

# 生物系統模擬

## Modeling and Simulation in Systems Biology

BEBI 5009

星期四 2,3,4

明達203

# Contact

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- Office hour: Friday afternoon or by appointment
  
- Course website: <https://ceiba.ntu.edu.tw/1062BEBI5009/>

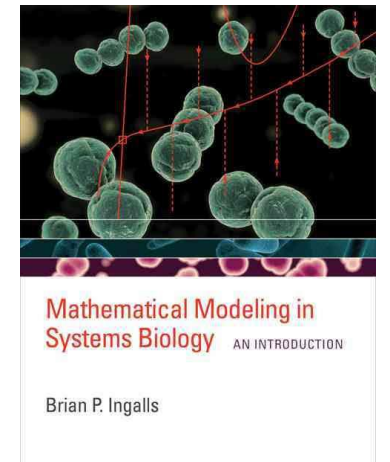
# Course introduction

- System techniques are integral to current research in molecular cell biology.
- System level investigations are often accompanied by mathematical models.
- These models serves as working hypothesis.
- They help us to understand and predict the behavior of complex systems.
- This course offer an introduction to mathematical concepts and techniques needed for the construction and interpretation of models in molecular systems biology

# Course objective

- Mathematical modelling is becoming an important tool for molecular and cell biology.
- Introduction to the key concepts that are needed for the construction and investigation of mathematical models in molecular systems biology
- Learning fundamental tools and modeling techniques to develop and apply quantitative models of cellular systems.
- Current topics in systems biology

# TEXTBOOK & Readings



- Mathematical Modeling in Systems Biology(2013), by Brian P. Ingalls
- [https://www.math.uwaterloo.ca/~bingalls/MMSB/MMSB\\_w\\_solutions.pdf](https://www.math.uwaterloo.ca/~bingalls/MMSB/MMSB_w_solutions.pdf)
- [https://www.math.uwaterloo.ca/~bingalls/MMSB/MMSB\\_code.xhtml](https://www.math.uwaterloo.ca/~bingalls/MMSB/MMSB_code.xhtml)
- Hard copy is in NTU library

## References:

- Stochastic Modelling for Systems Biology(2011) by Darren J. Wilkinson (ebook in NTU library)

# Evaluation

編號	項目	百分比	說明
1	期中考	30%	in class
2	期末報告	30%	書面 + 口頭
3	作業	40%	6-8 HW, 會需要用MATLAB來寫作業

Homework:

# Homework:

- About 4-6 HWs in total, ~biweekly
- Due in 2 week after the HW is distributed. Due date and time will be TBA
- HW is due at 9am on Thursday before the class.
- Late homework will not be accepted for any circumstances.
- Matlab/Python code could be sent by email to me or upload to CEIBA

- Class Attendance:
  - Strongly Recommended
  - I don not take attendance in a regular basis
- Policy on missed exams:
  - Students who experience a serious medical condition or other emergency may be excused
  - He/She must contact the instructor BEFORE the exam (Easiest way is to send me an email)
  - He/She must VERIFY their condition by official documents
  - NO EXCEPTIONS will be made for job interviews, holiday travel, or other non-academic activities
  - No make-up exam (Grades will be adjusted based on other elements)



# Academic Dishonesty

- Violations can include cheating on exams, plagiarism, reuse of assignments without permission, improper use of the Internet and electronic devices, unauthorized collaboration, alteration of graded assignments, forgery, falsification and lying.
- May result in
  - ▲ Failure on an assignment
  - ▲ Failure in a course
  - ▲ Permanent transcript notation
  - ▲ Expulsion

# Tentative course outline

Date	
3月1日	Introduction
3月8日	Introduction to Matlab/Python
3月15日	Systems of differential equations , Separation of Timescales
3月22日	Enzyme kinetics , Cooperativity
3月29日	Phase plane analysis , Stability
4月5日	放假日
4月12日	Sensitivity analysis; Parameter fitting
4月19日	Review
4月26日	期中考
5月3日	Stochastic processes and simulation
5月10日	Stochastic Modeling
5月17日	Gene regulatory networks; Invited talk Dr. Wen Hao-Jui
5月24日	Signal transduction pathways
5月31日	Metabolic network
6月7日	Oral presentation
6月14日	Oral presentation
6月21日	Term project due

