW3 3/5, 3/12, 出 HW1 5/14, 5/21, 交 HW3 3/19, 3/26, 交 HW1 5/28, 出 HW4 4/9、出 HW2 6/4, 6/11, 交 HW4, 4/16, 6/18, 出 HW5 4/23, 交 HW2

7/2, 交 HW5 及 term paper

原則上: 3n 週出作業, 3n+2 週繳交

### **Matlab Program**

Download: 請洽台大各系所

洪維恩,Matlab 程式設計,旗標,台北市,2013 . (合適的入門書)

張智星, Matlab 程式設計入門篇, 第四版, 碁峰, 2016.

蒙以正,數位信號處理:應用 Matlab, 旗標, 台北市, 2007.

繆紹綱譯,數位影像處理-運用 Matlab,東華,2005.

預計看書學習所花時間: 3~5天

### **Python Program**

Download: https://www.python.org/

## 研究所和大學以前追求知識的方法有什麼不同?

研究所:觀念的學習

大學:

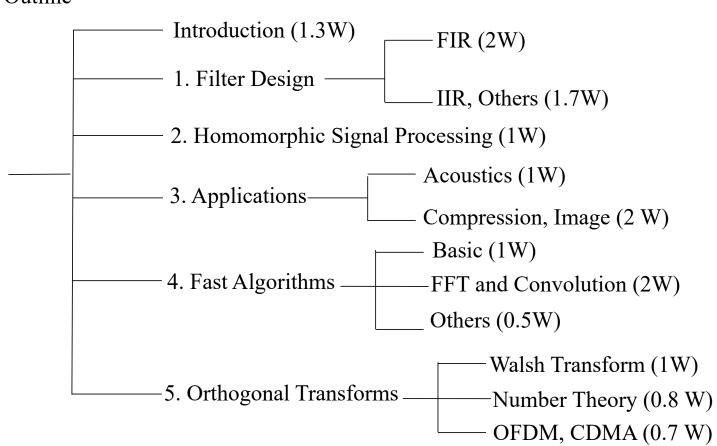
### **Question:**

Why should we use the Fourier transform?

Is the Fourier transform the best choice in any condition?

### I. Introduction



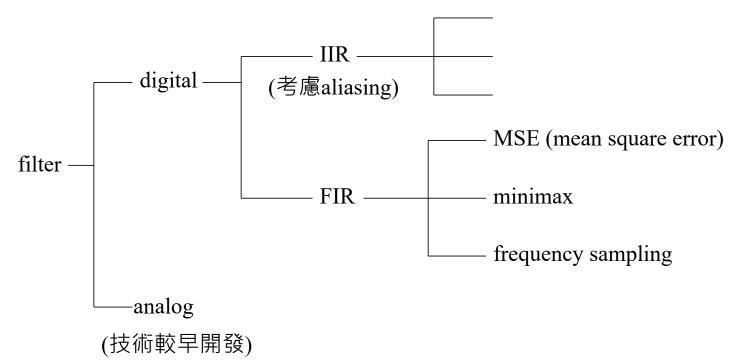


目標:

- (1) 對 Digital Signal Processing 作更有系統且深入的了解
- (2) 學習 Digital Signal Processing 幾個重要子領域的基礎知識

#### Part 1: Filter

• Filter 的分類



FIR filter 的優點:

缺點: An FIR filter is impossible to have the ideal frequency response of

### **Part 2: Homomorphic Signal Processing**

● 概念:把 convolution 變成 addition

### Part 3: Applications of DSP

filter design, data compression (image, video, text), acoustics (speech, music), image analysis (structural similarity, sharpness), 3D accelerometer

- Part 4: Fast Algorithms
- Basic Implementation Techniques

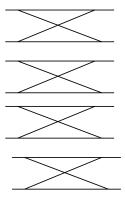
Example: one complex number multiplication

=? Real number multiplication.

