

## 1 Continuation about collective communication

The communication model under discussion is the **Alpha-Beta Model**. Its formula is given by:

$$\text{Communication Model} = \alpha + n \times \beta$$

where

$$\beta = \frac{1}{B}$$

The second term,  $n \times \beta$ , dominates; hence, we aim to minimize this term to utilize the bandwidth as efficiently as possible.

## 2 Benefits of Ring Algorithm

- It utilizes the bandwidth properly, and at any time any connection between any two nodes works
- It can be implemented for any random number of nodes

## 3 Bandwidth Utilization and MST Preference

**Important:** In machine learning, the **Minimum Spanning Tree (MST)** is often preferred because it fully utilizes the available bandwidth.

## 4 Primitives in Ring Algorithm

### 4.1 All Gather

Allgather

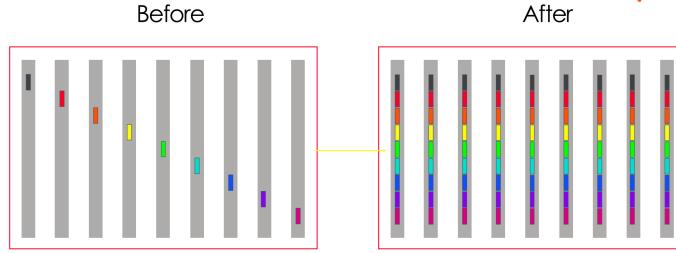


Figure 1: All Gather in Ring Algorithm

Cost of All Gather is given by:

$$(p - 1) \left( \alpha + \frac{n}{p} \times \beta \right)$$

### 4.2 Reduce Scatter

This is not a reduce + scatter, instead it becomes a primitive.

Reduce-scatter

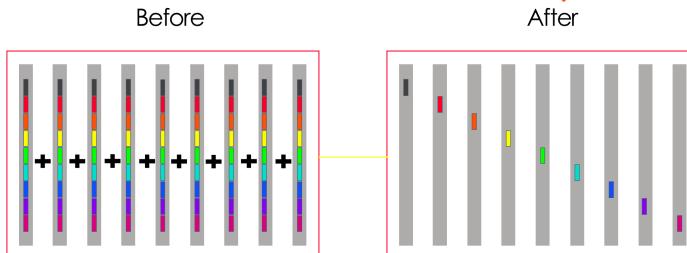


Figure 2: Reduce Scatter in Ring Algorithm

Cost of Reduce Scatter is given by:

$$(p - 1) \left( \alpha + \frac{n}{p} \cdot \beta + \frac{n}{p} \cdot \gamma \right)$$

### 4.3 Reduce Scatter vs All Gather

- **Important:** The **Reduce Scatter** operation (reduce followed by scatter) incurs more latency than **All Gather** due to an additional step involving the introduction of a  $\gamma$  term.
- For any primitive that requires performing a reduction, there exists an additional  $\gamma$  term. For long messages, this term becomes expensive because it represents an extra computation requiring significant FLOPs. Thus, it demands compute power from CPUs or GPUs.
- In the context of machine learning, this implies allocating **Streaming Multiprocessors (SMs)** from GPUs, where an SM represents a computing unit. For example, NVIDIA's H100 GPU contains nearly 130 SMs. This introduces a **compute bottleneck** in addition to the bandwidth bottleneck.

To alleviate this, we aim to minimize the  $\gamma$  term. Modern GPU architectures include dedicated hardware units specifically designed to process  $\gamma$ . Similarly, network chips now include specialized components for  $\gamma$ -reduction operations. This represents a **co-design approach** between networking and machine learning systems. Check the concept of NVSHARP!

**Question:** Can the Ring algorithm perform better? In other words, how can we prove that scatter or gather using MST is most optimal in terms of bandwidth?

**Answer:** MST is better because we always prefer direct communication to the destination cell instead of sequential (hop-by-hop) transmission which is useful for the case of scatter and gather.

## 5 Building Blocks for Broadcast (Large Messages)

- In MST, **broadcast** is a primitive operation. In the ring topology, it is implemented as **scatter + all-gather**, so the latency is the sum of both.
- In MST, **reduce** is a primitive operation. In the ring topology, it is implemented as **reduce-scatter + gather**.
- All reduce can be termed as the sum of Reduce Scatter and All Gather

On a high level, we prefer **reduce-scatter + all-gather** for All Reduce because it offers higher bandwidth utilization and lower memory consumption.