# Ch1-4: mathematical modelling in molecular systems biology

- Chapter 1 introduces molecular systems biology and describes some basic notions of mathematical modelling, concluding with four short case-studies.
- Chapter 2 introduces dynamic mathematical models of chemical reaction networks. These are differential equation models based on mass-action rate laws. Some basic methods for analysis and simulation are described.
- Chapter 3 covers biochemical kinetics, providing rate laws for biochemical processes (i.e. enzyme-catalysed reactions and cooperative binding). The last section treats common approximation methods.
- Chapter 4 introduces techniques for analysis of differential equation models, including phase plane analysis, stability, bifurcations, and sensitivity analysis.

# Ch 5-8: specific biological domain

- Chapter 5 covers modelling of metabolic networks. Sensitivity analysis plays a central role in the investigation of these models. The last section introduces stoichiometric modelling, which is often applied to large-scale metabolic networks.
- Chapter 6 addresses modelling of signal transduction pathways. The examples taken up in this chapter survey a range of information-processing tasks performed by these pathways. The last section introduces the use of frequency-response analysis for studying cellular input-output systems.
- Chapter 7 introduces modelling of gene regulatory networks. The chapter starts with a treatment of gene expression, then presents examples illustrating a range of gene-circuit functions. The final section introduces stochastic modelling in molecular systems biology.
- Chapter 8 covers modelling of electrophysiology and neuronal action potentials. One section contains a brief introduction to spatial modelling using partial differential equations.

- Essential biological concepts and mathematical fundamentals will be reviewed.
- Introduction of Python/MATLAB programming.

# XPPAUT

- a freely available program that that was written specifically for dynamic modelling
- <http://www.math.pitt.edu/~bard/xpp/installonwindows.html>

# MATLAB

- NTU App Share
- EE電二130 (or 132) , 電機系大學部學生
- SciLab (free): <http://www.scilab.org/>
- Octave (free): <https://www.gnu.org/software/octave/>
- Tutorials
- <https://www.mathworks.com/support/learn-with-matlab-tutorials.html>
- Matlab On Ramp

# Learn with MATLAB and Simulink Tutorials

Get started with the basics of MATLAB and Simulink

Learn MATLAB in Just 2 Hours

## Learn MATLAB Basics

MATLAB<sup>®</sup> is the high-level language and interactive environment used by millions of engineers and scientists worldwide. It lets you visualize ideas across disciplines including signal and image processing, communications, control systems, and computational finance.

### Read Documentation Basics

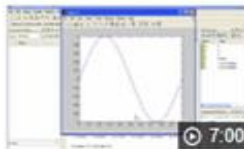
**Desktop Basics:** Enter commands and view results

**Matrices and Arrays:** Create variables that contain multiple values

**Array Indexing:** Access data in an array.

» See more documentation topics

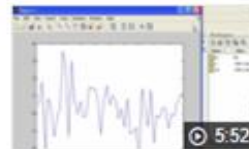
### Watch Introductory Videos



Getting Started with  
MATLAB



Image Processing Made  
Easy



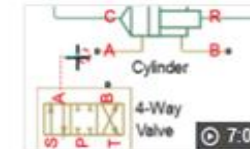
Using Basic Plotting  
Functions



Getting Started with  
Simulink



Physical Modeling with  
Simscape



Modeling a Hydraulic  
Actuation System

## Learn Simulink Basics

Simulink<sup>®</sup> is a block diagram environment for multi-domain simulation and Model-Based Design. It supports simulation, automatic code generation, and continuous test and verification of embedded systems. Simulate dynamic systems leveraging graphical editors, customizable block libraries, and solvers for modeling.

