

# University of Glasgow

## Degrees of BEng in Engineering

### POWER ENGINEERING 3 (UESTC3005)

2017

**Attempt all questions. The total number of possible marks is 100.**

*The numbers in square brackets in the right-hand margin indicate the marks allotted to the part of the question against which the mark is shown. These marks are for guidance only.*

**An electronic calculator may be used provided that it does not have a facility for either textual storage or display, or for graphical display.**

**If a calculator is used, intermediate steps in the calculation should be indicated.**

Q1 Consider the single-phase AC circuit shown in Figure Q1.

- (i) The current  $i(t)$  can be written in the form  $i(t) = I_m \cos(\omega t + \phi)$  A, determine the values of  $I_m$  and  $\phi$ . [4]
- (ii) Calculate the average power dissipation  $P_{avg}$  in the circuit, and explain where the power is dissipated. [4]
- (iii) Construct a phasor diagram showing input voltage  $v(t)$  and current  $i(t)$  [2].

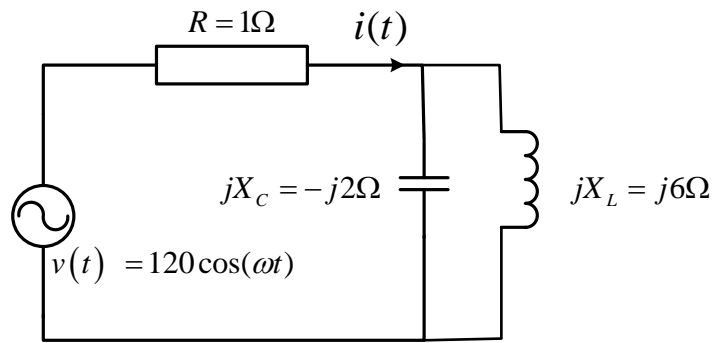


Figure Q1

- Q2 (a) A balanced delta connected load of  $(20 + j20) \Omega$  is connected to a 3-phase 220V/50Hz (RMS phase voltages) power supply shown in Figure Q2.

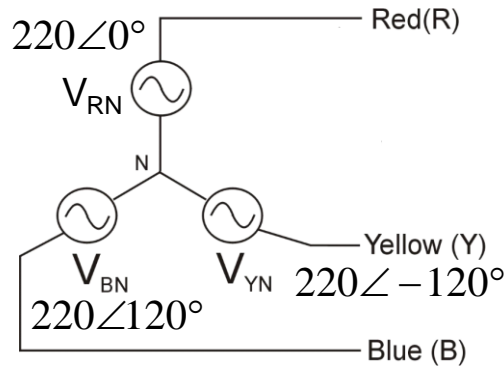


Figure Q2 Balanced 3-phase power supply

Draw the circuit diagram and from this:

- (i) Draw the circuit diagram including the implementation of a two-wattmeter power measurement [2]
  - (ii) Calculate the magnitude of the line voltages. [1]
  - (iii) Calculate the three line currents ( $I_R$ ,  $I_Y$  and  $I_B$ ). [3]
  - (iv) Construct a phasor diagram showing all line voltages ( $V_{RY}$ ,  $V_{YB}$  and  $V_{BR}$ ) and phase voltages ( $V_{RN}$ ,  $V_{YN}$  and  $V_{BN}$ ). [6]
  - (v) Determine the total output supply power (W) using two-wattmeter measurements. [3]
- (b) An unbalanced delta connected load consisting of  $Z_{RY} (10+j10)\Omega$ ,  $Z_{YB} (10+j0)\Omega$  and  $Z_{BR} (0+j10)\Omega$  is connected to the power supply shown in Figure Q2. Draw the circuit diagram and from this:
- (i) Calculate the three load phase currents ( $I_{RY}$ ,  $I_{YB}$  and  $I_{BR}$ ). [3]
  - (ii) Calculate the three line currents ( $I_R$ ,  $I_Y$  and  $I_B$ ). [3]
  - (iii) Calculate the three load phase power consumptions (W) [3]
  - (iv) Construct a phasor diagram showing three line voltages ( $V_{RY}$ ,  $V_{YB}$  and  $V_{BR}$ ), three load phase currents ( $I_{RY}$ ,  $I_{YB}$  and  $I_{BR}$ ). [6]

Q3 (a) Given the equivalent circuit parameters shown on Table Q3 for a 110V/10V single phase transformer, determine the following for a  $2\Omega$  resistive load connected to the secondary terminals:

- (i) Draw the equivalent circuit labelling all circuit parameters [2]
- (ii) Output load voltage (V) [2]
- (iii) Output load current (A) [2]
- (iv) Output load power (W) [2]
- (v) Transformer losses (W) [2]
- (vi) Efficiency (%) [3]
- (vii) Voltage Regulation (%) [3]

Parameter	Value
$R_c$	$5k\Omega$
$X_M$	$600\Omega$
$R_{leq}$	$15\Omega$
$X_{leq}$	$3\Omega$

Table Q3

(b) A three-phase  $\Delta/Y$  transformer bank is rated 110kV/22kV and delivers 3300kVA to a balanced delta connected load at rated voltage. Assuming an ideal transformer, calculate the following:

- (i) Construct a phasor diagram showing all primary phase voltages and secondary line voltages for the three-phase transformer in the question. [6]
- (ii) Bank Ratio and Phase Ratio. [2]
- (iii) The magnitudes of the secondary line currents [2]
- (iv) The magnitudes of the primary line current [2]
- (v) The magnitudes of the currents in the primary coils [2]

Q4 (a) A 2-pole star connected three-phase induction motor has the per-phase equivalent circuit shown in Fig. Q4

- (i) If the locked rotor test produces a per phase input power of 2000 W with a phase current of 100 A at a phase voltage of 40V, and the phase resistance of the motor windings is measured at  $0.1 \Omega$  using a multimeter, calculate the rotor resistance  $R_r$  and stator resistances  $R_s$ , and total leakage reactance  $X_{eq}$

[6]

- (ii) If the slip at a given load is  $s = 0.03$ , calculate the motor speed  $n_r$  (rpm), motor output power  $P_o$  (W), motor output torque  $T_o$  (N.m) and efficiency when operating with a 220V 50Hz supply where 220V is the phase voltage  $V_{ph}$ .

[12]

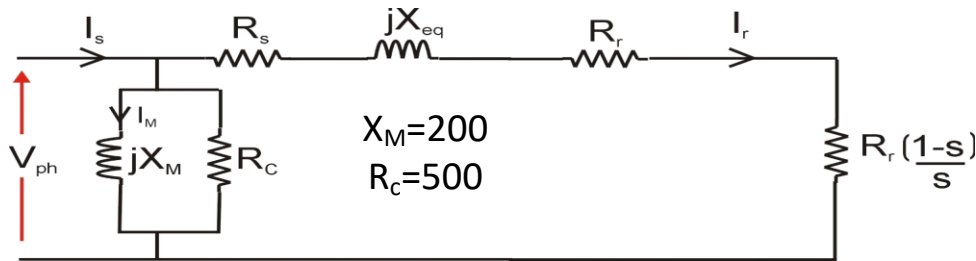


Fig Q4

- (b) A star connected 3-phase wound field synchronous generator with a synchronous reactance  $X_s$  of  $3\Omega$  is connected to a 690V (line) grid and supplies 2MW at 0.9 lagging power factor at its terminals. Calculate the phase current and resultant voltage  $V_{XS}$  across the synchronous reactance, and determine the required excitation voltage ( $E_{ph}$ ) and load angle ( $\delta$ ).

[12]