

```
clear
clc

a = 1:10;
b = 'stybn';
c = [1 1 2; 2 3 4];
who
```

您的变量为:

a b c

whos

| Name | Size | Bytes | Class | Attributes |
|------|------|-------|--------|------------|
| a | 1x10 | 80 | double | |
| b | 1x5 | 10 | char | |
| c | 2x3 | 48 | double | |

```
save a
```

```
clear
load a
who
```

您的变量为:

a b c

whos

| Name | Size | Bytes | Class | Attributes |
|------|------|-------|--------|------------|
| a | 1x10 | 80 | double | |
| b | 1x5 | 10 | char | |
| c | 2x3 | 48 | double | |

实验一 . MATLAB 语言基础

一. MATLAB 的基本计算功能

例1.1.1: 用**Matlab** 显示**430/12**的不同显示结果

```
clear
clc
430/12
```

ans = 35.8333

```
format short
430/12
```

ans = 35.8333

```
format long
430/12
```

```
ans =
    35.833333333333336
```

```
format short e
430/12
```

```
ans =
    3.5833e+01
```

```
format long e
430/12
```

```
ans =
    3.583333333333334e+01
```

```
format hex
430/12
```

```
ans =
    4041eaaaaaaaaab
```

```
format bank
430/12
```

```
ans =
    35.83
```

```
format +
430/12
```

```
ans =
    +
```

```
format rat
430/12
```

```
ans =
    215/6
```

二. MATLAB 矩阵和数组的创建和保存

例1.2.1: 用指令产生数值矩阵

```
clear
```

```
clc
format short

A = [];
x = 9;
y = pi/6;
A = [3 5 sin(y);cos(y) x^2 7;x/2 5 1]
```

```
A = 3×3
    3.0000    5.0000    0.5000
    0.8660   81.0000    7.0000
    4.5000    5.0000    1.0000
```

例1.2.2：矩阵元素的修改

```
A(3,3) = 0
```

```
A = 3×3
    3.0000    5.0000    0.5000
    0.8660   81.0000    7.0000
    4.5000    5.0000         0
```

```
A(2,6) = 1
```

```
A = 3×6
    3.0000    5.0000    0.5000         0         0         0
    0.8660   81.0000    7.0000         0         0    1.0000
    4.5000    5.0000         0         0         0         0
```

例1.2.3：复数矩阵的建立和输入

```
a = 2.7;
b = 13/25;
C = [1 2*a+i*b b*sqrt(a);sin(pi/4) a+5*b 3.5+1]
```

```
C = 2×3 complex
    1.0000 + 0.0000i    5.4000 + 0.5200i    0.8544 + 0.0000i
    0.7071 + 0.0000i    5.3000 + 0.0000i    4.5000 + 0.0000i
```

```
R = [1 2 3 ;4 5 6];
M = [11 12 13 ;14 15 16];
CN = R+i*M
```

```
CN = 2×3 complex
    1.0000 +11.0000i    2.0000 +12.0000i    3.0000 +13.0000i
    4.0000 +14.0000i    5.0000 +15.0000i    6.0000 +16.0000i
```

例1.2.4：符号矩阵的生成

```

a11 = 'a';
a12 = 'b';
a13 = 'c';
a21 = 'Jack';
a22 = 'Help Me!';
a23 = 'No Way!';
sym_matrix = str2sym('[a, b, c;Jack,HelpMe,NoWay ]')

```

```

sym_matrix =

$$\begin{pmatrix} a & b & c \\ \text{Jack} & \text{HelpMe} & \text{NoWay} \end{pmatrix}$$


```

help sym

sym - Create symbolic variables, expressions, functions, matrices

This MATLAB function creates symbolic variable x.

```

x = sym('x')
A = sym('a',[n1 ... nM])
A = sym('a',n)
sym(___,set)
sym(___, 'clear')
sym(num)
sym(num,flag)
sym(strnum)
symexpr = sym(h)

```

另请参阅 `assume`, `double`, `reset`, `str2sym`, `symfun`, `syms`, `symvar`

sym 的文档
名为 sym 的其他函数

```

% sym1 = str2sym('[a,b,c;a21,a22,a23]')
% sym2 = sym([a11,a12,a13;a21,a22,a23])

```

```

sym_digits = str2sym('[1 2 3;a b c;sin(x) cos(y) tan(z)]')

```

```

sym_digits =

$$\begin{pmatrix} 1 & 2 & 3 \\ a & b & c \\ \sin(x) & \cos(y) & \tan(z) \end{pmatrix}$$


```

```

syms a b c;
M1 = sym('Classical');
M2 = sym('Jazz');
M3 = sym('Blues');
syms_matrix = [a b c;M1 M2 M3;2 3 5]

```

```

syms_matrix =

$$\begin{pmatrix} a & b & c \\ \text{Classical} & \text{Jazz} & \text{Blues} \\ 2 & 3 & 5 \end{pmatrix}$$


```

```
Dight_Matrix = [1/3 sqrt(2) 3.4234;exp(0.23) log(29) 23^(-11.23)]
```

```
Dight_Matrix = 2×3
    0.3333    1.4142    3.4234
    1.2586    3.3673    0.0000
```

```
Syms_Matrix = sym(Dight_Matrix)
```

```
Syms_Matrix =
(
    1/3          sqrt(2)          17117/5000
    56682305357268997582476122586655 5174709270083729
    450359962737049622517998136852481014120480182583521197362564300
)
```

例1.2.5：大矩阵的生成

```
example;
```

```
exm = 5×6
    456    468    873     2    579    55
     21    687     54   488     8    13
     65   4567     88    98    21     5
    456     68   4589   654     5   987
   5488    10     9     6    33    77
```

```
size(exm)
```

```
ans = 1×2
     5     6
```

例1.2.6：多维数组的创建

```
A1 = [1 2 3 ;4 5 6 ;7 8 9];
A2 = A1';
A3=A1-A2;
A4(:,:,1) = A1;
A4(:,:,2) = A2;
A4(:,:,3) = A3;
A4
```

```
A4 =
A4(:,:,1) =
     1     2     3
     4     5     6
     7     8     9
```

```
A4(:,:,2) =
     1     4     7
     2     5     8
     3     6     9
```

```
A4(:, :, 3) =
```

| | | |
|---|----|----|
| 0 | -2 | -4 |
| 2 | 0 | -2 |
| 4 | 2 | 0 |

```
A5 = cat(3,A1,A2,A3)
```

```
A5 =
```

```
A5(:, :, 1) =
```

| | | |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

```
A5(:, :, 2) =
```

| | | |
|---|---|---|
| 1 | 4 | 7 |
| 2 | 5 | 8 |
| 3 | 6 | 9 |

```
A5(:, :, 3) =
```

| | | |
|---|----|----|
| 0 | -2 | -4 |
| 2 | 0 | -2 |
| 4 | 2 | 0 |

```
A6 = cat(2,A1,A2,A3)
```

```
A6 = 3×9
```

| | | | | | | | | |
|---|---|---|---|---|---|---|----|----|
| 1 | 2 | 3 | 1 | 4 | 7 | 0 | -2 | -4 |
| 4 | 5 | 6 | 2 | 5 | 8 | 2 | 0 | -2 |
| 7 | 8 | 9 | 3 | 6 | 9 | 4 | 2 | 0 |

```
A7 = cat(1,A1,A2,A3)
```

```
A7 = 9×3
```

| | | |
|---|----|----|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |
| 1 | 4 | 7 |
| 2 | 5 | 8 |
| 3 | 6 | 9 |
| 0 | -2 | -4 |
| 2 | 0 | -2 |
| 4 | 2 | 0 |

```
size(A)
```

```
ans = 1×2
```

| | |
|---|---|
| 3 | 6 |
|---|---|

```
size(A4)
```

```
ans = 1×3
```

| | | |
|---|---|---|
| 3 | 3 | 3 |
|---|---|---|

例1.2.7：产生一个**3×4**随机矩阵

```
R = rand(3,4)
```

```
R = 3×4
    0.2511    0.3517    0.5497    0.7572
    0.6160    0.8308    0.9172    0.7537
    0.4733    0.5853    0.2858    0.3804
```

例1.2.8：产生一个在区间**[10, 20]**内均匀分布的**4**阶随机矩阵

```
a = 10;
b = 20;
x = a+(b-a)*rand(4)
```

```
x = 4×4
    15.6782    17.7917    14.6939    17.9428
    10.7585    19.3401    10.1190    13.1122
    10.5395    11.2991    13.3712    15.2853
    15.3080    15.6882    11.6218    11.6565
```

例1.2.9：产生均值为0.6，方差为**0.1**的**4**阶矩阵

```
mu = 0.6;
sigma = 0.1;
x = mu + sqrt(sigma)*randn(4)
```

```
x = 4×4
    0.6960    1.1413    1.0284    1.0543
    0.4102    0.5386    0.2610   -0.0201
    0.7549   -0.0762    0.9039    0.5375
    0.8338    0.3345    0.6392    0.2180
```

