



**POWER ENGINEERING**  
**#07 THREE-PHASE AC POWER SYSTEMS**  
**POWER MEASUREMENT (2)**

2018



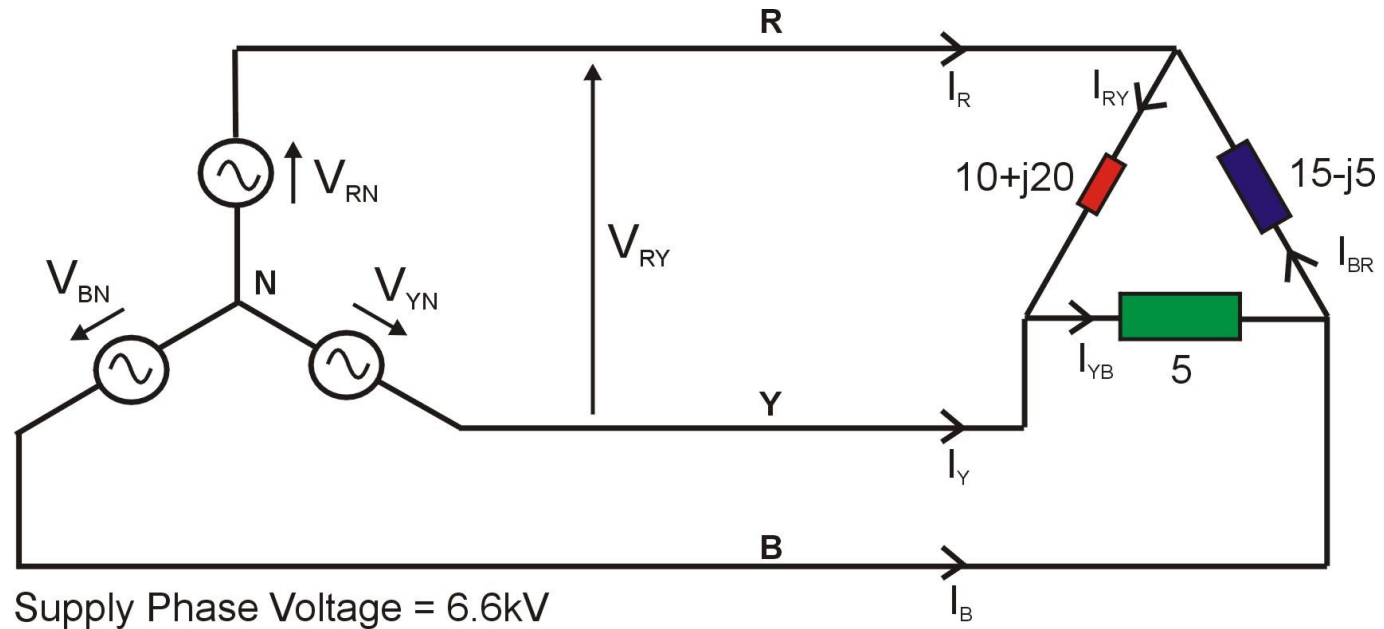
University  
of Glasgow

# Unbalanced 3 Phase AC Systems

*Today we will investigate:*

- Unbalanced Delta connected load: Example #1 - continued
- Unbalanced Delta connected load: Example #2
- Unbalanced 3 wire Star connected load
- Unbalanced 4 wire Star connected load
- Unbalanced 4 wire Star connected load: Example
- Summary of application of 3 and 2 Wattmeter Methods

## Unbalanced Delta connected load example #1 cont :



Determine:

- 1] All the load phase currents
- 2] Draw a phasor diagram (to scale) showing all line voltages and load phase currents. From this estimate the line currents.
- 3] The total 3 phase power (W) at the load