### 5.1 Summary of Collective Communication Primitives

1. Reduce = Reduce-scatter + Gather
2. All-reduce = Reduce-scatter + All-gather
3. Broadcast = Scatter + All-gather

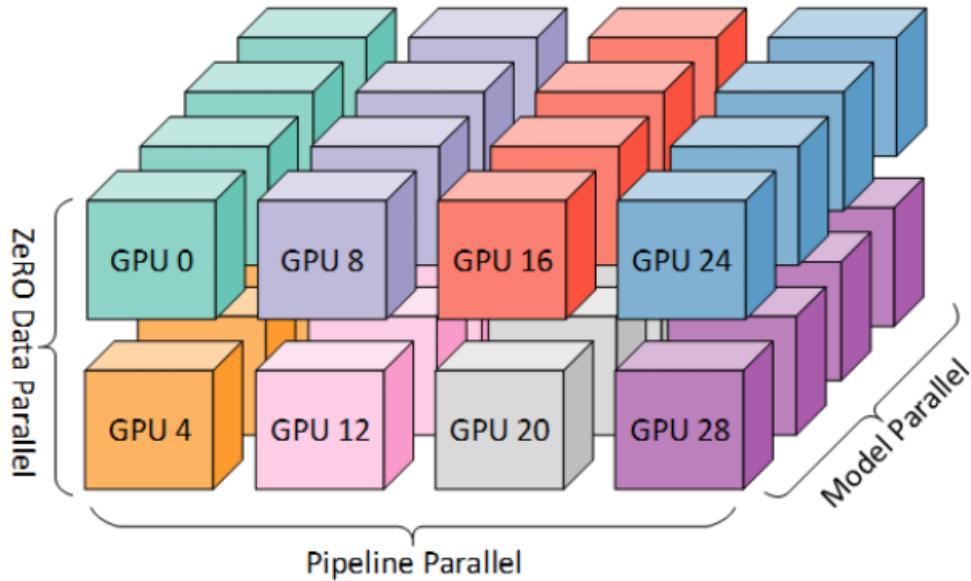
## 6 Real Cluster Setup for Training ChatGPT

### 6.1 Hardware (H200 GPUs)

Each compute node is equipped with up to eight NVIDIA H200 GPUs. To scale up training capacity, additional nodes are added to form a larger distributed cluster.

### 6.2 Interconnect and Communication

Within a single node, the eight GPUs are connected through a high-speed interconnect (such as NVLink or NVSwitch), which enables fast data exchange and efficient parallel computation. Across the cluster, multiple nodes are interconnected—typically through a high-bandwidth network topology. Communication within the same interconnect group is very fast, whereas communication between different groups occurs over links with comparatively lower bandwidth.



### 6.3 GPU vs TPU Interconnects

- **GPU Clusters:** Typically use a 2D mesh topology, connecting GPUs in rows and columns for efficient communication.
- **TPU Clusters:** Use a 3D mesh, adding an extra dimension of connectivity for better scalability and parallelism.
- **Hierarchy of Meshes:** A 1D mesh can be extended into a 2D mesh, and a 2D mesh can be expanded into a 3D mesh, allowing larger clusters to communicate efficiently.

## 7 Collective Communication

### 7.1 Pros:

- Structured and well-defined communication primitives – makes the communication pattern predictable and organized.
- Well optimized – designed for efficiency, ensuring data moves quickly between nodes.
- Mathematically analyzable – performance can be understood and predicted using formal analysis.

### 7.2 Cons:

- Lack of fault tolerance – if a single node fails, the entire collective operation fails, which can disrupt computations.
- Requires homogeneity – performs best when all nodes are identical and all bandwidths are equal, which is rarely achievable in real-world systems.

## 8 Operations of Database

### 8.1 CRUD:

- **Create:** Add new data to the database.
- **Read:** Retrieve existing data.
- **Update:** Modify existing data.
- **Delete:** Remove data from the database.

### 8.2 Online Transaction Processing (OLTP)

- Reads only a small number of records per query, supporting fast transactions.
- Provides low-latency, random-access writes for real-time updates.
- Used by end users or customers through web applications.
- Represents the current state of the data.
- Typically handles data sizes from gigabytes to terabytes.