例1.2.10：用**rand** 函数可以产生任意行列的**0~1** 分布的随机矩阵

```
ra = rand(2,4)
```

```
ra = 2×4
    0.9619    0.7749    0.8687    0.3998
    0.0046    0.8173    0.0844    0.2599
```

例1.2.11：利用**diag** 函数产生对角阵

```
a = randn(5,5)
```

```
a = 5×5
    1.0984   -0.8236   -1.3337   -0.2620   -1.1564
   -0.2779   -1.5771    1.1275   -1.7502   -0.5336
    0.7015    0.5080    0.3502   -0.2857   -2.0026
   -2.0518    0.2820   -0.2991   -0.8314    0.9642
```

```
-0.3538    0.0335    0.0229   -0.9792    0.5201
```

```
d = diag(a)
```

```
d = 5×1
    1.0984
   -1.5771
    0.3502
   -0.8314
    0.5201
```

```
D = diag(d)
```

```
D = 5×5
    1.0984         0         0         0         0
         0   -1.5771         0         0         0
         0         0    0.3502         0         0
         0         0         0   -0.8314         0
         0         0         0         0    0.5201
```

例1.2.12: 提取矩阵的子阵

```
B = magic(5)
```

```
B = 5×5
    17    24     1     8    15
    23     5     7    14    16
     4     6    13    20    22
    10    12    19    21     3
    11    18    25     2     9
```

```
B1 = B(1:2,[1 3 5])
```

```
B1 = 2×3
    17     1    15
    23     7    16
```

```
B2 = B([3,1],:)
```

```
B2 = 2×5
     4     6    13    20    22
    17    24     1     8    15
```

```
B([1,3],[2,4])=zeros(2)
```

```
B = 5×5
    17     0     1     0    15
    23     5     7    14    16
     4     0    13     0    22
    10    12    19    21     3
    11    18    25     2     9
```

```
L = B(1,:)<5
```

```
L = 1×5 logical ##
     0     1     1     1     0
```

```
B = B(1,L)
```

```
B = 1×3
     0     1     0
```


例1.2.13: 矩阵的旋转和转置的区别

```
A = [1 2 3 4;5 6 7 8;9 10 11 12];  
B1 = rot90(A)
```

```
B1 = 4×3  
     4     8    12  
     3     7    11  
     2     6    10  
     1     5     9
```

```
BT = A'
```

```
BT = 4×3  
     1     5     9  
     2     6    10  
     3     7    11  
     4     8    12
```

```
B2 = rot90(A,2)
```

```
B2 = 3×4  
    12    11    10     9  
     8     7     6     5  
     4     3     2     1
```

例1.2.14: 矩阵的变维

```
B = reshape(A,2,6)
```

```
B = 2×6  
     1     9     6     3    11     8  
     5     2    10     7     4    12
```

例1.2.15: 部分元素的截取

```
LA = tril(A,-1)
```

```
LA = 3×4  
     0     0     0     0  
     5     0     0     0  
     9    10     0     0
```

```
UA = triu(A,1)
```

```
UA = 3×4  
     0     2     3     4  
     0     0     7     8  
     0     0     0    12
```

```
save mytrix A B
```

```
clear
load mytrix
```

例1.2.16：创建等差数列

```
clear
clc
a = [0:0.5:10];
x = linspace(0,1,75);
a = 1:4;
b = 1:2:7;
c = [b,a]
```

```
c = 1×8
     1     3     5     7     1     2     3     4
```

```
d = [a(1:2:4),4 0.2 8]
```

```
d = 1×5
     1.0000     3.0000     4.0000     0.2000     8.0000
```

例1.2.17：利用函数 **logspace** 创建等比数列

```
logspace(0,2,11)
```

```
ans = 1×11
     1.0000     1.5849     2.5119     3.9811     6.3096    10.0000    15.8489    25.1189 ...
```

例1.2.18：矩阵相加运算

```
A = [1 1 1 ;1 2 3 ;1 3 6];
B = [8 1 6 ;3 5 7 ;4 9 2];
C = A+B
```

```
C = 3×3
     9     2     7
     4     7    10
     5    12     8
```

```
D = A-B
```

```
D = 3×3
    -7     0    -5
    -2    -3    -4
    -3    -6     4
```

例1.2.19：矩阵乘法运算

```
X = [2 3 4 5;1 2 2 1];
Y = [0 1 1;1 1 0;0 0 1;1 0 0];
```

```
Z = X*Y
```

```
Z = 2×3
      8      5      6
      3      3      3
```

```
a = 2*X
```

```
a = 2×4
      4      6      8      10
      2      4      4      2
```

例1.2.20: 矩阵的点积运算

```
X = [-1 0 2];
Y = [-2 -1 1];
Z = dot(X,Y)
```

```
Z = 4
```

```
sum(X.*Y)
```

```
ans = 4
```

例1.2.21: 向量的叉乘

```
a = [1 2 3];
b = [4 5 6];
c = cross(a,b)
```

```
c = 1×3
     -3      6     -3
```

例1.2.22: 计算混合积

```
a = [1 2 3];
b = [4 5 6];
c = [-3 6 -3];
x = dot(a,cross(b,c))
```

```
x = 54
```

例1.2.23: 展开多项式

```
w = conv([1 2 2],conv([1 4],[1 1]))
```

```
w = 1×5
      1      7     16     18      8
```

```
P = poly2str(w,'s')
```

```
P =
```

```
' s^4 + 7 s^3 + 16 s^2 + 18 s + 8'
```

例1.2.24: 矩阵的非整数乘方

```
A = [3 6 7;9 2 5;1 6 3];  
Ap1 = A.^0.3
```

```
Ap1 = 3×3  
    1.3904    1.7118    1.7928  
    1.9332    1.2311    1.6207  
    1.0000    1.7118    1.3904
```

```
pA1 = (0.5)^A
```

```
pA1 = 3×3 complex  
    1.4867 + 0.0000i    0.2124 + 0.0000i   -2.5695 + 0.0000i  
   -13.2981 + 0.0000i    8.4944 + 0.0000i    6.7506 - 0.0000i  
    11.3044 - 0.0000i   -8.2394 + 0.0000i   -4.1478 + 0.0000i
```

```
Ap2 = A.^0.4
```

```
Ap2 = 3×3  
    1.5518    2.0477    2.1779  
    2.4082    1.3195    1.9037  
    1.0000    2.0477    1.5518
```

```
pA2 = (0.4)^A
```

```
pA2 = 3×3 complex  
   -0.7682 - 0.0000i    2.6657 + 0.0000i   -3.0069 + 0.0000i  
  -25.5662 + 0.0000i   14.0796 + 0.0000i   16.4940 - 0.0000i  
   24.9116 - 0.0000i  -15.6848 - 0.0000i  -13.0019 + 0.0000i
```

例1.2.25: 求方程组的解

```
clear  
clc  
A = [5 6 0 0 0;1 5 6 0 0;0 1 5 6 0;0 0 1 5 6;0 0 0 1 5];  
B = [1 0 0 0 1]';  
R_A = rank(A)
```

```
R_A = 5
```

```
X = A\B
```

```
X = 5×1  
    2.2662  
   -1.7218  
    1.0571  
   -0.5940  
    0.3188
```

```
C = [A,B]
```

```
C = 5×6
    5     6     0     0     0     1
    1     5     6     0     0     0
    0     1     5     6     0     0
    0     0     1     5     6     0
    0     0     0     1     5     1
```

```
R = rref(C)
```

```
R = 5×6
    1.0000     0     0     0     0     2.2662
         0    1.0000     0     0     0    -1.7218
         0     0    1.0000     0     0     1.0571
         0     0     0    1.0000     0    -0.5940
         0     0     0     0    1.0000     0.3188
```

例1.2.26：求方程组的一个特解

```
A = [1 1 -3 -1;3 -1 -3 4;1 5 -9 -8];
B = [1 4 0]';
X = A\B
```

警告: 秩亏, 秩 = 2, tol = 8.837264e-15。

```
X = 4×1
     0
     0
 -0.5333
  0.6000
```

```
C = [A,B]
```

```
C = 3×5
     1     1     -3     -1     1
     3    -1     -3     4     4
     1     5     -9     -8     0
```

```
R = rref(C)
```

```
R = 3×5
    1.0000     0    -1.5000     0.7500     1.2500
         0    1.0000    -1.5000    -1.7500    -0.2500
         0     0         0         0         0
```

三. MATLAB 程序设计

例1.3.1：字符变量的输入和检查

```
clear
clc
a = 'this is a string';
isstr(a)
```

```
ans = logical
```