**Solution done on Whiteboard**

## Lecture 6 : Unbalanced Delta Load

$$I_R = I_{RY} - I_{BR}$$

$$I_Y = I_{YB} - I_{RY}$$

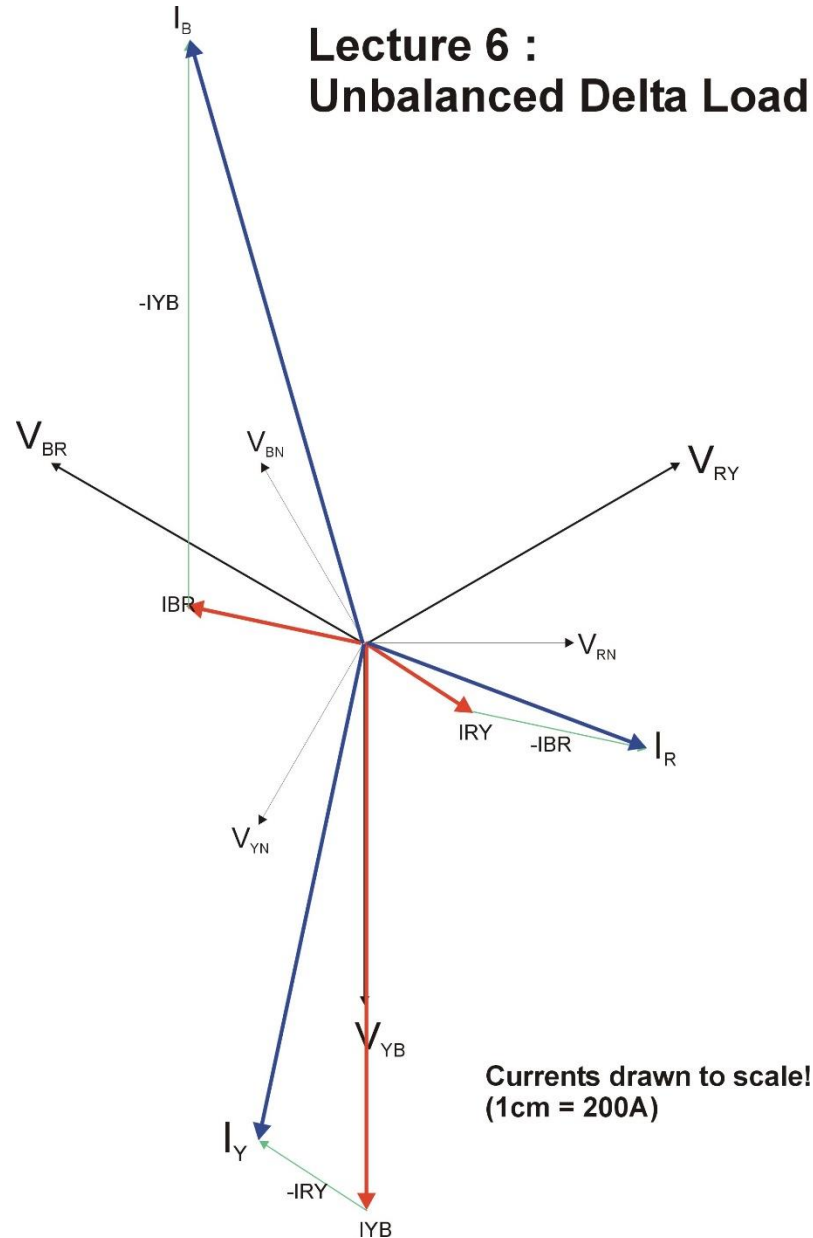
$$I_B = I_{BR} - I_{YB}$$

From Phasor Diagram:

$$I_R = 1220 \angle -20^\circ$$

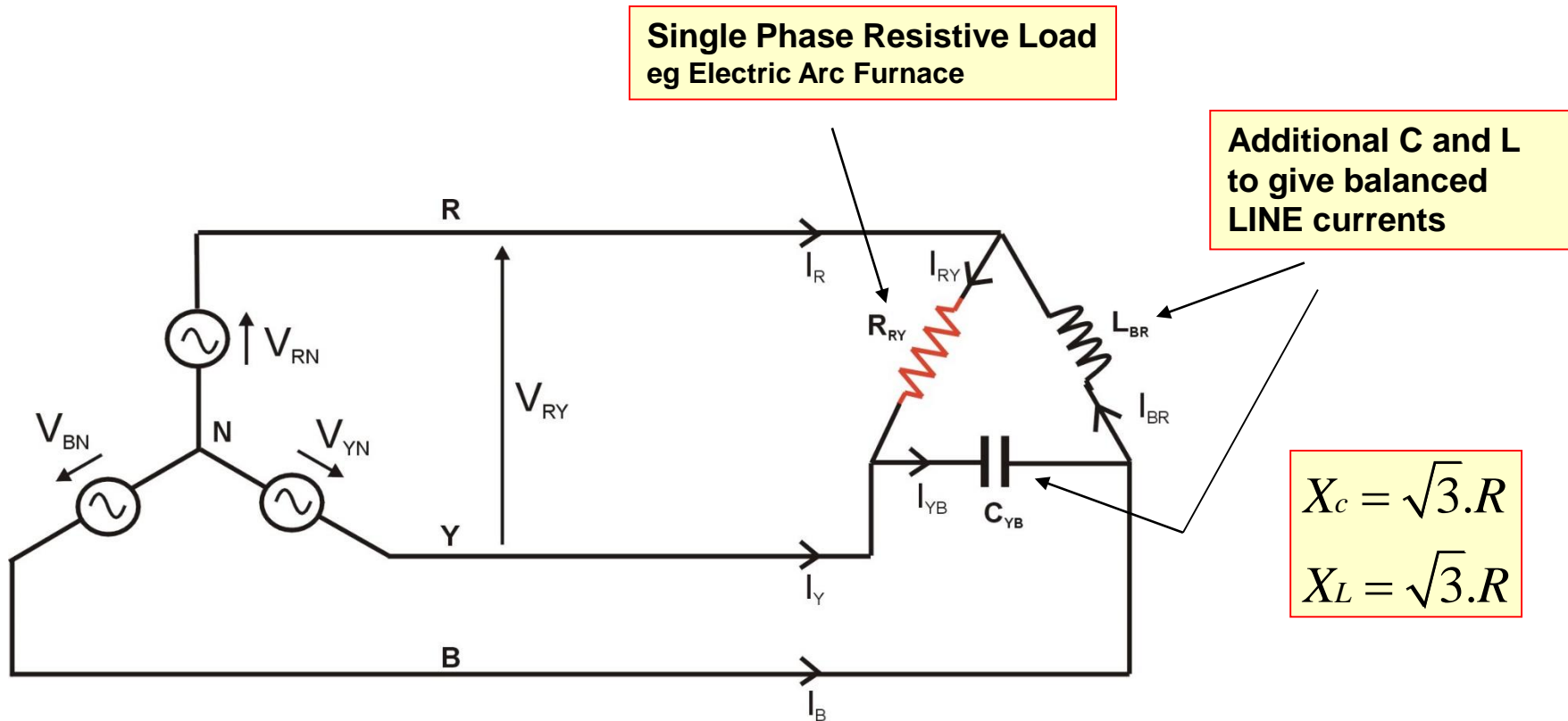
$$I_Y = 2040 \angle -102^\circ$$

$$I_B = 2520 \angle 107^\circ$$



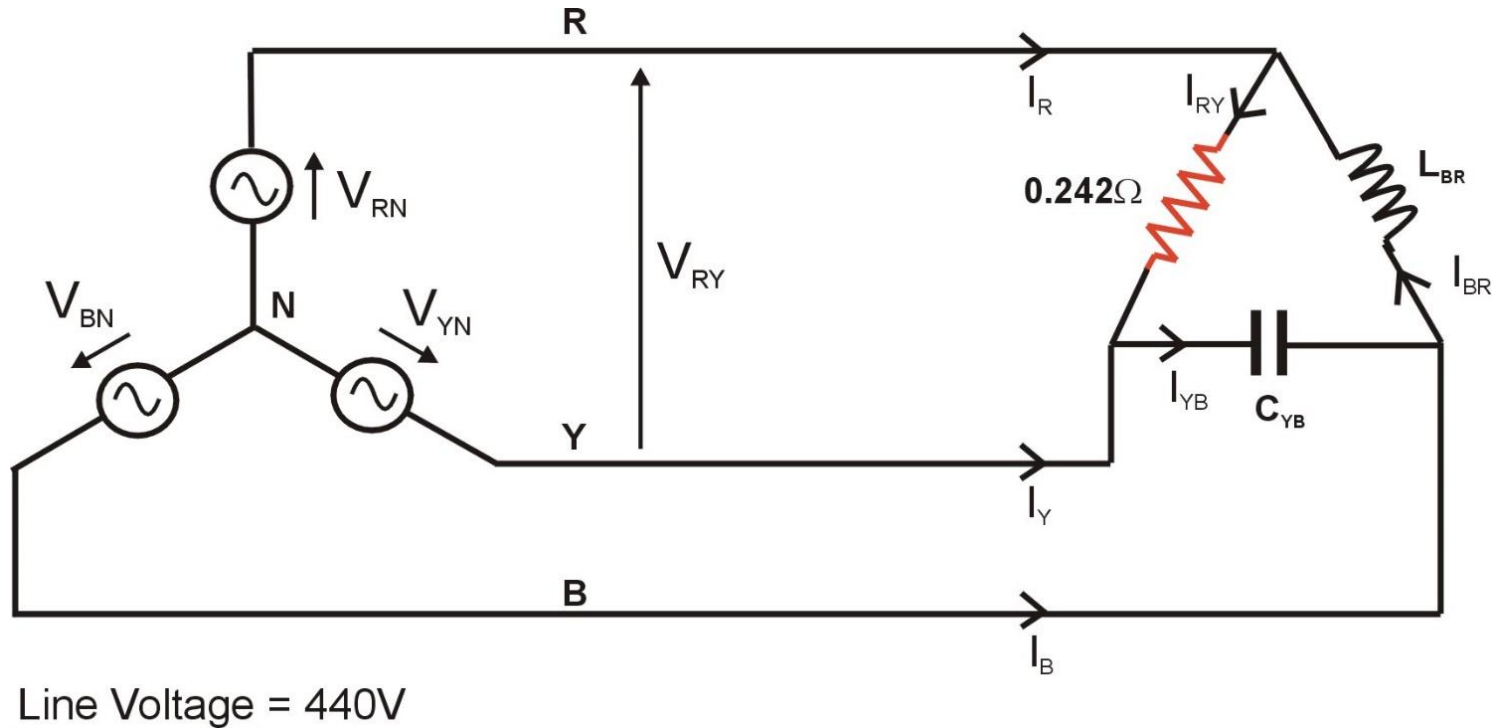
## Unbalanced Delta connected load example #2:

### Connecting a large single phase load to a 3 phase system



**Note: the relative positions of L and C is essential for balanced operation**

# Example

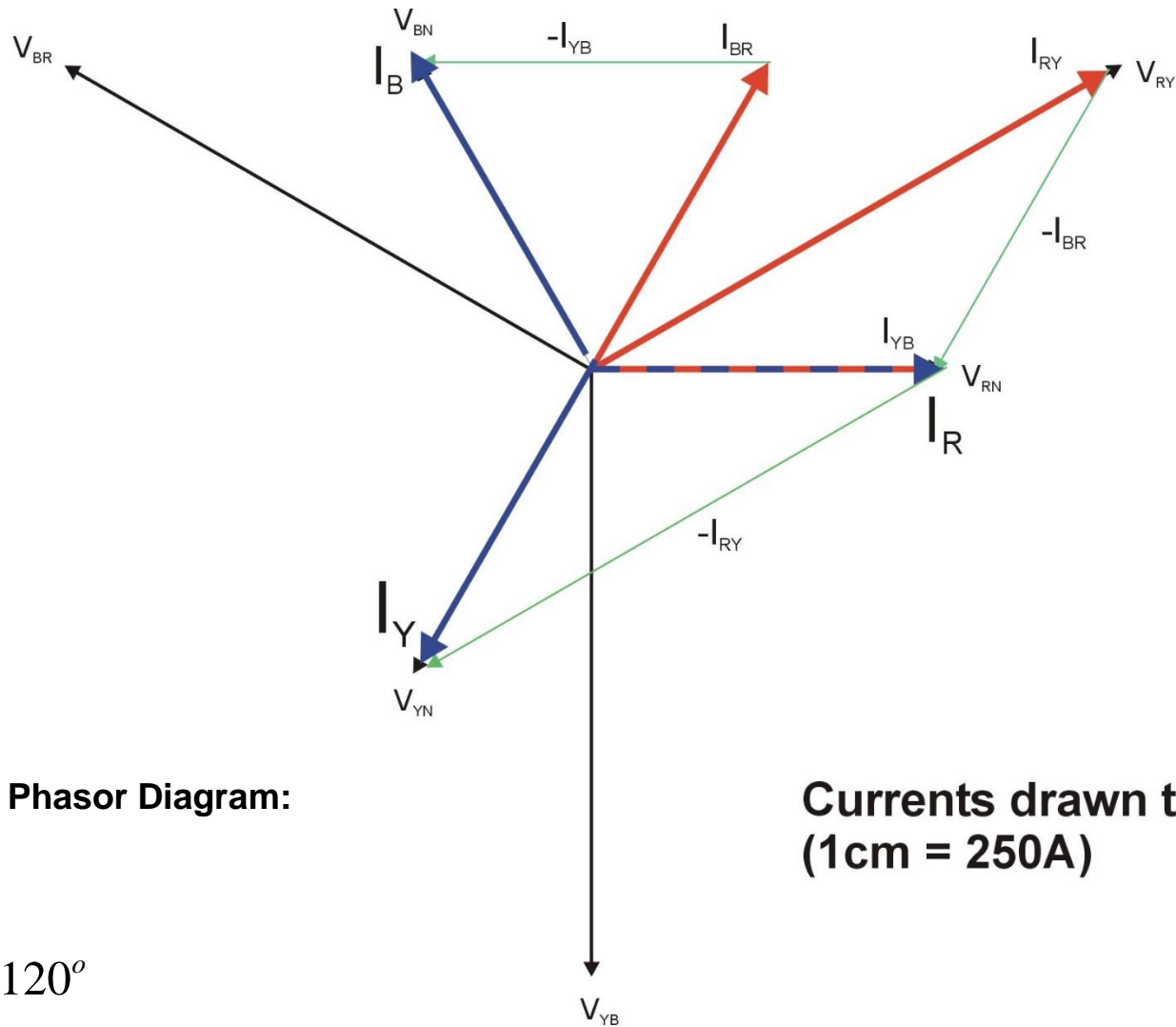


Determine:

- 1] The Output Power (W) of the single phase load
- 2] The magnitude of the line currents for single phase load only connection
- 3] The line currents (phasors) for the balanced RCL configuration

