

2016 Lifeskills Mathematics

National 5 Paper 2

Finalised Marking Instructions

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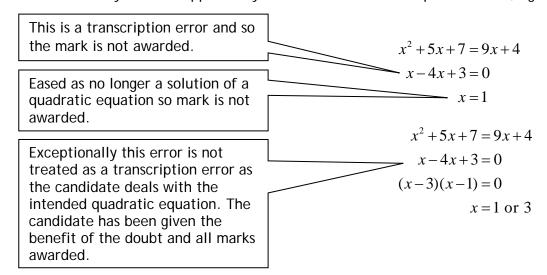
General Marking Principles for National 5 Lifeskills Mathematics

This information is provided to help you understand the general principles you must apply when marking candidate responses to questions in this Paper. These principles must be read in conjunction with the detailed marking instructions, which identify the key features required in candidate responses.

For each question the marking instructions are generally in two sections, namely Illustrative Scheme and Generic Scheme. The Illustrative Scheme covers methods which are commonly seen throughout the marking. The Generic Scheme indicates the rationale for which each mark is awarded. In general, markers should use the Illustrative Scheme and only use the Generic Scheme where a candidate has used a method not covered in the Illustrative Scheme.

- (a) Marks for each candidate response must <u>always</u> be assigned in line with these General Marking Principles and the Detailed Marking Instructions for this assessment.
- (b) Marking should always be positive. This means that, for each candidate response, marks are accumulated for the demonstration of relevant skills, knowledge and understanding: they are not deducted from a maximum on the basis of errors or omissions.
- (c) If a specific candidate response does not seem to be covered by either the principles or detailed Marking Instructions, and you are uncertain how to assess it, you must seek guidance from your Team Leader.
- (d) Credit must be assigned in accordance with the specific assessment guidelines.
- (e) One mark is available for each •. There are no half marks.
- (f) Working subsequent to an error must be **followed through**, with possible credit for the subsequent working, provided that the level of difficulty involved is approximately similar. Where, subsequent to an error, the working for a follow through mark has been eased, the follow through mark cannot be awarded.
- (g) As indicated on the front of the question paper, full credit should only be given where the solution contains appropriate working. Unless specifically mentioned in the marking instructions, a correct answer with no working receives no credit.
- (h) Candidates may use any mathematically correct method to answer questions except in cases where a particular method is specified or excluded.
- (i) As a consequence of an error perceived to be trivial, casual or insignificant, eg $6 \times 6 = 12$ candidates lose the opportunity of gaining a mark. However, note the second example in comment (j).

(j) Where a transcription error (paper to script or within script) occurs, the candidate should normally lose the opportunity to be awarded the next process mark, eg



(k) Horizontal/vertical marking

Where a question results in two pairs of solutions, this technique should be applied, but only if indicated in the detailed marking instructions for the question.

Example:

$$\bullet^5 \quad x = 2 \quad x = -4$$

$$\bullet^6 \quad y = 5 \quad y = -7$$

Horizontal:
$$\bullet^5$$
 $x=2$ and $x=-4$ Vertical: \bullet^5 $x=2$ and $y=5$ \bullet^6 $y=5$ and $y=-7$

Markers should choose whichever method benefits the candidate, but **not** a combination of both.

(I) In final answers, unless specifically mentioned in the detailed marking instructions, numerical values should be simplified as far as possible, eg:

$$\frac{15}{12} \text{ must be simplified to } \frac{5}{4} \text{ or } 1\frac{1}{4} \qquad \frac{43}{1} \text{ must be simplified to } 43$$

$$\frac{15}{0 \cdot 3} \text{ must be simplified to } 50 \qquad \frac{\frac{4}{5}}{3} \text{ must be simplified to } \frac{4}{15}$$

$$\sqrt{64} \text{ must be simplified to } 8^*$$

*The square root of perfect squares up to and including 100 must be known.

(m) Commonly Observed Responses (COR) are shown in the marking instructions to help mark common and/or non-routine solutions. CORs may also be used as a guide when marking similar non-routine candidate responses.