Trade-off: "Multiplication" takes longer than "addition"

• FFT and Convolution

Due to the Cooley-Tukey algorithm (butterflies), the complexity of the FFT is:



The complexity of the convolution is: 3個 DFTs,  $O(N \log_2 N)$ 

• Part 5: Orthogonal Transforms

DFT 的兩個主要用途:

Question: DFT 的缺點是什麼? 
$$DFT x[n]$$
  $x n e^{j\frac{2-mn}{N}}$ 

- Walsh Transform (CDMA)
- Number Theoretic Transform

- Orthogonal Frequency-Division Multiplexing (OFDM)
- Code Division Multiple Access (CDMA)

# Review 1: Four Types of the Fourier Transform

● 四種 Fourier transforms 的比較

	time domain	frequency domain	
(1) Fourier transform	continuous, aperiodic	continuous, aperiodic	
(2) Fourier series	continuous, periodic	discrete, aperiodic	
	(or continuous, only the value in a finite duration is known)		
(3) discrete-time Fourier transform	discrete, aperiodic	continuous, periodic	
(4) discrete Fourier transform	discrete, periodic  (or discrete, only the value in a finite duration is known)	discrete, periodic	

### (1) Fourier Transform

 $X f \qquad x t e^{j2 ft} dt , \qquad x t \qquad X f e^{j2 ft} df$ 

Alternative definitions

X  $x t e^{-j t} dt$  ,  $x t = \frac{1}{2} X e^{j t} dt$ 

(2) Fourier series (suitable for period function)

$$X[m]$$
  $\int_{0}^{T} x \ t \ e^{-j\frac{2\pi}{3}}$ 

X[m]  $\int_{0}^{T} x \ t \ e^{-j\frac{2-m}{T}t} dt$   $x \ t \ T^{-1}$   $X[m]e^{j\frac{2-m}{T}t}$ 

T: 週期  $x \ t \ x \ t \ T$  Possible frequencies are to satisfy:

$$e^{j2} ft e^{j2} f(t T)$$

頻率和 
$$m$$
 之間的關係:  $f$   $\frac{m}{T}$   $\frac{1}{T}$  整數倍

$$\frac{1}{T}$$
 整數倍

### (3) Discrete-time Fourier transform (DSP 常用)

$$X f$$
  $x n e^{j2 f n}$ ,  $x n$   $t = 0$   $t = 0$ 

### (4) Discrete Fourier transform (DFT) (DSP 常用)

$$X m = \sum_{n=0}^{N-1} x n e^{j\frac{2mn}{N}}, x n = \frac{1}{N} \sum_{m=0}^{N-1} X m e^{j\frac{2mn}{N}}$$

頻率和 
$$m$$
 之間的關係:  $f$   $\frac{m}{N_t}$   $\frac{m}{N}f_s$  where  $f_s = 1/\Delta_t$  (sampling frequency)

# Review 2: Normalized Frequency

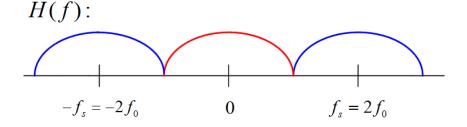
### (1) Definition of **normalized frequency** F:

$$F \quad \frac{f}{f_s} \quad f \quad t \quad \frac{t}{2} \quad \text{where } f_s = 1/\Delta_t \text{ (sampling frequency)}$$

$$\Delta_t : \text{sampling interval}$$

### (2) folding frequency $f_0$

$$f_0$$
  $\frac{f_s}{2}$  若以 normalized frequency 來表示, folding frequency = 1/2



For the discrete time Fourier transform

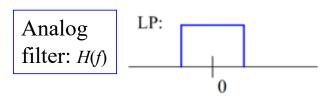
(1) 
$$G(f) = G(f + f_s)$$
 i.e.,  $G(F) = G(F + 1)$ .