### Read Documentation Basics

**Create a Simple Model:** Build and simulate a model.

**Model a Dynamic System:** Create a dynamic control system.

**Simulate a Dynamic System:** Simulate and evaluate system behavior.

» See more documentation topics

### Watch Introductory Videos



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# 2018 狗年興旺

新禧慶賀

[MATLAB & Simulink](#) / [控制相關產品](#) / [研發管理](#)

》 10/26 新竹喜來登, 美、澳資深科學家來台分享科技趨勢

[活動快遞](#) / [線上技術研討會](#) / [產品新聞與資源中心](#)

- 2018 MATLAB & Simulink 免費體驗課程, 培養跨領域技能, 打造多工優勢最佳選擇! 人工智慧(AI)應用/工業4.0/智慧工廠/物聯網/深度學習/資料解析/金融科技/機器人。 2/1起開始報名!迅速額滿請把握機會!
- Polyspace程式碼分析和驗證工具, 幫您分析系統中難以察覺的程式錯誤。免費上機操作體驗課程, 12/14(四)新竹, 現在就報名!
- MATLAB & Simulink 最新版本R2017b發佈, 深度學習時代來臨! 更快更新的處理! 新增文本分析工具箱、MATLAB-GPU轉碼器、LTE系統電路設計工具箱、Simulink需求管理工具、Simulink驗證標準檢測工具 和Simulink程式碼覆盖率測試工具 了解更多!

>> 活動總覽



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[產品資源中心](#) / [免費體驗課程](#) / [產品型錄下載](#) / [下載技術文件](#) / [看產品操作示範檔](#) / [參加線上產品技術說明會](#) / [索取技術文件組合套件](#)