例1.3.2：建立学生档案结构体

```
student_rec.number=1;
student_rec.name='张三'
```

student_rec = 包含以下字段的 struct:

```
number: 1
name: '张三'
```

```
student_rec.height=180;
student_rec.test=[100 80 75;77,60,92;67 28 90;100 89 78];
student_rec
```

student_rec = 包含以下字段的 struct:

```
number: 1
name: '张三'
height: 180
test: [4x3 double]
```

```
student_rec.test
```

```
ans = 4x3
    100     80     75
     77     60     92
     67     28     90
    100     89     78
```

```
b(50,2) = struct(student_rec)
```

b = 包含以下字段的 50x2 struct 数组:

```
number
name
height
test
⋮
```

```
b(43,2).Number=50+43;
b(43,2).Name='李四'
```

b = 包含以下字段的 50x2 struct 数组:

```
number
name
height
test
Number
Name
⋮
```

```
b(43,2).Height=186;
b(43,2).Test=[83 80 78;97 80 72;69 88 80;87 99 100];
b(1,1).weight = 90
```

b = 包含以下字段的 50x2 struct 数组:

```
number
```

```

name
height
test
Number
Name
Height
Test
weight
:
:

```

```
b = rmfield(b,'weight')
```

b = 包含以下字段的 50x2 struct 数组:

```

number
name
height
test
Number
Name
Height
Test
:
:

```

例1.3.3: 用单元数据结构来构造某个学生的档案。

```
B={1,'张三',180,[100 80 75;77,60,92;67,28,90;100,89,78]}
```

```

B = 1x4 cell 数组
    {[1]}    {'张三'}    {[180]}    {4x3 double}

```

```
size(B)
```

```

ans = 1x2
     1     4

```

```
B{4}
```

```

ans = 4x3
    100     80     75
     77     60     92
     67     28     90
    100     89     78

```

```
celldisp(B)
```

```

B{1} =
     1

```

```

B{2} =
张三

```

```

B{3} =
    180

```

B{4} =

| | | |
|-----|----|----|
| 100 | 80 | 75 |
| 77 | 60 | 92 |
| 67 | 28 | 90 |
| 100 | 89 | 78 |

B(3) = []

B = 1x3 cell 数组
{[1]} {张三} {4x3 double}

例1.3.4: 计算向量元素的平均值

```
average(1:100)
```

```
m = 1  
n = 100  
ans = 50.5000
```

```
help average
```

'average' 用于 声明函数。

例1.3.5: 计算 **Matlab** 中特殊值 **EPS**

```
clear  
clc  
EPS = 1;  
num = 0;  
while(1+EPS>1)  
    EPS = EPS/2;  
    num = num + 1;  
end  
num
```

```
num = 53
```

```
EPS
```

```
EPS = 1.1102e-16
```

```
EPS = EPS*2
```

```
EPS = 2.2204e-16
```

```
eps
```

```
ans = 2.2204e-16
```


例1.3.6: 求 **EPS** 的另一种方法

```
EPS = 1;
for num=1:100
    EPS = EPS/2;
    if (1+EPS)<=1
        EPS = 2*EPS;
        break;
    end
end
EPS
```

EPS = 2.2204e-16

num

num = 53

例1.3.7: 折扣问题，购买**2.5**元/斤的苹果，若购买量超过**50**斤，给**20%**的折扣；超过**100**斤，给**30%**的折扣

```
apples = 100;
cost = apples*2.5;
if (apples>50)&&(apples<100)
    cost = 0.8*cost;
elseif apples>100
    cost = 0.7*cost
end
```

例1.3.8: 用 **eval** 产生**5** 阶的**Hilbert** 矩阵

```
n = 5;
t = '1/(i+j-1)';
a = zeros(n);
for i=1:n
    for j=1:n
        a(i,j)=eval(t);
    end
end
a
```

```
a = 5x5
    1.0000    0.5000    0.3333    0.2500    0.2000
    0.5000    0.3333    0.2500    0.2000    0.1667
    0.3333    0.2500    0.2000    0.1667    0.1429
    0.2500    0.2000    0.1667    0.1429    0.1250
    0.2000    0.1667    0.1429    0.1250    0.1111
```

例1.3.9: **feval** 函数的使用

```
disp('函数对应索引值为sin->1,cos->2,log->3')
```

函数对应索引值为sin->1,cos->2,log->3

```
fun = ['sin'; 'cos'; 'log'];  
k = input('选择函数号:')
```

```
k = 1
```

```
x = input('输入要计算的值:')
```

```
x = 67
```

```
feval(fun(k,:),x)
```

```
ans = -0.8555
```

例1.3.10：用递归调用形式计算n的阶乘

```
clear  
clc  
factor(6)
```

```
ans = 720
```

例1.3.11：编写函数 **M** 文件并对其进行调试

```
test(magic(4))
```

```
q = 4.7133e+17
```

```
a = 4x4
```

```
-3.1863    1.0883   -3.5366    3.0117  
-1.9563    2.5800   -0.1965   -0.8170  
-2.6270    1.7545    0.8161    0.2333  
-1.1552    3.3609   -3.0005    3.5246
```

```
a = 4x4
```

```
-3.1863    1.0883   -3.5366    3.0117  
-1.9563    2.5800   -0.1965   -0.8170  
-2.6270    1.7545    0.8161    0.2333  
-1.1552    3.3609   -3.0005    3.5246
```

```
ans = 4x4
```

```
-3.1863    1.0883   -3.5366    3.0117  
-1.9563    2.5800   -0.1965   -0.8170  
-2.6270    1.7545    0.8161    0.2333  
-1.1552    3.3609   -3.0005    3.5246
```

实验二．控制系统时域分析法

例2.1：试绘制出典型二阶系统中，当 $\omega_n = 6$ ， ξ 分别为0.1，0.2，……，1.0，2.0时的单位阶跃响应

```
clear
clc
clf
```

```
Wn = 6
```

```
Wn = 6
```

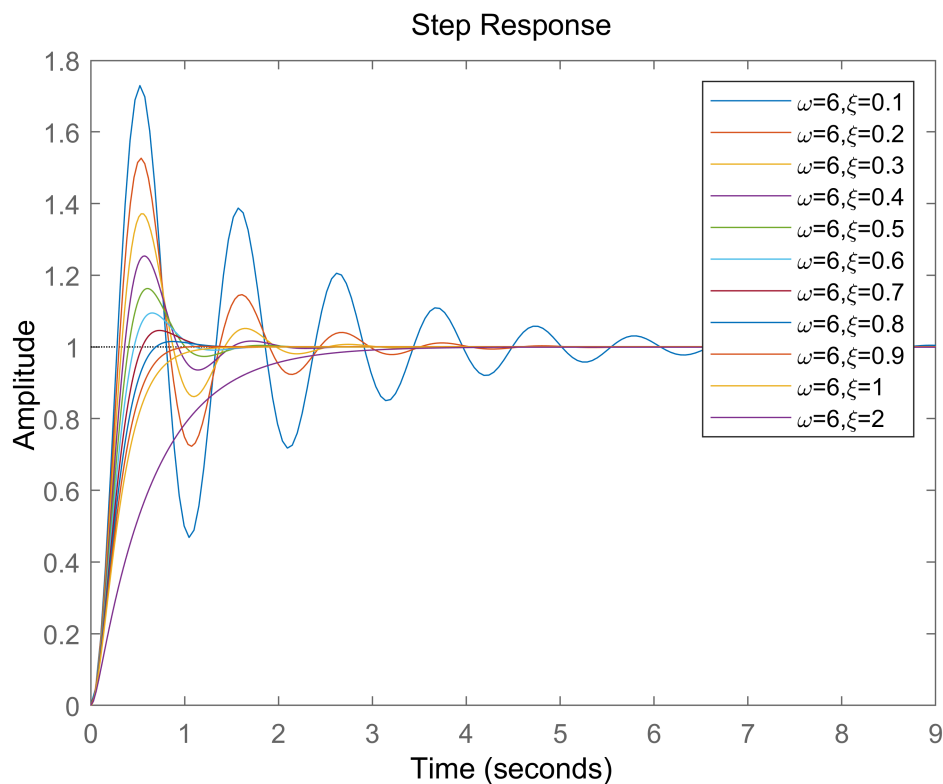
```
kesai = [0.1:0.1:1,2]
```

```
kesai = 1x11
    0.1000    0.2000    0.3000    0.4000    0.5000    0.6000    0.7000    0.8000 ...
```

```
le = [];
x = '\omega=6,\xi=';
hold on
for kos=kesai
    num = Wn^2;
    den = [1,2*kos*Wn,Wn^2];
    step(num,den);

    num2str(kos);
    y = [x,num2str(kos)];
    le = [le,string(y)];

end
legend(le)
hold off
```