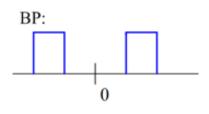
(2) If g[n] is real  $G(F) = G^*(-F)$  (\* means conjugation)

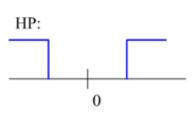
只需知道 
$$G(F)$$
 for  $0 \le F \le \frac{1}{2}$  (即  $0 < f < f_0$ )

就可以知道全部的 G(F)

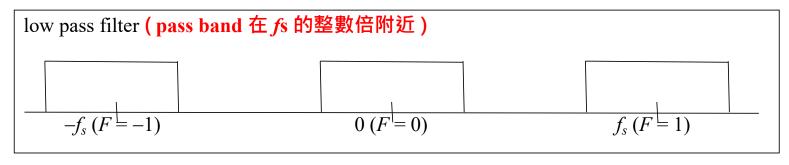
(3) If 
$$g[n] = g[-n]$$
 (even)  $\longrightarrow$   $G(F) = G(-F)$ ,  
 $g[n] = -g[-n]$  (odd)  $\longrightarrow$   $G(F) = -G(-F)$ 

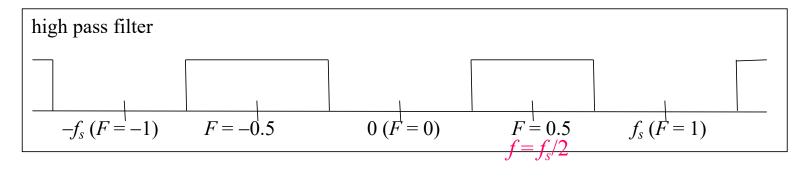


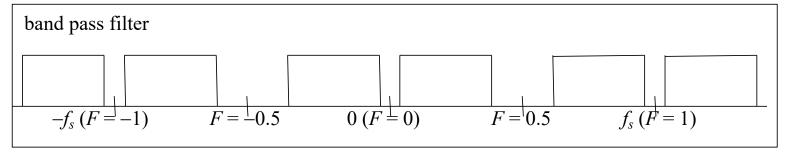




• Discrete time Fourier transform of the lowpass, highpass, and band pass filters







# Review 3: Z Transform and Laplace Transform

### • Z-Transform

suitable for discrete signals

$$G z \qquad g n z^n$$

Compared with the discrete time Fourier transform:

$$G f \qquad g n e^{j2 f n} \qquad z e^{j2 f}$$

### • Laplace Transform

suitable for continuous signals

One-sided form 
$$G$$
  $s$   $_{0}$   $g(t)e^{-st}dt$   
Two-sided form  $G$   $s$   $g(t)e^{-st}dt$ 

Compared with the Fourier transform:

$$G f g t e^{j2 ft} dt$$
  $s j2 f$ 

# Review 4: IIR Filter Design

Two types of digital filter:

- (1) IIR filter (infinite impulse response filter)
- (2) FIR filer (finite impulse response filer)

There are 3 popular methods to design the IIR filter.

Advantage:

Disadvantage:

### An IIR Filter May Not be Hard to Implement

Ex: 
$$h[n] = (0.9)^n$$
, for  $n \ge 0$ ,  $h[n] = 0$ , otherwise  $y[n] = x[n] * h[n]$ 

Z transform

### Method 1: Impulse Invariance

白話一點,就是直接做 sampling

analog filter  $h_a(t)$ 

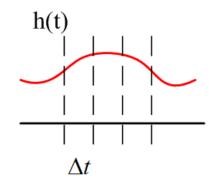
digital filter h[n]

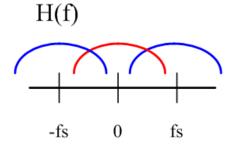
 $h n h_a n_t$ 

Advantage: Simple

Disadvantage: (1) infinite

(2)





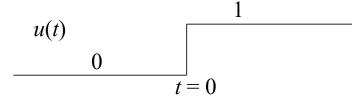
### **Method 2**: Step Invariance

對 step function 的 response 作 sampling

analog filter 
$$h_a(t)$$

digital filter h[n]

step function (continuous form)



step function (discrete form)

Laplace transform of u(t):

$$\frac{1}{s}$$

Fourier transform of u(t):

$$\frac{1}{j2} f$$

$$\frac{1}{1}$$

Step 1 Calculate the convolution of  $h_a(t)$  and u(t)

$$h_{a,u}$$
  $t$   $h_a$   $t$   $u$   $t$   $h_a$   $u$   $t$   $d$   $t$   $h_a$   $d$   $H_{a,u}(f)$   $\frac{H_a(f)}{j2\ f}$  (其實就是對  $h_a(t)$  做積分)