- (n) Unless specifically mentioned in the marking instructions, the following should not be penalised:
 - Working subsequent to a correct answer
 - Correct working in the wrong part of a question
 - Legitimate variations in numerical answers/algebraic expressions, eg angles in degrees rounded to nearest degree
 - Omission of units
 - Bad form (bad form only becomes bad form if subsequent working is correct), eg $(x^3 + 2x^2 + 3x + 2)(2x + 1)$ written as $(x^3 + 2x^2 + 3x + 2) \times 2x + 1$

$$2x^4 + 4x^3 + 6x^2 + 4x + x^3 + 2x^2 + 3x + 2$$
 written as $2x^4 + 5x^3 + 8x^2 + 7x + 2$ gains full credit

- Repeated error within a question, but not between questions or papers
- (o) In any 'Show that...' question, where the candidate has to arrive at a required result, the last mark of that part is not available as a follow-through from a previous error unless specified in the detailed marking instructions.
- (p) All working should be carefully checked, even where a fundamental misunderstanding is apparent early in the candidate's response. Marks may still be available later in the question so reference must be made continually to the marking instructions. The appearance of the correct answer does not necessarily indicate that the candidate has gained all the available marks.
- (q) Scored-out working which has not been replaced should be marked where still legible. However, if the scored out working has been replaced, only the work which has not been scored out should be marked.
- (r) Where a candidate has made multiple attempts using the same strategy and not identified their final answer, mark all attempts and award the lowest mark.

For example:

Strategy 1 attempt 1 is worth 3 marks.	Strategy 2 attempt 1 is worth 1 mark.
Strategy 1 attempt 2 is worth 4 marks.	Strategy 2 attempt 2 is worth 5 marks.
From the attempts using strategy 1, the resultant mark would be 3.	From the attempts using strategy 2, the resultant mark would be 1.

In this case, award 3 marks.

Detailed Marking Instructions for each question

Question		Generic Scheme	Illustrative Scheme	Max Mark
1.	(a)	Ans: proof		2
		• 1 Strategy: know how to calculate percentage difference in population	$\bullet^{1} \frac{21400}{5347600} \times 100 = \dots$	
		• ² Process: calculate percentage growth	• ² 0· 4	
		Alternative Strategy:		
		• 1 Strategy: know to find 0.4% and add it on	• Finding 0.4% of 5347600 and adding it on	
		• ² Process: Calculate population in 2015 and round to the nearest hundred.	• ² 5347600 ÷ 100 x 0·4 + 5347600 = 5369000	

Notes:

Commonly Observed Responses:

1. $21400/5369000 \times 100 = 0.39 = 0.4$ award $1/2 \times \checkmark$

Questio	on	Generic Scheme	Illustrative Scheme	Max Mark
(b)	Ans: 5 433 700		3
		• 1 Strategy: identify multiplier	•¹ 1·004	
		• ² Strategy: identify power	• 2 3	
		• 3 Process/Communication: calculate population	•³ 5 433 700	

1. For an answer of 5 433 700 without working

award 3/3 ✓✓✓

2. If candidate calculates 3 annual increase accept rounding to nearest hundred for each year. ie ((2016): 5 390 500, (2017): 5 4121 00, (2018): 5 433 700)