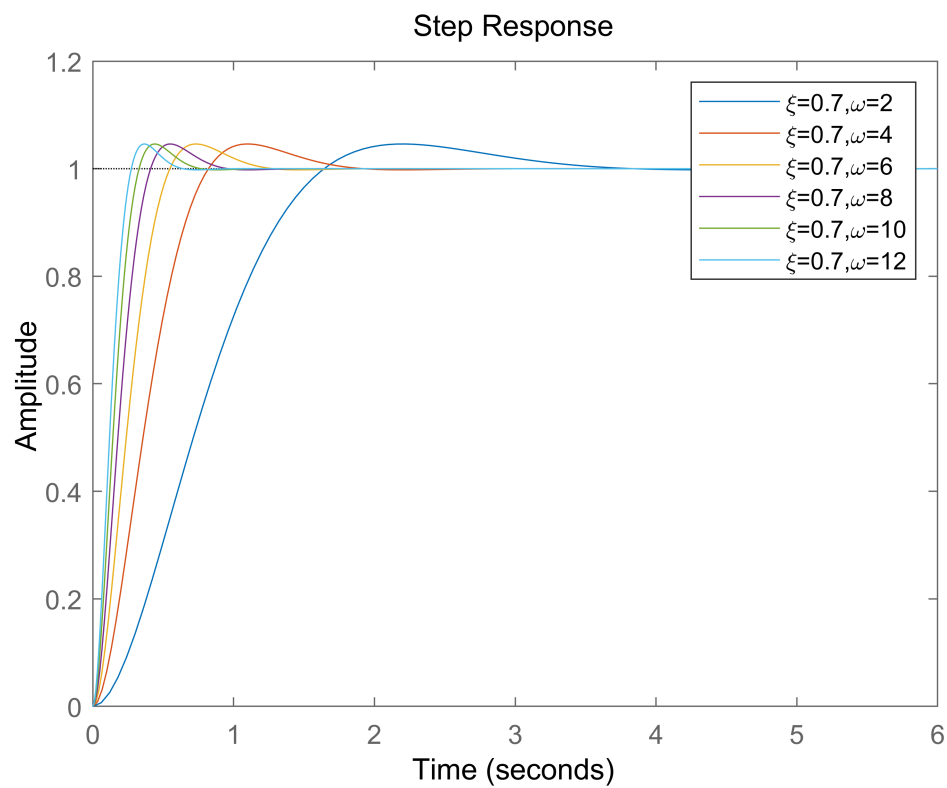


例2.2：绘制出当 $\xi=0.7$ ， ω_n 取2, 4, 6, 8, 10, 12 时的单位阶跃响应

```
clear
clc
clf

le = [];
x = '\xi=0.7,\omega=';
w = [2:2:12];
kesai = 0.7;
hold on
for Wn = w
    num = Wn^2;
    den = [1,2*kesai*Wn,Wn^2];
    step(num,den,6)

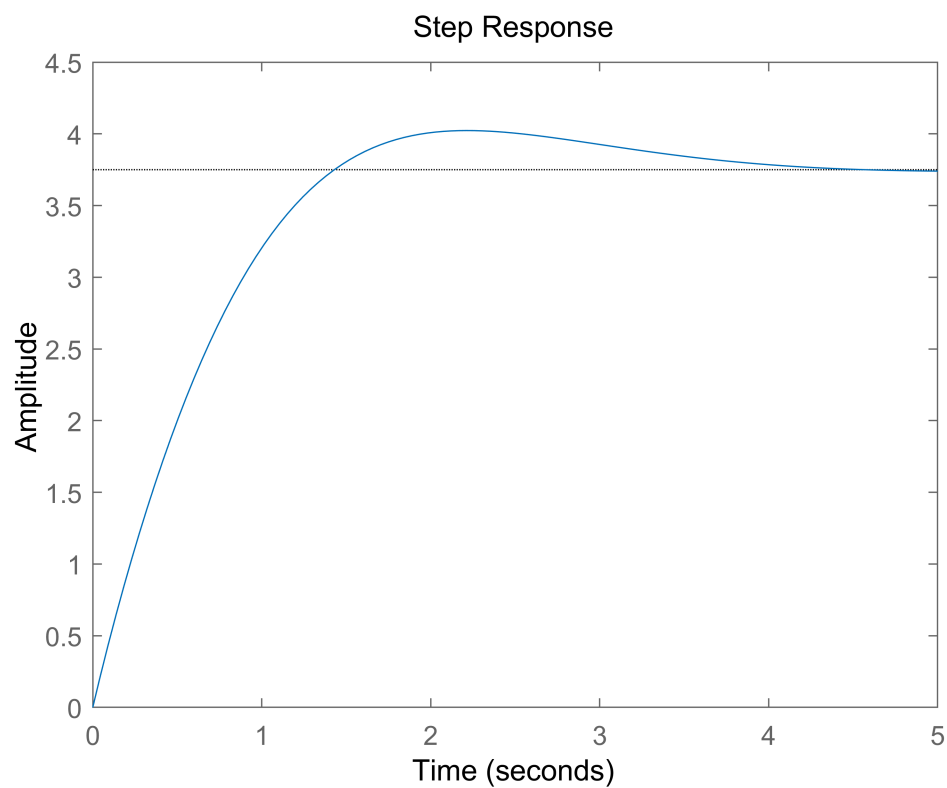
    num2str(Wn);
    y = [x,num2str(Wn)];
    le = [le,string(y)];
end
legend(le)
hold off
```



例2.3：求三阶系统的单位阶跃响应

```
clear
clc
clf

num = [5 25 30];
den = [1 6 10 8];
step(num,den)
```

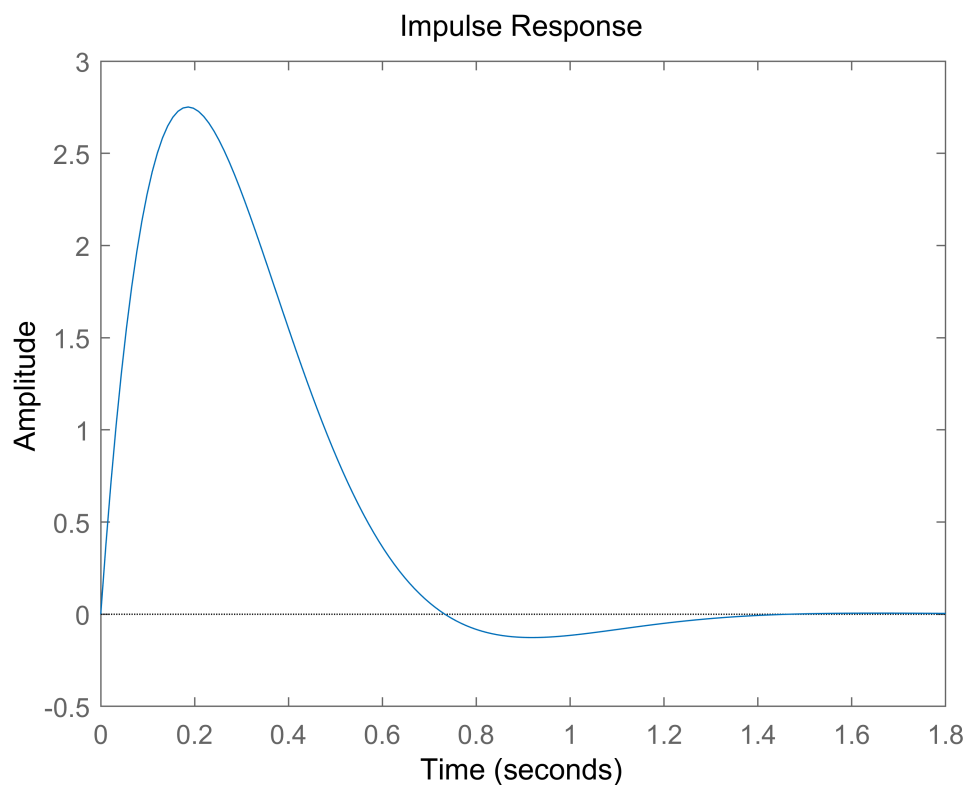


例2.4：当典型二阶系统中 $\xi=0.7$ ， $\omega_n=6$ 时的单位冲激响应

```
Wn =6;
kesai = 0.7
```

```
kesai = 0.7000
```

```
% hold on
num = Wn^2;
den = [1,2*kesai*Wn,Wn^2];
impulse(num,den)
```



```
% hold off
```