Step 2 Perform sampling for  $h_{a,u}(t)$ 

$$h_u n h_{a,u} n_t$$

Step 3 Calculate h[n] from  $h n h_u n h_u n 1$ 

Note: Since 
$$h_u n$$
  $h n$   $u n$   $H_u z$   $\frac{1}{1} z^1 H z$ 

$$H z 1 z^1 H_u z$$
So  $h n$   $h_u n$   $h_u n$  1

Advantage of the step invariance method:

\*主要 Advantage:

Disadvantage of the step invariance method:

較為間接,設計上稍微複雜

### **Method 3**: Bilinear Transform

Suppose that we have known an analog filter  $h_a(t)$  whose frequency response is  $H_a(f)$ .

To design the digital filter h[n] with the frequency response H(f),

$$H$$
  $f_{new}$   $H_a$   $f_{old}$   $f_{old} \in (-\infty, \infty)$  
$$f_{new} \in (-f_s/2, f_s/2)$$
 
$$f_s = 1/\Delta_t \text{ (sampling frequency)}$$

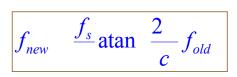
• The relation between  $f_{new}$  and  $f_{old}$  is determined by the mapping function

$$c = \frac{1}{1 + z^{-1}}$$
  $c = \frac{1}{2} \int_{low} \frac{1}{t}$   $c = \frac{1}{2$ 

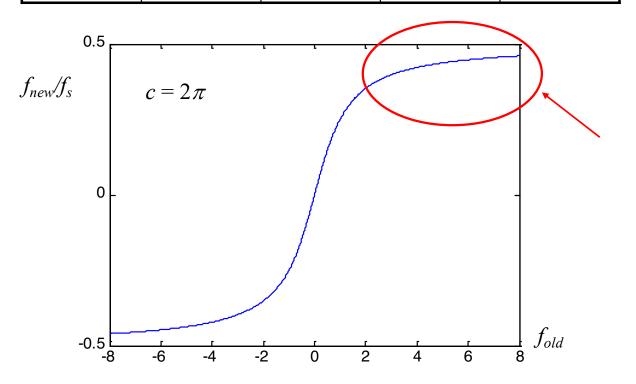
• Suppose that the Laplace transform of the analog filter  $h_a(t)$  is  $H_{a,L}(s)$ 

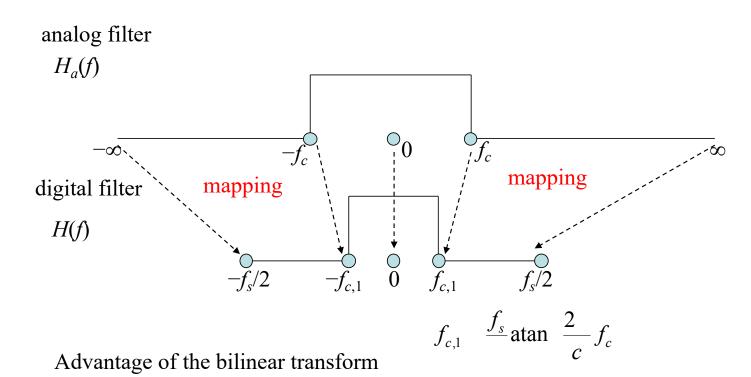
The Z transform of the digital filter h[n] is  $H_z(z)$ 

$$H_{z} z H_{a,L} c \frac{1}{1} \frac{z^{-1}}{z^{-1}}$$



$f_{\mathit{old}}$	-∞	0	8	1
$f_{new}$				





Disadvantage of the bilinear transform

### 附錄一: 學習 DSP 知識把握的要點

- (1) Concepts: 這個方法的核心概念、基本精神是什麼
- (2) Comparison: 這方法和其他方法之間,有什麼相同的地方? 有什麼相異的地方
- (3) Advantages: 這方法的優點是什麼 (3-1) Why? 造成這些優點的原因是什麼
- (4) Applications: 這個方法要用來處理什麼問題,有什麼應用
- (5) Disadvantages: 這方法的缺點是什麼

(5-1) Why? 造成這些缺點的原因是什麼

(6) Innovations: 這方法有什麼可以改進的地方 或是可以推廣到什麼地方