award 3/3 ✓✓✓

3. Accept $5437600 \times 1.004^4 = 543370$

award 3/3 ✓ ✓ ✓

4. If candidate does $5347600 \times 1.004^3 = 5412000$

award 2/3 √×√

5. Where an incorrect percentage is used, the working must be followed through to give the possibility of awarding 2/3

×√v

eg for an answer of 6 039 400 (5 369 $000 \times 1 \cdot 04^3$), with working

award 2/3 ×√√

6. For an answer of 5 390 500 (5 369 000 $\times 1.004$), no working necessary

award 1/3 √××

7. For an answer of 16 171 400 (5 369 000 \times 1.004 \times 3), with working

award 1/3 √xx

8. For an answer of 5 433 400 (5 369 000 + 21 476 \times 3), with working

award 1/3 ✓××

9. For an answer of 64 400 (5 369 000 × 0⋅004 × 3)

award 0/3 xxx

10. For an answer of 5 433 200 (5 369 000 + 21400 × 3)

award 0/3 xxx

Que	Question		Generic Scheme	Illustrative Scheme	Max Mark
2.			Ans: 01:30 (on Sunday 10 th) • 1 Strategy: knows how to deal	• 1 evidence of adding flight time	2
			with time zone and flight time • 2 Process/Communication: state time	and subtracting time difference • 2 01:30 (on Sunday 10 th)	

For the following answers no working is necessary

- 1. For an arrival time of 17:30 (add flight time and adds time difference) award 1/2

۷.	award 1/2
3.	For an arrival time of 00:40 (subtracts flight time and adds time difference) award 1/2
Comm	nonly Observed Responses:

Que	stion	Generic Scheme	Illustrative Scheme	Max Mark
3.		Ans: • 1 Strategy/Process: find any one of the three angles for the April poll.	• 1,2 Yes - 133° No - 184° Undecided - 43°	3
		 Strategy/Process: find the other two angles. Communication: make one valid comment. 	 eg similar proportion chose 'yes' in survey 2. 	
		Alternative strategy:	larger proportion chose 'no' in survey 2. smaller proportion chose 'undecided' in survey 2.	
		• 1 Strategy/Process: find all three percentages for December 2013 Poll.	 December 2013 Poll: Yes 37%, No 39% and Undecided 24% 	
		• 2 Strategy/Process: find all three percentages for April 2014 Poll.	 April 2014 Poll: Yes 37%, No 51% and Undecided 12% 	
		• 3 Communication: make one valid comment.	• a g similar proportion chose 'yes' in survey 2. larger proportion chose 'no' in survey 2. smaller proportion chose 'undecided' in survey 2.	

- 1. If no calculations are attempted all comments are invalid 0/3
- 2. All comments must refer to percentages, fractions, proportion etc
- 3. If candidate assumes that there are the same number of people in each poll then •¹ is not available but •² can be awarded for Yes 442, No 469, Undecided 295. In this case only, if they refer to the number of people •³ can be awarded comparing the number of people in each category.
- 4. If only one category has been considered in both opinion polls, then all three marks are available.

Question			Generic Scheme	Illustrative Scheme	Max Mark
4.	(a)	(i)	Ans: 1:100 000		1
			•¹ Communication: find the scale	•¹ 1:100 000	
		(ii)	 Ans: 074°, 9.6 km Communication: correct bearing Communication: distance in kilometres 	• 2 074° • 3 9·6 km	2

- 1. For 1cm=1km award 1/1 treat the = as bad form
- 2. Allow a tolerance of +/- 1° for angle
- 3. Allow a tolerance of +/- 0.1 km for length
- 4. For 1 the leading 0 must be present in the bearing
- 5. Candidates must use the scale that they have found in part (a) for part (b)

Commonly Observed Responses:

1. For 1 cm : 1 km award 1/1 ✓

2. For 9.8 cm: 9.8 km award 0/1 ×

Question	Generic Scheme	Illustrative Scheme	
(b)	Ans: 23 (minutes)		3
	• ¹ Strategy: use correct speed	•¹ use 27 km/hr	
	• ² Process: find time in hours to 3 decimal places	• 2 10·2 ÷ 27 = 0·377 (hours)	
	• 3 Communication: find the time in minutes, and round	• 3 0· $377 \times 60 = 22· 66 \rightarrow 23$	
	Alternative strategy		
	• 1 Strategy: Compare time needed for 21 km/h and 27 km/h	•¹ use 27 km/hr and 21 km/hr	
	• 2 Process: find time in hours for both speeds to 3 decimal places	• 2 10·2 ÷ 27 = 0·377 (hours) and 10·2 ÷ 21 = 0·845 (hours)	
	• 3 Communication: select shortest time, convert to minutes and round	• ³ 0· 377 × 60 = 22· 66 →23	

- If candidate only uses 21 or 24 km/hr •² and •³ are available.
 For •² time in hours must be to at least 3 decimal places rounded or truncated.
 In the alternative strategy, only the shortest time needs to be converted to minutes.