**Solution done on Whiteboard**





**Estimated from Phasor Diagram:**

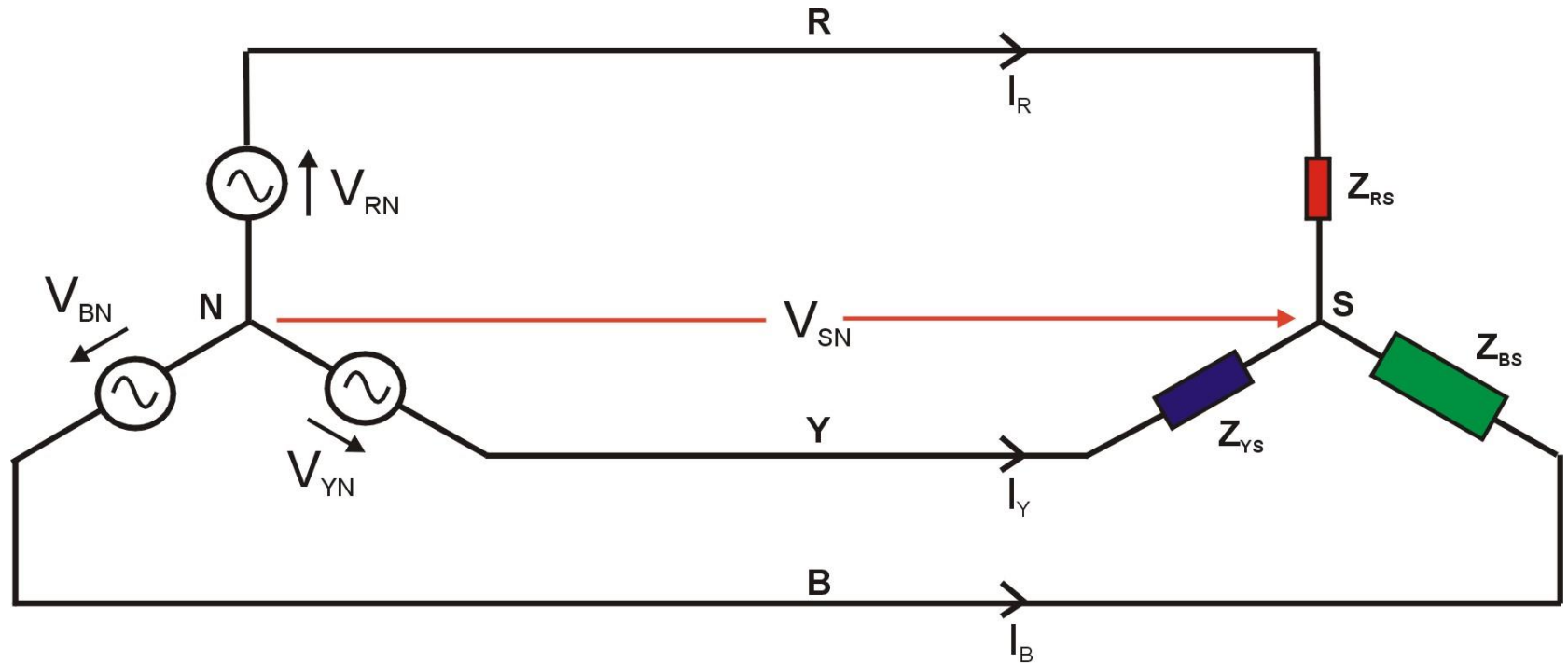
$$I_R = 1050 \angle 0^\circ$$

$$I_Y = 1050 \angle -120^\circ$$

$$I_B = 1050 \angle 120^\circ$$

**Currents drawn to scale!  
(1cm = 250A)**

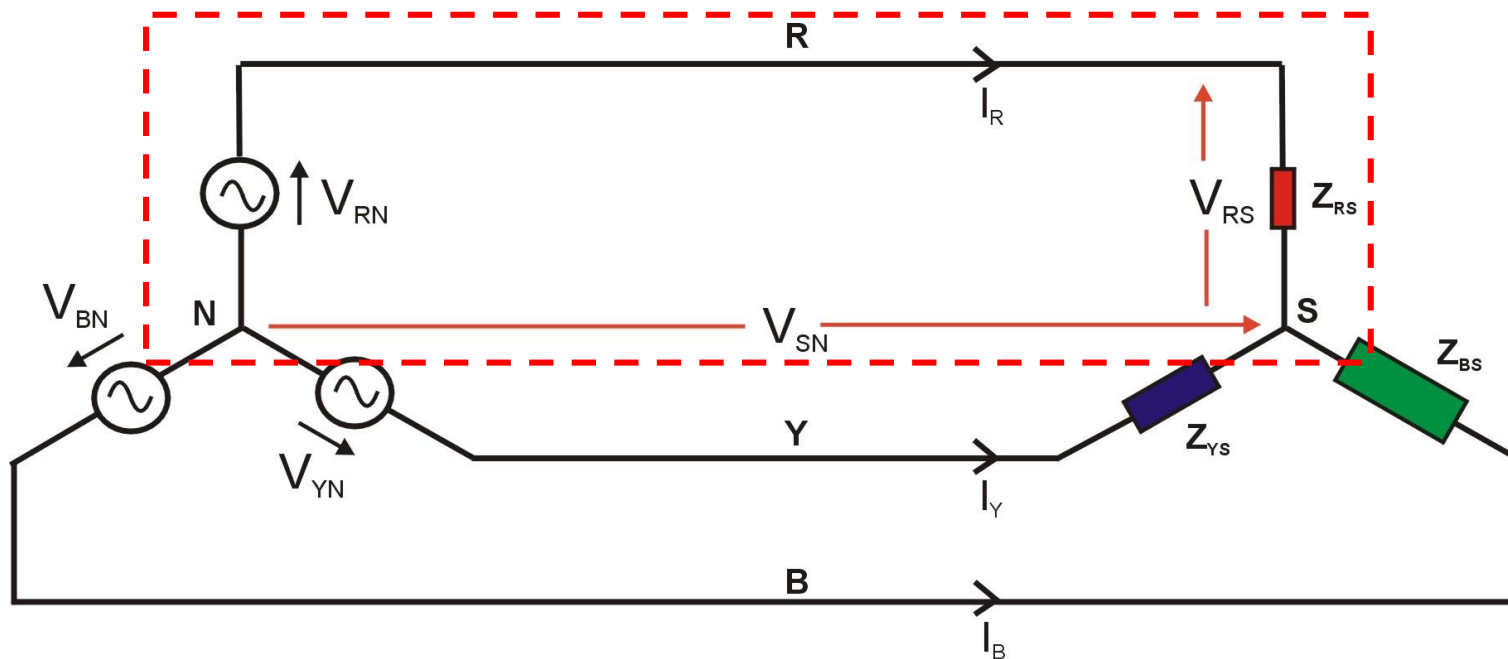
## Unbalanced 3 wire Star connected load:



For the Unbalanced load:  $Z_{RS} \neq Z_{YS} \neq Z_{BS}$

Therefore:  $I_R \neq I_Y \neq I_B$  AND  $V_{SN} \neq 0$

## Unbalanced 3 wire Star connected load:



$$V_{RN} = V_{RS} + V_{SN}$$

$$V_{YN} = V_{YS} + V_{SN}$$

$$V_{BN} = V_{BS} + V_{SN}$$

Note: these are PHASORS

First of all we need to find an equation for  $V_{SN}$

????????????