最專業的技术及服务團隊

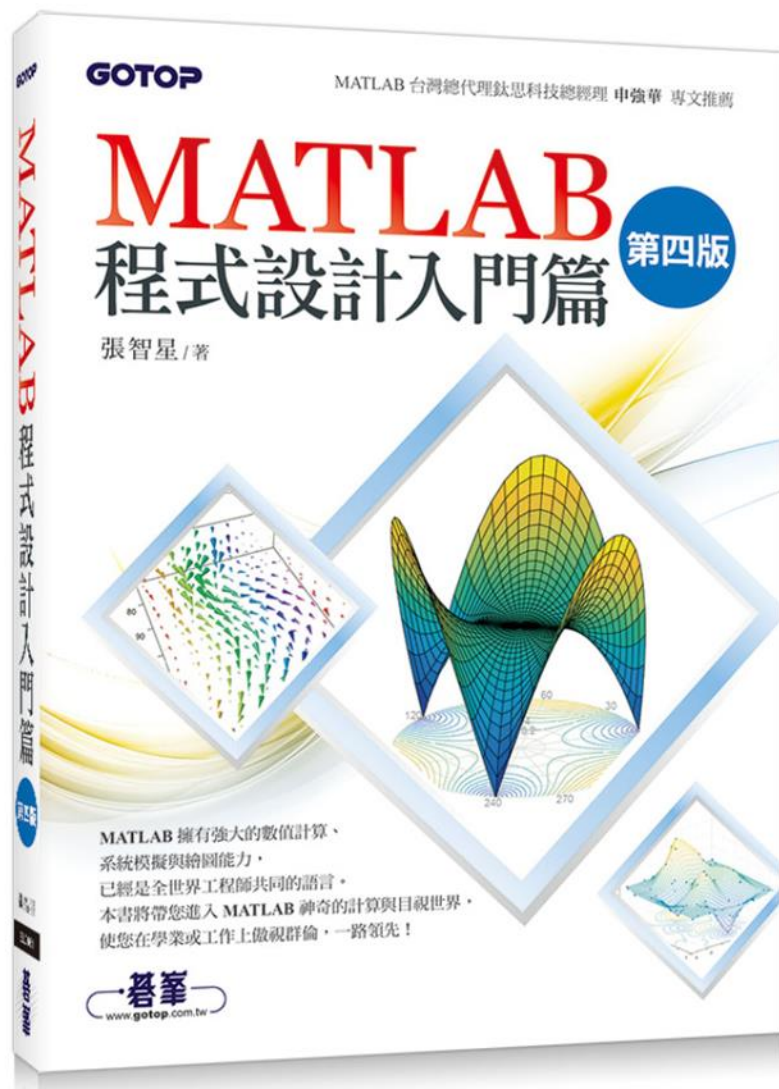
<https://www.terasoft.com.tw/>

<https://www.terasoft.com.tw/event/workshops/2018/>

# MATLAB 程式設計【入門篇】

## MATLAB程式設計《入門篇》：投影片 & 教學影片

張智星



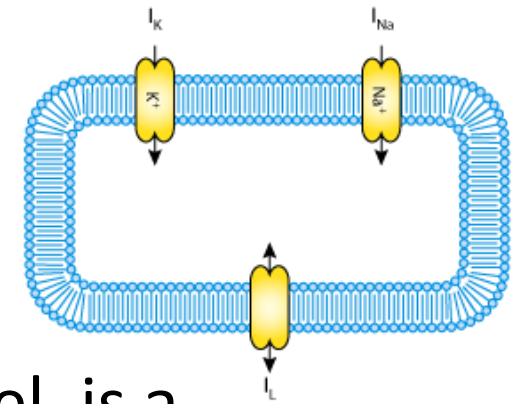
各章主題	投影片	教學影片
MATLAB小傳與外觀	01-MATLAB小傳與外觀.ppt	按此觀看影片
初探MATLAB	02-初探MATLAB.ppt	按此觀看影片
二維平面繪圖	03-二維平面繪圖.ppt	按此觀看影片
三維立體繪圖	04-三維立體繪圖.ppt	按此觀看影片
特殊圖形	05-特殊圖形.ppt	按此觀看影片
動畫製作	06-動畫製作.ppt	按此觀看影片
握把式圖形與 GUI 設計	07-握把式圖形與 GUI 設計.ppt	按此觀看影片
GUIDE	08-GUIDE.ppt	
矩陣的處理與運算	09-矩陣的處理與運算.ppt	按此觀看影片
字元與字串	10-字元與字串.ppt	按此觀看影片
多維陣列	11-多維陣列.ppt	按此觀看影片
異質陣列	12-異質陣列.ppt	按此觀看影片
結構陣列	13-結構陣列.ppt	按此觀看影片
MATLAB 的運算元	14-MATLAB 的運算元.ppt	
M檔案	15-M檔案.ppt	
程式流程控制	16-程式流程控制.ppt	按此觀看影片
程式除錯	17-程式除錯.ppt	按此觀看影片
檔案讀寫	18-檔案讀寫.ppt	按此觀看影片
影像顯示與讀寫	19-影像顯示與讀寫.ppt	按此觀看影片
音訊讀寫、錄製與播放	20-音訊讀寫、錄製與播放.ppt	按此觀看影片