例2.5：单位阶跃响应，单位冲激响应及零输入响应（设初始状态 $\mathbf{x}_0=[1 \ 1 \ 1 \ -1]^T$ ）

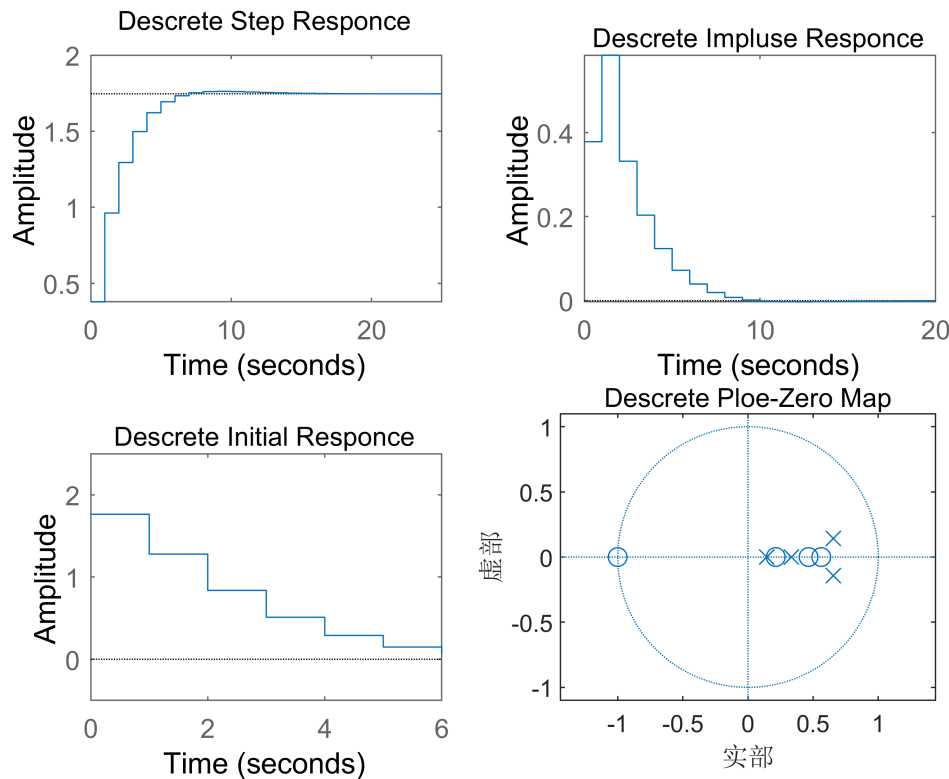
```
clear
clc
clf

a0=[-1.6,-0.9,0,0;0.9,0,0,0; 0.4,0.5,-5,-2.45;0,0,2.45,0];
b0=[1;0;1;0];
c0=[1,1,1,1];
d0=[0];
t=0.5;
[a,b,c,d]=c2dm(a0,b0,c0,d0,t,'tustin');
figure(3);
subplot(2,2,1);
dstep(a,b,c,d);
title('Descrete Step Responce');
subplot(2,2,2);
dimpulse(a,b,c,d);
title('Descrete Impluse Responce');
subplot(2,2,3);
x0=[1;1;1;-1];
```

```

dinitial(a,b,c,d,x0);
axis([0 6 -0.5 2.5]);
title('Descrete Initial Responce');
subplot(2,2,4);
[z,p,k]=ss2zp(a,b,c,d,1);
zplane(z,p);
title('Descrete Ploe-Zero Map');

```



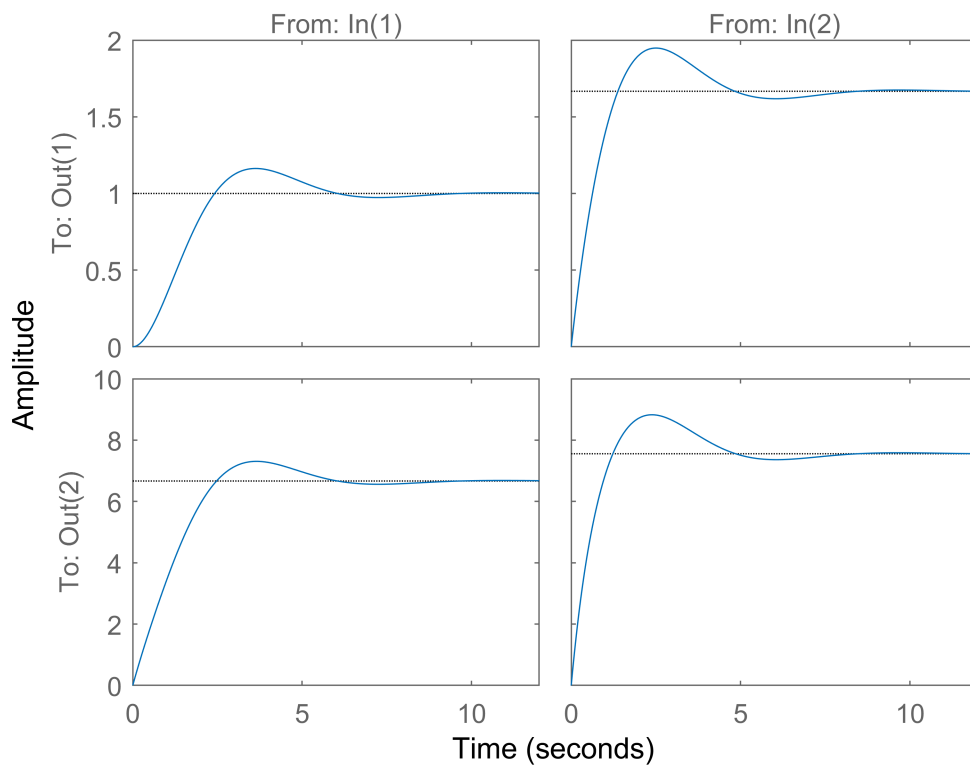
例2.6：求多输入多输出系统的单位阶跃响应和单位冲激响应

```

clf
a=[2.25 -5 -1.25 -0.5;2.25 -4.25 -1.25 -0.25;0.25 -0.5 -1.25 -1;1.25 -1.75 -0.25 -0.75];
b=[4 6;2 4;2 2;0 2];
c=[0 0 0 1;0 2 0 2];
d=zeros(2,2);
step(a,b,c,d);

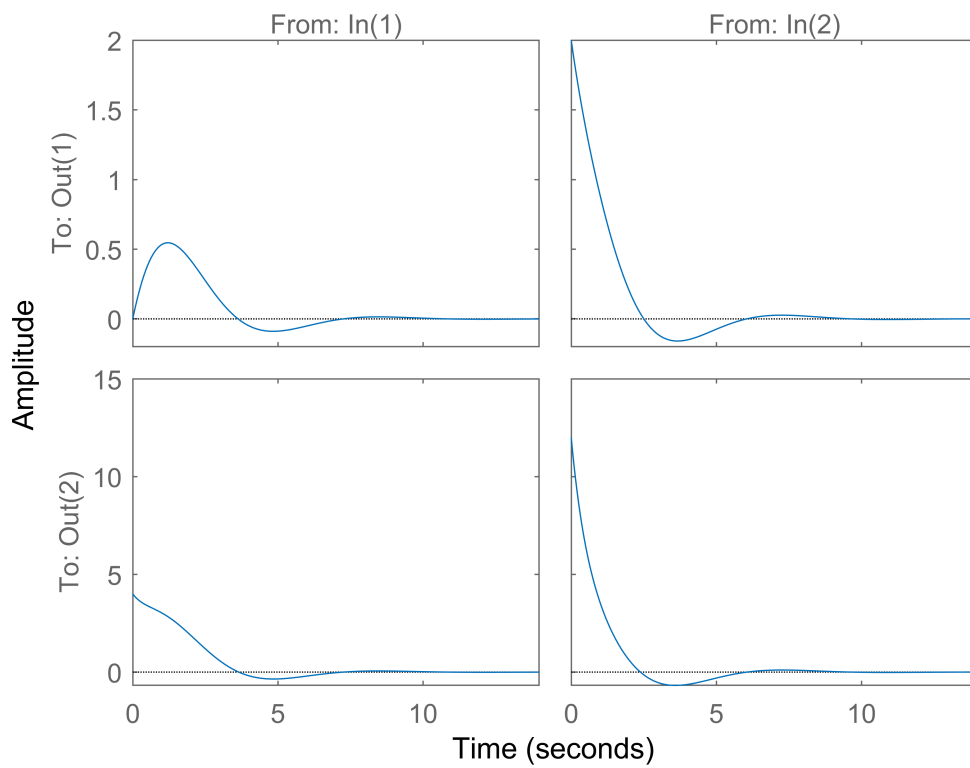
```

Step Response



```
impulse(a,b,c,d);
```

Impulse Response



例2.7：将例2.5 中的连续系统，以 $t=0.5$ 取样周期，采用双线性变换算法转换成离散系统，然后求出离散系统的单位阶跃响应、单位冲激响应及零输入响应（设初始状态 $\mathbf{x}_0=[1 \ 1 \ 1 \ -1]^T$ ）

```
clf

a=[-1.6 -0.9 0 0;0.9 0 0 0;0.4 0.5 -5 -2.45;0 0 2.45 0];
b=[1;0;1;0];
c=[1 1 1 1 ];
d=[0];
t=0.5;
sys = ss(a,b,c,d)
```

```
sys =

A =

      x1      x2      x3      x4
x1  -1.6   -0.9      0      0
x2   0.9      0      0      0
x3   0.4   0.5     -5   -2.45
x4      0      0   2.45      0

B =

      u1
x1      1
x2      0
x3      1
x4      0

C =

      x1  x2  x3  x4
y1      1   1   1   1

D =

      u1
y1      0
```