### 8.3 Online Analytical Processing (OLAP)

- Reads and aggregates large volumes of records to support analysis.
- Handles bulk imports or streaming writes via ETL processes.
- Used primarily by analysts for decision-making and insights.

- Stores historical events and data for long-term analysis.
- Typically deals with data sizes from terabytes to petabytes.

## 8.4 OLTP Data Considerations

- OLTP data must be highly available and carefully protected to ensure transactional integrity.
- An additional layer is needed on top of the database to prevent accidental corruption when multiple users are accessing and updating the data simultaneously.
- Any reads for analysis should be performed on a read-only copy to avoid affecting the live transactional data.

# 9 Data Warehousing

- **Data Warehouse** solves the problem of running analytics on live transactional data.
- It acts as a separate layer built on top of OLTP systems.
- It stores a read-only copy of data for analytic queries.
- It prevents heavy analytic queries from slowing down OLTP systems.
- It ensures data consistency for multiple analysts working at once.
- Data warehouses are common in large enterprises, small companies might use simpler solutions, such as **Levels.fyi** which used Google Sheets as a backend to scale to millions of users.
- It maintains low latency and supports ad-hoc analytic queries.

## 9.1 Extract-Transform-Load (ETL)

This is the common process used to populate a data warehouse:

- **Extract:** Get data from the various OLTP databases (e.g., periodic data dumps or continuous streaming).
- **Transform:** Convert the data into an analysis-friendly schema. This step includes data cleaning and restructuring.
- **Load:** Store the transformed data into the data warehouse.

## 9.2 Why use a Data Warehouse?

- **Separation of concerns:** Keeps OLTP and OLAP workloads isolated. It allows OLTP systems to focus on low-latency transactions while OLAP systems handle complex analytical queries. This separation ensures performance, reliability, and manageable latency for both.
- **Expertise and Management:** The systems require different management and expertise. It is easier to maintain and scale independently.

- **Optimized for Analytics:** Classic indexes used in OLTP (like SSTables, B-trees) are good for reading/writing single records but are not efficient for answering large-scale analytic queries. Data warehouses use different storage strategies (e.g., column-oriented storage).

### 9.3 Interaction with OLAP and OLTP

- Both OLAP and OLTP systems can often be interacted with using a **SQL query interface**.
- For OLAP, there is a growing trend of codeless user interfaces, including **Text2SQL** capabilities.

## 10 Distributed Computing and Big Data

### 10.1 Core Concepts

This area of study covers several key topics:

- Parallelism Basics
- Data Replication and Partitioning
- Batched Processing
- Streaming Processing

### 10.2 Parallel Data Processing

- **Central Issue:** The workload takes too long for a single processor to handle.
- **Basic Idea:** Split the workload across multiple processors and machines. This is achieved through a **Divide and Conquer** strategy.
  - **Divide and Conquer Strategy:** This strategy divides one problem into small sub-problems. This division keeps taking place until one processor can finish the work in an acceptable amount of time. This gives us a partial result. These partial results are merged back to form the final result for the main problem.

### 10.3 Data Processing Abstraction

- We need a way to represent various processing functions (e.g., sum, mean, PageRank, supervised learning, model inference).
- **Question:** How can we represent these arbitrarily complex processing functions?

### 10.4 Dataflow Graphs

- A **Dataflow Graph** is a common abstraction in parallel data processing.
- It is a directed graph representing a program:

- **Vertices (Nodes):** Abstract operations (computational primitives).
- **Edges:** Represent the direction of data flow, showing data dependency.

- **Examples:**

- **Relational Dataflows:** Used in RDBMS, Pandas. This is also known as a **Logical Query Plan** in database systems.
- **Matrix/Tensor Dataflows:** Used in NumPy, PyTorch, TensorFlow. This is also known as a **Neural Network Computational Graph** in ML systems.

## 10.5 Parallelism Paradigms

Key parallelism paradigms in data systems (assuming coordination):

- **Task Parallelism:** Different functions are executed on the same or different data.
- **Data Parallelism:** The same function is executed on different partitions of the data.
- **Hybrid Parallelism:** A combination of both task and data parallelism.