# MATLAB 程式設計【入門篇】：

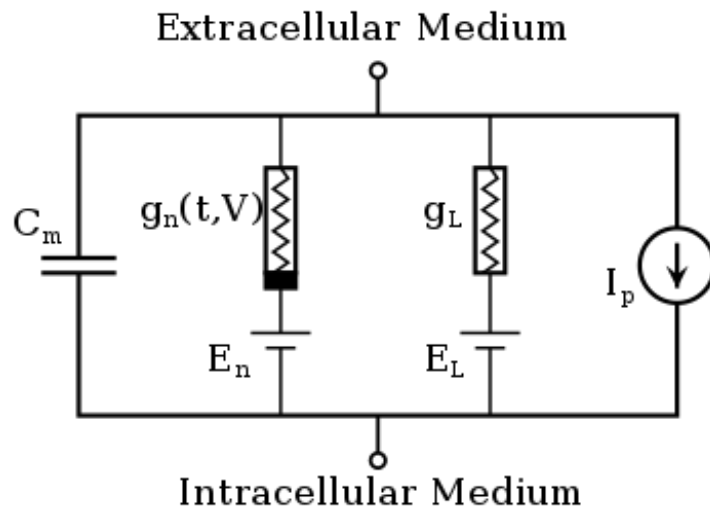
MATLAB程式設計：入門篇	
Roger Jang (張智星)	
<ul style="list-style-type: none"><li>• 本線上教材已經付梓成書，請見「<a href="#">峯峰連結</a>」。</li><li>• 姊妹作：<a href="#">MATLAB程式設計：進階篇</a></li><li>• Download: [<a href="#">all examples</a>] [<a href="#">all slides</a>]</li></ul>	
您是來自 140.112.175.36 的貴賓，您已點閱本站網頁 2 次。（從 2015/8/24 至今的點閱次數： <a href="#">90392</a> ）	
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Chapter 1: MATLAB 小傳與外觀	
本章介紹 MATLAB 與 MathWorks 公司的背景與歷史，並說明 MATLAB 第八版的外觀。 <a href="#">[Video]</a> <a href="#">[Slides]</a>	
<a href="#">1-1：MATLAB 小傳</a>	
<a href="#">1-2：MATLAB 第八版外觀</a>	
<a href="#">Chapter 1: Exercises</a>	
Chapter 2: 初探MATLAB	
本章介紹 MATLAB 的基本環境與操作，如果您是 MATLAB 的初學者，建議您先熟悉本章各節的內容，可讓您很快地進入情況，立即享用 MATLAB 的簡潔與方便。當然，如果您是MATLAB 老手，就可以直接跳到後面各章節，研讀各個相關主題。 <a href="#">[Video]</a> <a href="#">[Slides]</a> <a href="#">[Examples]</a>	
<a href="#">2-1：使用變數與基本運算</a>	
<a href="#">2-2：向量與矩陣的處理</a>	
<a href="#">2-3：常用數學函數</a>	
<a href="#">2-4：程式流程控制</a>	
<a href="#">2-5：M 檔案</a>	
<a href="#">2-6：搜尋路徑</a>	
<a href="#">2-7：工作空間與變數的儲存及載入</a>	
<a href="#">Chapter 2: Exercises</a>	
Chapter 3: 二維平面繪圖	
MATLAB 不但擅長矩陣相關的各種數值運算，也具有非常強大的繪圖功能，特別適用於各種科學目視表示法（Scientific Visualization）。本章將介紹 MATLAB 的基本二維（平面）繪圖功能，其他更高階的繪圖功能，將在後續章節逐一介紹。 <a href="#">[Video]</a> <a href="#">[Slides]</a> <a href="#">[Examples]</a>	
<a href="#">3-1：基本的二維繪圖指令</a>	
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<a href="#">3-5：其他平面繪圖指令</a>	
<a href="#">Chapter 3: Exercises</a>	
Chapter 4: 三維立體繪圖	



# Hodgkin–Huxley model



- The Hodgkin–Huxley model, or conductance-based model, is a mathematical model that describes how action potentials in neurons are initiated and propagated. It is a set of nonlinear differential equations that approximates the electrical characteristics of excitable cells such as neurons and cardiac myocytes.



Mathematically, the current flowing through the lipid bilayer is written as

$$I_c = C_m \frac{dV_m}{dt}$$

and the current through a given ion channel is the product

$$I_i = g_n(V_m - V_i)$$

where  $V_i$  is the **reversal potential** of the  $i$ -th ion channel. Thus, for a cell with sodium and potassium channels, the total current through the membrane is given by:

$$I = C_m \frac{dV_m}{dt} + g_K(V_m - V_K) + g_{Na}(V_m - V_{Na}) + g_l(V_m - V_l)$$