Continuous-time state-space model.

```
sysd=c2d(sys,t,'tustin')
```

```
sysd =

A =

      x1      x2      x3      x4
x1  0.3787  -0.3102      0      0
x2  0.3102   0.9302      0      0
x3  0.06729  0.08009  -0.2381  -0.4666
x4  0.04122  0.04906   0.4666   0.7142

B =

      u1
x1  0.3447
x2  0.07755
x3  0.2073
x4  0.127

C =
```

| | x1 | x2 | x3 | x4 |
|----|--------|--------|--------|--------|
| y1 | 0.8987 | 0.8746 | 0.6142 | 0.6238 |

D =

| | u1 |
|----|--------|
| y1 | 0.3782 |

Sample time: 0.5 seconds

Discrete-time state-space model.

a = sysd.A

a = 4x4

| | | | |
|--------|---------|---------|---------|
| 0.3787 | -0.3102 | 0 | 0 |
| 0.3102 | 0.9302 | 0 | 0 |
| 0.0673 | 0.0801 | -0.2381 | -0.4666 |
| 0.0412 | 0.0491 | 0.4666 | 0.7142 |

b = sysd.B

b = 4x1

| |
|--------|
| 0.3447 |
| 0.0776 |
| 0.2073 |
| 0.1270 |

c = sysd.C

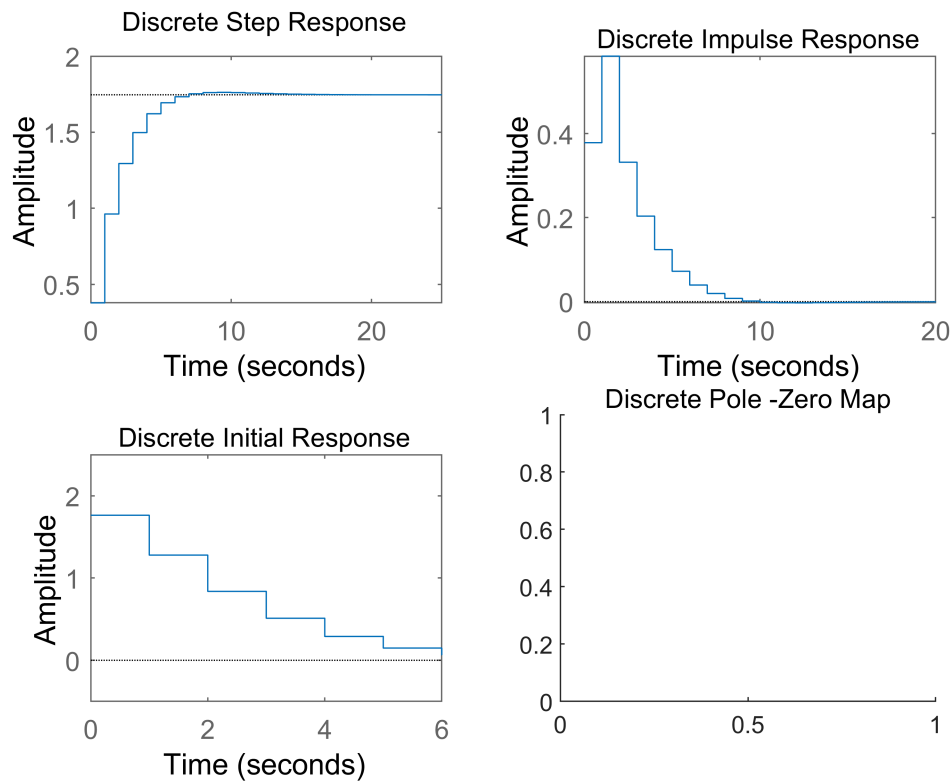
c = 1x4

| | | | |
|--------|--------|--------|--------|
| 0.8987 | 0.8746 | 0.6142 | 0.6238 |
|--------|--------|--------|--------|

d = sysd.D

d = 0.3782

```
figure(1)
subplot(2,2,1);
dstep(a,b,c,d);
title('Discrete Step Response');
subplot(2,2,2);
dimpulse(a,b,c,d);
title('Discrete Impulse Response');
subplot(2,2,3);
x0=[1;1;1;-1];
dinitial(a,b,c,d,x0);
axis([0 6 -0.5 2.5]);
title('Discrete Initial Response');
subplot(2,2,4);
[z,p,k]=ss2zp(a,b,c,d,1);
title('Discrete Pole -Zero Map');
```

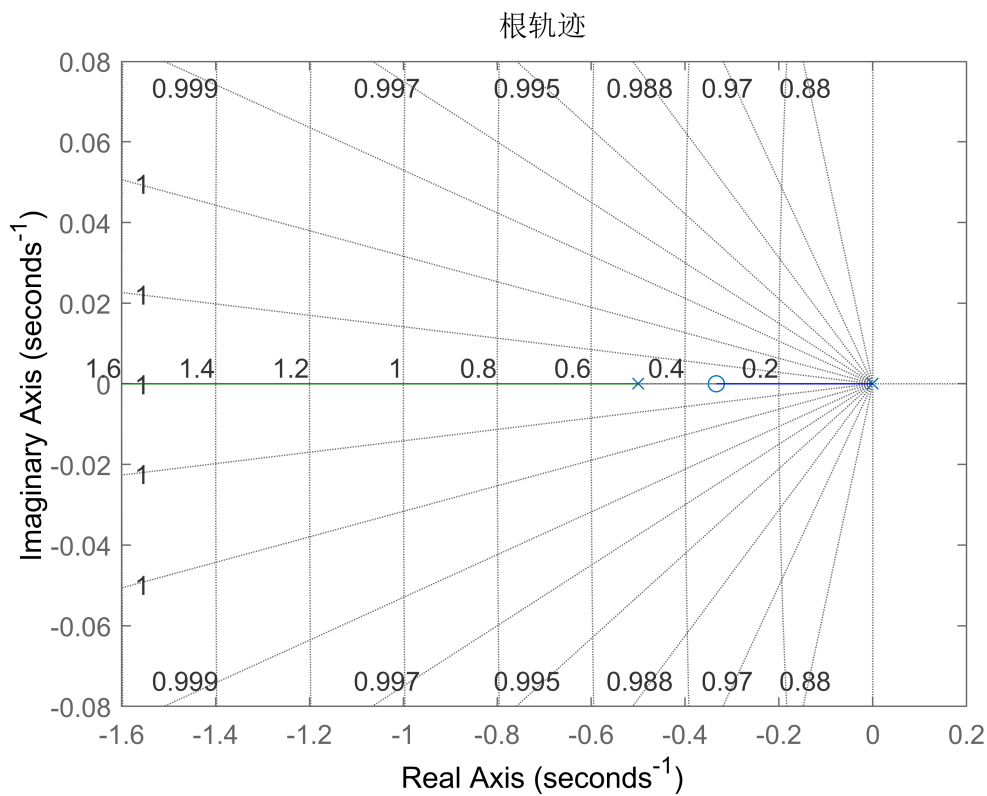


实验三. 控制系统的根轨迹法

例3.1: 绘制出通过单位负反馈构成的闭环系统的根轨迹

```
clear
clc
clf

num = [3 1];
den = [2 1 0];
rlocus(num,den)
sgrid
title('根轨迹')
```



例3.2：绘制出闭环系统的根轨迹，并确定交点处的增益 **k**

```
num=[1,5]
```

```
num = 1x2
      1      5
```