## Solution:

Step 1: Calculate  $V_{SN}$  using Millman's Theory:

$$V_{SN} = \frac{V_{RN}Y_R + V_{YN}Y_Y + V_{BN}Y_B}{Y_R + Y_Y + Y_B}$$

Note: Y are admittances

Step 2: Calculate load phase voltages:

$$V_{RS} = V_{RN} - V_{SN}$$

$$V_{YS} = V_{YN} - V_{SN}$$

$$V_{BS} = V_{BN} - V_{SN}$$

Step 3: Calculate line currents:

$$I_R = \frac{V_{RS}}{Z_{RS}}$$

$$I_Y = \frac{V_{YS}}{Z_{YS}}$$

$$I_B = \frac{V_{BS}}{Z_{BS}}$$

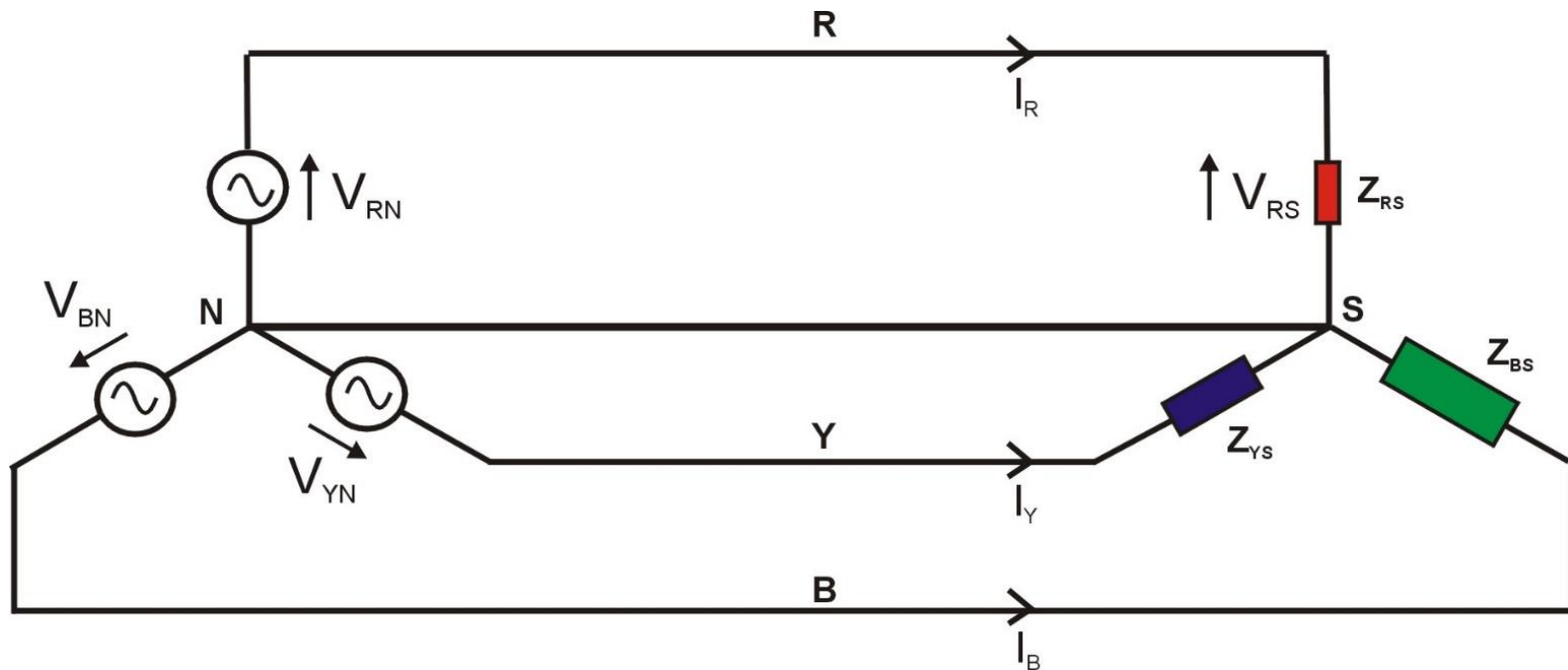
Step 4: Calculate Total Real Power:

$$P_T = |V_{RN}| \cdot |I_R| \cdot \cos\phi_R + |V_{YN}| \cdot |I_Y| \cdot \cos\phi_Y + |V_{BN}| \cdot |I_B| \cdot \cos\phi_B$$