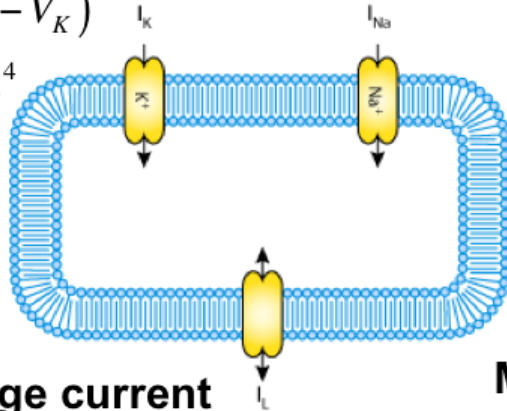
# Hodgkin-Huxley Model

<https://models.cellml.org/e/e1/tutorial>

## Potassium current

$$I_K = g_K (V - V_K)$$

$$g_K = g_{K_{\max}} n^4$$



## Leakage current

$$I_{\text{leak}} = g_{\text{leak}_{\max}} (V - V_{\text{leak}})$$

## Sodium current

$$I_{Na} = g_{Na} (V - V_{Na})$$

$$g_{Na} = g_{Na_{\max}} m^3 h$$

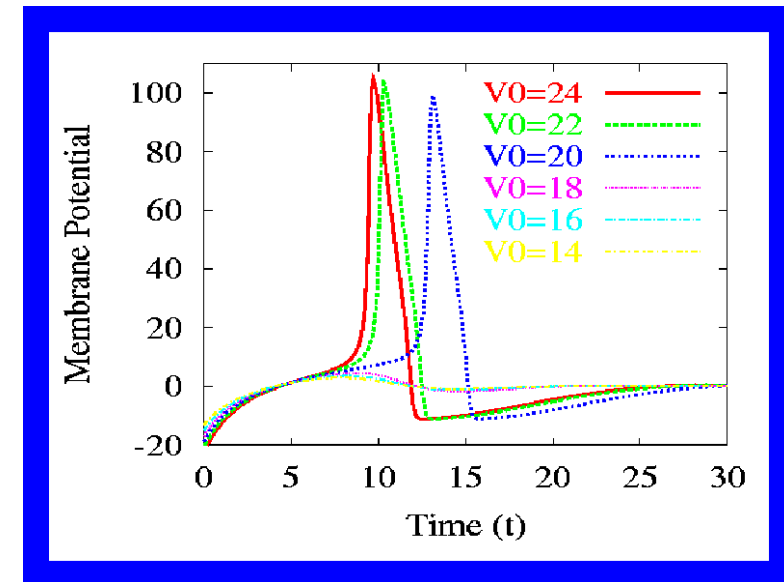
## Gates ( $n, m, h$ )

$$\frac{dX}{dt} = \alpha_X (1 - X) - \beta_X X$$

## Membrane potential

$$\frac{dV}{dt} = \frac{I_{\text{stim}} - (I_K + I_{Na} + I_{\text{leak}})}{C_m}$$

ophysical mechanism for the generation of action potentials.