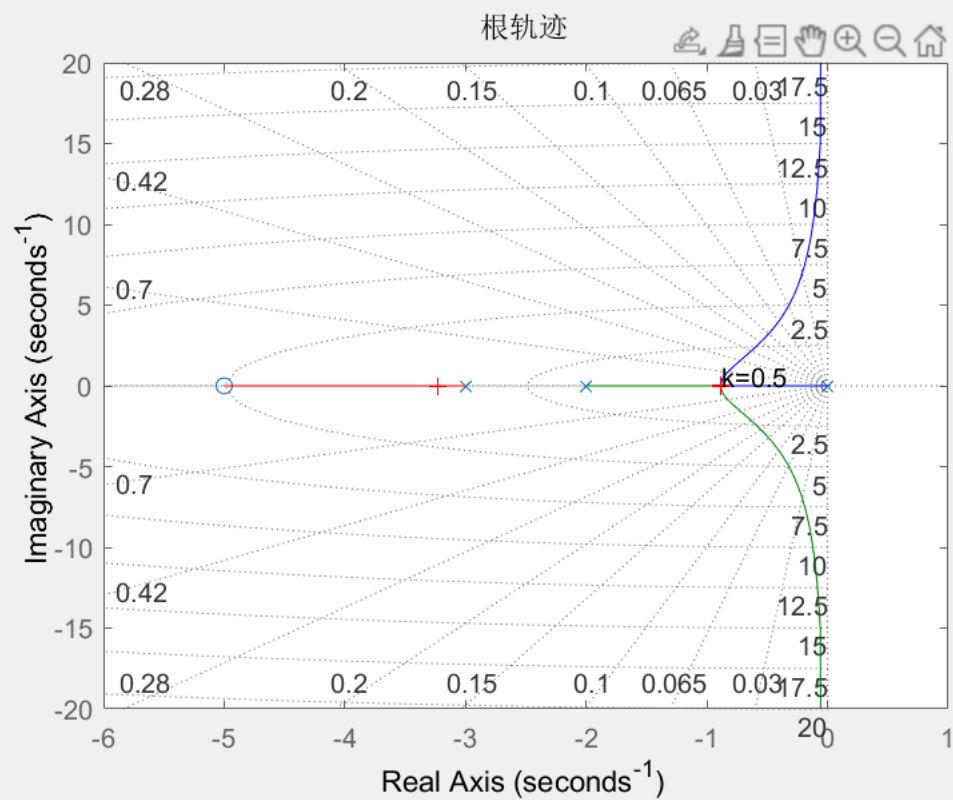
```
den=[1,5,6,0]
```

```
den = 1x4
      1      5      6      0
```

```
rlocus(num,den)
sgrid
title('根轨迹')
[k,p]=rlocfind(num,den)
```

```
Select a point in the graphics window
selected_point = -0.8744 - 0.0413i
k = 0.5081
p = 3x1
    -3.2274
    -0.8863
    -0.8863
```

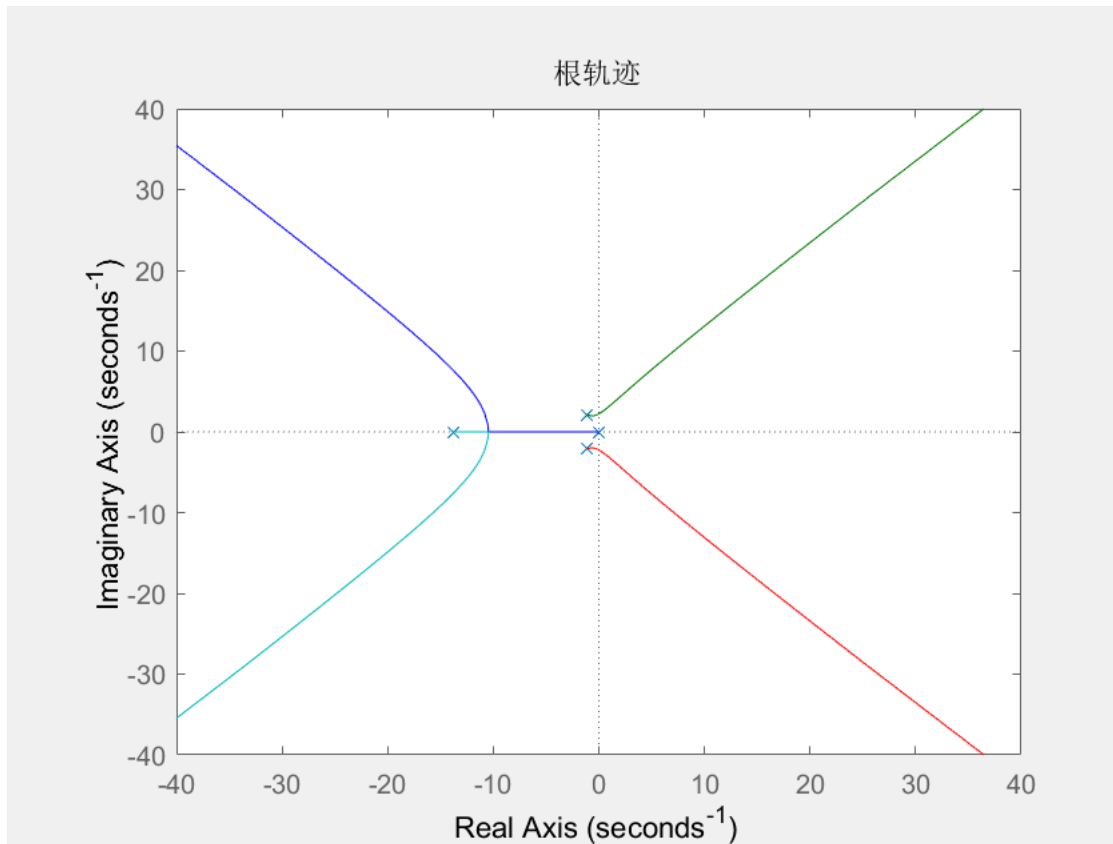
```
gtext('k=0.5')
```



例3.3：绘制出闭环系统的根轨迹

```
clear
clc
clf

num=[1];
den=[1,16,36,80,0];
rlocus(num,den)
title('根轨迹')
```



例3.4：绘制出闭环系统的根轨迹

```
num=[1,2]
```

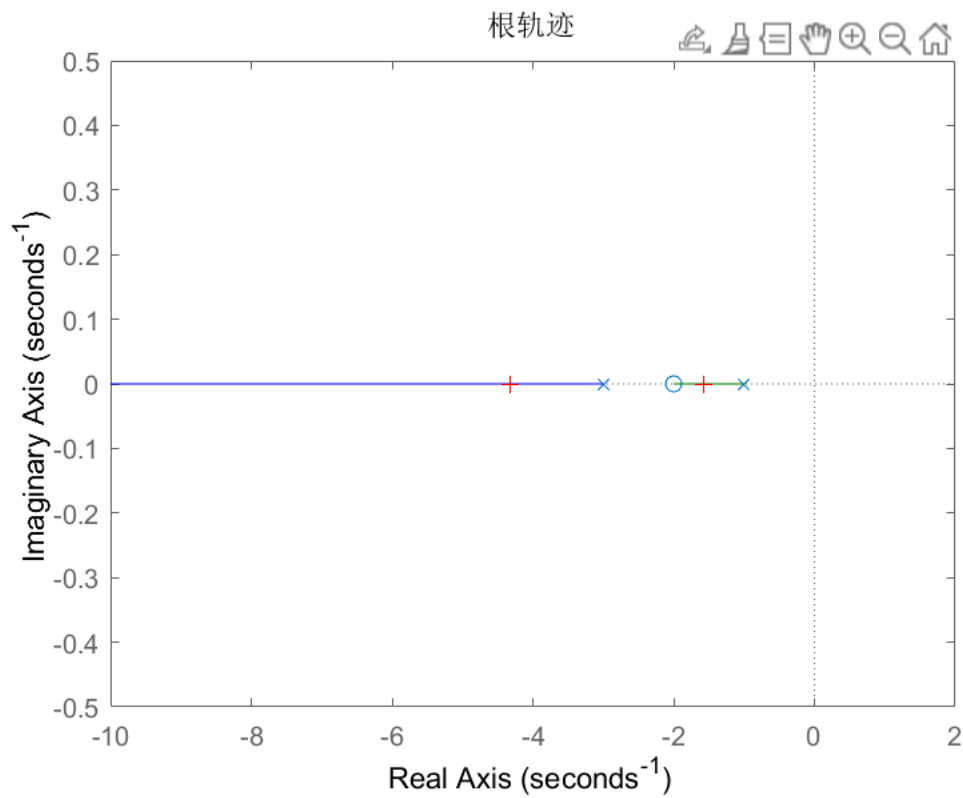
```
num = 1×2
      1    2
```

```
den=[1,4,3]
```

```
den = 1×3
      1    4    3
```

```
figure(1);
rlocus(num,den)
title('根轨迹')
[k,p]=rlocfind(num,den)
```

Select a point in the graphics window



```
selected_point = -4.3223 + 0.0010i
k = 1.8917
p = 2×1
    -4.3223
    -1.5694
```