Question			Generic Scheme	Illustrative Scheme	Max Mark
5.	(a)	(i)	Ans: (\$)183		2
			• 1 Strategy: identify the costs not included	• 1 \$32 and \$37	
			• ² Process: calculate the cost for card 1	\bullet^2 \$114 + 32 + 37 = \$183	
		(ii)	Ans: \$157 supported by working		4
			• 3 Strategy: identify the "missing" attraction and the two cheapest attractions	• 3 \$24, \$32 and \$30	
			• 4 Process: calculate the cost for card 2	• ⁴ \$71 + \$24 + \$32 + \$30 = \$157	
			• 5 Process: state cost of card 3	• ⁵ \$180	
			• 6 Communication: state the cheapest price	• ⁶ (\$)157	

- 1. If candidate chooses to buy two of card 2 and buys a one world observatory separately = \$174 do not award $•^3$, $•^4$ is still available.
- 2. 4 is available for adding at least 2 out of the 3 missing attractions to card 2 price.

Question	1	Generic Scheme	Illustrative Scheme	Max Mark
(b)		Ans: £1 gives \$1.555 or \$1 gives £0.643		2
		• 1 Strategy: evidence of knowing to divide	•¹ 157 ÷ 100·96 or 100·96 ÷ 157	
		• ² Process: state rounded answer	• 2 £1 gives \$1.555 or \$1 gives £0.643	

1. For •² units are essential

Que	stion		Generic Scheme	Illustrative Scheme	Max Mark
6.	(a)	(i)	Ans: 81·1		1
			• ¹ Process: calculate mean	\bullet^{1} (81·8 + 81·7 + 81·6 + 81·0 + 80·3 + 80·2) ÷ 6 = 81·1	
		(ii)	Ans: 0.72		3
			• Process: calculate $(x-\overline{x})^2$	• ² 0· 49, 0· 36, 0· 25, 0· 01, 0· 64, 0· 81	
			• 3 Strategy: substitute into formula	$\bullet^3 \sqrt{(2\cdot 56 \div 5)}$	
			• ⁴ Process: calculate standard deviation	• 4 0.72	

- 1. Alternative method
 - $^2 \sum x = 486 \cdot 6$ and $\sum x^2 = 39465 \cdot 82$
- Accept rounding or truncation to at least one decimal place for final answer
 The mark ⁴ can only be awarded when a two-step calculation has taken place.

Question		Generic Scheme	Illustrative Scheme	
	(b)	Ans: two valid comments		2
		• 1 Communication: comment regarding the mean	• 1 eg on average Goodhold give a faster lap time	
		• ² Communication: comment regarding standard deviation	• ² eg lap times with Goodhold are less consistent	

- 1. Comments must refer to the context of the question.
- 2. Example of an unacceptable comment eg his results were more spread out with goodhold (has not mentioned lap time) eg On average the data for goodhold is lower(does not refer to context)

Question		Generic Scheme	Illustrative Scheme	
(c)		Ans: 160 (km/hr)		3
		• 1 Strategy: correct substitution into S = D/T	$\bullet^1 S = 3.6/81$	
		• 2 Strategy: know how to change km/sec to km/hr	• ² × 60 × 60	
		• ³ Process: find speed in km/hr	•³ 160	
		Alternative Strategy		3
		•¹ Strategy: knows how to find the time in hours	• 1 81 ÷ 60 ÷ 60	
		• 2 Strategy: consistent substitution into S = D/T	• ² 3· 6 ÷	
		• ³ Process: find speed in km/hr	•³ 160	

- 1. Candidates are expected to work to at least 3 significant figures throughout.
- 2. 3 is only available for candidates who attempt to multiply or divide by 3600 (60×60)

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1. 81 \div 60 \div 60 = 0.0225 \div 3.6 = 0.00625 award 2/3 \checkmark \times \checkmark