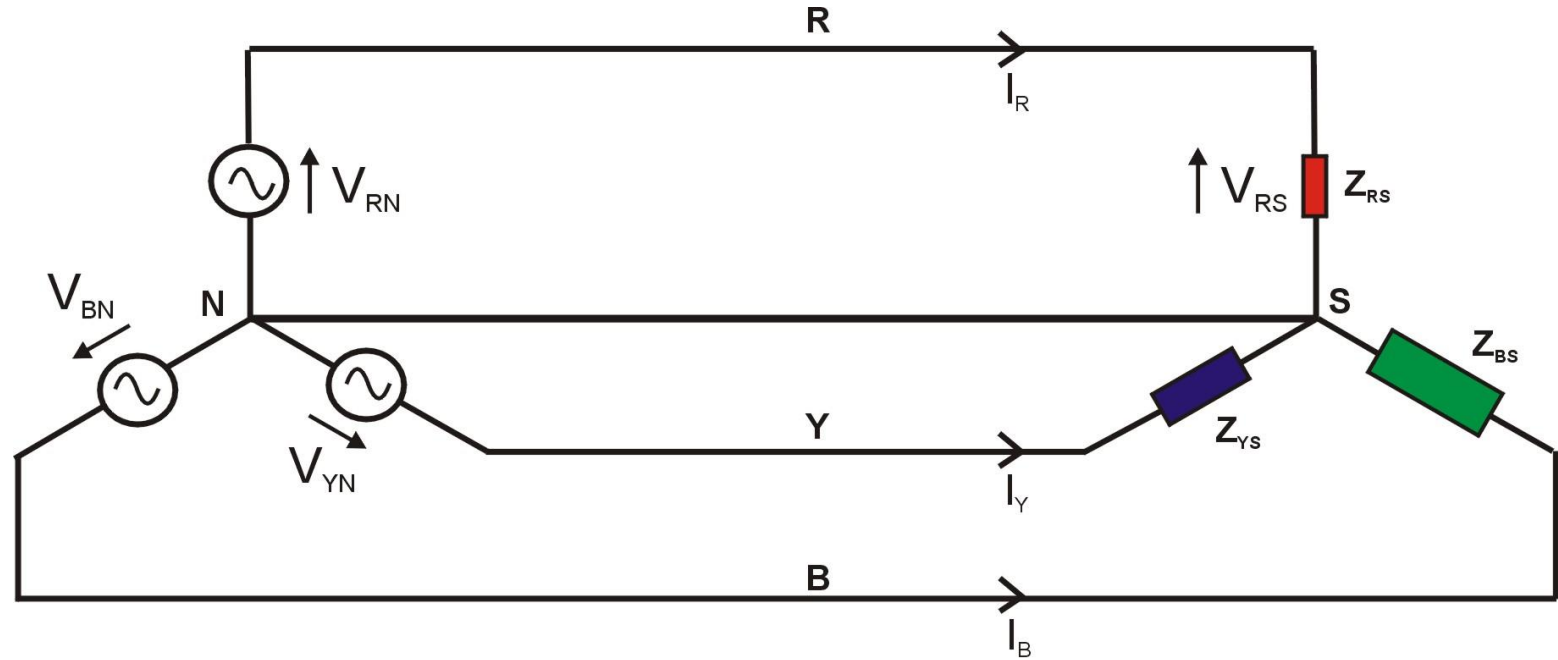
# Unbalanced 4 wire Star connected load:

The most important result of an unbalanced 3 wire Star connected load is that the load phase voltages are no longer equal to the supply phase voltages which could result in dangerous over-voltage conditions in one or more of the phases.

**A** solution is to have a physical connection between the generator neutral and the load star point:



## Unbalanced 4 wire Star connected load:



For the Unbalanced load:  $Z_{RS} \neq Z_{YS} \neq Z_{BS}$

Therefore:  $I_R \neq I_Y \neq I_B$  BUT  **$V_{SN} = 0$**  AND  $V_{RS} = V_{RN}$ ,  $V_{YS} = V_{YN}$  &  $V_{BS} = V_{BN}$

## Solution:

Step 1: Calculate individual line currents:

$$I_R = \frac{V_{RN}}{Z_{RS}}$$

$$I_Y = \frac{V_{YN}}{Z_{YS}}$$

$$I_B = \frac{V_{BN}}{Z_{BS}}$$

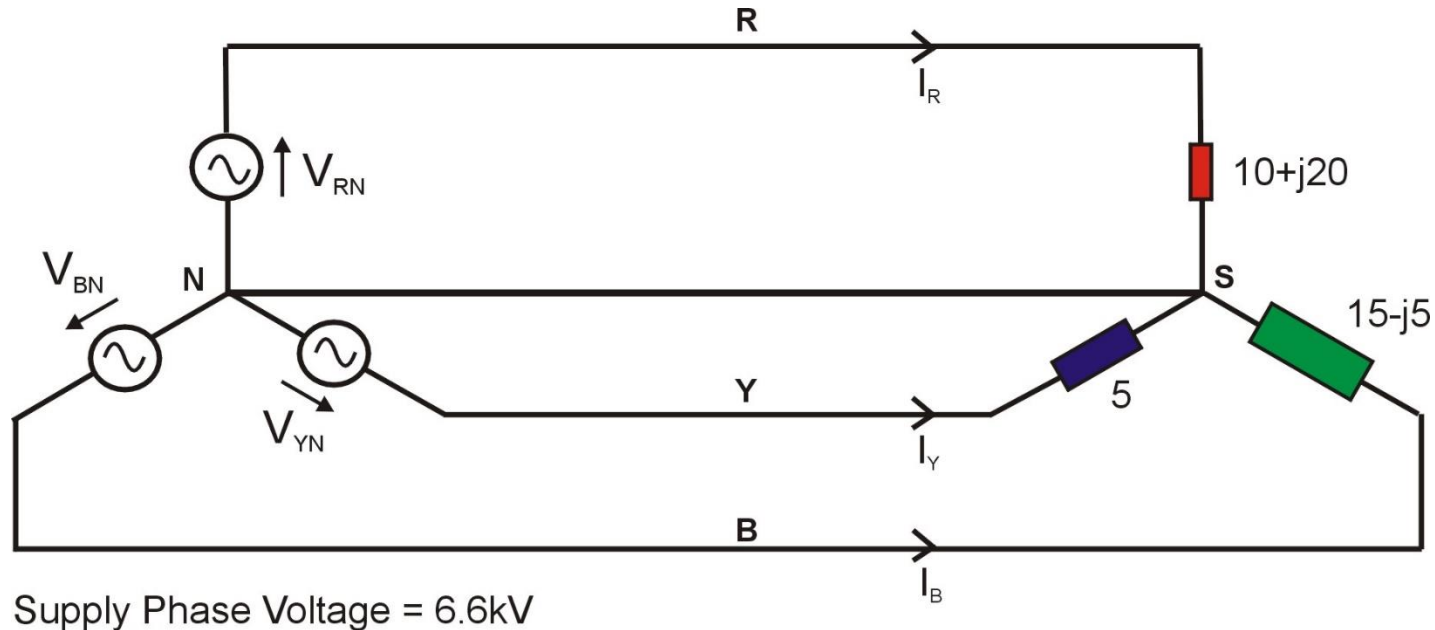
Step 2: Calculate Total Real Power:

$$P_T = |V_{RN}| \cdot |I_R| \cdot \cos\phi_R + |V_{YN}| \cdot |I_Y| \cdot \cos\phi_Y + |V_{BN}| \cdot |I_B| \cdot \cos\phi_B$$