## Probabilities of Channel Opening

$$\frac{dn}{dt} = \alpha_n (1 - n) - \beta_n n$$

$$\frac{dm}{dt} = \alpha_m (1 - m) - \beta_m m$$

$$\frac{dh}{dt} = \alpha_h (1 - h) - \beta_h h$$

## Membrane as a Capacitor

$$C_m \frac{dV}{dt} = I(t)$$

$$I(t) = I_{Na^+} + I_{K^+} - I_L$$

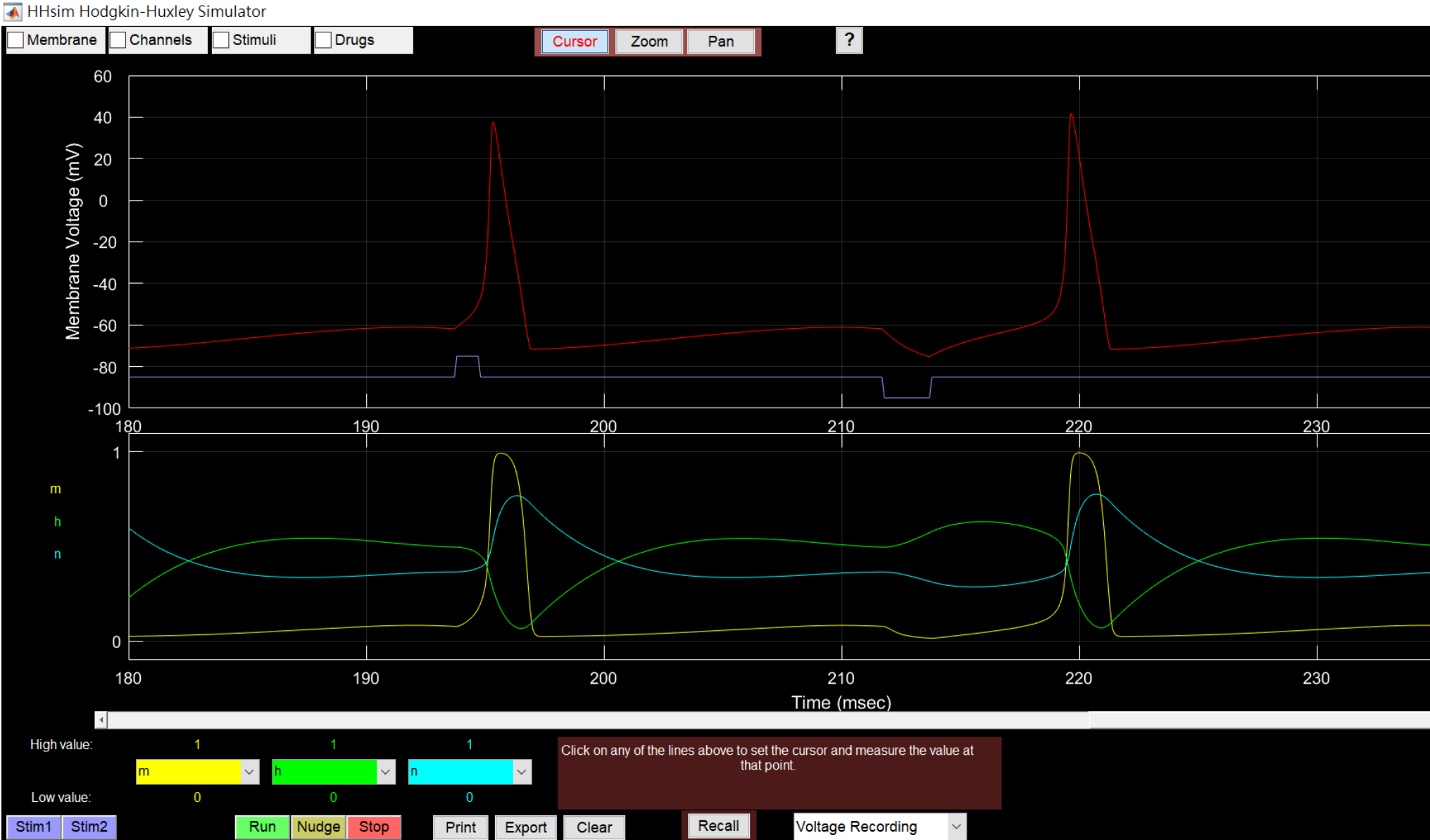
$$I_{K^+} = \bar{g}_K n^4 (V - V_K)$$

$$I_{Na^+} = \bar{g}_{Na} m^3 h (V - V_{Na})$$

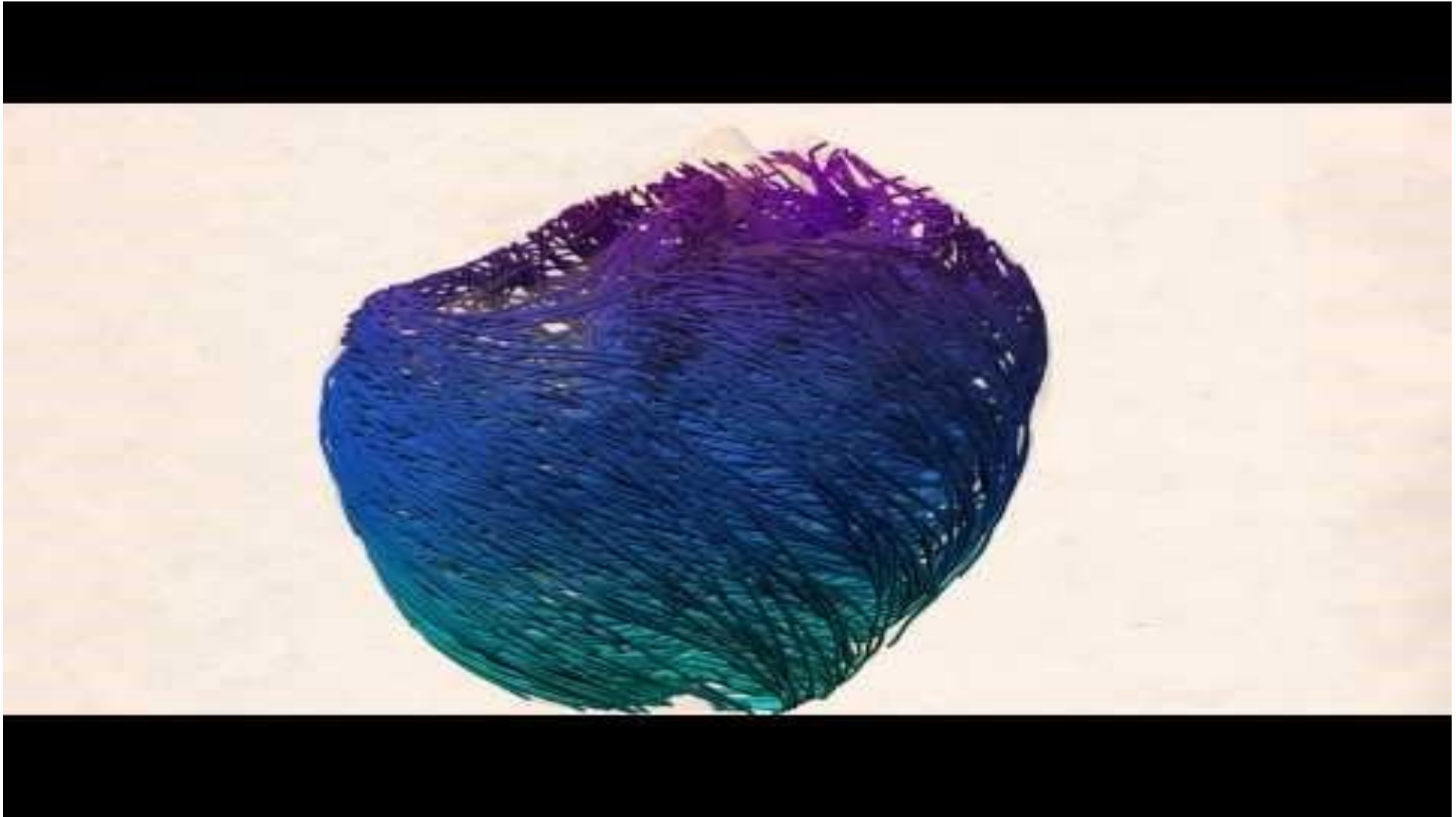
$$I_L = \bar{g}_L (V - V_L)$$

<http://www.amath.washington.edu/~qian/talks/talk5/>

# HHsim



# Alya Red: A Computational heart



<https://www.youtube.com/watch?v=hiKgDOXIPfk>

# Python



- Python is an interpreted high-level programming language for general-purpose programming. Created by Guido van Rossum and first released in 1991, Python has a design philosophy that emphasizes code readability, and a syntax that allows programmers to express concepts in fewer lines of code, notably using significant whitespace. It provides constructs that enable clear programming on both small and large scales.
- Python features a dynamic type system and automatic memory management. It supports multiple programming paradigms, including object-oriented, imperative, functional and procedural, and has a large and comprehensive standard library.



# Pre-Class Survey

- Self introduction
- your major, which year
- Research interest, whose lab you are from
- Why do you take this class?
- What's your expectation of the class?

# TA Time

Python