2. 81 \div 3.6 = 22.5 \longrightarrow 22.5 \times 60 \times 60 = 81000 award 2/3 \times \checkmark \checkmark

3. 81 \div 3.6 = 22.5 \longrightarrow 22.5 \div 60 \div 60 = 0.00625 award 1/3 \times \times \checkmark

4. 3.6 \times 81 = 291.6 \longrightarrow 291.6 \times 60 \times 60 = 1049760 award 2/3 \times \checkmark \checkmark

5. 3.6 \times 81 = 291.6 \longrightarrow 291.6 \div 60 \div 60 = 0.081 award 1/3 \times \times \checkmark

6. 3.6 \div 1.35 = 2.66... award 1/3 \times \times \checkmark
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Question		Generic Scheme	Illustrative Scheme	Max Mark
7.	(a)	Ans: (£)1100		4
		• 1 Process: calculate 5% of £15,000	•¹ £750	
		• ² Communicate: find gross pay	\bullet^2 750 + 500 = £1250	
		• ³ Process :calculate 12% of £1250	• ³ 12% of 1250 = £150	
		• 4 Communicate: find net pay	• ⁴ 1250 - 150 = 1100	

- 1. For an answer of £418 (working must be shown) award 4/4 if candidate states net pay is £1100
- 2. For an answer of £418 (working must be shown) award 3/4 if candidate does not state net pay is £1100.

- 1. For net pay = 750 + 440 = 1190 award 3/4 Candidate has found 12% of basic pay only, instead of 12% of gross pay.
- 2. For net pay of £1452 (commission = 5% of £23000) award 3/4

Ques	Question		Generic Scheme	Illustrative Scheme	
	(b)	(i)	Ans: (£) 418		1
			• 1 Process: net pay - monthly bills	•¹ 1100 - 682 = 418	
		(ii)	Ans: 6·1(%)		2
			• 2 Strategy: know how to find percentage increase	•² 15 ÷ 245 × 100	
			• ³ Process: calculate percentage increase	•³ 6·1	

- •² is available for calculations of the form a/b x 100 where a, b = 15 or 245 or 260 or 505.
 Both marks are available for a trial an improvement strategy leading to an answer between 5.9% and 6.3% inclusive. Working must be shown

Commonly Observed Responses:

(b)(i)

1. £770 (from net pay calculated as £1452)

award 1/1 ✓

(b)(ii)

2. $245 \div 260 \times 100 = 94.2\%$ leading to 100 - 94.2 = 5.8%award 1/2×√ 3. $260 \div 245 \times 100 = 106 \cdot 1\%$ award 1/2×√

4. $15 \div 260 \times 100 = 5.8\%$ award 1/2×✓

Question		Generic Scheme	Illustrative Scheme	
	(c)	Ans: Premier bank, 24 months		2
		• 1 Process: find the new monthly surplus	•¹ 403	
		• ² Communicate: correct choice of lender	• ² Premier Bank, 24 months	

If candidate calculates new monthly surplus that is less than £150.60 \bullet ² is available for "she can't afford any of the loans"

Commonly Observed Responses:

1. New monthly surplus of £755 so choose Tasko bank over 12 months (from surplus of £770)

award 2/2 ✓✓

Question			Generic Scheme	Illustrative Scheme	
	(b)	(i)	Ans: (£) 418		1
			• 1 Process: net pay - monthly bills	•¹ 1100 - 682 = 418	
		(ii)	Ans: 6·1(%)		2
			• 2 Strategy: know how to find percentage increase	•² 15 ÷ 245 × 100	
			Process: calculate percentage increase	•³ 6·1	

- •² is available for calculations of the form a/b x 100 where a, b = 15 or 245 or 260 or 505.
 Both marks are available for a trial an improvement strategy leading to an answer between 5.9% and 6.3% inclusive. Working must be shown

Commonly Observed Responses:

(b)(i)

1. £770 (from net pay calculated as £1452)

award 1/1 ✓

(b)(ii)