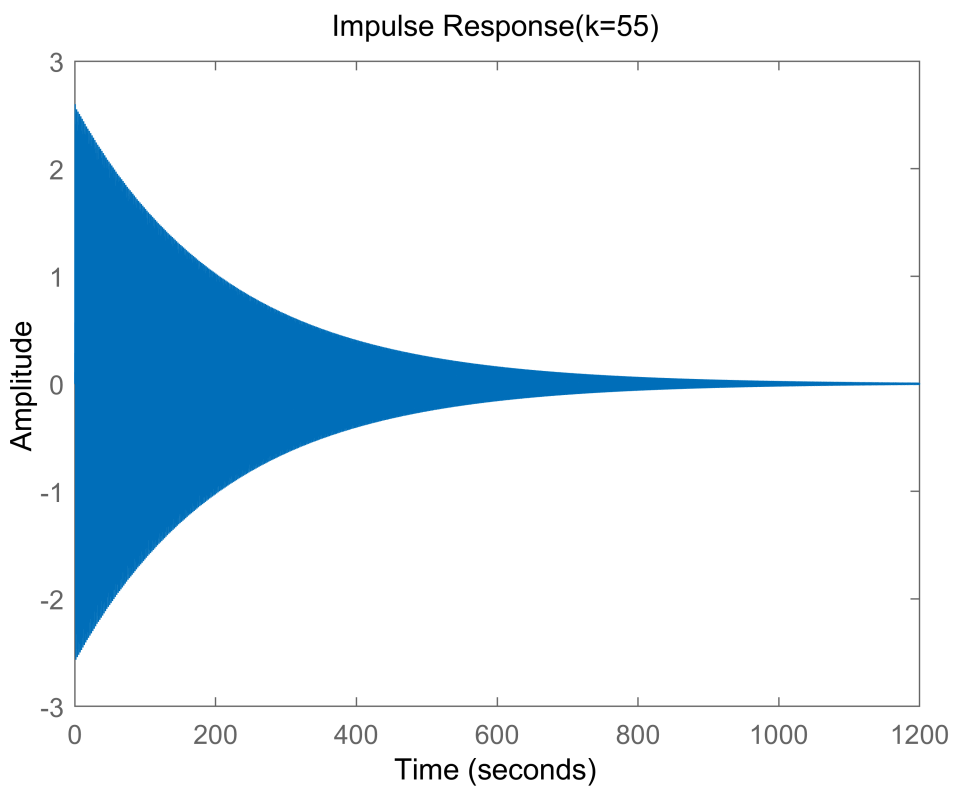
```
figure(2);
k=55;
num1=k*[1 2]
```

```
num1 = 1×2
    55    110
```

```
den=[1 4 3]
```

```
den = 1×3
    1     4     3
```

```
den1=conv(den,den);
[num,den]=cloop(num1,den1,-1);
impulse(num,den);
title('Impulse Response(k=55)')
```



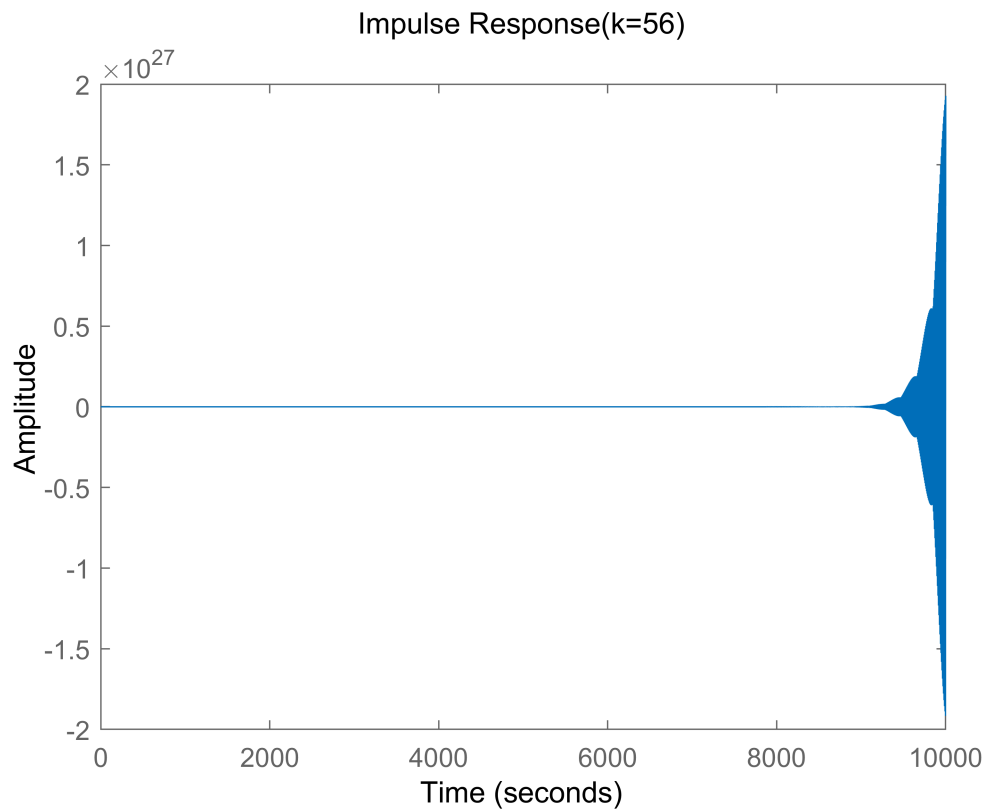
```
figure(3);
k=56;
num1=k*[1 2]
```

```
num1 = 1×2
      56   112
```

```
den=[1 4 3]
```

```
den = 1×3
      1      4      3
```

```
den1=conv(den,den);
[num,den]=cloop(num1,den1,-1);
impulse(num,den);
title('Impulse Response(k=56)')
```

实验四．控制系统反馈校正设计

例4.1：设计反馈控制器

```
clear
clc
clf

disp('Pole Placement ..... using transformation matrix')
```

Pole Placement using transformation matrix

```
a=[0 1 0;0 0 1;-6 -11 -6];
b=[0;0;10]
```

```
b = 3x1
     0
     0
    10
```

```
cam=ctrb(a,b);
disp('The rank of controllability matrix');
```

The rank of controllability matrix

```
rc=rank(cam)
```

```
rc = 3
```

```
beta=poly(a)
```

```
beta = 1x4  
    1.0000    6.0000   11.0000    6.0000
```

```
a1=beta(2);a2=beta(3);a3=beta(4);  
w=[a2 a1 1;a1 1 0;1 0 0];  
t=cam*w;  
j=[-2+2*sqrt(3)*i 0 0;0 -2-2*sqrt(3)*i 0;0 0 -10];  
alph=poly(j);  
aa1=alph(2);aa2=alph(3);aa3=alph(4);  
k=[aa3-a3 aa2-a2 aa1-a1]*(inv(t))
```

```
k = 1x3  
   15.4000    4.5000    0.8000
```

```
disp('Pole Placement ..... using Ackermann's formula');
```

```
Pole Placement ..... using Ackermann's formula
```

```
a=[0 1 0;0 0 1;-6 -11 -6];  
b=[0;0;10];  
cam=ctrb(a,b);  
disp('The rank of controllability matrix');
```

```
The rank of controllability matrix
```

```
rc=rank(cam)
```

```
rc = 3
```

```
j=[-2+2*sqrt(3)*i 0 0;0 2-2*sqrt(3)*i 0;0 0 -10];  
alph=poly(j);  
phi=polyvalm(alph,a);  
k=[0 0 1]*(inv(cam))*phi
```

```
k = 1x3 complex  
    7.4000 +13.8564i   -0.3000 + 1.3856i    0.4000 + 0.0000i
```

```
p=[-2+2*sqrt(3)*i -2-2*sqrt(3)*i -10];  
k=place(a,b,p)
```

```
k = 1x3  
   15.4000    4.5000    0.8000
```

例4.2：设计全阶状态观测器

```
a=[0 1 0;0 0 1;-6 -1 -6];  
b=[0;0;1]
```

```
b = 3×1
    0
    0
    1
```

```
c=[1 0 0]
```

```
c = 1×3
    1    0    0
```

```
disp('The rank of obserbability matrix')
```

```
The rank of obserbability matrix
```

```
ro=rank(observ(a,c))
```

```
ro = 3
```

```
a1=a';
b1=c';
c1=b';
p=[-2+2*sqrt(3)*i -2-2*sqrt(3)*i -5];
k=acker(a1,b1,p)
```

```
k = 1×3
    3.0000    17.0000   -31.0000
```

```
ke=k'
```

```
ke = 3×1
    3.0000
   17.0000
  -31.0000
```

例4.3：设计最小阶状态观测器

```
a=[0 1 0;0 0 1;-6 -11 -6];
b=[0;0;1];c=[1 0 0]
```

```
c = 1×3
    1    0    0
```

```
aaa=[a(1,1)];aab=[a(1,2:3)];
aba=[a(2:3,1)];abb=[a(2:3,2:3)];
ba=b(1,1);bb=b(2:3,1);
a1=abb;c1=aab;
disp('Design of a minimum-order observer');
```

```
Design of a minimum-order observer
```

```
ro=rank(observ(a1,c1))
```

```
ro = 2
```

```
ax=a1';
bx=c1';
p=[-2+2*sqrt(3)*i -2-2*sqrt(3)*i];
```

```
k=acker(ax,bx,p);  
ke=k'
```

```
ke = 2×1  
    -2  
    17
```