Note we can also calculate the current flowing down the Star-Neutral connection:

$$I_{SN} = I_R + I_Y + I_B$$

**Example:** a contractor is required to install a Star/Neutral connection. They are proposing using 10mm diameter wire – will this be sufficient?

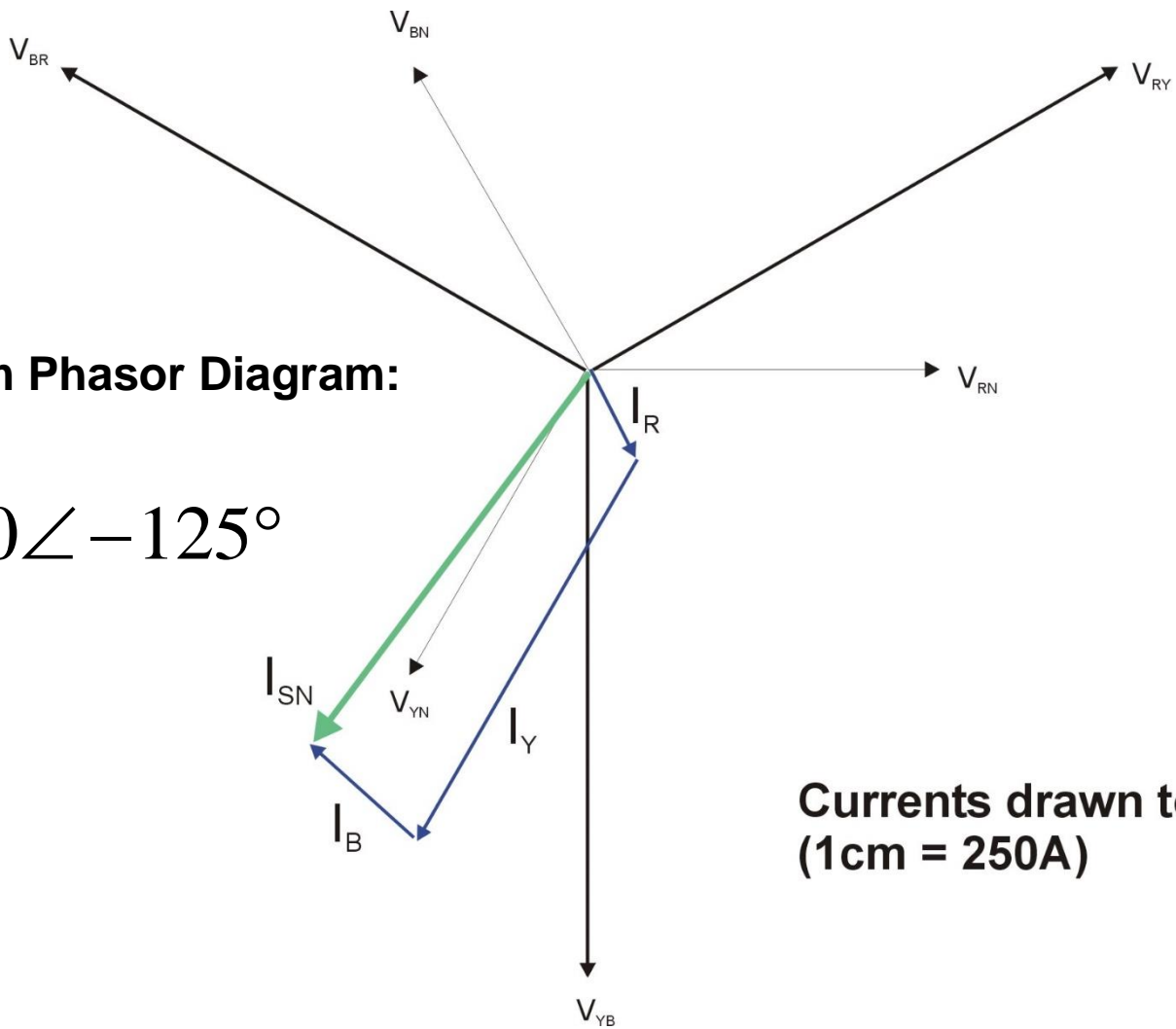


Determine:

- 1] All the line currents
- 2] The Star/Neutral line current
- 3] The current density ( $A/mm^2$ ) in the Star/Neutral connection



**Solution done on Whiteboard**



**Estimated from Phasor Diagram:**

$$I_{SN} = 1400 \angle -125^\circ$$

**Currents drawn to scale!  
(1cm = 250A)**

# Application of 3 Wattmeter and 2 Wattmeter Methods

	3 Wattmeter	2 Wattmeter
Balanced Star Load		
Balanced Delta Load		
Unbalanced Delta Load		
Unbalanced 3 wire Star Load		
Unbalanced 4 wire Star Load		