2. $245 \div 260 \times 100 = 94.2\%$ leading to 100 - 94.2 = 5.8%

award 1/2×√

3. $260 \div 245 \times 100 = 106 \cdot 1\%$

award 1/2×√

4. $15 \div 260 \times 100 = 5.8\%$

award 1/2×✓

Question		Generic Scheme	Illustrative Scheme	
(c)		Ans: Premier bank, 24 months		2
		• 1 Process: find the new monthly surplus	● ¹ 403	
		• ² Communicate: correct choice of lender	• ² Premier Bank, 24 months	

If candidate calculates new monthly surplus that is less than £150.60 \bullet ² is available for "she can't afford any of the loans"

Commonly Observed Responses:

2. New monthly surplus of £755 so choose Tasko bank over 12 months (from surplus of £770) award 2/2 ✓✓

Que	Question		Generic Scheme	Illustrative Scheme	Max Mark
8.	(a)		Ans: 32 candles		3
			•¹ Strategy: know how to use ratio	• 1 evidence of knowing how to scale up the ratio	
			• ² Process: find total amount of wax used	• ² 12000 + 4000 + 8000 = 24000 cm ³	
			• ³ Process: find number of candles	\bullet 3 24000 ÷ 729 = 32·92 = 32	
			Alternative Strategy:		
			• 1 Strategy: know how to use ratio	•¹ evidence of 3/6 of 729	
			• ² Process: finds volume of red wax available and volume of red wax in candle	• ² 12000cm ³ & 364· 5	
			• ³ Process: find number of candles	• 3 12000 ÷ 364·5 = 32·92 rounded to 32	

- 1. $36000 \div 729 = 49.38 = 49$ candles award $1/3 \times \times \checkmark$
- 2. For an answer of 48 candles (16x3) award $0/3 \times \times \times$
- 3. $12000 \div 729 = 16.46 = 16$ award $0/3 \times \times \times$

Question		Generic Scheme	Illustrative Scheme	
	(b)	Ans: (£)2·43 or 2·42		3
		• 1 Process:find cost of wax plus wicks	$\bullet^1 3 \times 13.75 + 32 \times 0.18 = 47.01$	
		• ² Process: add 65%	$\bullet^2 47.01 \times 1.65 = 77.57$	
		• ³ Process: find selling price of 1 candle	\bullet^3 77.57 ÷ 32 = 2.424 = 2.43	

- 1. Accept 2·42 or 2·43
- 2. Any rounding or truncation within the calculations must be at least to two decimal places.

Question	Generic Scheme	Illustrative Scheme	Max Mark
(c)	Ans: no supported by working		7
	• 1 Strategy: knows how to find compound volume	•¹ evidence	
	• ² Strategy: substitute into cylinder formula	$\bullet^2 V = \pi \times 3.5 \times 3.5 \times 12$	
	• ³ Process: find volume of cylinder	• ³ 461·8 (or 461·58)	
	• 4 Strategy: substitute into cone formula	$\bullet^4 V = \frac{1}{3} \times 3.5 \times 3.5 \times 4$	
	• ⁵ Process: find volume of cone	● ⁵ 51·3	
	• 6 Process: find the number of candles that can be made	$\bullet^6 \ 461 \cdot 8 + 51 \cdot 3 = 513 \cdot 1,$ $12000 \div 513 \cdot 1 = 23 \cdot 38$	
	• ⁷ Communication: valid conclusion	• 7 no he can't make 25 candles	

- 1. If candidate uses 7 for the radius at •² mark •⁴ can be awarded for radius of 7 or 3.5
- 2. If candidate calculates that more than 25 candles can be made 7 can be awarded for either yes he can make 25 or no he can't make (exactly) 25.
- 3. 6 is also available for $12000 \div 25 = 480$ or $513.1 \times 25 = 12827.5$

Commonly Observed Responses:

Where a radius of 7 is used leading to an answer of 5.8... so no. award 6/7(•2 lost)

[END OF MARKING INSTRUCTIONS]